

## Reference Book

### Measurement & Error

Def<sup>n</sup>:

- Instrument - device used for determining value or magnitude of a quantity.
- Accuracy - closeness with which an instrument reading approaches true value of variable being measured.
- Precision - measure of reproducibility of the instrument i.e. measure of degree of successive measurements.
- Sensitivity - ratio of output/response of instrument to the change in input.
- Resolution - smallest change in measured value to which the instrument will respond.
- Error - deviation from true value of measured variable

Precision characteristics → conformity

→ number of

significant figures

More significant figures, more is the precision of an instrument

$$\text{Range of error} = E_{\max} - E_{\min} \quad (1) \quad \text{and} \quad E_{\max} - E_{\min} \quad (2)$$

$$\text{Avg range of error} = \frac{(1) + (2)}{2}$$

\* Result of 2 numbers with different accuracy is only as accurate as the least accurate measurement.  
 {Some for multiplication}

Doubtful part i.e.  $k$  in  $\text{num} \pm k$  is always neglected irrespective of addition or subtraction.

$$\% \text{ Range of doubt} = \frac{k}{\text{num}} \times 100$$

Subtraction of measurement is avoided as range of doubt vastly increases

- Instrument: A device for determining the value or magnitude of a quantity or variable.
- Accuracy: Closeness with which an instrument reading approaches the true value of the variable being measured.
- Precision: A measure of reproducibility of the instrument measurement.
- Sensitivity: Ratio of o/p signal or response of instrument to change of input or measured variable.

Resolution: Smallest change in measured values to which the instrument will respond.

Error: Deviation from true value of the measured variable.

eg: 1 kg

0.99 kg

Instrument 1

1.01 kg

Instrument

2

Equally accurate

Accurate

eg: Instrument 1

1.01 kg

± 0.97 kg

0.98 kg

1.02 kg

Precise (choice)

Instrument 2

1.05 kg

1.05 kg

1.04 kg

1.05 kg

Precise instrument may be accurate but accurate instrument is less likely to be precise.

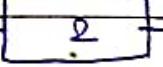
$$\text{Sensitivity} = \frac{\Delta O/P}{\Delta I/P}$$

$$\Delta O/P = 1 \text{ mV}$$



$$\Delta O/P = 1 \text{ V}$$

$$\Delta I/P = 1 \text{ mA}$$



$$\Delta O/P = 5 \text{ V}$$

Depends on

requirement

(user & application)

Beam balance of vegetable vendor would have resolution different from a jeweller.

### Significant figures

SF conveys the actual information regarding the magnitude of the measurement and precision of a quantity.

- (Q) A resistor R is specified as having a value of  $68\ \Omega$  (i.e. the value is closer to  $68\ \Omega$  than to  $67\ \Omega$  or  $69\ \Omega$ )

$$\text{True value} = 67.8\ \Omega$$

\* Population of Nagpur =  $40,00,000$

$$= 4 \times 10^6 \rightarrow \text{b/w } 3 \times 10^6 \text{ & } 5 \times 10^6$$

$$= 40 \times 10^5 \rightarrow \text{b/w } 39 \times 10^5 \text{ & } 41 \times 10^5$$

- (Q) A set of instrument measurements  $117.02V$ ,  $117.11V$ ,  $117.08V$ ,  $117.03V$ .

Range of error

$$\text{lower value} = E_{avg} - E_{min} = 117.06 - 117.02 = 0.04$$

$$\text{higher value} = E_{max} - E_{avg} = 117.11 - 117.06 = 0.05$$

\*\*

\* Check ambiguity of value not significant figures

- (Q)  $R_1 = 18(7)\ \Omega$       } (series (calculate  $R_{eq}$  till))  
 $R_2 = 3.624\ \Omega$       } (appropriate significant figures)

$$R_{eq} = 22.324 = 22.3\ \Omega$$

i.  $318 \text{ A}$

ii.  $35.68 \text{ N}$

iii. ? appropriate significant figures

$V = 113.464$

$\rightarrow 113 V$

1 5 C 2

35.68

318

(28) (5) (4)

35.68 X

16704 X X

191131 C 2 5

## Types of error

### Classifications

#### Gross Error

Caused by human error

- misreading
- incorrect adjustment
- improper selection & use of instrument
- computational mistake

#### Systematic error

#### \* Shortcoming of instrument

- Defective

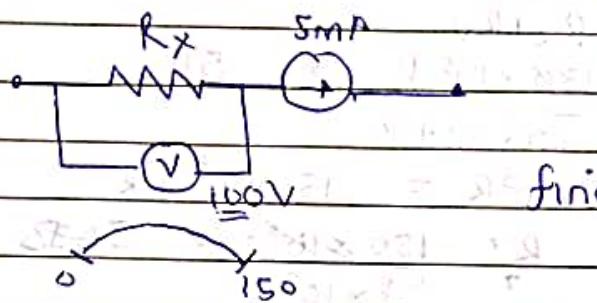
- Wear & tear

- effect of environment

### Random errors

The error whose causes cannot be directly established due to random variable variation of parameters.

e.g.:



- find : i) apparent resistance  
ii) True resistance  
iii) error

$$\text{Sensitivity} = 1000 \Omega/V$$

$$R = \frac{1000 \Omega}{\text{voltmeter}} \times 150 \Omega$$

$$= 150 k\Omega$$

$$\text{Apparent resistance} = \frac{100V}{5mA} = 20 k\Omega$$

$$\text{True resistance} = R_x + R_v = R + \Delta R$$

Method of successive approximations

$$R_T = \frac{R_x + R_v}{R_x + R_v} = \frac{150R}{150 + R} = 20$$

$$15R = 300 + 2R$$

$$13R = 300$$

$$R = 23.0768 k\Omega$$

$$\text{Error} = \frac{3.0768 k\Omega \times 100}{23.0768}$$

$$= 13.23\%$$

Repeat same if  $i = 800 \text{ mA}$   $V = 14.7 \text{ V}$ .

$$R_V = 150 \Omega$$

$$R_{opp} = 50 \Omega$$

$$\textcircled{P} \quad \frac{R_x \cdot R_V}{R_x + R_V} = R_{opp} \cdot R_{opp}$$

$$\therefore R_x^3 = \frac{180 \times 10^3 R}{150 \times 10^3 + R} \rightarrow 180$$

$$3 \times 10^3 R = 150 \times 10^3 + R$$

$$R = \frac{150 \times 10^3}{3 \times 10^3} \rightarrow 50.01 \Omega$$

$$\text{Error} = \frac{0.01}{50.01} \times 100$$

$$\approx 0.0199\% \approx 0.02\%$$

### Systematic Error

#### a) Instrumental Error

- inherent due to mechanical structure
- friction
- irregular spring tension
- excess pulling of spring  $\Rightarrow$  overloading the instrument
- calibration error.

#### b) Environmental Error

- change in temperature
- humidity
- pressure

Causes of error in electrostatic magnetic field

Wavelength between two minima is  $\lambda = \frac{2\pi d}{n}$  where  $d$  is distance between two minima.

c) Random error

→ Take average of multiple readings

x

x

x

x

Random error

Reference :

a) Gross error : class of errors which mainly covers human mistakes in reading or using instruments and recording and computing measurement result.

- Using scale that does not correspond to setting of range control of the voltmeter.

b) Systematic error:

i) Instrumental error: error inherent in measuring instruments because of their mechanical structure  
eg: friction in bearings, improper spring tension, calibration error.

Removing errors by : i) calibrating to proper standard

ii) Applying correction factors

iii) Selecting suitable instrument

ii) Environmental error: errors due to conditions surrounding the instrument

Change in temp., humidity, pressure etc

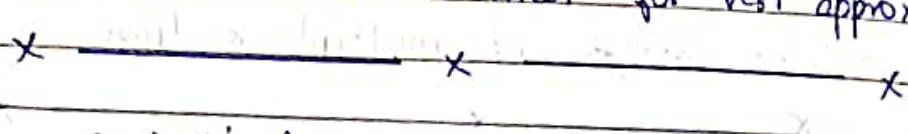
↳ change in  
elastic  
property

iii) Static & Dynamic

↳ caused by limitation  
of measuring instrument

↳ instrument not responding  
fast enough for a change  
in measured variable

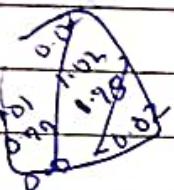
Random error: Error due to unknown cause when all statistical errors are accounted. Removing error is by increasing number of readings & using statistical mean for best approximation.



## Statistical Analysis

### i) Arithmetic Mean

$$\bar{x} = \frac{x_1 + x_2 + \dots + x_n}{n} = \frac{\sum x_i}{N}$$



### ii) Deviation from Mean

$$d_1 = x_1 - \bar{x}$$

$$d_2 = x_2 - \bar{x}$$

error in finding  $d_n = x_n - \bar{x}$  is same as in  $\bar{x}$

so  $\sum d_i = 0$  is same as in  $\bar{x}$

iii) Average deviation: if errors given as

It is an indication of precision of an instrument.

$$D = \frac{|d_1| + |d_2| + |d_3| + \dots + |d_n|}{n}$$

$$D = \frac{\sum |d_i|}{n}$$

N)

Standard Deviation

$$\sigma = \sqrt{\frac{d_1^2 + d_2^2 + \dots + d_n^2}{n}}$$

$$\sigma = \sqrt{\frac{\sum d_i^2}{n}} \quad (\text{if } d_i \text{ is too large}) \quad (\text{in exam})$$

(for  $\infty$  data pts)

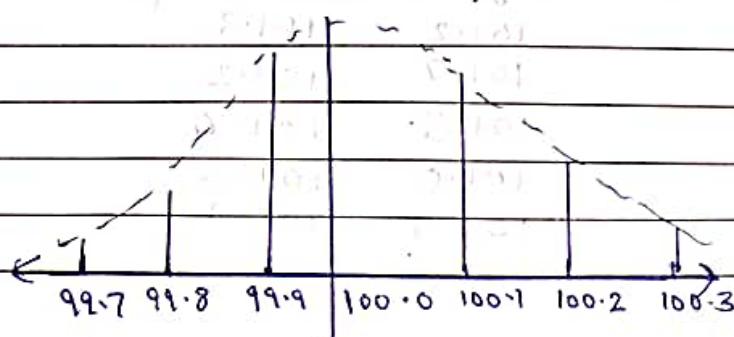
$$\sigma = \sqrt{\frac{\sum d_i^2}{n-1}} \quad (\text{for finite data pts})$$

$$\text{Variance} = \sigma^2$$

Probability of Errors

## (i) Normal Distribution

eg: Voltage Reading	No. of Reading
99.7	1
99.8	4
99.9	12
100.0	19
100.1	10
100.2	3
100.3	1

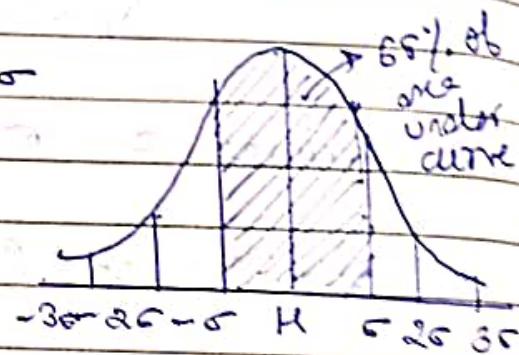


Normal law

- \* All observations include small errors.
- \* Errors can be +ve as well as -ve
- \* Equal probability of +ve & -ve errors
- \* Small errors are more probable.
- \* Large errors are less probable.

