Stats 501 final Project

Debabrata Halder, Piusha Gullapalli, Snehil Verma

2022-12-25

Attribute Information:

Parameters -

age: the age of an individual

workclass: a general term to represent the employment status of an individual

fnlwgt: final weight. This is the number of people the census believes the entry represents.

education: the highest level of education achieved by an individual.

education_num: the highest level of education achieved in numerical form.

marital_status: marital status of an individual.

occupation: the general type of occupation of an individual

relationship: represents what this individual is relative to others.

race: Descriptions of an individual's race

sex: the sex of the individual

capital_gain: capital gains for an individual capital_loss: capital loss for an individual

hours_per_week: the hours an individual has reported to work per week

native country: country of origin for an individual

NOTE: Some values in the dataset is marked as "?". It means the value is unknown. ## Load Data

```
adult <- read.table("adult.data", sep = ",")
colnames(adult) <- c("age", "workclass", "fnlwgt", "education", "education_num", "marital_status", "occ</pre>
```

summary(adult)

##	age	workclass	${ t fnlwgt}$	education
##	Min. :17.00	Length:32561	Min. : 12285	Length:32561
##	1st Qu.:28.00	Class :character	1st Qu.: 117827	Class :character
##	Median :37.00	Mode :character	Median : 178356	Mode :character
##	Mean :38.58		Mean : 189778	
##	3rd Qu.:48.00		3rd Qu.: 237051	
##	Max. :90.00		Max. :1484705	
##	education_num	marital_status	occupation	relationship
##	Min. : 1.00	Length: 32561	Length: 32561	Length:32561
##	1st Qu.: 9.00	Class :character	Class :character	Class :character
##	Median :10.00	Mode :character	Mode :character	Mode :character
##	Mean :10.08			

```
3rd Qu.:12.00
##
           :16.00
   Max.
##
       race
                           sex
                                            capital_gain
                                                            capital loss
##
  Length: 32561
                       Length: 32561
                                                                       0.0
                                           Min.
                                                       0
                                                           Min.
##
   Class : character
                       Class : character
                                           1st Qu.:
                                                       0
                                                           1st Qu.:
                                                                       0.0
   Mode :character
                                                       0
                                                           Median:
                                                                       0.0
##
                     Mode :character
                                           Median:
##
                                                                      87.3
                                           Mean
                                                 : 1078
                                                           Mean
                                                                   :
##
                                           3rd Qu.:
                                                       0
                                                           3rd Qu.:
                                                                       0.0
##
                                           Max.
                                                  :99999
                                                           Max.
                                                                   :4356.0
##
   hours_per_week native_country
                                          fifty_k
                    Length: 32561
                                        Length: 32561
  Min. : 1.00
   1st Qu.:40.00
                    Class : character
                                        Class : character
##
##
  Median :40.00
                    Mode :character
                                        Mode :character
## Mean
           :40.44
## 3rd Qu.:45.00
## Max.
           :99.00
```

Test to check if average capital gain is different for Female/Male:

Motivation: we want to find out if the capital gain differs based on gender.

Assumptions:

- 1. The dataset is a random sample of original population.
- 2. The data comes from a normal distribution.
- 3. The sample size is large enough to conduct any test.
- 4. And the final assumptions is homogeneity of variance.

Hypothesis:

##

H0: capital gain is equal for both gender

568.4105

Ha: capital gain is not equal.

```
# adult %>%
# group_by(sex) %>%
# summarise(record_count = n())

female <- filter(adult, str_detect(sex, 'Female'))
male <- filter(adult, str_detect(sex, 'Male'))

t.test(capital_gain ~ sex, data=adult) # Unpooled</pre>
```

```
##
## Welch Two Sample t-test
##
## data: capital_gain by sex
## t = -10.324, df = 31563, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group Female and group Male is not equal
## 95 percent confidence interval:
## -905.4303 -616.4888
## sample estimates:
## mean in group Female mean in group Male</pre>
```

1329.3701

```
t.test(capital_gain ~ sex, var.equal=TRUE, data=adult) # Pooled
##
##
    Two Sample t-test
##
## data: capital_gain by sex
## t = -8.758, df = 32559, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group Female and group Male is not equal
## 95 percent confidence interval:
   -931.2616 -590.6575
## sample estimates:
## mean in group Female
                            mean in group Male
##
                568.4105
                                      1329.3701
gain_sex<-adult %>%
  group_by(sex) %>%
  summarize(avg_captital_gain=mean(capital_gain))
gain_sex %>%
  ggplot(aes(x=sex, y=avg_captital_gain,fill=avg_captital_gain))+
  geom_tile(color="white",size=0.3)+
  scale_fill_gradient(low="pink",high="purple")
  1500 -
                                                                         avg_captital_gain
avg_captital_gain
                                                                              1200
  1000 -
                                                                              1000
                                                                              800
                                                                              600
   500 -
                      Female
                                                   Male
                                     sex
```

Conclusion: Looking at the p value which is close to 0, we can reject the null hypothesis.

We have evidence that suggests that the true difference in means between group Female and group Male is not equal to 0.

We have evidence to say that there is a difference in the average capital gain of Male and Female

```
t.test(capital_loss ~ sex, data=adult) # Unpooled
   Welch Two Sample t-test
##
##
## data: capital_loss by sex
## t = -8.8911, df = 26312, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group Female and group Male is not equal
## 95 percent confidence interval:
## -47.62897 -30.42238
## sample estimates:
## mean in group Female
                          mean in group Male
##
                61.18763
                                     100.21331
t.test(capital_loss ~ sex, var.equal=TRUE, data=adult) # Pooled
##
##
   Two Sample t-test
##
## data: capital_loss by sex
## t = -8.2308, df = 32559, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group Female and group Male is not equal
## 95 percent confidence interval:
## -48.31906 -29.73229
## sample estimates:
## mean in group Female
                          mean in group Male
##
                61.18763
                                     100.21331
```

Checking if average capital gain differs by race

Motivation: we want to find out if the capital gain differs based on race.

