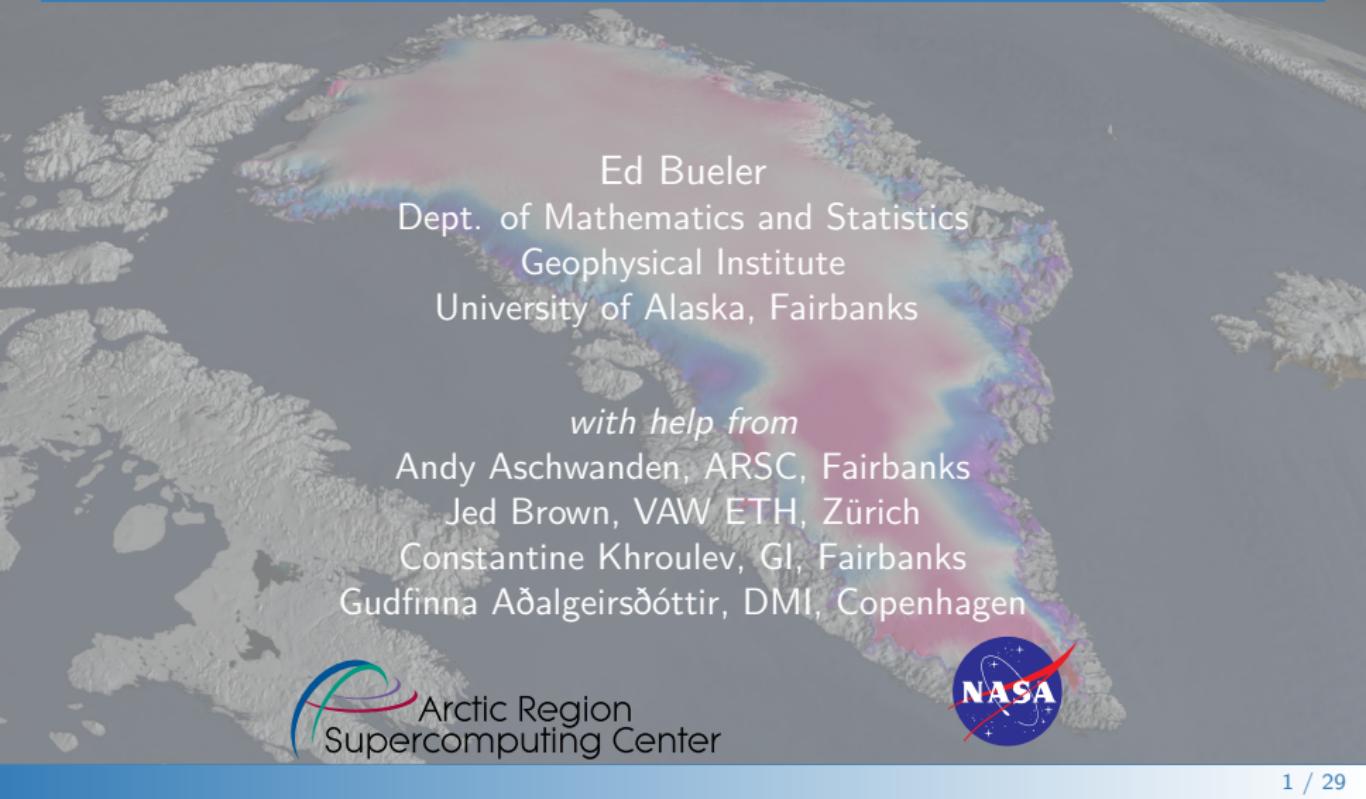


Greenland ice sheet flow computations

scaling-up to high spatial resolution and fast boundary processes



Ed Bueler
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with help from
Andy Aschwanden, ARSC, Fairbanks
Jed Brown, VAW ETH, Zürich
Constantine Khroulev, GI, Fairbanks
Gudfinna Aðalgeirsðóttir, DMI, Copenhagen



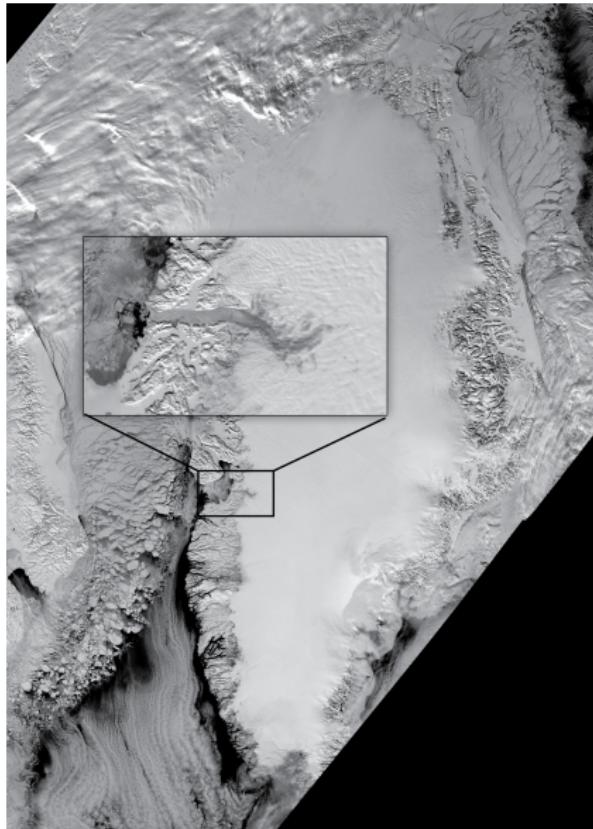
Outline

why compute Greenland's flow?

ice sheets: modeling and observations

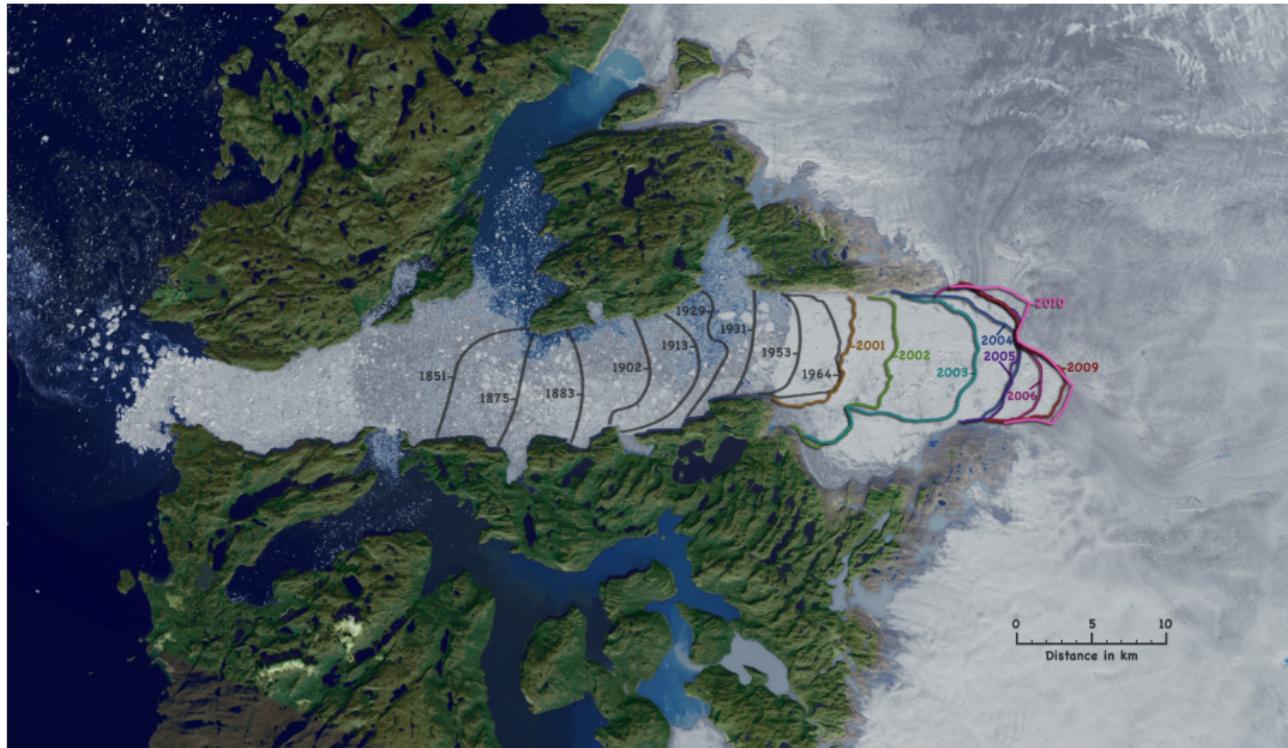
scaling-up: how to get more ISM from HPC

