Stats 501 final Project

Debabrata Halder, Piusha Gullapalli, Snehil Verma

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Attribute Information:

Parameters -

age: the age of an individual

workclass: a general term to represent the employment status of an individual

fnlwgt: final weight. This is the number of people the census believes the entry represents.

education: the highest level of education achieved by an individual.

education_num: the highest level of education achieved in numerical form.

marital_status: marital status of an individual.

occupation: the general type of occupation of an individual

relationship: represents what this individual is relative to others.

race: Descriptions of an individual's race

sex: the sex of the individual

capital_gain: capital gains for an individual

capital_loss: capital loss for an individual

hours_per_week: the hours an individual has reported to work per week

native_country: country of origin for an individual

NOTE: Some values in the dataset is marked as "?". It means the value is unknown. ## Load Data

```
adult <- read.table("adult.data", sep = ",")
colnames(adult) <- c("age", "workclass", "fnlwgt", "education", "education_num", "marital_status", "occu
```

```
summary(adult)
```

```
##       age          workclass           fnlwgt          education
## Min.   :17.00   Length:32561      Min.   :  12285   Length:32561
## 1st Qu.:28.00   Class :character   1st Qu.: 117827   Class :character
## Median :37.00   Mode  :character   Median : 178356   Mode  :character
## Mean   :38.58                      Mean   : 189778
## 3rd Qu.:48.00                      3rd Qu.: 237051
## Max.   :90.00                      Max.   :1484705
## education_num   marital_status    occupation        relationship
## Min.   : 1.00   Length:32561      Length:32561      Length:32561
## 1st Qu.: 9.00   Class :character   Class :character   Class :character
## Median :10.00   Mode  :character   Mode  :character   Mode  :character
## Mean   :10.08
```

```
##  3rd Qu.:12.00
##  Max.   :16.00
##      race               sex           capital_gain     capital_loss
##  Length:32561       Length:32561       Min.   :     0   Min.   :   0.0
##  Class :character   Class :character   1st Qu.:     0   1st Qu.:   0.0
##  Mode  :character   Mode  :character   Median :     0   Median :   0.0
##                                        Mean   :  1078   Mean   :  87.3
##                                        3rd Qu.:     0   3rd Qu.:   0.0
##                                        Max.   : 99999   Max.   :4356.0
##  hours_per_week  native_country       fifty_k
##  Min.   : 1.00   Length:32561       Length:32561
##  1st Qu.:40.00   Class :character   Class :character
##  Median :40.00   Mode  :character   Mode  :character
##  Mean   :40.44
##  3rd Qu.:45.00
##  Max.   :99.00
```

Test to check if average capital gain is different for Female/Male:

Motivation: we want to find out if the capital gain differs based on gender.

Assumptions:

1. The dataset is a random sample of original population.

2. The data comes from a normal distribution.

3. The sample size is large enough to conduct any test.

4. And the final assumptions is homogeneity of variance.

Hypothesis:

H0: capital gain is equal for both gender

Ha: capital gain is not equal.

```
# adult %>%
#   group_by(sex) %>%
#   summarise(record_count = n())

female <- filter(adult, str_detect(sex, 'Female'))
male <- filter(adult, str_detect(sex, 'Male'))


t.test(capital_gain ~ sex, data=adult) # Unpooled
```
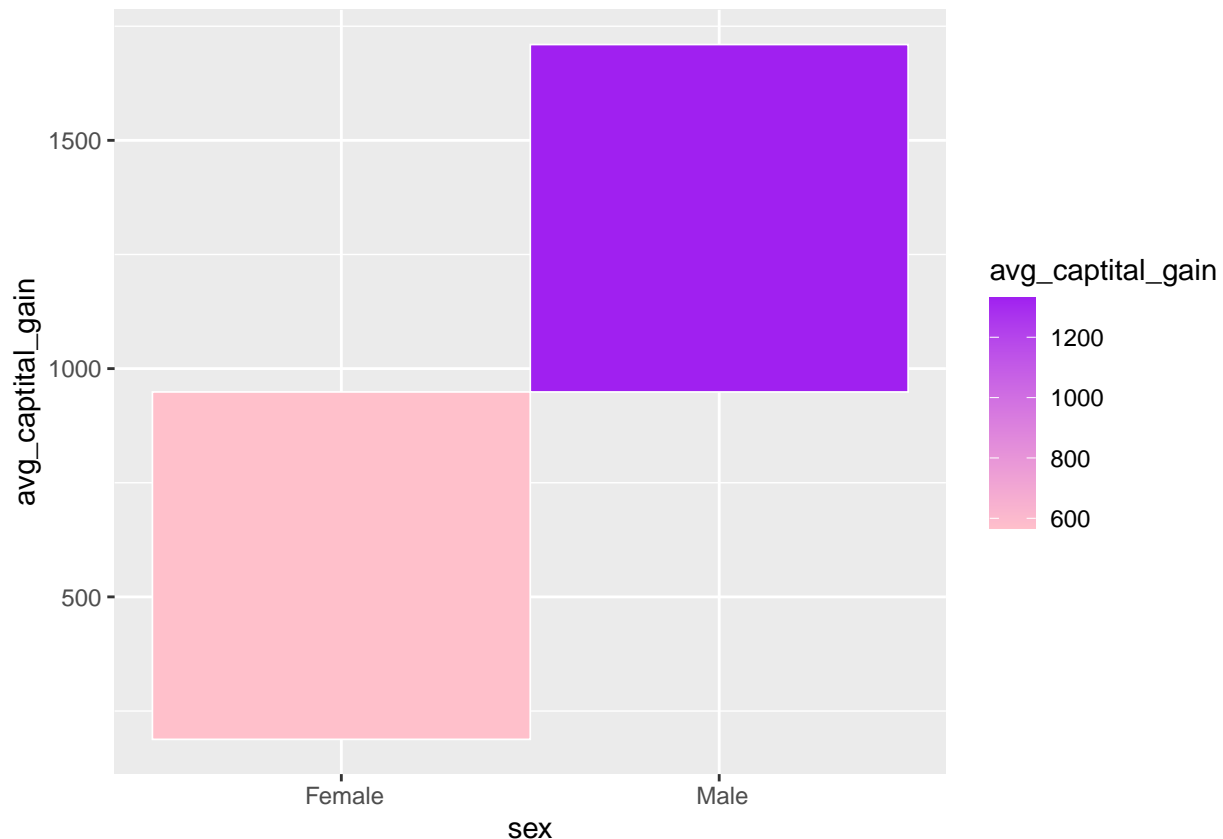
```
##
##  Welch Two Sample t-test
##
## data:  capital_gain by sex
## t = -10.324, df = 31563, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group  Female and group  Male is not equal
## 95 percent confidence interval:
##  -905.4303 -616.4888
## sample estimates:
## mean in group  Female   mean in group  Male
##             568.4105              1329.3701
```

```
t.test(capital_gain ~ sex, var.equal=TRUE, data=adult)    # Pooled
```

```
##
##  Two Sample t-test
##
## data:  capital_gain by sex
## t = -8.758, df = 32559, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group  Female and group  Male is not equal
## 95 percent confidence interval:
##  -931.2616 -590.6575
## sample estimates:
## mean in group  Female    mean in group  Male
##               568.4105                1329.3701
```

```
gain_sex<-adult %>%
  group_by(sex) %>%
  summarize(avg_captital_gain=mean(capital_gain))

gain_sex %>%
  ggplot(aes(x=sex, y=avg_captital_gain,fill=avg_captital_gain))+
  geom_tile(color="white",size=0.3)+
  scale_fill_gradient(low="pink",high="purple")
```


Conclusion: Looking at the p value which is close to 0, we can reject the null hypothesis.

We have evidence that suggests that the true difference in means between group Female and group Male is not equal to 0.

We have evidence to say that there is a difference in the average capital gain of Male and Female

```
t.test(capital_loss ~ sex, data=adult) # Unpooled
```

```
##
##   Welch Two Sample t-test
##
## data:  capital_loss by sex
## t = -8.8911, df = 26312, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group  Female and group  Male is not equal
## 95 percent confidence interval:
##  -47.62897 -30.42238
## sample estimates:
## mean in group  Female   mean in group  Male
##               61.18763              100.21331
```

```
t.test(capital_loss ~ sex, var.equal=TRUE, data=adult)   # Pooled
```

```
##
##   Two Sample t-test
##
## data:  capital_loss by sex
## t = -8.2308, df = 32559, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group  Female and group  Male is not equal
## 95 percent confidence interval:
##  -48.31906 -29.73229
## sample estimates:
## mean in group  Female   mean in group  Male
##               61.18763              100.21331
```

Checking if average capital gain differs by race

Motivation: we want to find out if the capital gain differs based on race.

Assumptions:

1. The dataset is a random sample of original population.

2. The data comes from a normal distribution.

3. The sample size is large enough to conduct any test.

4. And the final assumptions is homogeneity of variance.

Hypothesis:

H0: capital gain is equal for all race

Ha: there exist a pair of race for which capital gain is not equal.

```
# adult %>%
#   group_by(race) %>%
#   summarise(record_count = n())

anov_race <- aov(capital_gain ~ race, data = adult)
summary(anov_race)
```
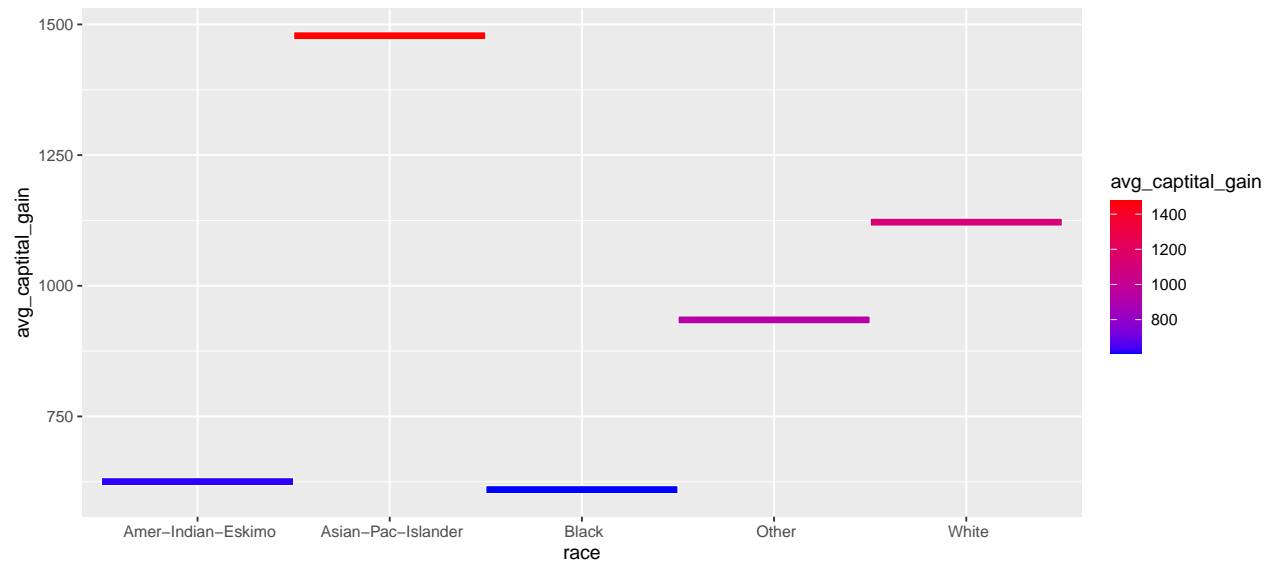
```
##                 Df    Sum Sq   Mean Sq F value  Pr(>F)
## race             4 9.733e+08 243318824   4.463 0.00132 **
## Residuals    32556 1.775e+12  54519345
## ---
```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
#TukeyHSD(anov_race)
```
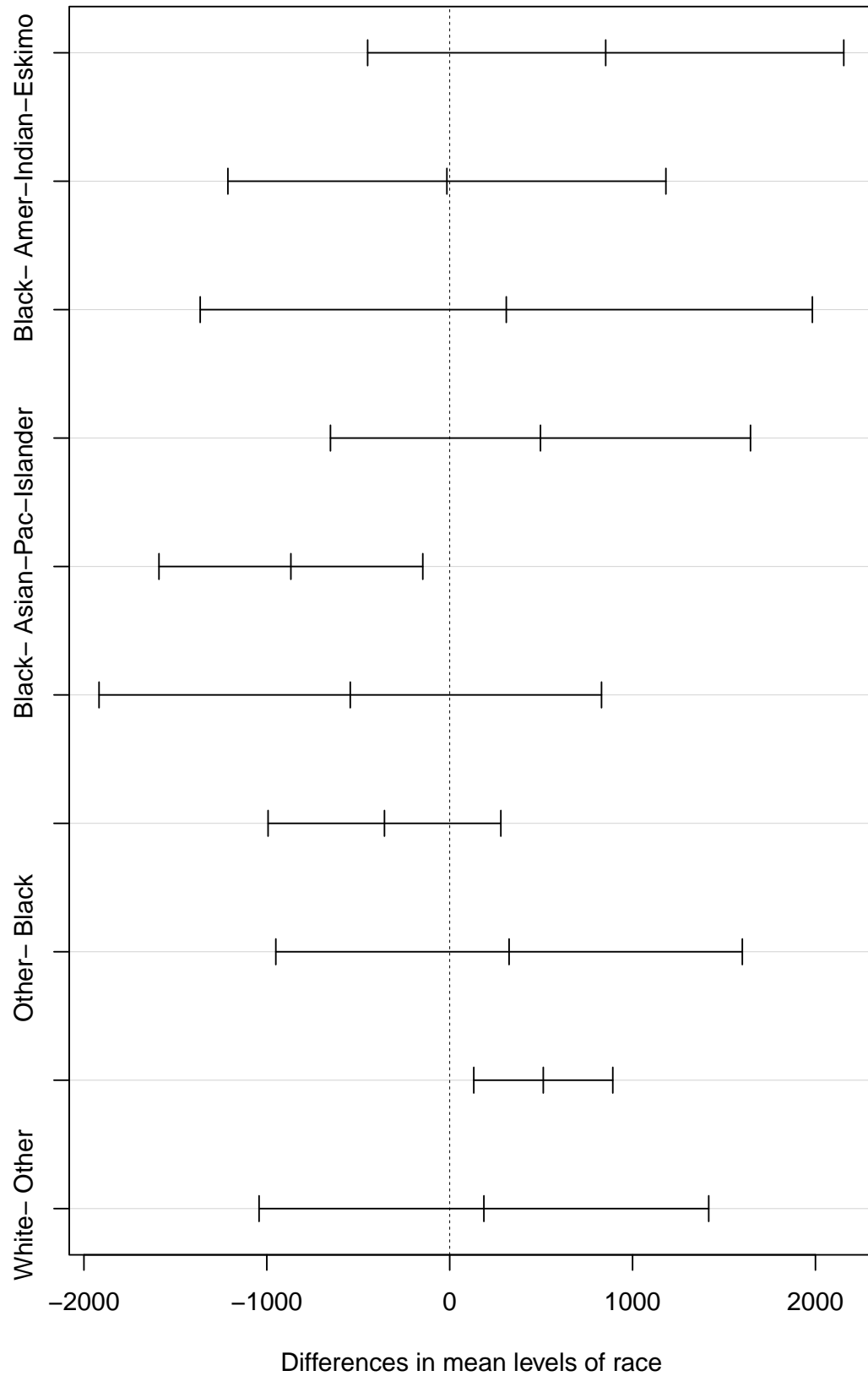
```
gain_race<-adult %>%
  group_by(race) %>%
  summarize(avg_captital_gain=mean(capital_gain))