Assumptions:

- 1. The dataset is a random sample of original population.
- 2. The data comes from a normal distribution.
- 3. The sample size is large enough to conduct any test.
- 4. And the final assumptions is homogeneity of variance.

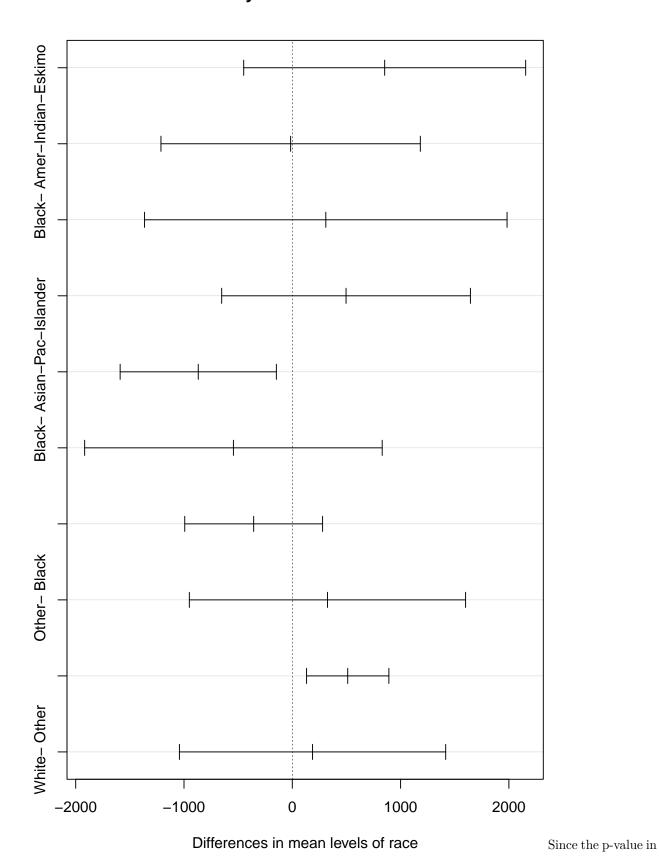
Hypothesis:

H0: capital gain is equal for all race

Ha: there exist a pair of race for which capital gain is not equal.

```
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
#TukeyHSD(anov_race)
gain_race<-adult %>%
  group_by(race) %>%
  summarize(avg_captital_gain=mean(capital_gain))
gain_race %>%
  ggplot(aes(x=race, y=avg_captital_gain,fill=avg_captital_gain))+
  geom_tile(color="white",size=0.3)+
  scale_fill_gradient(low="blue",high="red")
  1500 -
  1250 -
                                                                                  avg_captital_gain
avg_captital_gain
                                                                                      1400
                                                                                      1200
                                                                                      1000
                                                                                      800
   750 -
                                         Black
                                                                     White
        Amer-Indian-EskimoAsian-Pac-Islander
                                                       Other
                                         race
plot(TukeyHSD(aov(capital_gain ~ race, data = adult)))
```

95% family-wise confidence level



our ANOVA table (0.00132) is less than .05, we have sufficient evidence to reject the null hypothesis.

This means we have sufficient evidence to say that the mean capital gain is not equal across different races.

From the Tukey Test, we can see that there is a significant difference between the means for Black-Asian-Pac-Islander and White- Black, and the p values are below the significance level.

From the plots, we can see that the maximum average capital gain is in the race Asian-Pac-Islander.

Checking if average capital gain differs by occupation

Motivation: we want to find out if the capital gain differs based on occupation.

Assumptions:

- 1. The dataset is a random sample of original population.
- 2. The data comes from a normal distribution.
- 3. The sample size is large enough to conduct any test.
- 4. And the final assumptions is homogeneity of variance.

Hypothesis:

H0: capital gain is equal for all occupation

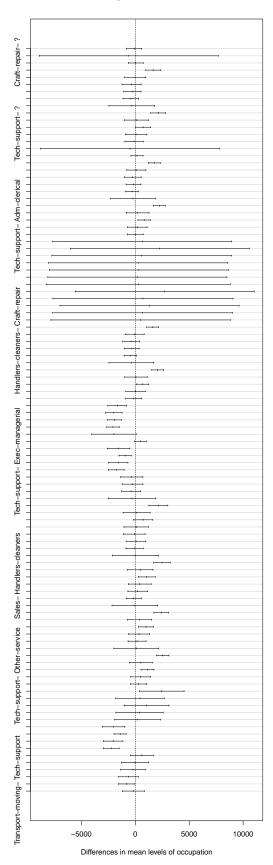
Ha: there exist a pair of occupation for which capital gain is not equal.

```
anov_occ <- aov(capital_gain ~ occupation, data = adult)
summary(anov_occ)</pre>
```

```
## Df Sum Sq Mean Sq F value Pr(>F)
## occupation    14 2.539e+10 1.813e+09    33.72 <2e-16 ***
## Residuals    32546 1.751e+12 5.379e+07
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
#TukeyHSD(anov_occ)

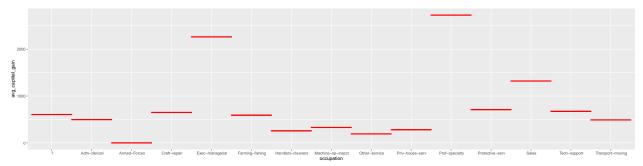
plot(TukeyHSD(aov(capital_gain ~ occupation, data = adult)))</pre>
```

95% family-wise confidence level



```
gain_occupation<-adult %>%
  group_by(occupation) %>%
  summarize(avg_captital_gain=mean(capital_gain))

gain_occupation %>%
  ggplot(aes(x=occupation, y=avg_captital_gain))+
  geom_tile(color="red",size=1)
```



Since the p-value in our ANOVA table (10^-16) is less than .05, we have sufficient evidence to reject the null hypothesis.

