

What is inpainting?



- **Modifying an image in a non-detectable form**



Detail of "Cornelia, Mother of the Gracchi" by J. Suvee (Louvre). Courtesy of Emile-Male "The Restorer's Handbook of easel painting".

Another example



Photo restoration



Object removal



Real world example: Object removal



From D. King, "The Commissar vanishes".

Object removal



Lenin and friend Trotsky



Where is ex-friend Trotsky?

From www.newseum.org

Object removal: What can't be done?



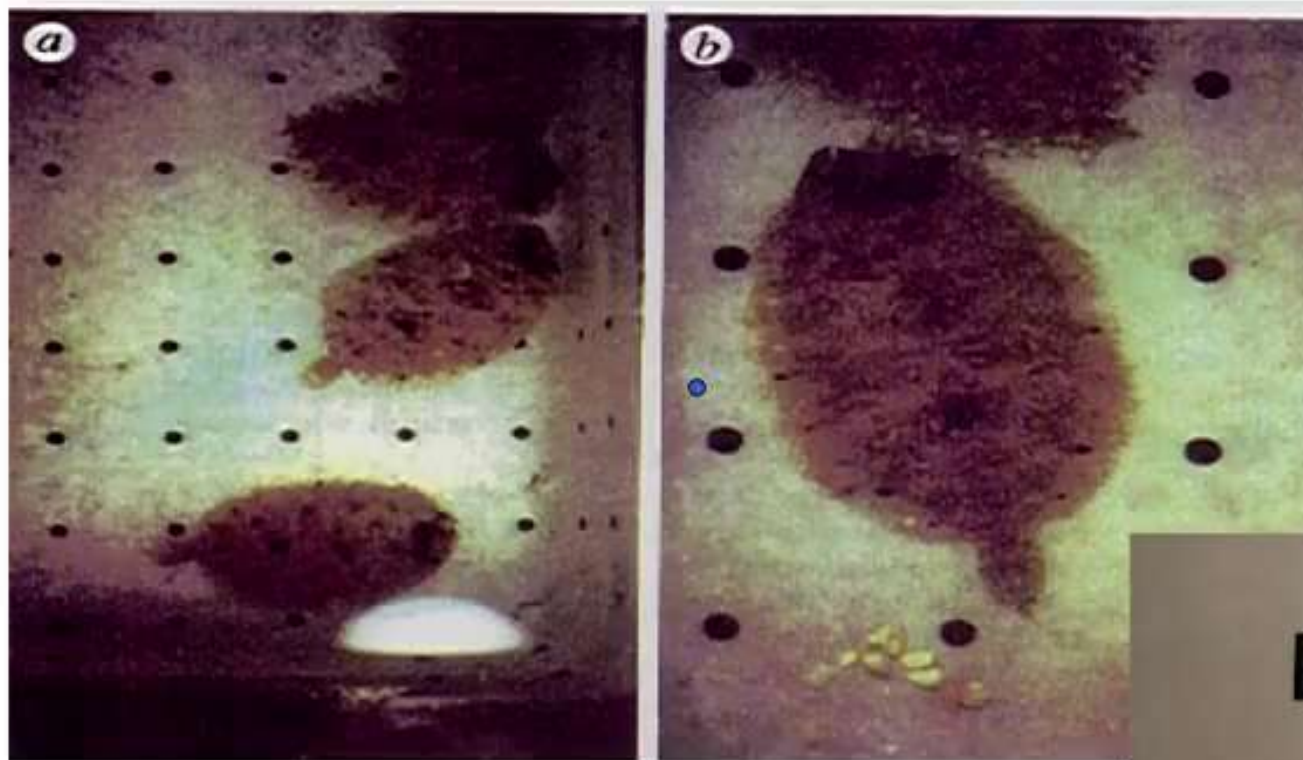
Biological inpainting



Biological inpainting



Biological inpainting



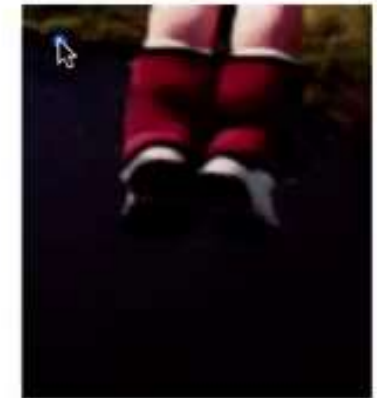
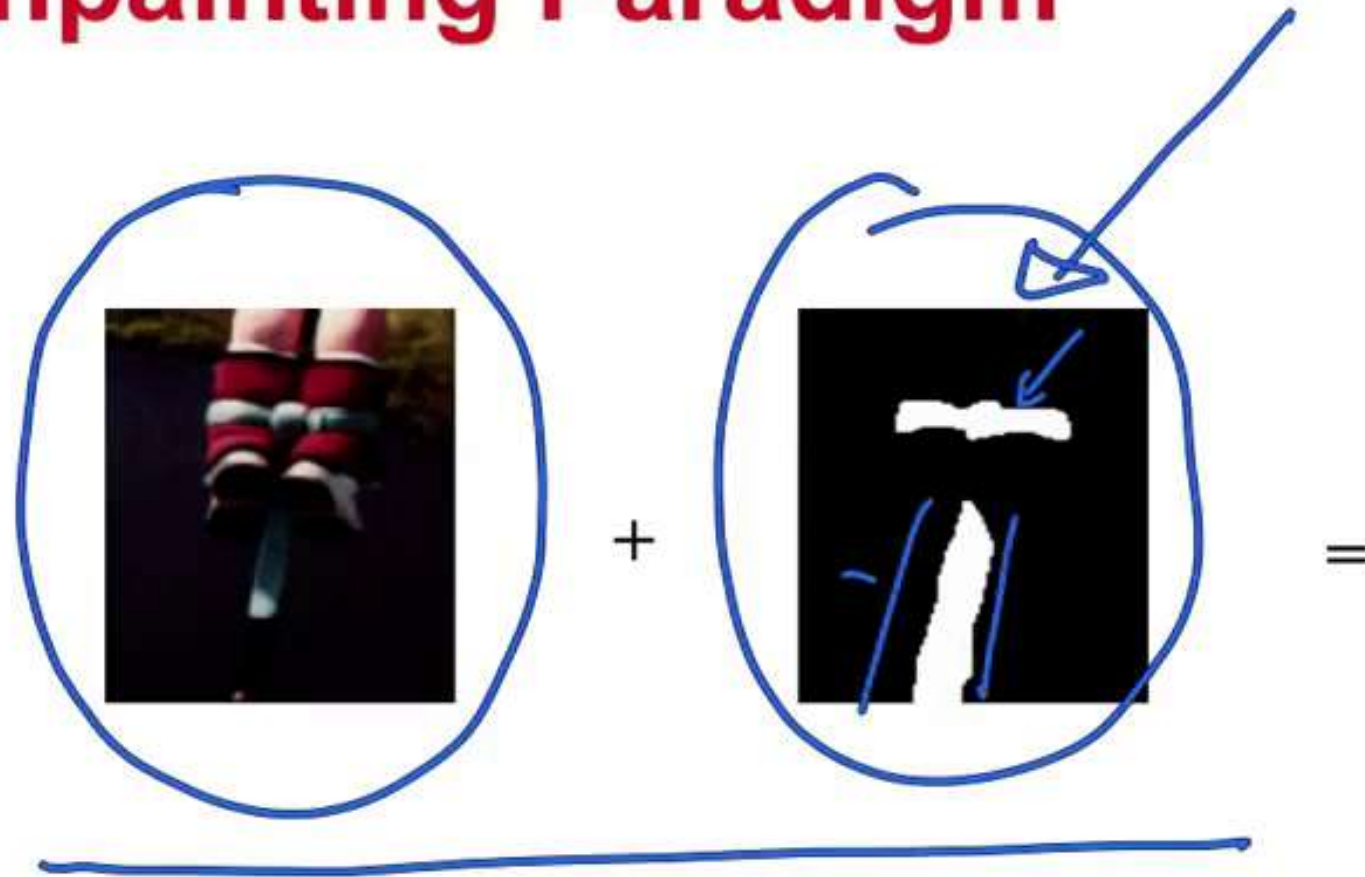
Courtesy of Ramachandran et al.

