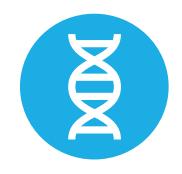


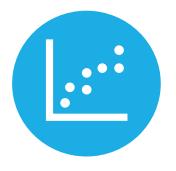
A SHORT OVERVIEW



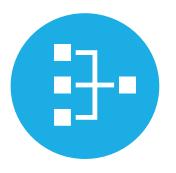




DNA METHYLATION



LINEAR REGRESSION
WITH
REGULARIZATION

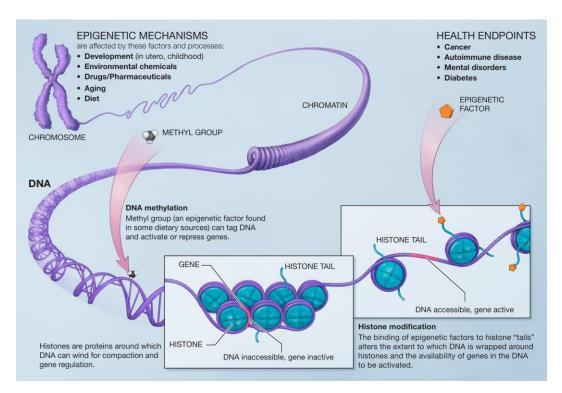


CHRONOLOGICAL AGE PREDICTION

CHRONOLOGICAL/BIOLOGICAL AGE

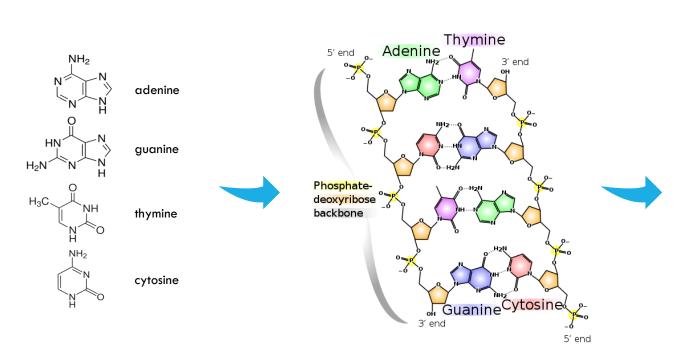
- Chronological age: time elapsed since birth
- Biological age: captures the different rate of functional deterioration across individuals
 - Aging has many manifestations (greying hair, wrinkles, reduced mobility, etc.)
 - Many manifestations are epigenetic (e.g. DNA methylation)

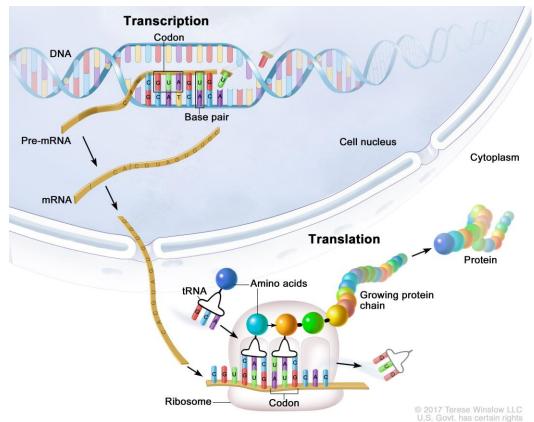
Epigenetic changes: changes functionally effecting the genome that do not involve a change in the nucleotide sequence of the DNA



NIH - National Institutes of Health

THE IMPORTANCE OF DNA





nucleobases

base-pairs, double-stranded helix structure

transcription, translation, proteins

DNA METHYLATION (DNAm)

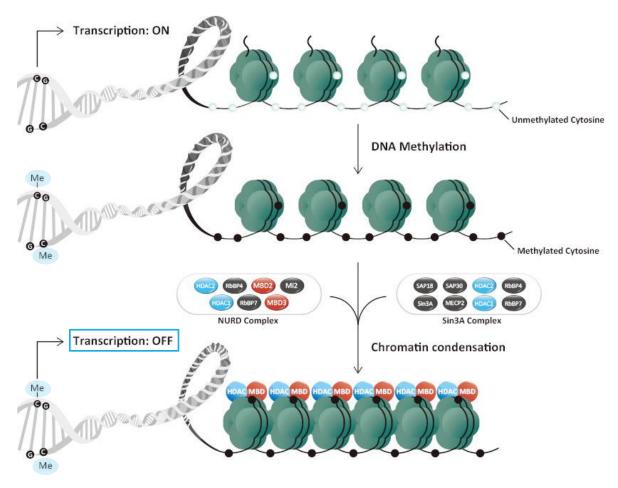
$$\begin{array}{c} NH_2 \\ NH_2 \\ NH_3 \\ NH_2 \\ NH_3 \\ NH_2 \\ NH_3 \\ NH_2 \\ NH_3 \\ NH$$

cytosine

5-methylcytosine

(almost exclusively in CpG dinucleotides)

