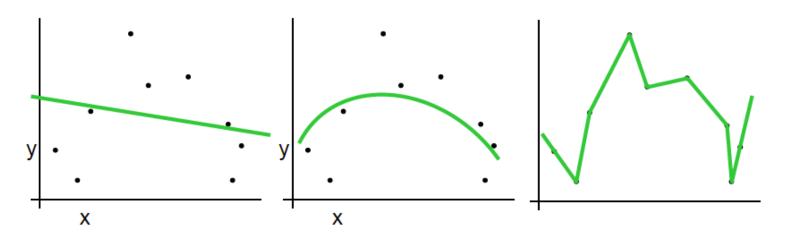
Cross-validation for detecting and preventing overfitting

Note to other teachers and users of these slides. Andrew would be delighted if you found this source material useful in giving your own lectures. Feel free to use these slides verbatim, or to modify them to fit your own needs. PowerPoint originals are available. If you make use of a significant portion of these slides in your own lecture, please include this message, or the following link to the source repository of Andrew's tutorials: http://www.cs.cmu.edu/~awm/tutorials. Comments and corrections gratefully received.

Andrew W. Moore
Professor
School of Computer Science
Carnegie Mellon University

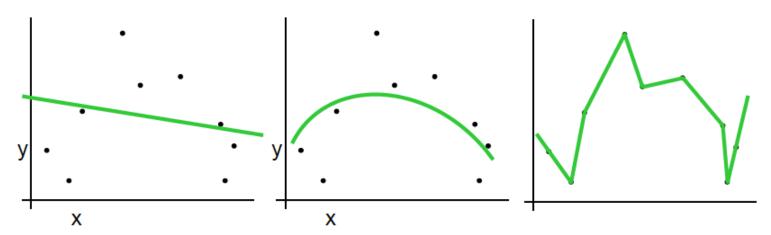
www.cs.cmu.edu/~awm awm@cs.cmu.edu 412-268-7599

Which is best?



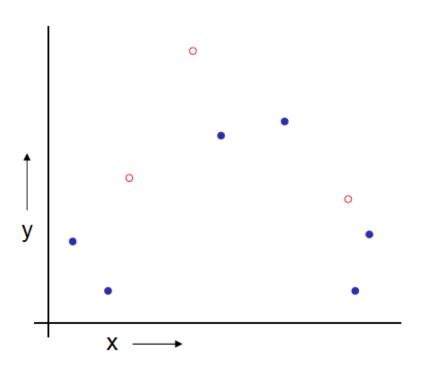
Why not choose the method with the best fit to the data?

What do we really want?

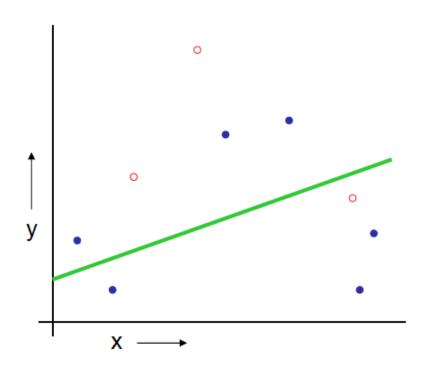


Why not choose the method with the best fit to the data?

"How well are you going to predict future data drawn from the same distribution?"

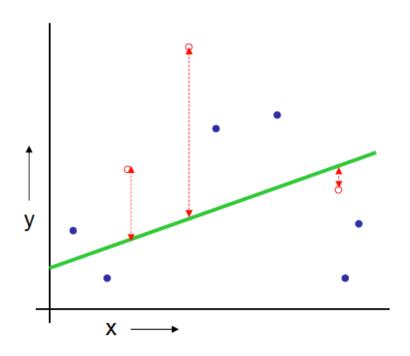


- Randomly choose
 of the data to be in a test set
- 2. The remainder is a training set



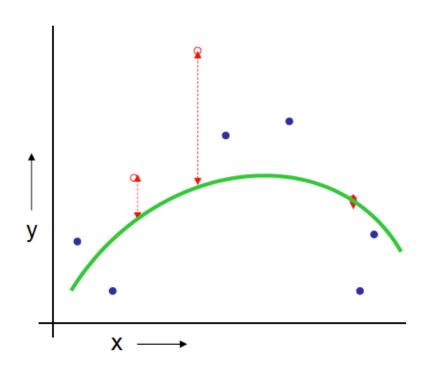
- Randomly choose
 of the data to be in a test set
- 2. The remainder is a training set
- 3. Perform your regression on the training set

(Linear regression example)



(Linear regression example)
Mean Squared Error = 2.4

- Randomly choose
 of the data to be in a test set
- 2. The remainder is a training set
- 3. Perform your regression on the training set
- 4. Estimate your future performance with the test set



(Quadratic regression example)

Mean Squared Error = 0.9

- Randomly choose
 of the data to be in a test set
- 2. The remainder is a training set
- 3. Perform your regression on the training set
- 4. Estimate your future performance with the test set

Good news:

- Very very simple
- Can then simply choose the method with the best test-set score

Bad news:

•What's the downside?