**\* Probable error (P.E)**

$$PE = \pm 0.6745 \times \sigma$$

Limiting Error

- \* certain percentage of guaranteed value.

e.g.: Resistor, digital thermometer.

- \* given by manufacturer

H.W.: find avg., deviation & probable error in

101.2      101.3

101.7      101.2

101.3      101.4

101.0      101.3

101.5      101.1

(Q) A 0-150V Voltmeter has a guaranteed accuracy of 1% full-scale reading. The voltage measured by this instrument is 83V. Calculate limiting error in %.

$$\text{Magnitude of limiting error} = 1\% \text{ of } 150V$$

$$= \pm 1.5V$$

limiting or

$$\text{limiting error} = \frac{1.5}{83} \times 100 = 1.8072\%$$

equally

(Q) The voltage in a circuit is dependent on value of 3 resistors  $V_{out} = \frac{R_1 \cdot R_2}{R_3}$ . If tolerance of each resistor is 0.1%. Find max error of generated voltage.

$$100 \times \left( \frac{\Delta V_{out}}{V_{out}} \right) = \left( \frac{\Delta R_1}{R_1} + \frac{\Delta R_2}{R_2} - \frac{\Delta R_3}{R_3} \right) \times 100$$

$$\therefore V_{out} \max \approx 0.1 + 0.1 + 0.1 = 0.3\%$$

$$\therefore V_{out} \min \approx -0.1 - 0.1 - 0.1 = -0.3\%$$

~~M7~~

$$V_{out} = \frac{1.01 R_1 \cdot 1.01 R_2}{0.99 R_3} \approx \frac{1.003 \left( \frac{R_1 R_2}{R_3} \right)}{1} = 3\%$$

Q) Current passing through resistor no ~~100Ω~~ of ~~100±~~  
 is  $2.00 \pm 0.01$  A. Using  $P = I^2 R$  find limit  
 error in power dissipation.

$$\begin{aligned}
 P &= I^2 R \\
 \log P &= 2 \log I + \log R \\
 \frac{\Delta I}{I} &\approx \frac{0.01}{2.00} + \frac{\Delta R}{R} \\
 &\boxed{\left[ \frac{0.02}{2.00} + \frac{0.2}{100} \right]} \\
 &\approx 0.22\% \\
 &\approx \left( \frac{0.01}{2.00} + \frac{0.2}{100} \right) \times 100 \\
 &= (1 + 0.2)\% \\
 [\% P] &= 1.2\%
 \end{aligned}$$

### Functional Elements of an Instruments

#### Application of Measuring System

Instrument

- i) Monitoring of a process or operation
- ii) Monitoring of a process
- iii) Control the process
- iv) Experimental Engineering

#### Elements of a Measuring System

## Primary Sensing Element [PSE]

measured

• measured - quantity to be measured

• measured is first detected by the PSE

• PSE should withdraw minimum energy from the measured.

• PSE may or may not be in direct physical contact with the measured.

ii)

## Variable Conversion Element [VCE]

• converts PSE signal from one form to another while preserving the information content.

Eg: ADC

iii)

## Variable Manipulation Element

• increase / decrease the strength of VCE signal.

• Signal conditioning

iv)

## Data Presentation Elements

• conveys information of measurement

## Transducer

- converts one form of energy to another form.

### i) Active Transducer self generating

- These are externally powered transducers
- Eg - all digital instrument transducers.

### ii) Passive Transducer

- Externally powered

- self generating type transducer
- Eg piezo-electric crystal

## Types of Instruments

### i) Deflection type

- o/p is in the form of deflection
- less accurate
- less sensitivity
- suitable for dynamic measurement
- Eg - spectrometer

### ii) Null type

- It attempts to maintain the deflection at suitable application of an opposite opposing force to the measured value.
- Eg : Weight - Balance

- More accurate
- High sensitivity.
- Not suitable for dynamic measurement.

Problems

1) Scale  $\Rightarrow 0 - 100V$

No of div = 200

Each div reeds =  $0.5V$

~~±~~ div  $0.5$  of div reeds

~~0.25~~  $\Rightarrow 0.25V$

2) No of div = 9999

Full scale Reading  $\Rightarrow 9.999 V$

$\therefore 1$  div reeds =  $9.999 \div 9999 = 0.001 V$

Resolution

3) (a) 3

(b) 2

(c) 4

(d) 5

(e) 1

(f) 1

4)  $R_1 = 28.4 \Omega$   $R_2 = 4.25 \Omega$

$R_3 = 56.605 \Omega$   $R_4 = 0.75 \Omega$

$R_{\text{series}} = 90.0 \Omega$

$$(02) \quad P = V I \cos \theta$$

$$\cos \theta = \cos^{-1} \left( \frac{P}{V I} \right)$$

$$\text{Error in } \theta \approx 0$$

### Youtube

Error = True value - Measured value

$$\Delta I = I_t - I_m$$

↓

Absolute error → remains constant throughout

∴ Relative error =  $\frac{\text{True} - \text{Measured}}{\text{True}} \times 100$

$$E_r = R \cdot E = \frac{\Delta A}{A_t} \rightarrow \text{Absolute error} = E$$

$$E_r \approx \left( \frac{A_m - 1}{A_t} \right)$$

$$A_t = \left( \frac{1}{1 + E_r} \right) A_m$$

CF → correction factor

$$[A_t = CF \times \rho_m]$$

$$(10 \pm 1) \text{ A} \quad (10 \pm 10\%) \text{ A}$$

↓  
(Error)  $\Sigma_A$

↓  
 $E_r$

Relative error decreases as we approach the full-scale reading.

7)

$$V = (200 \pm 2\%) V$$

$$\Omega R = (42 \pm 1.5\%) \Omega$$

$$P = V^2/R$$

$$P = \frac{200 \times 200}{42} = 952.38 \text{ W}$$

$$\frac{\Delta P}{P} \times 100 = 2 \frac{\Delta V}{V} \times 100 + \frac{\Delta R}{R} \times 100$$

$$\frac{\Delta P}{P} = \% E_r = 2 \times 2 + 1.5$$

$$= 5.5\%$$

$$P = (952.38 \pm 5.5\%) \text{ W}$$

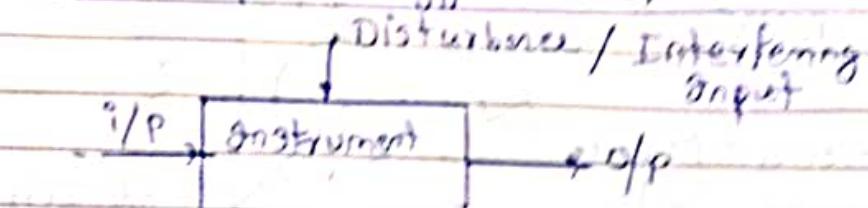
$$R_{eq} = R_1 + R_2$$

$$\Delta R_{eq} = \Delta R_1 + \Delta R_2$$

$$\frac{\Delta R_{eq}}{R_{eq}} = \frac{R_1}{R_{eq}} \frac{\Delta R_1}{R_1} + \frac{R_2}{R_{eq}} \frac{\Delta R_2}{R_2}$$

for multiplication  
for addition/subtraction  
just calculate normally

## Input Output Configuration of an Instrument



### i) Desired I/P

It is the i/p for which instrument is designed to be sensitive.

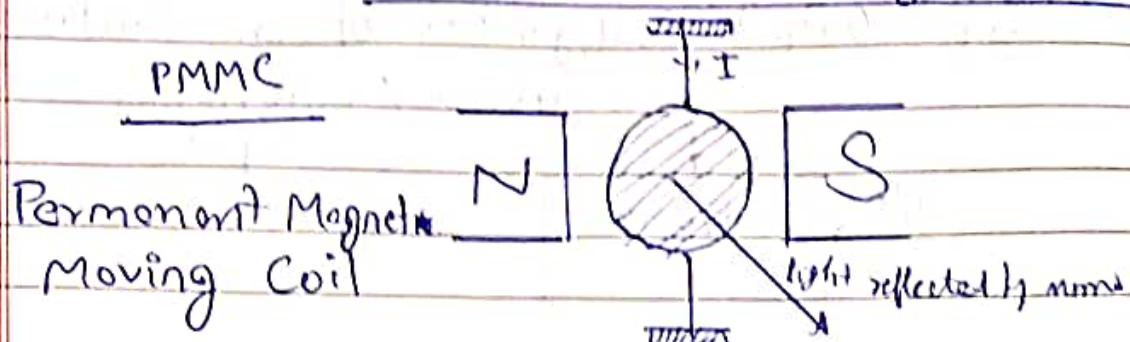
### ii) Interfering I/P

It is the i/p for which instrument is unintentionally sensitive.

### iii) Modifying Inputs

It is the i/p for which changes the input - output relationship of an instrument.

## Electromechanical Electrochemical Indicating Measurement



- coil is fine wire
  - suspended in a magnetic field is produced by permanent magnet
  - coil starts rotating when it comes in contact with earth
  - mirror to the coil
- Features
- Advantages →
- weightless pointer with  $\propto$  lever
  - Not portable
  - Not practical
  - Useful in modern devices

$$J = BAIN$$

where  $T \rightarrow$  Torque ( $Nm$ )

$B \rightarrow$  flux of air gap ( $W/m^2$  or tesla)

$A \rightarrow$  Area in  $m^2$

### Practical value

$$A \approx 0.5 \text{ cm}^2 \text{ to } 2.5 \text{ cm}^2$$

$B = 1500 \text{ gauss to } 5000 \text{ gauss or } 0.15 \text{ tesla}$   
 $\text{to } 0.5 \text{ tesla.}$

$$N = 100$$

$$I \approx 1 \text{ mA}$$

$$J \approx 3 \times 10^{-6} \text{ Nm} = T$$

(Q) What will happen if we apply AC to PMMC

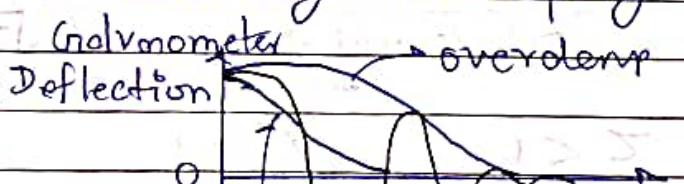
→ Fine vibrations occur instead of deflection

Won't be able to measure current.

(Q) What will happen if DC is suddenly removed?

### Dynamic Behaviour (DB)

- Dynamic Behaviour can be observed by suddenly interrupting the applied current.



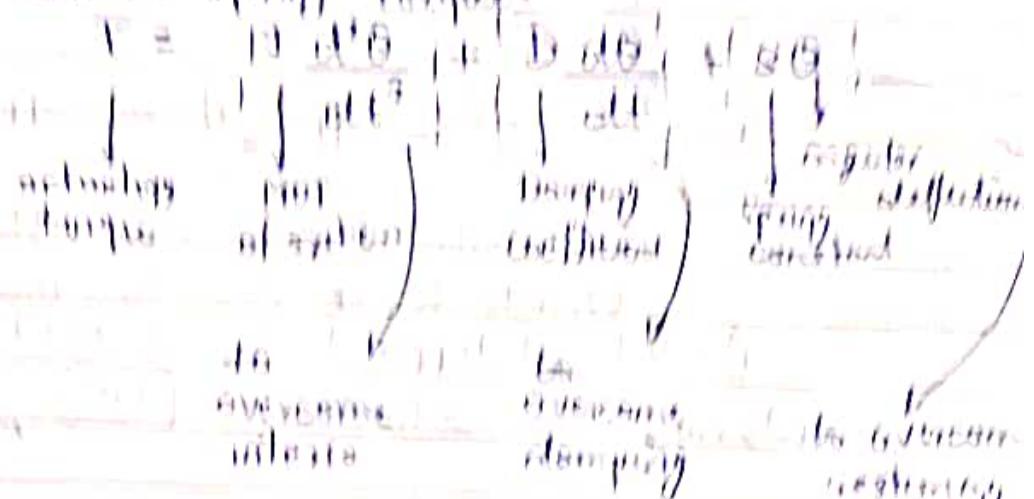
critically damped

HW: Read CDRX

Resonance

- If there are no forces acting on the system other than the restoring force of the spring, the system will oscillate with constant amplitude.