DNA methylation has a regulatory role by affecting the accessibility of different genomic regions, thus influencing transcription (~ activity)



https://www.genetex.com/Research/Overview/epigenetics/dna_methylation

DNA METHYLATION (DNAm)

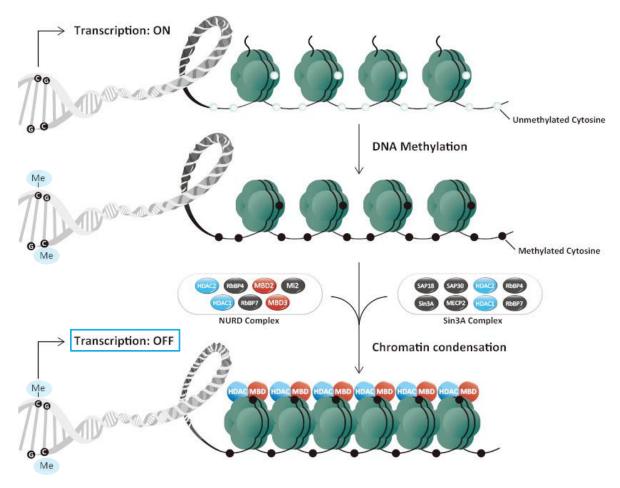
$$\begin{array}{c} NH_2 \\ NH_3C \\ NH_2 \\ NH_3C \\ N$$

cytosine

5-methylcytosine

(almost exclusively in CpG dinucleotides)

DNA methylation has a regulatory role by affecting the accessibility of different genomic regions, thus influencing transcription (~ activity)



https://www.genetex.com/Research/Overview/epigenetics/dna_methylation

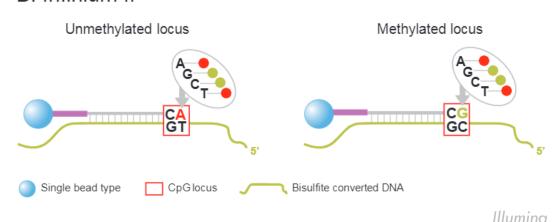
... but generally, it's much more complex

DNA METHYLATION (DNAm)

How is it measured? – a simplified picture

- Bisulfite conversion
 - cytosine \rightarrow uracil \rightarrow thymine
 - methyl-cytosine → cytosine
- 2. Amplification
- 3. Attachment of single DNA strands to probe sequences terminating right before the target site
- 4. Trying to elongate probe sequence with either A/T or G/C nucleotides labelled with different colors
- 5. Measuring resulting light intensities

B. Infinium II



$$\beta = \frac{I_{meth}}{(I_{meth} + I_{unmeth} + \alpha)}$$

 \rightarrow a single β -value for each genomic position of interest

LINEAR REGRESSION

~ "fit a line to the data (sometimes in many-many dimensions) that describes it well enough"

LINEAR REGRESSION

~ "**fit a line** to the data (sometimes in many-many dimensions) that describes it well enough" ... or more precisely:

- Given a $\{x_{i_j}\}_{i \in \{1,2,...s\}}^{j \in \{1,2,...k\}}$ set of k inputs/independent variables/features/predictors
- for s samples/observations,
- find the b_j coefficients of the (linear) function $f(\pmb{x_i}) = b_0 + \sum_{j=1}^k b_j x_{i_j} = \hat{y}_i$
- that minimizes the "prediction error" defined as $\sum_{i=1}^{S} (y_i \hat{y}_i)^2$ for the output/dependent variable/response of $y = (y_1, y_2, \dots y_S)$.