Jakobshavn Isbræ, west Greenland



*MODIS image
M. Fahnestock*

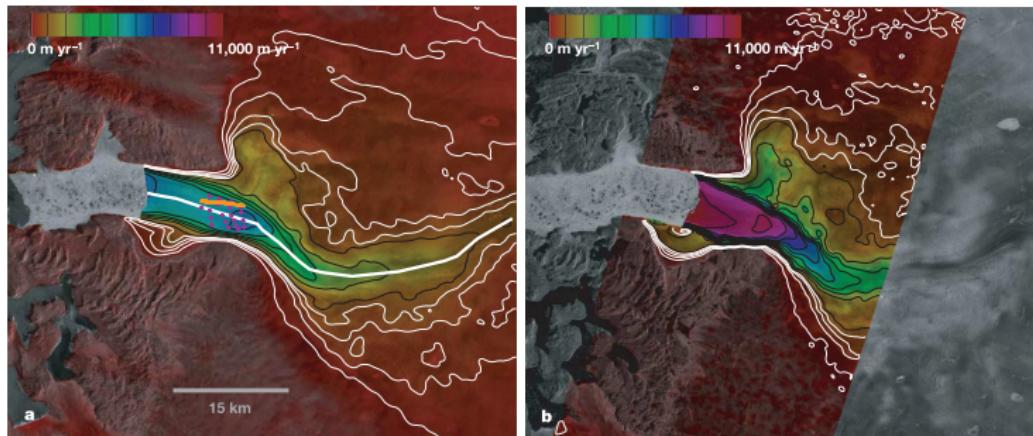
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NASA/Goddard Space Flight Center Scientific Visualization Studio

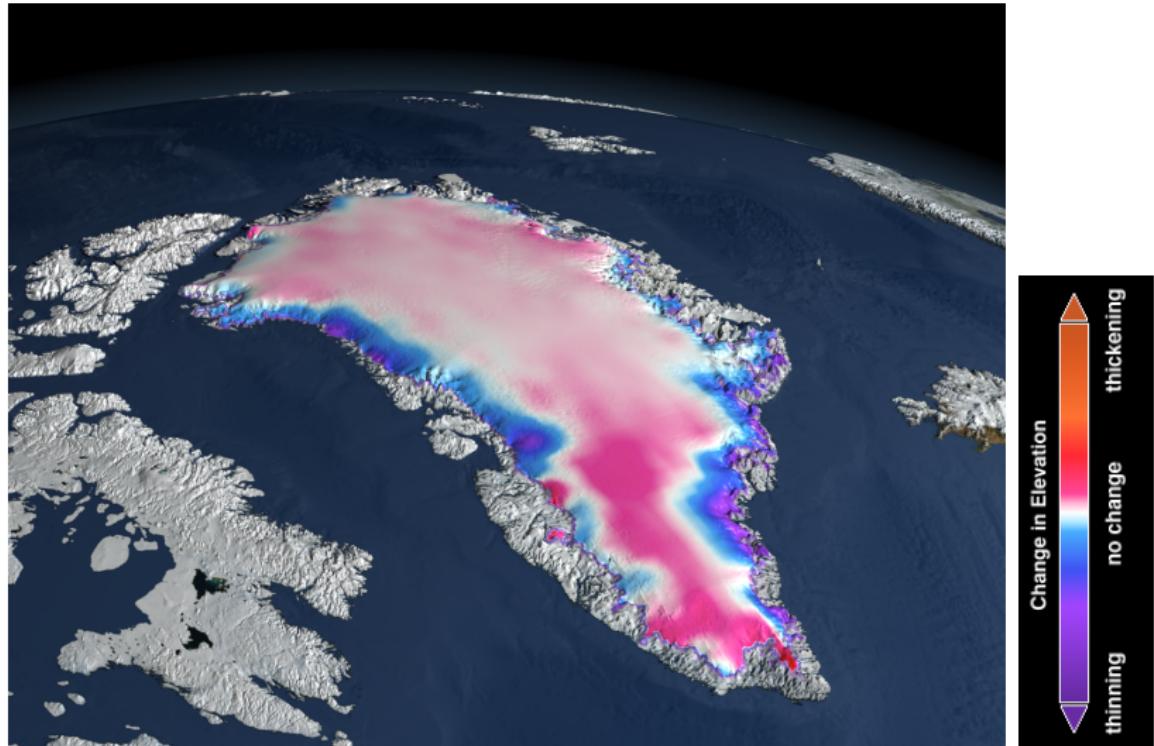
Speed-up of Jakobshavn Isbræ

- ▶ almost doubled its flow speed between the 1992 and 2000:
 - ▷ probably started by increase in ocean temperature from 1.7 C° in 1995 to 3.3 C° in 1998
 - ▷ ... thus increased melting under floating tongue
 - ▷ loss of floating tongue and its “backpressure” on upstream grounded ice
 - ▷ speed-up of grounded ice
- ▶ now drains about 7% of the entire ice sheet



Joughin et al. (2004)

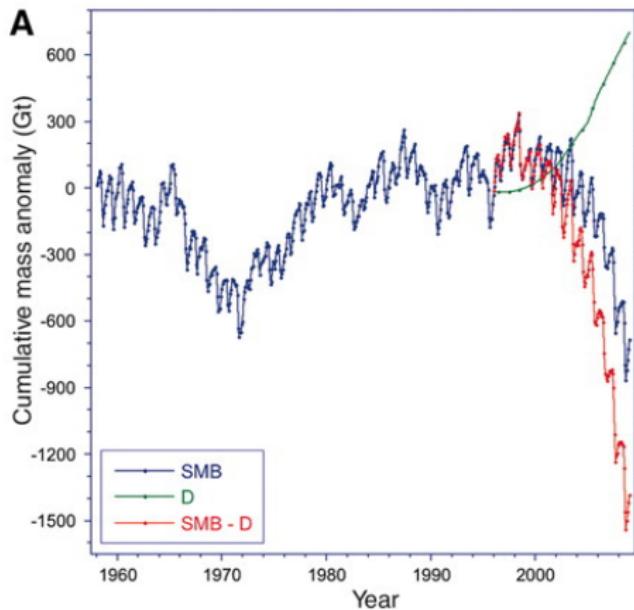
Elevation changes: surface melt and “discharge”



*IceSAT observations over 2003–2006 period; NASA/Goddard Space Flight Center
Scientific Visualization Studio*

The future of Greenland is the question

- ▶ before mid-90s mass loss was dominated by surface mass balance (= precipitation minus surface melt/runoff)
- ▶ since 2000, mass balance has been persistently negative
 - ▷ decrease in surface mass balance (**more melting beats more precipitation**)
 - ▷ increase in discharge (**calving**) from ice flow
- ▶ future mass loss partitioning: **unknown**
- ▶ models need to predict which climate changes have which effects



van den Broeke et al. (2009)

Why Greenland?

