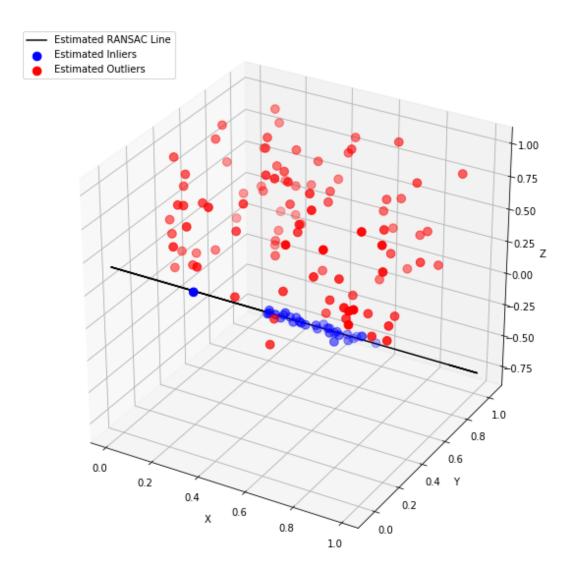
## BIOS 7718-Assignment 2 Source Code

## April 8, 2019

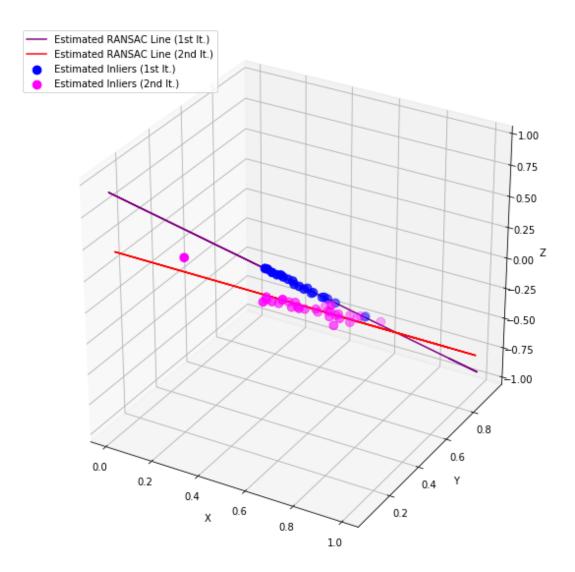
```
In [44]: #### Problem 1.1 ####
         import numpy as np
         import matplotlib.pyplot as plt
         from mpl_toolkits.mplot3d import Axes3D
         from skimage.measure import LineModelND, ransac
         # generate inliers prior to adding Gaussian noise
         x = np.arange(0.4, 0.70, 0.01).reshape(-1,1)
         y = x
         z = (1 - x - 2*y)/3
         inl = np.concatenate((x, y, z), axis = 1)
         # generate Gaussian noise
         # set seed
         np.random.seed(1212)
         mu = (0, 0, 0)
         cov = [[(0.03)**2,0,0], [0,(0.03)**2,0], [0,0,(0.03)**2]]
         err = np.random.multivariate_normal(mu, cov, 30)
         # add noise to inliers
         inl_final = inl + err
         # generate outliers
         # set seed
         np.random.seed(1212)
         outl = []
         for i in range(1,101):
             single_outl = np.random.uniform([0,0,0], [1,1,1])
             outl.append(single_outl)
         outl_final = np.array(outl)
         # combine all data
         all_data = np.vstack((inl_final, outl_final))
         # designate inliers and outliers
         indices = np.arange(all_data.shape[0])
```

```
inlier_indices = indices[0:30]
outlier_indices = indices[30:]
# robustly fit line only using inlier data with RANSAC algorithm
# set seed
np.random.seed(1212)
model_ransac, inliers = ransac(all_data, LineModelND,
                               min_samples=2,
                               residual threshold=0.08,
                               max_trials=500,
                               stop_probability = 0.99)
outliers = inliers == False
# 3D line coordinates
pred_line = model_ransac.predict(all_data[:,0])
# plot 3D line and data points fit using RANSAC
fig = plt.figure(figsize = (10,10))
ax = plt.axes(projection='3d')
ax.scatter(all_data[inliers][:, 0],
           all_data[inliers][:, 1],
           all_data[inliers][:, 2], c='b',
           marker='o', label='Estimated Inliers', s=75)
ax.scatter(all_data[outliers][:, 0],
           all_data[outliers][:, 1],
           all_data[outliers][:, 2], c='r',
           marker='o', label='Estimated Outliers', s=75)
ax.plot(pred_line[:,0], pred_line[:,1],
        pred_line[:,2], color = 'black',
        label='Estimated RANSAC Line')
ax.set_xlabel('X'), ax.set_ylabel('Y'), ax.set_zlabel('Z')
ax.legend(loc='upper left')
plt.show()
```



```
z_2 = 1 - x_2 - y_2
         inl_2 = np.concatenate((x_2, y_2, z_2), axis = 1)
