

Statistics 501 final Project

Debabrata Halder, Piusa Gullapalli, Snehil Verma

2022-12-25

Introduction and Data Background -

This data was extracted by Barry Becker from the 1994 Census database.

The data was extracted to be used for a prediction task to determine whether a person makes over 50K a year.

Conversion of original data as follows:

1. Discretized agrossincome into two ranges with threshold 50,000.
2. Convert U.S. to US to avoid periods.
3. Convert Unknown to “?”
4. Run MLC++ GenCVFiles to generate data,test.

Description of fnlwgt (final weight):

The weights on the CPS files are controlled to independent estimates of the civilian non institutional population of the US. These are prepared monthly for us by Population Division here at the Census Bureau.

Attribute Information:

Parameters -

age: the age of an individual

workclass: a general term to represent the employment status of an individual

fnlwgt: final weight. This is the number of people the census believes the entry represents.

education: the highest level of education achieved by an individual.

education_num: the highest level of education achieved in numerical form.

marital_status: marital status of an individual.

occupation: the general type of occupation of an individual

relationship: represents what this individual is relative to others.

race: Descriptions of an individual's race

sex: the sex of the individual

capital_gain: capital gains for an individual

capital_loss: capital loss for an individual

hours_per_week: the hours an individual has reported to work per week

native_country: country of origin for an individual

NOTE: Some values in the dataset is marked as “?”. It means the value is unknown.

Loading the Data

```
adult <- read.table("adult.data", sep = ",")
colnames(adult) <- c("age", "workclass", "fnlwgt", "education", "education_num", "marital_status", "occupation", "relationship", "sex", "capital_gain", "capital_loss", "hours_per_week", "native_country", "fifty_k")
summary(adult)
```

##	age	workclass	fnlwgt	education
##	Min. :17.00	Length:32561	Min. : 12285	Length:32561
##	1st Qu.:28.00	Class :character	1st Qu.: 117827	Class :character
##	Median :37.00	Mode :character	Median : 178356	Mode :character
##	Mean :38.58		Mean : 189778	
##	3rd Qu.:48.00		3rd Qu.: 237051	
##	Max. :90.00		Max. :1484705	
##	education_num	marital_status	occupation	relationship
##	Min. : 1.00	Length:32561	Length:32561	Length:32561
##	1st Qu.: 9.00	Class :character	Class :character	Class :character
##	Median :10.00	Mode :character	Mode :character	Mode :character
##	Mean :10.08			
##	3rd Qu.:12.00			
##	Max. :16.00			
##	race	sex	capital_gain	capital_loss
##	Length:32561	Length:32561	Min. : 0	Min. : 0.0
##	Class :character	Class :character	1st Qu.: 0	1st Qu.: 0.0
##	Mode :character	Mode :character	Median : 0	Median : 0.0
##			Mean : 1078	Mean : 87.3
##			3rd Qu.: 0	3rd Qu.: 0.0
##			Max. :99999	Max. :4356.0
##	hours_per_week	native_country	fifty_k	
##	Min. : 1.00	Length:32561	Length:32561	
##	1st Qu.:40.00	Class :character	Class :character	
##	Median :40.00	Mode :character	Mode :character	
##	Mean :40.44			
##	3rd Qu.:45.00			
##	Max. :99.00			

Test to check if average capital gain is different for Female/Male:

Motivation: we want to find out if the capital gain differs based on gender.

Assumptions:

1. The dataset is a random sample of original population.
2. The data comes from a normal distribution.
3. The sample size is large enough to conduct any test.
4. And the final assumptions is homogeneity of variance.

Hypothesis:

H0: capital gain is equal for both gender

Ha: capital gain is not equal.

```

# adult %>%
#   group_by(sex) %>%
#   summarise(record_count = n())

female <- filter(adult, str_detect(sex, 'Female'))
male <- filter(adult, str_detect(sex, 'Male'))

t.test(capital_gain ~ sex, data=adult) # Unpooled

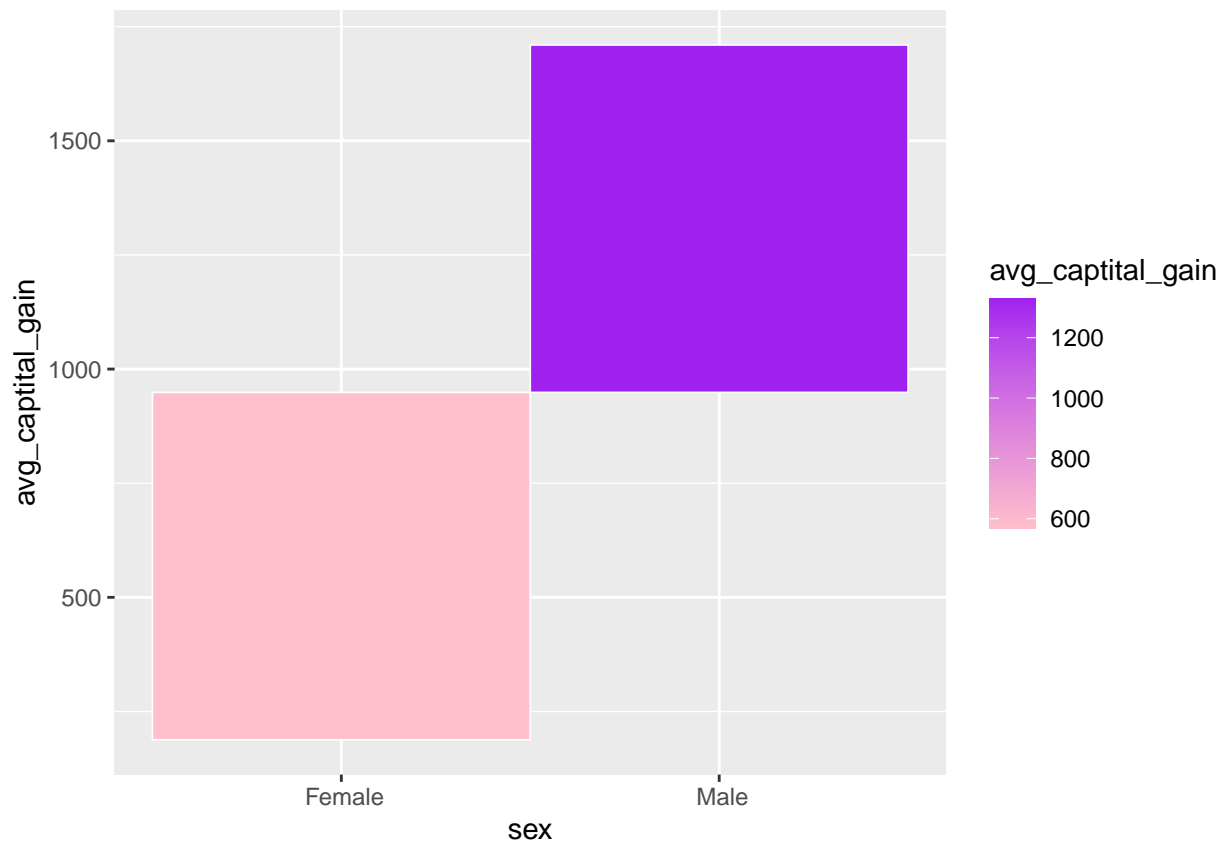
##
## Welch Two Sample t-test
##
## data: capital_gain by sex
## t = -10.324, df = 31563, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group Female and group Male is not equal
## 95 percent confidence interval:
## -905.4303 -616.4888
## sample estimates:
## mean in group Female mean in group Male
## 568.4105 1329.3701
t.test(capital_gain ~ sex, var.equal=TRUE, data=adult) # Pooled

##
## Two Sample t-test
##
## data: capital_gain by sex
## t = -8.758, df = 32559, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group Female and group Male is not equal
## 95 percent confidence interval:
## -931.2616 -590.6575
## sample estimates:
## mean in group Female mean in group Male
## 568.4105 1329.3701

gain_sex<-adult %>%
  group_by(sex) %>%
  summarize(avg_captital_gain=mean(capital_gain))

gain_sex %>%
  ggplot(aes(x=sex, y=avg_captital_gain,fill=avg_captital_gain))+
  geom_tile(color="white",size=0.3)+
  scale_fill_gradient(low="pink",high="purple")

```



Conclusion:

Looking at the p value which is close to 0, we can reject the null hypothesis.

We have evidence that suggests that the true difference in means between group Female and group Male is not equal to 0.

We have evidence to say that there is a difference in the average capital gain of Male and Female

```
t.test(capital_loss ~ sex, data=adult) # Unpooled
```

```
##
## Welch Two Sample t-test
##
## data: capital_loss by sex
## t = -8.8911, df = 26312, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group Female and group Male is not equal to 0
## 95 percent confidence interval:
## -47.62897 -30.42238
## sample estimates:
## mean in group Female mean in group Male
## 61.18763 100.21331
```

```
t.test(capital_loss ~ sex, var.equal=TRUE, data=adult) # Pooled
```

```
##
## Two Sample t-test
##
## data: capital_loss by sex
## t = -8.2308, df = 32559, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group Female and group Male is not equal to 0
```

```
## 95 percent confidence interval:
## -48.31906 -29.73229
## sample estimates:
## mean in group Female mean in group Male
## 61.18763 100.21331
```

Checking if average capital gain differs by race

Motivation: we want to find out if the capital gain differs based on race.

Assumptions:

1. The dataset is a random sample of original population.
2. The data comes from a normal distribution.
3. The sample size is large enough to conduct any test.
4. And the final assumptions is homogeneity of variance.

Hypothesis:

H0: capital gain is equal for all race

Ha: there exist a pair of race for which capital gain is not equal.

```
# adult %>%
#   group_by(race) %>%
#   summarise(record_count = n())

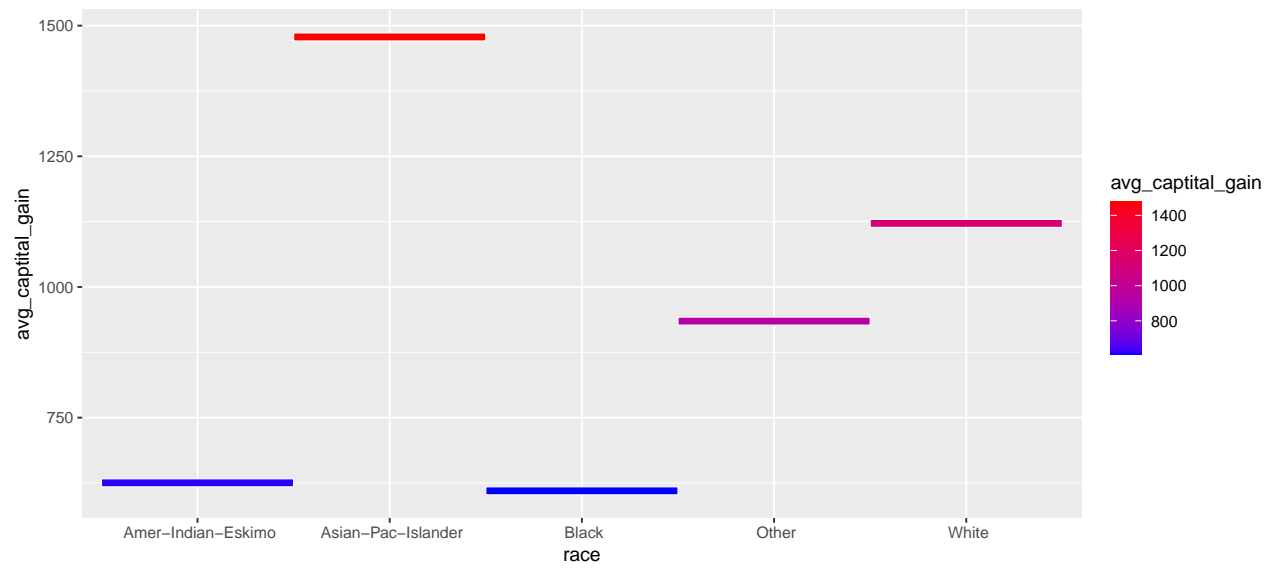
anov_race <- aov(capital_gain ~ race, data = adult)
summary(anov_race)

##              Df    Sum Sq  Mean Sq F value Pr(>F)
## race          4 9.733e+08 243318824   4.463 0.00132 **
## Residuals    32556 1.775e+12  54519345
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

#TukeyHSD(anov_race)

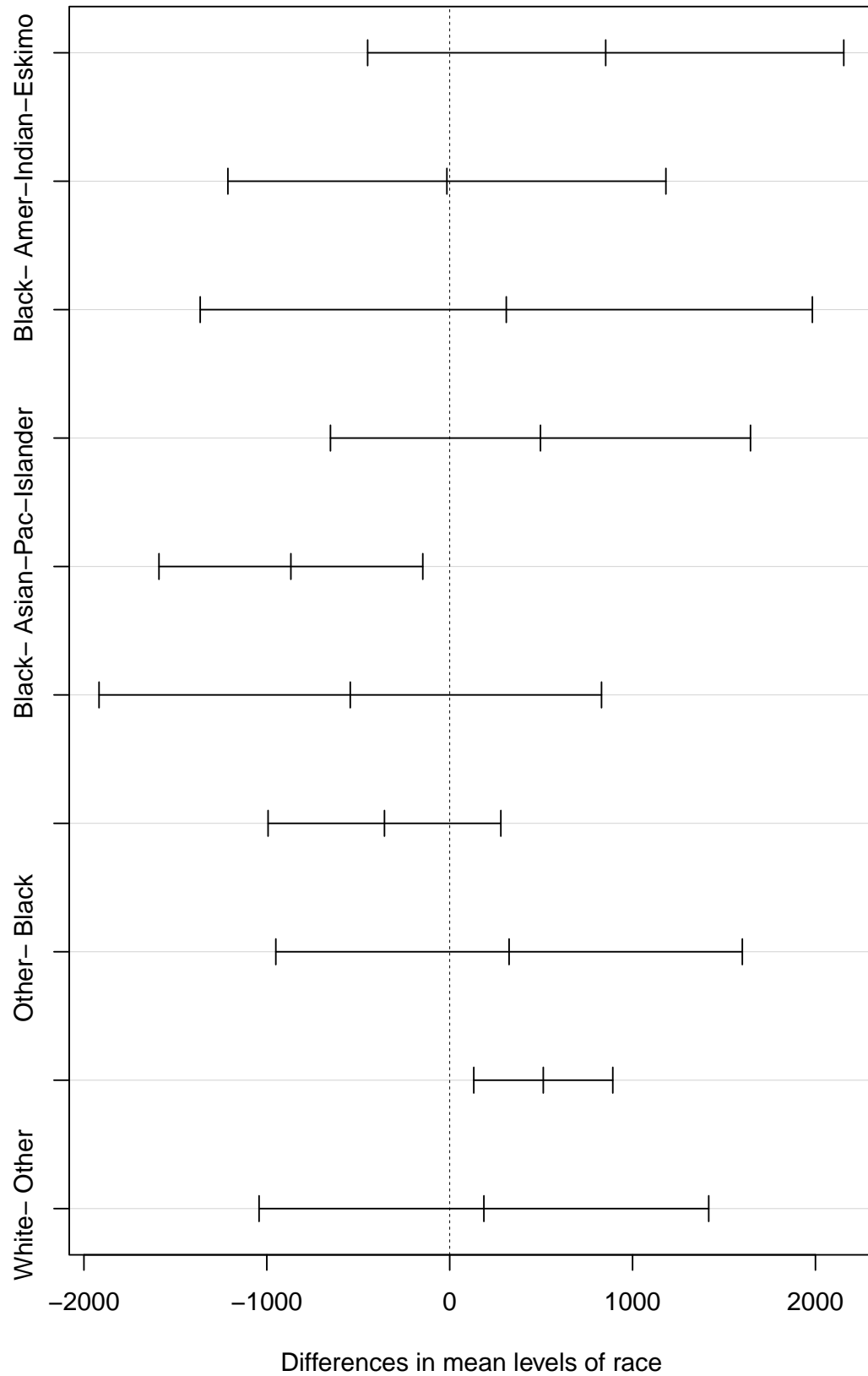
gain_race<-adult %>%
  group_by(race) %>%
  summarize(avg_captital_gain=mean(capital_gain))

gain_race %>%
  ggplot(aes(x=race, y=avg_captital_gain,fill=avg_captital_gain))+
  geom_tile(color="white",size=0.3)+
  scale_fill_gradient(low="blue",high="red")
```



```
plot(TukeyHSD(aov(capital_gain ~ race, data = adult)))
```

