

```
In [16]: import scipy.constants as const
import numpy as np
```

```
In [47]: def alpha(E_gamma=None, nu=None):
        """ Should specify E_gamma in eV
        """
        mecsquared = const.value('electron mass energy equivalent in MeV')
        * 10**6
        h = const.value('Planck constant in eV s')
        if E_gamma is None and nu is None:
            raise exception("Must specify photon properties")
        elif nu is None:
            a = E_gamma / mecsquared
        elif E_gamma is None:
            a = h * nu / mecsquared
        else:
            raise exception('Please only specify one photon property')

        return a
```

```
In [48]: def T_e_max(E_gamma=None, nu=None):
        """ Specify E_gamma in eV
        """
        h = const.value('Planck constant in eV s')
        if E_gamma is None and nu is None:
            raise exception("Must specify photon properties")
        elif nu is None:
            a = alpha(E_gamma=E_gamma)
            t = E_gamma * 2.0 * a / (1.0 + 2.0 * a)
        elif E_gamma is None:
            a = alpha(nu=nu)
            t = h * nu * 2.0 * a / (1.0 + 2.0 * a)
        else:
            raise exception('Please only specify one photon property')

        return t
```

```
In [49]: def theta_e(T_gamma, theta_gamma):
        a = alpha(E_gamma=T_gamma)
        inner = (1.0 + a) * np.tan(theta_gamma / 2.0)
        return np.arctan(1.0 / inner)
```

```
In [50]: def T_e(T_gamma, theta):  
         a = alpha(E_gamma=T_gamma)  
         numerator = T_gamma * a * (1.0 - np.cos(theta))  
         denominator = 1.0 + a * (1.0 - np.cos(theta))  
  
         return numerator / denominator
```

Problem 5: Anderson 6.4

```
In [51]: theta_prime = 60.0 * np.pi / 180.0
```

```
In [52]: T_g = 140000
```

```
In [53]: alpha(E_gamma=T_g)
```

```
Out[53]: 0.27397316778927894
```

Calculate the angle of scatter of the Compton electron

```
In [56]: theta_e(T_g, theta_prime) * 180.0 / np.pi
```

```
Out[56]: 53.664449190568014
```

```
In [57]: T_e(T_g, theta_prime)
```

```
Out[57]: 16867.500476176854
```

Problem 6

References:

- [Mn-54 \(http://www.nucleide.org/DDEP_WG/Nuclides/Mn-54_tables.pdf\)](http://www.nucleide.org/DDEP_WG/Nuclides/Mn-54_tables.pdf) gamma energy 834.855 keV
- [Cs-137 \(http://www.nucleide.org/DDEP_WG/Nuclides/Cs-137_tables.pdf\)](http://www.nucleide.org/DDEP_WG/Nuclides/Cs-137_tables.pdf) gamma energy 661.659 keV
- [Na-22 \(http://www.nucleide.org/DDEP_WG/Nuclides/Na-22_tables.pdf\)](http://www.nucleide.org/DDEP_WG/Nuclides/Na-22_tables.pdf) gamma energy 1274.577 keV

Mn-54:

```
In [58]: T_e_max(E_gamma=834855)
```

```
Out[58]: 639225.9473887982
```

```
In [59]: T_e_max(E_gamma=661659)
```

```
Out[59]: 477335.86413384555
```

```
In [60]: T_e_max(E_gamma=1274577)
```

```
Out[60]: 1061742.0485465585
```

Problem 7

```
In [61]: def sigma_kn(E_gamma):
          r = const.value('classical electron radius') * 100 # convert from
          m to cm

          a = alpha(E_gamma=E_gamma)

          answer = np.pi * r * r

          term1 = 2.0 * (1.0 + a) / a ** 2
          term1 *= (2.0 * (1.0 + a) / (1.0 + 2.0 * a) - np.log(1.0 + 2.0 * a
          ) / a)
          term1 += np.log(1.0 + 2.0 * a) / a
          term1 -= 2.0 * (1.0 + 3.0 * a) / (1.0 + 2.0 * a) ** 2

          return answer * term1
```