- Damped system: forces pushes the system to oscillate to a steady-state position where it is balanced by the opposing resultant spring forcing.



$$\text{Damping ratio } \zeta = \frac{\text{Damping ratio}}{\text{Natural frequency}} = \frac{\zeta}{\sqrt{k/m}}$$

$\zeta > 1$	$\zeta = 1$	$\zeta < 1$
over-damped	critically damped	under-damped

(Instability)

Undamped natural frequency → Frequency of oscillation of system when damping is zero.

$$f_n = \frac{1}{2\pi} \sqrt{\frac{k}{m}}$$

→ Instrument, in practice, is slightly underdamped, causing pointer to overshoot a little. Decreases response time but prevents damage to instrument.

→  $\frac{CDR_X}{ERDX}$  (Critical Damping Resistance External)

constant in galvanometer which determines the value of external resistance that produce critical damping. To determine CDR<sub>X</sub> observe galvanometer swing when current is applied / removed in galvanometer. Decreasing value of external resistance one at a time until a value is found for which overshoot just disappears i.e. CDR<sub>X</sub>

Youtube - 5.01.20

$$1) \text{ T.V} = 80V$$

$$M.V = 79V$$

$$\text{Abs. error} = 1V$$

$$2) \text{ error} = \frac{150 \times 1}{100} = 1.5V$$

$$\% \text{ limiting error} = \frac{1.5}{25.5} \times 100 = 2\%$$

$$3) \text{ error} = \frac{2}{100} \times 200 = 4V$$

$$\% \text{ error} = \frac{4}{100} \times 100 = 4\%$$

$$4) \text{ error} = \frac{2}{100} \times 300 = 6V$$

$$\text{Range} = 24 - 36V$$

$$\text{d) error} \approx \text{voltage} + 110.2$$

~~Let it be~~

$$\text{Range}_{\text{max}} = 0.1103 - 0.1102$$

$$d_1 \approx 0.110$$

$$d_2 \approx 0.110$$

$$d_3 \approx 0.110$$

$$d_4 \approx 0.110$$

$$d_5 \approx 0.110$$

~~1.4 digit~~ Range  $\rightarrow 110.3 - 110.2 = 0.1$

$$\text{Range} = 110.3 - 110.2 = 0.1$$

$$\text{d) } 110.2 - 110.1 = 0.1$$

$$\text{Range} = \frac{0.1 + 0.1}{2} = 0.1$$

$$\text{Range of error} = \frac{(I_{\text{max}} - I_{\text{avg}}) + (E_{\text{avg}} - E_{\text{min}})}{2}$$

$$\text{e) } R_1 + R_2 + R_3 \approx 0 \quad R_S = \sum R$$

$$R_S = 100 \Omega$$

$$R_1 + R_2 + R_3 = R$$

$$\frac{\partial R_1}{R_1} \cdot R_1 + \frac{\partial R_2}{R_2} \cdot R_2 + \frac{\partial R_3}{R_3} \cdot R_3 = \frac{\partial R}{R}$$

$$2 \times 10 + 3 \times 20 + 70 \times 5 = 100$$

$$\% R = \frac{20 + 60 + 350}{100} = 4.3\%$$

apparatus  
(all about  
electromagnetic)

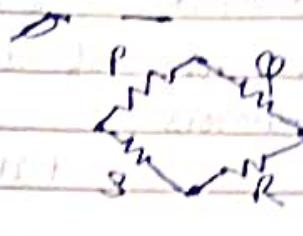
$$P = 10 \pm 2\%$$

$$\theta = 20 \pm 3^\circ$$

$$S = 70 \pm 5\%$$

$$P \cdot R \rightarrow Q \cdot S$$

$$R = \frac{Q \cdot S}{P}$$



$$\text{Error in } R = \frac{20 \times 70}{10} = 140 \text{ %}$$

dR

$$\log R = \log P + \log S - \log \theta$$

$$\frac{dR}{R} \times 100 = \frac{dP}{P} + \frac{dS}{S} + \frac{d\theta}{\theta}$$

$$\begin{aligned} & 2 + 3 + 5 \\ & = 10\% \end{aligned}$$

### \* Significant errors

Rules:

① All non-zero digits are significant

② Zero preceding first non-zero digit are not significant

eg: 0.00125  $\rightarrow$  3

③ zeros b/w 2 non-zero digits are significant

eg: 5.012  $\rightarrow$  4

④ zeros at end or right are significant provided they are on same side of decimal point

100.00  $\rightarrow$  5

4.000  $\rightarrow$  4

⑤ Exact numbers have no significant figures

Eg/  $1.213 + 3.43 + 2.3$

Addition/Subtraction : Result cannot have more digits to the right of decimal pt. than either of original numbers.

$$1.213 + 3.43 + 2.3$$

$$\approx 6.943 \rightarrow 6.9$$

Multiplication/Division : The result must be reported with no more significant figures as there are in measurement with the few significant figures.

$$1.4 \times 2.35 = 3.276$$

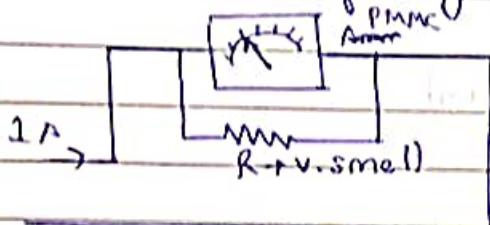
$$6.213 \div 3.43 = 1.8113 \approx 1.81$$

## DC Ammeter

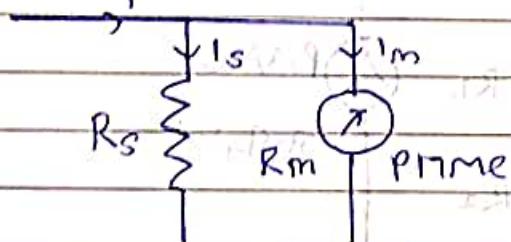
\* PMMC or d'Arsonval's Movement or Galvanometer

\* PMMC can handle very small current.

\* Reduce current flowing through PMMC.



OR



[which device has how much length used for resistance?]

(Q) A 1 mA movement with an internal resistance of  $100\Omega$  is to be converted to an ammeter of 0-100 mA. Calculate shunt resistance.

$$1 \times 100 = 99 R_s$$

$$100 = 99 R_s \\ R_s = 100/99 \\ \approx 1.01\Omega$$

$$0.01 \times 100(100 + 0.01) = (0.01 \times 100) \text{ ohms}$$

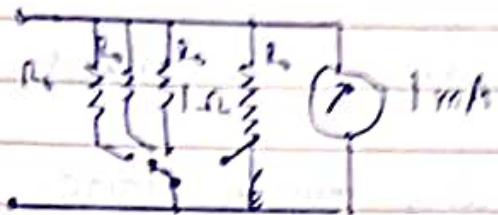
~~$$0.01 \times 100 + 0.01 \times 100 = 0.01 \times 100 + 0.01 \text{ ohms}$$~~

$R_s =$

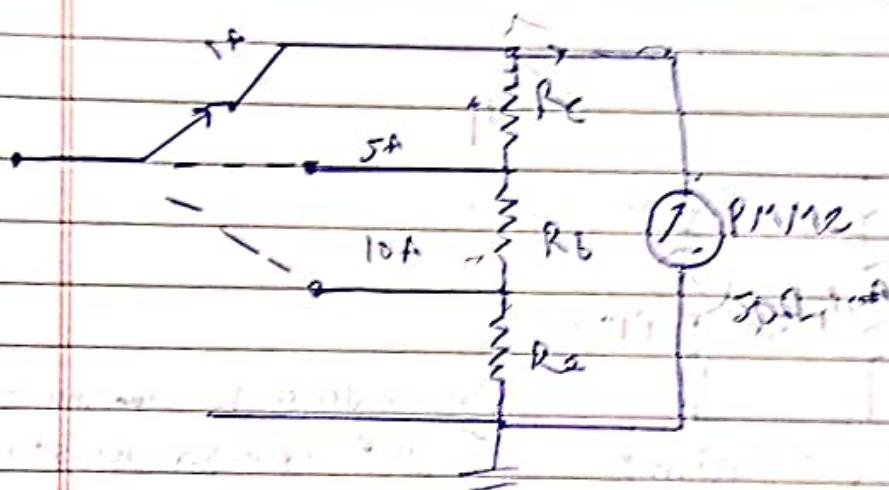
$$100 \times (100 + 0.01) = 101 \text{ ohms}$$

$$100 + 0.01 = 100.01 \text{ ohms}$$

## Multirange Ammeters



## Ayerton Shunt / Universal Shunt



Design an Ayerton Shunt to provide an ammeter with current range of 1A, 5A, 10A & Prime with an internal resistance of 50 Ω & FSD of 1mA to be used.

$$0.999 \cancel{R_s} (R_1 + R_2 + R_3) = (0.001) 50$$

$$\cancel{R_s} (R_1 + R_2 + R_3) = 50 \quad \text{--- (1)}$$

$$4.999 (R_1 + R_2) = (50 + R_3) 0.001 \quad 32$$

$$4999 R_1 + 0.4999 R_2 - 50 R_3 = 50 \quad \text{--- (2)}$$

$$9.999 R_2 = (50 + (R_3 + R_1)) \cancel{50} \quad 50$$

$$9999 R_2 = 0.001 R_1 - \cancel{50 + R_3} \quad \frac{50}{9999}$$

$$R_C = R_{B2} = 0.05 \Omega$$

$$R_B = R_B^2 = 10^5 \Omega$$

$$R_O = R_B^2 = 10^5 \Omega$$

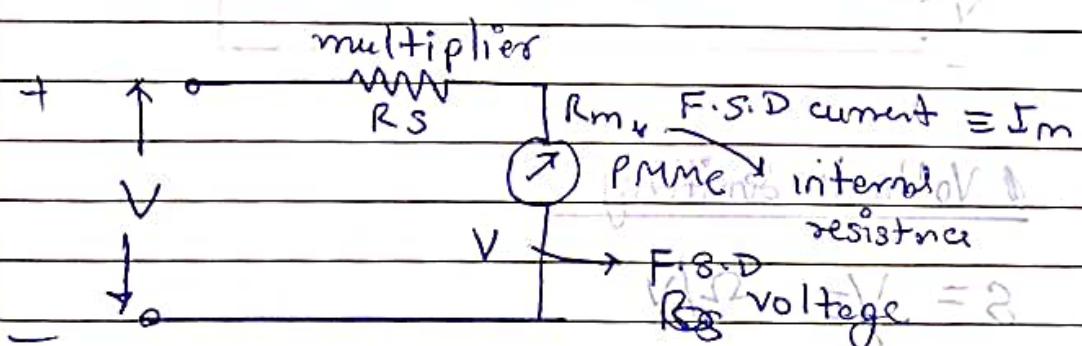
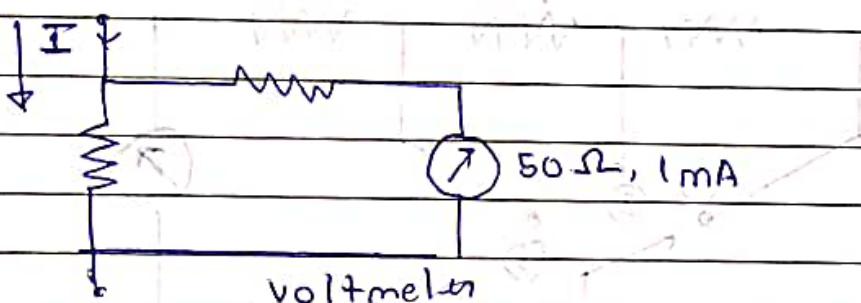
$$R_O = 5 \text{ m}\Omega$$