LINEAR REGRESSION

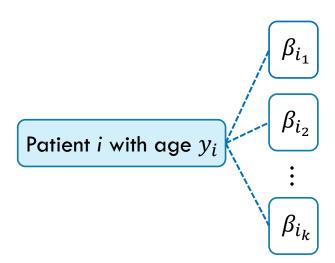
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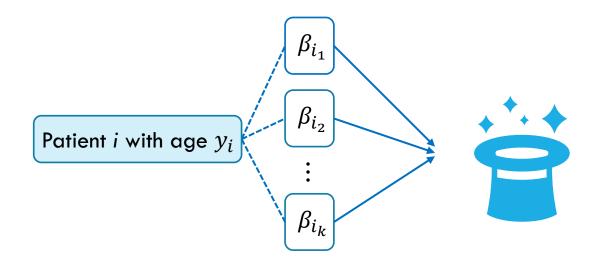
~ "method of ordinary least squares"

- inputs/independent variables/features/predictors: methylation β -values in targeted genomic positions
- samples/observations: patients
- output/dependent variable/response: chronological age

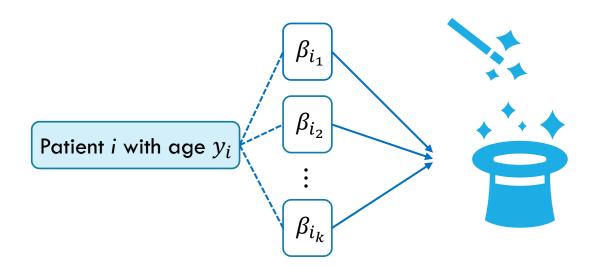
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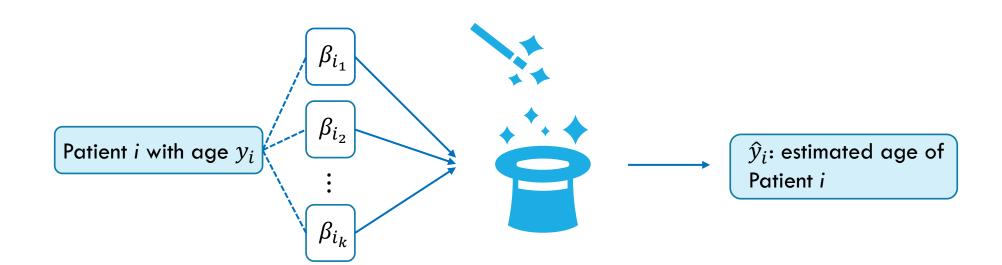
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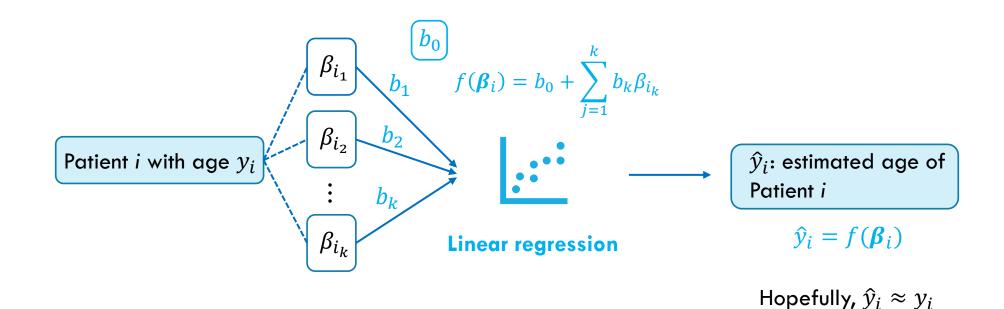
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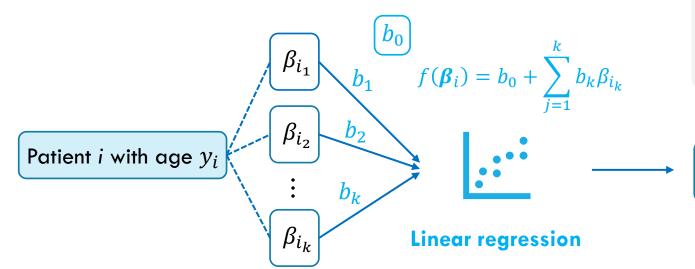
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- Is the model bad if a patient's predicted age is vastly different from his/her chronological age?
- What could cause such an effect besides a bad model?

 \hat{y}_i : estimated age of Patient i

$$\hat{y}_i = f(\boldsymbol{\beta}_i)$$

Hopefully, $\hat{y}_i \approx y_i$

- Number of features: 27K / 450K / 850K (depending on measurement platform)
- Number of patients: 10K at best (depending on data availability and research funds)
- There is an enormous chance of overfitting the model if we use all β -values for prediction!