This means we have sufficient evidence to say that the mean capital gain is not equal across different occupation.

From the Tukey test, we can see the p-values for different occupation pairs, and the difference in average capital gain.

From the plots, we can see that the maximum average capital gain is in the occupation of Exec-managerial.

Checking if average capital gain differs by workclass

Motivation: we want to find out if the capital gain differs based on workclass.

Assumptions:

- 1. The dataset is a random sample of original population.
- 2. The data comes from a normal distribution.
- 3. The sample size is large enough to conduct any test.
- 4. And the final assumptions is homogeneity of variance.

Hypothesis:

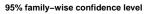
H0: capital gain is equal for all workclass

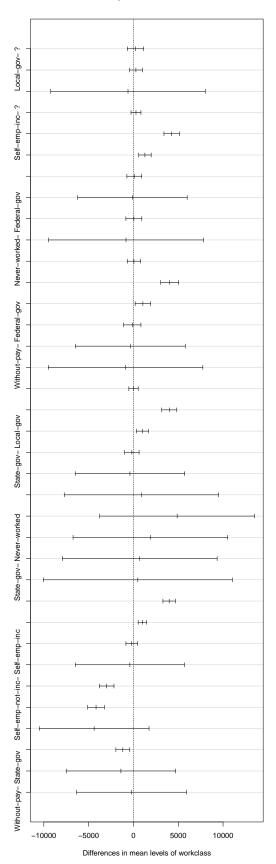
Ha: there exist a pair of workclass for which capital gain is not equal.

```
anov_wc <- aov(capital_gain ~ workclass, data = adult)
summary(anov_wc)</pre>
```

```
## Df Sum Sq Mean Sq F value Pr(>F)
## workclass 8 1.931e+10 2.413e+09 44.72 <2e-16 ***
## Residuals 32552 1.757e+12 5.396e+07
## ---
## Signif. codes: 0 '*** 0.001 '** 0.05 '.' 0.1 ' ' 1
```

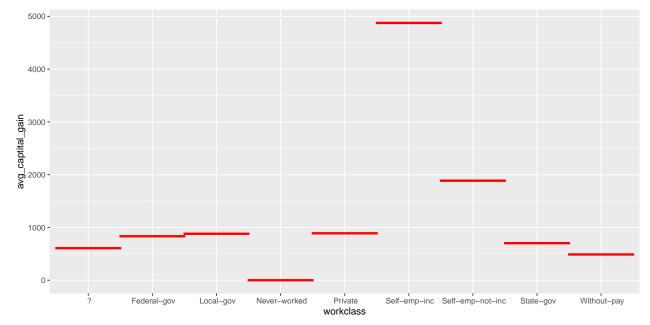
```
#TukeyHSD(anov_wc)
plot(TukeyHSD(aov(capital_gain ~ workclass, data = adult)))
```





```
gain_wc<-adult %>%
  group_by(workclass) %>%
  summarize(avg_captital_gain=mean(capital_gain))

gain_wc %>%
  ggplot(aes(x=workclass, y=avg_captital_gain))+
  geom_tile(color="red", size=1)
```



Since the p-value in our ANOVA table (10^-16) is less than .05, we have sufficient evidence to reject the null hypothesis.

This means we have sufficient evidence to say that the mean capital gain is not equal across different workclass.

From the Tukey test, we can see the p-values for different occupation pairs, and the difference in average capital gain.

From the plots, we can see that the maximum average capital gain is in the occupation of Self-emp-inc.

Checking if average capital gain differs by education level

Motivation: we want to find out if the capital gain differs based on education level.

Assumptions:

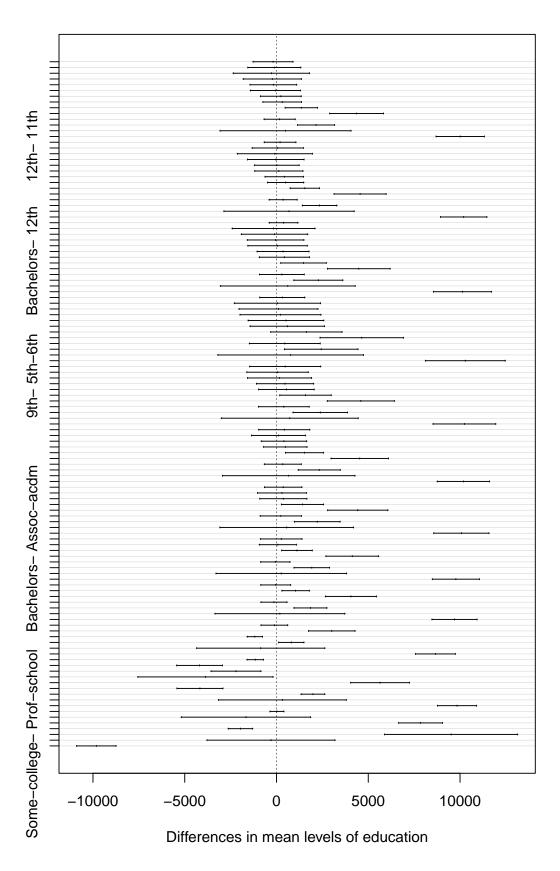
- 1. The dataset is a random sample of original population.
- 2. The data comes from a normal distribution.
- 3. The sample size is large enough to conduct any test.
- 4. And the final assumptions is homogeneity of variance.