Human Blind Spot

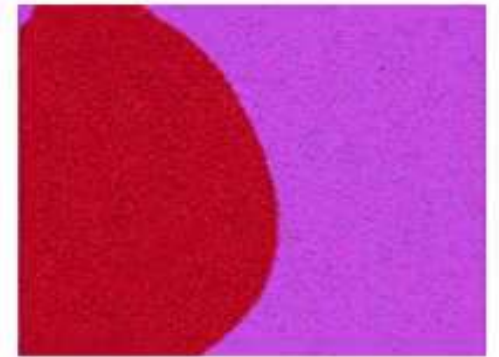
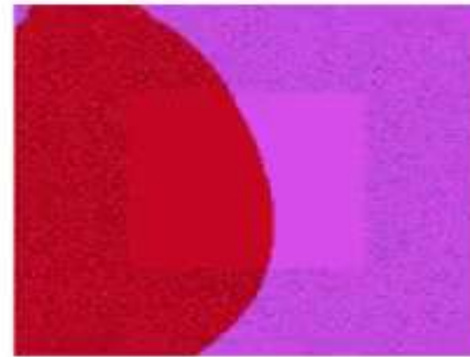
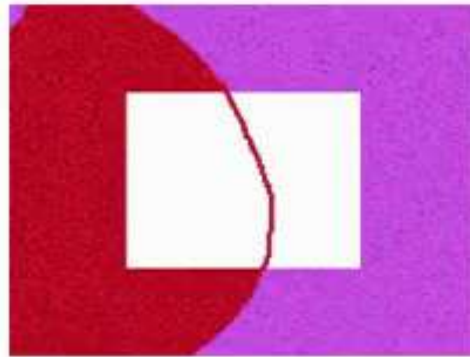
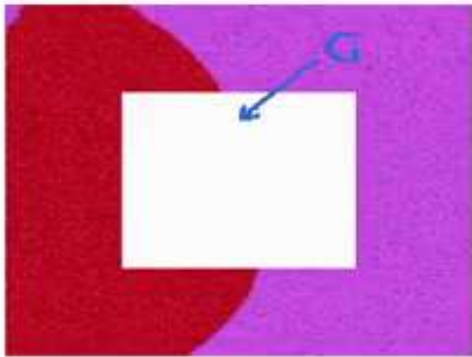


http://info.med.yale.edu/neurobio/mccormick/fill_in_seminar/figure16.html

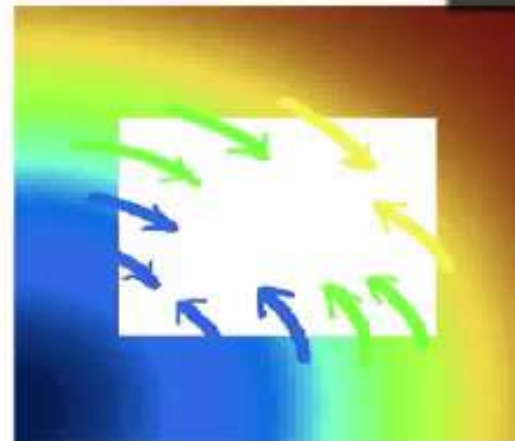
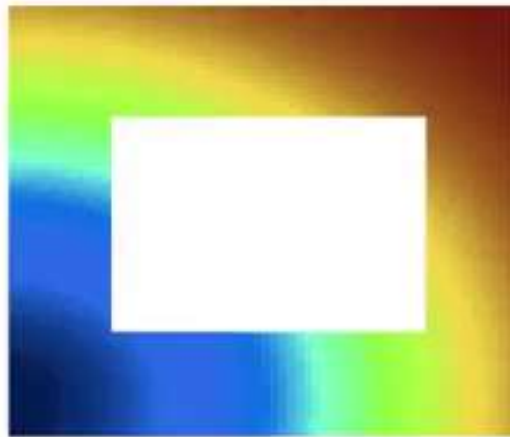
Inpainting Paradigm



How conservators inpaint?