95% family-wise confidence level



Since the p-value in our ANOVA table (0.00132) is less than .05, we have sufficient evidence to reject the null hypothesis.

This means we have sufficient evidence to say that the mean capital gain is not equal across different races.

From the Tukey Test, we can see that there is a significant difference between the means for Black- Asian-Pac-Islander and White- Black, and the p values are below the significance level.

From the plots, we can see that the maximum average capital gain is in the race Asian-Pac-Islander.

Checking if average capital gain differs by occupation

Motivation: we want to find out if the capital gain differs based on occupation.

Assumptions:

1. The dataset is a random sample of original population.
2. The data comes from a normal distribution.
3. The sample size is large enough to conduct any test.
4. And the final assumptions is homogeneity of variance.

Hypothesis:

H0: capital gain is equal for all occupation

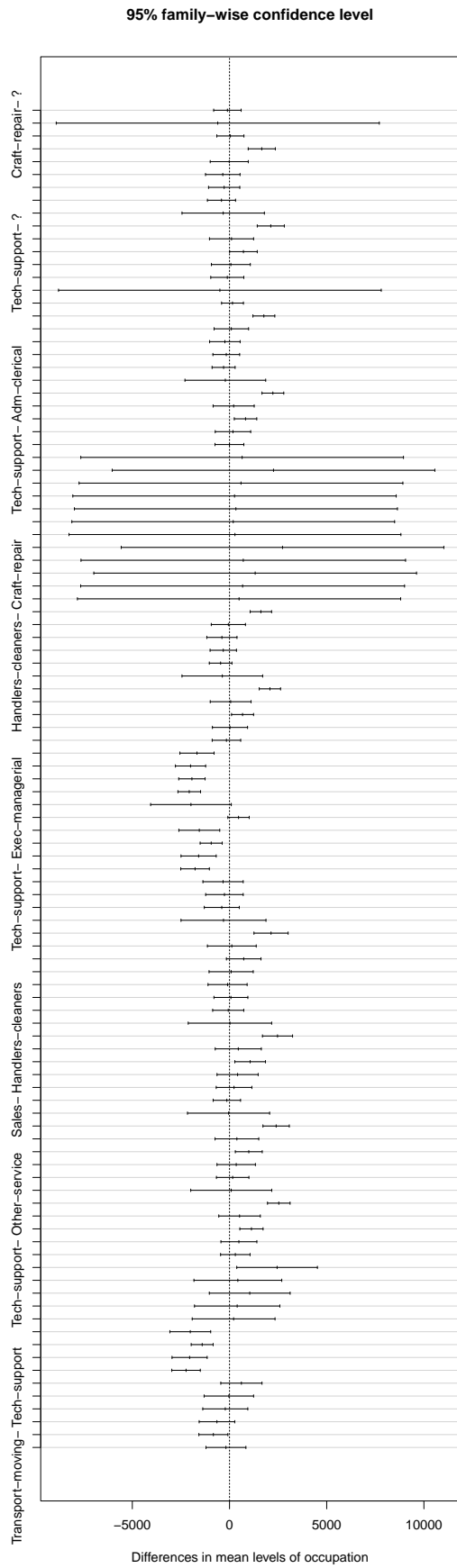
Ha: there exist a pair of occupation for which capital gain is not equal.

```
anov_occ <- aov(capital_gain ~ occupation, data = adult)
summary(anov_occ)

##              Df    Sum Sq   Mean Sq F value Pr(>F)
## occupation    14 2.539e+10  1.813e+09   33.72 <2e-16 ***
## Residuals  32546 1.751e+12  5.379e+07
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

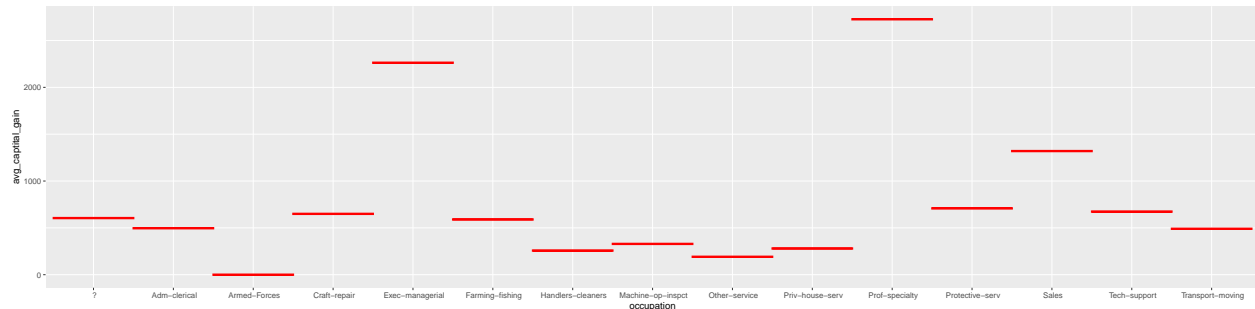
#TukeyHSD(anov_occ)

plot(TukeyHSD(aov(capital_gain ~ occupation, data = adult)))
```

```
gain_occupation <- adult %>%
  group_by(occupation) %>%
  summarize(avg_capital_gain = mean(capital_gain))

gain_occupation %>%
  ggplot(aes(x=occupation, y=avg_capital_gain)) +
  geom_tile(color="red", size=1)
```



Since the p-value in our ANOVA table (10^{-16}) is less than .05, we have sufficient evidence to reject the null hypothesis.

This means we have sufficient evidence to say that the mean capital gain is not equal across different occupation.

From the Tukey test, we can see the p-values for different occupation pairs, and the difference in average capital gain.

From the plots, we can see that the maximum average capital gain is in the occupation of Exec-managerial.

Checking if average capital gain differs by workclass

Motivation: we want to find out if the capital gain differs based on workclass.

Assumptions:

1. The dataset is a random sample of original population.
2. The data comes from a normal distribution.
3. The sample size is large enough to conduct any test.
4. And the final assumptions is homogeneity of variance.

Hypothesis:

H0: capital gain is equal for all workclass

Ha: there exist a pair of workclass for which capital gain is not equal.

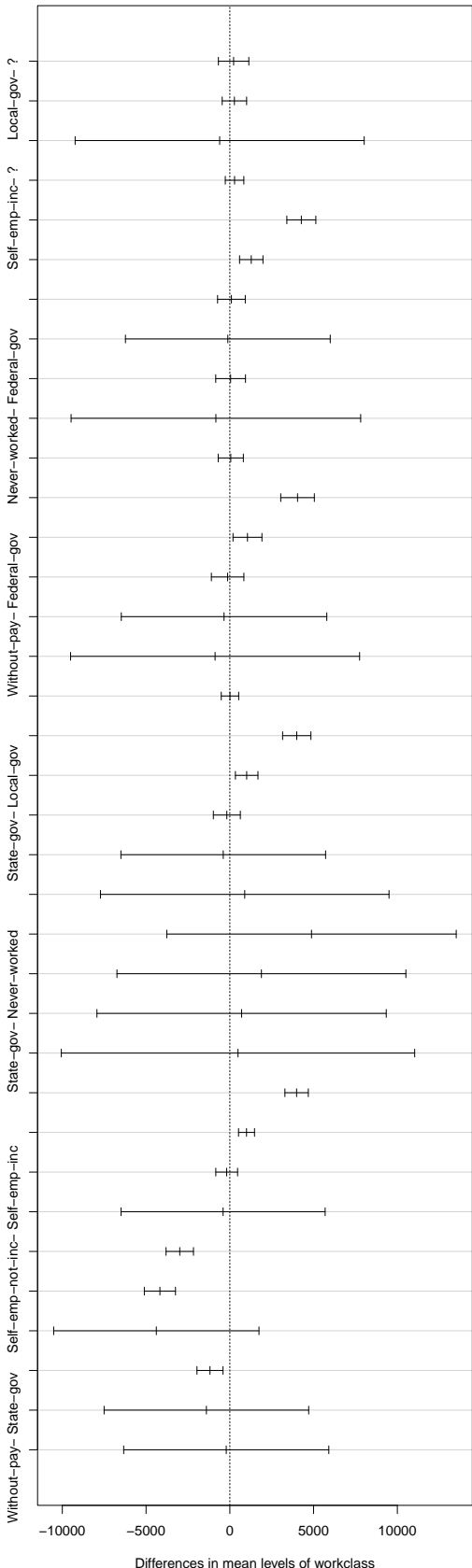
```
anov_wc <- aov(capital_gain ~ workclass, data = adult)
summary(anov_wc)
```

```
##              Df    Sum Sq  Mean Sq F value Pr(>F)
## workclass      8 1.931e+10 2.413e+09   44.72 <2e-16 ***
## Residuals    32552 1.757e+12 5.396e+07
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
#TukeyHSD(anov_wc)
```

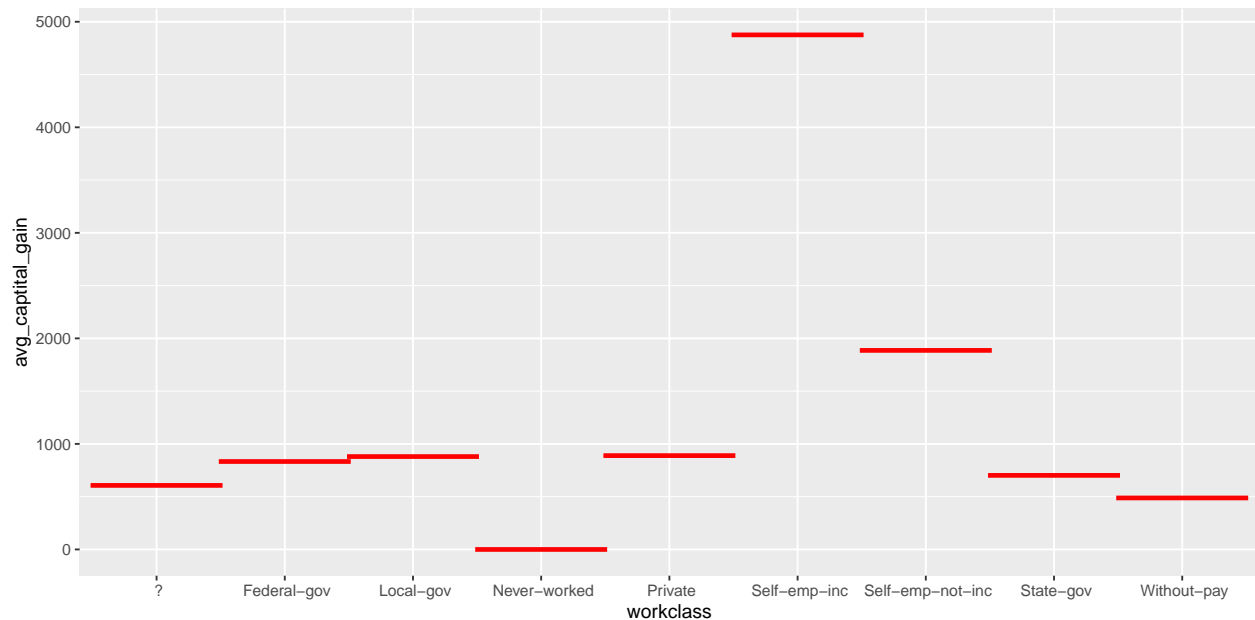
```
plot(TukeyHSD(aov(capital_gain ~ workclass, data = adult)))
```

95% family-wise confidence level



```
gain_wc<-adult %>%
  group_by(workclass) %>%
  summarize(avg_captital_gain=mean(capital_gain))

gain_wc %>%
  ggplot(aes(x=workclass, y=avg_captital_gain))+
  geom_tile(color="red",size=1)
```



Since the p-value in our ANOVA table (10^{-16}) is less than .05, we have sufficient evidence to reject the null hypothesis.