$$R_B = 5 \text{ m}\Omega$$

$$R_C = 0.05 \Omega$$

$$\approx 40 \text{ m}\Omega$$

### DC Voltmeters



$$V = I_m (R_S + R_m)$$

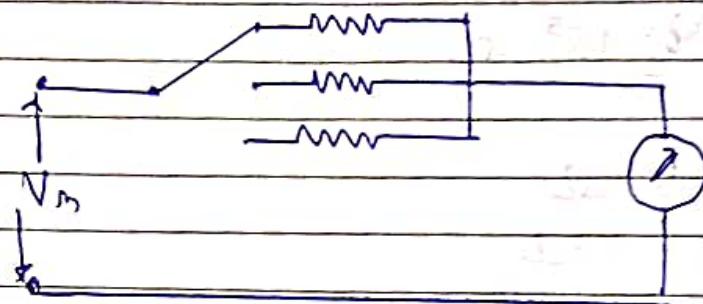
$$\left\{ \begin{array}{l} R_S = \frac{V}{I_m} - R_m \\ I_m = \text{full scale current} \end{array} \right.$$

$$V \times 2 = ?$$

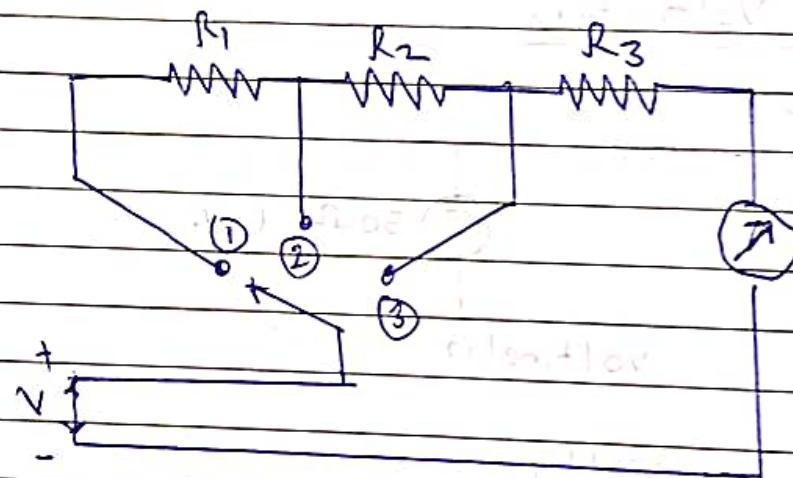
$$= 2V - R_o = R_o = R_F$$

## Multimeter

### \* Multirange Voltmeter



### \* Another Arrangement



### • Voltmeter Sensitivity

$$S = 1/I \quad \Omega/V$$

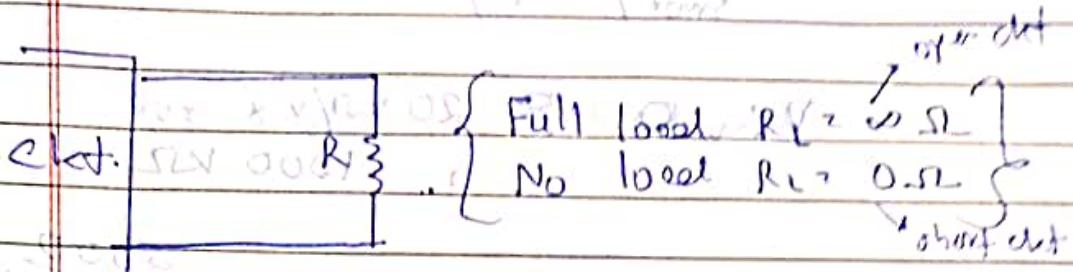
for Fig 1,

Total resistance  $\approx R_7$

$$R_T = S \times V$$

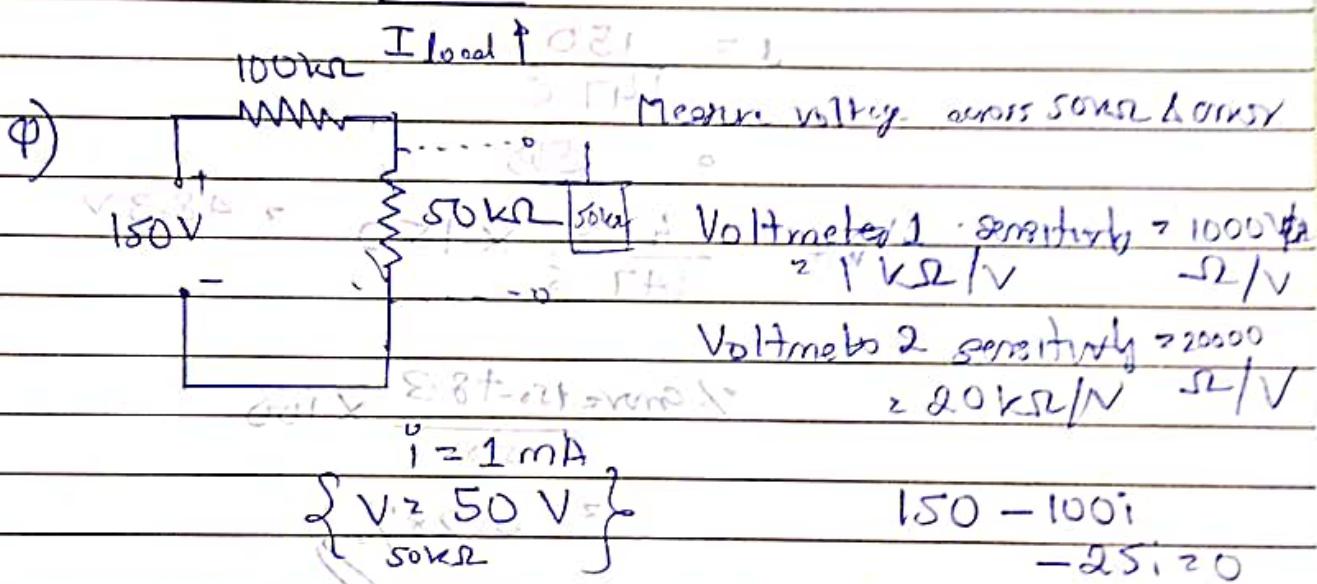
$$R_0 = R_T - R_{\text{amm}} = SV - R_{\text{amm}}$$

## Loading effect



Loading effect is caused by low sensitivity devices.

$$S_o = S_0 \cdot \frac{R_o}{R_o + R_L}$$



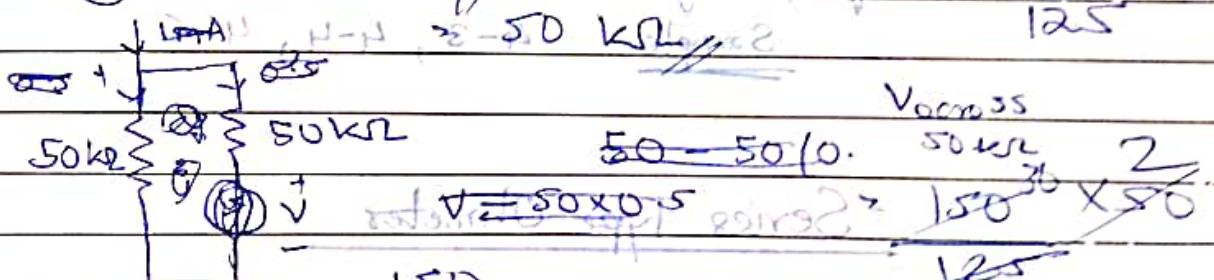
$$\textcircled{1} \quad i = 1 \text{ mA}$$

$$\left\{ \begin{array}{l} V_o = 50 \text{ V} \\ 50k\Omega \end{array} \right.$$

$$150 - 100i = 150 - 100 \cdot 0.001 = 150 - 0.1 = 149.9 \text{ V}$$

$$-25i = 0$$

$$i = \frac{150}{125} = \frac{150}{125} \text{ A}$$



$$V_{cross} = \frac{50 \times 100}{125 \times 2} \times 50 = \frac{5000}{250} \times 50 = 200 \times 50 = 10000 \text{ V}$$

$$= 1/5 \times 150 = 30 \text{ V}$$

$$= 30 \text{ V}$$

$$150 - 100i = 150 - 100 \cdot 0.001 = 150 - 0.1 = 149.9 \text{ V}$$

$$\frac{150 - 100i}{125 \times 2} = \frac{150 - 100 \cdot 0.001}{250} = \frac{150 - 0.1}{250} = \frac{149.9}{250} = 0.5996 \text{ V}$$

$$= 30 \text{ V}$$

Pratik  
Date

Smart 240V.

VR<sub>vol</sub> 2150 20 Vn/V + 30/

total 1000 VnL

5000  
105

$$\text{Req } \frac{50}{105} \times 100\% = \frac{5000}{105} \times 100\% = 47.6 \text{ kA}$$

$$i = \frac{150}{147.6}$$

• 150

$$150 = \frac{150}{147.6} \times 150 \rightarrow 48.3 \text{ V}$$

Series & shunt & shunt

$$\% \text{ error} = \frac{150 - 48.3}{150} \times 100$$

001 - 021

$$\frac{2}{2} \times 3.28\%$$

051 -

071 -

\* Assignment

Sample 4-3, 4-4, 4-6

200mV

0103 - 03

20f 1.2m

0101 - 021

20f 1.2m

0103 - 03

20f 1.2m

0101 - 021

Series Type Ohmeters

0101 - 021

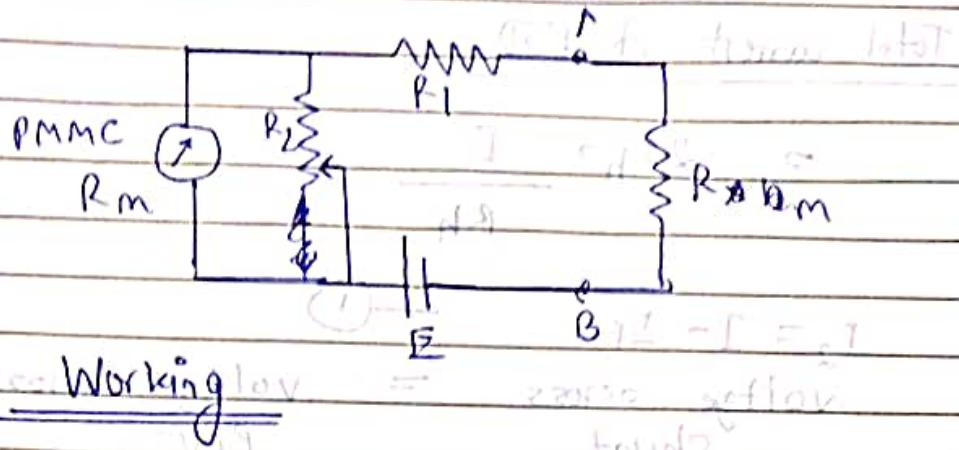
02 021 021 - 200mV

5x 021

040 - 040

V08

V08



- Short ckt AB
- Adjust  $R_2$  until FSD
- mark the PMMC position as  $0\Omega$ .
- Open ckt A-B
- PMMC indicated zero.
- Mark this position as  $\infty \Omega$ .
- Use known resistors to make intermediate markings.