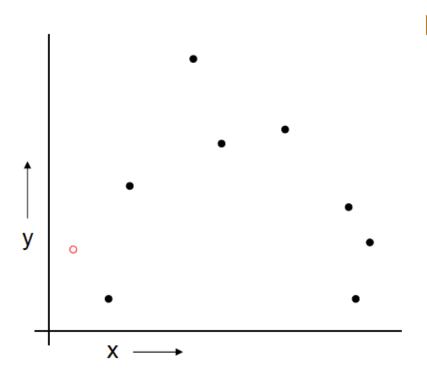
Good news:

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Bad news:

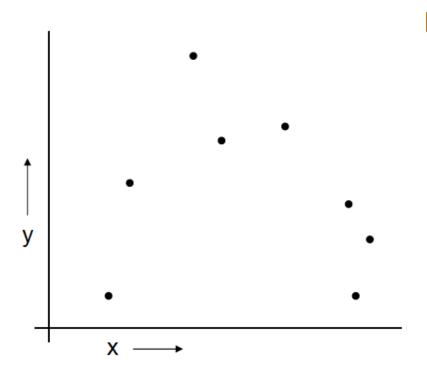
- Wastes data: we get an estimate of the best method to apply to 30% less data
- If we don't have much data, our test-set might just be lucky or unlucky

We say the "test-set estimator of performance has high variance"



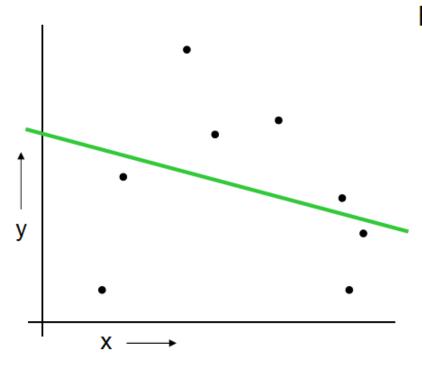
For k=1 to R

1. Let (x_k, y_k) be the k^{th} record



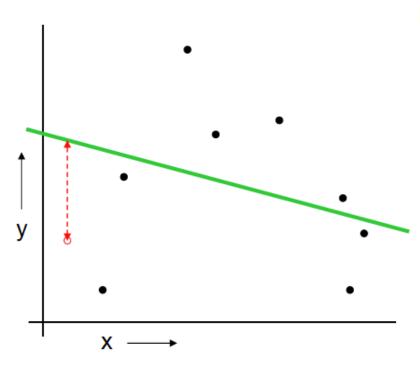
For k=1 to R

- 1. Let (x_k, y_k) be the k^{th} record
- 2. Temporarily remove (x_k, y_k) from the dataset



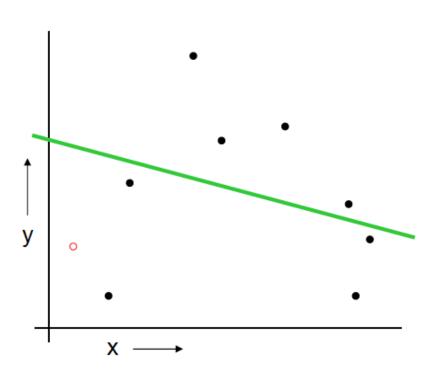
For k=1 to R

- 1. Let (x_k, y_k) be the k^{th} record
- 2. Temporarily remove (x_k, y_k) from the dataset
- Train on the remaining R-1 datapoints



For k=1 to R

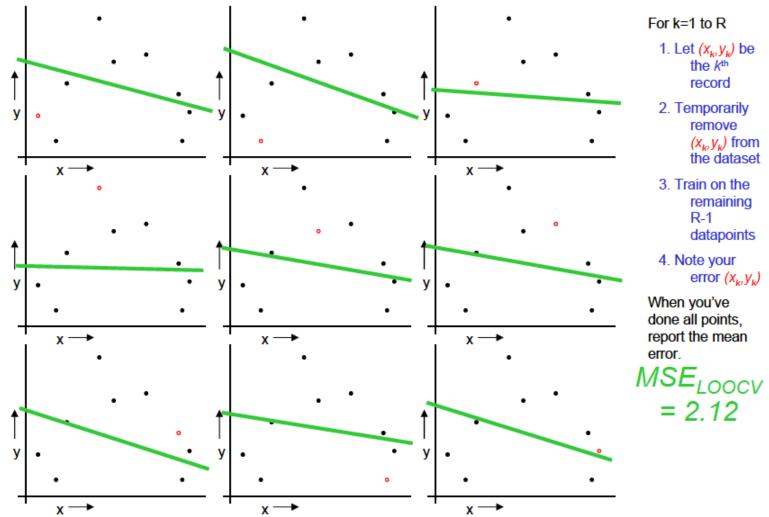
- 1. Let (x_k, y_k) be the k^{th} record
- 2. Temporarily remove (x_k, y_k) from the dataset
- Train on the remaining R-1 datapoints
- 4. Note your error (x_k, y_k)