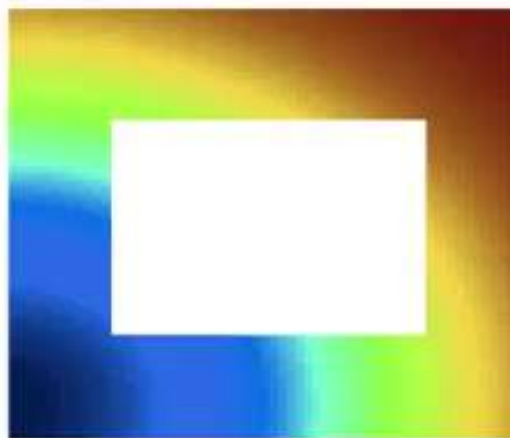
Automatic digital inpainting



$$\nabla L \cdot \vec{N} = 0$$

$L = \text{Information}$
 $N = \text{direction}$

Automatic digital inpainting



$$A = 0$$

$$\frac{\partial I}{\partial t} = A$$

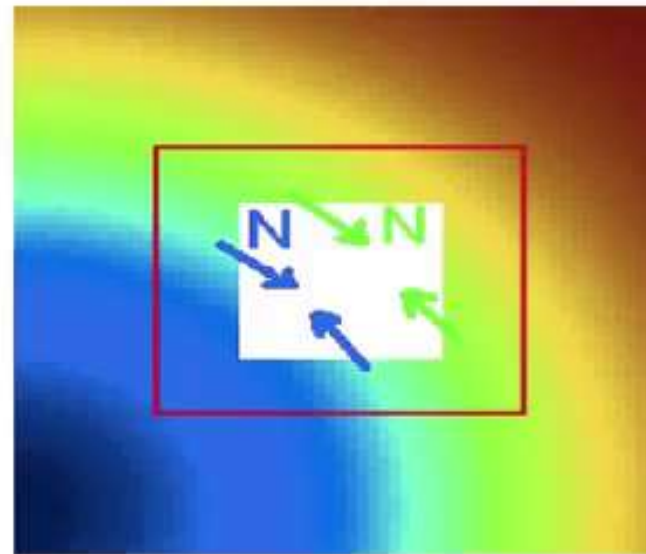
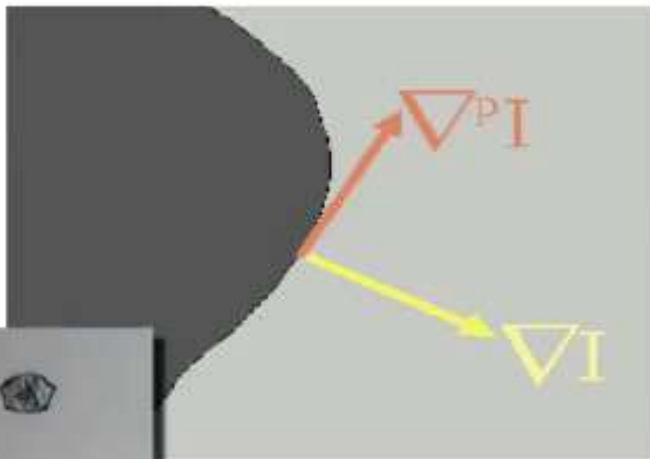
$$\nabla L \cdot \vec{N} = 0$$

$$0 - \frac{\partial I}{\partial t} = \nabla L \cdot \vec{N}$$



- **L = smoothness estimator (Laplacian)**
- **N = isophote direction (time variant)**

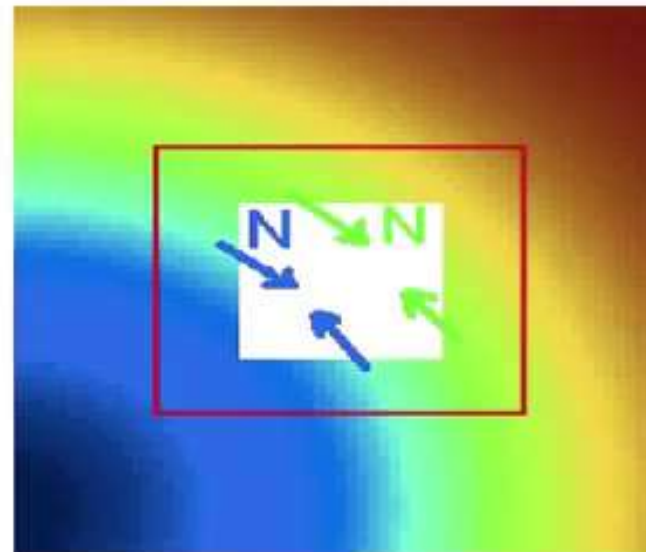
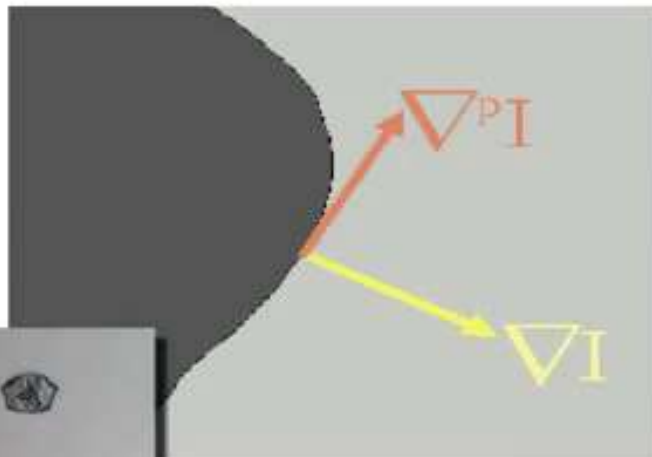
$$N = \nabla I^\perp$$



- **L = smoothness estimator (Laplacian)**
- **N = isophote direction (time variant)**

$$N = \nabla I^\perp$$

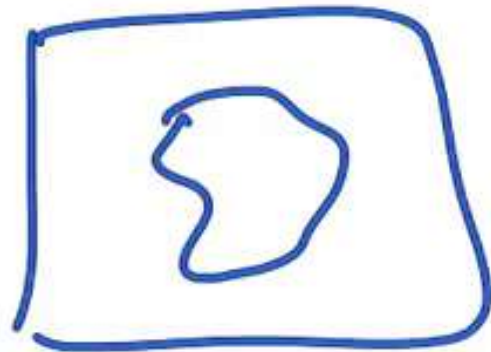
$$L = \nabla^2 I$$



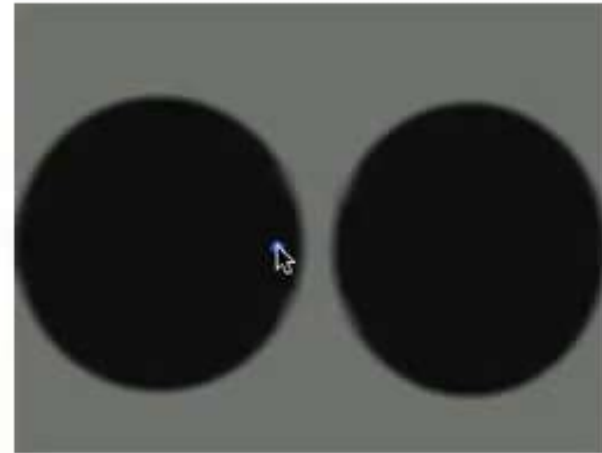
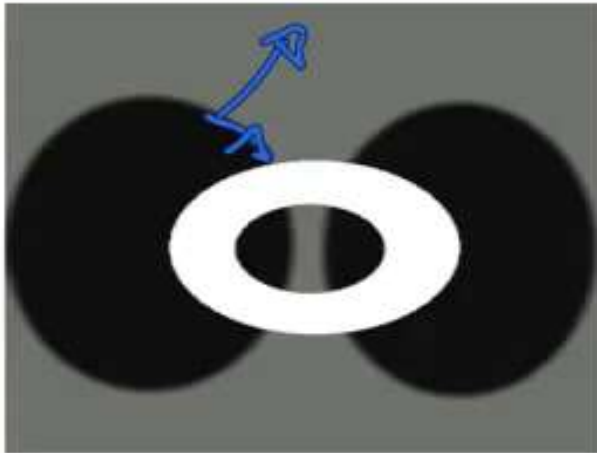
The equation

$$\Delta I = I_{xx} + I_{yy}$$

$$\frac{\partial I}{\partial t} = \nabla(\Delta I) \cdot \nabla_{\vec{N}}^{\perp} I = 0$$



