



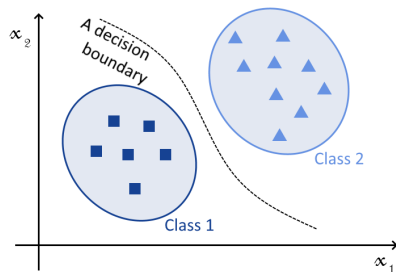
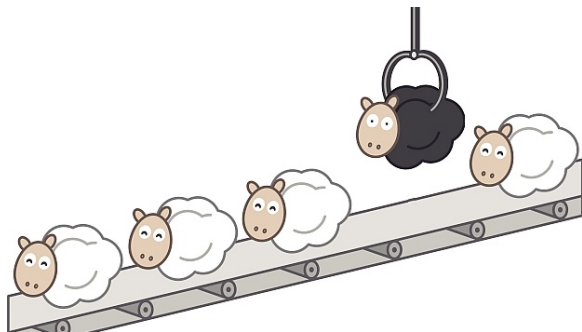
COMP 2211 Exploring Artificial Intelligence  
Artificial Neural Network - Perceptron  
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The Hong Kong University of Science and Technology, Hong Kong SAR, China



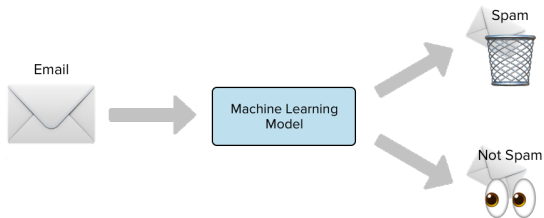
# Recap: What is Classification?

- **Classification** is the process of **predicting the class of given data**.
- **Classes** are sometimes called as **labels/categories**.

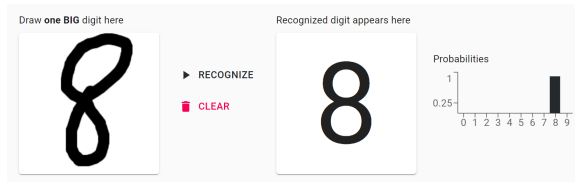


# Classification Examples

- **Spam detection** in email service: 2 classes - spam and not spam

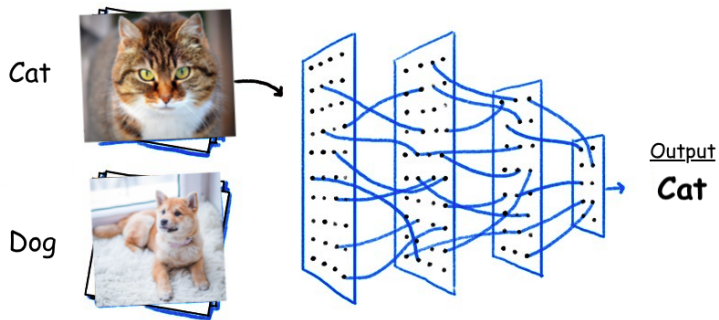


- **Handwritten digit recognition**: 10 classes - 0, 1, 2, ..., 9



# Classification Examples

- **Images classification:** 3 classes - cat, dog, none of them



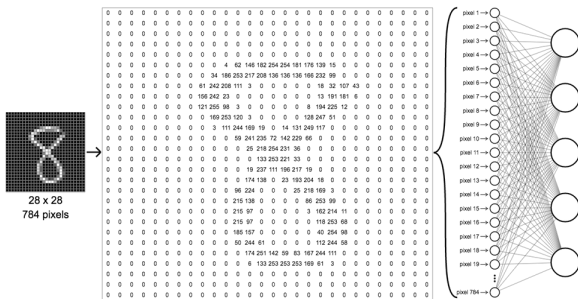
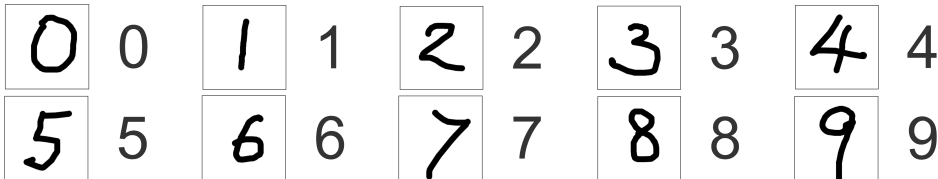
# Why Image Classification?

- **Image recognition and classification** is a **subdomain of computer vision**. It is an algorithm that looks at an image and **assigns it a label** from a collection of predefined labels or categories (e.g., a dog, a cat).
- Image classification and recognition are **vital components in robotics**, such as autonomous vehicles or domestic robots.
- It is also important in **security systems such as face recognition**, image search engines such as Google or Bing image search, and medical imaging such as cancer detection.



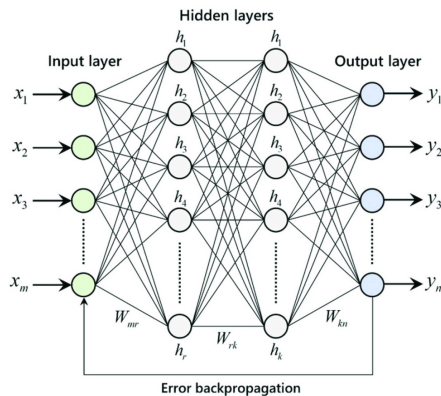
# Handwritten Digits Recognition using MLP

We will build an **Artificial Neural Network** to **recognize/classify handwritten digits**.

