

$$1. \quad \zeta = 0.148$$

$$A(\omega) = \frac{1}{\sqrt{(1 - \frac{\omega^2}{\omega_0^2})^2 + (\frac{2\zeta\omega}{\omega_0})^2}} = 1.31$$

$$\varphi(\omega) = -\arctan \frac{2\zeta \frac{\omega}{\omega_0}}{1 - (\frac{\omega}{\omega_0})^2} = -10.57^\circ$$

$$\sigma = \frac{|A(\omega) - 1|}{1} \times 100\% = 31\%$$

$$\Delta\varphi = -\arctan \frac{2\zeta \frac{\omega}{\omega_0}}{1 - (\frac{\omega}{\omega_0})^2} = -10.57^\circ$$

$$\zeta = 0.7 \text{ 时, } A(\omega) = 0.97$$

$$\varphi(\omega) = -43^\circ$$

$$\sigma = \frac{|0.97 - 1|}{1} = 3\%, \quad \Delta\varphi = -43^\circ$$

2. (1) - 阶测量系统

$$(1) \quad \text{令 } \frac{x}{s} = X$$

$$\frac{mnp}{q} \frac{d}{dt} X + X = \phi$$

$$(2) \quad \tau = \frac{mnp}{q}$$

$$(3) \quad \frac{mnp}{q} \cdot s X(s) + X(s) = \Phi(s)$$



$$\frac{X(s)}{\Phi(s)} = \frac{1}{1 + \frac{mnp}{q}s} = \frac{q}{q + mnp.s}$$

$$\frac{X(j\omega)}{\Phi(j\omega)} = \frac{q}{q + mnp.j\omega}$$

(4) τ 将减小 100 倍.

工作频率增大 100 倍.

$$3. (1) \varepsilon = \left| \frac{1}{\sqrt{1+(\omega\tau)^2}} - 1 \right| = 100\% \leq 5\%$$

$$\omega = 2\pi f = 200\pi,$$

$$\Rightarrow \tau \leq 5.2 \times 10^{-4} \text{ s}$$

$$(2) f' = 50 \text{ Hz} \Rightarrow \frac{\omega'}{2\pi} = 50 \Rightarrow \omega' = 100\pi$$

$$\varepsilon_2 = \left| \frac{1}{\sqrt{1+(\omega'\tau)^2}} - 1 \right| \times 100\% = 1.32\%$$

$$\varphi = -\arctan(\omega\tau) = -9.33^\circ$$