gain_race %>%
  ggplot(aes(x=race, y=avg_captital_gain,fill=avg_captital_gain))+
  geom_tile(color="white",size=0.3)+
  scale_fill_gradient(low="blue",high="red")
```



```
plot(TukeyHSD(aov(capital_gain ~ race, data = adult)))
```

95% family−wise confidence level

Differences in mean levels of race

Since the p-value in our ANOVA table (0.00132) is less than .05, we have sufficient evidence to reject the null hypothesis.

This means we have sufficient evidence to say that the mean capital gain is not equal across different races.

From the Tukey Test, we can see that there is a significant difference between the means for Black- Asian-Pac-Islander and White- Black, and the p values are below the significance level.

From the plots, we can see that the maximum average capital gain is in the race Asian-Pac-Islander.

Checking if average capital gain differs by occupation

Motivation: we want to find out if the capital gain differs based on occupation.

Assumptions:

1. The dataset is a random sample of original population.

2. The data comes from a normal distribution.

3. The sample size is large enough to conduct any test.

4. And the final assumptions is homogeneity of variance.

Hypothesis:

H0: capital gain is equal for all occupation

Ha: there exist a pair of occupation for which capital gain is not equal.

```
anov_occ <- aov(capital_gain ~ occupation, data = adult)
summary(anov_occ)
```

```
##                 Df    Sum Sq   Mean Sq F value Pr(>F)
## occupation      14 2.539e+10 1.813e+09   33.72 <2e-16 ***
## Residuals    32546 1.751e+12 5.379e+07
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```
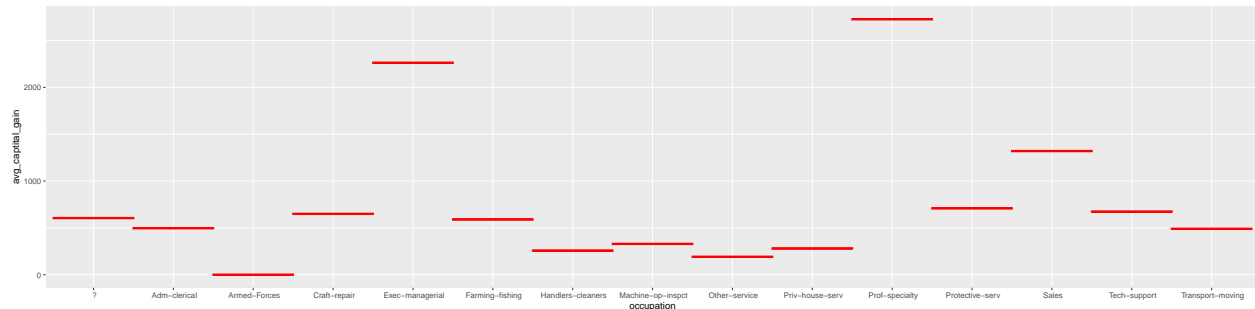
```
#TukeyHSD(anov_occ)
```

```
plot(TukeyHSD(aov(capital_gain ~ occupation, data = adult)))
```

95% family–wise confidence level

Differences in mean levels of occupation
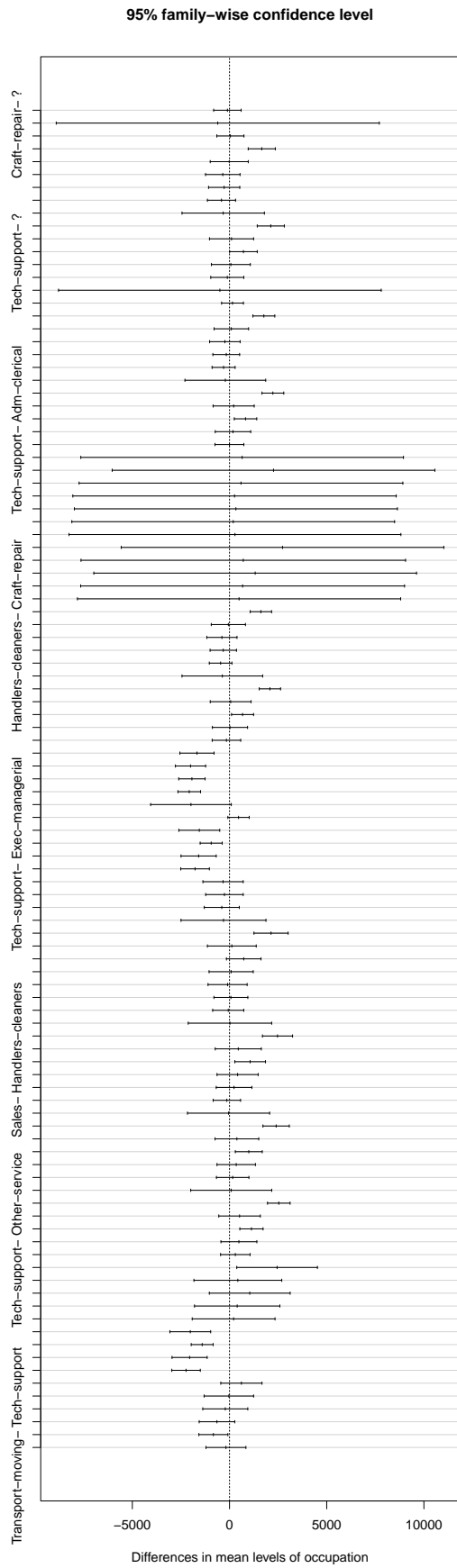
```
gain_occupation<-adult %>%
  group_by(occupation) %>%
  summarize(avg_captital_gain=mean(capital_gain))

gain_occupation %>%
  ggplot(aes(x=occupation, y=avg_captital_gain))+
  geom_tile(color="red",size=1)
```


Since the p-value in our ANOVA table (10^{-16}) is less than .05, we have sufficient evidence to reject the null hypothesis.

This means we have sufficient evidence to say that the mean capital gain is not equal across different occupation.

From the Tukey test, we can see the p-values for different occupation pairs, and the difference in average capital gain.

From the plots, we can see that the maximum average capital gain is in the occupation of Exec-managerial.

Checking if average capital gain differs by workclass

Motivation: we want to find out if the capital gain differs based on workclass.

Assumptions:

1. The dataset is a random sample of original population.

2. The data comes from a normal distribution.

3. The sample size is large enough to conduct any test.

4. And the final assumptions is homogeneity of variance.

Hypothesis:

H0: capital gain is equal for all workclass

Ha: there exist a pair of workclass for which capital gain is not equal.
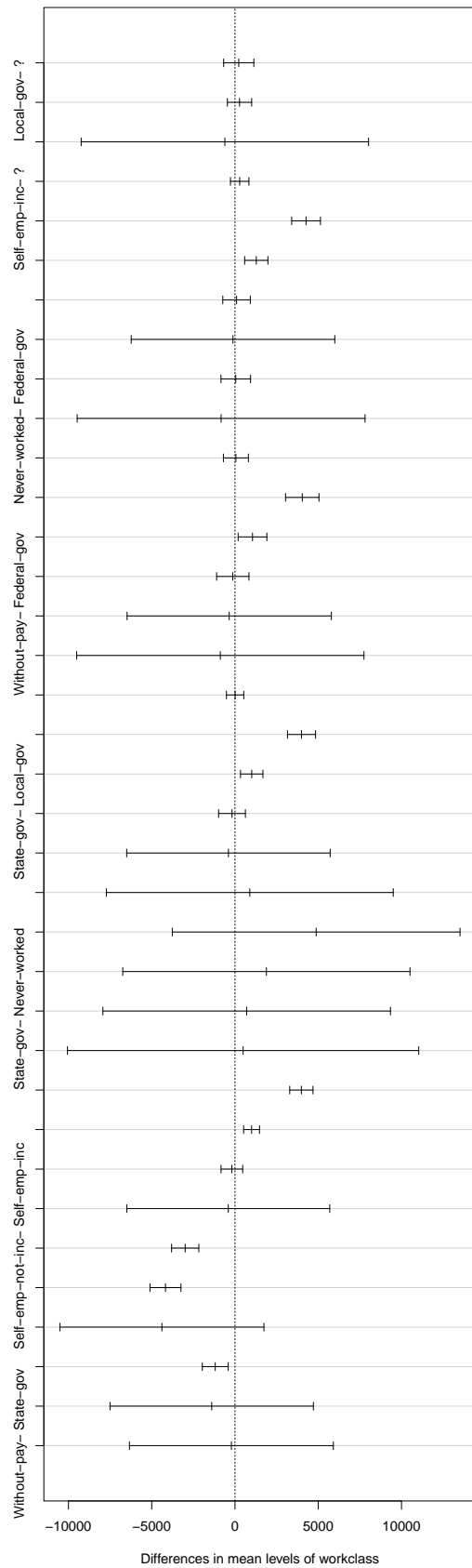
```
anov_wc <- aov(capital_gain ~ workclass, data = adult)
summary(anov_wc)

##                 Df    Sum Sq   Mean Sq F value Pr(>F)
## workclass        8 1.931e+10 2.413e+09   44.72 <2e-16 ***
## Residuals    32552 1.757e+12 5.396e+07
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
#TukeyHSD(anov_wc)
```

```
plot(TukeyHSD(aov(capital_gain ~ workclass, data = adult)))
```

95% family–wise confidence level

Differences in mean levels of workclass

```
gain_wc<-adult %>%
  group_by(workclass) %>%
  summarize(avg_captital_gain=mean(capital_gain))

gain_wc %>%
  ggplot(aes(x=workclass, y=avg_captital_gain))+
  geom_tile(color="red",size=1)
```
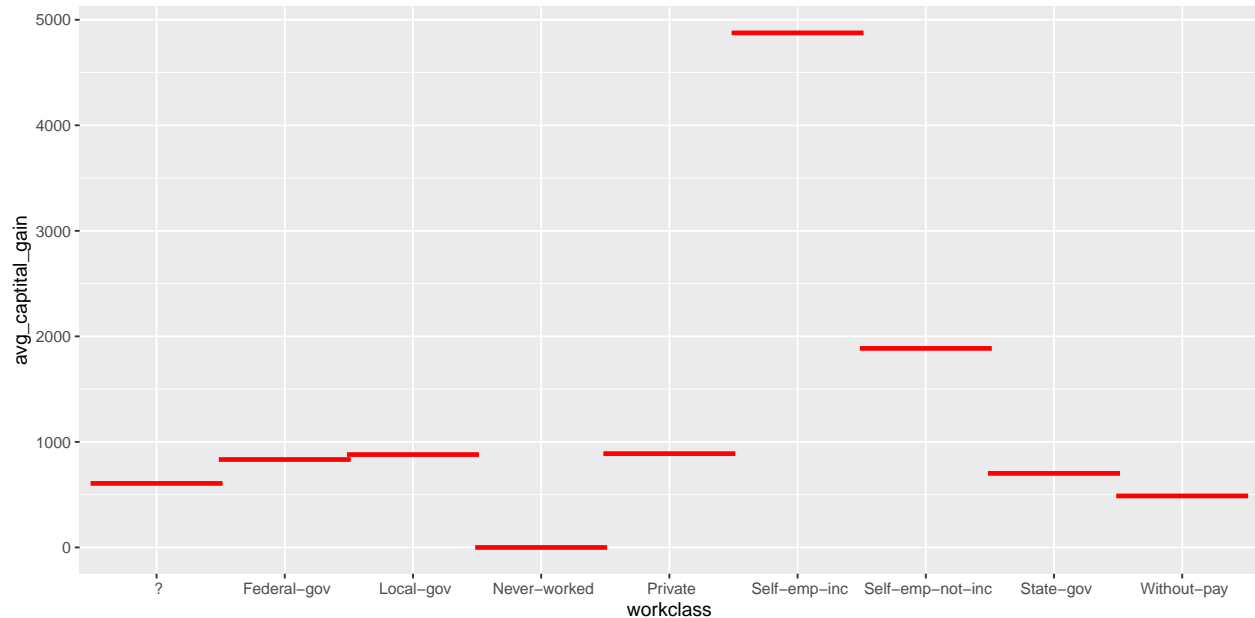

Since the p-value in our ANOVA table (10^-16) is less than .05, we have sufficient evidence to reject the null hypothesis.