This means we have sufficient evidence to say that the mean capital gain is not equal across different workclass.

From the Tukey test, we can see the p-values for different occupation pairs, and the difference in average capital gain.

From the plots, we can see that the maximum average capital gain is in the occupation of Self-emp-inc.

Checking if average capital gain differs by education level

Motivation: we want to find out if the capital gain differs based on education level.

Assumptions:

1. The dataset is a random sample of original population.
2. The data comes from a normal distribution.
3. The sample size is large enough to conduct any test.
4. And the final assumptions is homogeneity of variance.

Hypothesis:

H0: capital gain is equal for education level

Ha: there exist a pair of education level for which capital gain is not equal.

```

# adult %>%
#   group_by(education) %>%
#   summarise(record_count = n())

anov_edu <- aov(capital_gain ~ education, data = adult)
summary(anov_edu)

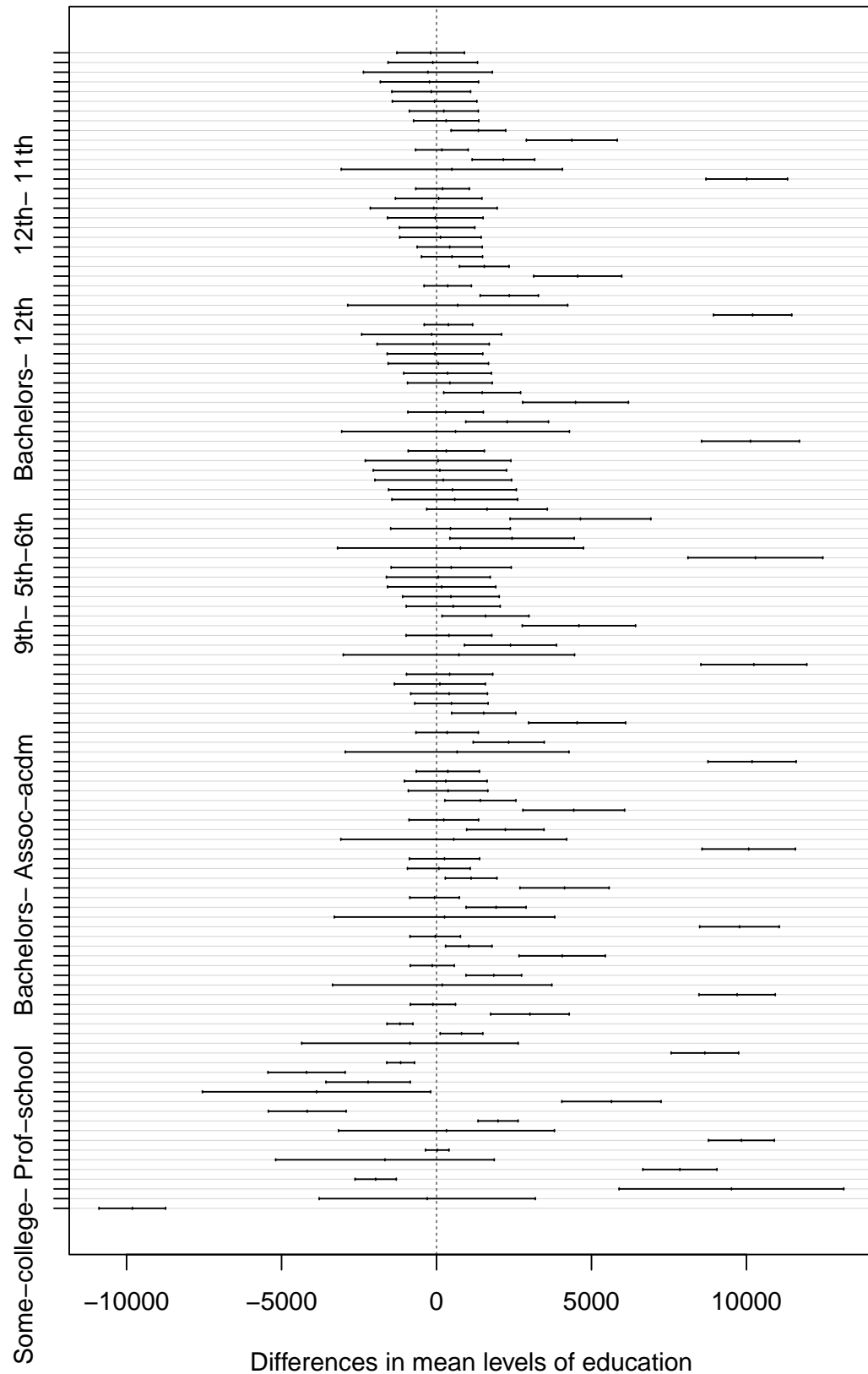
##              Df    Sum Sq  Mean Sq F value Pr(>F)
## education      15 6.953e+10 4.636e+09   88.41 <2e-16 ***
## Residuals  32545 1.706e+12 5.243e+07
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

#TukeyHSD(anov_edu)

plot(TukeyHSD(aov(capital_gain ~ education, data = adult)))

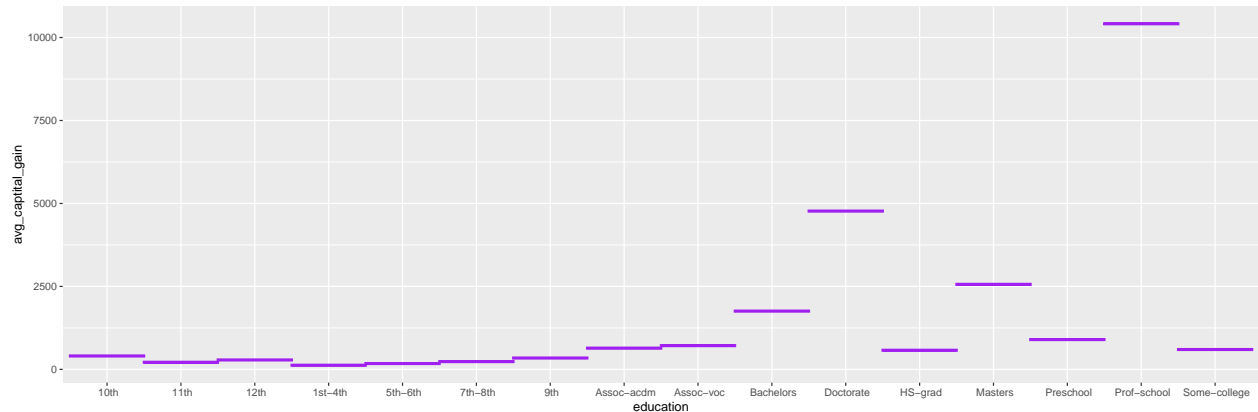
```

95% family-wise confidence level



```
gain_edu<-adult %>%
  group_by(education) %>%
  summarize(avg_captital_gain=mean(capital_gain))

gain_edu %>%
  ggplot(aes(x=education, y=avg_captital_gain))+
  geom_tile(color="purple",size=1)
```

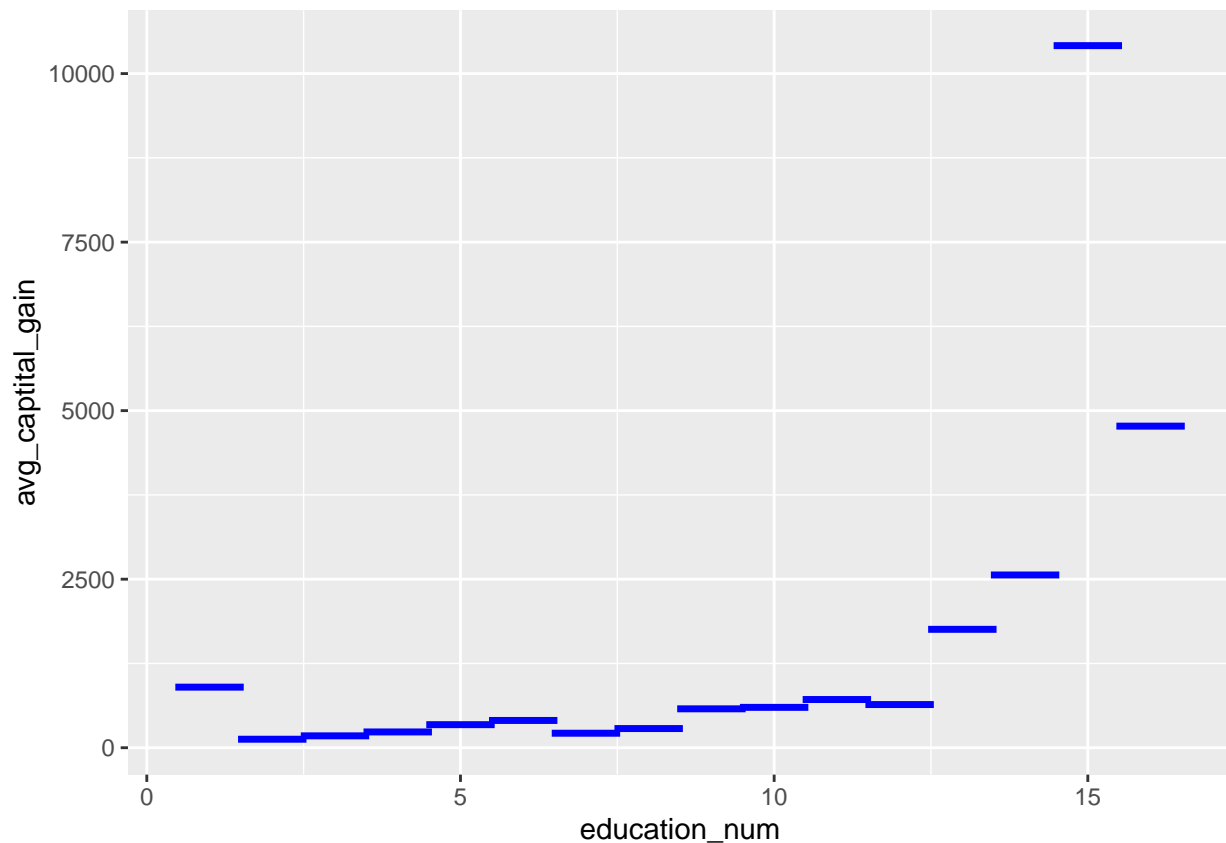


#Checking for education number

```
anov_edu_num <- aov(capital_gain ~ education_num, data = adult)
# summary(anov_edu_num)
# anov_edu_num

gain_edu_num<-adult %>%
  group_by(education_num) %>%
  summarize(avg_captital_gain=mean(capital_gain))

gain_edu_num %>%
  ggplot(aes(x=education_num, y=avg_captital_gain))+
  geom_tile(color="blue",size=1)
```

Since the p-value in our ANOVA table is less than .05, we have sufficient evidence to reject the null hypothesis. This means we have sufficient evidence to say that the mean capital gain is not equal across different education levels.

From the Tukey test, we can see the p-values for different education pairs, and the difference in average capital gain.

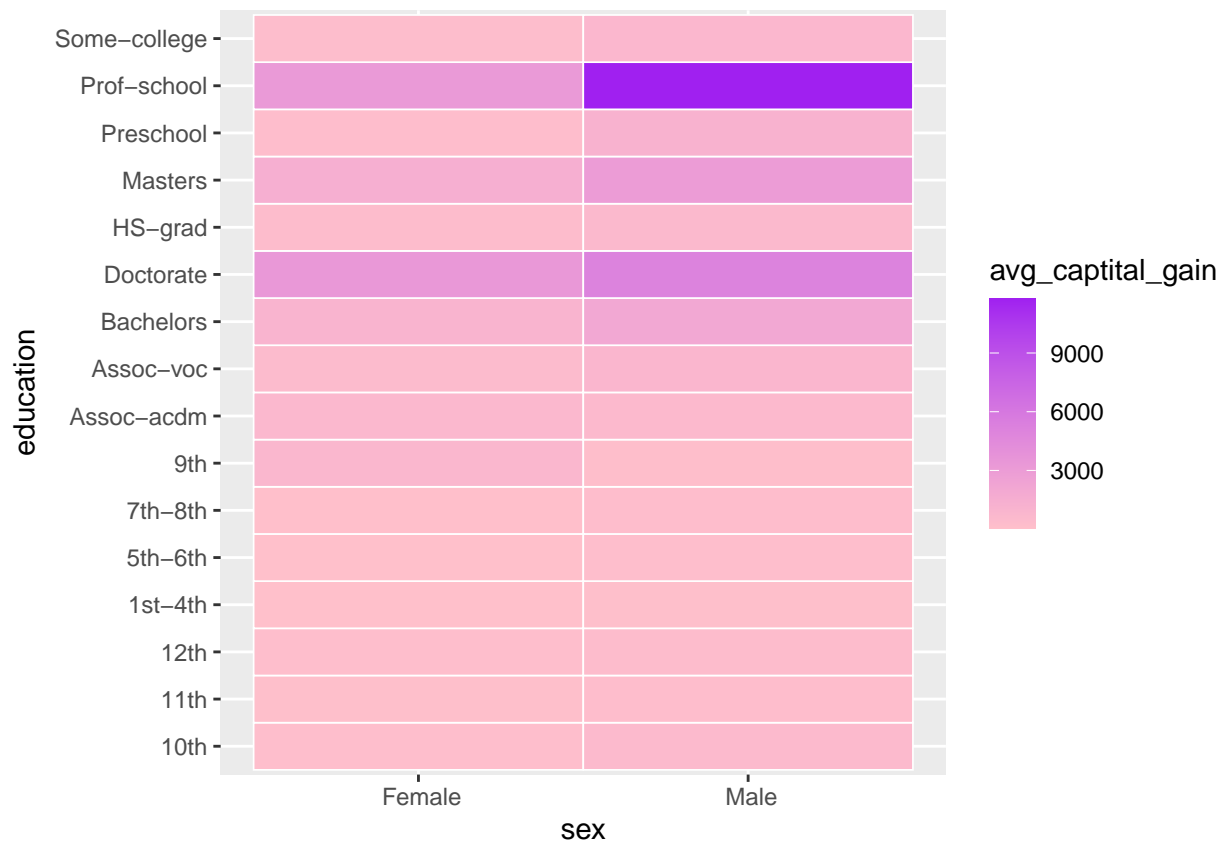
From the plots, we can see that the maximum average capital gain is with the education prof school.