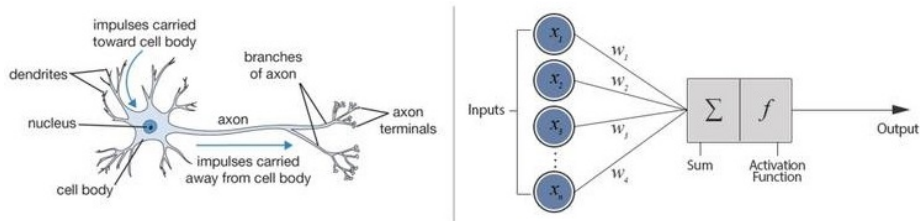


# Artificial Neural Network

- Artificial neural networks (ANN) are one of the most powerful artificial intelligence and machine learning algorithms.
- An ANN is considered a universal function approximator that transforms inputs into outputs.
- As the name suggests, it draws inspiration from neurons in our brain and the way they are connected.



# Biological Neuron vs Artificial Neuron



Biological Neuron	Artificial Neuron
Dendrites	Inputs
Cell Nucleus (Computation unit)	Node
Axon	Output
Synapse	Weight

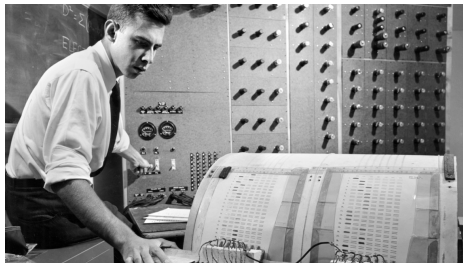
- **Node** = a linear function & an activation function



# Perceptron

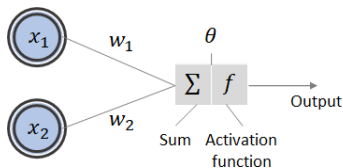
## What is a Perceptron?

- A **perceptron** is a **simple biological neuron model** in an artificial neural network.
- It performs certain **calculations to detect input data capabilities**.
- It is also the name of an early algorithm for **supervised learning** of **binary classifiers** (i.e., only two classes).
- Frank Rosenblatt invented perceptron in 1957.



Frank Rosenblatt works on the “Perceptron” - what he described as the first machine “capable of having an original idea”.

## An Example of Perceptron

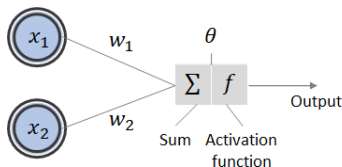


$$\text{output} = f(w_1 \times x_1 + w_2 \times x_2 + \theta)$$

Suppose  $x_1 = 3$ ,  $x_2 = 5$ ,  $w_1 = 0.2$ ,  $w_2 = 0.3$ ,  $\theta = 0.3$ ,  $f(x) = \frac{1}{1+e^{-x}}$

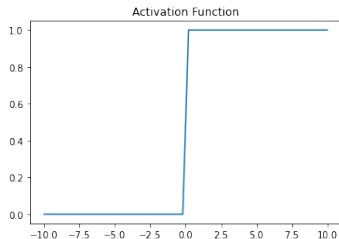
$$\begin{aligned}\text{output} &= f(0.2 \times 3 + 0.3 \times 5 + 0.3) \\ &= f(2.4) \\ &= \frac{1}{1 + e^{-2.4}} \\ &= 0.91683\end{aligned}$$

# Perceptron - Logical AND Example



- Suppose we will work on a problem of AND logical operation. The truth table of logical AND is as follows.

$x_1$	$x_2$	Output
0	0	0
0	1	0
1	0	0
1	1	1



- Assume the weights and bias are randomly generated, say  $w_1 = 0.1$ ,  $w_2 = 0.5$ ,  $\theta = -0.8$ . Also, we set learning rate  $\eta = 0.2$ .
- Activation function is

$$f(x) = \begin{cases} 0 & \text{if } x \leq 0 \\ 1 & \text{otherwise} \end{cases}$$

# Perceptron Learning Rules

- $x_1$  and  $x_2$  are inputs
  - $\theta$  is the bias
  - $w_1$  and  $w_2$  are weights
  - $O$  is the computed output
  - $T$  is the target
1. If the **output is correct** (i.e.,  $T$  is the same as  $O$ ), the weights  **$w_1$  and  $w_2$  are not updated**.
  2. If the **output is incorrect** (i.e.,  $T$  is different to  $O$ ), the weights  **$w_1$  and  $w_2$  are updated** according to the following rules such that the output of the perceptron for the new weights is closer to  $T$ .

$$\Delta w_i = \eta(T - O)x_i$$

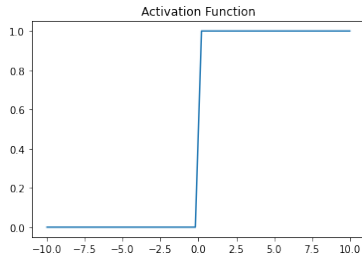
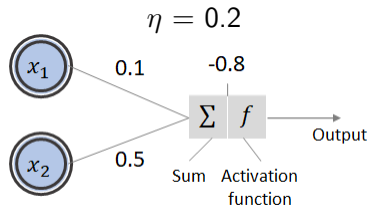
$$\Delta \theta = \eta(T - O)$$

$$w_i = w_i + \Delta w_i$$

$$\theta = \theta + \Delta \theta$$

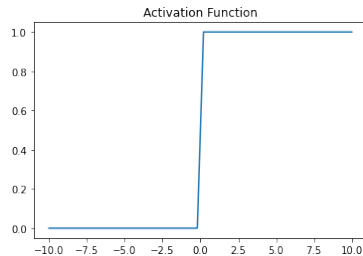
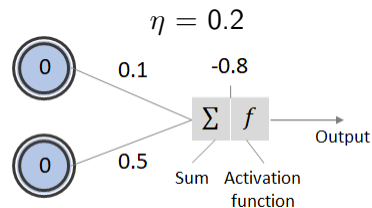
where  $i \in \{1, 2\}$ .

