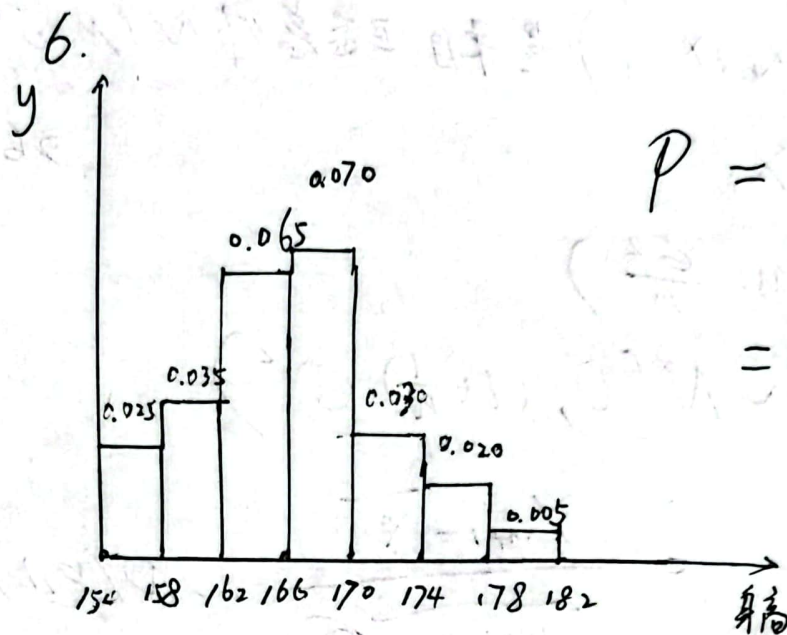
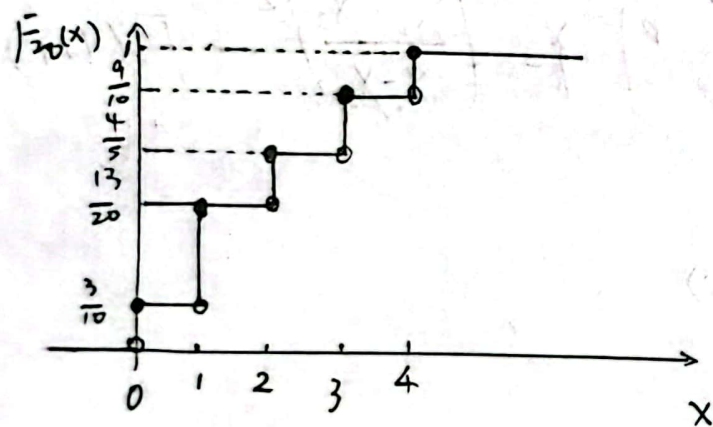


5. 损坏件数

x	0	1	2	3	4
频数	6	7	3	2	2
频率	$\frac{3}{10}$	$\frac{7}{20}$	$\frac{3}{20}$	$\frac{1}{10}$	$\frac{1}{10}$

$$F_{20}(x) = \begin{cases} 0 & x < 0 \\ \frac{3}{10} & 0 \leq x < 1 \\ \frac{13}{20} & 1 \leq x < 2 \\ \frac{4}{5} & 2 \leq x < 3 \\ \frac{9}{10} & 3 \leq x < 4 \\ 1 & 4 \leq x \end{cases}$$



$$p = (0.07 + 0.03 + \frac{0.02}{4} + \frac{0.035}{2}) \times 4 = 0.75$$

17.
$$Y = \frac{1}{\sigma^2} \sum_{i=1}^n (X_i - \mu)^2 = \sum_{i=1}^n \left(\frac{X_i - \mu}{\sigma} \right)^2$$

由于 (X_1, X_2, \dots, X_n) 是来自正态总体 $N(\mu, \sigma^2)$ 的样本, 则 $\frac{X_i - \mu}{\sigma} \sim N(0, 1) \quad (i=1, 2, 3, \dots, n)$

则 $\left(\frac{X_i - \mu}{\sigma} \right)^2 \sim \chi^2(1)$

则 $Y = \sum_{i=1}^n \left(\frac{X_i - \mu}{\sigma} \right)^2 \sim \chi^2(n)$



23. $(X_1, X_2, \dots, X_n, X_{n+1})$ 是来自正态总体 $N(\mu, \sigma^2)$ 的样本.

$$\bar{X} = \frac{1}{n} \sum_{i=1}^n X_i$$

$$\text{则 } \bar{X} \sim N(\mu, \frac{\sigma^2}{n})$$

$$\text{则 } X_{n+1} - \bar{X} \sim N(0, (1 + \frac{1}{n}) \sigma^2)$$

$$\Rightarrow \frac{X_{n+1} - \bar{X}}{\sqrt{(1 + \frac{1}{n}) \sigma^2}} = \frac{X_{n+1} - \bar{X}}{\sqrt{\frac{n+1}{n}} \sigma} \sim N(0, 1)$$

$$\text{由 } S^2 = \frac{1}{n-1} \sum_{i=1}^n (X_i - \bar{X})^2$$

$$\Rightarrow \frac{(n-1) S^2}{\sigma^2} = \sum_{i=1}^n \left(\frac{X_i - \bar{X}}{\sigma} \right)^2 \sim \chi^2(n-1)$$

$$\text{则 } Y = \frac{X_{n+1} - \bar{X}}{\sqrt{\frac{n+1}{n}} \sigma} \bigg/ \sqrt{\frac{(n-1) S^2}{\sigma^2} / (n-1)} \sim t(n-1)$$

$$\text{则 } Y \sim t(n-1)$$

26. (X_1, X_2) 是来自总体 $X \sim N(0, \sigma^2)$ 的样本

$$\text{a) } X_1 + X_2 \sim N(0, 2\sigma^2)$$

$$X_1 - X_2 \sim N(0, 2\sigma^2)$$

$$\text{b) } \frac{X_1 + X_2 - 0}{\sqrt{2} \sigma} \sim N(0, 1)$$

$$\text{a) } \left(\frac{X_1 + X_2}{\sqrt{2} \sigma} \right)^2 \sim \chi^2(1)$$

$$\left(\frac{X_1 - X_2}{\sqrt{2} \sigma} \right)^2 \sim \chi^2(1)$$

$$\text{b) } F = \left(\frac{X_1 + X_2}{X_1 - X_2} \right)^2 \sim F(1, 1)$$