         # generate Gaussian noise
         # set seed
         np.random.seed(1212)
         mu 2 = (0, 0, 0)
         cov_2 = [[(0.01)**2,0,0], [0,(0.01)**2,0], [0,0,(0.01)**2]]
         err_2 = np.random.multivariate_normal(mu_2, cov_2, 20)
         # add noise to inliers
         inl_2_final = inl_2 + err_2
         # combine all data
         all_data_2 = np.vstack((inl_2_final, all_data))
         # fit first line
         # set seed
         np.random.seed(1212)
         model_ransac_1, inliers_1 = ransac(all_data_2, LineModelND,
                                            min_samples=2,
                                            residual threshold=0.02,
                                            max_trials=500,
                                            stop_probability = 0.99)
         outliers_1 = inliers_1 == False
         # 3D line coordinates
         pred_line_1 = model_ransac_1.predict(all_data_2[:,0])
In [48]: # number of inliers detected (1st It.)
         np.sum(inliers_1)
Out[48]: 20
In [49]: # number of TRUE inliers detected (1st It.)
         np.sum(inliers_1[0:20])
Out [49]: 18
In [50]: # exlude inliers detected from second RANSAC fitting
         all_data_2_exc = all_data_2[outliers_1]
         # fit first line
         # set seed
         np.random.seed(1212)
         model_ransac_2, inliers_2 = ransac(all_data_2_exc,
                                            LineModelND,
                                            min_samples=2,
                                            residual_threshold=0.08,
```

```
max_trials=500,
                                   stop_probability = 0.99)
outliers_2 = inliers_2 == False
# 3D line coordinates
pred_line_2 = model_ransac_2.predict(all_data_2_exc[:,0])
# plot 3D line and data points fit using RANSAC
fig = plt.figure(figsize = (10,10))
ax = plt.axes(projection='3d')
ax.scatter(all_data_2[inliers_1][:, 0],
           all_data_2[inliers_1][:, 1],
           all_data_2[inliers_1][:, 2], c='b',
           marker='o',
           label='Estimated Inliers (1st It.)', s=75)
ax.plot(pred_line_1[:,0],
        pred_line_1[:,1],
       pred_line_1[:,2],
        color = 'purple',
        label='Estimated RANSAC Line (1st It.)')
ax.scatter(all_data_2_exc[inliers_2][:, 0],
           all_data_2_exc[inliers_2][:, 1],
           all_data_2_exc[inliers_2][:, 2],
           c='magenta',
           marker='o',
           label='Estimated Inliers (2nd It.)', s=75)
ax.plot(pred_line_2[:,0], pred_line_2[:,1],
        pred_line_2[:,2], color = 'r',
        label='Estimated RANSAC Line (2nd It.)')