Example



Courtesy of ACM



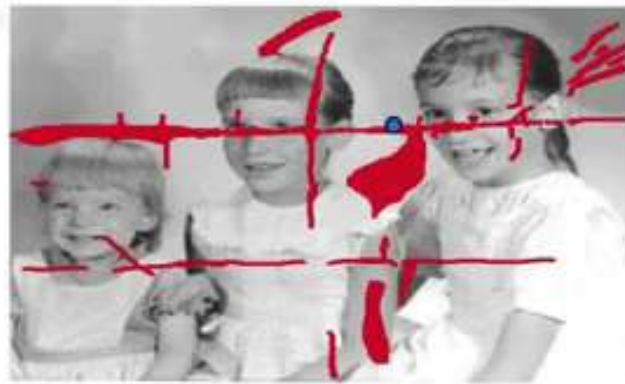
Example: Text removal



Courtesy of ACM



Example: Photo restoration



Courtesy of ACM

Example: Special effects



← ↩ ↪ → Courtesy of ACM

Example: Special effects



Example: Special effects



Example: Scratch removal



Automatic image inpainting/interpolation for compression and wireless transmission



Courtesy
of IEEE

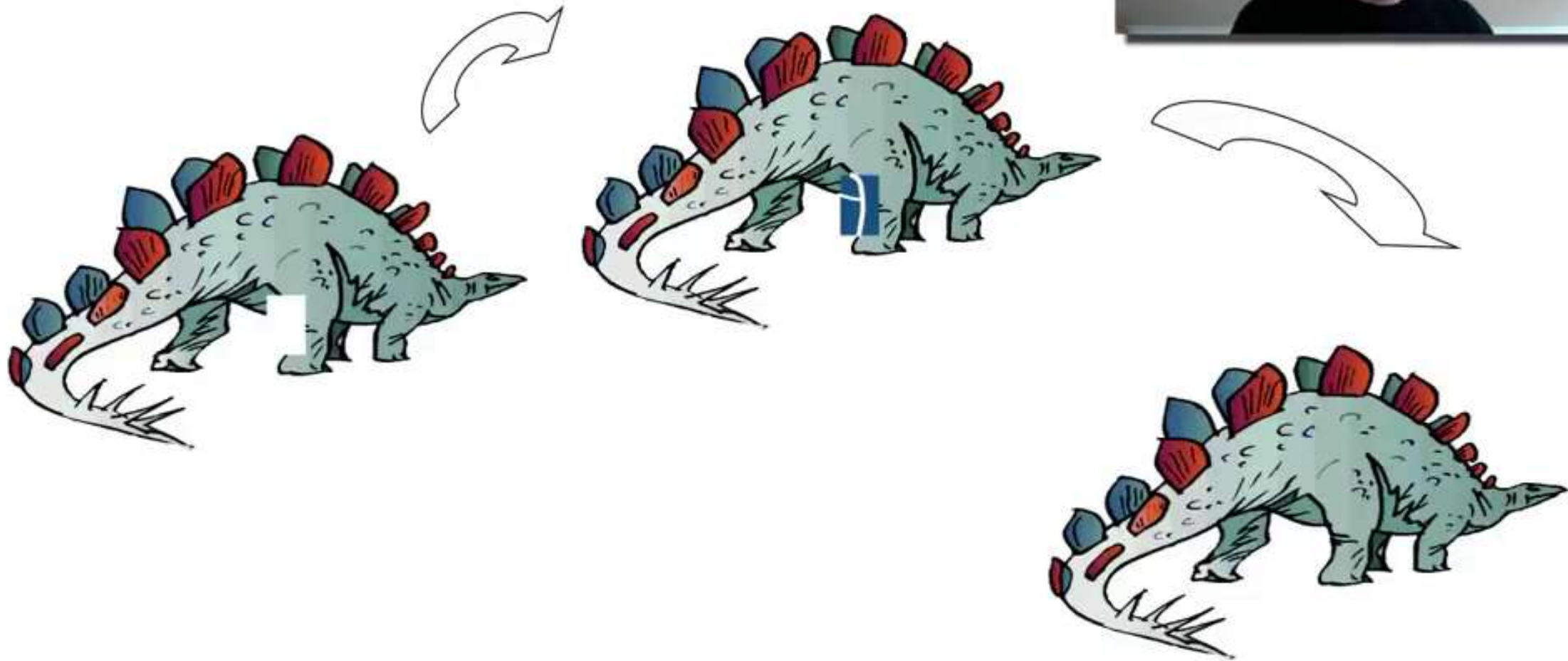
$$\dot{\mathbf{I}}_t = \nabla (\Delta \mathbf{I}) \cdot (\nabla \mathbf{I})^\perp$$



Courtesy
of IEEE

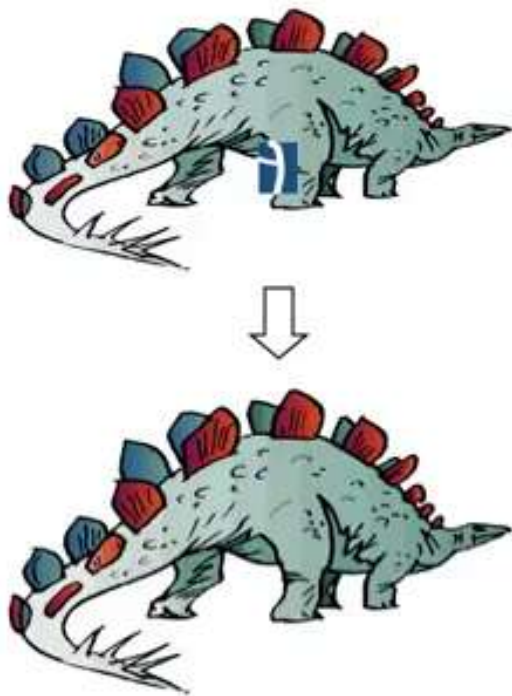


How conservators fill-in



Interpolate the gray values given the edges

$$\theta = \frac{\nabla I}{|\nabla I|}$$



$$\theta = \text{normalized gradient} \Rightarrow \theta \cdot \nabla I = \|\nabla I\|$$

$$\min(I) \int_{\Omega \cup \text{Band}} (\|\nabla I\| - \theta \cdot \nabla I) d\Omega$$

$$\frac{\partial I}{\partial t} = \text{div} \left(\frac{\nabla I}{\|\nabla I\|} \right) - \text{div}(\theta) = 0$$