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→ **REGULARIZATION!**

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Instead of simply minimizing $\sum_{i=1}^{s} (y_i - \hat{y}_i)^2$, let's minimize

$$\sum_{i=1}^{s} (y_i - \hat{y}_i)^2 + \alpha \sum_{j=1}^{k} b_j^2 + \lambda \sum_{j=1}^{k} |b_j|$$

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- $\alpha = 0, \lambda = 0 \rightarrow \text{ordinary least squares}$
- $\alpha = 0, \lambda \neq 0 \rightarrow$ "Lasso regression" (L1-regularization)
- $\alpha \neq 0, \lambda = 0 \rightarrow$ "Ridge regression" (L2-regularization)
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- What do you think would happen if either $\alpha \to \infty$ or $\lambda \to \infty$?
- How would you choose the optimal α and λ ?

• For details, check out Horvath (2013): DNA methylation age of human tissues and cell types

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 - Publicly available
 - From healthy donors
 - The data from a specific study was never split between train & test sets
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 - Many different tissues

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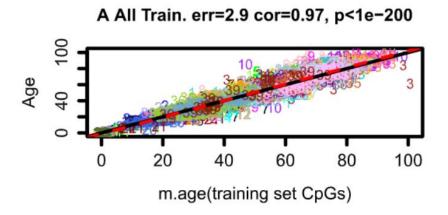
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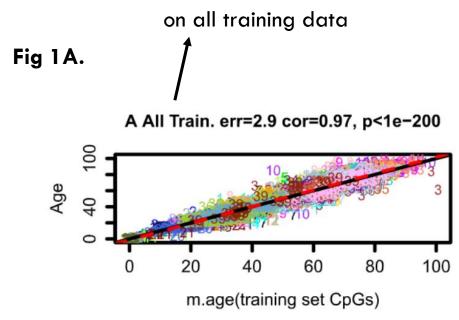
What's that?

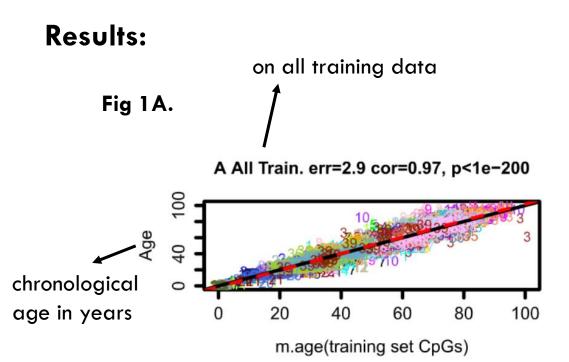
Results:

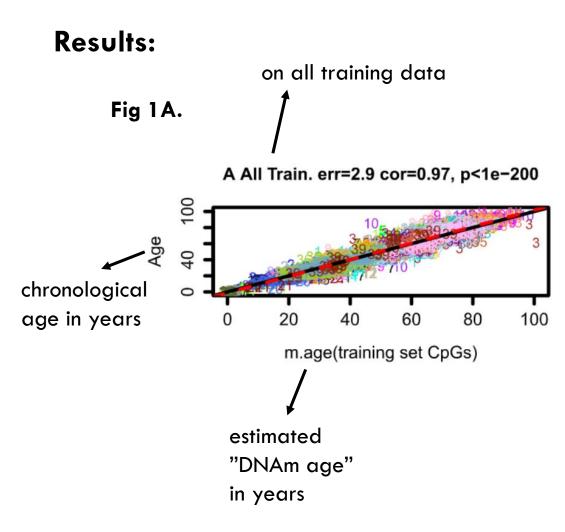
Fig 1A.