Hypothesis:

H0: capital gain is equal for education level

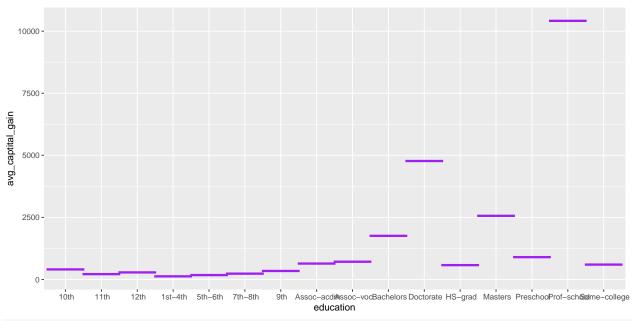
Ha: there exist a pair of education level for which capital gain is not equal.

95% family-wise confidence level



```
gain_edu<-adult %>%
  group_by(education) %>%
  summarize(avg_captital_gain=mean(capital_gain))

gain_edu %>%
  ggplot(aes(x=education, y=avg_captital_gain))+
  geom_tile(color="purple",size=1)
```

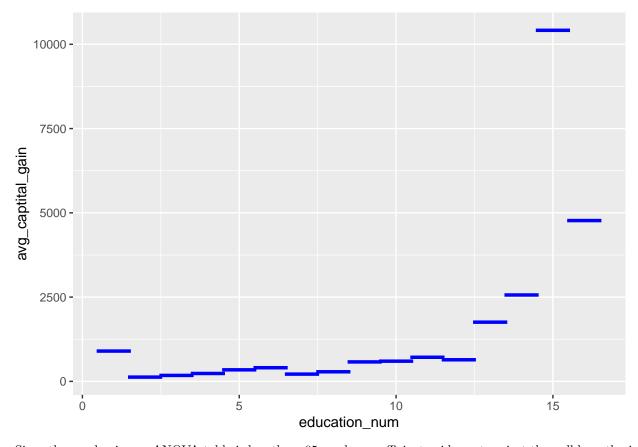


```
#Checking for education number

anov_edu_num <- aov(capital_gain ~ education_num, data = adult)
# summary(anov_edu_num)
# anov_edu_num

gain_edu_num<-adult %>%
    group_by(education_num) %>%
    summarize(avg_captital_gain=mean(capital_gain))

gain_edu_num %>%
    ggplot(aes(x=education_num, y=avg_captital_gain))+
    geom_tile(color="blue",size=1)
```



Since the p-value in our ANOVA table is less than .05, we have sufficient evidence to reject the null hypothesis.

This means we have sufficient evidence to say that the mean capital gain is not equal across different education levels.

From the Tukey test, we can see the p-values for different education pairs, and the difference in average capital gain.

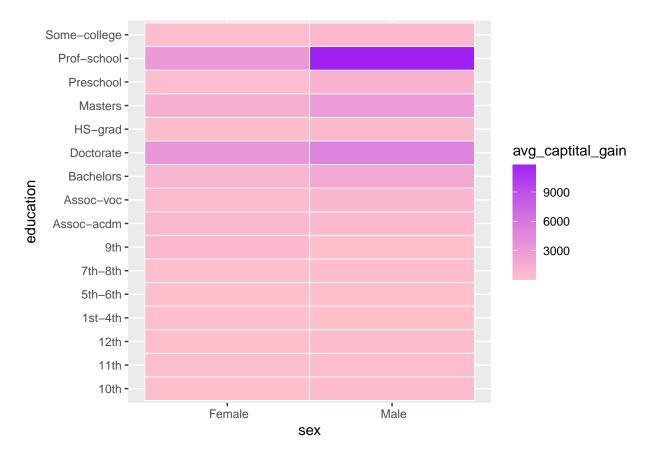
From the plots, we can see that the maximum average capital gain is with the education prof school.

Plotting gain on education and sex

```
education_sex<-adult %>%
  group_by(sex, education) %>%
  summarize(avg_captital_gain=mean(capital_gain))

## `summarise()` has grouped output by 'sex'. You can override using the `.groups`
## argument.

education_sex %>%
  ggplot(aes(x=sex,y=education,fill=avg_captital_gain))+
  geom_tile(color="white",size=0.3)+
  scale_fill_gradient(low="pink",high="purple")
```

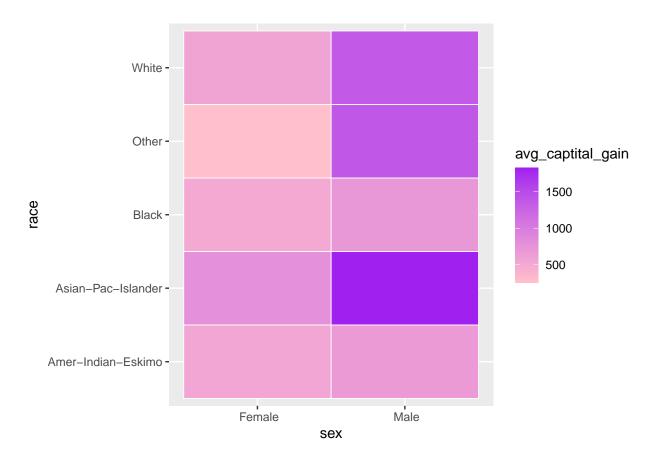


Plotting gain on race and sex

```
race_sex<-adult %>%
  group_by(sex, race) %>%
  summarize(avg_captital_gain=mean(capital_gain))

## `summarise()` has grouped output by 'sex'. You can override using the `.groups`
## argument.

race_sex %>%
  ggplot(aes(x=sex,y=race,fill=avg_captital_gain))+
  geom_tile(color="white",size=0.3)+
  scale_fill_gradient(low="pink",high="purple")
```