Example



The full functional

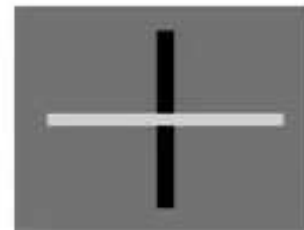
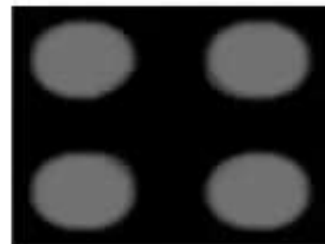
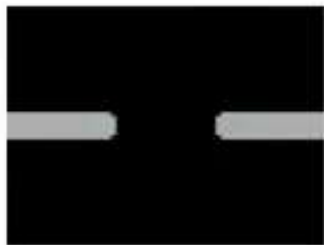
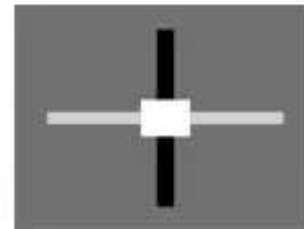
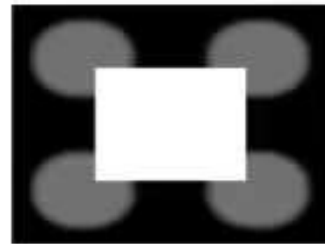
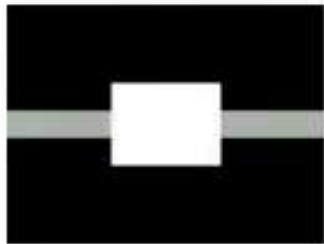
$$\min(I, \theta) \int_{\Omega \cup \text{Band}} \left[\text{div}(\theta)^p (a + b \|\nabla G * I\|) + c(\|\nabla I\| - \theta \cdot \nabla I) \right]$$

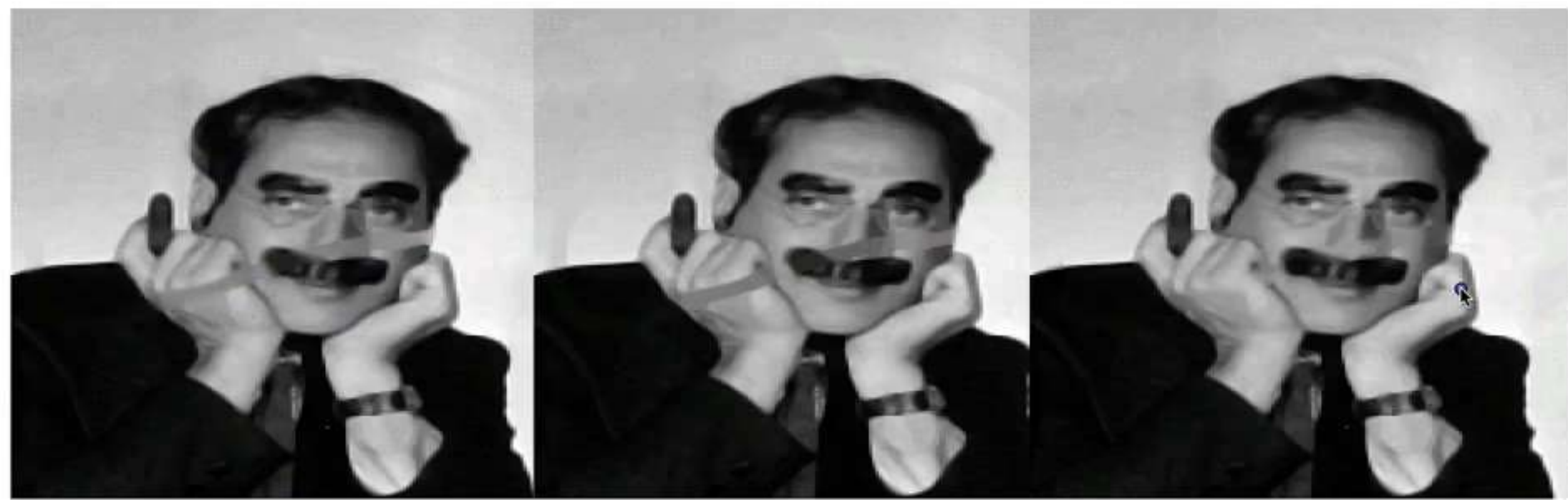
curvature. $\theta = \frac{\nabla I}{|\nabla I|}$

