1.

```
import tensorflow as tf
import numpy as np
from tensorflow.keras import regularizers
def func(t):
return np.sin(1 + t * np.pi * 2) / 2 + 1
def get_regression_dataset(start=0, end=3, seed=1, samples=80):
t = np.linspace(start, end, samples)
 oryginal = func(t)
 np.random.seed(seed)
 noisy = oryginal + np.random.normal(0, 0.2, samples)
 return noisy, oryginal
#define dataset
x_train, y_train = get_regression_dataset()
x_test, y_test = get_regression_dataset(seed=2)
x_train = x_train.reshape(80,1)
x_{\text{test}} = x_{\text{test.reshape}}(80,1)
y_train = y_train.reshape(80,1)
y_test = y_test.reshape(80,1)
x_train = tf.keras.utils.normalize(x_train, axis = 0) # scales data between 0 and 1
x_test = tf.keras.utils.normalize(x_test, axis = 0) # scales data between 0 and 1
model = tf.keras.Sequential(
 tf.keras.layers.Dense(10,input_shape=(1,), activation="relu", kernel_regularizer=regularizers.12(0.01)),
 tf.keras.layers.Dense(100, activation="relu", kernel_regularizer=regularizers.12(0.01)),
 tf.keras.layers.Dense(1)
```

2. Droput regulalizer

```
model = tf.keras.Sequential(
  [
   tf.keras.layers.Dense(10,input_shape=(1,), activation="relu"),
   tf.keras.layers.Dropout(0.2),
   tf.keras.layers.Dense(100, activation="relu"),
   tf.keras.layers.Dropout(0.2),
   tf.keras.layers.Dense(1)
  ]
}
```

```
Epoch 1/15
80/80 [========] - 1s 2ms/step - loss: 0.6688 - MSE: 0.6262
Epoch 2/15
80/80 [========] - Os 2ms/step - loss: 0.2927 - MSE: 0.1071
Epoch 3/15
80/80 [============== ] - Os 2ms/step - loss: 0.2778 - MSE: 0.1060
Epoch 4/15
80/80 [================ ] - Os 2ms/step - loss: 0.3158 - MSE: 0.1276
Epoch 5/15
80/80 [========] - Os 2ms/step - loss: 0.2625 - MSE: 0.0960
Epoch 6/15
80/80 [======== ] - Os 3ms/step - loss: 0.2513 - MSE: 0.0870
Epoch 7/15
80/80 [========] - Os 2ms/step - loss: 0.2444 - MSE: 0.0839
Epoch 8/15
80/80 [=======] - 0s 2ms/step - loss: 0.2383 - MSE: 0.0808
Epoch 9/15
80/80 [======== ] - Os 2ms/step - loss: 0.2632 - MSE: 0.1014
Epoch 10/15
80/80 [================ ] - Os 2ms/step - loss: 0.2652 - MSE: 0.0976
Epoch 11/15
80/80 [======== ] - Os 2ms/step - loss: 0.2135 - MSE: 0.0641
Epoch 12/15
80/80 [=========== ] - Os 2ms/step - loss: 0.2298 - MSE: 0.0746
Epoch 13/15
80/80 [=======] - Os 2ms/step - loss: 0.2662 - MSE: 0.0986
Epoch 14/15
80/80 [======] - Os 2ms/step - loss: 0.2353 - MSE: 0.0831
Epoch 15/15
80/80 [=======] - Os 2ms/step - loss: 0.2236 - MSE: 0.0802
3/3 [=======] - 0s 3ms/step - loss: 0.1855 - MSE: 0.0485
0.18549910187721252
0.048502955585718155
```