Average capital gain vs earning greater than or less than or equal to 50k.

```
# adult %>%
 group_by(fifty_k) %>%
  summarise(record\_count = n())
t.test(capital_gain ~ fifty_k, data=adult) # Unpooled
##
## Welch Two Sample t-test
## data: capital_gain by fifty_k
## t = -23.427, df = 7861.7, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group <=50K and group >50K is not equal t
## 95 percent confidence interval:
## -4180.166 -3534.614
## sample estimates:
## mean in group <=50K mean in group >50K
##
               148.7525
                                  4006.1425
t.test(capital_gain ~ fifty_k, var.equal=TRUE, data=adult) # Pooled
##
## Two Sample t-test
```

```
##
## data: capital_gain by fifty_k
## t = -41.342, df = 32559, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group <=50K and group >50K is not equal t
## 95 percent confidence interval:
   -4040.271 -3674.509
##
## sample estimates:
## mean in group <=50K mean in group >50K
                148.7525
                                     4006.1425
gain_fifty<-adult %>%
  group_by(fifty_k) %>%
  summarize(avg_captital_gain=mean(capital_gain))
gain_fifty %>%
  ggplot(aes(x=fifty_k, y=avg_captital_gain,fill=avg_captital_gain))+
  geom_tile(color="white",size=0.3)+
  scale_fill_gradient(low="pink",high="purple")
    6000 -
    4000 -
                                                                          avg_captital_gain
avg_captital_gain
                                                                               4000
                                                                               3000
    2000 -
                                                                               2000
                                                                               1000
      0 -
   -2000 -
                       <=50K
                                                    >50K
```

Looking at the p value which is close to 0, we can reject the null hypothesis.

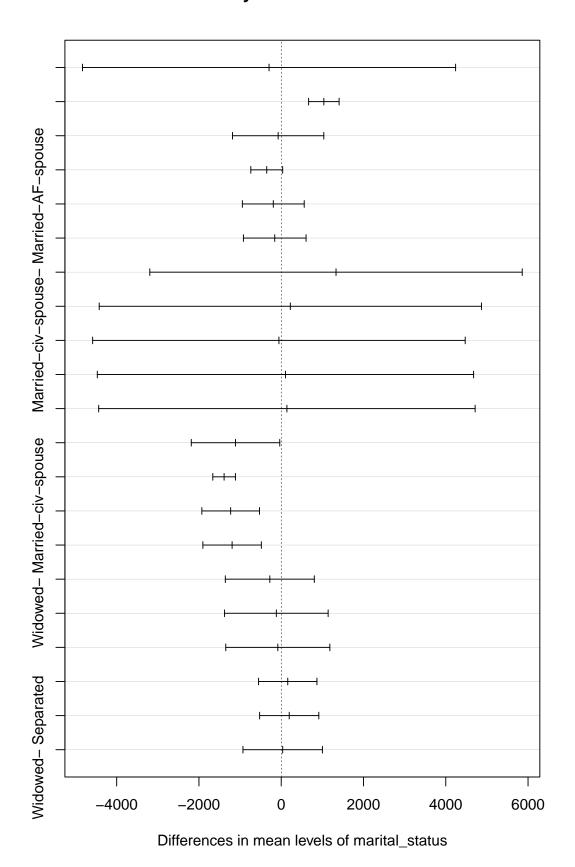
We have evidence that suggests that the true difference in means between group that earns less than or equal to 50k and more than 50 is not equal to 0.

We have evidence to say that there is a significant difference in the average capital gain.

fifty_k

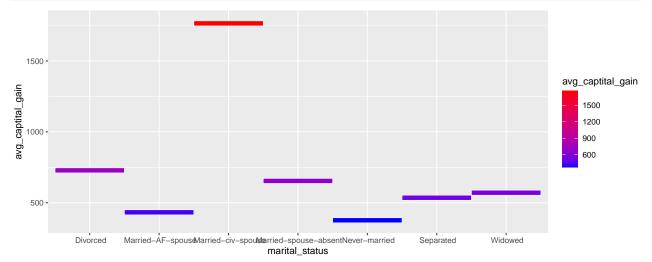
Checking if average capital gain differs by marital status

95% family-wise confidence level



```
gain_marital<-adult %>%
  group_by(marital_status) %>%
  summarize(avg_captital_gain=mean(capital_gain))

gain_marital %>%
  ggplot(aes(x=marital_status, y=avg_captital_gain,fill=avg_captital_gain))+
  geom_tile(color="white",size=0.3)+
  scale_fill_gradient(low="blue",high="red")
```



Since the p-value in our ANOVA table is less than .05, we have sufficient evidence to reject the null hypothesis.

This means we have sufficient evidence to say that the mean capital gain is not equal across different marital-status.

From the Tukey test, we can see the p-values for different marital status pairs, and the difference in average capital gain.

From the plots, we can see that the maximum average capital gain is with married-civ-spouse.

Real Estate data set: Real Estate

```
real_estate <- read.csv("Real_Estate.csv")
summary(real_estate)</pre>
```

```
##
          No
                    X1.transaction.date X2.house.age
##
    Min.
           :
             1.0
                    Min.
                            :2013
                                         Min.
                                                : 0.000
##
   1st Qu.:104.2
                    1st Qu.:2013
                                         1st Qu.: 9.025
   Median :207.5
                    Median:2013
                                         Median :16.100
           :207.5
                            :2013
                                                 :17.713
##
   Mean
                    Mean
                                         Mean
    3rd Qu.:310.8
                    3rd Qu.:2013
                                         3rd Qu.:28.150
##
##
   {\tt Max.}
           :414.0
                    Max.
                            :2014
                                         Max.
                                                 :43.800
##
   X3.distance.to.the.nearest.MRT.station X4.number.of.convenience.stores
           : 23.38
##
   Min.
                                            Min.
                                                   : 0.000
##
   1st Qu.: 289.32
                                            1st Qu.: 1.000
  Median: 492.23
                                            Median : 4.000
##
   Mean
           :1083.89
                                            Mean
                                                   : 4.094
##
    3rd Qu.:1454.28
                                            3rd Qu.: 6.000
  Max.
           :6488.02
                                            Max.
                                                    :10.000
```

```
##
     X5.latitude
                      X6.longitude
                                      Y.house.price.of.unit.area
  Min.
           :24.93
                            :121.5
                                      Min.
                                            : 7.60
##
                    Min.
   1st Qu.:24.96
                     1st Qu.:121.5
                                      1st Qu.: 27.70
                     Median :121.5
                                      Median : 38.45
## Median :24.97
           :24.97
##
   Mean
                     Mean
                            :121.5
                                      Mean
                                              : 37.98
    3rd Qu.:24.98
                                      3rd Qu.: 46.60
##
                     3rd Qu.:121.5
   Max.
           :25.01
                                             :117.50
                     Max.
                            :121.6
                                      Max.
ls(real_estate)
## [1] "No"
## [2] "X1.transaction.date"
## [3] "X2.house.age"
## [4] "X3.distance.to.the.nearest.MRT.station"
## [5] "X4.number.of.convenience.stores"
## [6] "X5.latitude"
## [7] "X6.longitude"
## [8] "Y.house.price.of.unit.area"
pairs(real_estate[,2:8], pch=19)
                  20
                      40
                                                           121.48
                                                                  121.56
                           to.the.nearest.f
                                      er.of.convenien
                                                   X5 latitude
                                                              X6.longitude
                                                                                   120
```