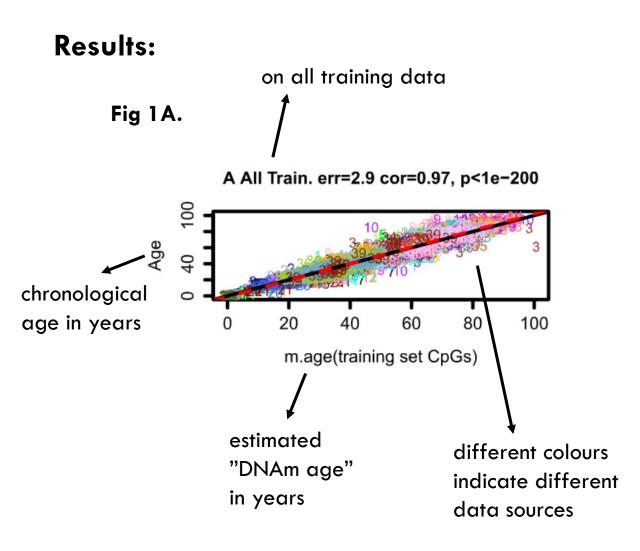


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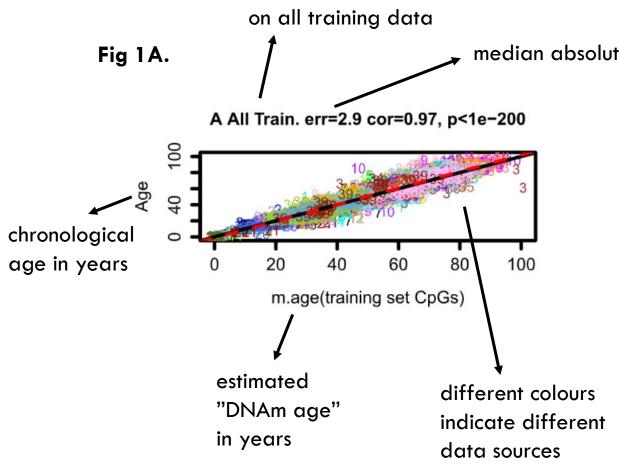




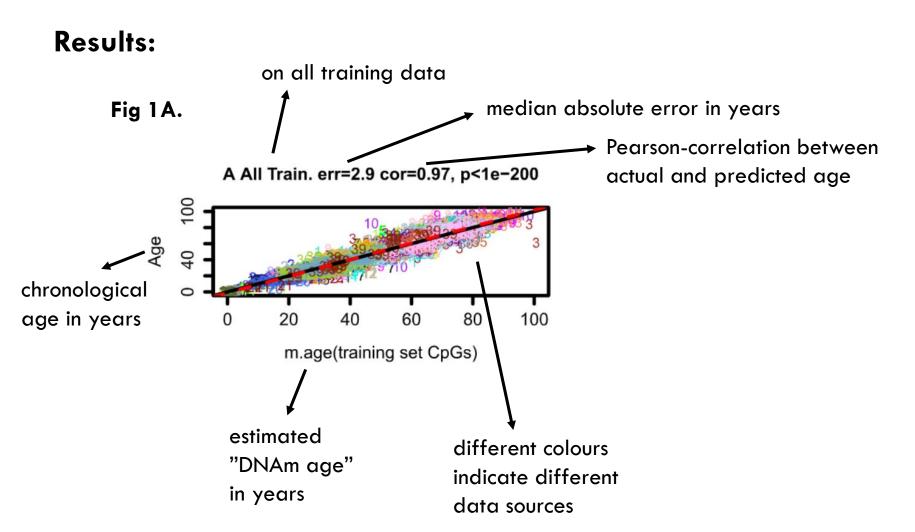








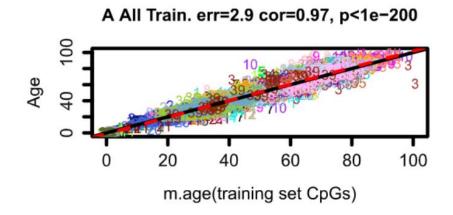
median absolute error in years: for half of the patients in the training set, the
difference between the estimated and the
actual age was smaller than 2.9 years



Results:

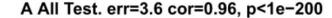


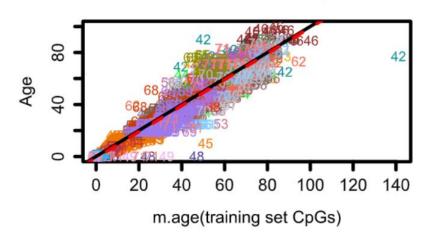
Fig 1A. on all training data





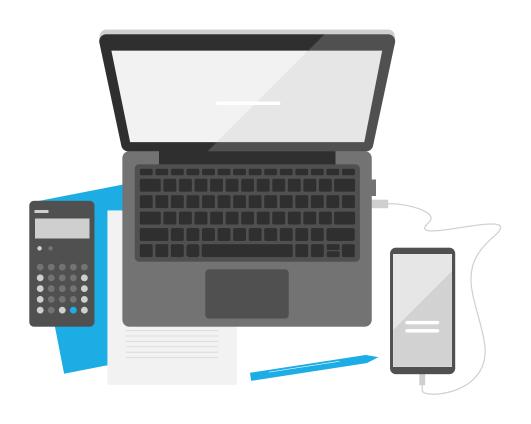
on all test data





- On which dataset would you expect higher correlation? Why?
- On which dataset would you expect higher median absolute error? Why?

TRYING IT OUT FOR REAL...



- 1. Downloading an appropriate dataset
- 2. Building a model that predicts age
- 3. Testing the Horvath multi-tissue epigenetic clock
- 4. Comparing the results