This means we have sufficient evidence to say that the mean capital gain is not equal across different workclass.

From the Tukey test, we can see the p-values for different occupation pairs, and the difference in average capital gain.

From the plots, we can see that the maximum average capital gain is in the occupation of Self-emp-inc.

Checking if average capital gain differs by education level

Motivation: we want to find out if the capital gain differs based on education level.

Assumptions:

1. The dataset is a random sample of original population.

2. The data comes from a normal distribution.

3. The sample size is large enough to conduct any test.

4. And the final assumptions is homogeneity of variance.

Hypothesis:

H0: capital gain is equal for education level

Ha: there exist a pair of education level for which capital gain is not equal.

```r
# adult %>%
#   group_by(education) %>%
#   summarise(record_count = n())

anov_edu <- aov(capital_gain ~ education, data = adult)
summary(anov_edu)
```
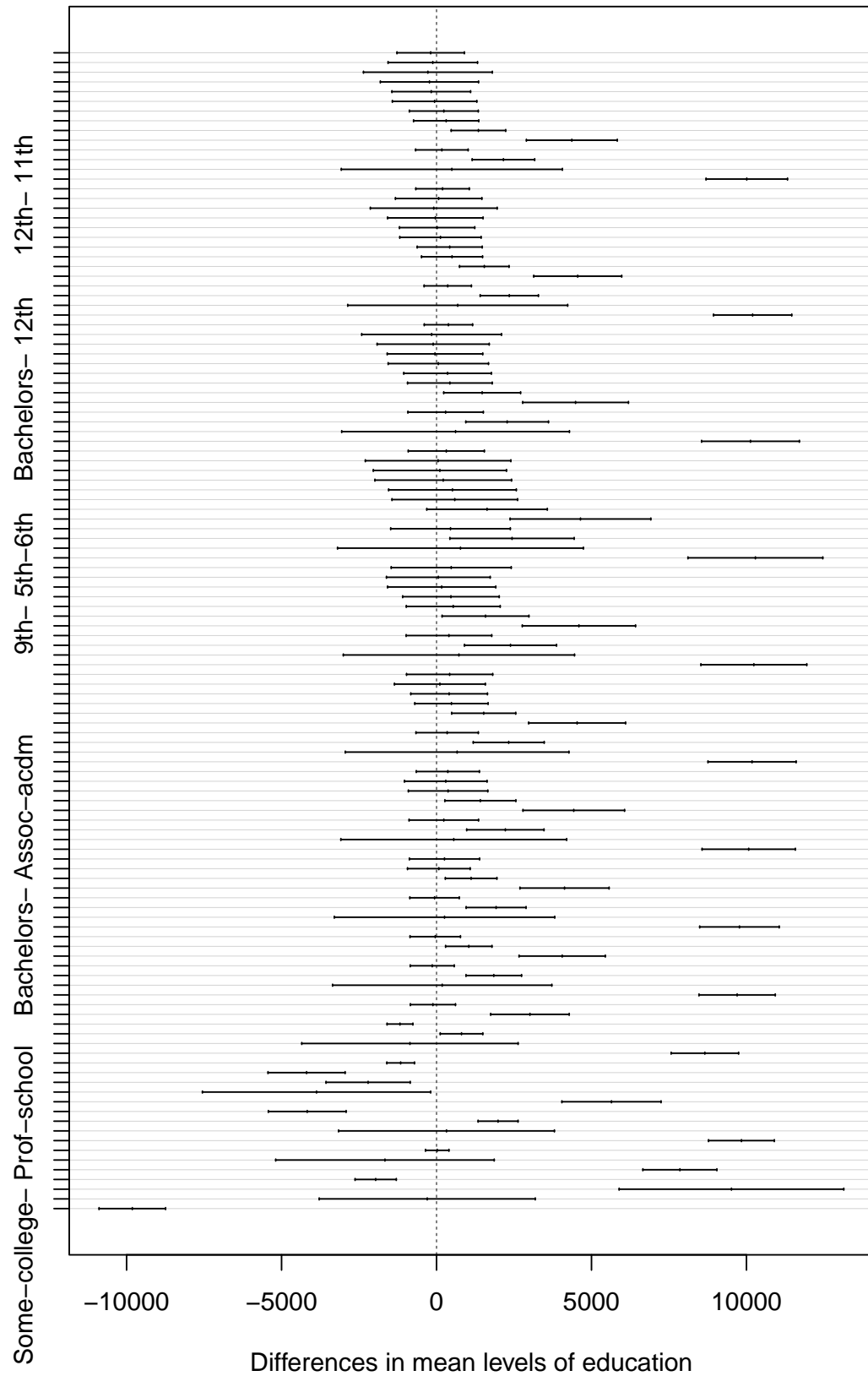
```
##                 Df    Sum Sq    Mean Sq F value Pr(>F)
## education       15 6.953e+10  4.636e+09   88.41 <2e-16 ***
## Residuals    32545 1.706e+12  5.243e+07
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```r
#TukeyHSD(anov_edu)
```

```r
plot(TukeyHSD(aov(capital_gain ~ education, data = adult)))
```

95% family−wise confidence level

Differences in mean levels of education

```r
gain_edu<-adult %>%
  group_by(education) %>%
  summarize(avg_captital_gain=mean(capital_gain))

gain_edu %>%
  ggplot(aes(x=education, y=avg_captital_gain))+
  geom_tile(color="purple",size=1)
```
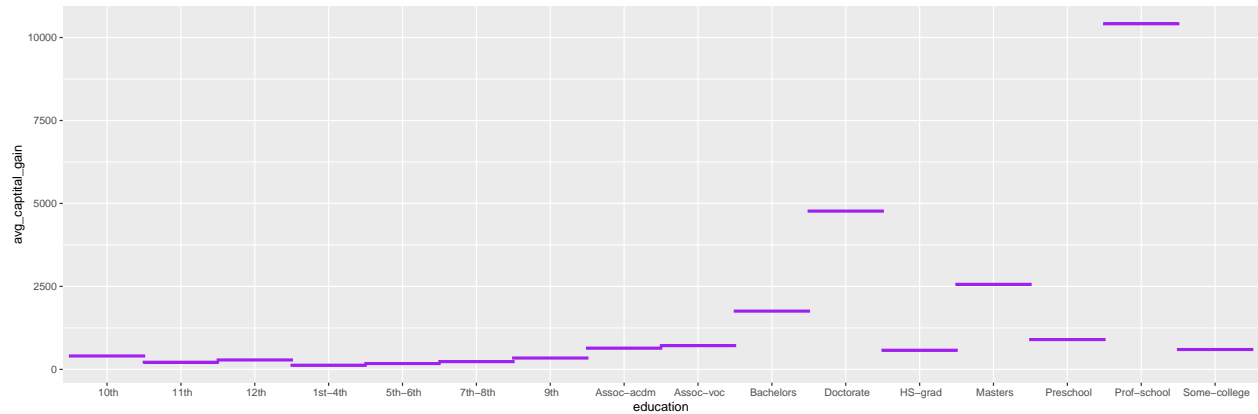


```r
#Checking for education number

anov_edu_num <- aov(capital_gain ~ education_num, data = adult)
# summary(anov_edu_num)
# anov_edu_num

gain_edu_num<-adult %>%
  group_by(education_num) %>%
  summarize(avg_captital_gain=mean(capital_gain))

gain_edu_num %>%
  ggplot(aes(x=education_num, y=avg_captital_gain))+
  geom_tile(color="blue",size=1)
```
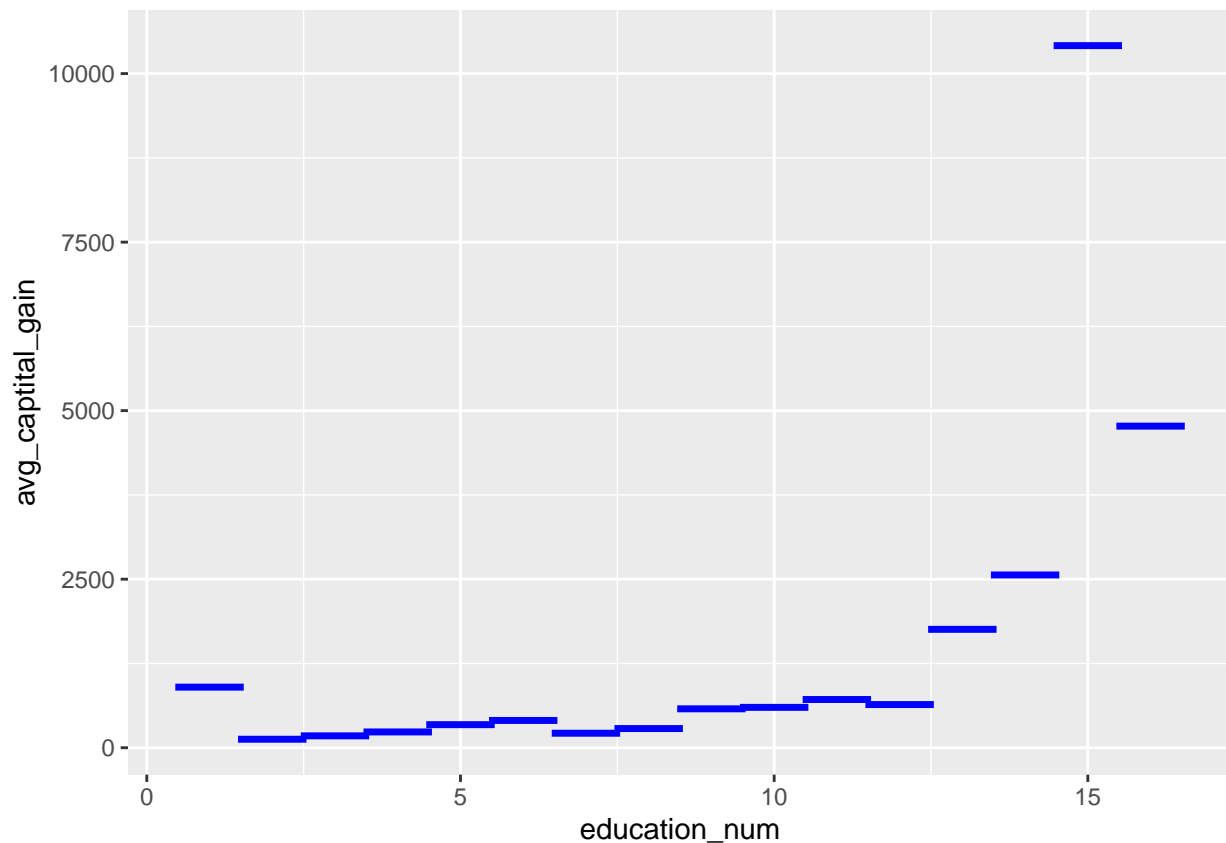
Since the p-value in our ANOVA table is less than .05, we have sufficient evidence to reject the null hypothesis.

This means we have sufficient evidence to say that the mean capital gain is not equal across different education levels.

From the Tukey test, we can see the p-values for different education pairs, and the difference in average capital gain.

From the plots, we can see that the maximum average capital gain is with the education prof school.

