# Introduction to Intelligent Vehicles [ 3. Timing Analysis II ]

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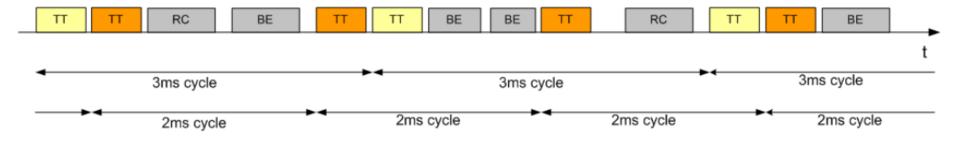
**National Taiwan University** 

### Outline

- ☐ Introduction to Other In-Vehicle Networks
- ☐ Timing Analysis of Time Division Multiple Access (TDMA)
  Based Protocols
- ☐ Real-Time Calculus (RTC)

### **TTEthernet**

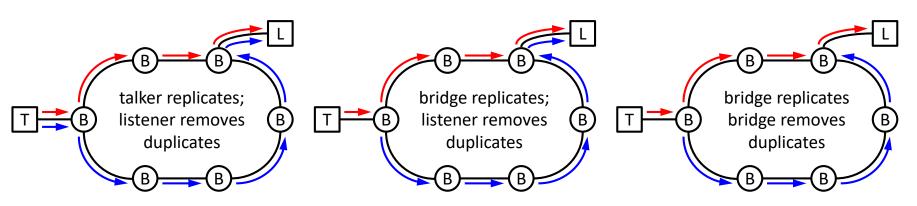
- ☐ Why TT, not pure Ethernet?
- Features
  - Quality of Service (QoS) and preemption
  - > Time synchronization
- ☐ Traffic types
  - Time-Triggered (TT) traffic (highest priority)
    - Sent over the network at predefined (scheduled) time
  - ➤ Rate-Constrained (RC) traffic
    - Sent over the network with predefined bandwidth
  - Best-Effort (BE) traffic (lowest priority)
    - Conventional Ethernet



### Time-Sensitive Networking (TSN)

#### Features

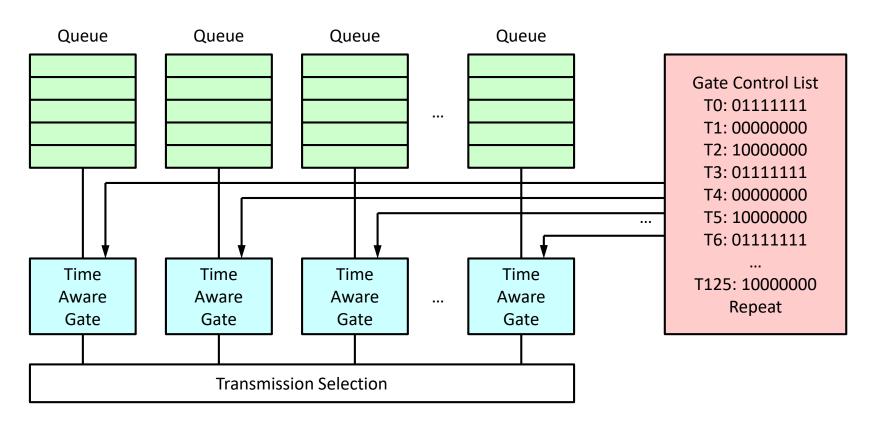
- ➤ Another name: Audio Video Bridging (AVB)
- Quality of Service and preemption
  - Achieve timing guarantees for high-priority messages
- > Frame replication and elimination
- > Time synchronization
- > Time aware shaper



https://standards.ieee.org/events/automotive/2015/03\_IEEE\_TSN\_Standards\_Overview\_and\_Update\_v4.pdf

### Time-Sensitive Networking (TSN)

#### ☐ Time aware shaper



http://www.ieee802.org/1/files/public/docs2012/bv-boiger-time-aware-shaper-0712-v01.pdf

### Other Protocols with TDMA Concepts

- □ FlexRay
  - https://en.wikipedia.org/wiki/FlexRay
- ☐ Time-Triggered Protocol
  - https://en.wikipedia.org/wiki/Time-Triggered Protocol

### Outline

- ☐ Introduction to Potential In-Vehicle Networks
- ☐ <u>Timing Analysis of Time Division Multiple Access (TDMA)</u>
  Based Protocols
- ☐ Real-Time Calculus (RTC)