- ▶ its changes affect future sea level rise
 - ▷ 7 m rise if completely melted ... unlikely ... is 1 or 2 m likely?
- ▶ observations over the past decades show:
 - ▷ rapid acceleration of outlet glaciers
 - ▷ thinning around the margin
 - ▷ increased mass loss
- ▶ it's a testbed for ice sheet modeling:
 - ▷ recent observational attention: lots of flights, ground measurements
 - ▷ exhibits the kind of worrying dynamics we want to "explain"
 - ▷ Antarctic ice sheet has 10× the area thus 10× the cost



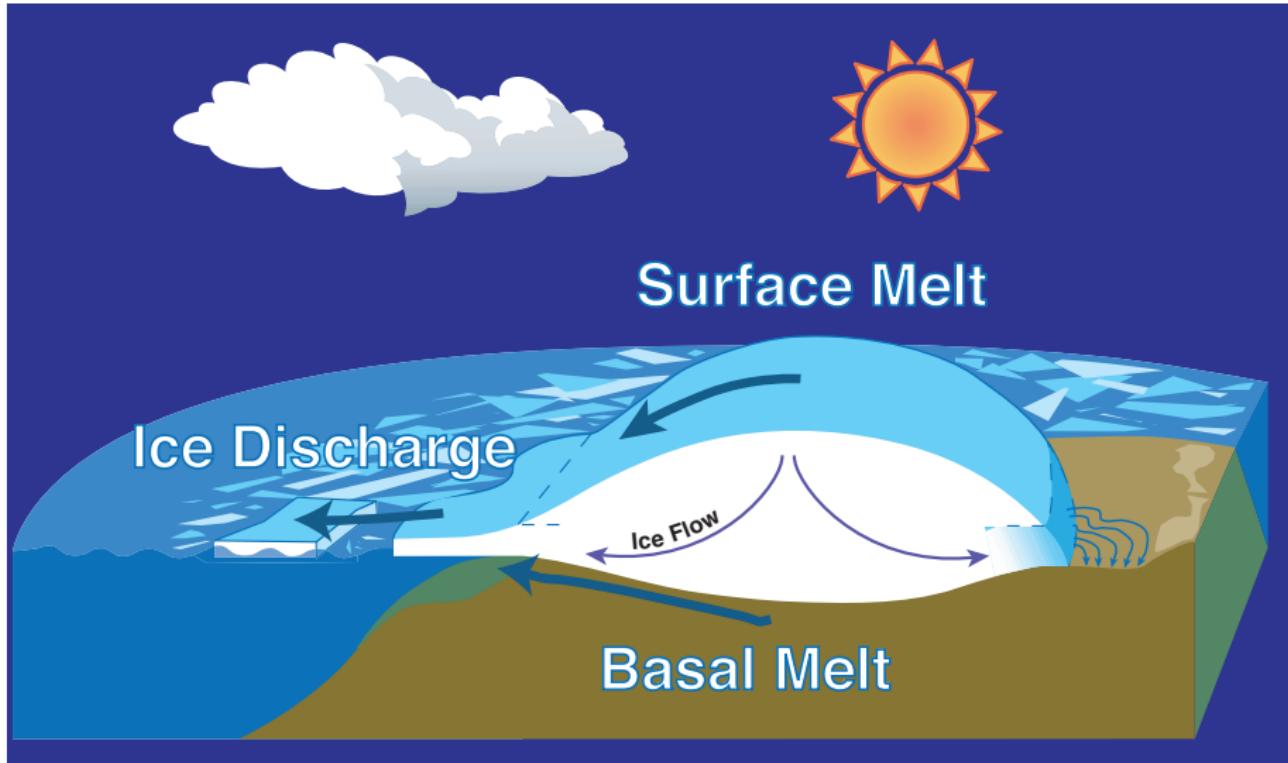
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How does an ice sheet lose mass?



modified from ICESat brochure

IPCC and ice sheet models

IPCC (2007), Box 4.1: Ice Sheet Dynamics and Stability

“...but recent changes in ice sheet margins and ice streams cannot be simulated accurately with these models, . . .”

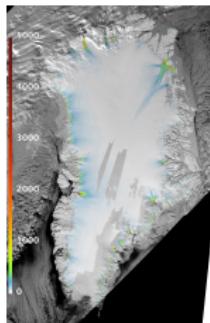
- ▶ IPCC = Intergovernmental Panel on Climate Change
= {2007 Nobel Peace Prize winners} \ {Al Gore}
- ▶ above statement \implies lots of attention from modelers

progress report 2011:

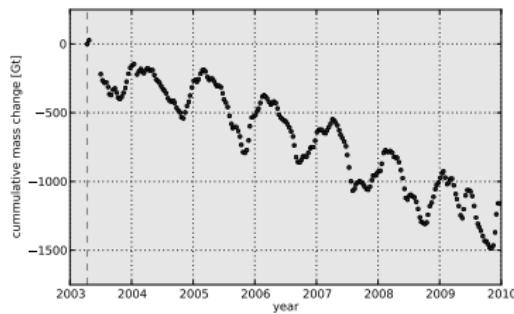
- ▶ PISM is doing a decent job reproducing the past two decades
 - ▷ before anything else, get the present, observed period right!
 - ▷ model validation

Ice sheet model validation using

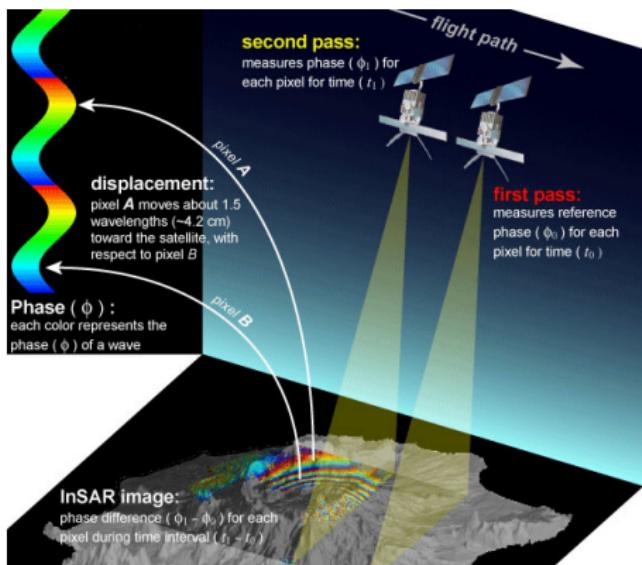
- ▶ observed mean flow speed from 2000, 2006–2008 (InSAR)



