

GATE 2010 EC, 60th Question Analysis

Question 60

60) What are the minimum numbers of NOT gates and 2-input OR gates required to design the logic of the driver for this 7-segment display?

- (a) 3 NOT and 4 OR
- (b) 2 NOT and 4 OR

(c) 1 NOT and 3 OR

(d) 2 NOT and 3 OR

Correct Answer: (D)

(GATE EC 2009)

Question Analysis:

- Let the 4-bit BCD input be D, C, B, A where A is the LSB.
- Let the output of the required 7-segment driver be F .
- The segment should glow for decimal inputs 0, 2, 3, 5, 6, 7, 8, 9 and remain OFF for 1, 4.
- The canonical SOP expression is $F = \sum m(0, 2, 3, 5, 6, 7, 8, 9)$.
- The don't care conditions are $d = \sum m(10, 11, 12, 13, 14, 15)$.
- After Karnaugh map simplification, the minimized expression is $F = A + B + \overline{C} + \overline{D}$.
- For NOT gates, \overline{C} and \overline{D} are required.
- For OR gates, the implementation can be written as $F = (A + B) + (\overline{C} + \overline{D})$.
- Hence, the minimum requirement is 2 NOT gates and 3 two-input OR gates.

Required Components & Pin Connections

S.No	Component	Component	Arduino Pin
1	Arduino Uno Board	Output a (seg a)	Digital 2
2	Breadboard	Output b (seg b)	Digital 3
3	Seven segment (1)	Output c (seg c)	Digital 4
4	Resistors: 220Ω (1)	Output d (seg d)	Digital 5
5	Jumper Wires	Output e (seg e)	Digital 6
6	USB Cable	Output f (seg f)	Digital 7
		Output g (seg g)	Digital 8
		GND	GND
		VCC	5V

Logic Description

- Let the 4-bit BCD inputs be D, C, B, A .
- Initialize the inputs as $D = 0, C = 0, B = 0, A = 0$.
- Let the output of the required 7-segment driver be F .
- From the experimental truth table, the segment should glow for 0, 2, 3, 5, 6, 7, 8, 9 and remain OFF for 1, 4.
- The canonical expression obtained from the truth table is $F = \sum m(0, 2, 3, 5, 6, 7, 8, 9)$.
- The don't care conditions are $d = \sum m(10, 11, 12, 13, 14, 15)$.
- After Karnaugh map simplification, the minimized output expression is $F = A + B + C' + D'$.
- Implement the logic using two NOT operations to generate C' and D' .
- Combine the terms using three two-input OR gates as $F = (A + B) + (C' + D')$.
- Change the inputs as per the truth table and observe the segment display.
- The segment glows when $F = 1$ and remains OFF when $F = 0$.

Code Uploading Steps

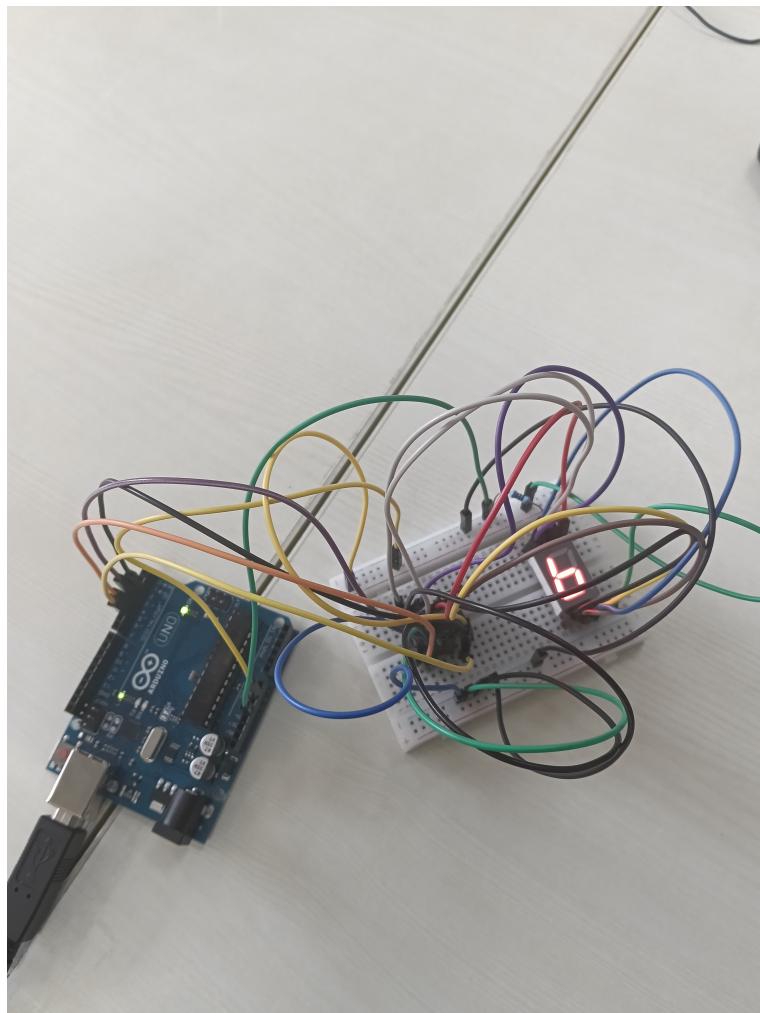
- Create a Platform IO project
- Write the code in main.cpp in src
- Run the PIO project with command "pio run". It will compile the code and create .hex file
- Copy the .hex file to ArduinoDroid folder
- Connect the Arduino UNO to mobile with OTG cable
- Upload the hex file using "upload precompiled" option
- Observe the output and verify the expression

Hardware Implementation

The above problem is implemented and tested in hardware using Arduino UNO board. Here we used a seven segment display, and inputs A B C D to display output F is 1 or 0 as per truth table and verified the expression.

Experimental Truth Table

Decimal	D	C	B	A	F (Output)
0	0	0	0	0	1
1	0	0	0	1	0
2	0	0	1	0	1
3	0	0	1	1	1
4	0	1	0	0	0
5	0	1	0	1	1
6	0	1	1	0	1
7	0	1	1	1	1
8	1	0	0	0	1
9	1	0	0	1	1
10	1	0	1	0	X
11	1	0	1	1	X
12	1	1	0	0	X
13	1	1	0	1	X
14	1	1	1	0	X
15	1	1	1	1	X



Conclusion

- From the experimental truth table, $F = 1$ for decimal inputs 0, 2, 3, 5, 6, 7, 8, 9 and $F = 0$ for 1, 4.
- The minimized Boolean expression obtained is $F = A + B + C' + D'$.
- The logic implementation requires 2 NOT gates and 3 two-input OR gates.
- This matches option (D) from the original GATE question.
- The hardware experiment confirms the theoretical logic of the 7-segment driver.