ax.set_xlabel('X'), ax.set_ylabel('Y'), ax.set_zlabel('Z')
ax.legend(loc='upper left')
plt.show()
```



```
# Hough transform to detect circles
         circles = cv2.HoughCircles(car_img_smooth, cv2.HOUGH_GRADIENT, 1, 80,
                                     param1=100, param2=30, minRadius=0, maxRadius=0)
         circles = np.uint16(np.around(circles))
         for i in circles[0,:]:
             # draw the outer circle
             cv2.circle(car_img,(i[0],i[1]),i[2],(0,255,0),2)
             # draw the center of the circle
             cv2.circle(car_img,(i[0],i[1]),2,(255,0,0),5)
         cv2.imwrite('/Users/piper/Piper Documents/Biomedical Imaging/Assignments/Assignment 2
Out[52]: True
In [53]: ##### Problem 2.2 #####
         # read image in
         nuclei_img = cv2.imread('/Users/piper/Piper Documents/Biomedical Imaging/Assignments/
         nuclei_img_grey = cv2.cvtColor(nuclei_img, cv2.COLOR_BGR2GRAY)
         # smooth image with Gaussian filter
         nuclei_img_smooth = cv2.GaussianBlur(nuclei_img_grey, (31,31), 5)
         # Hough transform to detect circles
         circles = cv2.HoughCircles(nuclei_img_grey, cv2.HOUGH_GRADIENT, 1, 40,
                                   param1=150, param2=12, minRadius=0, maxRadius=30)
         circles = np.uint16(np.around(circles))
         for i in circles[0,:]:
             # draw the center of the circle
             cv2.circle(nuclei_img,(i[0],i[1]),2,(0,0,255),10)
         cv2.imwrite('/Users/piper/Piper Documents/Biomedical Imaging/Assignments/Assignment 2
Out[53]: True
In [54]: # number of detected nuclei
         np.shape(circles)[1]
Out[54]: 44
In [55]: ##### Problem 3.1 #####
         coin_img = cv2.imread('/Users/piper/Piper Documents/Biomedical Imaging/Assignments/Ass
         coin_img_grey = cv2.imread('/Users/piper/Piper Documents/Biomedical Imaging/Assignment
         coin_img_grey_final = ~coin_img_grey
         # create kernel
```

```
kernel = np.ones((11,11), np.uint8)
# thresholding grey-scale image
ret, thresh_img = cv2.threshold(coin_img_grey_final, 0, 255, cv2.THRESH_BINARY + cv2.
# erode image to get foreground
erode_img = cv2.erode(thresh_img, kernel, iterations=2)
# dilate image to get background
dilate_img = cv2.dilate(thresh_img, kernel, iterations=2)
# subtract eroded and dilated images to get 'unknown' region
unknown = cv2.subtract(dilate_img, erode_img)
# label markers
ret, markers = cv2.connectedComponents(erode_img)
# add 1 to all labels so that sure background is 1
markers = markers+1
# mark unknown region with 0
markers[unknown==255] = 0
# apply watershed transform
markers = cv2.watershed(coin_img, markers)
# make each segment a different color
coin_img[markers == -1] = [0,0,0]
coin_img[markers == 1] = [211,211,211]
coin_img[markers == 2] = [128,0,0]
coin_img[markers == 3] = [220, 20, 60]
coin_img[markers == 4] = [255,0,0]
coin_img[markers == 5] = [255,99,71]
coin_img[markers == 6] = [255,69,0]
coin_img[markers == 7] = [255,140,0]
coin_img[markers == 8] = [255,215,0]
coin_img[markers == 9] = [218,165,32]
coin_img[markers == 10] = [0,100,0]
coin_img[markers == 11] = [0,255,0]
coin_img[markers == 12] = [50,205,50]
coin_img[markers == 13] = [0,250,154]
coin_img[markers == 14] = [46,139,87]
coin_img[markers == 15] = [32,178,170]
coin_img[markers == 16] = [47,79,79]
coin_img[markers == 17] = [0,255,255]
coin_img[markers == 18] = [0,191,255]
coin_img[markers == 19] = [135,206,250]
coin_img[markers == 20] = [0,0,128]
```

```
coin_img[markers == 21] = [0,0,255]
         coin_img[markers == 22] = [138,43,226]
         coin_img[markers == 23] = [75,0,130]
         # save image
         cv2.imwrite('/Users/piper/Piper Documents/Biomedical Imaging/Assignments/Assignment 2
Out [55]: True
In [56]: np.unique(markers)
Out[56]: array([-1, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16,
                17, 18, 19, 20, 21, 22, 23], dtype=int32)
In [57]: ##### Problem 3.2 #####
        particle_img = cv2.imread('/Users/piper/Piper Documents/Biomedical Imaging/Assignments
        particle_img_grey = cv2.imread('/Users/piper/Piper Documents/Biomedical Imaging/Assign
        particle_img_grey_final = ~particle_img_grey
         # thresholding
        ret, thresh_img = cv2.threshold(particle_img_grey_final, 0, 255, cv2.THRESH_BINARY +
         # noise removal using opening operation