## Initial

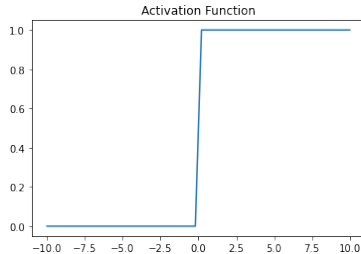
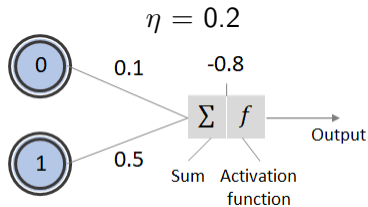
[illegible]

# Round 1 - Step 1

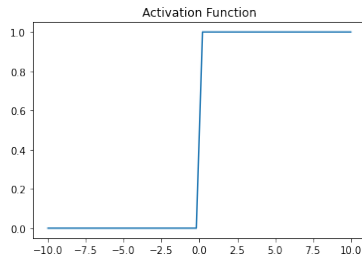
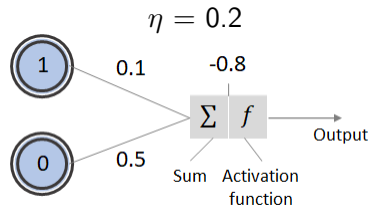
$x_1$	$x_2$	$T$	$O$	$\Delta w_1$	$w_1$	$\Delta w_2$	$w_2$	$\Delta \theta$	$\theta$
-	-	-	-	-	0.1	-	0.5	-	-0.8
0	0	0	0	0	0.1	0	0.5	0	-0.8



## Round 1 - Step 2

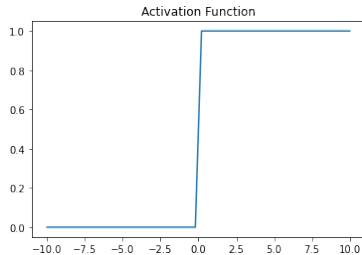
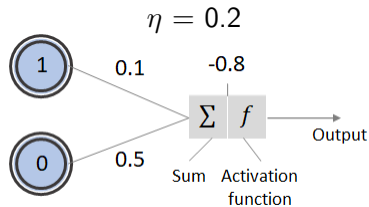
[illegible]

## Round 1 - Step 3

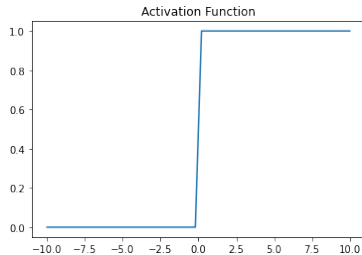
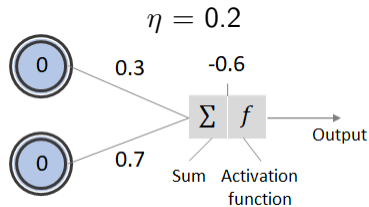
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## Round 1 - Step 4

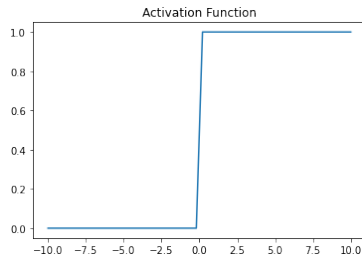
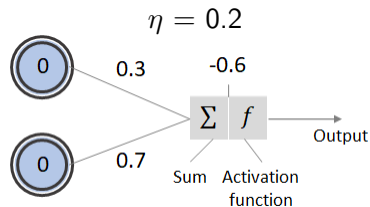
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## Round 2 - Step 1

[illegible]

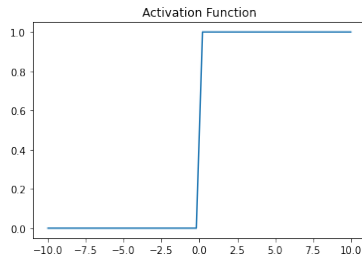
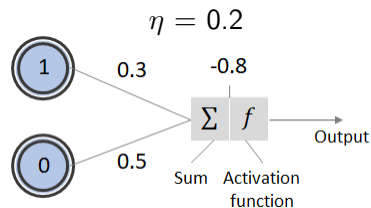
## Round 2 - Step 2

$x_1$	$x_2$	$T$	$O$	$\Delta w_1$	$w_1$	$\Delta w_2$	$w_2$	$\Delta \theta$	$\theta$
-	-	-	-	-	0.1	-	0.5	-	-0.8
0	0	0	0	0	0.1	0	0.5	0	-0.8
0	1	0	0	0	0.1	0	0.5	0	-0.8
1	0	0	0	0	0.1	0	0.5	0	-0.8
<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0.2</b>	<b>0.3</b>	<b>0.2</b>	<b>0.7</b>	<b>0.2</b>	<b>-0.6</b>
0	0	0	0	0	0.3	0	0.7	0	-0.6
<b>0</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0.3</b>	<b>-0.2</b>	<b>0.5</b>	<b>-0.2</b>	<b>-0.8</b>