### **Abstraction**

#### ☐ [Wikipedia]

- > In software engineering and computer science, abstraction is
  - The <u>process</u> of removing physical, spatial, or temporal details or attributes in the study of objects or systems in order to more closely attend to other details of interest
    - It is also very similar in nature to the process of generalization
  - The <u>objects</u> which are created by keeping common features or attributes to various concrete objects or systems of study
    - i.e., the result of the process

#### > John V. Guttag

 "The essence of abstractions is preserving information that is relevant in a given context, and forgetting information that is irrelevant in that context"

#### Example

> Timing analysis of Controller Area Network (CAN)

### **Problem Formulation**

- ☐ There is a set of time slots scheduled to serve a message in a TDMA-based protocol
  - ➤ The network schedule and the message arrivals are defined by "patterns"
- ☐ What is the worst-case response time of the message?
- Assumptions
  - > Each time slot has the same length
  - > Each time slot serves exactly one instance/frame
  - > An instance/frame is transmitted only if the whole time slot is available
    - No transmission if the instance/frame arrives in the middle of the time slot

### Message Definitions

#### ☐ Synchronous message

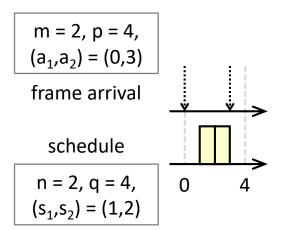
- > The network knows the time that each frame of the message is sent
- Example 1: Buses arrive at 7am, 8am, 9am, ...
- Example 2: Abstraction of TSN traffic in TSN
- > Example 3: Abstraction of Time-Triggered traffic in TTEthernet

#### ■ Asynchronous message

- The network does not know the time that each frame of the message is sent but knows the period (or pattern) of the message
- > Example 1: Buses arrive every hour
- Example 2: Abstraction of AVB traffic in TSN
- > Example 3: Abstraction of Rate-Constrained traffic in TTEthernet

### Pattern Definition

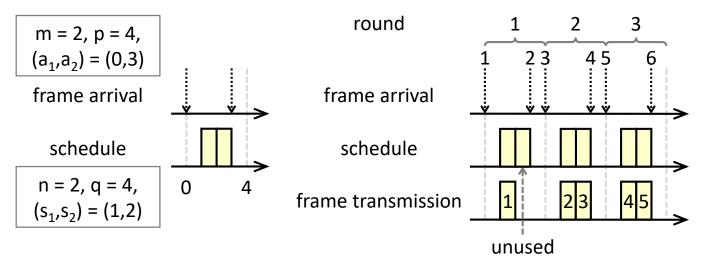
- $\square$  Frame arrival pattern (m, p,  $a_1$ ,  $a_2$ ,  $a_3$ , ...,  $a_m$ )
  - Arriving times of frames: a<sub>1</sub>,a<sub>2</sub>,a<sub>3</sub>,...,a<sub>m</sub>
  - > The pattern repeats with a period p
- $\square$  Schedule pattern (n, q, s<sub>1</sub>, s<sub>2</sub>, s<sub>3</sub>, ..., s<sub>n</sub>)
  - > Starting times of time slots: s<sub>1</sub>,s<sub>2</sub>,s<sub>3</sub>,...,s<sub>n</sub>
  - > The pattern repeats with a period q



 $\square$  If m/p > n/q (demand > supply), then it is not schedulable

### Synchronous Message

- ☐ Theorem: we only need to consider <u>two rounds</u> to compute the worst-case response time
  - Length of a round = least common multiple of p and q

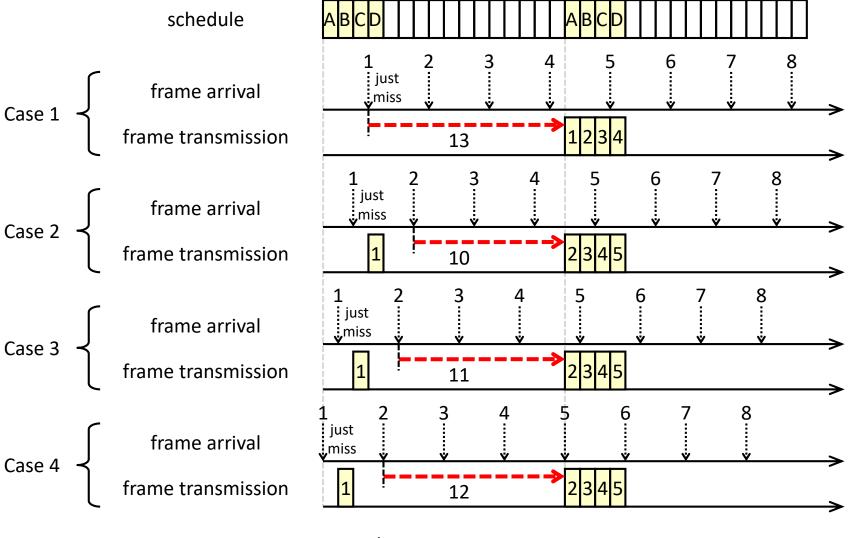


- ☐ For your reference
  - ➤ Why two rounds?
    - The numbers of unscheduled frames after first and second rounds are the same