L1 regulalizer

```
model = tf.keras.Sequential(
[
    tf.keras.layers.Dense(10,input_shape=(1,), activation="relu", kernel_regularizer=regularizers.l1(0.01)),
    tf.keras.layers.Dense(100, activation="relu", kernel_regularizer=regularizers.l1(0.01)),
    tf.keras.layers.Dense(1)
]
```

```
Epoch 1/15
  80/80 [=======] - 1s 1ms/step - loss: 1.5580 - MSE: 0.5585
 Epoch 2/15
 80/80 [========] - 0s 1ms/step - loss: 0.7035 - MSE: 0.1060
 Epoch 3/15
  80/80 [======= ] - Os 1ms/step - loss: 0.4384 - MSE: 0.1038
  Epoch 4/15
  80/80 [=======] - Os 2ms/step - loss: 0.3852 - MSE: 0.1024
  Epoch 5/15
  80/80 [========= ] - Os 2ms/step - loss: 0.3758 - MSE: 0.1015
  Epoch 6/15
  80/80 [===========] - Os 2ms/step - loss: 0.3695 - MSE: 0.1024
  Epoch 7/15
  80/80 [========] - Os 1ms/step - loss: 0.3700 - MSE: 0.1053
  Epoch 8/15
  80/80 [========= ] - Os 1ms/step - loss: 0.3662 - MSE: 0.1068
  80/80 [======= ] - Os 1ms/step - loss: 0.3609 - MSE: 0.1046
  Epoch 10/15
  80/80 [======== ] - Os 1ms/step - loss: 0.3568 - MSE: 0.1031
  Epoch 11/15
  80/80 [======] - Os 1ms/step - loss: 0.3598 - MSE: 0.1069
  Epoch 12/15
  80/80 [=======] - Os 1ms/step - loss: 0.3518 - MSE: 0.1059
  Epoch 13/15
 80/80 [========= ] - Os 1ms/step - loss: 0.3601 - MSE: 0.1073
 Epoch 14/15
 80/80 [======] - Os 1ms/step - loss: 0.3521 - MSE: 0.1032
 Epoch 15/15
  80/80 [=======] - Os 1ms/step - loss: 0.3504 - MSE: 0.1040
  3/3 [==========] - 0s 3ms/step - loss: 0.3473 - MSE: 0.1021
  0.34725329279899597
0.10210946947336197
```

L2 regulalizer

```
model = tf.keras.Sequential(
  [
  tf.keras.layers.Dense(10,input_shape=(1,), activation="relu", kernel_regularizer=regularizers.12(0.01)),
  tf.keras.layers.Dense(100, activation="relu", kernel_regularizer=regularizers.12(0.01)),
  tf.keras.layers.Dense(1)
  ]
)
```

```
Epoch 1/15
80/80 [=============] - 1s 1ms/step - loss: 0.8617 - MSE: 0.7325
Epoch 2/15
80/80 [========] - Os 1ms/step - loss: 0.3759 - MSE: 0.1446
Epoch 3/15
80/80 [========] - Os 1ms/step - loss: 0.3314 - MSE: 0.1149
Epoch 4/15
Epoch 5/15
Epoch 6/15
Epoch 7/15
80/80 [============= - - os 2ms/step - loss: 0.3170 - MSE: 0.1131
Epoch 8/15
Epoch 9/15
80/80 [===========] - 0s 2ms/step - loss: 0.3129 - MSE: 0.1094
Epoch 10/15
Epoch 11/15
80/80 [=======] - Os 1ms/step - loss: 0.3104 - MSE: 0.1067
Epoch 12/15
80/80 [=======] - Os 1ms/step - loss: 0.3107 - MSE: 0.1049
Epoch 13/15
80/80 [===========] - 0s 1ms/step - loss: 0.3070 - MSE: 0.1044
Epoch 14/15
Epoch 15/15
3/3 [======] - Os 2ms/step - loss: 0.3005 - MSE: 0.0988
0.30049461126327515
0.09883756190538406
```

Zastosowanie metody DROPOUT pozwala uzyskać wyniki najbardziej zbliżone do zakładanych. Regularyzacja technikami L1 oraz L2 daje podobne wyniki. Technika DROPUT w tym wypadku mogła okazać się najbardziej dostosowana ze względu na pominięcie obserwacji odstających. Metody L1 oraz L2 wykonane zostały z określonymi wartościami alfa, które mogą nie być najbardziej dostosowane to badanego przypadku.