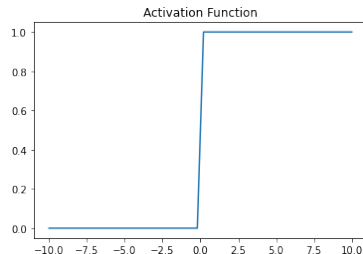
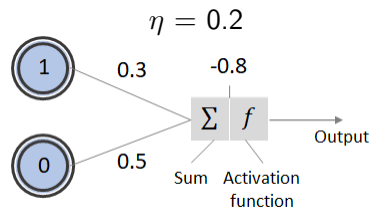
## Round 2 - Step 3

$x_1$	$x_2$	$T$	$O$	$\Delta w_1$	$w_1$	$\Delta w_2$	$w_2$	$\Delta \theta$	$\theta$
-	-	-	-	-	0.1	-	0.5	-	-0.8
0	0	0	0	0	0.1	0	0.5	0	-0.8
0	1	0	0	0	0.1	0	0.5	0	-0.8
1	0	0	0	0	0.1	0	0.5	0	-0.8
<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0.2</b>	<b>0.3</b>	<b>0.2</b>	<b>0.7</b>	<b>0.2</b>	<b>-0.6</b>
0	0	0	0	0	0.3	0	0.7	0	-0.6
<b>0</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0.3</b>	<b>-0.2</b>	<b>0.5</b>	<b>-0.2</b>	<b>-0.8</b>
1	0	0	0	0	0.3	0	0.5	0	-0.8



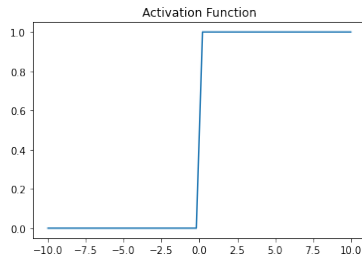
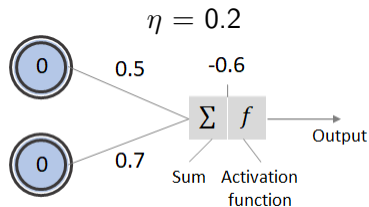
## Round 2 - Step 4

$x_1$	$x_2$	$T$	$O$	$\Delta w_1$	$w_1$	$\Delta w_2$	$w_2$	$\Delta \theta$	$\theta$
-	-	-	-	-	0.1	-	0.5	-	-0.8
0	0	0	0	0	0.1	0	0.5	0	-0.8
0	1	0	0	0	0.1	0	0.5	0	-0.8
1	0	0	0	0	0.1	0	0.5	0	-0.8
1	1	1	0	0.2	0.3	0.2	0.7	0.2	-0.6
0	0	0	0	0	0.3	0	0.7	0	-0.6
0	1	0	1	0	0.3	-0.2	0.5	-0.2	-0.8
1	0	0	0	0	0.3	0	0.5	0	-0.8
1	1	1	0	0.2	0.5	0.2	0.7	0.2	-0.6



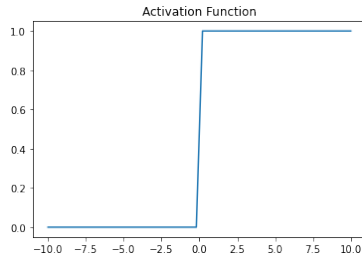
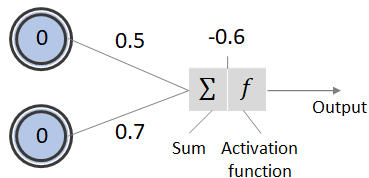
## Round 3 - Step 1

$x_1$	$x_2$	$T$	$O$	$\Delta w_1$	$w_1$	$\Delta w_2$	$w_2$	$\Delta \theta$	$\theta$
-	-	-	-	-	0.1	-	0.5	-	-0.8
0	0	0	0	0	0.1	0	0.5	0	-0.8
0	1	0	0	0	0.1	0	0.5	0	-0.8
1	0	0	0	0	0.1	0	0.5	0	-0.8
<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0.2</b>	<b>0.3</b>	<b>0.2</b>	<b>0.7</b>	<b>0.2</b>	<b>-0.6</b>
0	0	0	0	0	0.3	0	0.7	0	-0.6
<b>0</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0.3</b>	<b>-0.2</b>	<b>0.5</b>	<b>-0.2</b>	<b>-0.8</b>
1	0	0	0	0	0.3	0	0.5	0	-0.8
<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0.2</b>	<b>0.5</b>	<b>0.2</b>	<b>0.7</b>	<b>0.2</b>	<b>-0.6</b>
0	0	0	0	0	0.5	0	0.7	0	-0.6



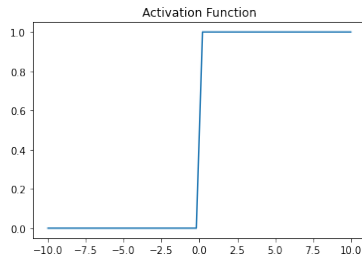
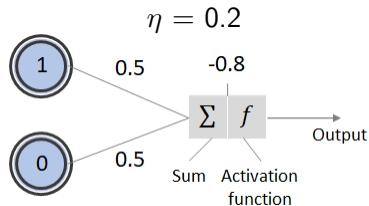
## Round 3 - Step 2