Plotting gain on education and sex

```
education_sex<-adult %>%
  group_by(sex, education) %>%
  summarize(avg_capital_gain=mean(capital_gain))
```

```
## `summarise()` has grouped output by 'sex'. You can override using the `.groups`
## argument.
```

```
education_sex %>%
  ggplot(aes(x=sex,y=education,fill=avg_capital_gain))+
  geom_tile(color="white",size=0.3)+
  scale_fill_gradient(low="pink",high="purple")
```

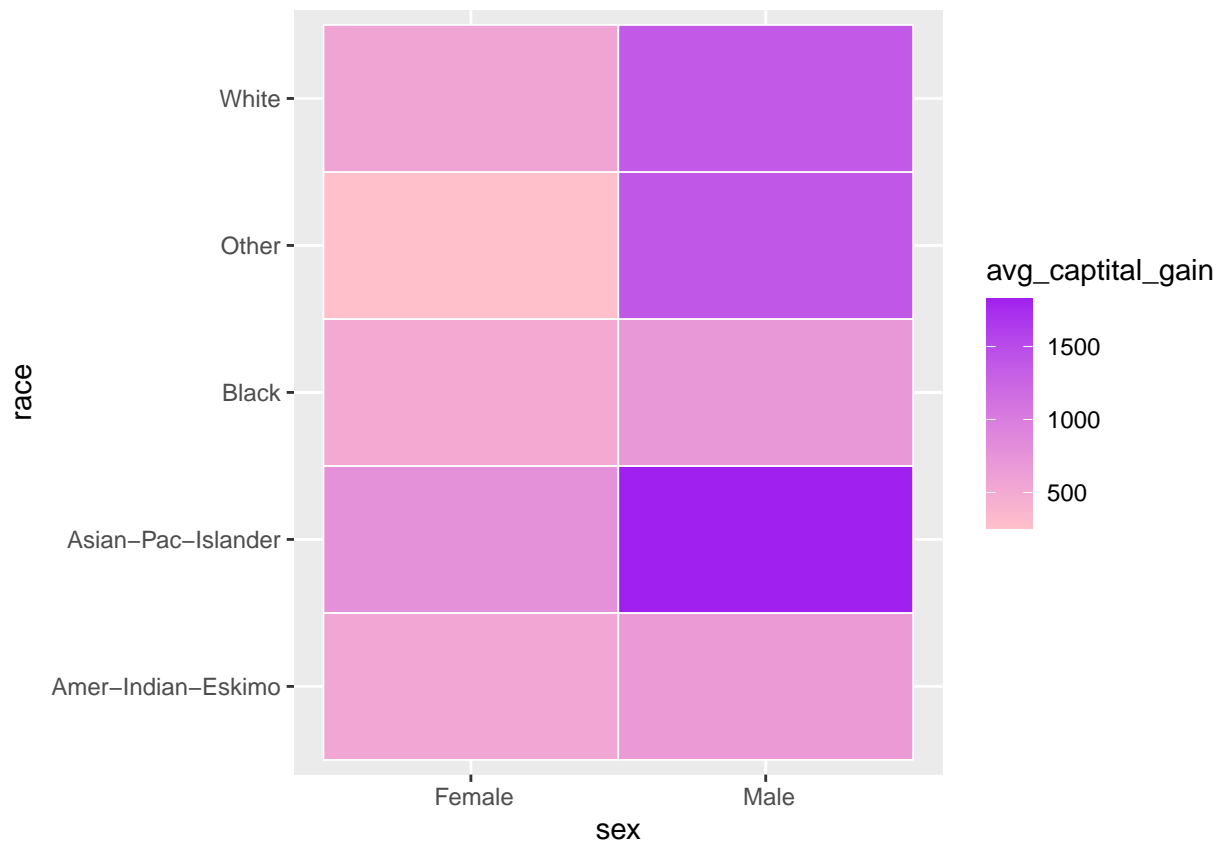


Plotting gain on race and sex

```
race_sex <- adult %>%
  group_by(sex, race) %>%
  summarize(avg_captital_gain = mean(capital_gain))
```

`summarise()` has grouped output by 'sex'. You can override using the `.groups`
argument.

```
race_sex %>%
  ggplot(aes(x=sex, y=race, fill=avg_captital_gain)) +
  geom_tile(color="white", size=0.3) +
  scale_fill_gradient(low="pink", high="purple")
```



Average capital gain vs earning greater than or less than or equal to 50k.

```
# adult %>%
#   group_by(fifty_k) %>%
#   summarise(record_count = n())

t.test(capital_gain ~ fifty_k, data=adult) # Unpooled

##
## Welch Two Sample t-test
##
## data: capital_gain by fifty_k
## t = -23.427, df = 7861.7, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group <=50K and group >50K is not equal to 0
## 95 percent confidence interval:
## -4180.166 -3534.614
## sample estimates:
## mean in group <=50K mean in group >50K
## 148.7525 4006.1425

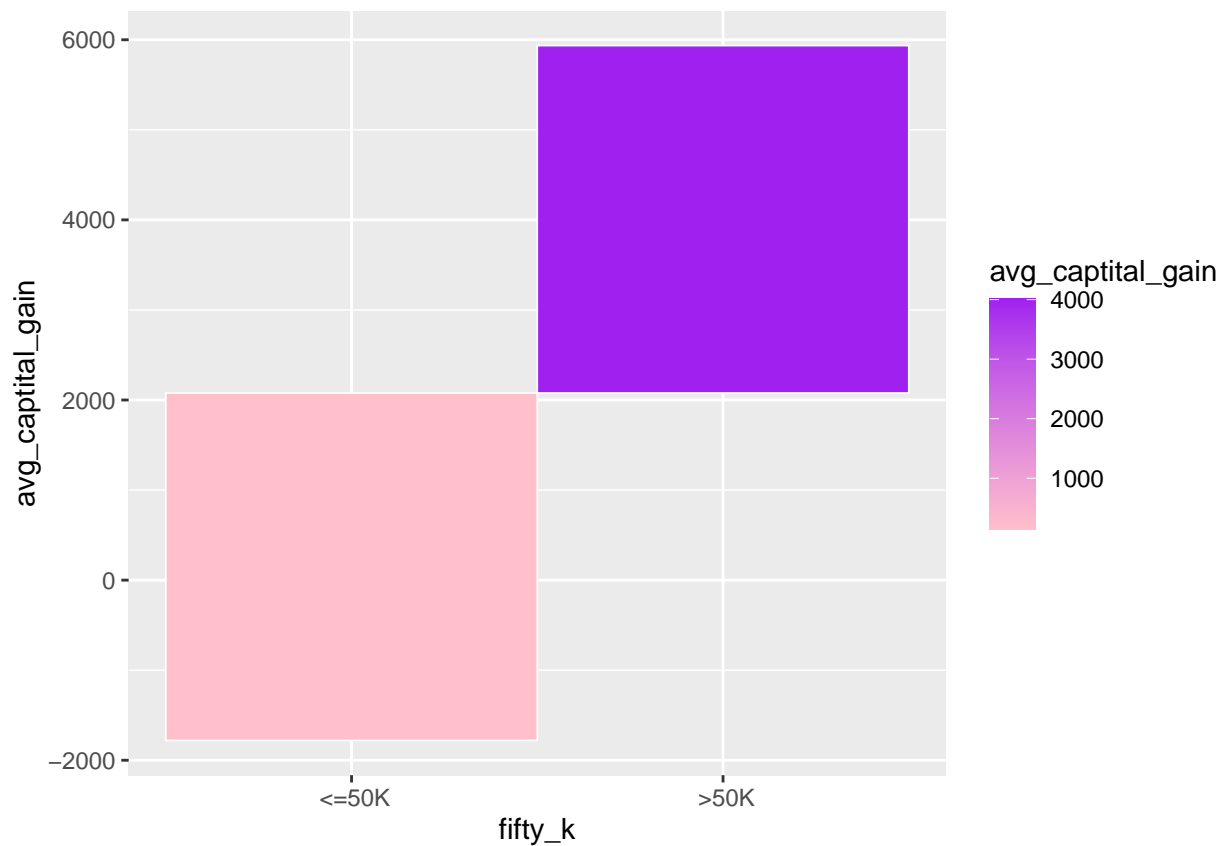
t.test(capital_gain ~ fifty_k, var.equal=TRUE, data=adult) # Pooled

##
## Two Sample t-test
```

```
##
## data: capital_gain by fifty_k
## t = -41.342, df = 32559, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group <=50K and group >50K is not equal to 0
## 95 percent confidence interval:
## -4040.271 -3674.509
## sample estimates:
## mean in group <=50K mean in group >50K
## 148.7525 4006.1425
```

```
gain_fifty<-adult %>%
  group_by(fifty_k) %>%
  summarize(avg_captital_gain=mean(capital_gain))

gain_fifty %>%
  ggplot(aes(x=fifty_k, y=avg_captital_gain,fill=avg_captital_gain))+
  geom_tile(color="white",size=0.3)+
  scale_fill_gradient(low="pink",high="purple")
```



Looking at the p value which is close to 0, we can reject the null hypothesis.

We have evidence that suggests that the true difference in means between group that earns less than or equal to 50k and more than 50 is not equal to 0.

We have evidence to say that there is a significant difference in the average capital gain.

Checking if average capital gain differs by marital status

```
# adult %>%
#   group_by(race) %>%
#   summarise(record_count = n())

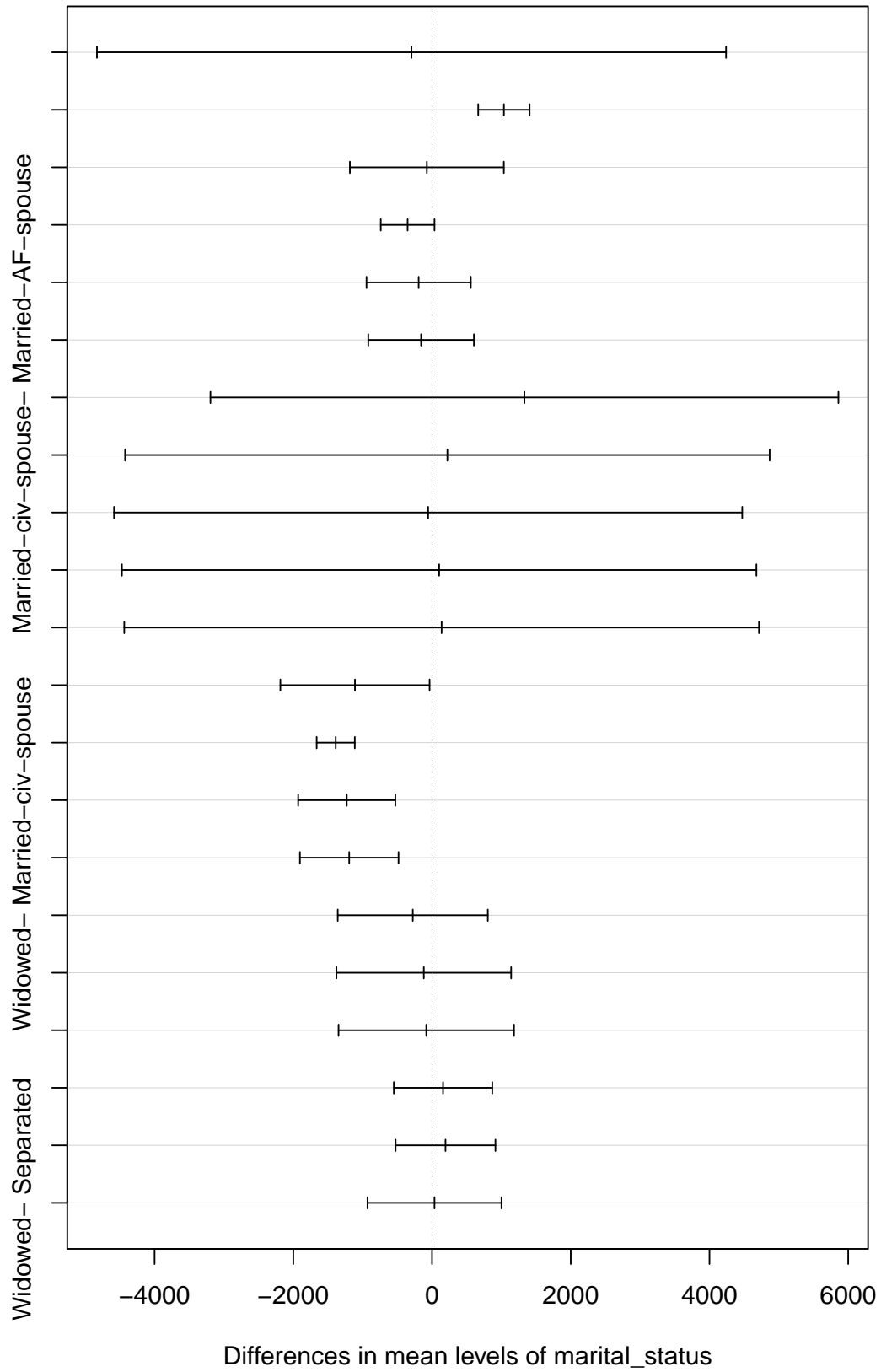
anov_race <- aov(capital_gain ~ marital_status, data = adult)
summary(anov_race)

##              Df    Sum Sq   Mean Sq F value Pr(>F)
## marital_status    6 1.351e+10 2.251e+09   41.58 <2e-16 ***
## Residuals       32554 1.762e+12 5.414e+07
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

#TukeyHSD(anov_race)

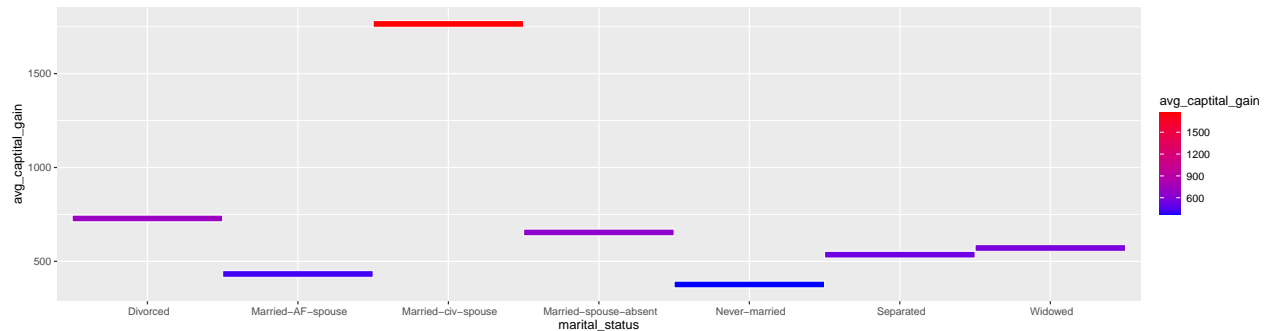
plot(TukeyHSD(aov(capital_gain ~ marital_status, data = adult)))
```

95% family-wise confidence level



```
gain_marital<-adult %>%
  group_by(marital_status) %>%
  summarize(avg_captital_gain=mean(capital_gain))

gain_marital %>%
  ggplot(aes(x=marital_status, y=avg_captital_gain,fill=avg_captital_gain))+
  geom_tile(color="white",size=0.3)+
  scale_fill_gradient(low="blue",high="red")
```



Since the p-value in our ANOVA table is less than .05, we have sufficient evidence to reject the null hypothesis. This means we have sufficient evidence to say that the mean capital gain is not equal across different marital-status.