Plotting gain on education and sex

```
education_sex<-adult %>%
  group_by(sex, education) %>%
  summarize(avg_captital_gain=mean(capital_gain))
```

```
## `summarise()` has grouped output by 'sex'. You can override using the `.groups`
## argument.
```

```
education_sex %>%
  ggplot(aes(x=sex,y=education,fill=avg_captital_gain))+
  geom_tile(color="white",size=0.3)+
  scale_fill_gradient(low="pink",high="purple")
```
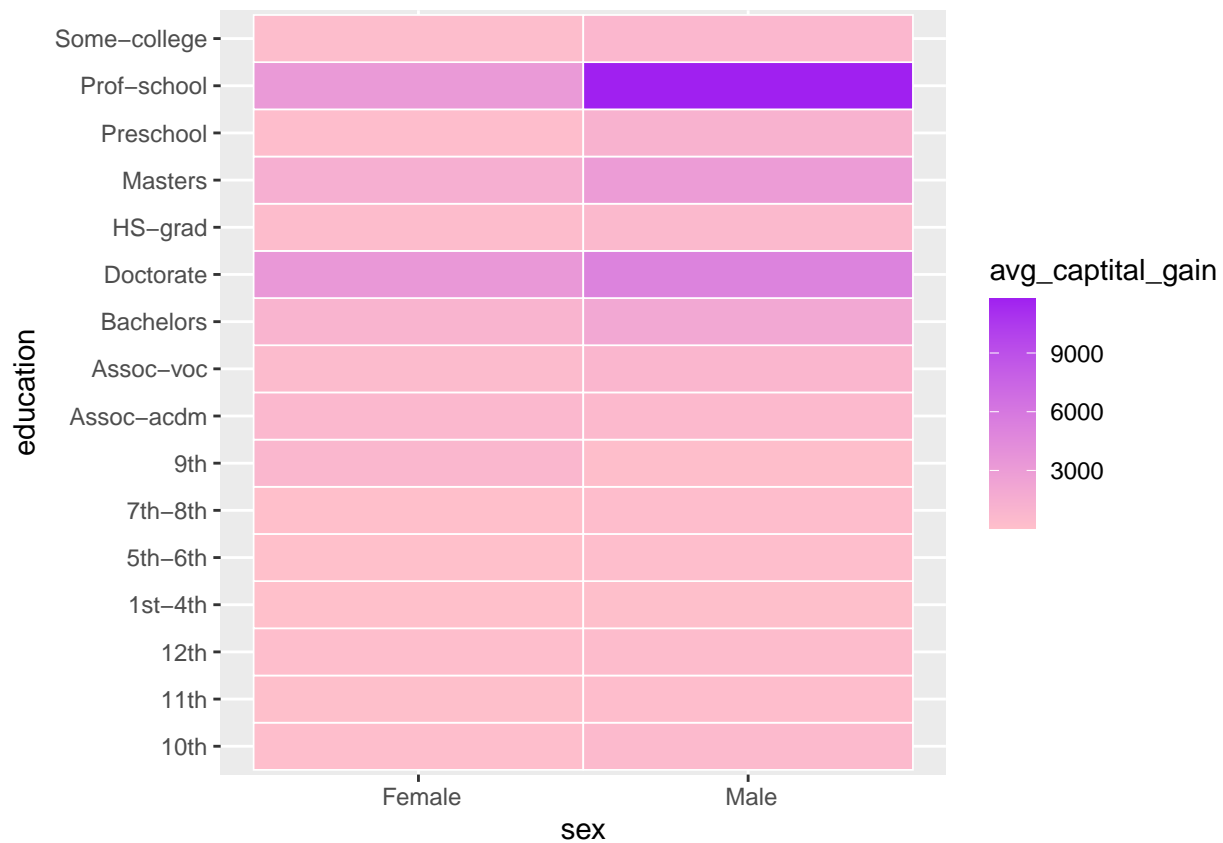
Plotting gain on race and sex

```
race_sex<-adult %>%
  group_by(sex, race) %>%
  summarize(avg_captital_gain=mean(capital_gain))
```

```
## `summarise()` has grouped output by 'sex'. You can override using the `.groups`
## argument.
```

```
race_sex %>%
  ggplot(aes(x=sex,y=race,fill=avg_captital_gain))+
  geom_tile(color="white",size=0.3)+
  scale_fill_gradient(low="pink",high="purple")
```

Average capital gain vs earning greater than or less than or equal to 50k.

```
# adult %>%
#   group_by(fifty_k) %>%
#   summarise(record_count = n())
```

```
t.test(capital_gain ~ fifty_k, data=adult) # Unpooled
```

```
##
##  Welch Two Sample t-test
##
## data:  capital_gain by fifty_k
## t = -23.427, df = 7861.7, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group  <=50K and group  >50K is not equal to
## 95 percent confidence interval:
##  -4180.166 -3534.614
## sample estimates:
## mean in group  <=50K  mean in group  >50K
##             148.7525             4006.1425
```

```
t.test(capital_gain ~ fifty_k, var.equal=TRUE, data=adult)   # Pooled
```

```
##
##  Two Sample t-test
```

```
##
## data:  capital_gain by fifty_k
## t = -41.342, df = 32559, p-value < 2.2e-16
## alternative hypothesis: true difference in means between group  <=50K and group  >50K is not equal to
## 95 percent confidence interval:
##  -4040.271 -3674.509
## sample estimates:
## mean in group  <=50K  mean in group  >50K
##              148.7525             4006.1425
```

```
gain_fifty<-adult %>%
  group_by(fifty_k) %>%
  summarize(avg_captital_gain=mean(capital_gain))

gain_fifty %>%
  ggplot(aes(x=fifty_k, y=avg_captital_gain,fill=avg_captital_gain))+
  geom_tile(color="white",size=0.3)+
  scale_fill_gradient(low="pink",high="purple")
```
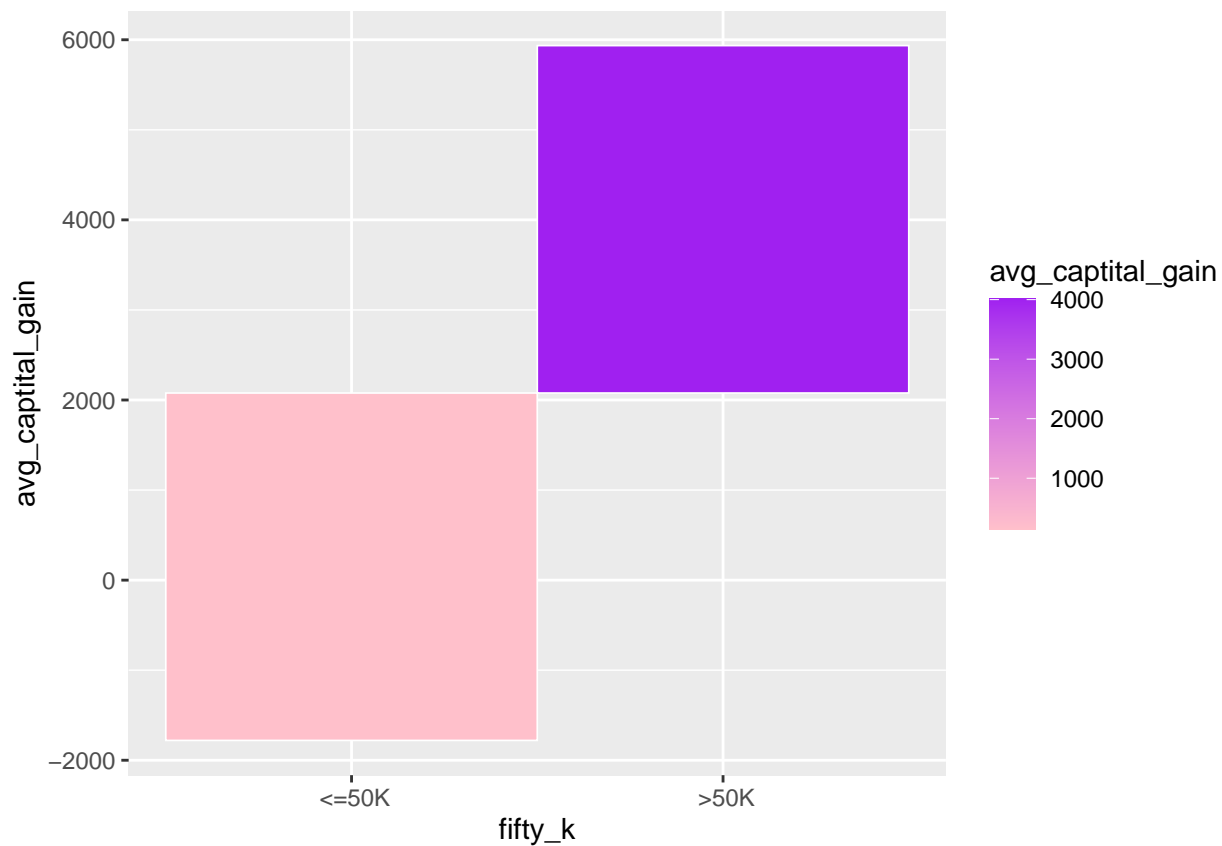

Looking at the p value which is close to 0, we can reject the null hypothesis.

We have evidence that suggests that the true difference in means between group that earns less than or equal to 50k and more than 50 is not equal to 0.

We have evidence to say that there is a significant difference in the average capital gain.

Checking if average capital gain differs by marital status

```r
# adult %>%
#   group_by(race) %>%
#   summarise(record_count = n())

anov_race <- aov(capital_gain ~ marital_status, data = adult)
summary(anov_race)
```

```
##                  Df    Sum Sq   Mean Sq F value Pr(>F)
## marital_status    6 1.351e+10 2.251e+09   41.58 <2e-16 ***
## Residuals     32554 1.762e+12 5.414e+07
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```r
#TukeyHSD(anov_race)

plot(TukeyHSD(aov(capital_gain ~ marital_status, data = adult)))
```

95% family−wise confidence level

Differences in mean levels of marital_status
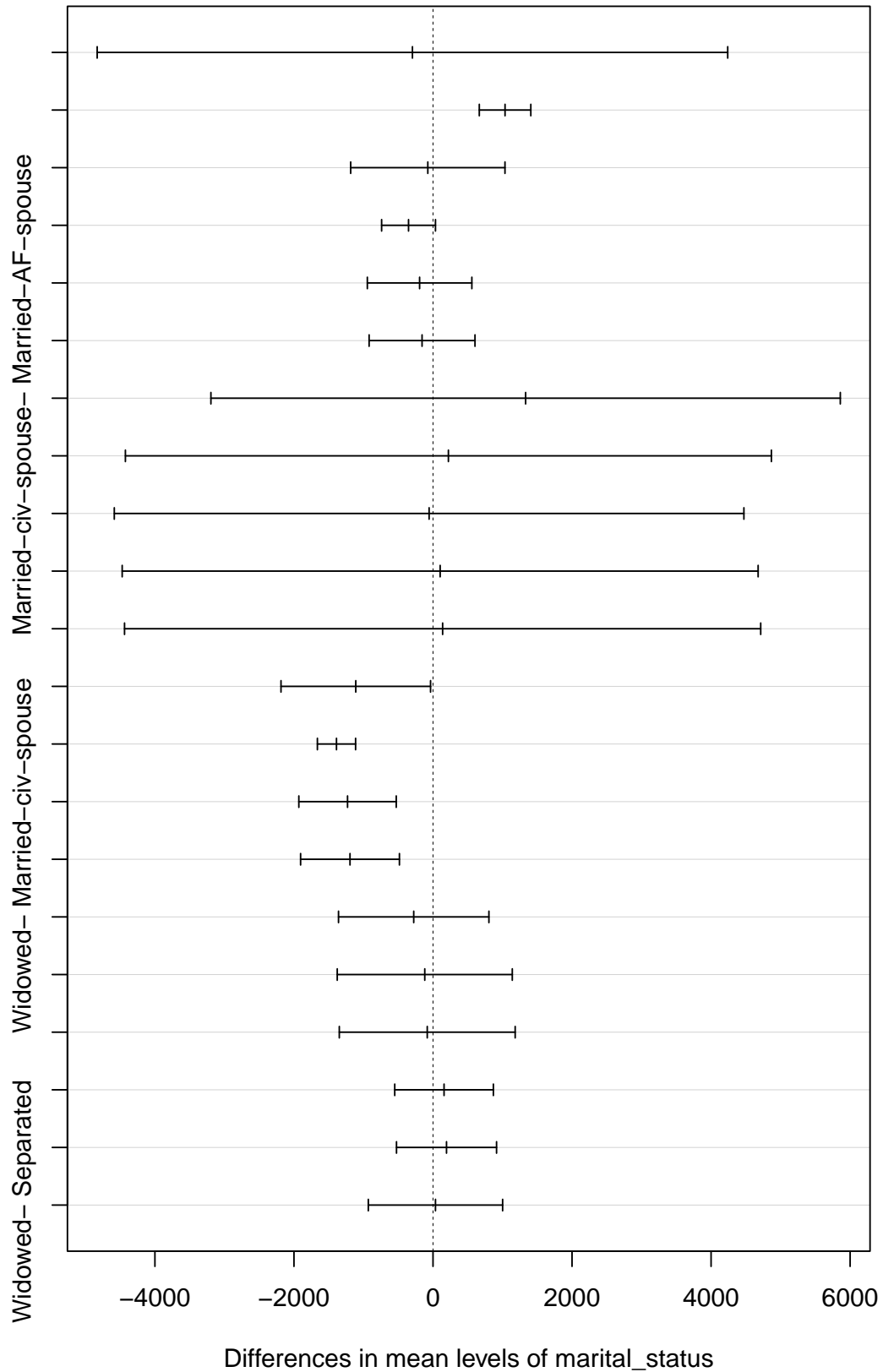
```
gain_marital<-adult %>%
  group_by(marital_status) %>%
  summarize(avg_captital_gain=mean(capital_gain))

gain_marital %>%
  ggplot(aes(x=marital_status, y=avg_captital_gain,fill=avg_captital_gain))+
  geom_tile(color="white",size=0.3)+
  scale_fill_gradient(low="blue",high="red")
```
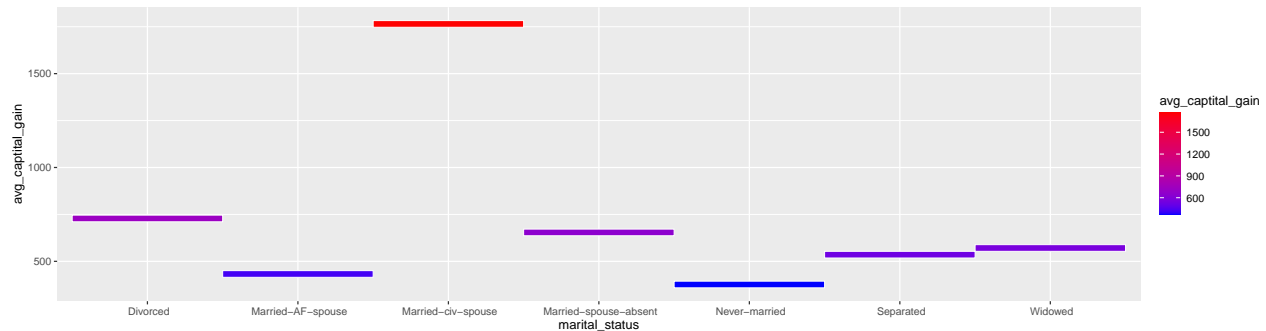

Since the p-value in our ANOVA table is less than .05, we have sufficient evidence to reject the null hypothesis.