Drawbacks

- Calibration
- internal battery slowly discharges

### Half Scale Deflection

$R_h$ : Half Scale Deflection

$$R_h = \left( R_1 + \frac{R_2 \cdot R_m}{R_2 + R_m} \right)$$

$$\frac{(R_m + R_2) + R_1}{R_m + R_2} = R_h$$

$$I_{A_h} = \frac{E}{2R_h}$$

Total current at FSD

$$= 2I_h^2 \frac{E}{R_h}$$

$$I_2 = I - I_{FSD} \quad \textcircled{1}$$

voltage across shunt = voltage across PMMC

$$I_2 R_2 = I_{FSD} R_m$$

$$\therefore R_2 = \frac{I_{FSD} R_m}{I_2} \quad \textcircled{2}$$

$$\therefore R_2 = \frac{I_{FSD} R_m}{I_T - I_{FSD}}$$

$$= \frac{I_{FSD} R_m}{I_{FSD} R_m + R_h} \frac{E}{I_T} \quad \textcircled{3}$$

$$R_2 = \frac{(I_{FSD} R_m) R_h}{E - I_{FSD} R_h}$$

we know  $R_h = R_2 + R_m$

$$R_h = R_h - R_2 R_m$$

$$\therefore R_h = R_2 + R_m$$

$$\frac{R_2 R_m}{R_2 + R_m} = R_h - R_2$$

$$\frac{R_m}{1 + \frac{R_m}{R_2}} = R_h - R_2$$

$$\frac{1}{1 + \frac{R_m}{R_2}} = \frac{R_h - R_2}{R_m}$$

$$1 + \frac{R_m}{R_2} = \frac{R_m}{R_h - R_i}$$

$$\frac{R_m}{R_2} = \frac{(R_m - 1)}{(R_h - R_i) \times 0.002} = 0.81 \quad (F=8)$$

$$\left\{ \begin{array}{l} R_2 = \frac{R_m}{R_m - 1} \\ \frac{R_m}{R_h - R_i} \end{array} \right\}$$

$$\frac{\frac{R_m}{R_m - 1}}{R_h - R_i} = \frac{IFSD R_m R_h}{E - IFSD R_h}$$

$$R_h - R_i$$

$$\textcircled{1} \rightarrow 0.81 = 0.24$$

$$\frac{R_m}{R_m - 1} = \frac{E - IFSD R_h}{IFSD R_h}$$

$$\textcircled{2} \quad \frac{R_h - R_i}{R_h - R_i} = \frac{IFSD R_h \times 0.002}{E - IFSD R_h}$$

$$\frac{R_h - R_i}{R_h - R_i} = \frac{IFSD R_h}{E - IFSD R_h + IFSD R_i}$$

$$R_h - R_i = \frac{IFSD R_h}{E - IFSD R_h + IFSD R_i}$$

$$R_h - R_i = \frac{R_m IFSD R_h}{E - IFSD R_h + IFSD R_i}$$

$$\textcircled{2} \rightarrow 0.24 = 0.002$$

$$R_i = R_h - \frac{R_m IFSD R_h}{E - IFSD R_h + IFSD R_i}$$

$$\left\{ R_i = R_h \left( 1 - \frac{R_m IFSD}{E - IFSD R_i} \right) \right\}$$

$$0.24 + 0.3582 = (1 - \frac{0.24}{0.24 + 0.3582}) \times 0.002$$

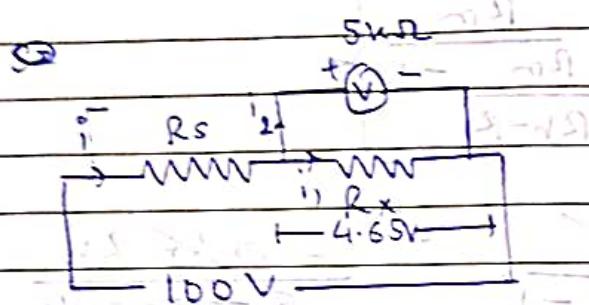
Assignment Example 4-7

$$0.24 + 0.3582 = 0.24 + 0.002$$

Assignment question

$$4-7) R_V = \frac{100 \Omega \times 50 V}{Y}$$

$$\therefore 5000 \Omega = 5 k\Omega$$



$$4.65 = i R_x \quad \text{--- (1)}$$

$$\therefore \left( \frac{5000 R_x + R_s}{5000 + R_x} \right) i = 100 \quad \text{--- (2)}$$

$$i_s = i_1 + i_2 \quad \text{--- (3)}$$

$$R_s \cdot i = 95.35 V \quad \text{--- (4)}$$

$$5000 i_2 = 4.65 \quad \text{--- (5)}$$

$$i_2 = 9.3 \times 10^{-4} A$$

~~$$\left( \frac{5000 R_x}{5000 + R_x} \right) i = -4.65$$~~

~~$$\left( \frac{5000 R_x}{5000 + R_x} \right) (i_1 + 9.3 \times 10^{-4}) = 23250 + 4.65$$~~

~~$$5000 R_x i_1 + 4.65 R_x = 23250 + 4.65$$~~

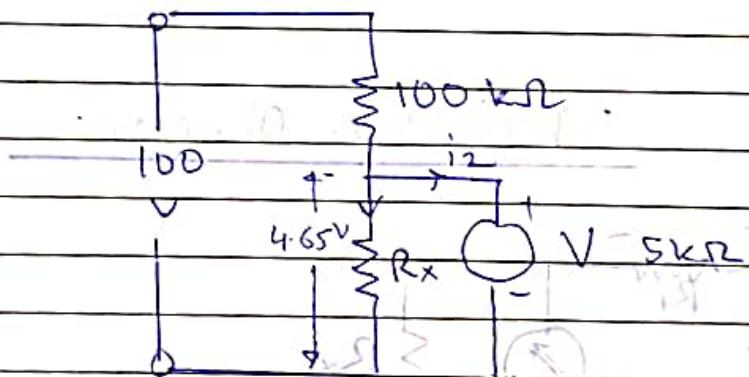
4-7)

 ~~$R_i = 100 \text{ k}\Omega$~~  ~~$V = 5 \text{ k}\Omega, 4.65 \text{ V}$~~ 

$$i = 0.9535 \text{ A}$$

$$\frac{4767.5 R_x}{5000 + R_x} \approx 4.65$$

$$4762.85 R_x \approx 23250 \Rightarrow$$



~~$i = 0.9535 \text{ mA}$~~

$$i_2 = 0.93 \text{ mA}$$

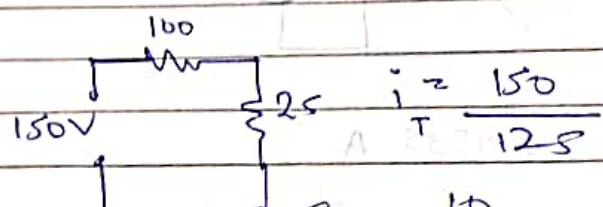
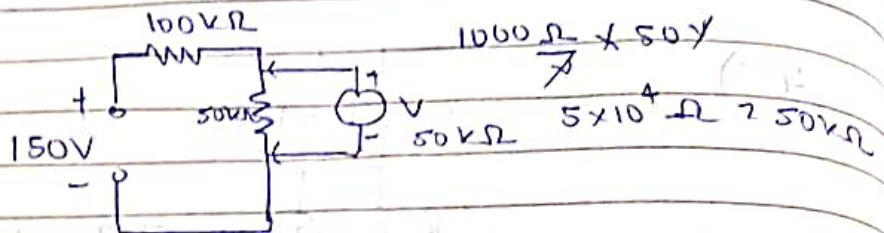
$$i_1 = 0.0265 \text{ mA}$$

$$\{ R_x = 180 \text{ k}\Omega \}$$

Ansatz falsch

0 → 3mA

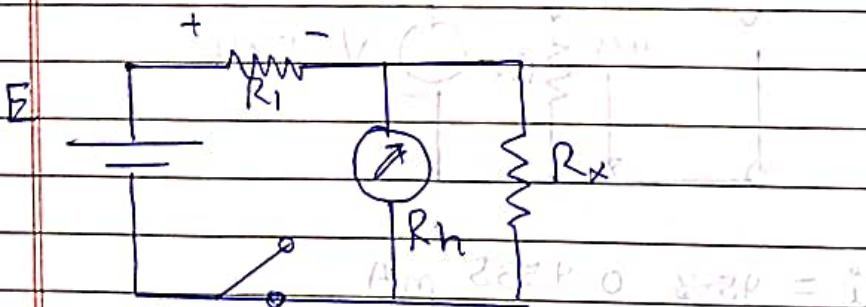
4-6)



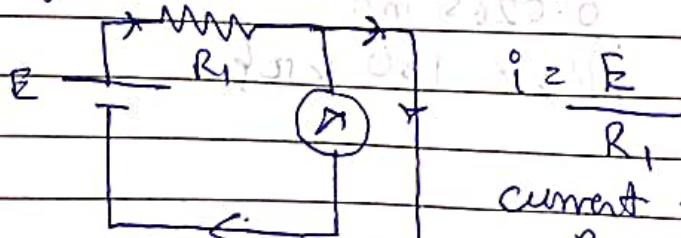
$$V = \frac{78}{50k} \times 50 = 30V$$

4-4) (b)

### Shunt Type Ohmeter



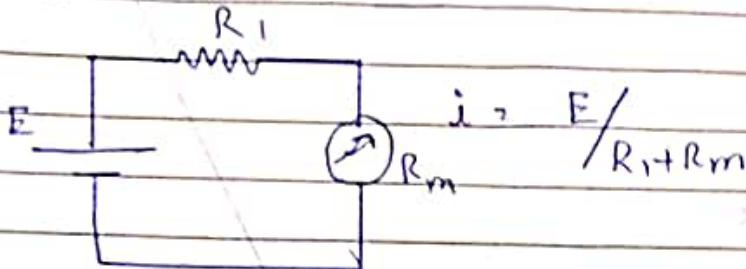
$$i) R_s = 0.5\Omega$$



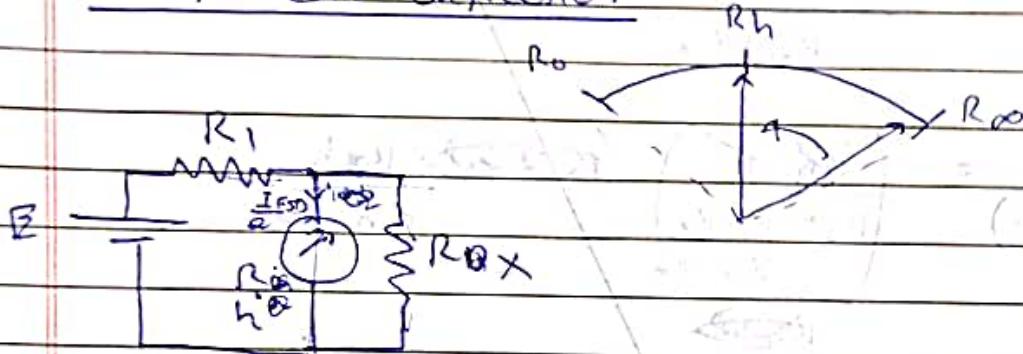
current through  
P.M.M.e = 0

ii)

$$R_x = \infty$$



$$I = I_{FSD}$$

Half Scale deflection

$$i = \frac{E}{R_1 + R_h + R_{sh}}$$

$$i_{FSD} = \frac{E}{R_1 + R_h + R_m}$$

$$\frac{i_{FSD}}{2} = \frac{E}{R_1 + \frac{R_h \cdot R_m}{R_h + R_m}} = \left( \frac{E}{R_1 + R_m} \right) \frac{1}{2}$$