From the Tukey test, we can see the p-values for different marital status pairs, and the difference in average capital gain.

From the plots, we can see that the maximum average capital gain is with married-civ-spouse.

Checking if average capital gain differs by native country

Motivation: we want to find out if the capital gain differs based on native country.

Assumptions:

1. The dataset is a random sample of original population.
2. The data comes from a normal distribution.
3. The sample size is large enough to conduct any test.
4. And the final assumptions is homogeneity of variance.

Hypothesis:

H0: capital gain is equal for different native countries

Ha: there exist a pair of native countries for which capital gain is not equal.

```
# adult %>%
#   group_by(native_country) %>%
#   summarise(record_count = n())

anov_country <- aov(capital_gain ~ native_country, data = adult)
summary(anov_country)
```

```
##           Df    Sum Sq Mean Sq F value Pr(>F)
## native_country    41 2.256e+09 55022066   1.009  0.455
## Residuals      32519 1.774e+12 54541935
```

The figure is a horizontal box plot titled 'avg. column sum'. The y-axis is labeled 'avg. column sum' and has a logarithmic scale with major ticks at 0, 100, 1000, and 10000. The x-axis lists 40 models: 1, Cascade, Cbtree, Cbr, Cbr2, Cbr3, Cbr4, Cbr5, Cbr6, Cbr7, Cbr8, Cbr9, Cbr10, Cbr11, Cbr12, Cbr13, Cbr14, Cbr15, Cbr16, Cbr17, Cbr18, Cbr19, Cbr20, Cbr21, Cbr22, Cbr23, Cbr24, Cbr25, Cbr26, Cbr27, Cbr28, Cbr29, Cbr30, Cbr31, Cbr32, Cbr33, Cbr34, Cbr35, Cbr36, Cbr37, Cbr38, Cbr39, Cbr40. The plot shows the distribution of the average column sum for each model. The 'Ada' model has the highest average column sum, followed by 'Ada2', 'Ada3', and 'Ada4'. 'Ada5' has a very low average column sum, near 0. Most other models have average column sums between 100 and 1000.

Model	Approx. Median avg. column sum
1	1500
Cascade	100
Cbtree	300
Cbr	40
Cbr2	30
Cbr3	40
Cbr4	300
Cbr5	40
Cbr6	50
Cbr7	40
Cbr8	80
Cbr9	90
Cbr10	40
Cbr11	150
Cbr12	40
Cbr13	40
Cbr14	40
Cbr15	40
Cbr16	40
Cbr17	40
Cbr18	40
Cbr19	40
Cbr20	40
Cbr21	40
Cbr22	40
Cbr23	40
Cbr24	40
Cbr25	40
Cbr26	40
Cbr27	40
Cbr28	40
Cbr29	40
Cbr30	40
Cbr31	40
Cbr32	40
Cbr33	40
Cbr34	40
Cbr35	40
Cbr36	40
Cbr37	40
Cbr38	40
Cbr39	40
Cbr40	40
Ada	10000
Ada2	2000
Ada3	4000
Ada4	4000
Ada5	10
Ada6	40
Ada7	40
Ada8	40
Ada9	40
Ada10	40
Ada11	40
Ada12	40
Ada13	40
Ada14	40
Ada15	40
Ada16	40
Ada17	40
Ada18	40
Ada19	40
Ada20	40
Ada21	40
Ada22	40
Ada23	40
Ada24	40
Ada25	40
Ada26	40
Ada27	40
Ada28	40
Ada29	40
Ada30	40
Ada31	40
Ada32	40
Ada33	40
Ada34	40
Ada35	40
Ada36	40
Ada37	40
Ada38	40
Ada39	40
Ada40	40

This means we do not have sufficient evidence to say that the mean capital gain is not equal across different native countries.

Real Estate data set: Real Estate

```
##           No           X1.transaction.date  X2.house.age
##  Min.      : 1.0      Min.      :2013      Min.      : 0.000
##  1st Qu.:104.2      1st Qu.:2013      1st Qu.: 9.025
##  Median :207.5      Median :2013      Median :16.100
##  Mean     :207.5      Mean     :2013      Mean     :17.713
##  3rd Qu.:310.8      3rd Qu.:2013      3rd Qu.:28.150
##  Max.      :414.0      Max.      :2014      Max.      :43.800
##  X3.distance.to.the.nearest.MRT.station X4.number.of.convenience.stores
##  Min.      : 23.38                                Min.      : 0.000
##  1st Qu.: 289.32                                1st Qu.: 1.000
##  Median   : 492.23                                Median   : 4.000
##  Mean     :1083.89                                Mean     : 4.094
##  3rd Qu.:1454.28                                3rd Qu.: 6.000
```

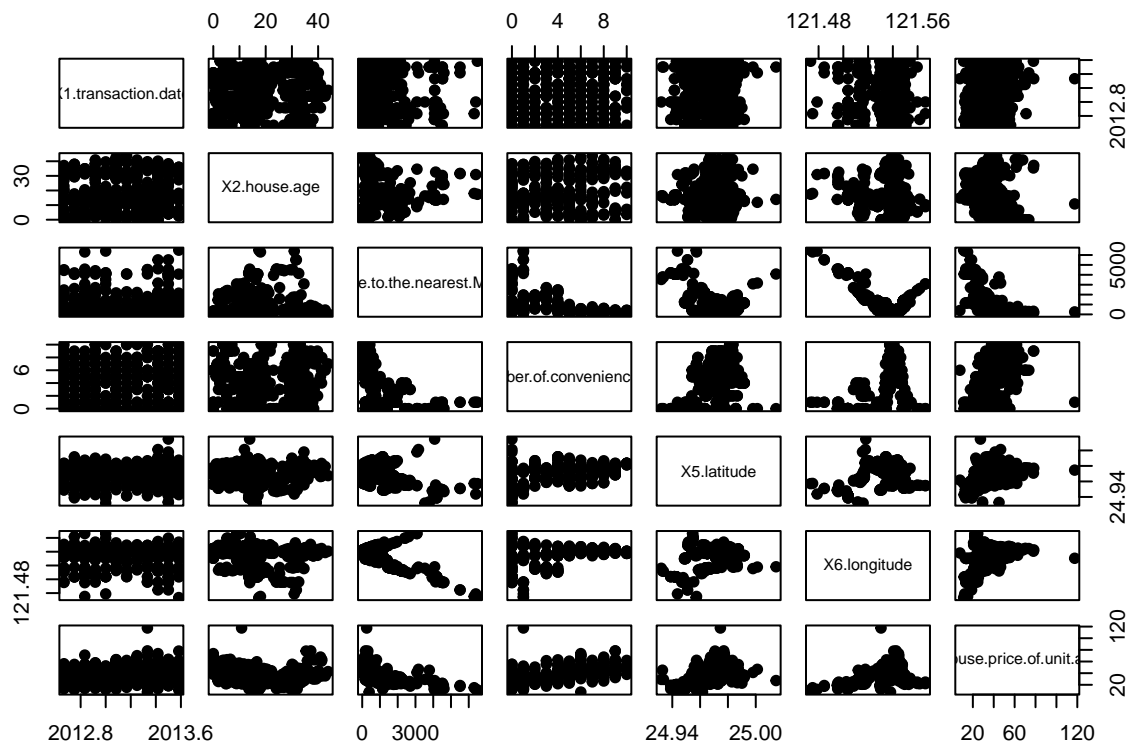


```
## Max. :6488.02 Max. :10.000
## X5.latitude X6.longitude Y.house.price.of.unit.area
## Min. :24.93 Min. :121.5 Min. : 7.60
## 1st Qu.:24.96 1st Qu.:121.5 1st Qu.: 27.70
## Median :24.97 Median :121.5 Median : 38.45
## Mean :24.97 Mean :121.5 Mean : 37.98
## 3rd Qu.:24.98 3rd Qu.:121.5 3rd Qu.: 46.60
## Max. :25.01 Max. :121.6 Max. :117.50
```

```
ls(real_estate)
```

```
## [1] "No"
## [2] "X1.transaction.date"
## [3] "X2.house.age"
## [4] "X3.distance.to.the.nearest.MRT.station"
## [5] "X4.number.of.convenience.stores"
## [6] "X5.latitude"
## [7] "X6.longitude"
## [8] "Y.house.price.of.unit.area"
```

```
pairs(real_estate[,2:8], pch=19)
```

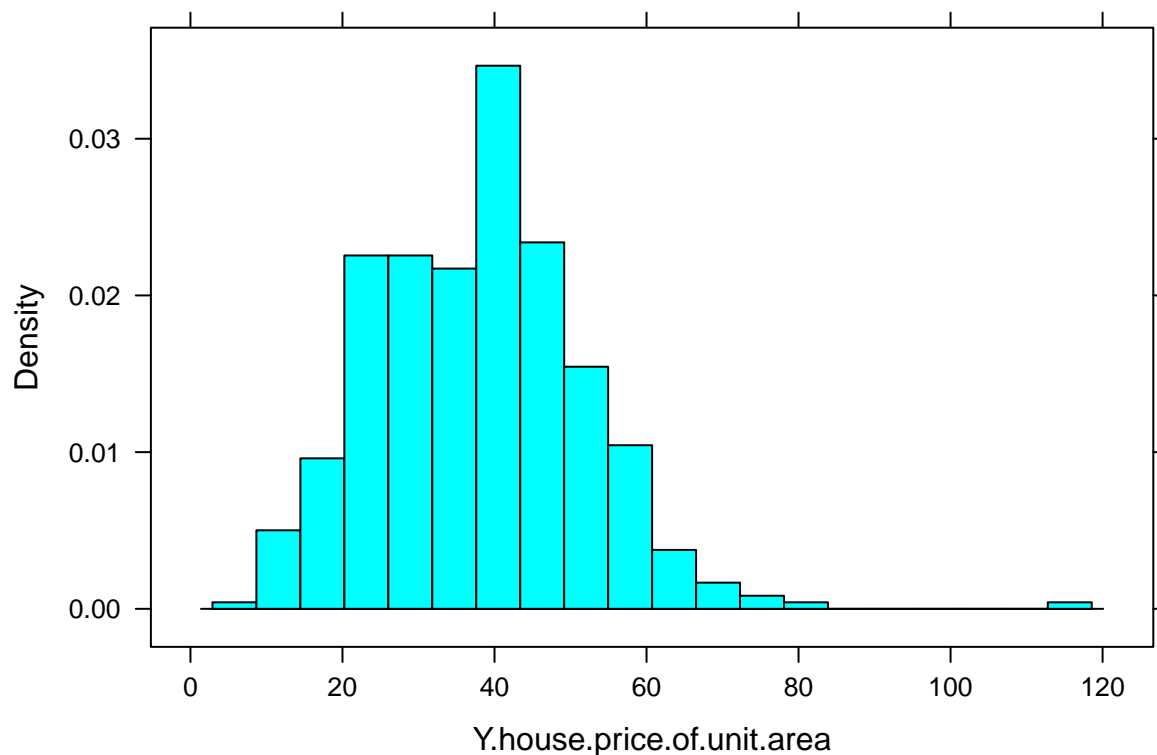


```
#xyplot(Y.house.price.of.unit.area ~ X4.number.of.convenience.stores,data=real_estate) # positive trend
#xyplot(Y.house.price.of.unit.area ~ X3.distance.to.the.nearest.MRT.station,data=real_estate) # negative trend
```

```
# study with distance to metro station.
```

```
#check value distribution.
```

```
histogram(~Y.house.price.of.unit.area, data=real_estate, nint=20)
```



```
#check correlation between house price and distance to metro station.
cor(Y.house.price.of.unit.area ~ X3.distance.to.the.nearest.MRT.station, data=real_estate) # -0.673
```

