Binary Tree Traversals

Data structures
Fall 2018

Binary Tree Traversal

- Many binary tree operations are done by performing a traversal of the binary tree.
- In a traversal, each element of the binary tree is visited exactly once.
- During the visit of an element, all action (make a clone, display, evaluate the operator, etc.) with respect to this element is taken.

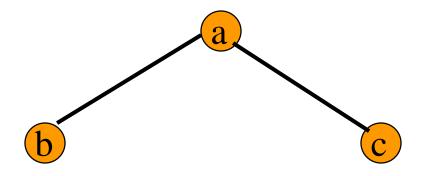
Binary Tree Traversal Methods

- Preorder
- Inorder
- Postorder
- Level order

Preorder Traversal

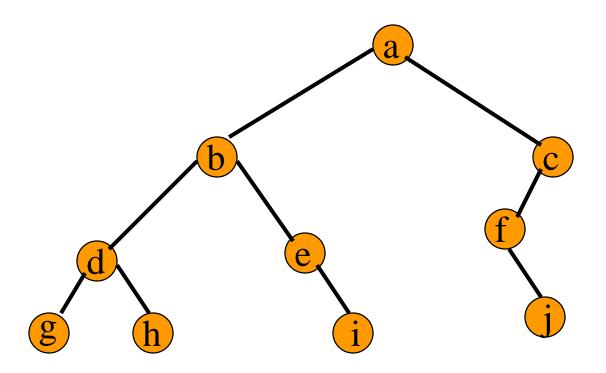
```
public static void preOrder(BinaryTreeNode t)
   if (t != null)
     visit(t);
     preOrder(t.leftChild);
     preOrder(t.rightChild);
```

Preorder Example (visit = print)



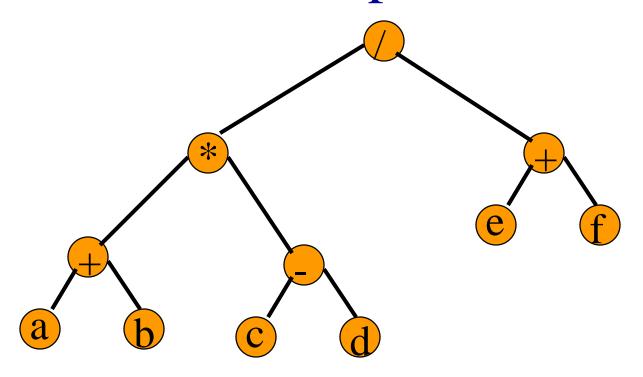
a b c

Preorder Example (visit = print)



abdgheicfj

Preorder Of Expression Tree



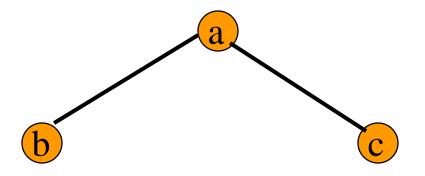
$$/ * + a b - c d + e f$$

Gives prefix form of expression!

Inorder Traversal

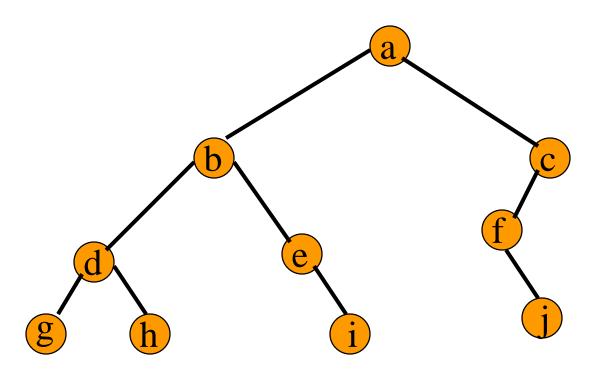
```
public static void inOrder(BinaryTreeNode t)
   if (t != null)
     inOrder(t.leftChild);
     visit(t);
     inOrder(t.rightChild);
```

Inorder Example (visit = print)



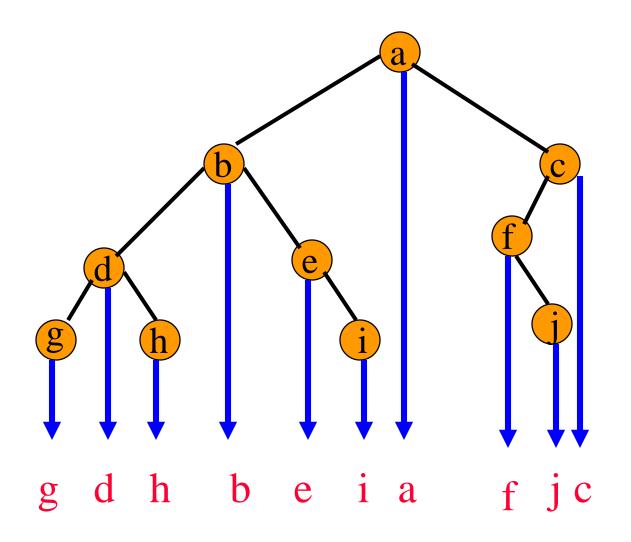
bac

Inorder Example (visit = print)