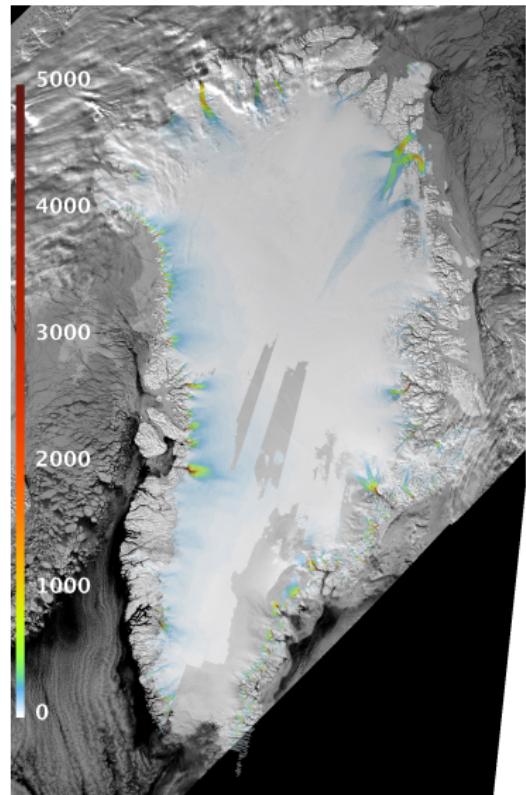
- ▶ observed cumulative mass change from 2003–2009 (GRACE)



Flow speed from InSAR

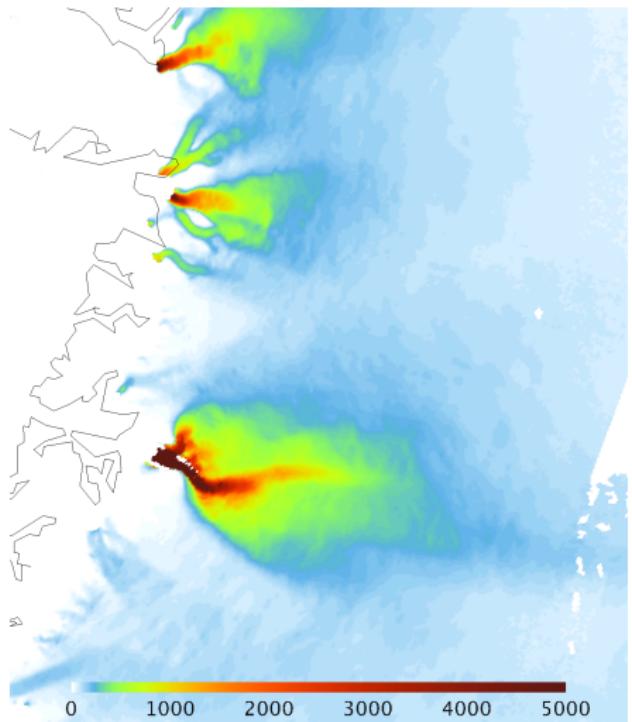


credit: USGS

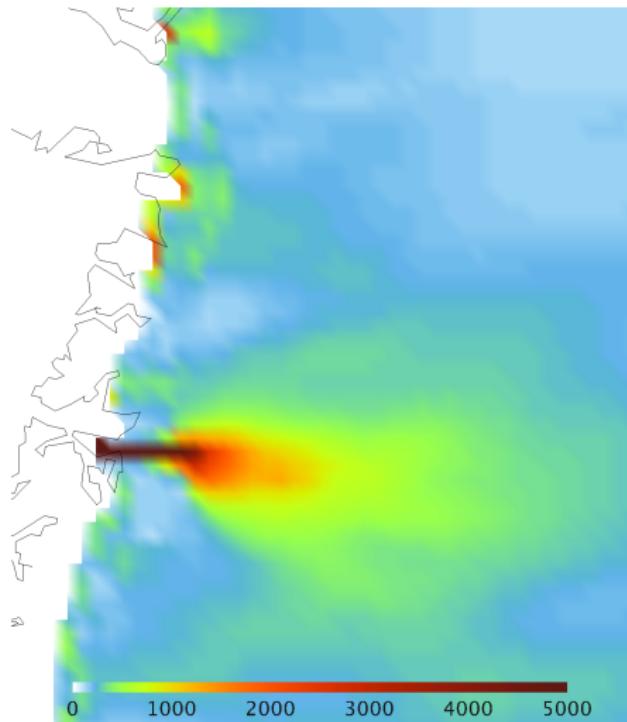


credit: I. Joughin

Results: Jakobshavn Isbræ

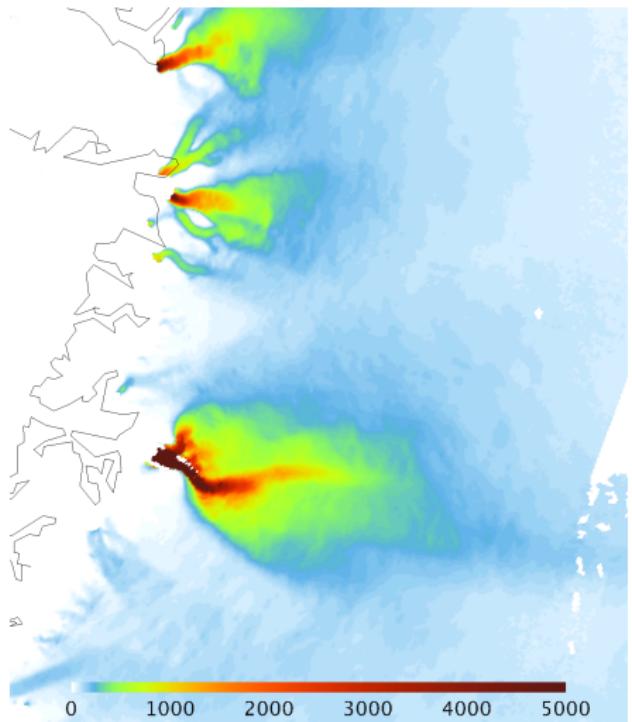


InSAR (*Joughin et al., 2010*)