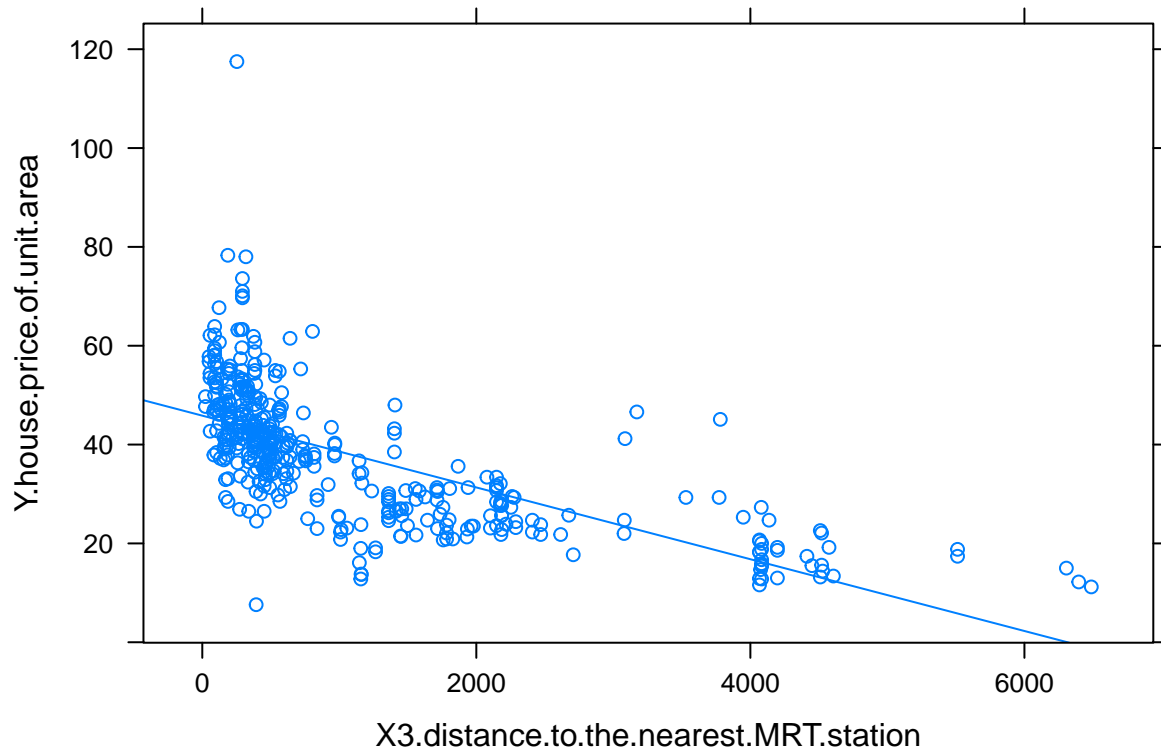
```
## [1] -0.6736129
```

```
#the least squares line regression line.
m1 <- lm(Y.house.price.of.unit.area ~ X3.distance.to.the.nearest.MRT.station, data=real_estate)
summary(m1)
```

```
##
## Call:
## lm(formula = Y.house.price.of.unit.area ~ X3.distance.to.the.nearest.MRT.station,
##     data = real_estate)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -35.396  -6.007  -1.195   4.831  73.483
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    45.8514271   0.6526105   70.26  <2e-16
## X3.distance.to.the.nearest.MRT.station -0.0072621   0.0003925  -18.50  <2e-16
##
## (Intercept)          ***
## X3.distance.to.the.nearest.MRT.station ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 10.07 on 412 degrees of freedom
## Multiple R-squared:  0.4538, Adjusted R-squared:  0.4524
## F-statistic: 342.2 on 1 and 412 DF, p-value: < 2.2e-16
```

```
#xy plot
```

```
xyplot(Y.house.price.of.unit.area ~ X3.distance.to.the.nearest.MRT.station, data=real_estate, type=c("p",
```



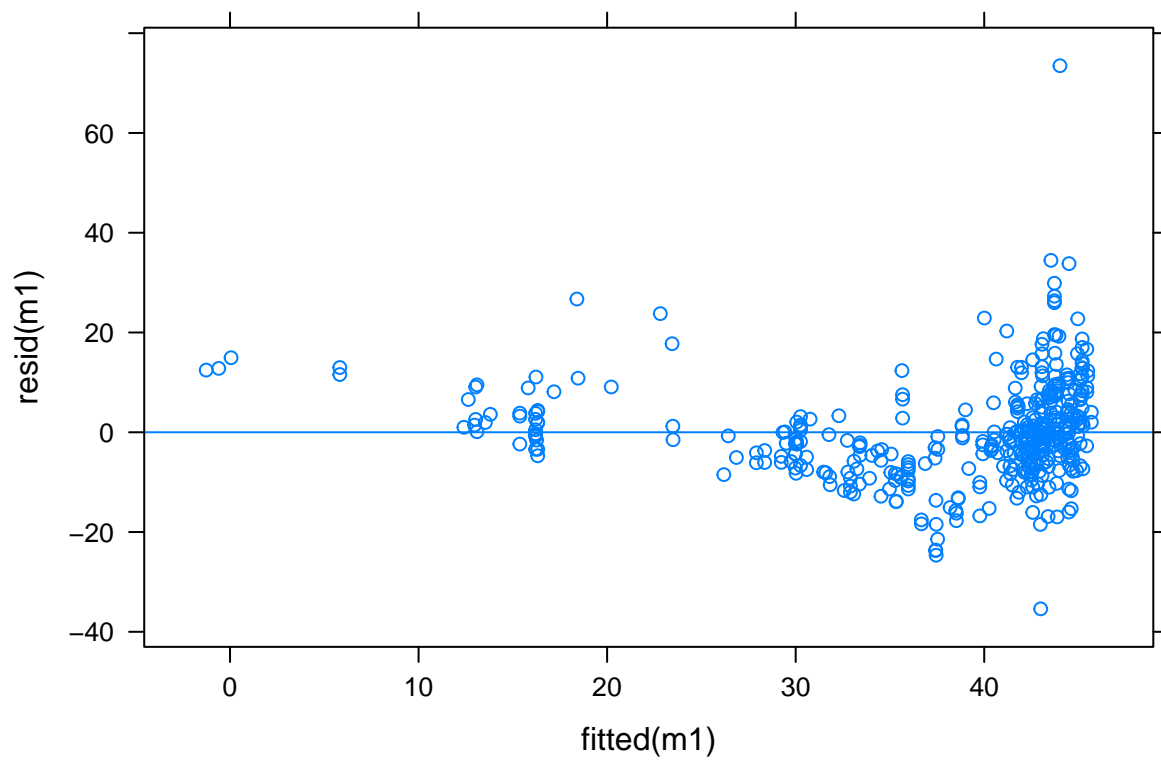
As-

sumption Check:

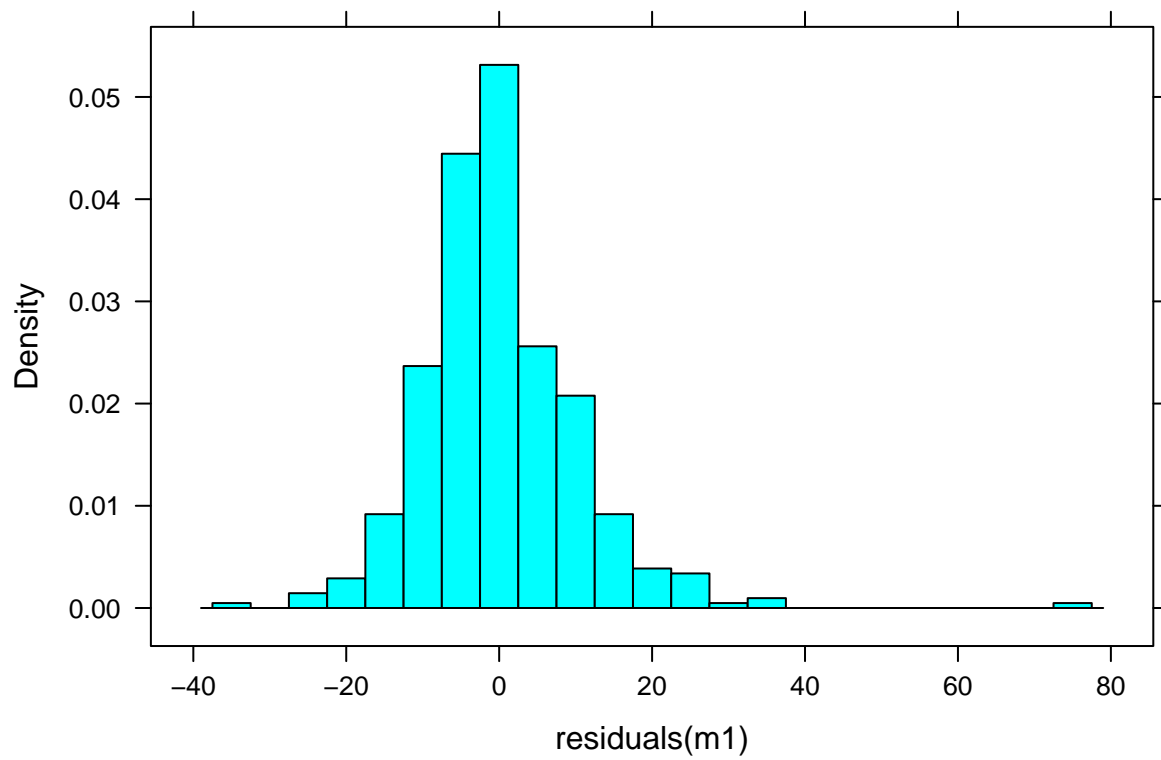
1. Residual are uniformly distributed around $y=0$ horizontal line.
2. Residual follows normal distribution.
3. The relationship between two variables should be linear.
4. The observation should be independent of each other.

```
#normalty check of errors/residual and assumptions check *
```

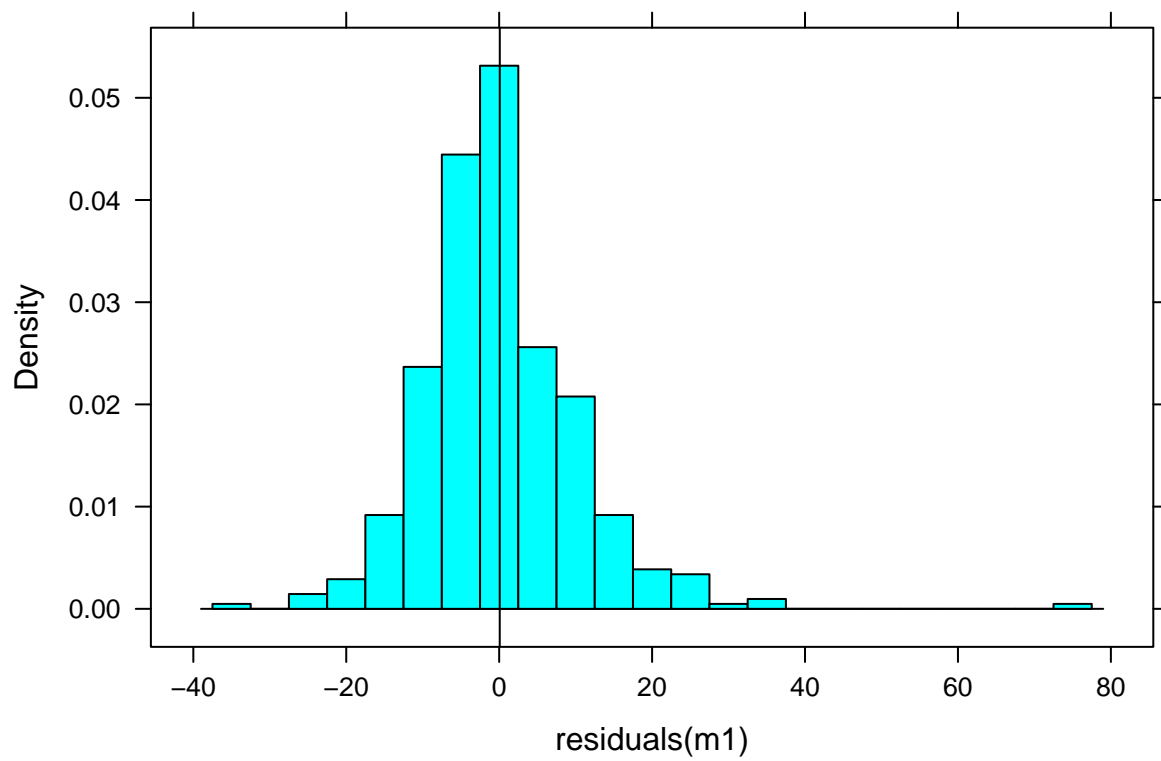
```
xyplot(resid(m1)~fitted(m1), data=real_estate, type=c("p","r"))
```



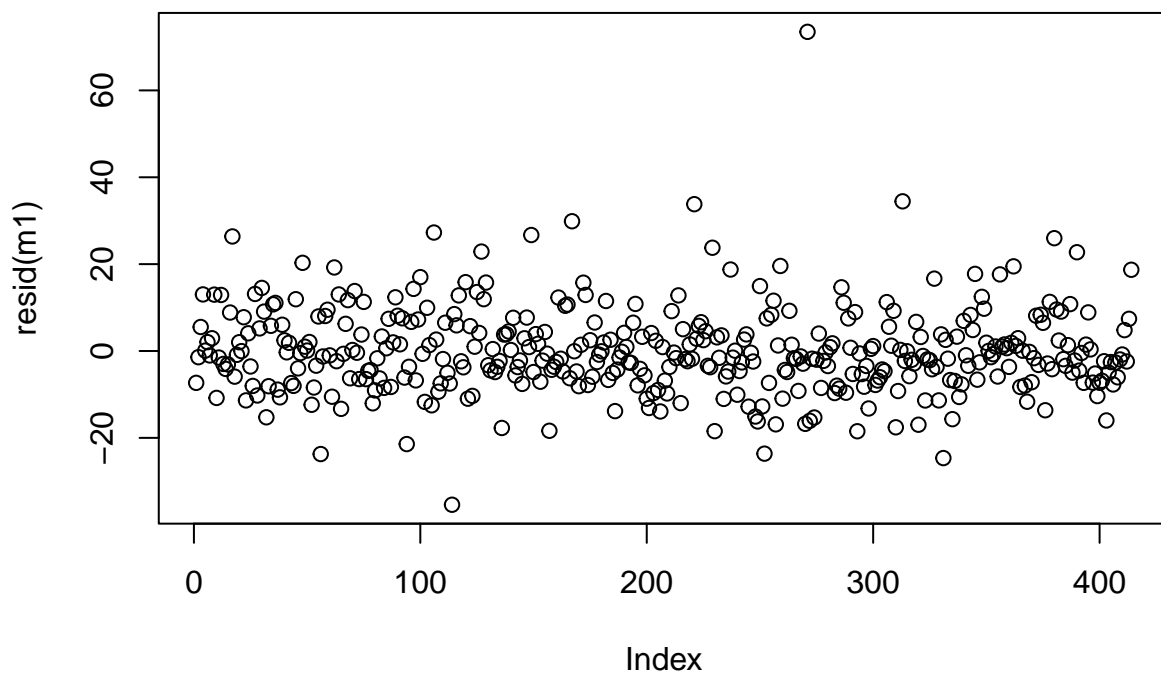
```
histogram(residuals(m1),width=5)
```