~~$$2 \cdot \frac{E}{R_1 + R_m} = R_1 + \frac{R_h \cdot R_m}{R_h + R_m}$$~~

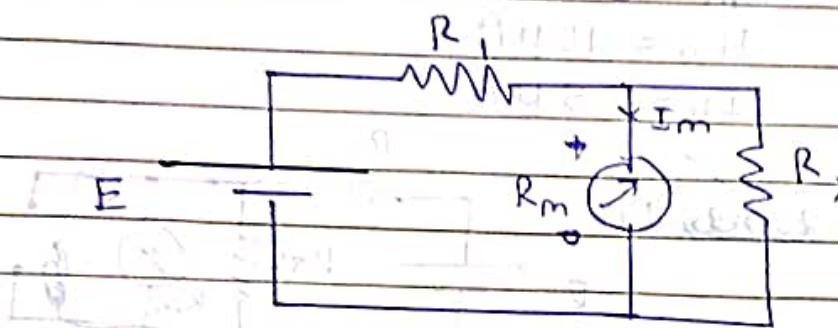
~~$$R_1 = \frac{R_h \cdot R_m}{R_h + R_m} - 2R_m$$~~

~~$$R_1 = \frac{R_m (R_h - 2)}{R_h + R_m}$$~~

$$2R_1R_m + R_1R_x + R_1 + R_mR_x + R_mR_x = 2R_1 + 2R_m$$

$$2R_1R_m + 2R_1R_x + R_1 + R_mR_x = 2R_1 + 2R_m$$

$$R_x = \frac{R_1 + 2R_m - 2R_1R_m}{2R_1 + R_m}$$



$$\text{EOD} \quad i_T = E$$

$$R_1 + \frac{R_mR_x}{R_m + R_x}$$

$$\text{fixed} \quad I_m = \left( \frac{R_x}{R_x + R_m} \right) \left( \frac{E}{R_1 + \frac{R_mR_x}{R_m + R_x}} \right)$$

Cell or DMM 20mV + 10V

$$S = \frac{I_m V_{mm} \times 20}{I_{FSD}} \frac{R_x(R_1 + R_m)}{R_m + (R_1 + R_x) + R_1R_x}$$

$$R_p = \frac{R_1R_m}{R_1 + R_m} \quad \therefore S = \frac{R_p}{R_x + R_p}$$

$$\text{for HSD, } R_m = R_x \quad I_m = \frac{I_{FSD}}{2}$$

$$0.5 I_{FSD} = \frac{ER_x}{R_1R_m + R_1R_x + R_mR_x}$$

$$\therefore R_{\cancel{\text{HSD}}} \quad \left\{ R_h = \frac{R_1R_m}{R_1 + R_m} \right\}$$

## Multimeter

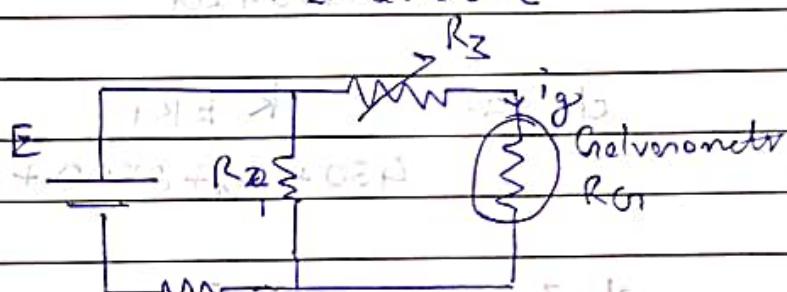
- multimeter range ohmmeter (low internal R)
- multirange voltmeter (high internal R)
- multirange ohmmeter (high internal R)

~~multimeter range ammeter (high internal R)~~

Eg 4.1

$$E = 1.5V$$

$$R_2 = 2500\Omega$$



$$\textcircled{X} \quad R'_3 = 450\Omega$$

$$\textcircled{X} \quad d_1 = 150 \text{ mm}$$

$$\textcircled{X} \quad R''_3 = 24950\Omega$$

$$\textcircled{X} \quad d_2 = 75 \text{ mm}$$

$$\textcircled{X} \quad E = i_T \times \left[ \frac{R_1(R_3 + R_G)}{R_3 + R_G + R_1} + R_2 \right]$$

$$\textcircled{X} \quad R_3 + R_G = R_S$$

$$\textcircled{X} \quad i_T = \frac{E}{R_S + R_2}$$

$$\frac{R_1 R_S + R_2}{R_S + R_1}$$

$$\textcircled{X} \quad i_g \neq \frac{E}{\left( \frac{R_1 R_S}{R_1 + R_S} + R_2 \right) \left( \frac{R_1}{R_1 + R_S} \right)} \quad i_g \propto d$$

$$\frac{d_1}{d_2} = \frac{\frac{ERI}{R_1 + (R_3' R_0 + R_{01}) + R_2}}{\frac{(R_1 + R_3'' R_{01})}{(R_1 + R_3' + R_{01})}}$$

$$\left( \frac{ERI}{R_1 + (R_3'' + R_{01}) + R_2} \right) \times \frac{1}{(R_1 + R_3'' + R_{01})}$$

$$d_1 = \frac{\frac{ERI}{(450 + R_{01}) + 2500}}{1 + 450 + R_{01}} \times \frac{1}{1 + 450 + R_{01}}$$

$$d_1 = \frac{K E R I}{450 + R_{01} + 2500 + 1125000 + 2500 R_{01}}$$

$$d_2 = \frac{\frac{K E R I}{950 + R_{01} + 2500}}{1 + 950 + R_{01}} \times \frac{1}{1 + 950 + R_{01}}$$

$$d_2 = \frac{K E R I}{950 + R_{01} + 2500 + 2375000 + 2500 R_{01}}$$

$$2 = \frac{d_1}{d_2} = \frac{950 + R_{01}}{950 + R_{01} + 2500} = \frac{240450 + R_{01} 2500}{481127950 + 2500 R_{01}}$$

$$2500 R_{01} = 122550$$

$$\{ R_{01} = 49.5 \}$$

1. 30. 04. (18) (3) F  
 2014 (2014) 2014 (2014)  
 2014 (2014) 2014 (2014)

$$S = \frac{i_g}{d}$$

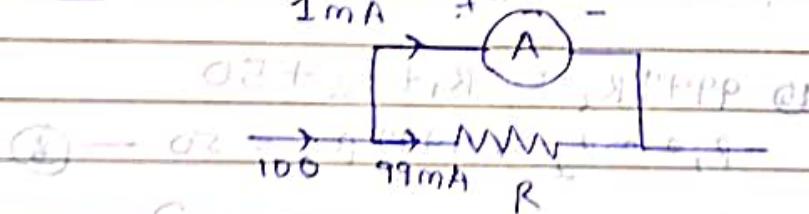
$$i_g = \left( \frac{E}{R_1 + R_S} \right) \frac{R_1}{R_1 + R_S}$$

$$i_g = \frac{3 \text{ mA}}{150 \text{ mm}} = 0.02 \text{ mA} \times 2 \times 10^3 = 1.2 \mu\text{A}$$

~~$$S = 0.21.2 \mu\text{A} = 0.21.2 \text{ d}/\mu\text{A}$$~~

~~$$D = 75 + 50 \text{ mm} = 125 \text{ mm}/\mu\text{A}$$~~

~~$$T_{4.2} = 50 \text{ } \mu\text{s} \Rightarrow R_g = 100 \Omega$$~~



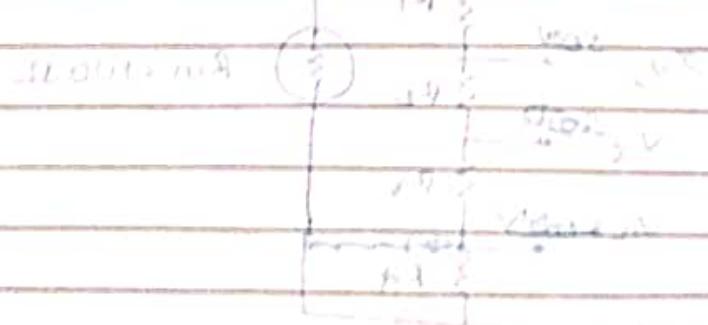
$$V_o = 100 \times \left( \frac{R_g}{R_g + R} \right) = 99$$

$$100 = 100 \times \frac{100}{100+R} = 0.99$$

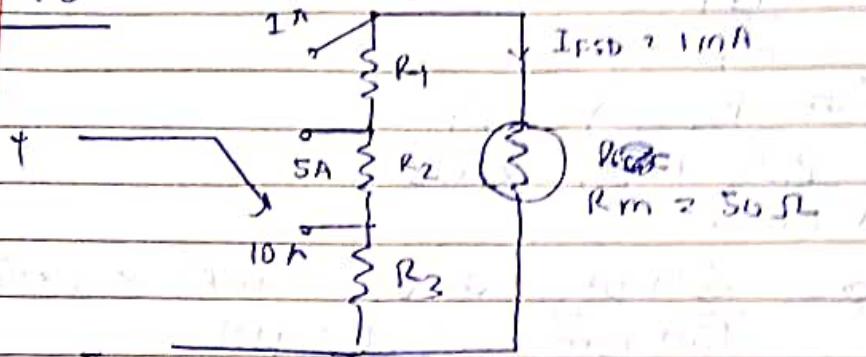
$$100 = 0.99 + 0.99R$$

$$100 = 0.99 + 0.99R$$

$$1.01 \Omega$$



4.3



$$999(R_1 + R_2 + R_3) = 150$$

$$R_1 + R_2 + R_3 = 0.05 \quad \text{--- (1)}$$

$$4999(R_2 + R_3) = R_1 + 50$$

$$-R_1 + 4999R_2 + 4999R_3 = 50 \quad \text{--- (2)}$$

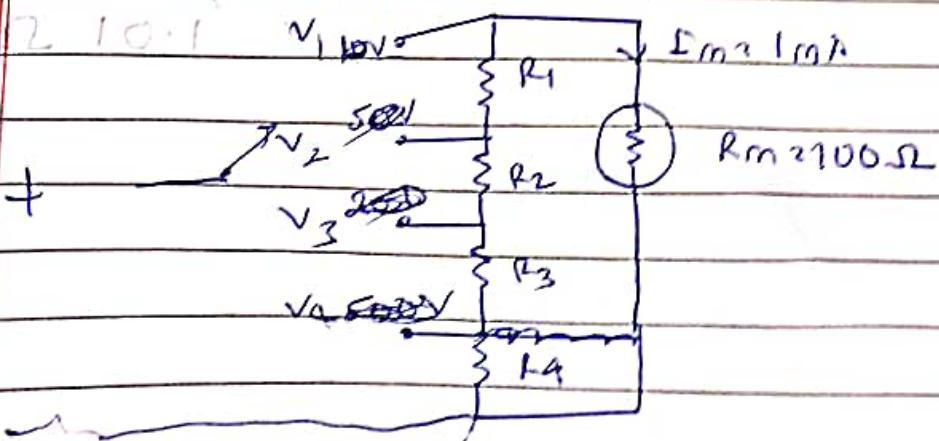
$$9999R_3 = R_1 + R_2 + 50$$

$$-R_1 - R_2 + 9999R_3 = 50 \quad \text{--- (3)}$$

$$\begin{aligned} PP &= \left\{ \begin{array}{l} R_1 = 0.039\text{ }\Omega \\ R_2 = 5.005 \times 10^3\text{ }\Omega \\ R_3 = 5.005 \times 10^3\text{ }\Omega \end{array} \right\} \\ PP.C &= \left\{ \begin{array}{l} R_1 = 0.039\text{ }\Omega \\ R_2 = 5.005 \times 10^3\text{ }\Omega \\ R_3 = 5.005 \times 10^3\text{ }\Omega \end{array} \right\} \end{aligned}$$