 $\#xyplot(Y.house.price.of.unit.area \sim X4.number.of.convenience.stores, data=real_estate) \# positive tren \\ \#xyplot(Y.house.price.of.unit.area \sim X3.distance.to.the.nearest.MRT.station, data=real_estate) \# negati$

20 60

120

24.94 25.00

study with distance to metro station.

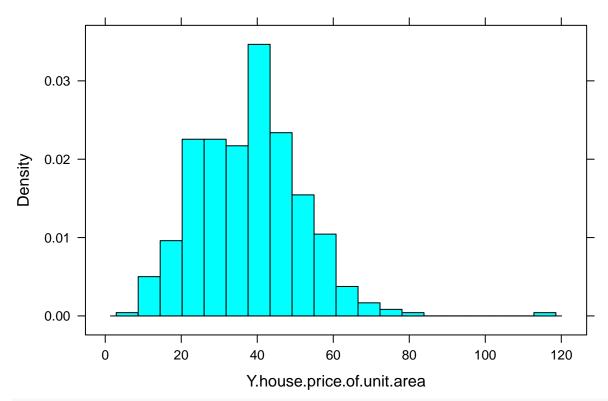
#check value distribution.

2013.6

2012.8

histogram(~Y.house.price.of.unit.area, data=real_estate, nint=20)

0 3000



#check correlation between house price and distance to metro station.

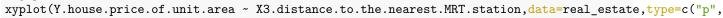
cor(Y.house.price.of.unit.area ~ X3.distance.to.the.nearest.MRT.station, data=real_estate) # -0.673