This means we have sufficient evidence to say that the mean capital gain is not equal across different marital-status.

From the Tukey test, we can see the p-values for different marital status pairs, and the difference in average capital gain.

From the plots, we can see that the maximum average capital gain is with married-civ-spouse.

Real Estate data set: Real_Estate

```
real_estate <- read.csv("Real_Estate.csv")
summary(real_estate)
```

```
##        No         X1.transaction.date  X2.house.age
##  Min.   :  1.0   Min.   :2013         Min.   : 0.000
##  1st Qu.:104.2   1st Qu.:2013         1st Qu.: 9.025
##  Median :207.5   Median :2013         Median :16.100
##  Mean   :207.5   Mean   :2013         Mean   :17.713
##  3rd Qu.:310.8   3rd Qu.:2013         3rd Qu.:28.150
##  Max.   :414.0   Max.   :2014         Max.   :43.800
##  X3.distance.to.the.nearest.MRT.station X4.number.of.convenience.stores
##  Min.   :  23.38                        Min.   : 0.000
##  1st Qu.: 289.32                        1st Qu.: 1.000
##  Median : 492.23                        Median : 4.000
##  Mean   :1083.89                        Mean   : 4.094
##  3rd Qu.:1454.28                        3rd Qu.: 6.000
##  Max.   :6488.02                        Max.   :10.000
##   X5.latitude     X6.longitude   Y.house.price.of.unit.area
##  Min.   :24.93   Min.   :121.5   Min.   :  7.60
##  1st Qu.:24.96   1st Qu.:121.5   1st Qu.: 27.70
##  Median :24.97   Median :121.5   Median : 38.45
##  Mean   :24.97   Mean   :121.5   Mean   : 37.98
##  3rd Qu.:24.98   3rd Qu.:121.5   3rd Qu.: 46.60
```

```
## Max.   :25.01   Max.   :121.6   Max.    :117.50
```

```
ls(real_estate)
```

```
## [1] "No"
## [2] "X1.transaction.date"
## [3] "X2.house.age"
## [4] "X3.distance.to.the.nearest.MRT.station"
## [5] "X4.number.of.convenience.stores"
## [6] "X5.latitude"
## [7] "X6.longitude"
## [8] "Y.house.price.of.unit.area"
```

```
pairs(real_estate[,2:8], pch=19)
```
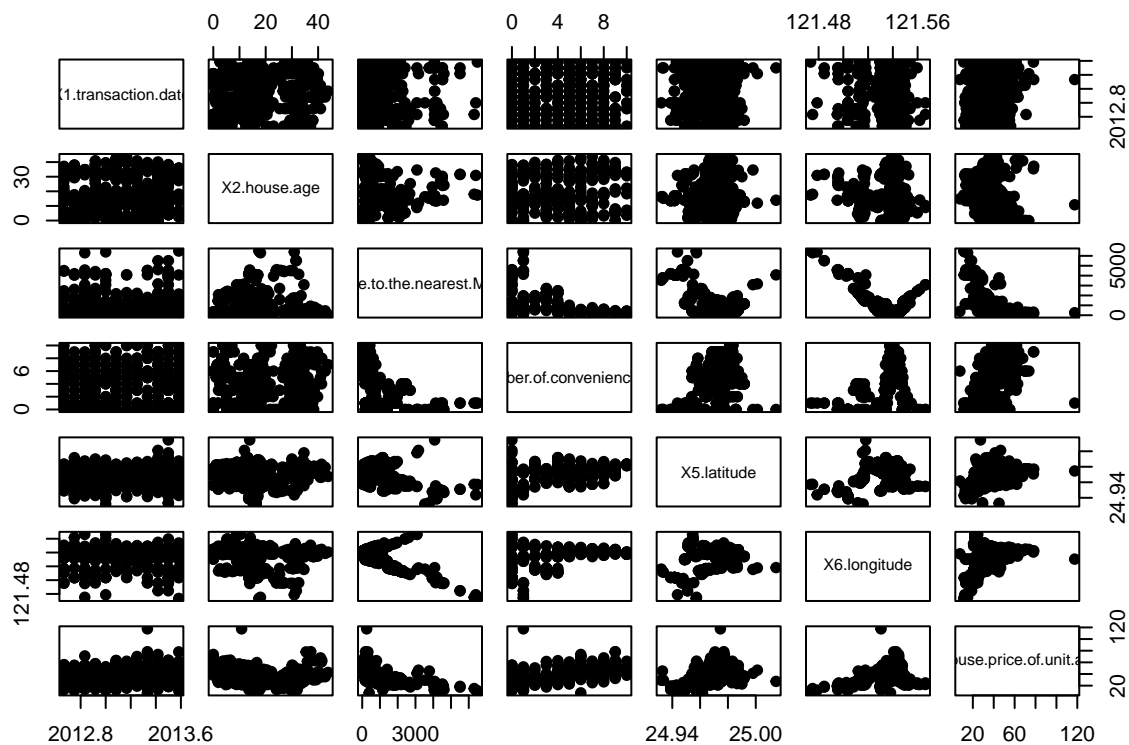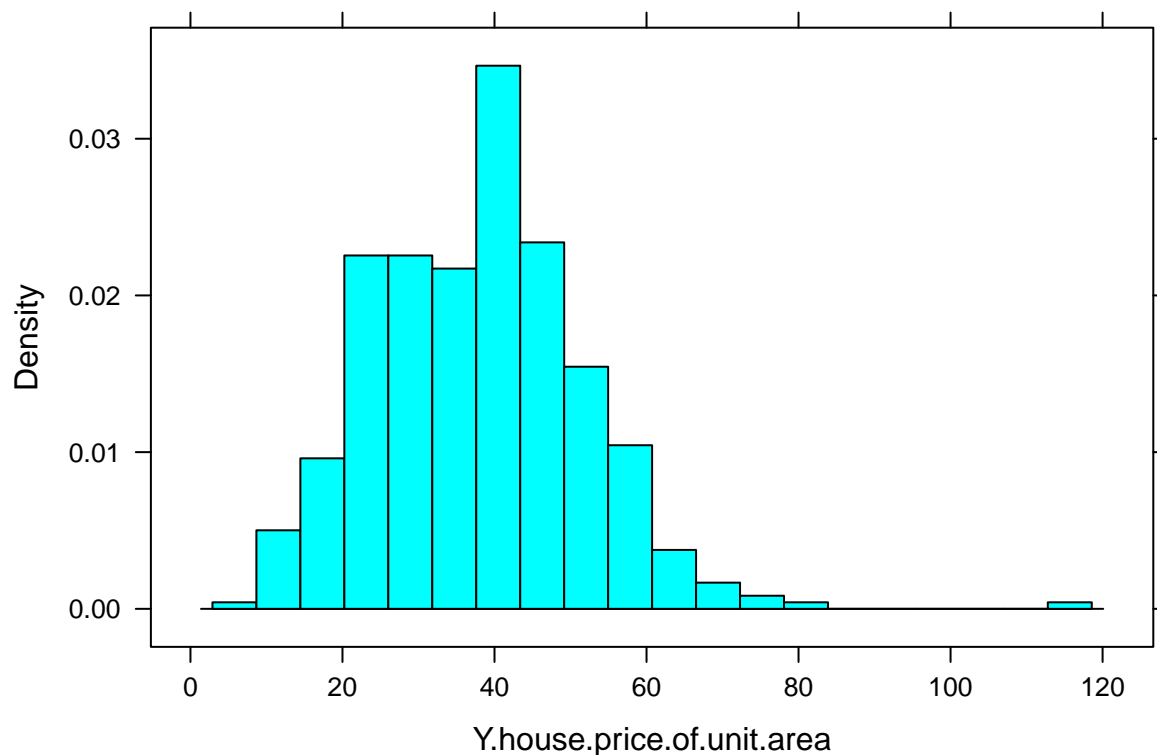


```
#xyplot(Y.house.price.of.unit.area ~ X4.number.of.convenience.stores,data=real_estate)  # positive tren
#xyplot(Y.house.price.of.unit.area ~ X3.distance.to.the.nearest.MRT.station,data=real_estate)  # negati


# study with distance to metro station.

#check value distribution.
histogram(~Y.house.price.of.unit.area, data=real_estate, nint=20)
```

```
#check correlation between house price and distance to metro station.
cor(Y.house.price.of.unit.area ~ X3.distance.to.the.nearest.MRT.station, data=real_estate) # -0.673
```

```
## [1] -0.6736129
```

```
#the least squares line  regression line.
m1 <- lm(Y.house.price.of.unit.area ~ X3.distance.to.the.nearest.MRT.station, data=real_estate)
summary(m1)
```

```
##
## Call:
## lm(formula = Y.house.price.of.unit.area ~ X3.distance.to.the.nearest.MRT.station,
##     data = real_estate)
##
## Residuals:
##     Min      1Q  Median      3Q     Max
## -35.396  -6.007  -1.195   4.831  73.483
##
## Coefficients:
##                                        Estimate Std. Error t value Pr(>|t|)
## (Intercept)                          45.8514271  0.6526105   70.26   <2e-16
## X3.distance.to.the.nearest.MRT.station -0.0072621  0.0003925  -18.50   <2e-16
##
## (Intercept)                          ***
## X3.distance.to.the.nearest.MRT.station ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 10.07 on 412 degrees of freedom
## Multiple R-squared:  0.4538, Adjusted R-squared:  0.4524
## F-statistic: 342.2 on 1 and 412 DF,  p-value: < 2.2e-16
```

```
#xy plot
xyplot(Y.house.price.of.unit.area ~ X3.distance.to.the.nearest.MRT.station,data=real_estate,type=c("p",
```
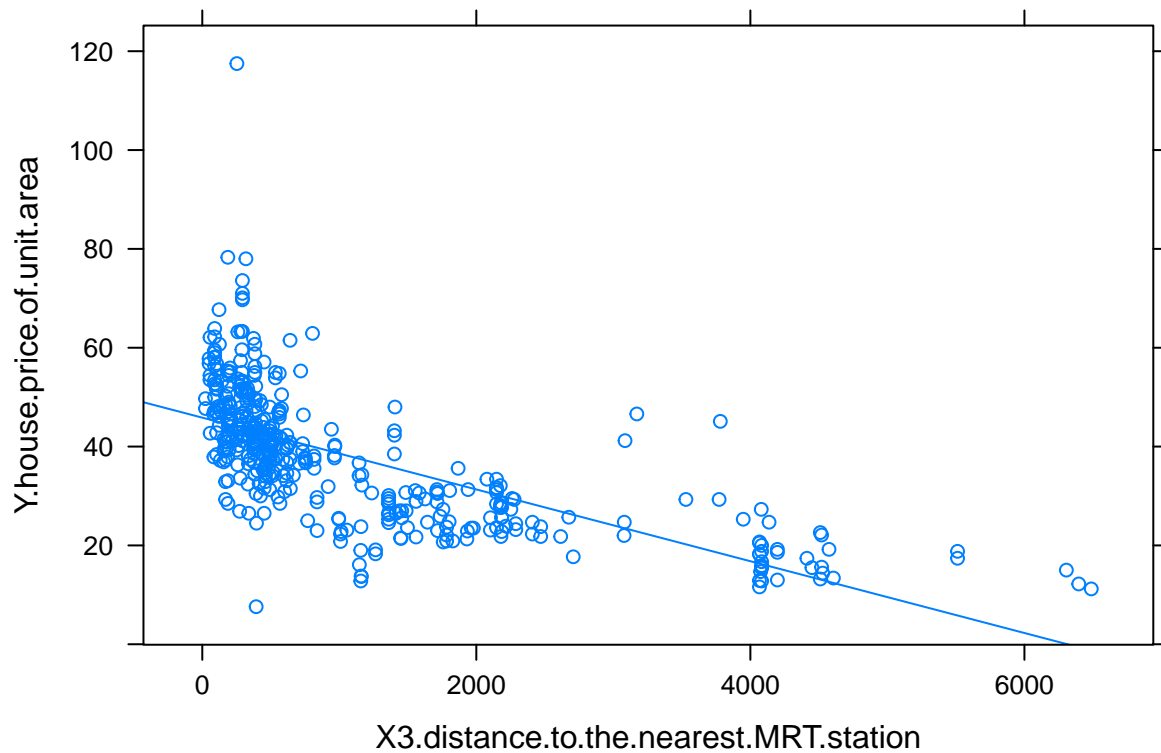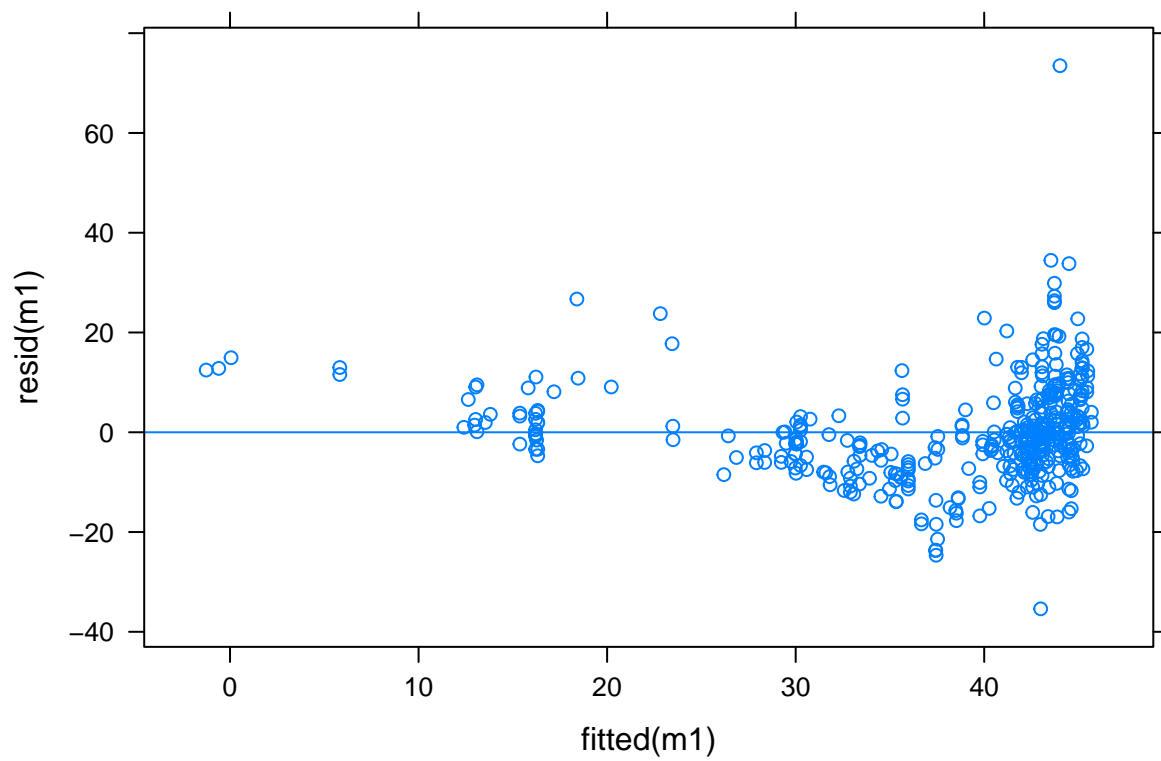