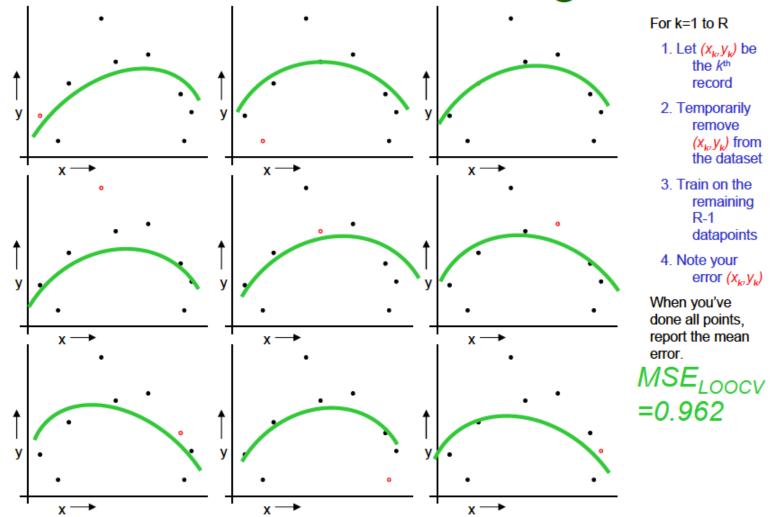
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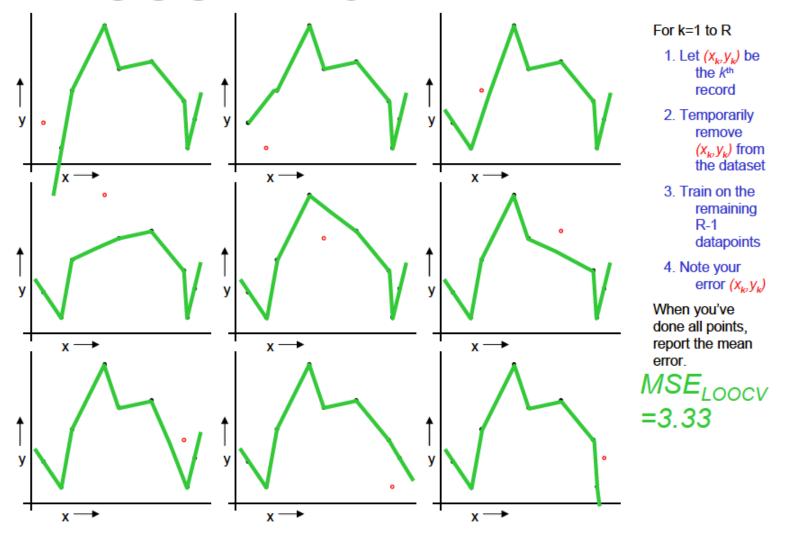
When you've done all points, report the mean error.



LOOCV for Quadratic Regression



LOOCV for Join The Dots

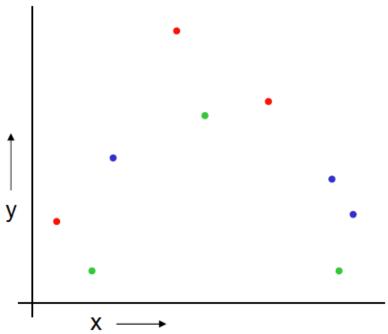


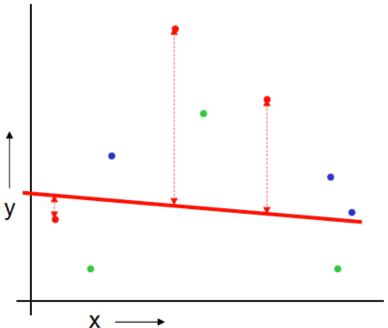
Which kind of Cross Validation?

	Downside	Upside
Test-set	Variance: unreliable estimate of future performance	Cheap
Leave- one-out	Expensive. Has some weird behavior	Doesn't waste data

..can we get the best of both worlds?