$x_1$	$x_2$	$T$	$O$	$\Delta w_1$	$w_1$	$\Delta w_2$	$w_2$	$\Delta \theta$	$\theta$
-	-	-	-	-	0.1	-	0.5	-	-0.8
0	0	0	0	0	0.1	0	0.5	0	-0.8
0	1	0	0	0	0.1	0	0.5	0	-0.8
1	0	0	0	0	0.1	0	0.5	0	-0.8
<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0.2</b>	<b>0.3</b>	<b>0.2</b>	<b>0.7</b>	<b>0.2</b>	<b>-0.6</b>
0	0	0	0	0	0.3	0	0.7	0	-0.6
<b>0</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0.3</b>	<b>-0.2</b>	<b>0.5</b>	<b>-0.2</b>	<b>-0.8</b>
1	0	0	0	0	0.3	0	0.5	0	-0.8
<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0.2</b>	<b>0.5</b>	<b>0.2</b>	<b>0.7</b>	<b>0.2</b>	<b>-0.6</b>
0	0	0	0	0	0.5	0	0.7	0	-0.6
<b>0</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0.5</b>	<b>-0.2</b>	<b>0.5</b>	<b>-0.2</b>	<b>-0.8</b>



## Round 3 - Step 3

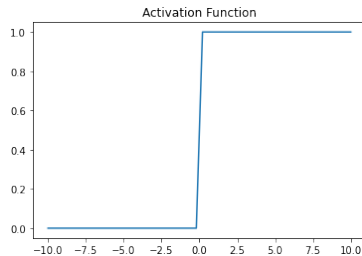
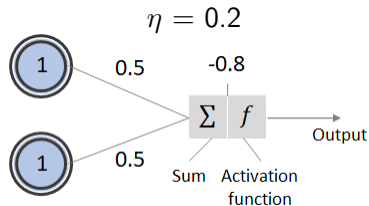
$x_1$	$x_2$	$T$	$O$	$\Delta w_1$	$w_1$	$\Delta w_2$	$w_2$	$\Delta \theta$	$\theta$
-	-	-	-	-	0.1	-	0.5	-	-0.8
0	0	0	0	0	0.1	0	0.5	0	-0.8
0	1	0	0	0	0.1	0	0.5	0	-0.8
1	0	0	0	0	0.1	0	0.5	0	-0.8
<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0.2</b>	<b>0.3</b>	<b>0.2</b>	<b>0.7</b>	<b>0.2</b>	<b>-0.6</b>
0	0	0	0	0	0.3	0	0.7	0	-0.6
<b>0</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0.3</b>	<b>-0.2</b>	<b>0.5</b>	<b>-0.2</b>	<b>-0.8</b>
1	0	0	0	0	0.3	0	0.5	0	-0.8
<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0.2</b>	<b>0.5</b>	<b>0.2</b>	<b>0.7</b>	<b>0.2</b>	<b>-0.6</b>
0	0	0	0	0	0.5	0	0.7	0	-0.6
<b>0</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0.5</b>	<b>-0.2</b>	<b>0.5</b>	<b>-0.2</b>	<b>-0.8</b>
1	0	0	0	0	0.5	0	0.5	0	-0.8





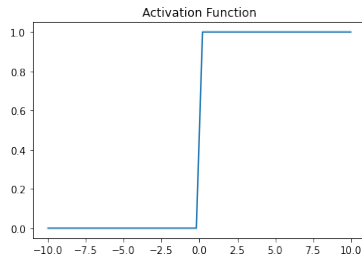
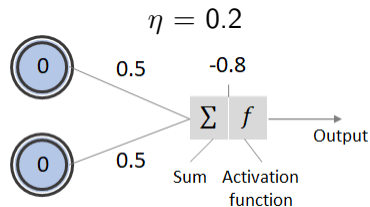
## Round 3 - Step 4

$x_1$	$x_2$	$T$	$O$	$\Delta w_1$	$w_1$	$\Delta w_2$	$w_2$	$\Delta \theta$	$\theta$
-	-	-	-	-	0.1	-	0.5	-	-0.8
0	0	0	0	0	0.1	0	0.5	0	-0.8
0	1	0	0	0	0.1	0	0.5	0	-0.8
1	0	0	0	0	0.1	0	0.5	0	-0.8
<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0.2</b>	<b>0.3</b>	<b>0.2</b>	<b>0.7</b>	<b>0.2</b>	<b>-0.6</b>
0	0	0	0	0	0.3	0	0.7	0	-0.6
<b>0</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0.3</b>	<b>-0.2</b>	<b>0.5</b>	<b>-0.2</b>	<b>-0.8</b>
1	0	0	0	0	0.3	0	0.5	0	-0.8
<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0.2</b>	<b>0.5</b>	<b>0.2</b>	<b>0.7</b>	<b>0.2</b>	<b>-0.6</b>
0	0	0	0	0	0.5	0	0.7	0	-0.6
<b>0</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0.5</b>	<b>-0.2</b>	<b>0.5</b>	<b>-0.2</b>	<b>-0.8</b>
1	0	0	0	0	0.5	0	0.5	0	-0.8
1	1	1	1	0	0.5	0	0.5	0	-0.8



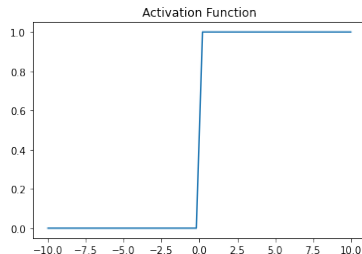
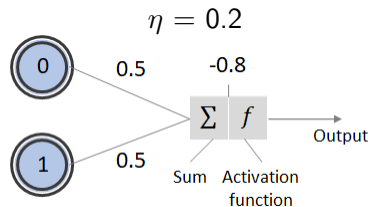
## Round 4 - Step 1