4.4 + PP.U = 0.1

$$PP.U = R_m = 100\text{ }\Omega$$



$$R_{q1} = \frac{V_1}{I_1}$$

$$= \frac{10}{1mA}$$

$$R_{q2} = 10000 \Omega$$

$$R_A = 10000 - 100$$

$$= 9900 \Omega$$

$$R_{q3} = \frac{50}{1mA} \rightarrow 50000 \Omega$$

$$50000 = 9900 + 100 + R + 50000$$

$$50000 = 9900 + 100 + R + 50000$$

$$R = 40 k\Omega$$

$$R_T = S \times V$$

$$\left\{ R_s = R_s \times V \right. \quad \left. R_m \right\}$$

$\downarrow$   
resistor  
of multiplier

$$\left\{ S = \frac{1}{I_{fsol}} - \frac{\Omega}{V} \right\}$$

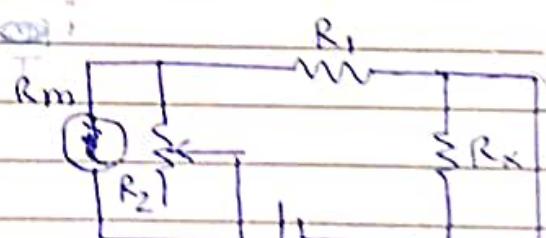
4-8

$$R_m = 50 \Omega$$

$$i_{fsol} \rightarrow 1mA$$

$$E = 3V$$

$$A_{m2+1} R_h = 2000 \Omega$$



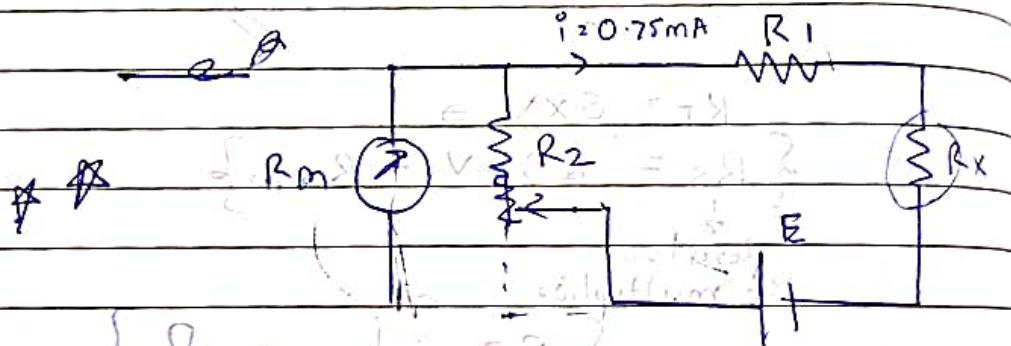
$$\left( \frac{R_2}{R_m + R_2} \right) \frac{E}{R_2 R_m + R_1} = A_{m2+1} i_{fsol}$$

$$\left( \frac{R_2}{R_m + R_2} \right) \frac{E}{R_2 R_m + R_1 R_h} = i_{fsol}$$

$$\frac{3R_2}{(50+R_2)} \left( \frac{3}{50R_2 + R_1} \right) = 1$$

$$I = \frac{3R_2}{(50+R_2)(50R_2 + 80R_1 + R_1 + R_2)}$$

$$2500R_2 + 2500R_1 + 50R_1R_2 = 0 + 50R_2^2 \\ + 50R_1 + R_1R_2 \approx 3R_2 \cdot 0000$$



$I = V$  for full scale deflection

$$R_2 = 0$$

$R_X = \text{Total Resistor effect in k}\Omega$

$$i_{fsel} = \frac{E}{2R_h}$$

$$2000 = 1.5 \text{ mA}$$

$$i_{fsel} = 1 \text{ mA}$$

$$i_{R_2} = 0.5 \text{ mA}$$

$$i_{fsel} R_m = i_{R_2} R_2$$

$$R_2 = \frac{1 \times 5000}{0.5} = 100 \text{ }\Omega$$

if:

$$i_{hsat} = 0.5 \text{ mA}$$

~~$$0.5 \times 50 = 8 \times 100 \times i_2$$~~

~~$$i_2 = 0.25 \text{ mA}$$~~

~~$$2.5 + 0.75 R_1 + 2000 \times 0.75 = 3$$~~

~~$$\text{Loop 3} \quad R_p = \frac{R_m R_2}{R_m + R_2} = 33.3 \Omega$$~~

~~$$R_1 = R_h - R_p$$~~

~~$$= 1966.7 \Omega$$~~

### \* IMP points

#### Series Type Ohmmeter

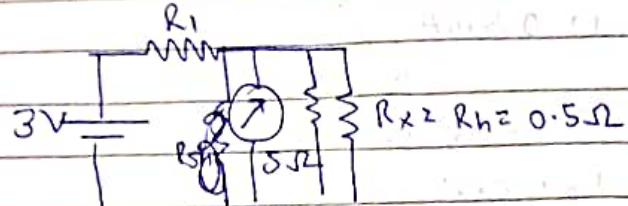
→ for full scale deflection, put  $R_2 = 0$ . The current through battery  $\neq$  current through galvanometer.

→ Use  $i_T = \frac{E_{battery}}{(R_x + R_p)}$

$E_{battery}$  is constant  $\Rightarrow$  half scale deflection  $\Rightarrow$  Total resistance = Resistance of galvanometer + reading hsd

$$\rightarrow \left\{ R_x = R_p + R_{series} \right\}$$

49



$$V_m = 5 \times 10^5 \text{ mA}$$

$$\approx 2500 \text{ mV}$$

$$i_h = 50 \frac{50}{0.5} = 500 \text{ mA}$$

$$i_h = 100 \text{ mA}$$

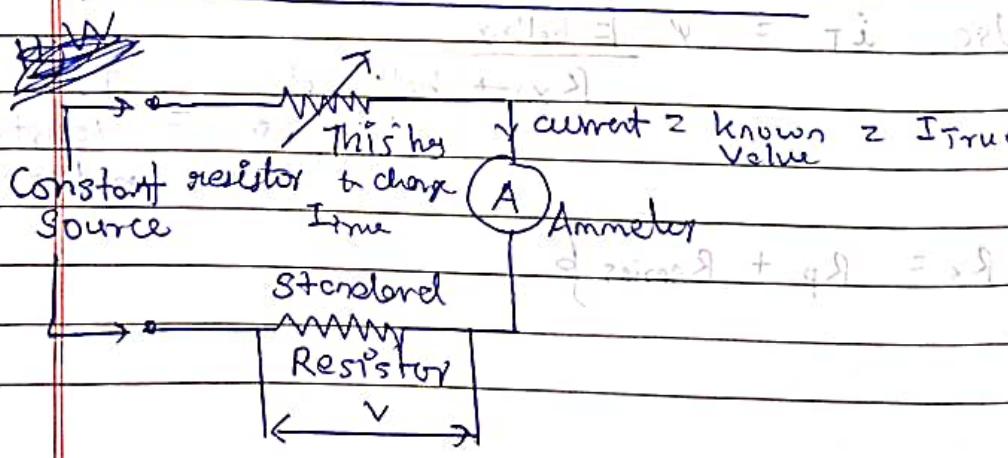
$$i_{sh} = 50 - 5 = 45 \text{ mA}$$

$$i_b = \frac{3/0.5}{30/5} = 6 \text{ A}$$

$$R_{sh} = \frac{2.5}{45} = 5/99 \Omega$$

→ multimeter → Multirange Voltmeter ← Ammeter → Multirange + Ohmmeter

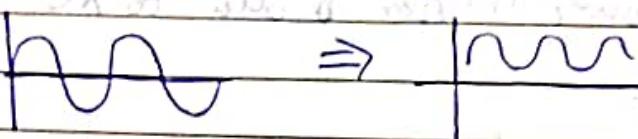
### Calibration of instrument



~~H.W.~~

5.0) Determine Derive a method to calibrate a voltmeter.

Alternating current indicating instrument



unidirectional torque

→ rectification

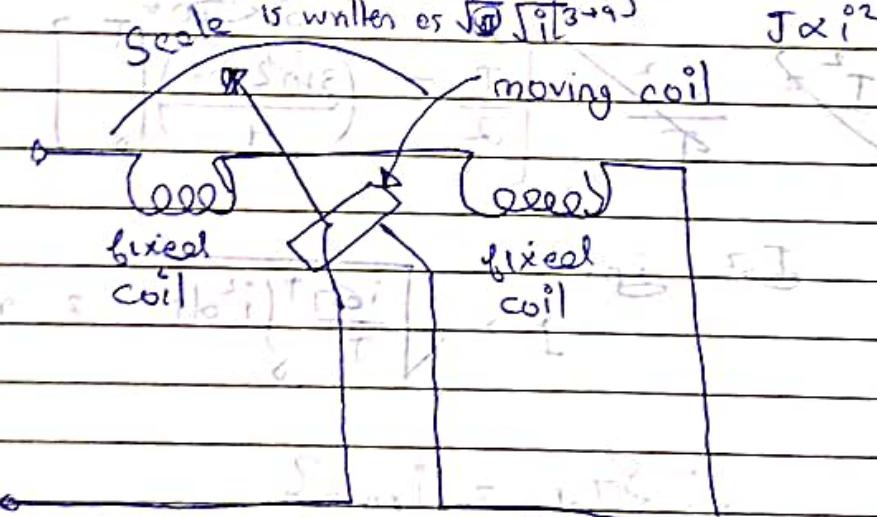
→ heating effect

$B \rightarrow$  is function of

$$\left\{ \begin{array}{l} 1+1 \\ 2+4 \end{array} \right\}$$

~~$B \propto J = BAN$~~  → function of  $i^2$

moving coil



$$T \propto BAN$$

$T \propto i^2$   $\therefore T \propto i^2$   $\therefore T \propto \theta$   $\therefore \theta \propto i^2$   $\therefore \theta \propto i^2$

$$\theta \propto i^2$$

$$\{I_{dc} = i_{rms}\}$$

\* An AC produce heat in a given resistance some average rate, as of DC.

