

5B April 22 Homework: pages 57-67 in Singapore Math Book

# Triangles



**A triangle has three sides and three angles**

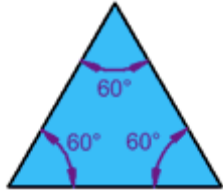
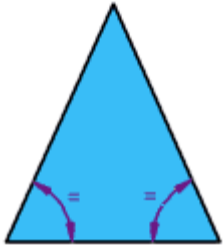



**The three angles always add to  $180^\circ$**

## Equilateral, Isosceles and Scalene

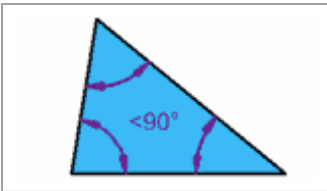
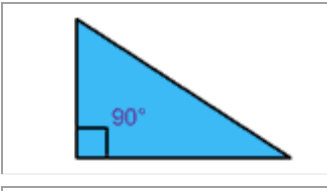
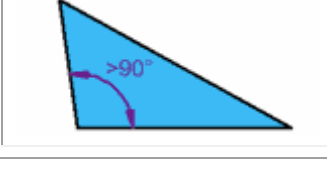
There are three special names given to triangles that tell how many sides (or angles) are equal.

There can be **3**, **2** or **no** equal sides/angles:

	<b>Equilateral Triangle</b>  <b>Three</b> equal sides <b>Three</b> equal angles, always $60^\circ$
	<b>Isosceles Triangle</b>  <b>Two</b> equal sides <b>Two</b> equal angles
	<b>Scalene Triangle</b>  <b>No</b> equal sides <b>No</b> equal angles

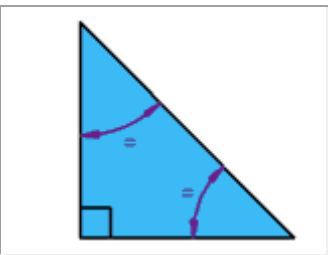
## What Type of Angle?

Triangles can also have names that tell you what **type of angle** is inside:

	<b>Acute Triangle</b> All angles are less than $90^\circ$
	<b>Right Triangle</b> Has a right angle ( $90^\circ$ )
	<b>Obtuse Triangle</b> Has an angle more than $90^\circ$

## Combining the Names

Sometimes a triangle will have two names, for example:

	<b>Right Isosceles Triangle</b> Has a right angle ( $90^\circ$ ), and also two equal angles Can you guess what the equal angles are?
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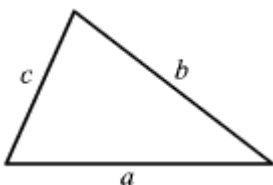
Question: Can you draw a right equilateral right triangle? Or an obtuse isosceles triangle? Or an obtuse equilateral triangle?

THEOREMS (IN TEXT):

1. THE 3 ANGLES OF A TRIANGLE ADD UP TO 180 DEGREES.
2. WHEN 1 ANGLE OF A TRIANGLE IS A RIGHT ANGLE, THE OTHER 2 ANGLES ADD UP TO 90 DEGREES.
3. THE EXTERIOR ANGLE OF A TRIANGLE IS EQUAL TO THE SUM OF THE INTERIOR OPPOSITE ANGLES.

## 4. Triangle Inequality Theorem

The sum of the lengths of any two sides of a triangle is greater than the length of the third side.



In the figure, the following [inequalities](#) hold.

$$a + b > c$$

$$a + c > b$$

$$b + c > a$$

**Example:**

Check whether it is possible to have a triangle with the given side lengths.

7, 9, 13

Add any two sides and see if it is greater than the other side.

The sum of 7 and 9 is 16 and 16 is greater than 13.

The sum of 9 and 13 is 21 and 21 is greater than 7.

The sum of 7 and 13 is 20 and 20 is greater than 9.

This set of side lengths not satisfies Triangle Inequality Theorem.

These lengths do form a triangle.

**Example:**

Check whether the given side lengths form a triangle.

4, 8, 15

Check whether the sides satisfy the Triangle Inequality Theorem.

Add any two sides and see if it is greater than the other side.

The sum of 4 and 8 is 12 and 12 is less than 15.

This set of side lengths does not satisfy Triangle Inequality Theorem.

These lengths do not form a triangle.