Part (a)

```
In [62]: E = 661659.0 # eV
```

```
In [63]: sigma_kn(E)
```

```
Out[63]: 2.5619923244178853e-25
```

Convert from cm^2 to b

```
In [64]: sigma_kn(E) * 10**24
```

```
Out[64]: 0.25619923244178855
```

Part (b)

From the notes, $\sigma_{atomic} = \sigma_{Compton} = Z * \sigma_{KN}$

```
In [67]: sigma_kn(E) * 10**24 * 82.0
```

```
Out[67]: 21.008337060226662
```

Part (c)

$$(\mu/\rho)_{is} = n_m \sigma_{is}, n_m = \frac{N_A Z}{M_m}$$

```
In [68]: rho = 11.34 # g/cm^3
n_m = const.Avogadro * 82.0 / 207.2
```

```
In [70]: n_m * sigma_kn(E) * 82.0 * rho
```

```
Out[70]: 56.77795443140117
```

Problem 8

```
In [72]: def sigma_prime(T_e, T_gamma=500000):
    r = const.value('classical electron radius') * 100 # convert to cm
    a = alpha(E_gamma=T_gamma)

    constant_part = np.pi * r * r / (a * T_gamma)

    other_part = T_e ** 2 / (T_gamma - T_e) ** 2
    other_part *= (1 / a ** 2 + (T_gamma - T_e) / T_gamma - 2 * (T_gamma - T_e) / (a * T_e))
    other_part += 2.0

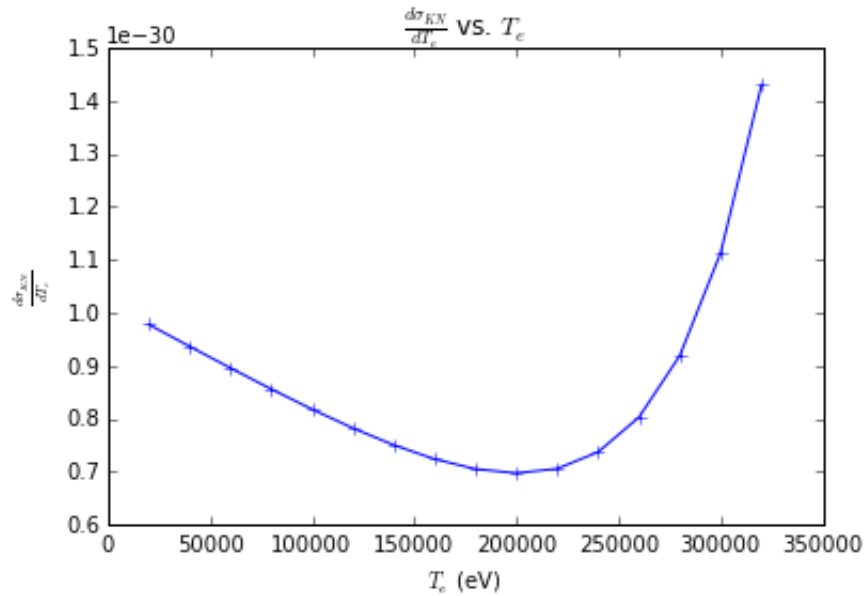
    return other_part * constant_part
```

```
In [73]: %matplotlib inline
```

```
In [74]: import matplotlib.pyplot as plt
```

```
In [75]: T_in = np.arange(20000, T_e_max(E_gamma=500000), 20000)
```

```
In [81]: plt.plot(T_in, sigma_prime(T_in), 'b-+')
plt.ylabel(r'$\frac{d\sigma_{KN}}{dT_e}$')
plt.xlabel(r'$T_e$ (eV)')
plt.title(r'$\frac{d\sigma_{KN}}{dT_e}$ vs. $T_e$')
plt.show()
```



```
In [ ]:
```