#### **Practice**

- ☐ Analyze the following patterns
  - > Assume they are synchronous
- $\square$  Frame arrival pattern: (m = 4, p = 10,  $\mathbf{a}$  = 0, 3, 5, 6)
- $\square$  Schedule pattern: (n = 2, q = 5, s = 1, 2)

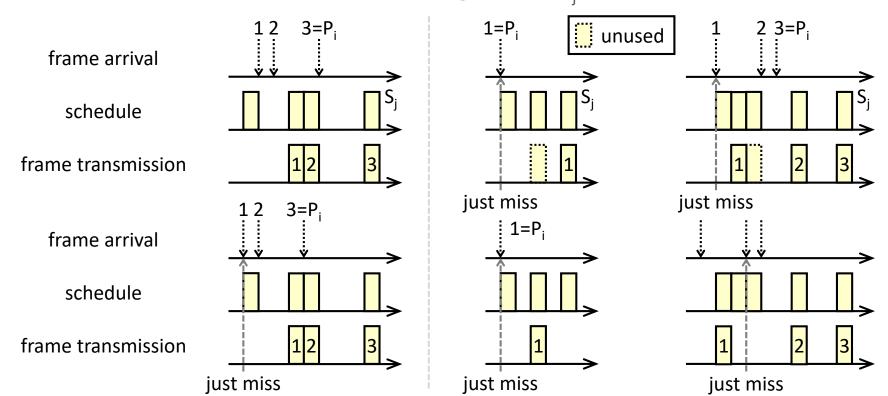
### Asynchronous Message: Example



And more cases ...

### Asynchronous Message: Theorem

- $\Box$  Theorem: if the worst case happens when frame  $P_i$  is assigned to time slot  $S_i$ , then
  - > P<sub>i</sub> or one frame before P<sub>i</sub> must <u>just miss</u> an assigned time slot, and
  - ➤ There must be no unused time slot between the ending time of the just-missed time slot and the starting time of S<sub>i</sub>



### Asynchronous Message: Duplication

- $\square$  Frame arrival pattern (m, p,  $a_1$ ,  $a_2$ ,  $a_3$ , ...,  $a_m$ )
  - Arriving times of frames: a<sub>1</sub>,a<sub>2</sub>,a<sub>3</sub>,...,a<sub>m</sub>
  - > The pattern repeats with a period p
- $\square$  Schedule pattern (n, q, s<sub>1</sub>, s<sub>2</sub>, s<sub>3</sub>, ..., s<sub>n</sub>)
  - $\triangleright$  Starting times of time slots:  $s_1, s_2, s_3, ..., s_n$
  - > The pattern repeats with a period q
- Assumption (or duplication until)
  - $\triangleright$  p = q = least common multiple of p and q
- ☐ Duplication again
  - $\Rightarrow$   $a_{m+1} = a_1 + p$ ,  $a_{m+2} = a_2 + p$ , ...,  $a_{2m} = a_m + p$
  - >  $s_{n+1} = s_1 + q$ ,  $s_{n+2} = s_2 + q$ , ...,  $s_{2n} = s_n + q$
  - Fix m, n, p, q this time

### Asynchronous Message: Example

- ☐ Frame arrival pattern
  - $\rightarrow$  (m = 4, p = 16, **a** = 3, 7, 11, 15, 19, 23, 27, 31)
- ☐ Schedule pattern
  - $\rightarrow$  (n = 4, q = 16, s = 0, 1, 2, 3, 16, 17, 18, 19)
- ☐ The patterns here are just for simpler computation later
  - > They do not follow the original definitions

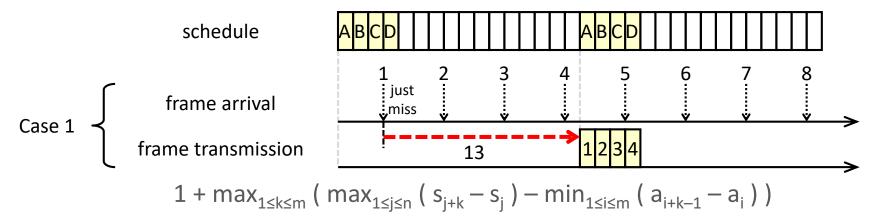
### Asynchronous Message: Equation

- ☐ We only need to consider a finite number of different alignments of the frame arrival and the schedule
  - > They are the cases that a frame just misses a time slot
  - > The worst-case response time is

$$1 + \max_{1 \le k \le m} (\max_{1 \le j \le n} (s_{j+k} - s_j) - \min_{1 \le i \le m} (a_{i+k-1} - a_i))$$