Assumption Check:

1. Residual are uniformly distributed around y=0 horizontal line.

2. Residual follows normal distribution.

3. The relationship between two variables should be linear.

4. The observation should be independent of each other.

```
#normalty check of errors/residual and assumptions check *
xyplot(resid(m1)~fitted(m1), data=real_estate, type=c("p","r"))
```
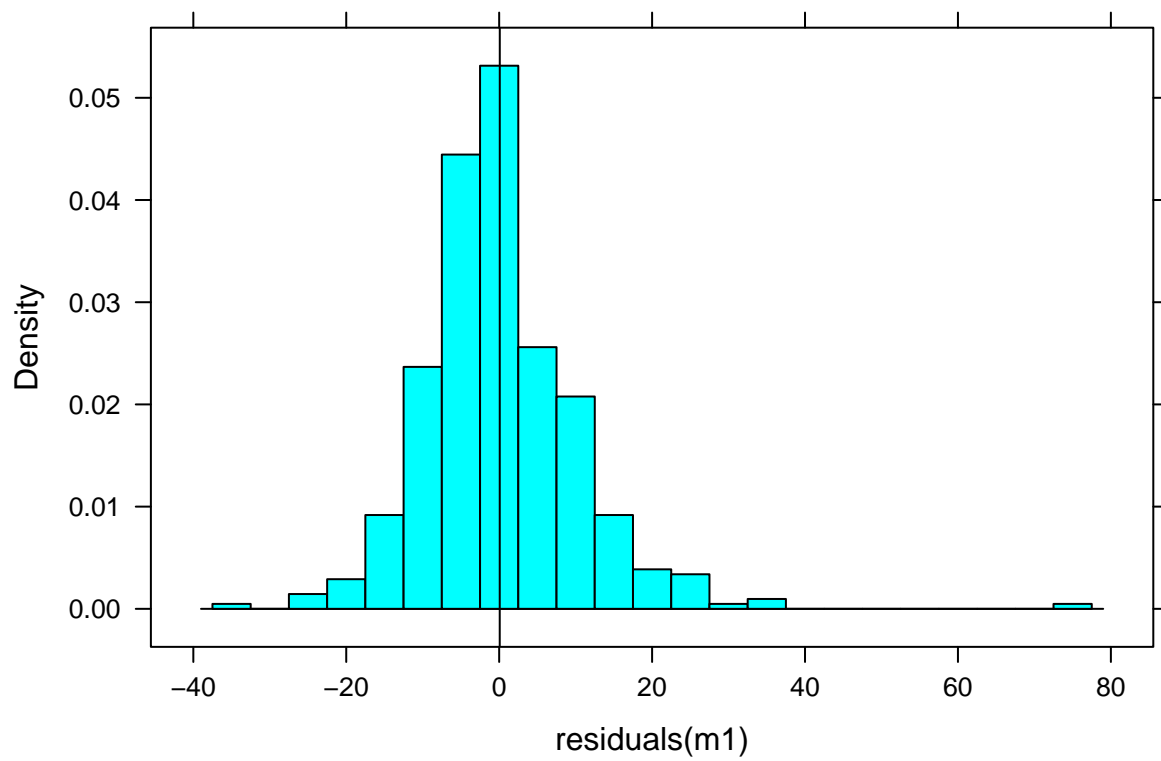
```
histogram(residuals(m1),width=5)
```
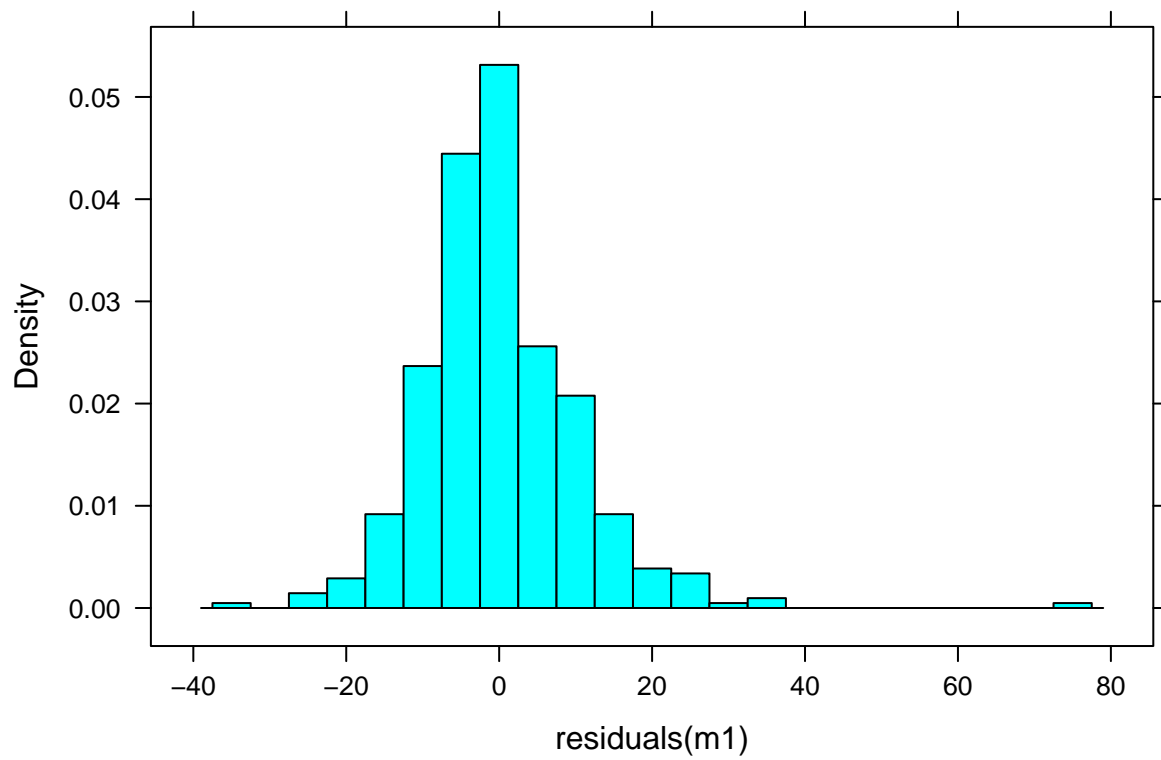


```
ladd(panel.qqmathline(resid(m1)))
```

`plot(resid(m1))`
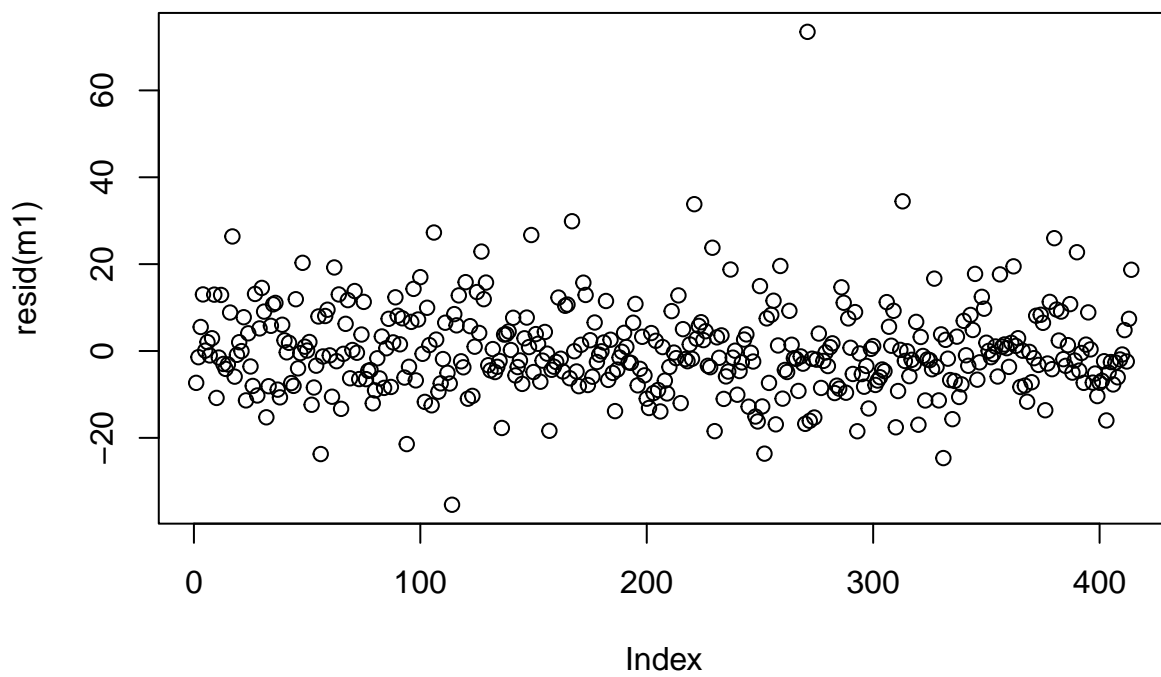
`plot(density(resid(m1)))`

density.default(x = resid(m1))
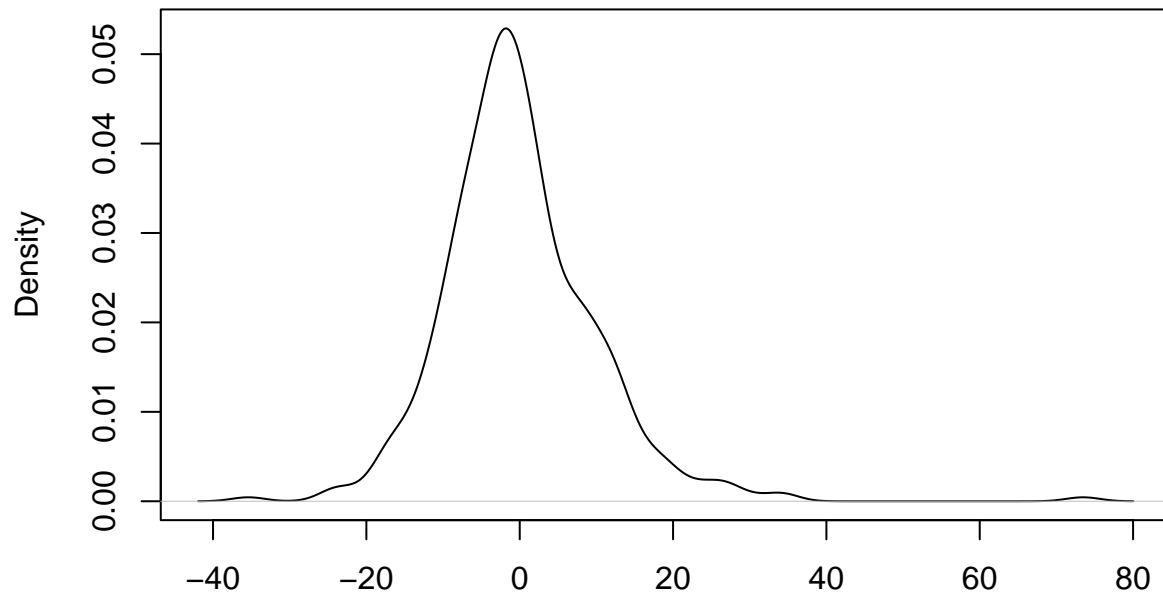
N = 414   Bandwidth = 2.181

```
qqnorm(resid(m1))
qqline(resid(m1))
```

