

Equations used for this project

[github/piotrkossa/Turing-Pattern-Simulation-In-Unity](https://github.com/piotrkossa/Turing-Pattern-Simulation-In-Unity)

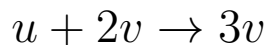
[Used Source](#)

1 The Project Goal

The goal of this project is to implement the Gray-Scott reaction-diffusion model in real time in Unity. It leverages the parallel processing power of the GPU using Compute Shaders to visualize complex Turing patterns at an efficient refresh rate. This document provides a brief description of the mathematical model and its implementation.

2 Overview

The simulation bases on the interaction between an **Activator** (u) and an **Inhibitor** (v). Everything is driven by a single reaction, where the **Activator** is used up to create more of the **Inhibitor**.



If that was all, the reaction would stop after a certain amount of time. This is why two processes are constantly active to keep it running:

1. A specified amount of the **Activator** (u) is continuously added to the system, controlled by the **Feed Rate** (f)
2. The **Inhibitor** (v) is slowly removed, controlled by the **Kill Rate** (k)

Obtained patterns come from how the chemicals diffuse on the plane and not the reaction alone. Spreading out at different speeds causes creation of new unique patterns, even after minor change of **Diffusion Rates** (D_u, D_v)

3 Equations of the Gray-Scott Model

$$\begin{aligned}\partial u / \partial t &= (D_u * \nabla^2 u) - (u * v^2) + (f * (1 - u)) \\ \partial v / \partial t &= (D_v * \nabla^2 v) + (u * v^2) - ((k + f) * v)\end{aligned}$$

Symbol	Description
u	Concentration of Activator
v	Concentration of Inhibitor
D_u, D_v	Diffusion Rates of Chemicals
$\nabla^2 u, \nabla^2 v$	Laplacian - Spatial Diffusion
f	The Feed Rate, represents a constant supply of substance u
k	The Kill Rate, represents the rate of removal of substance v
$\partial u / \partial t, \partial v / \partial t$	Time Derivatives of Concentrations

4 The Laplacian

The Laplacian operator (∇^2) is calculated using a 3x3 convolution kernel:

$$\begin{bmatrix} 0.05 & 0.20 & 0.05 \\ 0.20 & -1.0 & 0.20 \\ 0.05 & 0.20 & 0.05 \end{bmatrix}$$

For each pixel, the values of its eight neighbors and itself are multiplied by the corresponding weights in the kernel, and the results are summed up to produce the final Laplacian value.