

Oszacuj błąd względny i bezwzględny wyrażenia (2.1)

$$P = \frac{R^2 I^2}{C+R} \text{ [W]}$$

$$C = 1.1 \text{ [mF]} \pm 5\%$$

$$\Delta C = 1.1 \cdot \frac{5}{100} = 0.055$$

$$R = 1 \pm 2\%$$

$$\Delta R = 1 \cdot \frac{2}{100} = 0.02$$

$$I = 1.2 \pm 1\%$$

$$\Delta I = 1.2 \cdot \frac{1}{100} = 0.012$$

$$\delta X = 5\% = \frac{\Delta X}{|X|} \Rightarrow 5\% \cdot X = \Delta X$$

$$(f_a)' = f_b + a'f \quad \left| \left(\frac{f}{g}\right)' = \frac{f'g - g'f}{g^2} \right| \quad (cf)' = cf' \quad \left| a' = 0 \right| \quad x' = 1$$

$$f'_c = \left| \begin{array}{cc} f = R^2 I^2 & f'_c = 0 \\ g = C+R & g' = 1 \end{array} \right| \frac{f'_g - g'_f f}{g^2} = \frac{-R^2 I^2}{(C+R)^2} \quad f'_c = -\frac{R^2 I^2}{(C+R)^2}$$

$$f'_I = (I^2)' \frac{R^2}{C+R} = (2I)' \frac{R^2}{C+R} = 2I \cdot \frac{R^2}{C+R}$$

$$f'_I = \frac{2R^2 I}{C+R}$$

$$f'_R = \left| \begin{array}{cc} f = R^2 I^2 & f'_R = 2RI^2 \\ g = C+R & g'_R = 1 \end{array} \right| \frac{f'_R - g'_R f}{(C+R)^2} = \frac{2RI^2(C+R) - 1 \cdot (R^2 I^2)}{(C+R)^2} =$$

$$= \frac{2R^2 I^2 + 2RI^2 C - R^2 I^2}{(C+R)^2} = \frac{R^2 I^2 (2-1) + RI^2 (2C)}{(C+R)^2} = \frac{RI^2 (R+2C)}{(C+R)^2}$$

$$= \frac{RI^2 (R+2C)}{(C+R)^2} \quad f'_R = \frac{RI^2 (R+2C)}{(C+R)^2}$$

$$\Delta f(x,y,z) = |f'_x| \Delta x + |f'_y| \Delta y + |f'_z| \Delta z \quad \delta f = \frac{\Delta f}{f} \quad \Delta f = 0.04206$$

$$|f'_c| \Delta C = \frac{1.1^2 \cdot 1.44}{2 \cdot 1^2} = \frac{1.44}{4.4} = 0.0327 \quad \Delta f = \frac{\Delta f}{|f|} = \frac{0.04206}{1.1 \cdot 1.44 / 2.1} = 0.01795$$

$$|f'_I| \Delta I = \frac{2 \cdot 1 \cdot 1.2}{2.1} = 0.012 = 0.01371$$

$$\Delta f = \frac{0.04206}{0.6877} = 0.0614$$

$$|f'_R| \Delta R = \frac{1 \cdot 1.44 \cdot (1+2.2)}{2.1^2} = 0.01 = \frac{4 \cdot 608}{4.41} \cdot 0.01 = 0.0104$$