Normal Q–Q Plot

Con-

clusion:
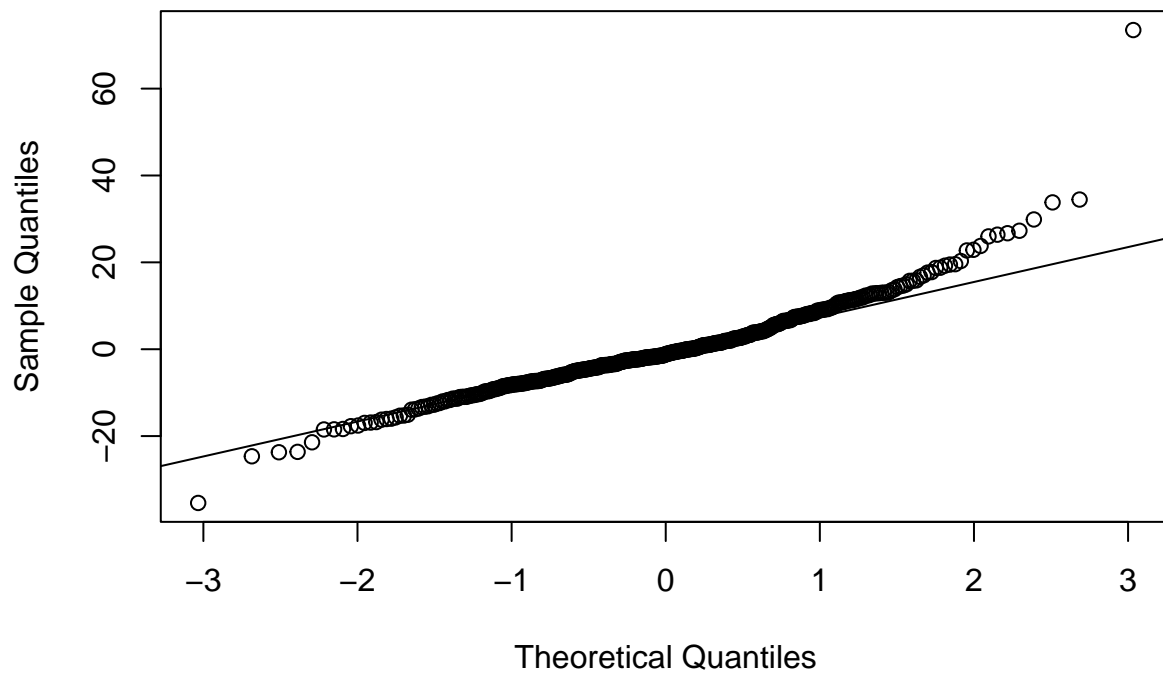
All assuptions holds here. From differnt graphs we can see that the conditions for linear model fitting holds.

