

Due Date: April 06, 2014

**21.2.1** Compute the sum of each of the following arithmetic series:

(a)  $21 + 28 + 35 + \cdots + 105$

(b) The arithmetic series with first term 7, common difference  $-3$ , and 14 terms

(c)  $\frac{1}{2} + \frac{5}{6} + \frac{7}{6} + \cdots + \frac{19}{2}$

**21.2.2** The sum of a 15-term arithmetic series with first term 7 is  $-210$ . What is the common difference?

**21.2.3** The sum of the first 5 terms of an arithmetic series is 70. The sum of the first 10 terms of this arithmetic series is 210. What is the first term of the series?

**21.2.4** Explain why an arithmetic series with an odd number of terms has its sum equal to the number of terms times the middle term of the series.

**21.2.5** The sum of 5 consecutive even integers is 4 less than the sum of the first 8 consecutive odd positive integers. What is the smallest of the even integers? (Source: AMC 10)

**21.2.6** If the sum of the first  $3n$  positive integers is 150 more than the sum of the first  $n$  positive integers, then what is the sum of the first  $4n$  positive integers?

**21.2.7** Suppose that the sequence  $a_1, a_2, a_3, \dots, a_{200}$  is an arithmetic sequence with  $a_1 + a_2 + \cdots + a_{100} = 100$  and  $a_{101} + a_{102} + \cdots + a_{200} = 200$ . What is the value of  $a_2 - a_1$ ? (Source: AMC 10)