$x_1$	$x_2$	$T$	$O$	$\Delta w_1$	$w_1$	$\Delta w_2$	$w_2$	$\Delta \theta$	$\theta$
-	-	-	-	-	0.1	-	0.5	-	-0.8
0	0	0	0	0	0.1	0	0.5	0	-0.8
0	1	0	0	0	0.1	0	0.5	0	-0.8
1	0	0	0	0	0.1	0	0.5	0	-0.8
<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0.2</b>	<b>0.3</b>	<b>0.2</b>	<b>0.7</b>	<b>0.2</b>	<b>-0.6</b>
0	0	0	0	0	0.3	0	0.7	0	-0.6
<b>0</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0.3</b>	<b>-0.2</b>	<b>0.5</b>	<b>-0.2</b>	<b>-0.8</b>
1	0	0	0	0	0.3	0	0.5	0	-0.8
<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0.2</b>	<b>0.5</b>	<b>0.2</b>	<b>0.7</b>	<b>0.2</b>	<b>-0.6</b>
0	0	0	0	0	0.5	0	0.7	0	-0.6
<b>0</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0.5</b>	<b>-0.2</b>	<b>0.5</b>	<b>-0.2</b>	<b>-0.8</b>
1	0	0	0	0	0.5	0	0.5	0	-0.8
1	1	1	1	0	0.5	0	0.5	0	-0.8
0	0	0	0	0	0.5	0	0.5	0	-0.8



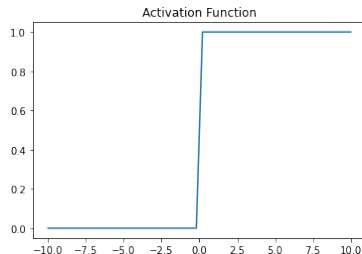
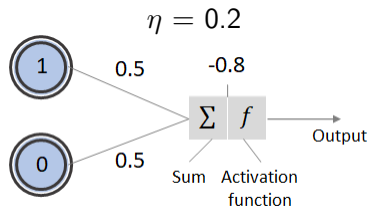
## Round 4 - Step 2

$x_1$	$x_2$	$T$	$O$	$\Delta w_1$	$w_1$	$\Delta w_2$	$w_2$	$\Delta \theta$	$\theta$
-	-	-	-	-	0.1	-	0.5	-	-0.8
0	0	0	0	0	0.1	0	0.5	0	-0.8
0	1	0	0	0	0.1	0	0.5	0	-0.8
1	0	0	0	0	0.1	0	0.5	0	-0.8
<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0.2</b>	<b>0.3</b>	<b>0.2</b>	<b>0.7</b>	<b>0.2</b>	<b>-0.6</b>
0	0	0	0	0	0.3	0	0.7	0	-0.6
<b>0</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0.3</b>	<b>-0.2</b>	<b>0.5</b>	<b>-0.2</b>	<b>-0.8</b>
1	0	0	0	0	0.3	0	0.5	0	-0.8
<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0.2</b>	<b>0.5</b>	<b>0.2</b>	<b>0.7</b>	<b>0.2</b>	<b>-0.6</b>
0	0	0	0	0	0.5	0	0.7	0	-0.6
<b>0</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0.5</b>	<b>-0.2</b>	<b>0.5</b>	<b>-0.2</b>	<b>-0.8</b>
1	0	0	0	0	0.5	0	0.5	0	-0.8
1	1	1	1	0	0.5	0	0.5	0	-0.8
0	0	0	0	0	0.5	0	0.5	0	-0.8
0	1	0	0	0	0.5	0	0.5	0	-0.8



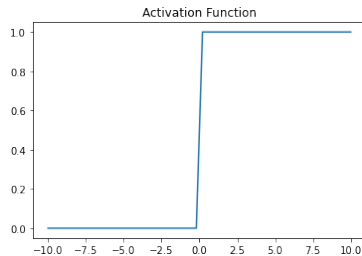
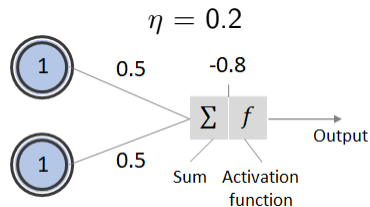
## Round 4 - Step 3

$x_1$	$x_2$	$T$	$O$	$\Delta w_1$	$w_1$	$\Delta w_2$	$w_2$	$\Delta \theta$	$\theta$
-	-	-	-	-	0.1	-	0.5	-	-0.8
0	0	0	0	0	0.1	0	0.5	0	-0.8
0	1	0	0	0	0.1	0	0.5	0	-0.8
1	0	0	0	0	0.1	0	0.5	0	-0.8
<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0.2</b>	<b>0.3</b>	<b>0.2</b>	<b>0.7</b>	<b>0.2</b>	<b>-0.6</b>
0	0	0	0	0	0.3	0	0.7	0	-0.6
<b>0</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0.3</b>	<b>-0.2</b>	<b>0.5</b>	<b>-0.2</b>	<b>-0.8</b>
1	0	0	0	0	0.3	0	0.5	0	-0.8
<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0.2</b>	<b>0.5</b>	<b>0.2</b>	<b>0.7</b>	<b>0.2</b>	<b>-0.6</b>
0	0	0	0	0	0.5	0	0.7	0	-0.6
<b>0</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0.5</b>	<b>-0.2</b>	<b>0.5</b>	<b>-0.2</b>	<b>-0.8</b>
1	0	0	0	0	0.5	0	0.5	0	-0.8
1	1	1	1	0	0.5	0	0.5	0	-0.8
0	0	0	0	0	0.5	0	0.5	0	-0.8
0	1	0	0	0	0.5	0	0.5	0	-0.8
1	0	0	0	0	0.5	0	0.5	0	-0.8