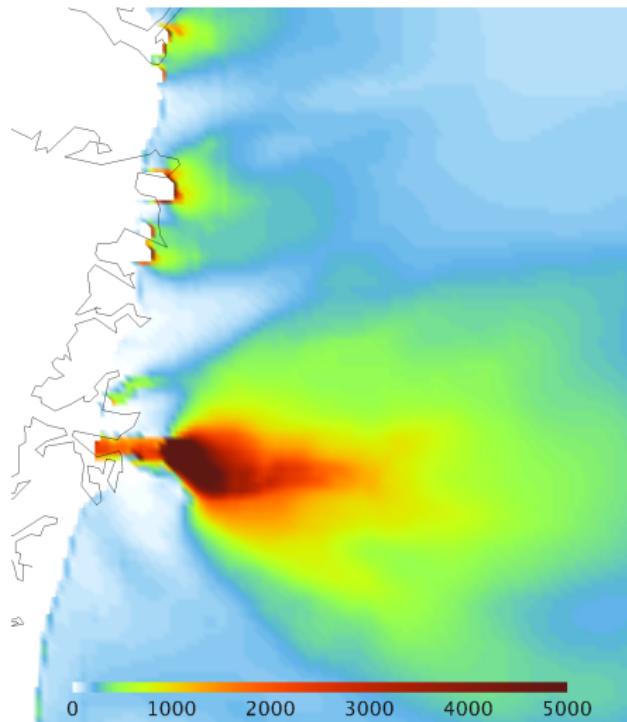


PISM: 5 km grid resolution

Results: Jakobshavn Isbræ

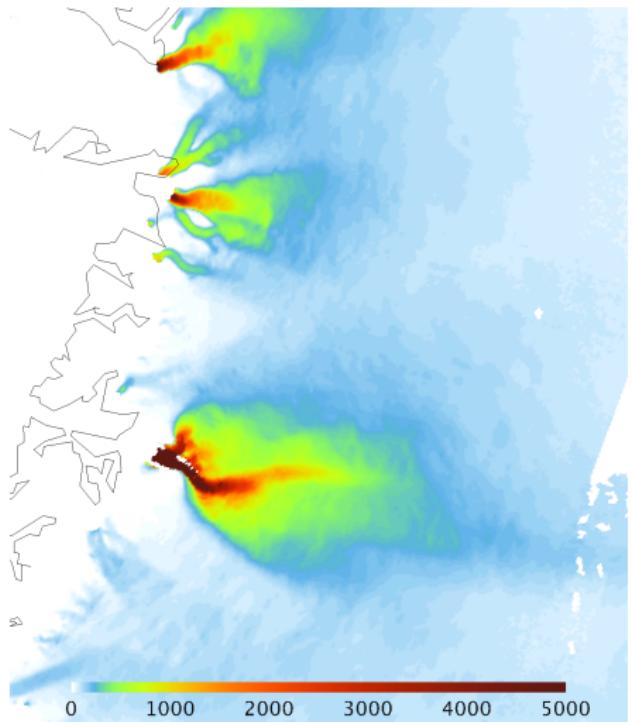


InSAR (*Joughin et al., 2010*)

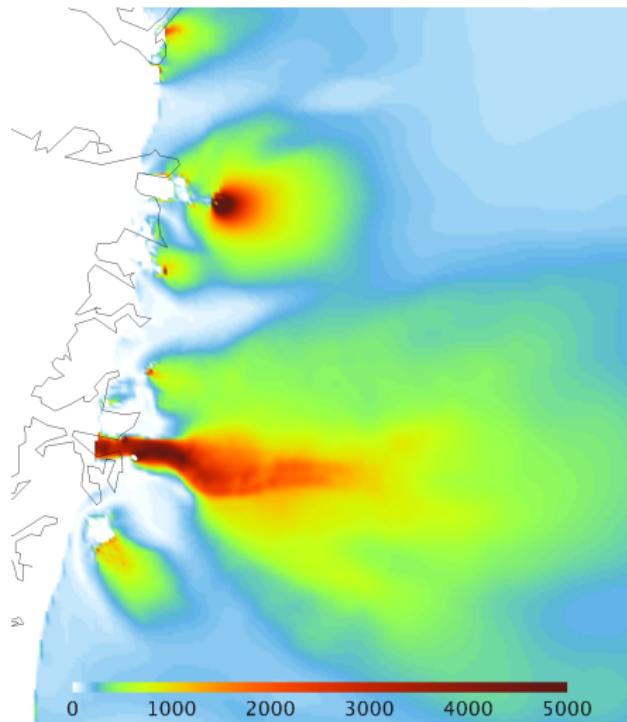


PISM: 2 km grid resolution

Results: Jakobshavn Isbræ

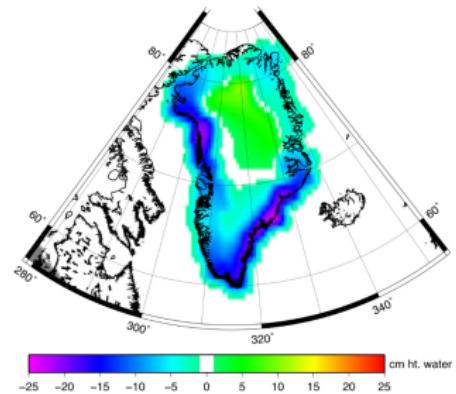
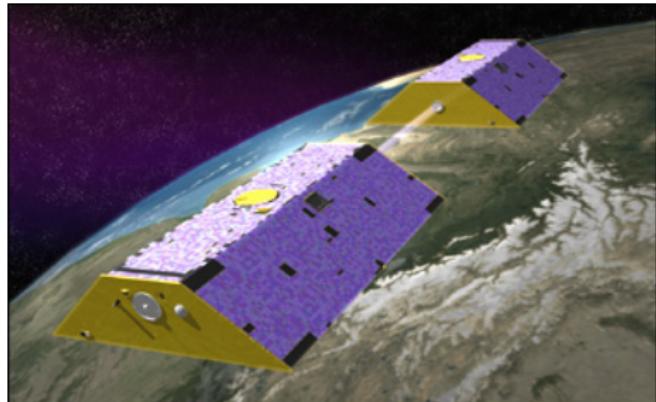


InSAR (*Joughin et al., 2010*)



PISM: 1 km grid resolution

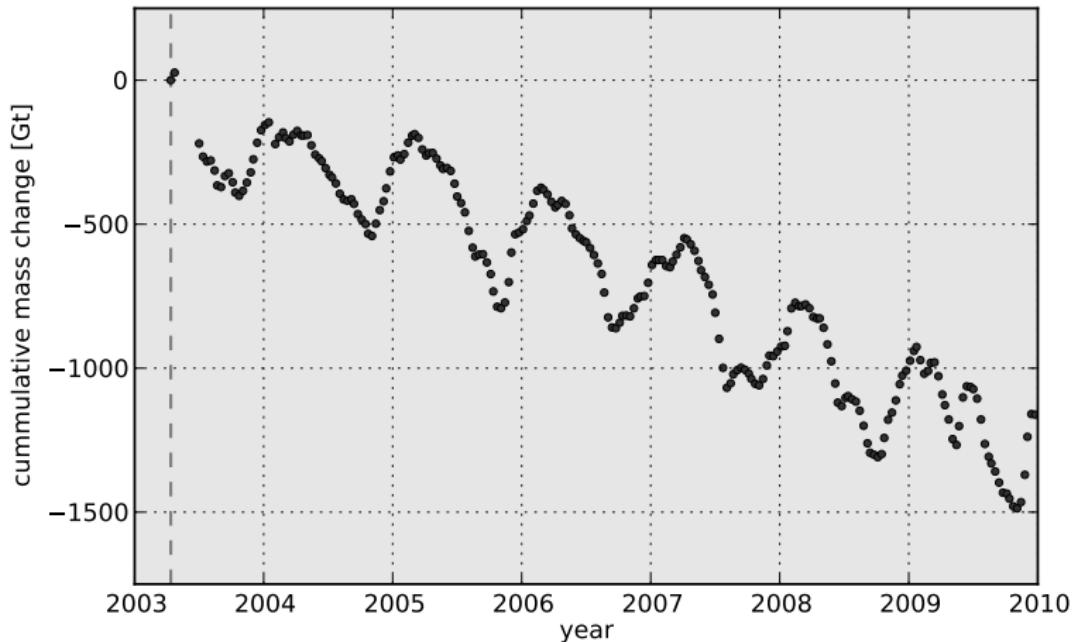
Gravity Recovery and Climate Experiment (GRACE)