- Solved via E-L: Coupled 2nd order PDEs



Examples

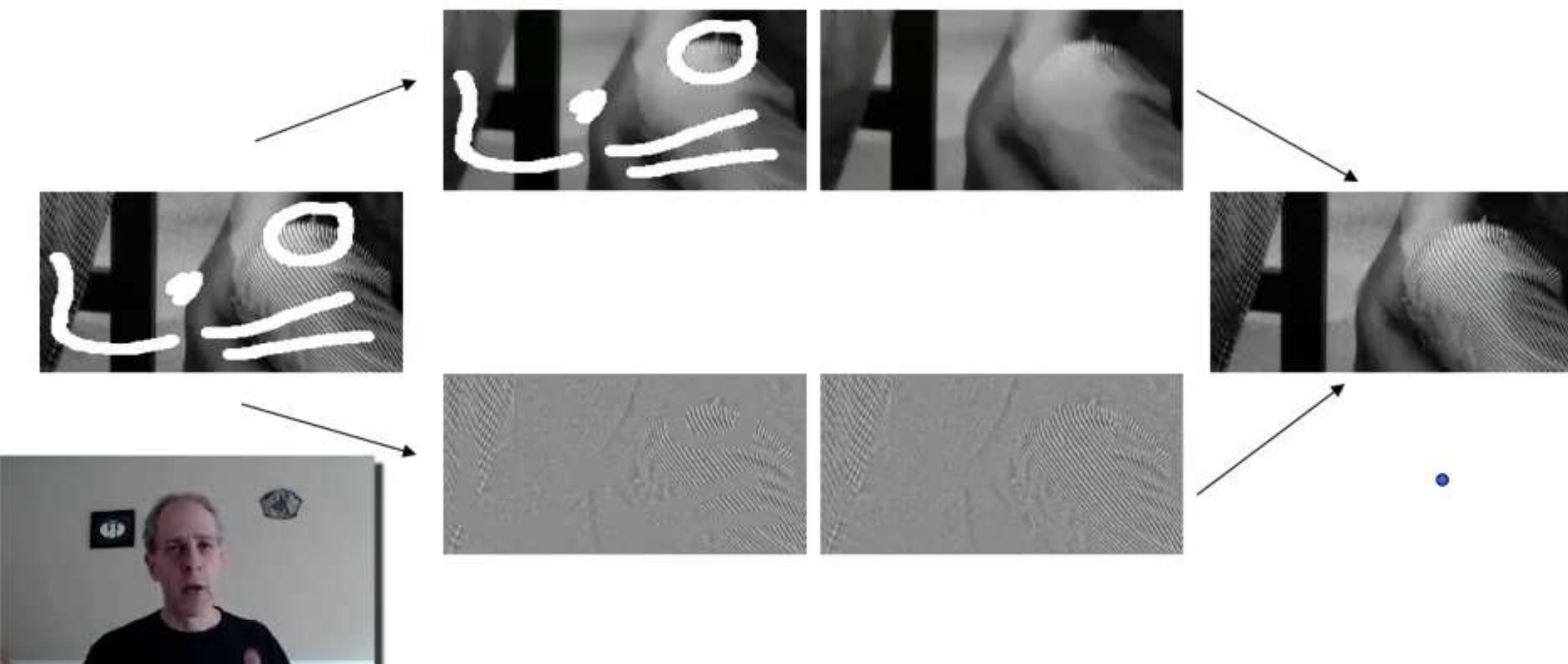




Examples

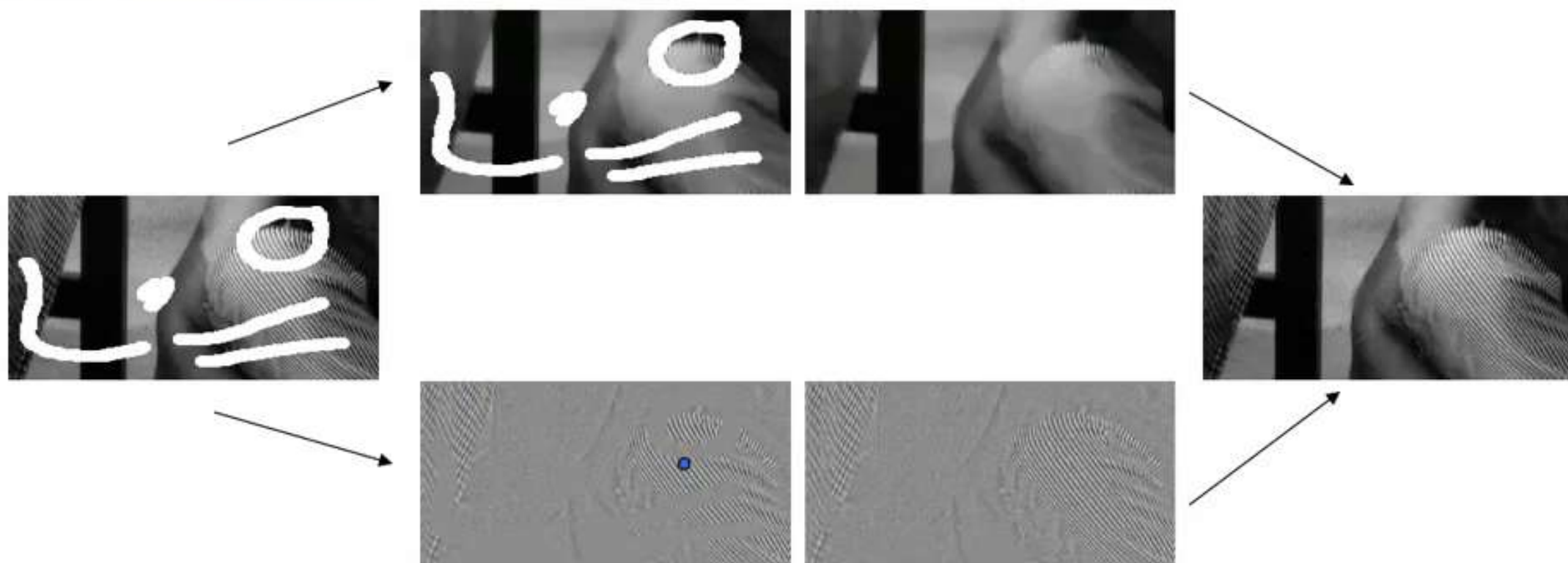


Inpainting and Image Decomposition