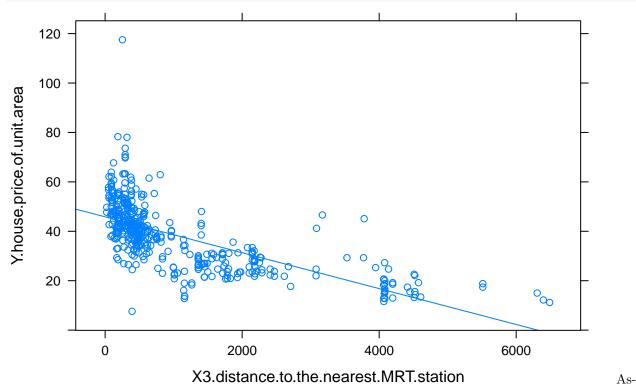
```
## [1] -0.6736129
#the least squares line regression line.
m1 <- lm(Y.house.price.of.unit.area ~ X3.distance.to.the.nearest.MRT.station, data=real_estate)
summary(m1)
##
## Call:
## lm(formula = Y.house.price.of.unit.area ~ X3.distance.to.the.nearest.MRT.station,
##
       data = real_estate)
##
## Residuals:
       Min
                                       Max
                1Q Median
                                3Q
  -35.396 -6.007 -1.195
                             4.831
                                  73.483
## Coefficients:
                                            Estimate Std. Error t value Pr(>|t|)
                                          45.8514271 0.6526105
                                                                  70.26
## (Intercept)
                                                                          <2e-16
## X3.distance.to.the.nearest.MRT.station -0.0072621 0.0003925 -18.50
                                                                          <2e-16
##
## (Intercept)
## X3.distance.to.the.nearest.MRT.station ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 10.07 on 412 degrees of freedom
Multiple R-squared: 0.4538, Adjusted R-squared: 0.4524
F-statistic: 342.2 on 1 and 412 DF, p-value: < 2.2e-16</pre>

##



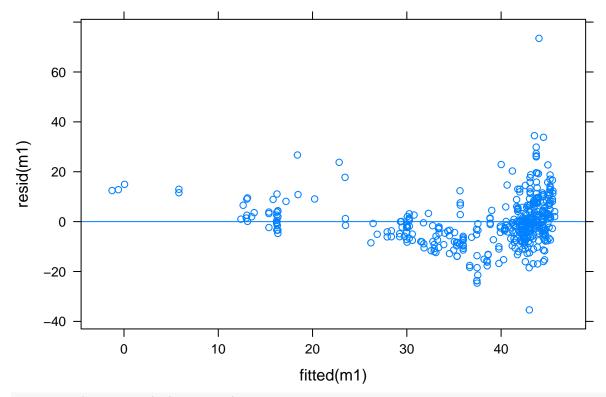


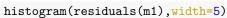


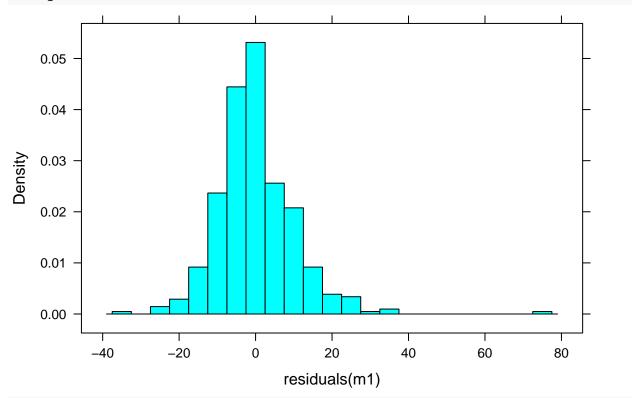
$sumption\ Check:$

- 1. Residual are uniformly distributed around y=0 horizontal line.
- 2. Residual follows normal distribution.
- 3. The relationship between two variables should be linear.
- 4. The observation should be independent of each other.

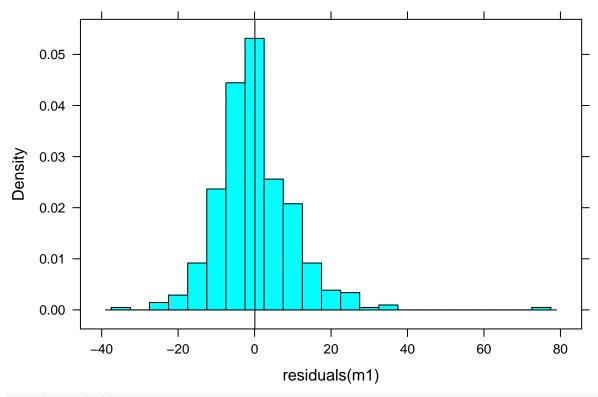
```
#normalty check of errors/residual and assumptions check *
xyplot(resid(m1)~fitted(m1), data=real_estate, type=c("p","r"))
```

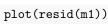


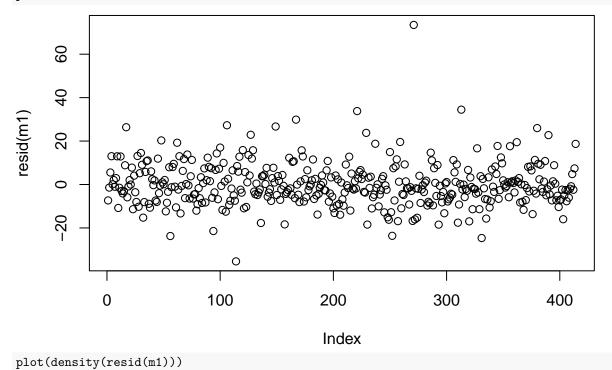




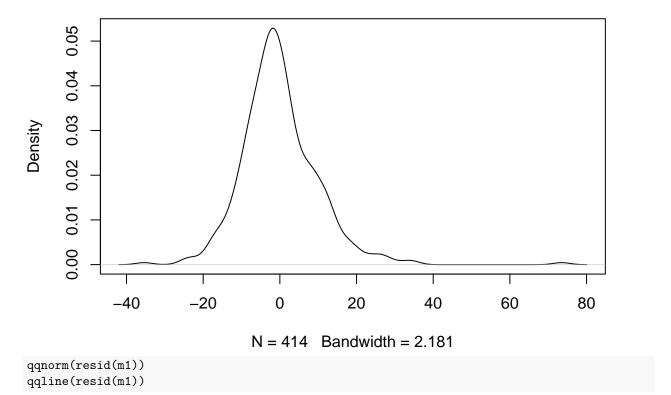
ladd(panel.qqmathline(resid(m1)))



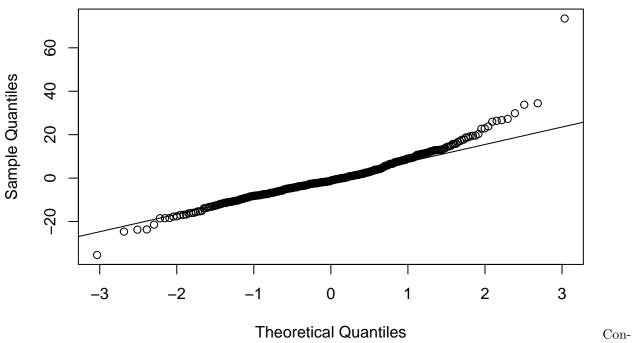




density.default(x = resid(m1))



Normal Q-Q Plot



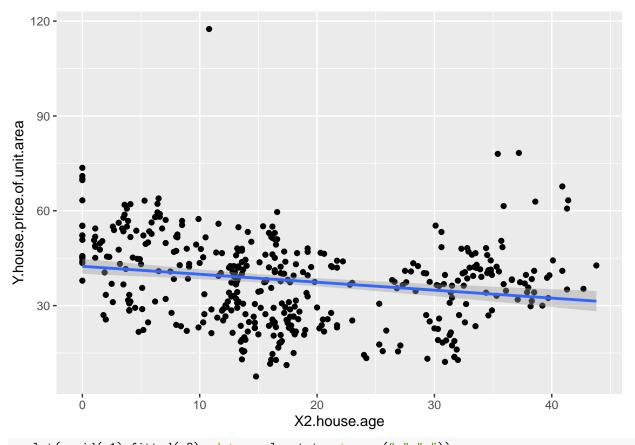
clusion:

All assuptions holds here. From differnt graphs we can see that the conditions for linear model fitting holds.

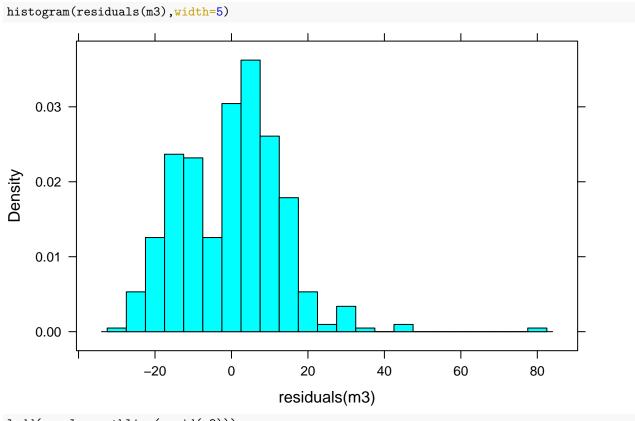
```
#Checking if house price varies with number of convenience stores:
m2 <- lm(Y.house.price.of.unit.area ~ X4.number.of.convenience.stores, data=real_estate)
summary(m2)
##
## Call:
## lm(formula = Y.house.price.of.unit.area ~ X4.number.of.convenience.stores,
      data = real_estate)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