#Checking if house price varies with number of convenience stores:

```
m2 <- lm(Y.house.price.of.unit.area ~ X4.number.of.convenience.stores, data=real_estate)
summary(m2)
```

```
##
## Call:
## lm(formula = Y.house.price.of.unit.area ~ X4.number.of.convenience.stores,
##     data = real_estate)
##
## Residuals:
##     Min      1Q  Median      3Q     Max
## -35.407  -7.341  -1.788   5.984  87.681
##
## Coefficients:
##                                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)                      27.1811     0.9419   28.86   <2e-16 ***
## X4.number.of.convenience.stores   2.6377     0.1868   14.12   <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 11.18 on 412 degrees of freedom
## Multiple R-squared:  0.326,  Adjusted R-squared:  0.3244
## F-statistic: 199.3 on 1 and 412 DF,  p-value: < 2.2e-16
```

```
m3 <- lm(Y.house.price.of.unit.area ~ X2.house.age, data=real_estate)
summary(m3)
```

```
##
## Call:
## lm(formula = Y.house.price.of.unit.area ~ X2.house.age, data = real_estate)
##
## Residuals:
##     Min      1Q  Median      3Q     Max
## -31.113 -10.738   1.626   8.199  77.781
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  42.43470    1.21098  35.042  < 2e-16 ***
## X2.house.age -0.25149    0.05752  -4.372 1.56e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.32 on 412 degrees of freedom
## Multiple R-squared:  0.04434,    Adjusted R-squared:  0.04202
## F-statistic: 19.11 on 1 and 412 DF,  p-value: 1.56e-05
```

```
ggplot(real_estate, aes( X2.house.age, Y.house.price.of.unit.area)) + geom_point() + stat_smooth(method
```
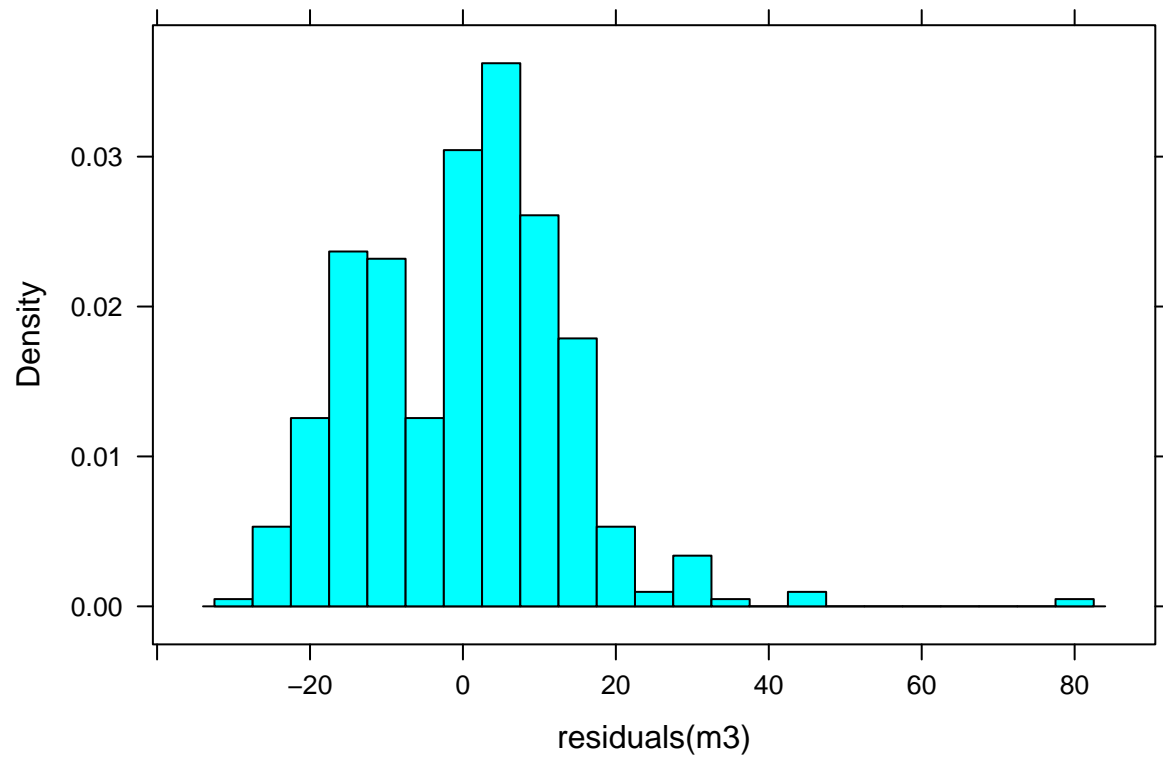
```
## `geom_smooth()` using formula 'y ~ x'
```
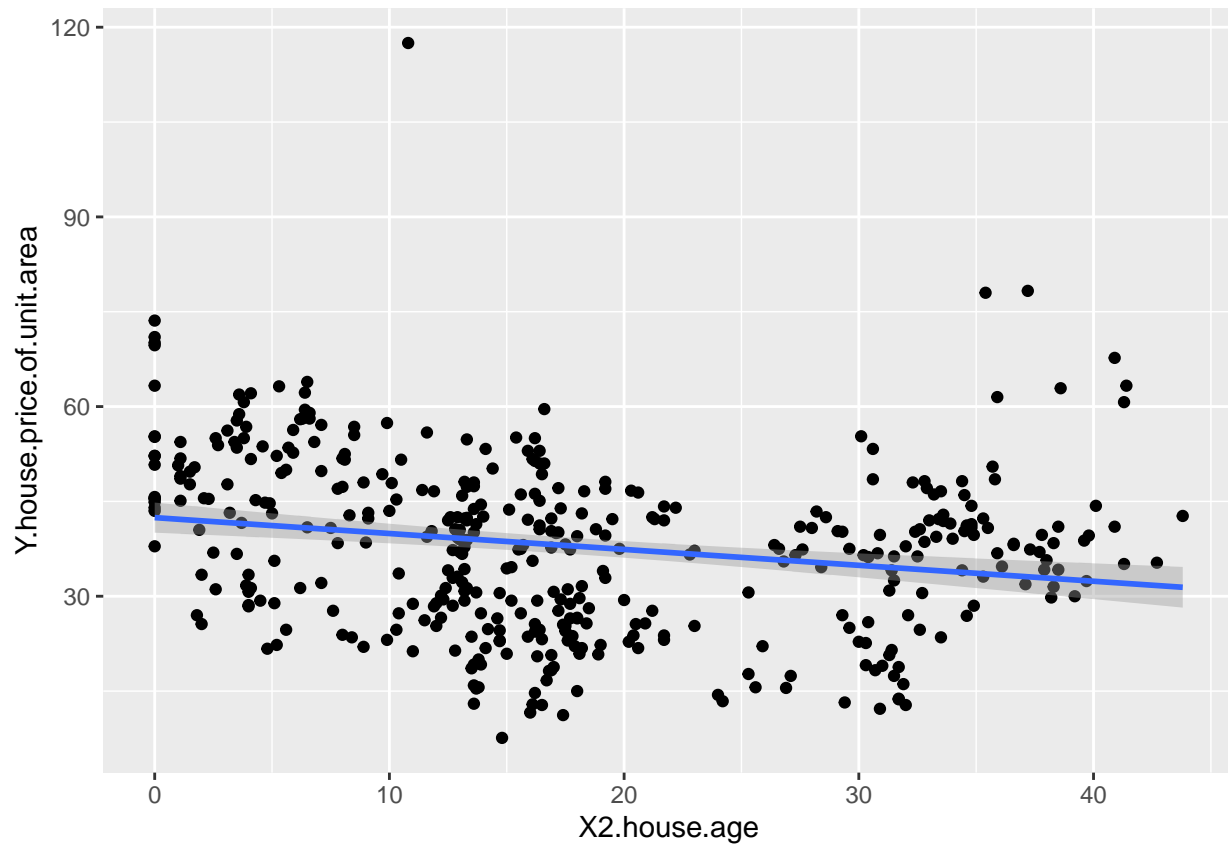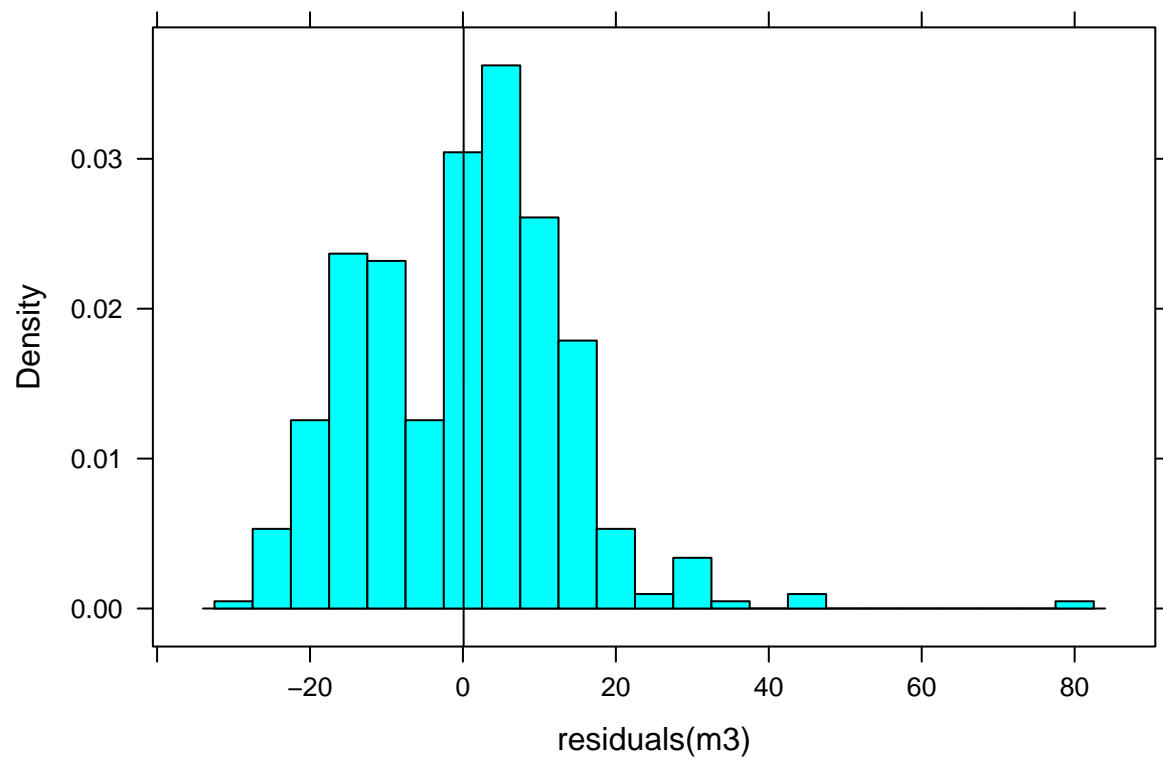
```
xyplot(resid(m1)~fitted(m3), data=real_estate, type=c("p","r"))
```
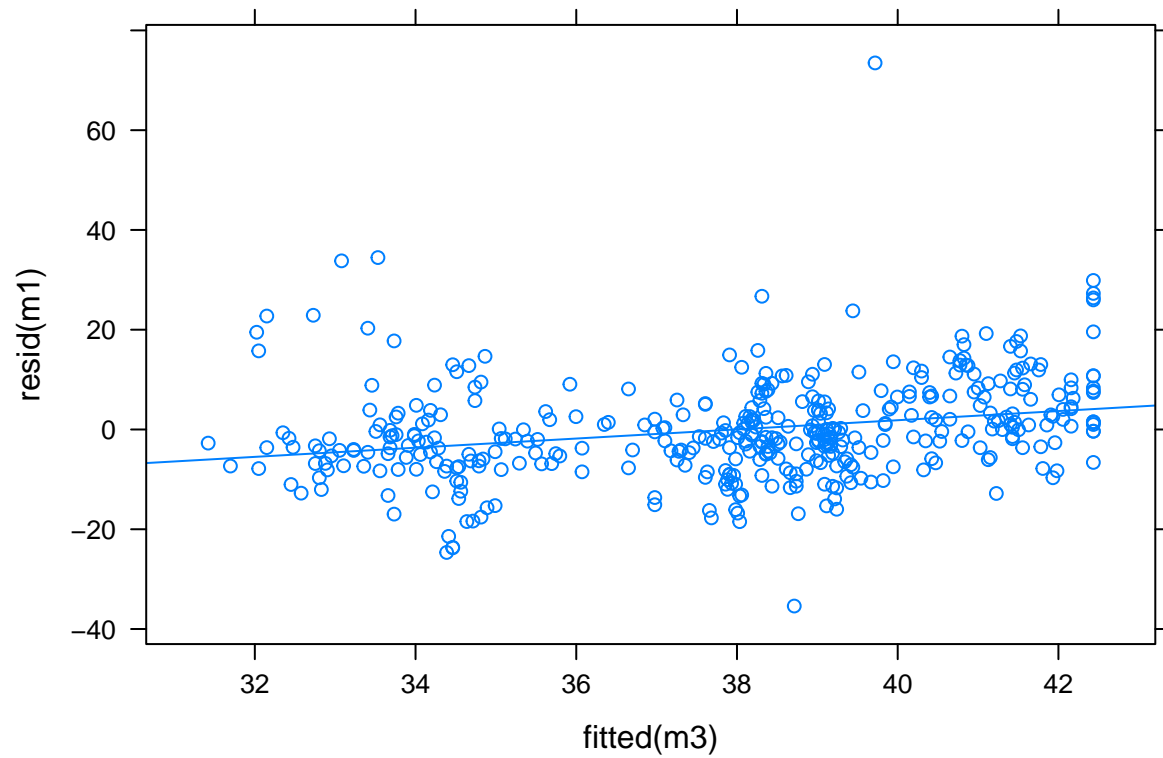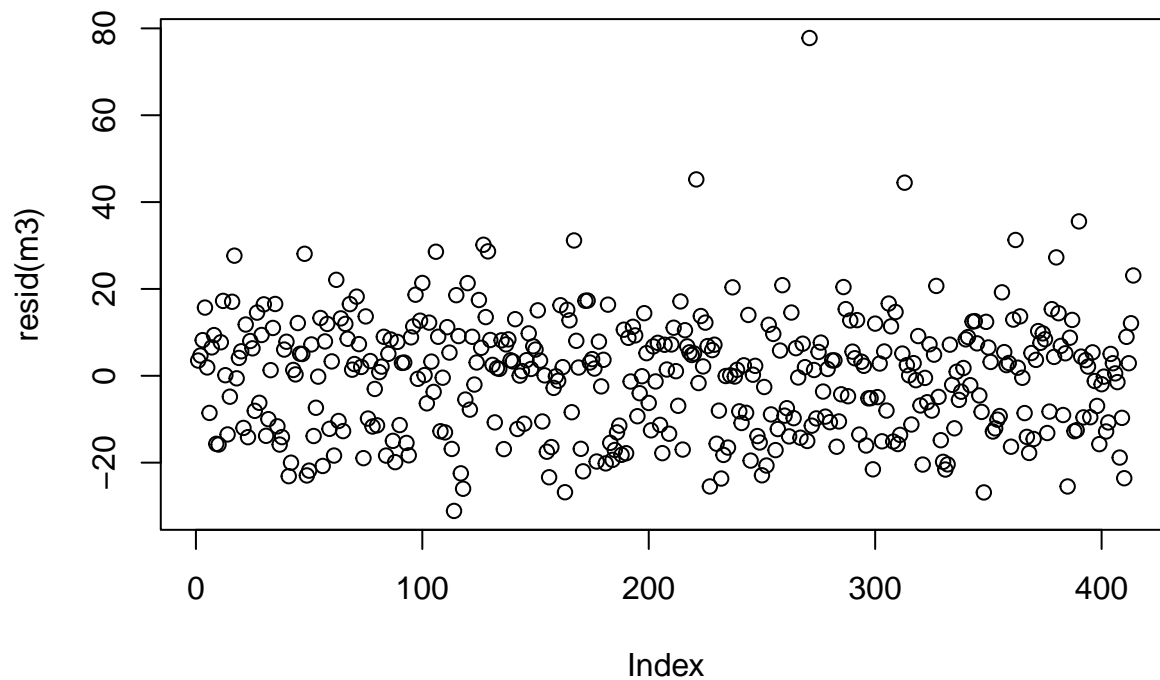
```
histogram(residuals(m3),width=5)
```
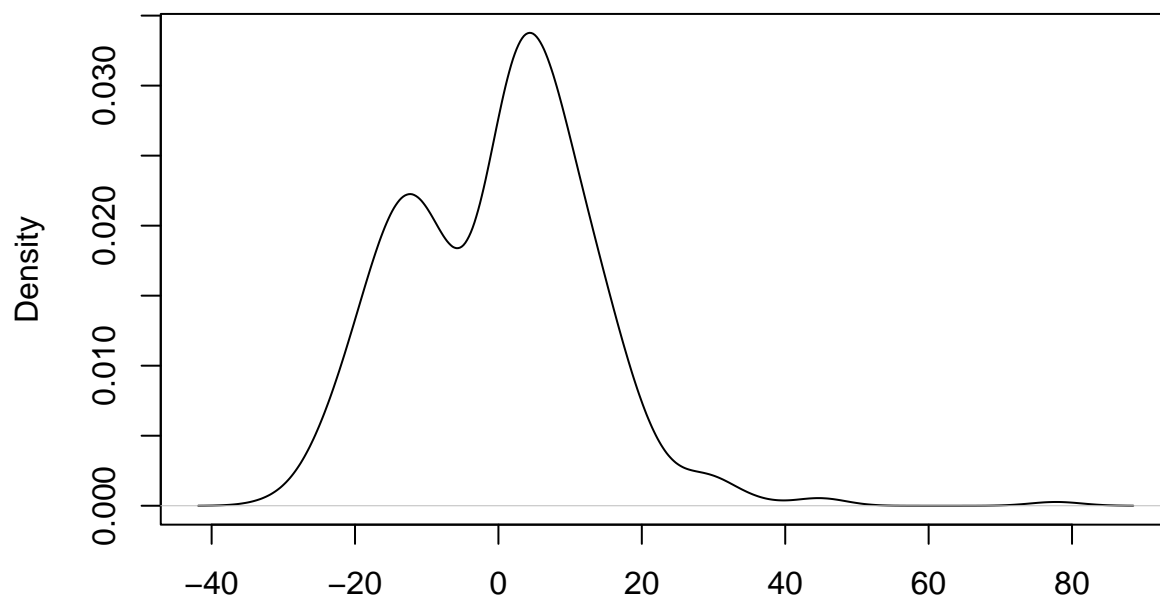


```
ladd(panel.qqmathline(resid(m3)))
```



```
plot(resid(m3))
```
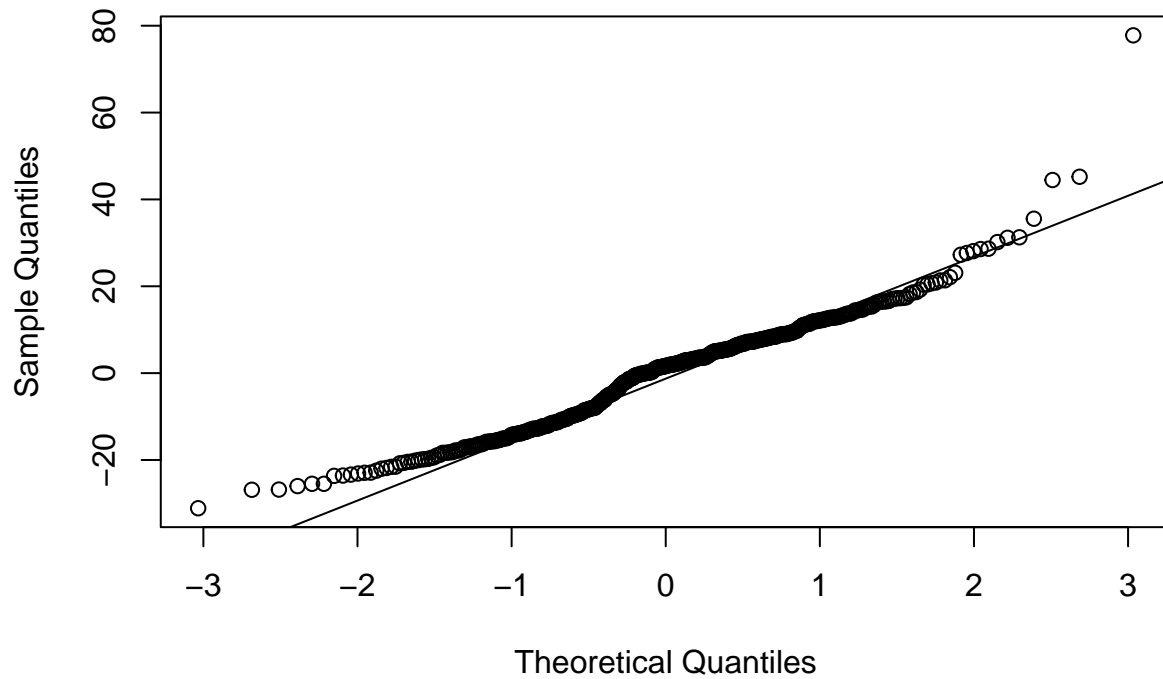
```
plot(density(resid(m3)))
```

density.default(x = resid(m3))

N = 414   Bandwidth = 3.587

```
qqnorm(resid(m3))
qqline(resid(m3))
```

Normal Q–Q Plot

Conclusion:

From the above graphs, the relationship between house price and house age is not linear, and from Q_Q plot also, we can see that the residuals are not on a straight lines and uniform distribution of error around y=0 horizontal lines doesn't hold also, so we should not use linear model to predict the house price based on house age. And if we build the model, we can see that the R-squared value is around 4%, which also indicates linear model is not suitable to predict the house price based on house age.