- "1" is the transmission time
- " $\max_{1 \le k \le m}$  (...)" is the waiting time
- What is the meaning of the equation?
  - Assume the i-th frame just misses the j-th time slot
  - Calculate the response time of the k-th frame after the i-th frame
    - k = 1 for the i-th frame itself
- > What is the meaning of the equation, again?
  - The densest part of the frame arrival pattern is served by the least dense part of the schedule pattern

### Asynchronous Message: Example

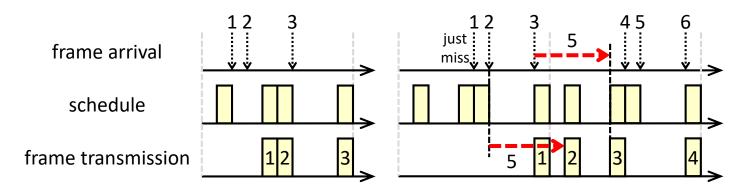


- Frame arrival pattern: (m = 4, p = 16, a = 3, 7, 11, 15, 19, 23, 27, 31)
- Schedule pattern: (n = 4, q = 16, s = 0,1,2,3,16,17,18,19)

k	$max_{1 \le j \le n} \left( s_{j+k} - s_{j} \right)$	=	$\min_{1 \le i \le m} (a_{i+k-1} - a_i)$	=	() in max <sub>1≤k≤m</sub> ()
1	$\max_{1 \le j \le 4} (s_{j+1} - s_j)$	(j=4) → 13	$\min_{1 \le i \le 4} (a_i - a_i)$	(i=1,2,3,4) → 0	13
2	$\max_{1 \le j \le 4} (s_{j+2} - s_j)$	(j=3,4) → 14	$\min_{1 \le i \le 4} (a_{i+1} - a_i)$	(i=1,2,3,4) → 4	10
3	$\max_{1 \le j \le 4} (s_{j+3} - s_j)$	(j=2,3,4) → 15	$\min_{1 \le i \le 4} (a_{i+2} - a_i)$	(i=1,2,3,4) → 8	7
4	$\max_{1 \le j \le 4} (s_{j+4} - s_j)$	(j=1,2,3,4) → 16	$\min_{1 \le i \le 4} (a_{i+3} - a_i)$	(i=1,2,3,4) → 12	4

note: this is waiting time 19

### Asynchronous Message: Example



- ☐ Frame arrival pattern: (m = 3, p = 10, a = 2, 3, 6, 12, 13, 16)
- ☐ Schedule pattern: (n = 4, q = 10, s = 1, 4, 5, 9, 11, 14, 15, 19)

k	$max_{1 \le j \le n} ( s_{j+k} - s_j )$	=	$\min_{1 \le i \le m} (a_{i+k-1} - a_i)$	=	() in max <sub>1≤k≤m</sub> ()
1	$\max_{1 \le j \le 4} (s_{j+1} - s_j)$	(j=3) → 4	$\min_{1 \le i \le 3} (a_i - a_i)$	(i=1,2,3) → 0	4
2	$\max_{1 \le j \le 4} (s_{j+2} - s_j)$	(j=3) → 6	$\min_{1 \le i \le 3} (a_{i+1} - a_i)$	(i=1) → 1	5
3	$\max_{1 \le j \le 4} (s_{j+3} - s_j)$	(j=3) → 9	$\min_{1 \le i \le 3} (a_{i+2} - a_i)$	(i=1) → 4	5

note: this is waiting time

#### **Practice**

- ☐ Analyze the following patterns
  - > Assume they are asynchronous
- $\square$  Frame arrival pattern: (m = 4, p = 10,  $\mathbf{a}$  = 0, 3, 5, 6)
- $\square$  Schedule pattern: (n = 2, q = 5, s = 1, 2)

### Discussion

- ☐ They imply the optimal scheduling for a message
  - > As early as possible for a synchronous message
  - > As evenly as possible for an asynchronous message
  - ➤ How to resolve conflicts between multiple messages?
- ☐ Gaps to a practical protocol
  - > Each time slot has the same length
  - > Each time slot serves exactly one frame
  - > Frame arrival and network schedule are described by patterns
  - Multiple switches?