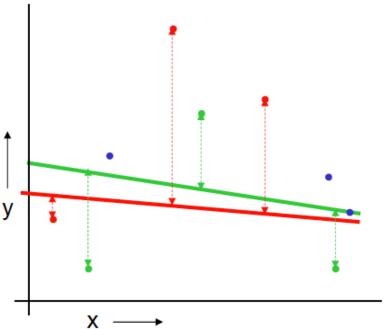
Randomly break the dataset into k partitions (in our example we'll have k=3 partitions colored Red Green and Blue)





Randomly break the dataset into k partitions (in our example we'll have k=3 partitions colored Red Green and Blue)

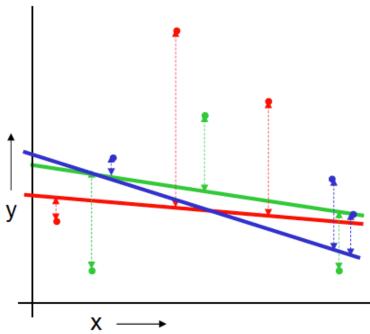
For the red partition: Train on all the points not in the red partition. Find the test-set sum of errors on the red points.



Randomly break the dataset into k partitions (in our example we'll have k=3 partitions colored Red Green and Blue)

For the red partition: Train on all the points not in the red partition. Find the test-set sum of errors on the red points.

For the green partition: Train on all the points not in the green partition. Find the test-set sum of errors on the green points.



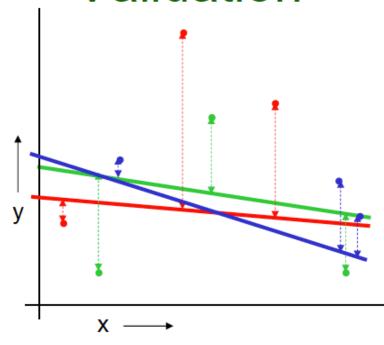
Randomly break the dataset into k partitions (in our example we'll have k=3 partitions colored Red Green and Blue)

For the red partition: Train on all the points not in the red partition. Find the test-set sum of errors on the red points.

For the green partition: Train on all the points not in the green partition.

Find the test-set sum of errors on the green points.

For the blue partition: Train on all the points not in the blue partition. Find the test-set sum of errors on the blue points.



Linear Regression MSE_{3FOLD} =2.05

Randomly break the dataset into k partitions (in our example we'll have k=3 partitions colored Red Green and Blue)

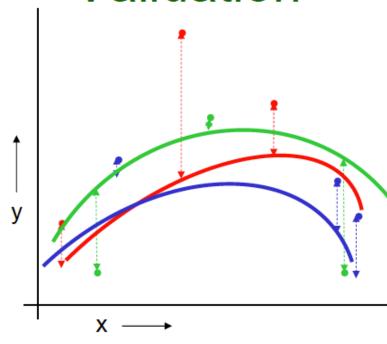
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Find the test-set sum of errors on the green points.

For the blue partition: Train on all the points not in the blue partition. Find the test-set sum of errors on the blue points.

Then report the mean error



Quadratic Regression MSE_{3FOLD} =1.11

Randomly break the dataset into k partitions (in our example we'll have k=3 partitions colored Red Green and Blue)

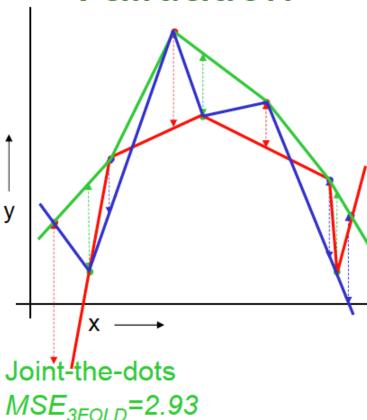
For the red partition: Train on all the points not in the red partition. Find the test-set sum of errors on the red points.

For the green partition: Train on all the points not in the green partition.

Find the test-set sum of errors on the green points.

For the blue partition: Train on all the points not in the blue partition. Find the test-set sum of errors on the blue points.

Then report the mean error



Randomly break the dataset into k partitions (in our example we'll have k=3 partitions colored Red Green and Blue)

For the red partition: Train on all the points not in the red partition. Find the test-set sum of errors on the red points.

For the green partition: Train on all the points not in the green partition.

Find the test-set sum of errors on the green points.

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Then report the mean error

Which kind of Cross Validation?

	Downside	Upside
Test-set	Variance: unreliable estimate of future performance	Cheap
Leave- one-out	Expensive. Has some weird behavior	Doesn't waste data
10-fold	Wastes 10% of the data. 10 times more expensive than test set	Only wastes 10%. Only 10 times more expensive instead of R times.
3-fold	Wastier than 10-fold. Expensivier than test set	Slightly better than test- set
R-fold	Identical to Leave-one-out	