        kernel = np.ones((11,11), np.uint8)
         open_img = cv2.morphologyEx(thresh_img, cv2.MORPH_OPEN, kernel, iterations = 1)
         # sure background area
         sure_bg = cv2.dilate(open_img, kernel, iterations = 1)
         # sure foreground area
        dist_transform = cv2.distanceTransform(open_img, cv2.DIST_L2, 5)
        ret, sure_fg = cv2.threshold(dist_transform, 0.15*dist_transform.max(), 255, 0)
         # unknown region
         sure_fg = np.uint8(sure_fg)
        unknown = cv2.subtract(sure_bg, sure_fg)
         # label markers
        ret, markers = cv2.connectedComponents(sure_fg)
         # add 1 to all labels so that sure background is 1
        markers = markers + 1
         # mark unknown region with O
        markers[unknown==255] = 0
         # apply watershed transform
        markers = cv2.watershed(particle_img, markers)
```

```
# make each segment a different color
                          particle_img[markers == -1] = [0,0,0]
                          particle_img[markers == 1] = [211,211,211]
                          particle_img[markers == 2] = [128,0,0]
                          particle img[markers == 3] = [220, 20, 60]
                          particle_img[markers == 4] = [255,0,0]
                          particle img[markers == 5] = [255,99,71]
                          particle_img[markers == 6] = [255,69,0]
                          particle_img[markers == 7] = [255,140,0]
                          particle_img[markers == 8] = [255,215,0]
                          particle_img[markers == 9] = [218,165,32]
                          particle_img[markers == 10] = [0,100,0]
                          particle_img[markers == 11] = [0,255,0]
                          particle_img[markers == 12] = [50,205,50]
                          particle_img[markers == 13] = [0,250,154]
                          particle_img[markers == 14] = [46,139,87]
                          particle_img[markers == 15] = [32,178,170]
                          particle_img[markers == 16] = [47,79,79]
                          particle_img[markers == 17] = [0,255,255]
                          particle_img[markers == 18] = [0,191,255]
                          particle_img[markers == 19] = [135,206,250]
                          particle_img[markers == 20] = [0,0,128]
                          particle_img[markers == 21] = [0,0,255]
                          particle_img[markers == 22] = [138,43,226]
                          particle_img[markers == 23] = [75,0,130]
                          particle_img[markers == 24] = [147,112,219]
                          particle_img[markers == 25] = [128,0,128]
                          particle_img[markers == 26] = [255,0,255]
                          particle_img[markers == 27] = [199,21,133]
                          particle_img[markers == 28] = [255,105,180]
                          particle_img[markers == 29] = [219,112,147]
                          particle_img[markers == 30] = [255,192,203]
                           # save image
                           cv2.imwrite('/Users/piper/Piper Documents/Biomedical Imaging/Assignments/Assignment 2
Out[57]: True
In [58]: np.unique(markers)
Out[58]: array([-1, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16,
                                               17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30],
                                            dtype=int32)
In [59]: # generate overlay images for Problem 3
                           img_1 = cv2.imread('/Users/piper/Piper Documents/Biomedical Imaging/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignment
                           img_2 = cv2.imread('/Users/piper/Piper Documents/Biomedical Imaging/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignments/Assignment
                          w1 = cv2.imread('/Users/piper/Piper Documents/Biomedical Imaging/Assignments/Assignments
                          w2 = cv2.imread('/Users/piper/Piper Documents/Biomedical Imaging/Assignments/Assignments
```

```
combine_1 = cv2.addWeighted(img_1, 0.6, w1, 0.4, 0)
combine_2 = cv2.addWeighted(img_2, 0.6, w2, 0.4, 0)

# save images
cv2.imwrite('/Users/piper/Piper Documents/Biomedical Imaging/Assignments/Assignment 2
cv2.imwrite('/Users/piper/Piper Documents/Biomedical Imaging/Assignments/Assignment 2
Out[59]: True
```