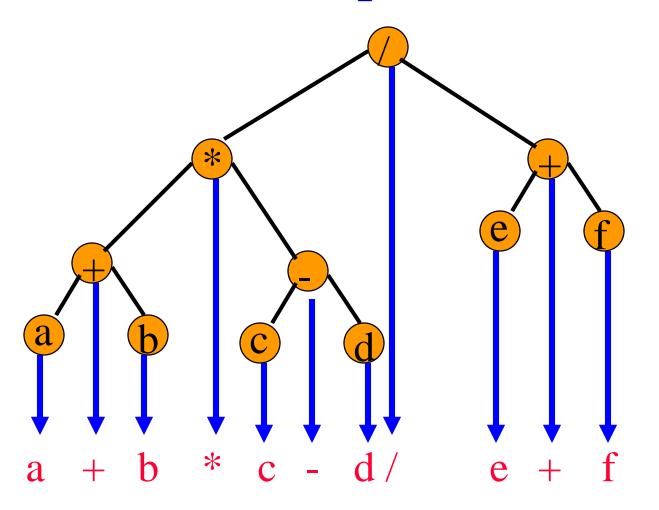


gdhbeiafjc

Inorder By Projection (Squishing)



Inorder Of Expression Tree

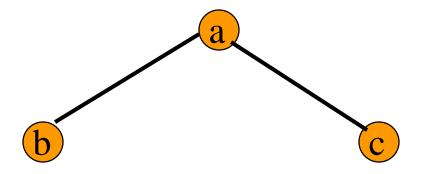


Gives infix form of expression (sans parentheses)!

Postorder Traversal

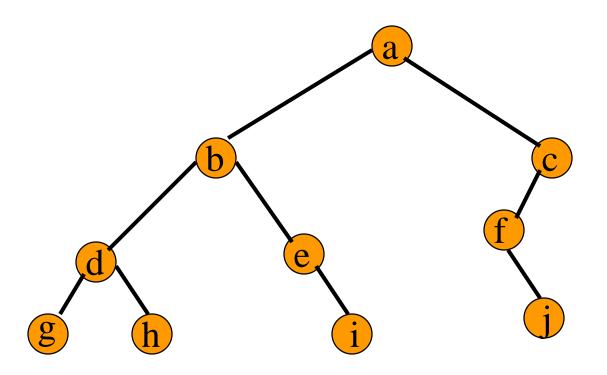
```
public static void postOrder(BinaryTreeNode t)
   if (t != null)
     postOrder(t.leftChild);
     postOrder(t.rightChild);
     visit(t);
```

Postorder Example (visit = print)



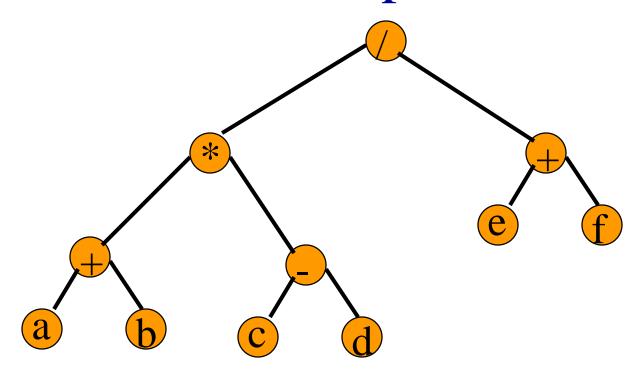
b c a

Postorder Example (visit = print)



ghdiebjfca

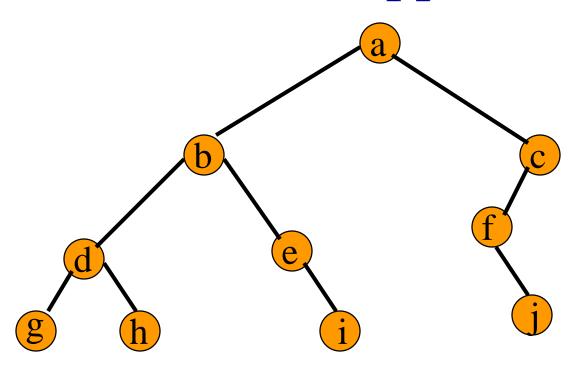
Postorder Of Expression Tree



$$a b + c d - * e f + /$$

Gives postfix form of expression!

