

Quiz 08.md

## Quiz 08

Attempts	Score
1/1000	9/9

### Question 01

What is the dictionary used in JPEG?

#### Answer

Discrete cosine transform (DCT).

#### Explanation

### Question 02

Consider a  $2 \times 4$  dictionary  $D$  composed of the transpose of the 2-dimensional atoms  $(0,1)$ ,  $(1,1)$ ,  $(0,1)$ , and  $(2,1)$  (these form the columns of  $D$ ). The sparsest representation of the vector  $x=(2,2)$  is given by the transpose of (these are the  $\alpha$ ):

#### Answer

$(0,2,0,0)$

#### Explanation

### Question 03

We want to obtain sparse representations of signals of dimension  $N = 64$ . We have a dictionary with  $k = 100$  atoms. How many possible active sets (subspaces) we have with sparsity  $L = 3$ ?

#### Answer

$(100!)/((97!)(3!))$

#### Explanation

### Question 04

Consider the Gaussian Mixture Model in the last video. We want to use it to represent signals in  $N = 64$  dimensions. If we have  $k = 100$  Gaussians in the mixture, then the number of possible active sets (subspaces) is

#### Answer

100

#### Explanation

### Question 05

Are sparse modeling and compressed sensing the same?

## Answer

No, sparse modeling is about signal models and representations; compressed sensing is about an efficient novel data acquisition protocol.

## Explanation

## Question 06

What needs to change in the general expression of image denoising we used for sparse modeling (equation in slide 4 of the 1st video this week) if instead of Gaussian additive noise we consider other types of additive noise?

## Answer

We need to change the data fitting term, relationship with measurements, from a quadratic penalty to a penalty tailored to the noise.

## Explanation

## Question 07

Consider a dictionary D composed of both the complete DCT basis and the complete Fourier basis, a concatenation of both. Will the representation of a signal be unique when using such dictionary?

## Answer

No, there will be at least two different possible representations for all signals.

## Explanation

## Question 08

Consider you have a dictionary composed of 100 random  $10 \times 10$  patches from the given image. If you perform sparse coding with this dictionary:

## Answer

The average number of non-zero coefficients will be equal or greater than when using the dictionary of the same size for sparse representations, obtained with  $\min_{\mathbf{D}, \alpha} \|\alpha\|_0 \quad \text{s.t.} \quad \sum_i \|\mathbf{D}\alpha - \mathbf{y}_i\|_2^2 \leq \epsilon$  where  $\mathbf{y}_i$  is an image patch.

## Explanation

## Question 09

Consider a video and use the patches of the current frame as dictionary for encoding the next frame. For scenes with only static objects:

## Answer

This will result in very sparse codes on average.

## Explanation