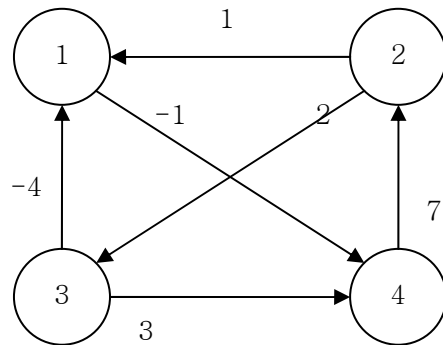


## Analysis of Algorithms

Final Exam: 9 June 2003

1. Suppose that B-Tree-Search is implemented to use binary search rather than linear search within each node. Show that this change makes the CPU time required  $O(\log n)$ , independently of how  $t$  might be chosen as a function of  $n$ .
2. Write a nonrecursive version of Find-Set( $x$ ) with path compression. (The parent of  $x$  is denoted by  $p[x]$ .)
3. Give a counterexample to the conjecture that if there is a path from  $u$  to  $v$  in a directed graph  $G$ , then any depth-first search must result in  $d[v] \leq f[u]$ . ( $d[v]$  and  $f[v]$  denote the discovery time and finish time of  $v$ , respectively.)
4. Run the Floyd-Warshall algorithm on the following graph. Show the matrix  $D^{(k)}$  (i.e.,  $D^{(0)}$ , ...,  $D^{(4)}$ ).



5. Give an efficient push-relabel algorithm to find a maximum matching in a bipartite graph. Analyze your algorithm.
6. Write the definition of NP-completeness and explain how to prove that a problem is NP-complete.

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