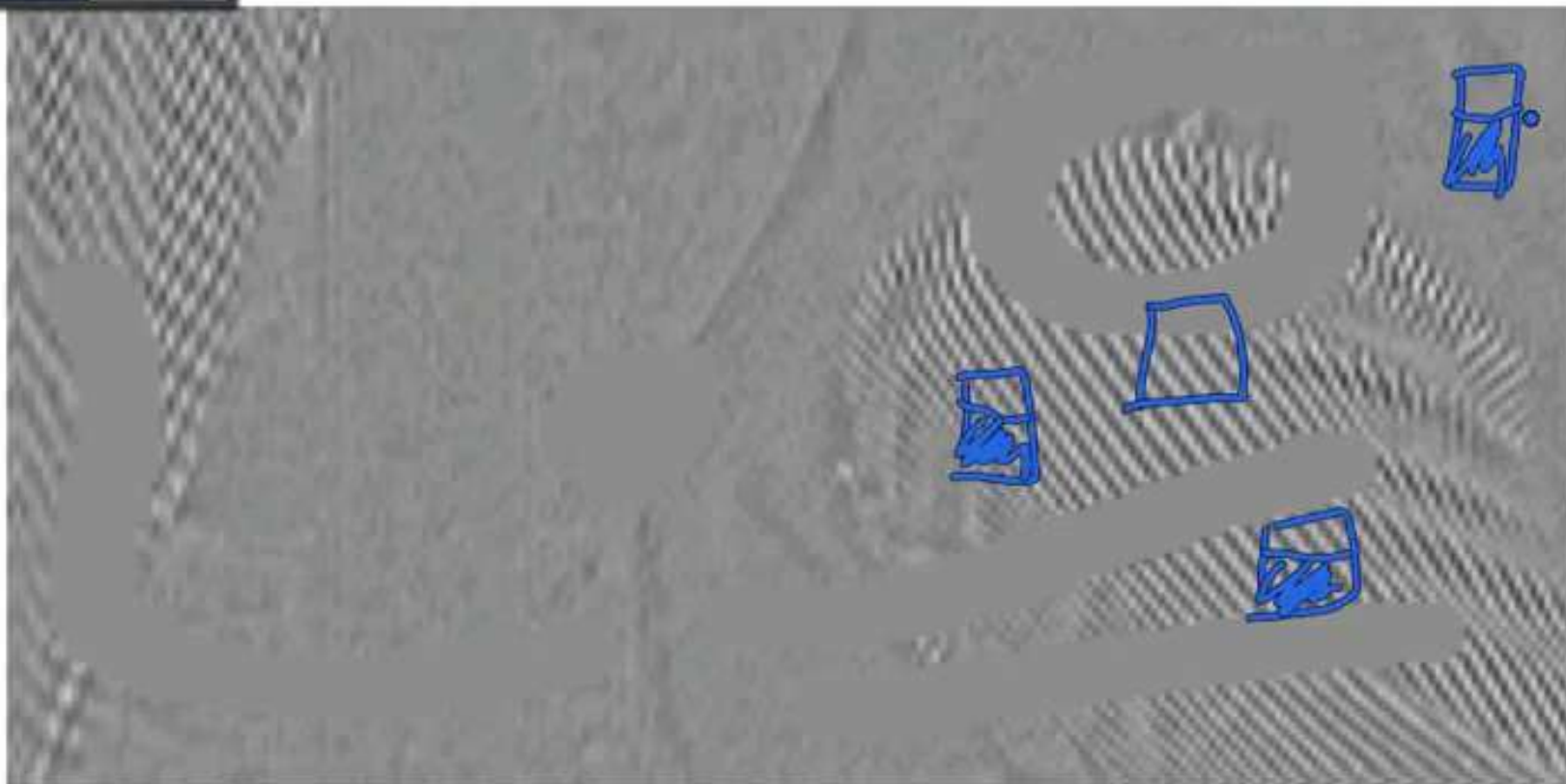


Smart Cut and Paste



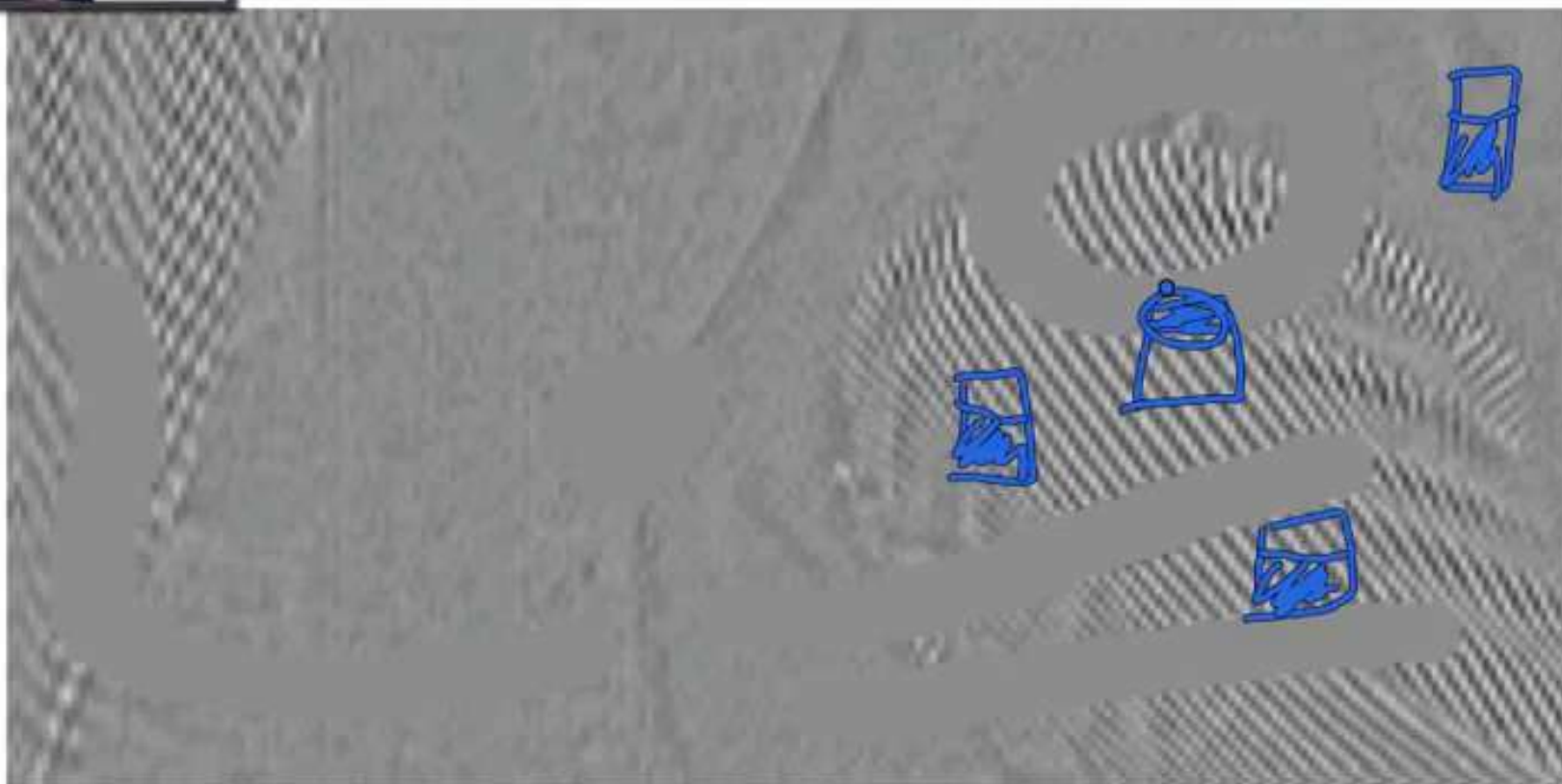


Smart Cut and Paste



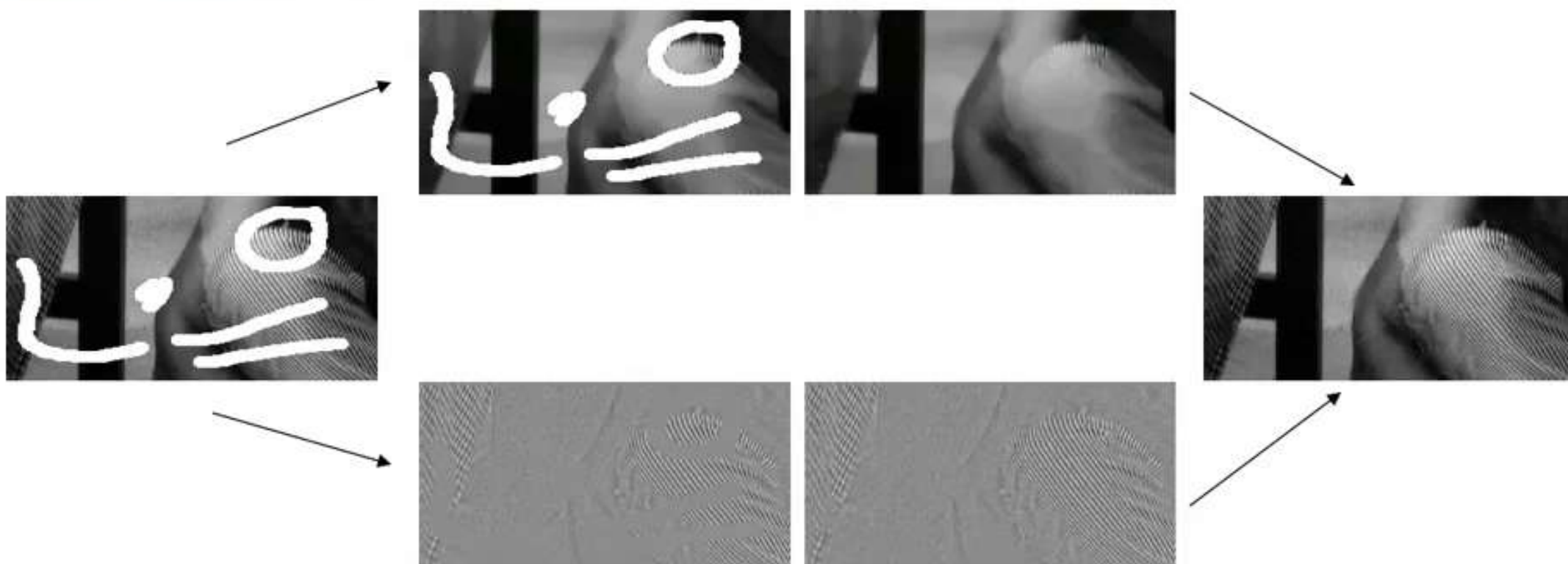


Smart Cut and Paste