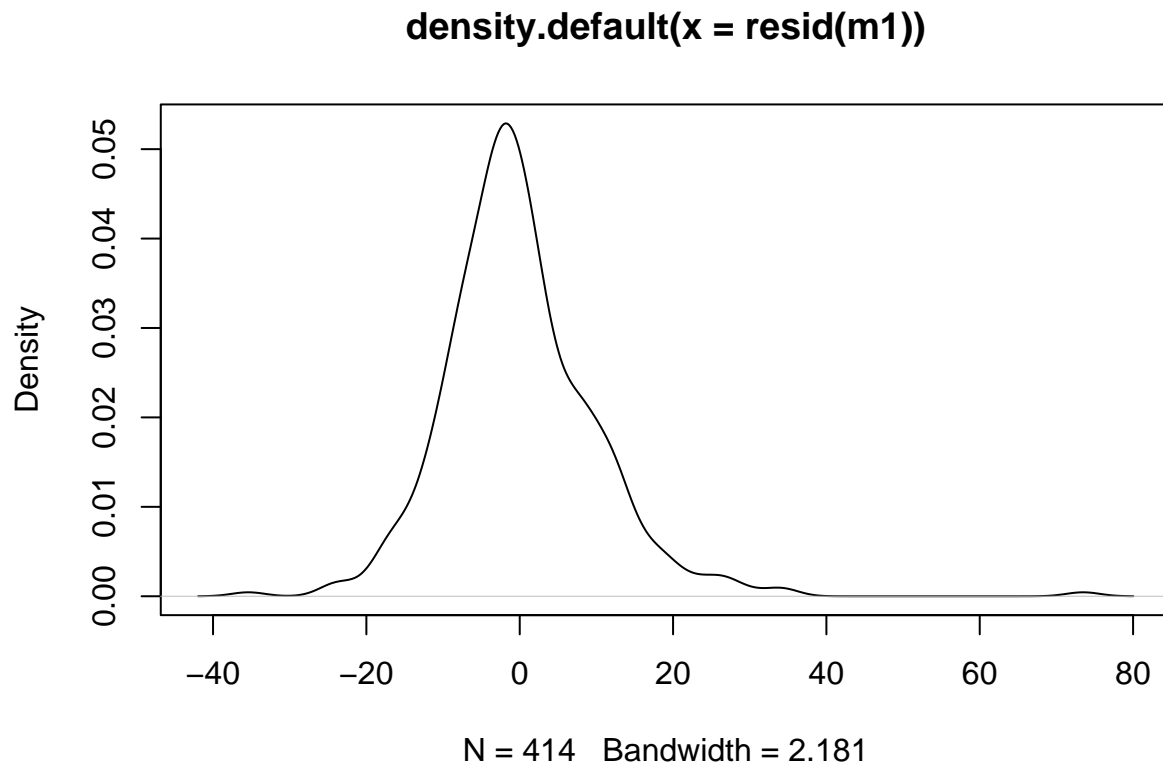
```
ladd(panel.qqmathline(resid(m1)))
```



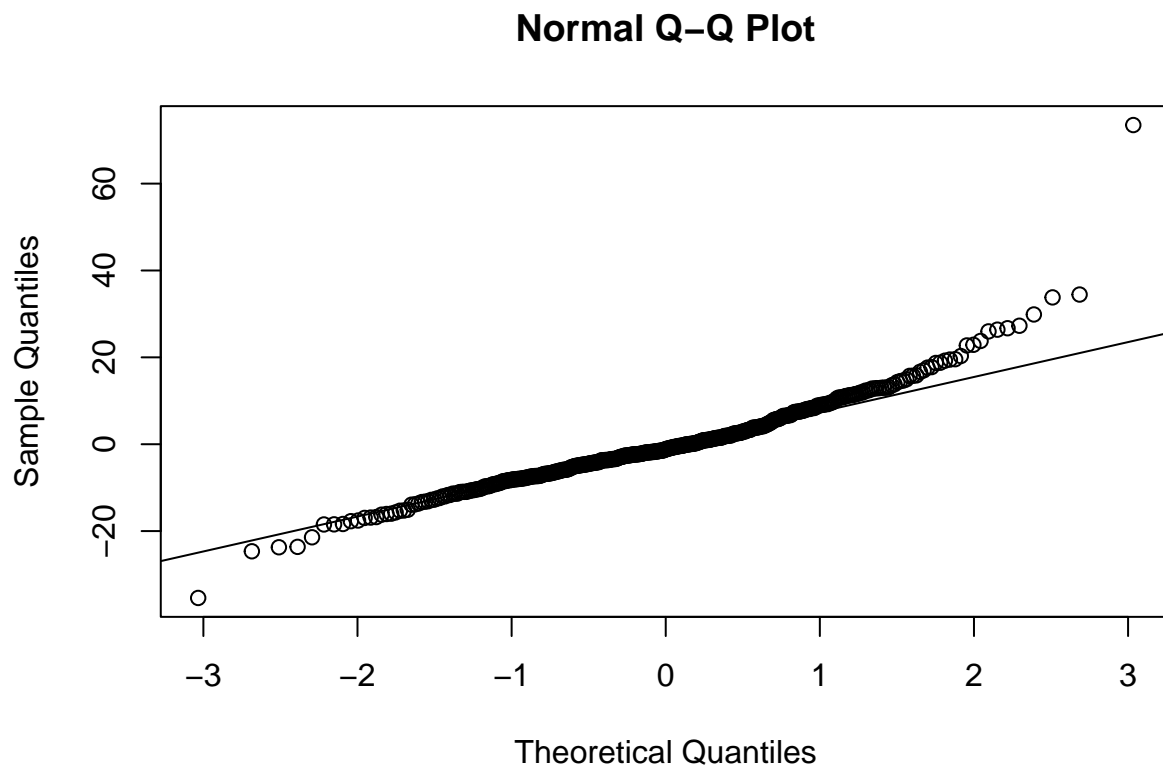
```
plot(resid(m1))
```



```
plot(density(resid(m1)))
```



```
qqnorm(resid(m1))
qqline(resid(m1))
```



clusion:

All assumptions holds here. From differnt graphs we can see that the conditions for linear model fitting holds.

#Checking if house price varies with number of convenience stores:

```
m2 <- lm(Y.house.price.of.unit.area ~ X4.number.of.convenience.stores, data=real_estate)
summary(m2)
```

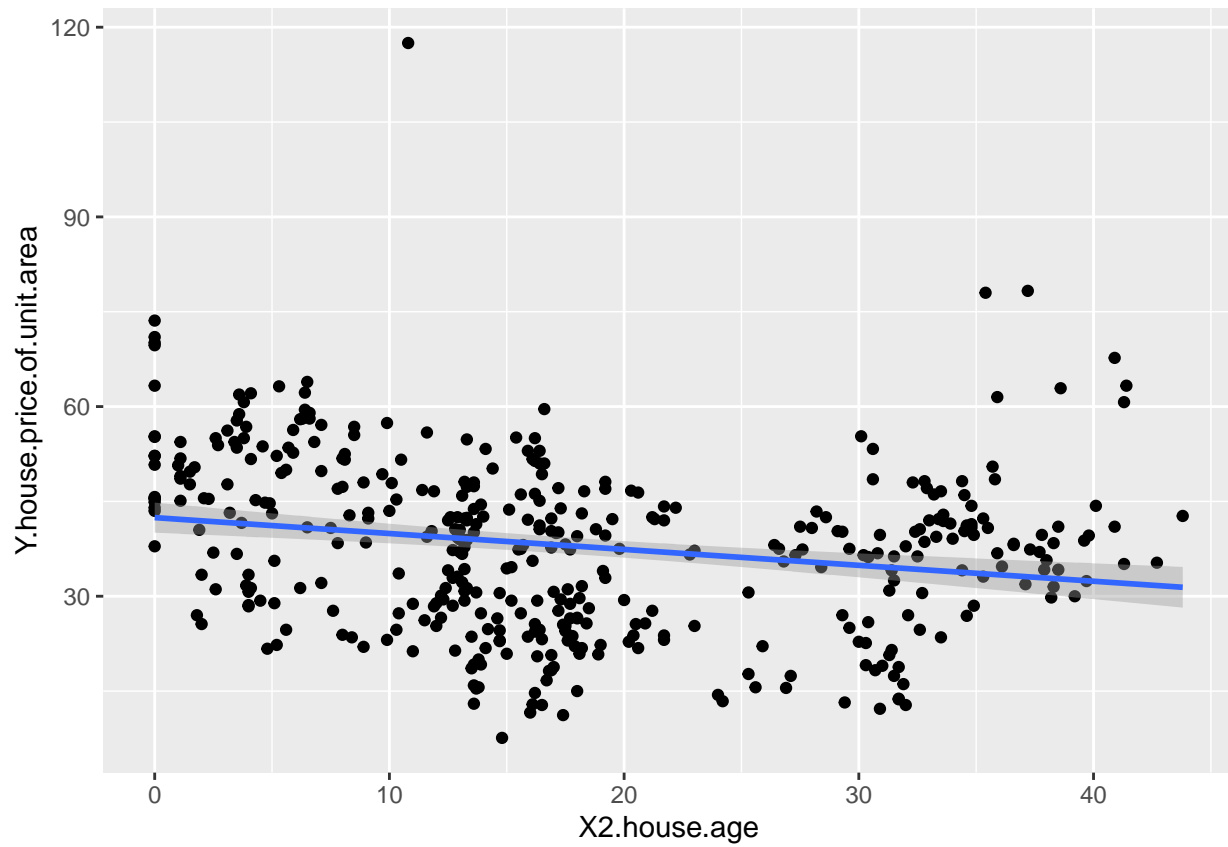
```
##
## Call:
## lm(formula = Y.house.price.of.unit.area ~ X4.number.of.convenience.stores,
##     data = real_estate)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -35.407  -7.341  -1.788   5.984  87.681
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      27.1811     0.9419   28.86  <2e-16 ***
## X4.number.of.convenience.stores  2.6377     0.1868   14.12  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 11.18 on 412 degrees of freedom
## Multiple R-squared:  0.326, Adjusted R-squared:  0.3244
## F-statistic: 199.3 on 1 and 412 DF, p-value: < 2.2e-16
```

```
m3 <- lm(Y.house.price.of.unit.area ~ X2.house.age, data=real_estate)
summary(m3)
```

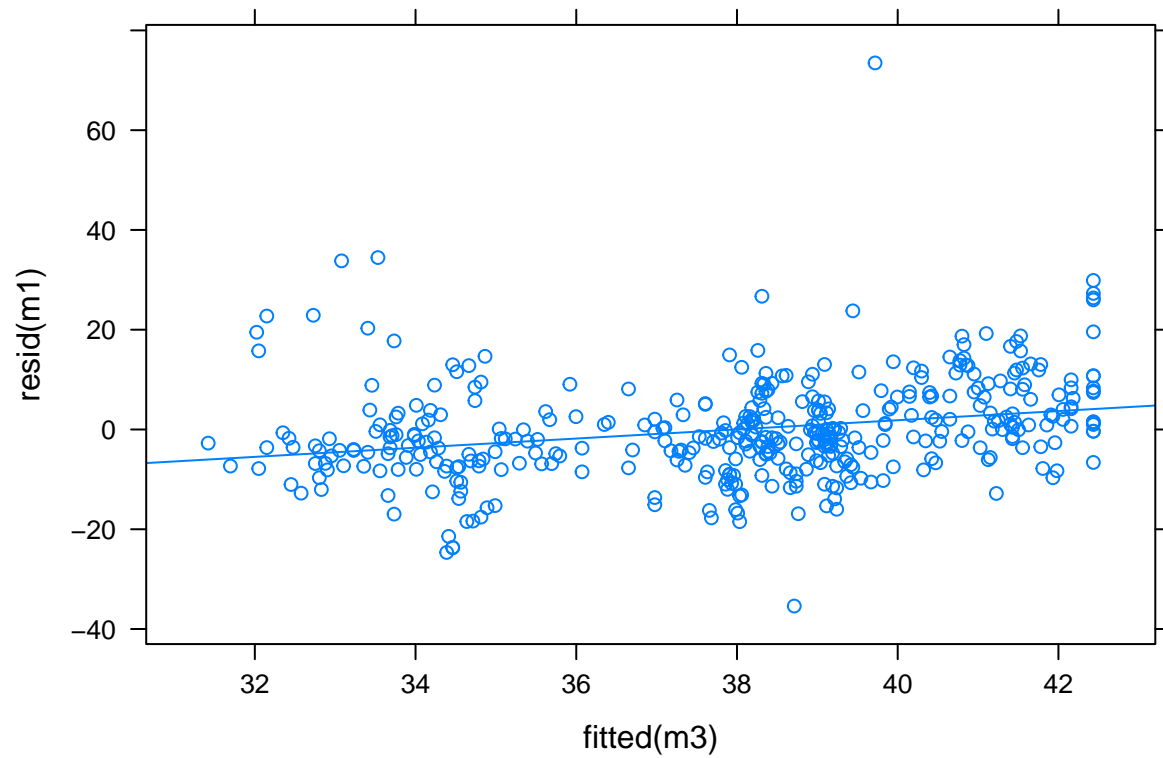
```
##
## Call:
## lm(formula = Y.house.price.of.unit.area ~ X2.house.age, data = real_estate)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -31.113 -10.738   1.626   8.199  77.781
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  42.43470     1.21098   35.042  < 2e-16 ***
## X2.house.age -0.25149     0.05752   -4.372 1.56e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.32 on 412 degrees of freedom
## Multiple R-squared:  0.04434, Adjusted R-squared:  0.04202
## F-statistic: 19.11 on 1 and 412 DF, p-value: 1.56e-05
```

```
ggplot(real_estate, aes( X2.house.age, Y.house.price.of.unit.area)) + geom_point() + stat_smooth(method
```