thanks to A. Arendt

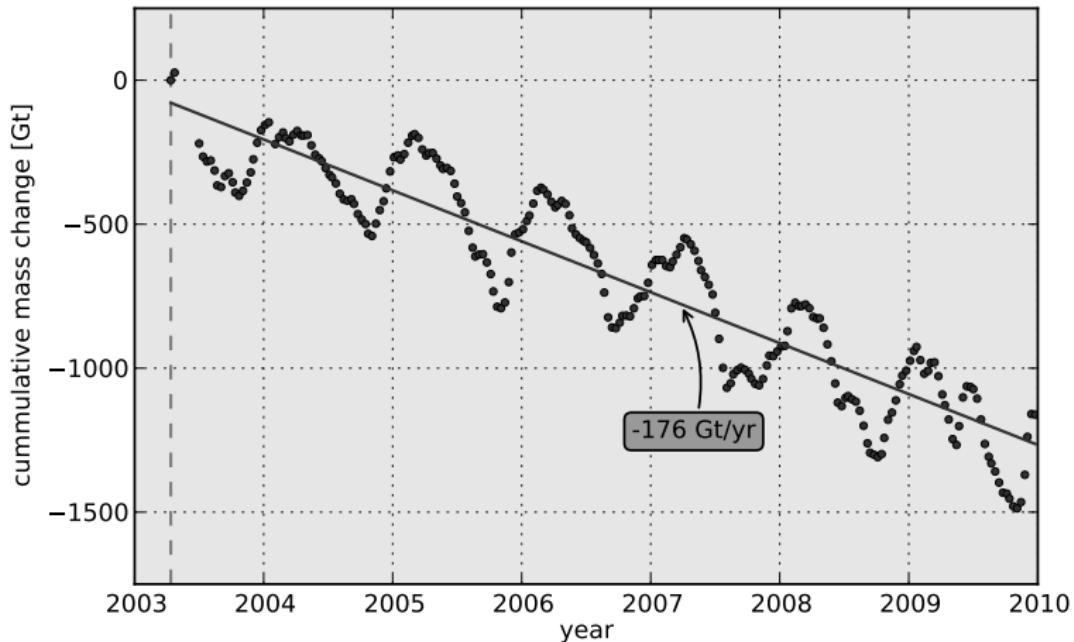
- ▶ precisely measures distance between pair of satellites
- ▶ estimates deviation of gravity field from uniform sphere shape

Observed mass changes



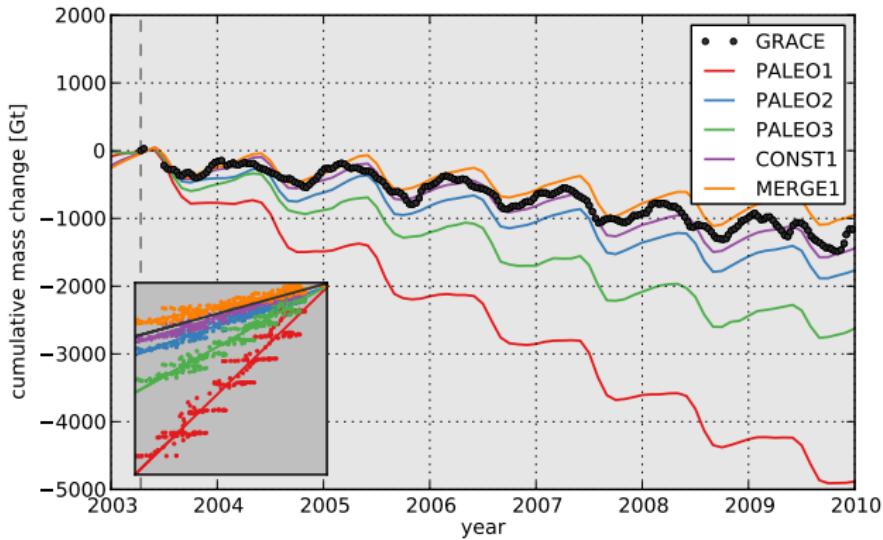
Luthcke, et al. (unpublished; new high-resolution solutions)

Observed mass changes



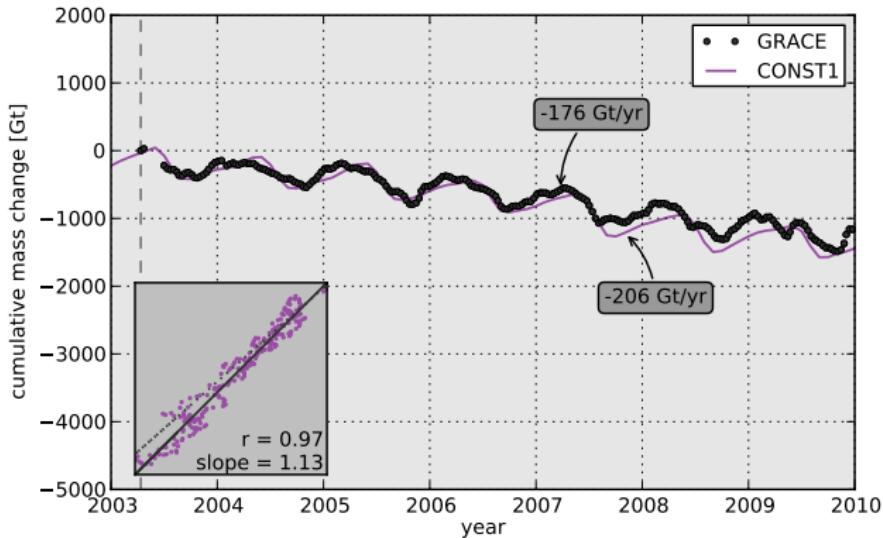
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Modeled and observed mass changes



- ▶ new coupled models of Greenland
 - ▷ PISM + regional climate model (HIRHAM at DMI Copenhagen)

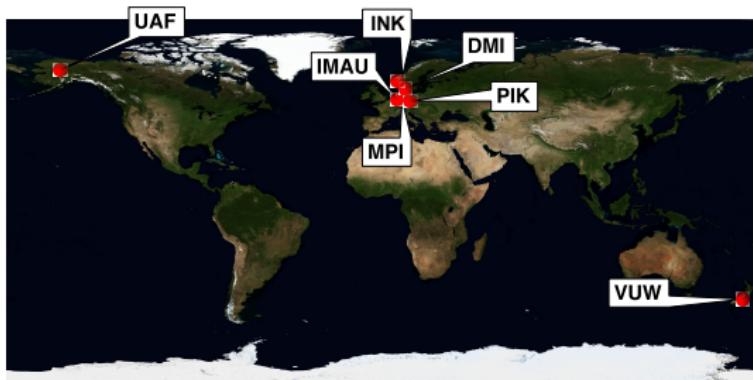
Modeled and observed mass changes



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What is PISM?

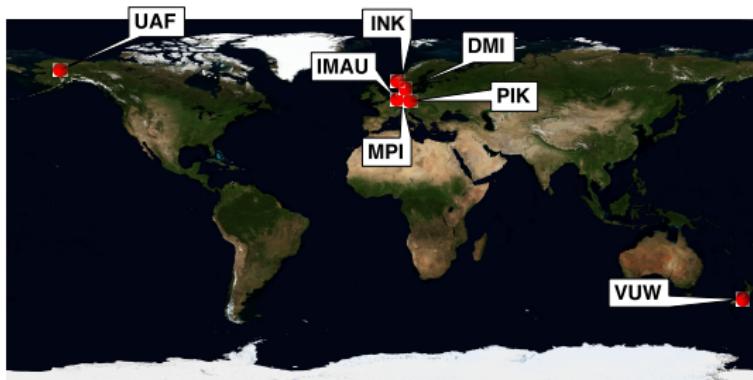
- ▶ PISM = Parallel Ice Sheet Model www.pism-docs.org
- ▶ open source (C++, python), PETSc-over-MPI, regular grid
- ▶ adaptive time-stepping
- ▶ supported by NASA; now a joint project with PIK in Germany
- ▶ the best ice sheet model in the world
- ▶ ... was developed in Fairbanks



user base:

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user base:

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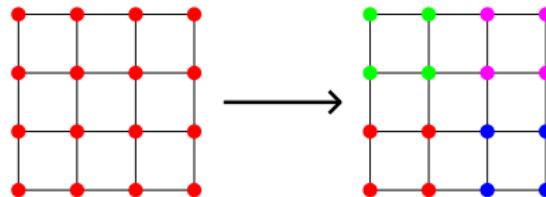
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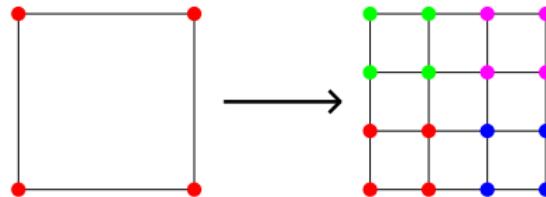
scaling-up: how to get more ISM from HPC

Scaling

- ▶ plan for the rest of my talk: beat up PISM because it scales badly
- ▶ ... though it scales way better than any other current ISM
- ▶ definitions in convenient 2D grid case:
 - ▷ **strong scaling:** for fixed problem,
 $4 \times$ the number of processors \Rightarrow (1/4)th the execution time



- ▷ **weak scaling:** for fixed number of d.o.f.s *per processor*,
 $4 \times$ the number of processors \Rightarrow *same* execution time



Min prerequisite for weak scaling: convergence

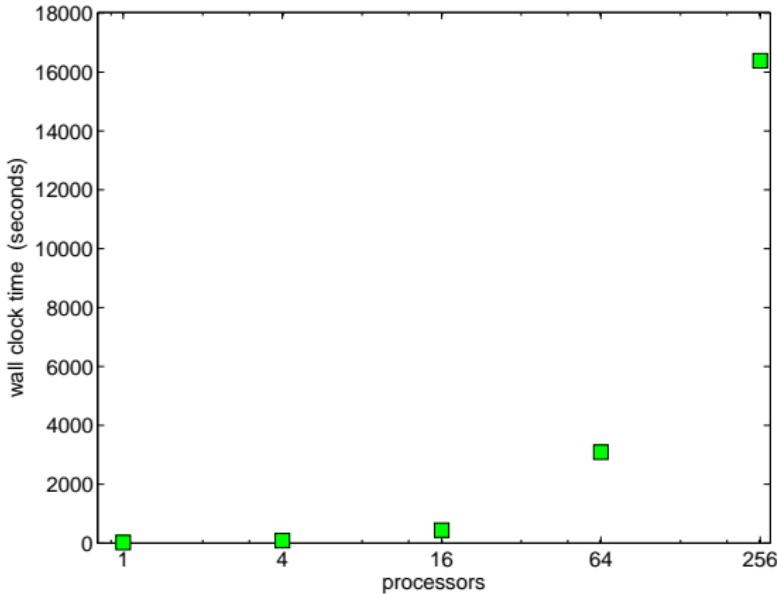
- ▶ six runs, each 100 model year with same data
- ▶ on refining grids: 40, 20, 10, 5, 2.5 km
- ▶ surface velocity (m/year) →
- ▶ my first informal study
- ▶ results:

res	procs	wall clock
40 km	1	8 sec
20 km	1	75 sec
10 km	64	57 sec
5 km	64	14 min
3 km	128	56 min
2 km	128	285 min

- ▶ on Cray XT5
 - ▷ pingo.arsc.edu

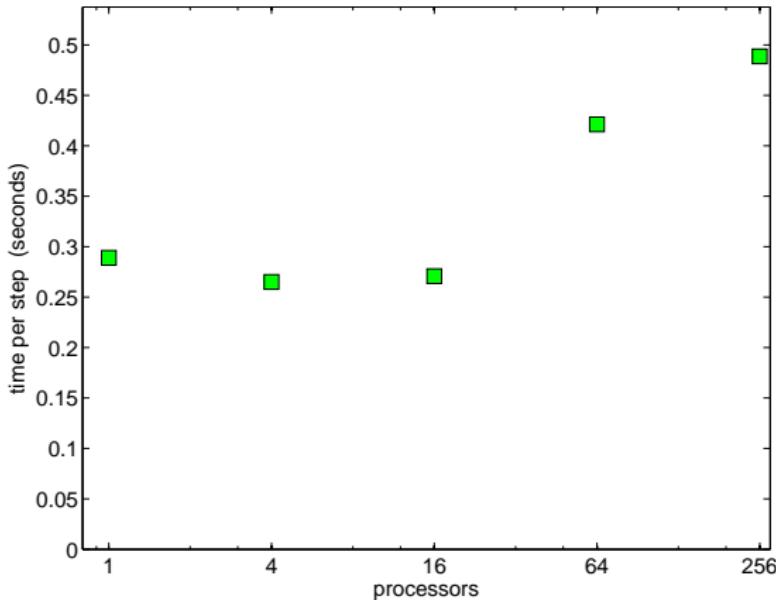
Weak scaling: the reality

- ▶ here's the problem →
 - ▷ 100 model year runs
 - ▷ increase d.o.f.s and processors in proportion
 - ▶ a la weak scaling
 - ▷ it is **not** giving constant-time for whole run
 - ▷ it is giving constant-time per model time step
 - ▶ but who cares
- ▶ we observe: short time steps on fine grids blocks weak scaling



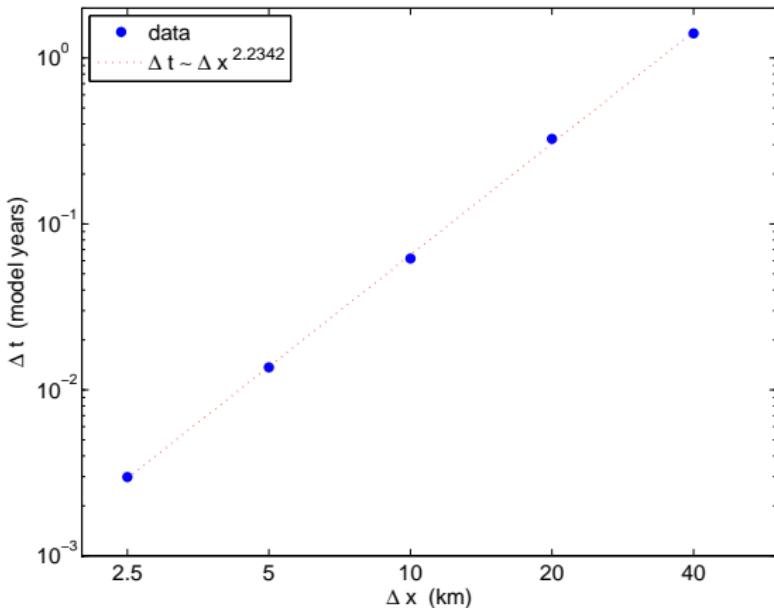
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Weak scaling: the troubles

1 PISM evolves temperature and geometry by explicit time-stepping

- ▷ major evolution equation is wildly-nonlinear diffusion
- ▷ ice thickness H changes by

$$\frac{\partial H}{\partial t} \doteq \nabla \cdot (CH^5 |\nabla H|^2 \nabla H)$$