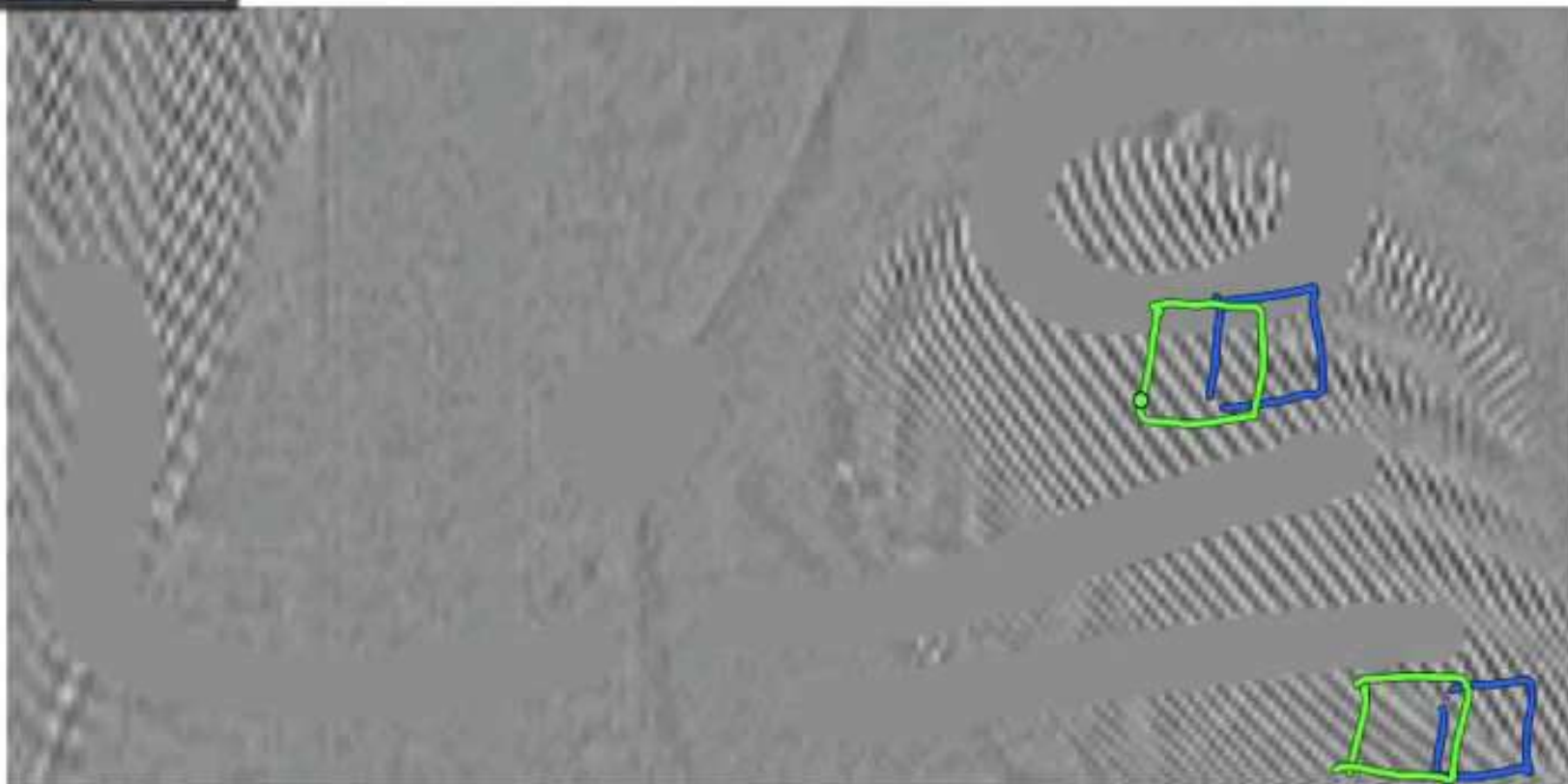


Smart Cut and Paste





Smart Cut and Paste



Combine it All



Courtesy of IEEE



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