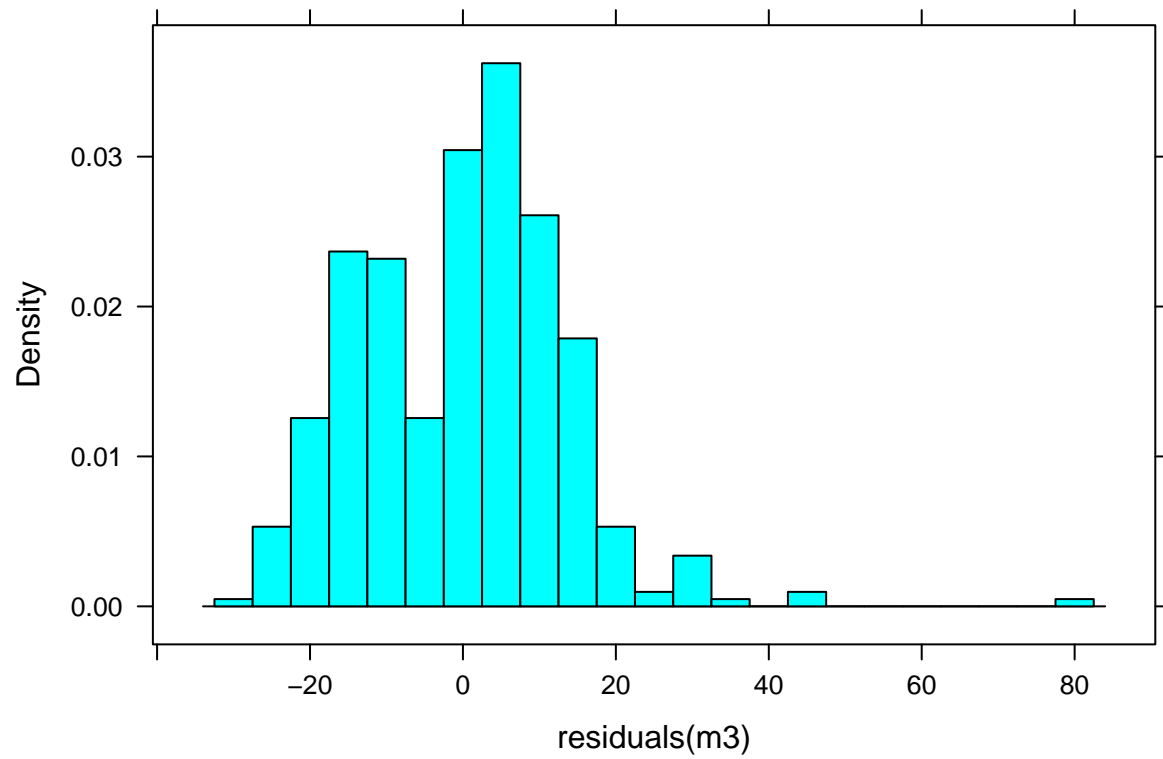
```
## `geom_smooth()` using formula 'y ~ x'
```



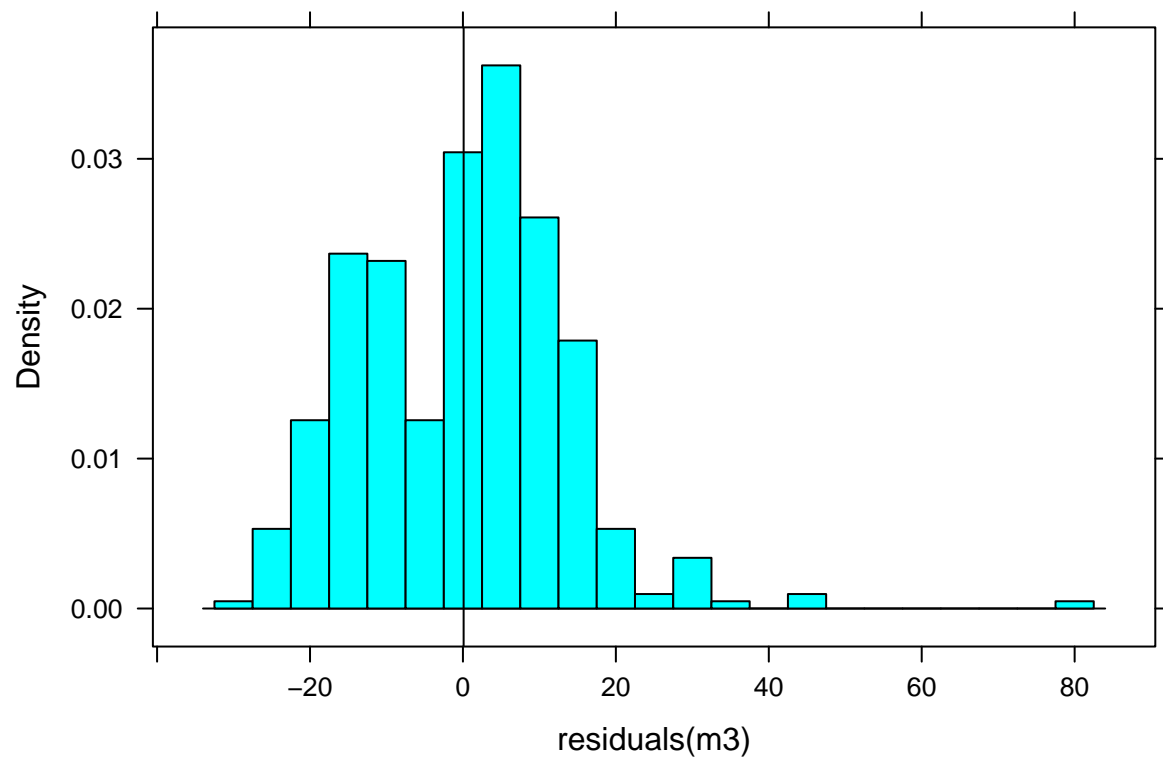
```
xyplot(resid(m1)~fitted(m3), data=real_estate, type=c("p","r"))
```



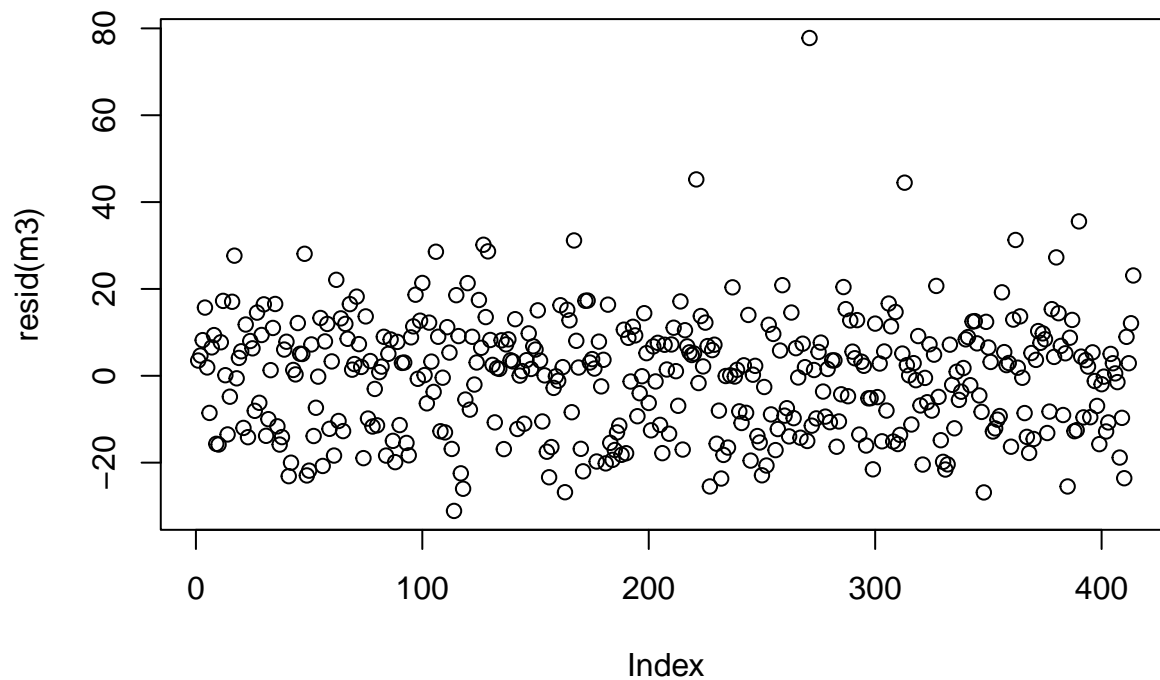

```
histogram(residuals(m3),width=5)
```



```
ladd(panel.qqmathline(resid(m3)))
```

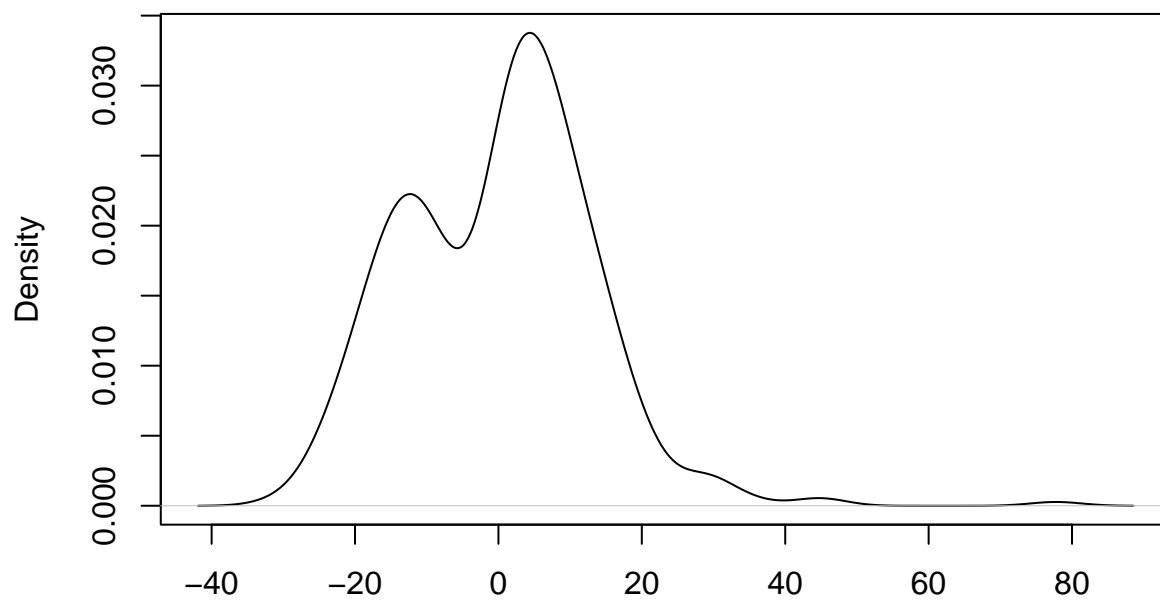


```
plot(resid(m3))
```



```
plot(density(resid(m3)))
```

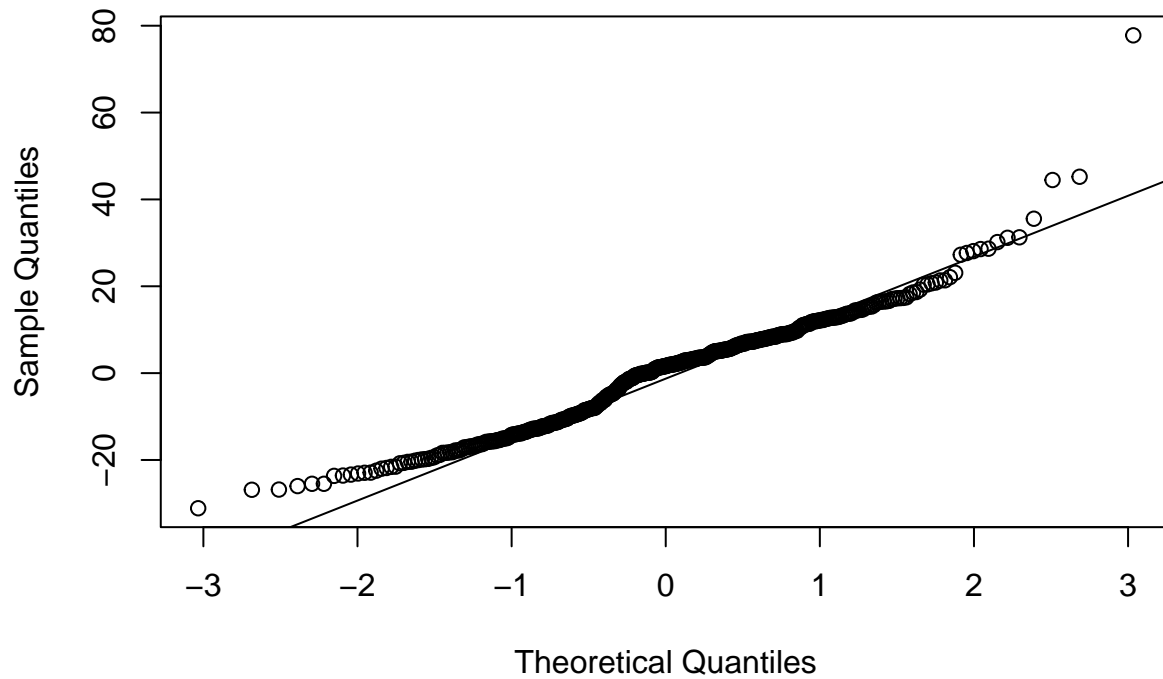
density.default(x = resid(m3))



N = 414 Bandwidth = 3.587

```
qqnorm(resid(m3))
qqline(resid(m3))
```

Normal Q-Q Plot



Conclusion:

From the above graphs, the relationship between house price and house age is not linear, and from Q_Q plot also, we can see that the residuals are not on a straight lines and uniform distribution of error around $y=0$ horizontal lines doesn't hold also, so we should not use linear model to predict the house price based on house age. And if we build the model, we can see that the R-squared value is around 4%, which also indicates linear model is not suitable to predict the house price based on house age.