- ▷ explicit method scales badly because

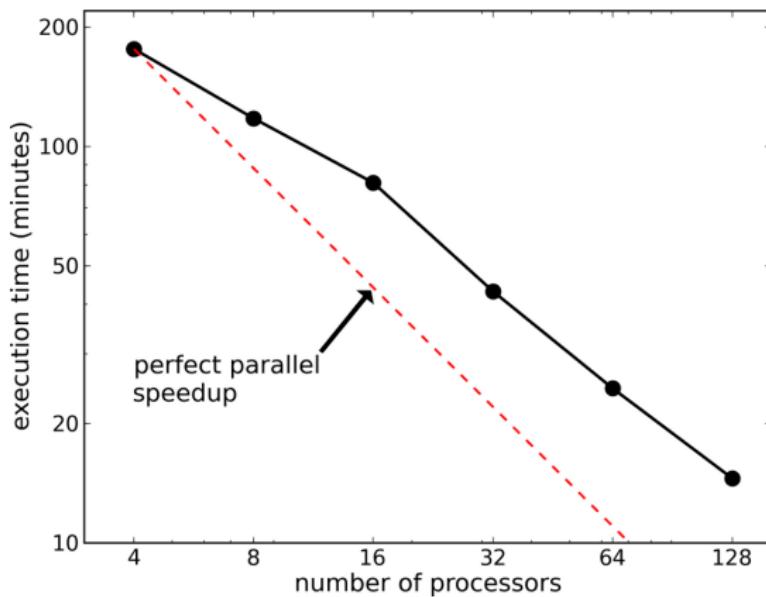
$$\Delta t \sim \Delta x^2$$

- ▷ *implicit time steps, you idiot!*
- ▷ but we are not solving PDEs; boundary value problem is * subject to inequality

$$H \geq 0$$

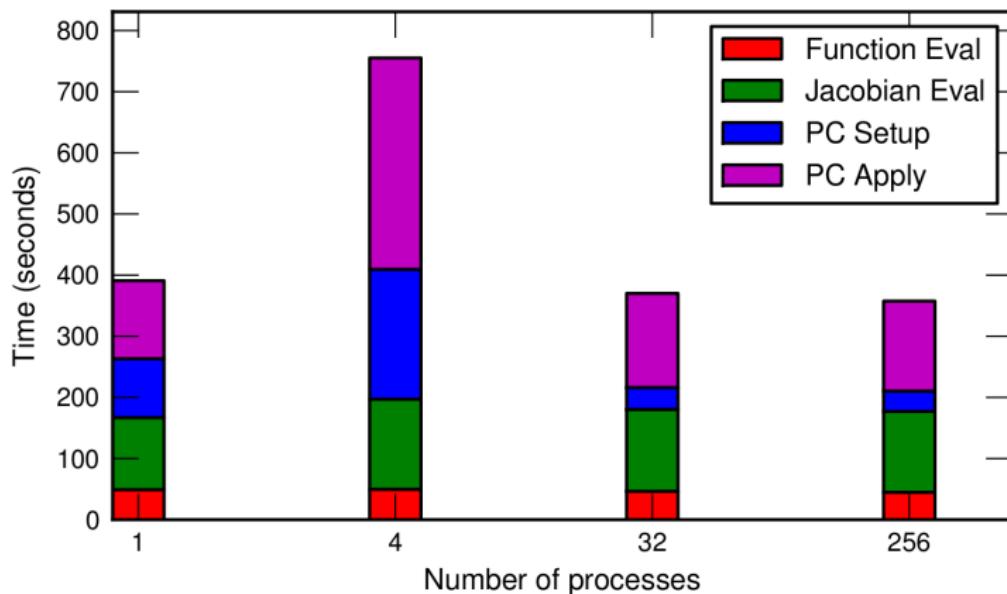
- ▷ so we don't really know how to solve well-posed implicit time steps

Scaling: results so far; idealized ice sheets



- ▶ PISM: strong scaling on time-dependent run including many 2D stress solutions
- ▶ Jed Brown's hydrostatic ice solver [*submitted 2011*]: awesome weak scaling on time-independent 3D stress solver; *not yet in PISM!*

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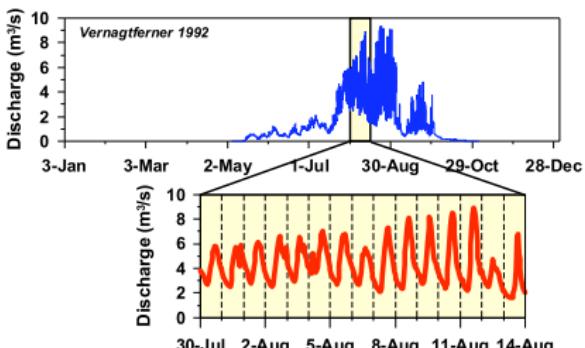
Weak scaling: the troubles

2 liquid water at boundaries

- ▷ big lakes form and drain . . . in 90 minutes (upper)
- ▷ hydrograph shows brief summer period of surface melt (lower)
- ▷ ice flow model must “see” liquid runoff at surface *and* its effect on subglacial resistance
 - ▶ boundary liquid timescales are minutes–weeks
 - ▶ ice sheet model runs are decades–millenia



S. Das

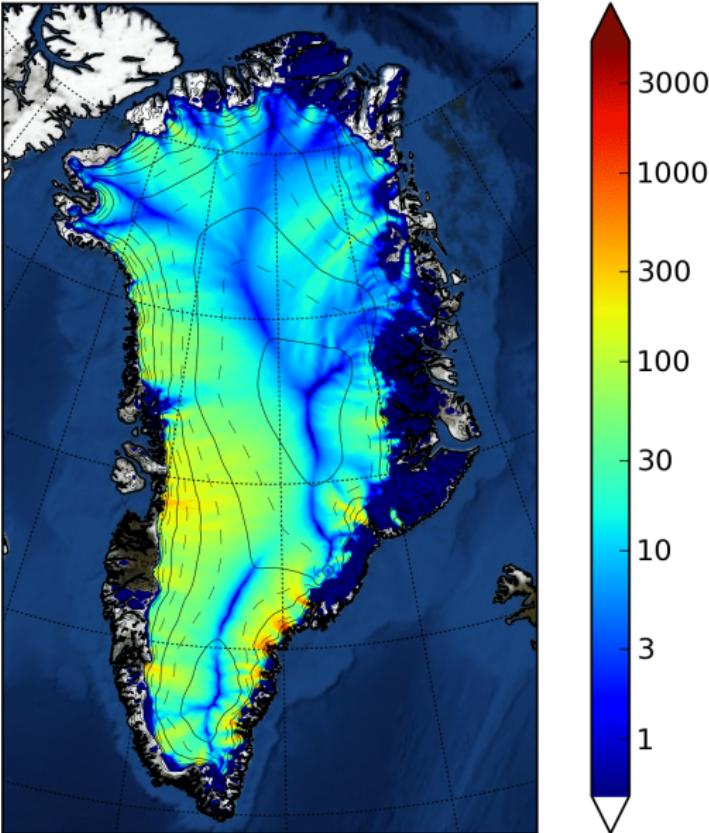


R. Hock et al. (2005)

Weak scaling: the troubles

3 solve PDEs on domain with fractal boundary

- ▷ velocity is big near the boundary
- ▷ boundary is a [coastline](#)
... Mandelbrot warned us about those things
- ▷ at each timestep, want to solve nonlinear elliptic problems on this fractal



Summary

- ▶ model Greenland ice sheet flow! it is on the move!
- ▶ PISM is getting good fit to observed flow speeds, mass changes
- ▶ challenges to scaling:
 - ▷ equations need new thinking
 - need well-posed implicit time steps
 - and better solvers too
 - ▷ short time-scale processes on all ice sheet surfaces
 - liquid water
 - ▷ fast ice dynamics along fractal boundaries
- ▶ much bigger Antarctic ice sheet in the background
- ▶ thanks for your attention!