## Round 4 - Step 4

$x_1$	$x_2$	$T$	$O$	$\Delta w_1$	$w_1$	$\Delta w_2$	$w_2$	$\Delta \theta$	$\theta$
-	-	-	-	-	0.1	-	0.5	-	-0.8
0	0	0	0	0	0.1	0	0.5	0	-0.8
0	1	0	0	0	0.1	0	0.5	0	-0.8
1	0	0	0	0	0.1	0	0.5	0	-0.8
<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0.2</b>	<b>0.3</b>	<b>0.2</b>	<b>0.7</b>	<b>0.2</b>	<b>-0.6</b>
0	0	0	0	0	0.3	0	0.7	0	-0.6
<b>0</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0.3</b>	<b>-0.2</b>	<b>0.5</b>	<b>-0.2</b>	<b>-0.8</b>
1	0	0	0	0	0.3	0	0.5	0	-0.8
<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>0.2</b>	<b>0.5</b>	<b>0.2</b>	<b>0.7</b>	<b>0.2</b>	<b>-0.6</b>
0	0	0	0	0	0.5	0	0.7	0	-0.6
<b>0</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0.5</b>	<b>-0.2</b>	<b>0.5</b>	<b>-0.2</b>	<b>-0.8</b>
1	0	0	0	0	0.5	0	0.5	0	-0.8
1	1	1	1	0	0.5	0	0.5	0	-0.8
0	0	0	0	0	0.5	0	0.5	0	-0.8
0	1	0	0	0	0.5	0	0.5	0	-0.8
1	0	0	0	0	0.5	0	0.5	0	-0.8
1	1	1	1	0	0.5	0	0.5	0	-0.8



# Perceptron Implementation from Scratch I

```
import math # Import math module

class Perceptron:
    def __init__(self):
        """ Perceptron initialization """
        self.w = [0.1,0.5]      # Weights
        self.theta = -0.8       # Bias
        self.learningRate = 0.2 # Eta

    def response(self,x):
        """ Perceptron output """
        # Calculate weighted sum
        y = x[0] * self.w[0] + x[1] * self.w[1] + self.theta
        # If weighted sum > 0, return 1. Otherwise return 0
        if y > 0:
            return 1
        else:
            return 0
```

## Perceptron Implementation from Scratch II

```
def updateWeights(self,x,iterError):  
    """ Weights update """  
    #  $w_i = w_i + \eta * (T - O) * x_i$   
    self.w[0] += self.learningRate * iterError * x[0]  
    self.w[1] += self.learningRate * iterError * x[1]  
  
def updateBias(self,iterError):  
    """ Bias update """  
    #  $\theta = \theta + \eta * (T - O)$   
    self.theta += self.learningRate * iterError  
  
def train(self,data):  
    """ Training """  
    learned = True # Should perform training  
    round = 0      # Initialize round to 0
```

# Perceptron Implementation from Scratch III

```
while learned:
    totalError = 0.0
    for x in data:
        r = self.response(x)
        if x[2] != r:
            roundError = x[2] - r
            self.updateWeights(x, roundError)
            self.updateBias(roundError)
            totalError += abs(roundError)
    round += 1

if math.isclose(totalError, 0) or round >= 100:
    print("Total number of rounds (epochs): ", round)
    print("Final weights: ", self.w)
    print("Final bias: ", self.theta)
    learned = False
```

# While learned is true  
# Initialize totalError to 0  
# For each data sample  
# Calculate perceptron output of x  
# If the output is different to target  
# Error = target - perceptron output  
# Update weights  
# Update bias  
# Update total error  
  
# Stopping condition  
# Print total num of rounds  
# Print final weights  
# Print final bias  
# Stop learning



# Perceptron Implementation from Scratch IV

```
""" Main function """
```

```
perceptron = Perceptron()
```

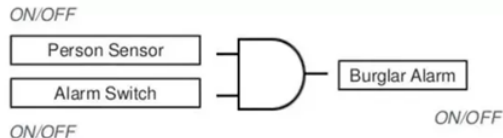
```
trainset = [[0,0,0], [0,1,0], [1,0,0], [1,1,1]]
```

```
perceptron.train(trainset)
```

```
# Create Perceptron object
```

```
# Define training set
```

```
# Perform training
```



If both the Person Sensor AND the Alarm Switch are on then the Burglar Alarm is activated.



# Perceptron Implementation using Scikit-Learn

```
import numpy as np # Import NumPy
from sklearn.linear_model import Perceptron # Import Perceptron class from Scikit-Learn

inputs = np.array([[0,0], [0,1], [1,0], [1,1]]) # Inputs
outputs = np.array([0, 0, 0, 1]) # Expected outputs

# Create and fit a perceptron model
# Set learning rate (eta0)
model = Perceptron(eta0=0.2)
model.fit(inputs, outputs)

# Use the trained model to predict the outputs
predicted_outputs = model.predict([[0,0], [1,0], [1,1], [0,1]])
print(predicted_outputs) # Print the predicated outputs

print(model.coef_) # Print the final weights
print(model.intercept_) # Print the bias
```

# Stopping Rules

- Use maximum training time

The training may go a bit beyond the specified time limit in order to complete the current cycle.