Traversal Applications

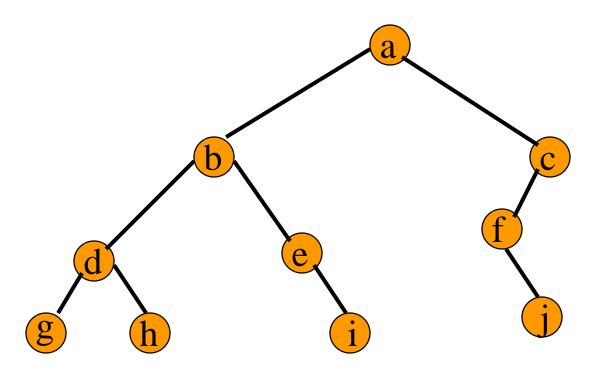


- Make a clone.
- Determine height.
- •Determine number of nodes.

Level Order

```
Let t be the tree root.
while (t != null)
  visit t and put its children on a FIFO queue;
  remove a node from the FIFO queue and
  call it t;
  // remove returns null when queue is empty
```

Level-Order Example (visit = print)



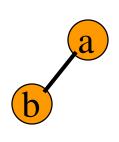
abcdefghij

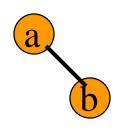
Binary Tree Construction

- Suppose that the elements in a binary tree are distinct.
- Can you construct the binary tree from which a given traversal sequence came?
- When a traversal sequence has more than one element, the binary tree is not uniquely defined.
- Therefore, the tree from which the sequence was obtained cannot be reconstructed uniquely.

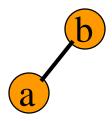
Some Examples

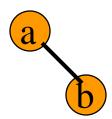
preorder
= ab
inorder



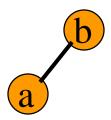


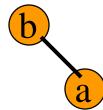
= ab



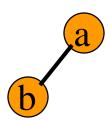


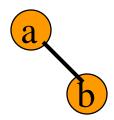
postorder = ab





level order = ab





Binary Tree Construction

- Can you construct the binary tree, given two traversal sequences?
- Depends on which two sequences are given.

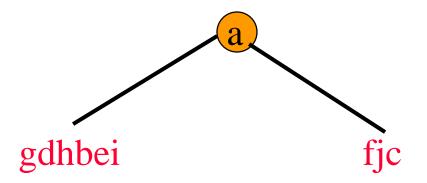
Preorder And Postorder

preorder = ab
postorder = ba
b

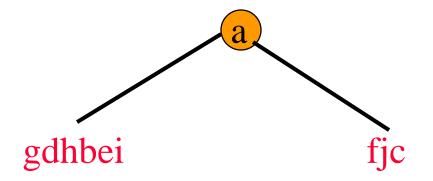
- Preorder and postorder do not uniquely define a binary tree.
- Nor do preorder and level order (same example).
- Nor do postorder and level order (same example).

Inorder And Preorder

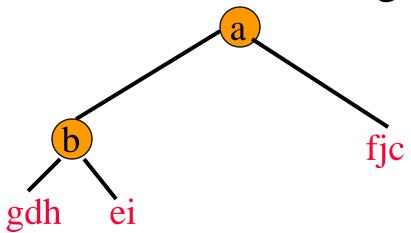
- inorder = g d h b e i a f j c
- preorder = a b d g h e i c f j
- Scan the preorder left to right using the inorder to separate left and right subtrees.
- a is the root of the tree; gdhbei are in the left subtree; fjc are in the right subtree.



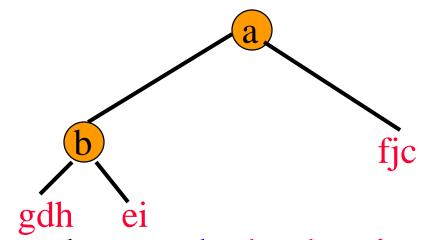
Inorder And Preorder



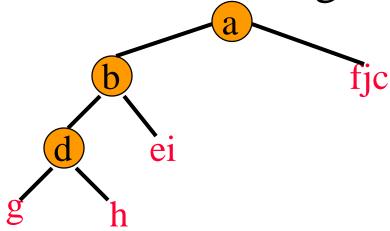
- preorder = a b d g h e i c f j
- b is the next root; gdh are in the left subtree; ei are in the right subtree.



Inorder And Preorder



- preorder = abdgheicfj
- d is the next root; g is in the left subtree; h is in the right subtree.



Inorder And Postorder

- Scan postorder from right to left using inorder to separate left and right subtrees.
- inorder = g d h b e i a f j c
- postorder = g h d i e b j f c a
- Tree root is a; gdhbei are in left subtree; fjc are in right subtree.

Inorder And Level Order

- Scan level order from left to right using inorder to separate left and right subtrees.
- inorder = g d h b e i a f j c
- level order = abcdefghij
- Tree root is a; gdhbei are in left subtree; fjc are in right subtree.