### Outline

- ☐ Introduction to Potential In-Vehicle Networks
- ☐ Timing Analysis of Time Division Multiple Access (TDMA)
  Based Protocols
- **☐** Real-Time Calculus (RTC)
  - ➤ The quizzes will not include RTC

### Min-Plus Algebra

#### ■ Minimum

$$\rightarrow$$
 (f $\bigoplus$ g)(t) = min (f(t),g(t))

#### Convolution

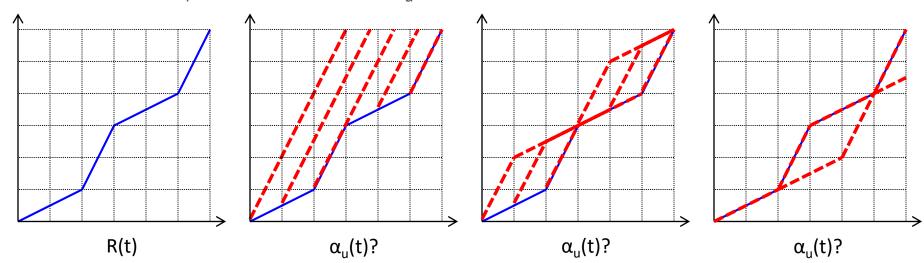
- $\rightarrow$  (f $\bigotimes$  g)(t) = inf<sub>0 \le s \le t</sub> (f(s) + g(t s))
- $\triangleright$  Example: f(x) = x and g(x) = 2x
- ightharpoonup Example:  $f(x) = x \text{ if } x \le 1$ ; f(x) = 3x of x > 1; g(x) = 2x

#### Deconvolution

- $\rightarrow$  ( f  $\bigcirc$  g )(t) = sup <sub>u > 0</sub> ( f (t + u) g(u) )
- $\triangleright$  Example: f(x) = x and g(x) = 2x
- ightharpoonup Example:  $f(x) = x \text{ if } x \le 1$ ; f(x) = 3x of x > 1; g(x) = 2x

### Input Arrival and Service Curves

- ☐ Input/output cumulative function, R(t) / R'(t)
  - > R(t): the amount of load that arrives in time interval [0,t)
  - > R'(t): the amount of load that leaves in time interval [0,t)
- $\square$  Input upper/lower arrival curves,  $\alpha_{II}(t) / \alpha_{II}(t)$ 
  - $\triangleright \alpha_{I}(t) \le R(s+t) R(s) \le \alpha_{IJ}(t)$
- $\square$  Input upper/lower service curves,  $\beta_{II}(t) / \beta_{II}(t)$ 
  - ightharpoonup ( R  $\bigotimes \beta_1$ )(t)  $\leq$  R'(t)  $\leq$  ( R  $\bigotimes \beta_2$ )(t)



### Output Arrival and Service Curves

- $\Box$  Given a process with  $\alpha_{u}(t)$ ,  $\alpha_{l}(t)$ ,  $\beta_{u}(t)$ ,  $\beta_{l}(t)$
- $\Box$  Output upper/lower arrival curves,  $\alpha'_{l}(t) / \alpha'_{l}(t)$

$$> \alpha'_{u} = ((\alpha_{u} \otimes \beta_{u}) \otimes \beta_{l}) \oplus \beta_{u}$$

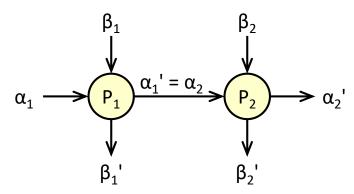
$$\triangleright \alpha'_{l} = ((\alpha_{l} \oslash \beta_{u}) \otimes \beta_{l}) \oplus \beta_{l}$$

■ Maximal backlog

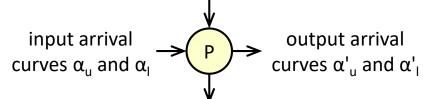
$$\triangleright$$
 b<sub>max</sub> = sup<sub>t \geq 0</sub> (  $\alpha_u(t) - \beta_l(t)$  )

■ Maximal delay

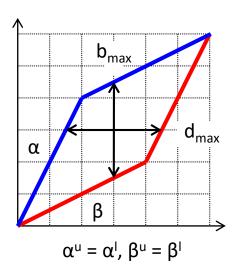
System analysis



input service curves  $\beta_u$  and  $\beta_l$ 



output service curves  $\beta'_{\mu}$  and  $\beta'_{\mu}$ 



## Q&A