## -35.407 -7.341 -1.788 5.984 87.681
##
## Coefficients:
##
                                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                   27.1811
                                               0.9419
                                                        28.86
                                                                <2e-16 ***
## X4.number.of.convenience.stores
                                    2.6377
                                               0.1868
                                                        14.12
                                                                <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 11.18 on 412 degrees of freedom
## Multiple R-squared: 0.326, Adjusted R-squared: 0.3244
## F-statistic: 199.3 on 1 and 412 DF, p-value: < 2.2e-16
m3 <- lm(Y.house.price.of.unit.area ~ X2.house.age, data=real_estate)
summary(m3)
##
## Call:
## lm(formula = Y.house.price.of.unit.area ~ X2.house.age, data = real_estate)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -31.113 -10.738
                   1.626
                            8.199 77.781
##
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 42.43470
                           1.21098 35.042 < 2e-16 ***
## X2.house.age -0.25149
                           0.05752 -4.372 1.56e-05 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.32 on 412 degrees of freedom
## Multiple R-squared: 0.04434,
                                   Adjusted R-squared: 0.04202
## F-statistic: 19.11 on 1 and 412 DF, p-value: 1.56e-05
```

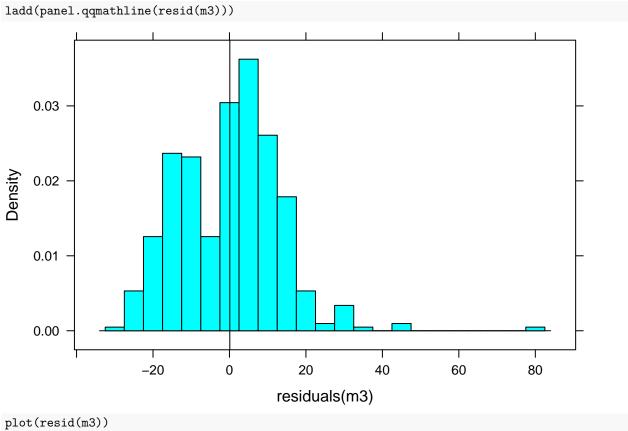
`geom_smooth()` using formula 'y ~ x'

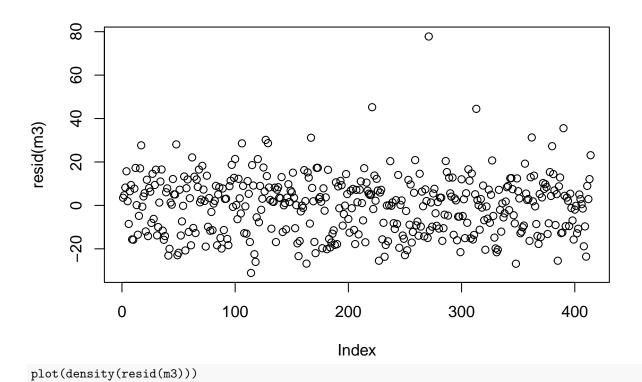
ggplot(real_estate, aes(X2.house.age, Y.house.price.of.unit.area)) + geom_point() + stat_smooth(method



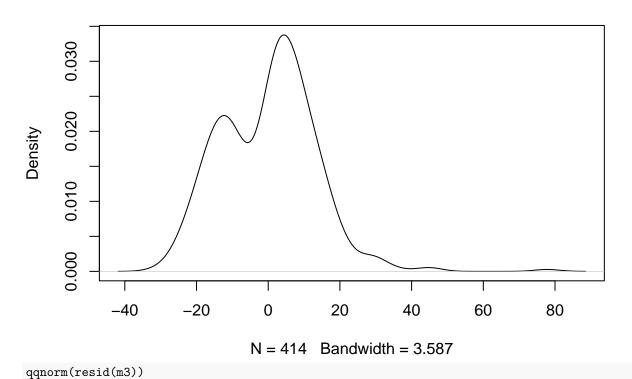
xyplot(resid(m1)~fitted(m3), data=real_estate, type=c("p","r")) resid(m1) -20 -40 т 36 fitted(m3)





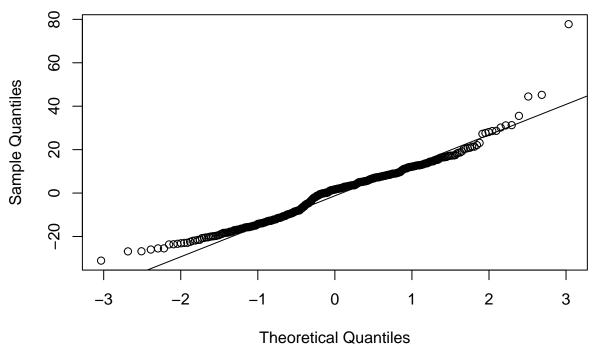


density.default(x = resid(m3))



qqline(resid(m3))

Normal Q-Q Plot



clusion:

From the above graphs, the relationship between house price and house age is not linear, and from Q_Q plot also, we can see that the residuals are not on a straight lines and uniform distribution of error around y=0 horizontal lines doesn't hold also, so we should not use linear model to predict the house price based on house age. And if we build the model, we can see that the R-squared value is around 4%, which also indicates linear model is not suitable to predict the house price based on house age.

Con-