- The maximum number of training cycles allowed

If the maximum number of cycles is exceeded, then training stops.

- Use minimum accuracy

Training will continue until the specified accuracy is attained.



## Terminologies - Learning and Epoch

- **Learning** is the **process of updating weights** in the perceptron.
  - We set weights  $w_1$  to 0.1,  $w_2$  to 0.5 initially, but it causes some errors. Then, we update the weight values to 0.5 and predict all instances correctly.
  - The whole process takes 4 rounds/epoches.
- **Epoch** refers to **one cycle through the full training dataset**.

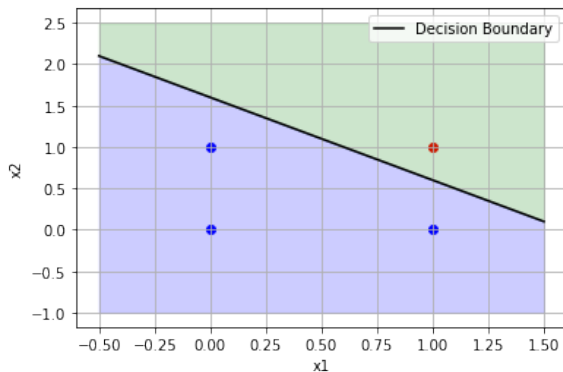
### Observation

According to the results of the perceptron learning procedure,  $w_1 = w_2 = 0.5$ . The relationship between the inputs, i.e.,  $x_1$ ,  $x_2$ , and the output  $y$  is

$$\begin{aligned} y &= \begin{cases} 0 & \text{if } 0.5x_1 + 0.5x_2 - 0.8 \leq 0 \\ 1 & \text{otherwise} \end{cases} \\ &= \begin{cases} 0 & \text{if } x_1 + x_2 \leq 1.6 \\ 1 & \text{otherwise} \end{cases} \end{aligned}$$

# Decision Boundary

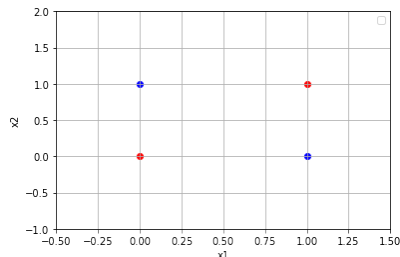
$$y = \begin{cases} 0 & \text{if } x_1 + x_2 \leq 1.6 \\ 1 & \text{otherwise} \end{cases}$$



# Problem

- Question: Can we apply the same perceptron learning procedure for the XOR gate, which has the truth table on the right? If so, show all the steps. If not, explain why.
- Answer: No, a perceptron cannot implement XOR. The reason is that the labels in XOR are not linearly separable, i.e. we cannot draw a straight line to separate the points (0,0),(1,1) from the points (0,1),(1,0).

$x_1$	$x_2$	Output
0	0	0
0	1	1
1	0	1
1	1	0



To solve the problem, we need a multi-layer perceptron.

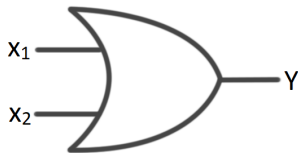
## Practice Problem

- Please apply the perceptron learning procedure for the OR gate. The truth table of logical OR is as follows.

$x_1$	$x_2$	Output
0	0	0
0	1	1
1	0	1
1	1	1

- Assume the weights and bias are randomly generated, say  $w_1 = 0.1$ ,  $w_2 = 0.5$ ,  $\theta = -0.8$ . Also, we set learning rate  $\eta = 0.2$ .
- Activation function is

$$f(x) = \begin{cases} 0 & \text{if } x \leq 0 \\ 1 & \text{otherwise} \end{cases}$$



## Initial, Round 1, Round 2, & Round 3

$x_1$	$x_2$	$T$	$O$	$\Delta w_1$	$w_1$	$\Delta w_2$	$w_2$	$\Delta \theta$	$\theta$
-	-	-	-	-	0.1	-	0.5	-	-0.8
0	0	0	0	0	0.1	0	0.5	0	-0.8
0	1	1	0	0	0.1	0.2	0.7	0.2	-0.6
1	0	1	0	0.2	0.3	0	0.7	0.2	-0.4
1	1	1	1	0	0.3	0	0.7	0	-0.4
0	0	0	0	0	0.3	0	0.7	0	-0.4
0	1	1	1	0	0.3	0	0.7	0	-0.4
1	0	1	0	0.2	0.5	0	0.7	0.2	-0.2
1	1	1	1	0	0.5	0	0.7	0	-0.2
0	0	0	0	0	0.5	0	0.7	0	-0.2
0	1	1	1	0	0.5	0	0.7	0	-0.2
1	0	1	1	0	0.5	0	0.7	0	-0.2
1	1	1	1	0	0.5	0	0.7	0	-0.2

The training converges in 3 epochs if the initial weights are  $w_1 = 0.1$ ,  $w_2 = 0.5$ , initial bias is  $\theta = -0.8$  and learning rate is  $\eta = 0.2$ . The final weights and bias are:  $w_1 = 0.5$ ,  $w_2 = 0.7$ ,  $\theta = -0.2$ .



That's all!

Any questions?