\* Power Transfer due to DC =  $I^2 R$

\* Average Power Transfer b due to AC =  $\frac{1}{T} \int_0^T i^2 R dt$

$$I^2 R = \frac{1}{T} \int_0^T i^2 R dt$$

$$\frac{I^2}{T} = \frac{i_m^2}{T} \int_0^T \left( \frac{1 - \cos 2\omega t}{2} \right) dt$$

$$\frac{I^2}{T} = \frac{i_m^2}{T} \left[ \frac{T}{2} - \left( \frac{\sin 2\omega t}{4} \right) \Big|_0^T \right]$$

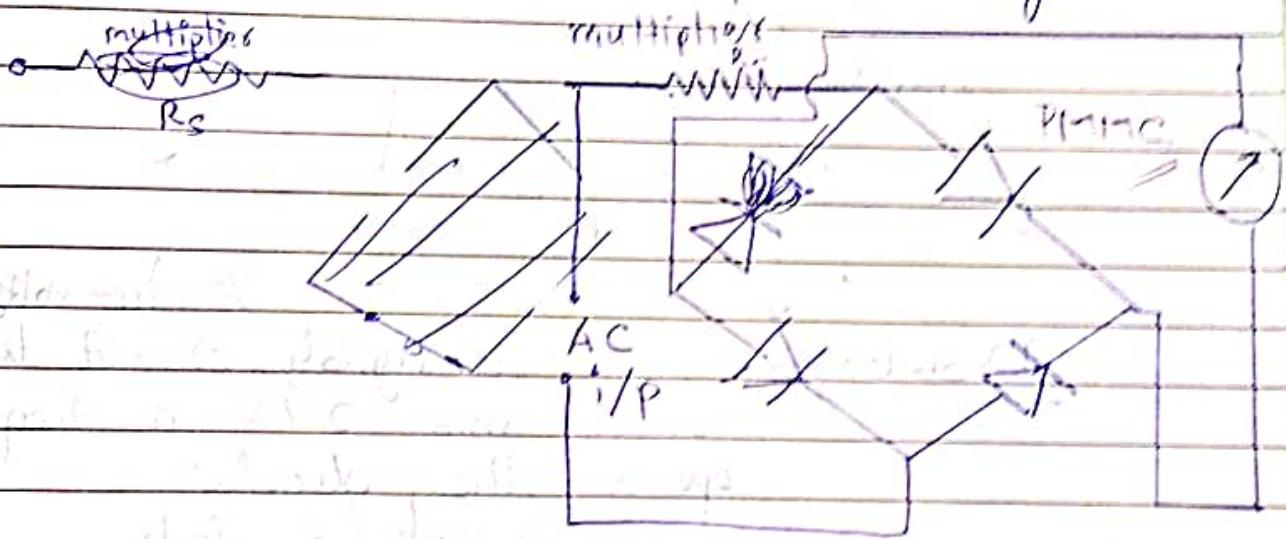
$$I^2 = i_m^2 \sqrt{\frac{1}{T} \int_0^T i^2 dt} = \text{root mean square}$$

$$\therefore \{ I_{\text{AC}} = i_m \}$$

So we can calibrate using DC & use it device for AC measurement with the same scale.

## Diseadvantages

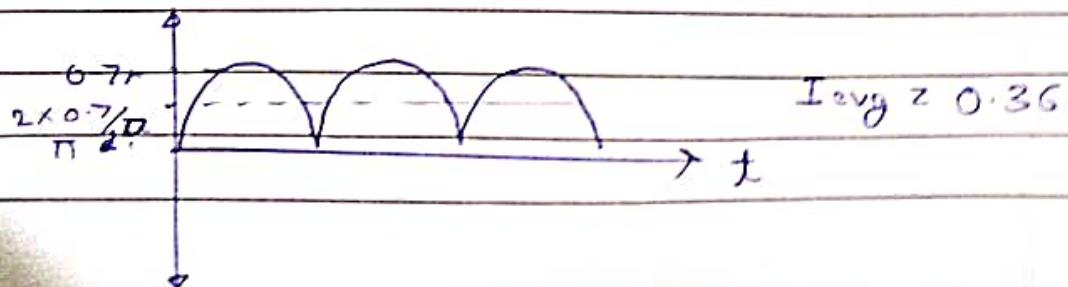
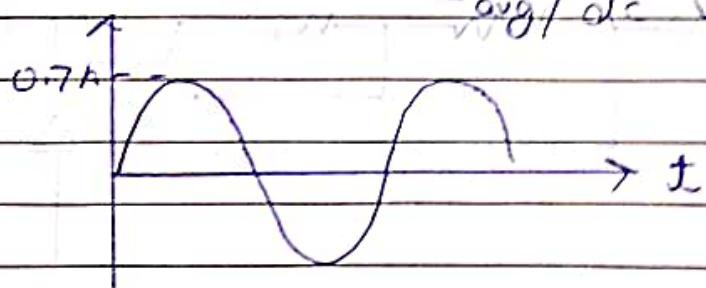
- cannot measure small current
- High power consumption  
Error due to heating of the coil
- weak flux due to nature of medium
- impedance of coil as a function of frequency

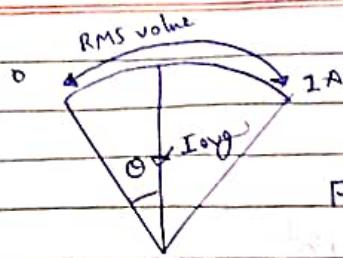


\* converts bidirectional AC into unidirectional DC

\* oscillations occur across

avg/dc value (critically damped)





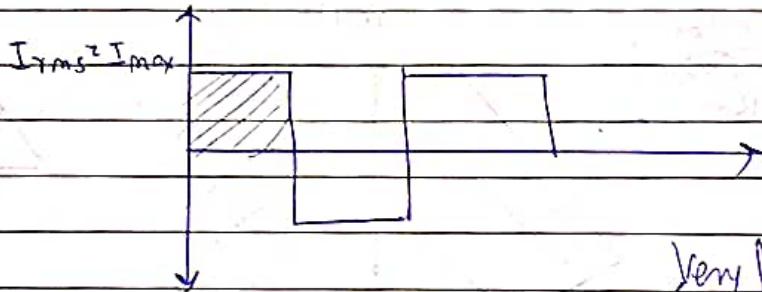
$$\text{Form factor} = \frac{\text{RMS}}{\text{avg. value}}$$

$$I_{\text{rms}}^2 = \frac{T}{T_0} / I_0$$

$$I_{\text{avg.}} = \frac{T}{T_0} / I_0$$

$$= 1.11 // \text{(only for sine wave)}$$

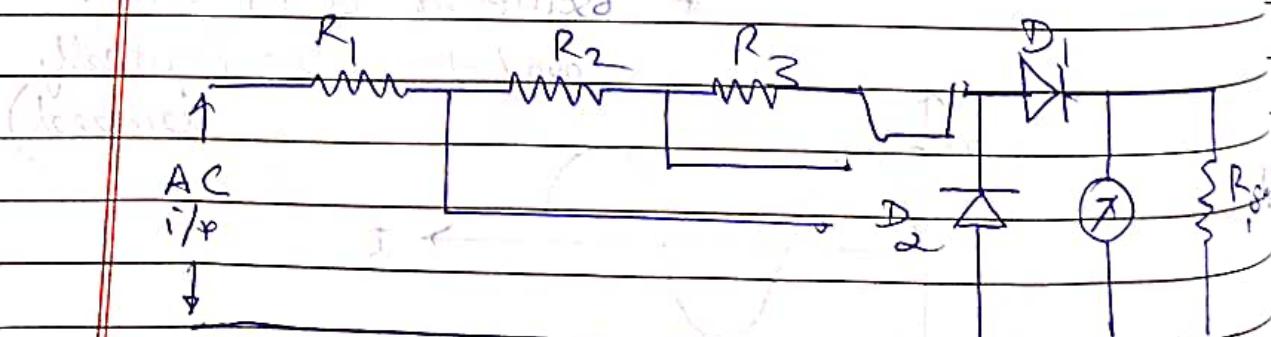
Q) What if signal is not sine wave?  
Use basic math to find area under curve.



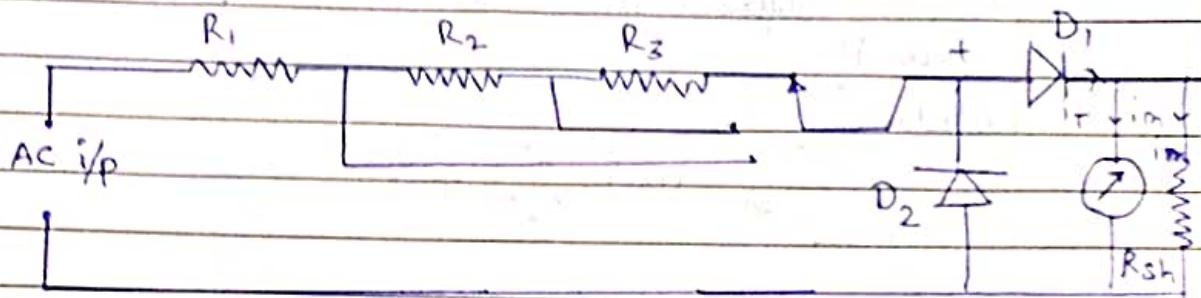
Very low voltage

- Drawbacks:
- Small signals cannot be amplified since min 0.7 V is required to operate the diode.
  - Non linearity of diode

2A. Bridge rectifier circuit - Non linear operation



## Typical Multimeter Circuits



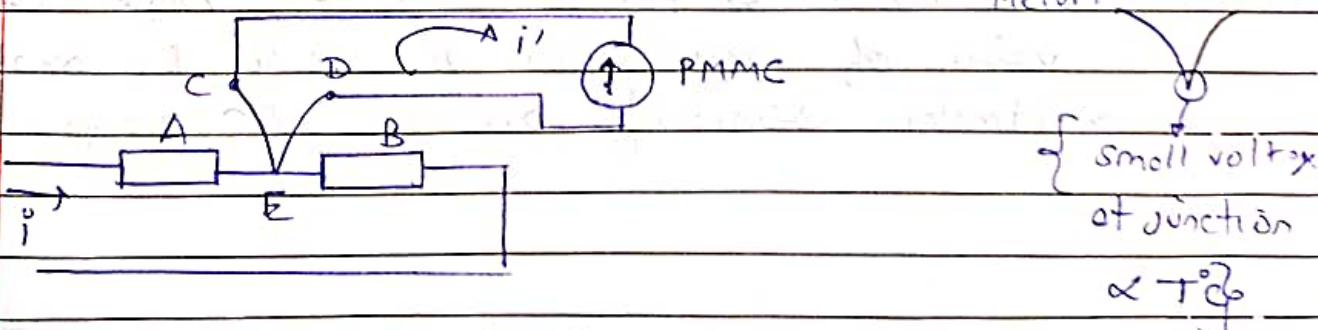
$$i_{\text{m}} = \left( \frac{R_{\text{m}}}{R_{\text{m}} + R_{\text{sh}}} \right) \times i$$

- PMMC deflection  $\propto$  Avg. values of half cycle
- $R_{\text{sh}}$ : a very low value resistor used to draw more current to push the needle linearly.
- Avg. value of half cycle = 0.45 RMS value
- $D_2$ : prevents reverse saturation current through  $D_1$ .
- $R_1, R_2 \& R_3$  are used to have multiple ranges.

Ammeter  
Thermoinstrument = combination of metal junction (P.T. junction) & PMMC

combination of thermocouple is PMMC.

- When two dissimilar metals are in contact
- small voltage is generated at the junction



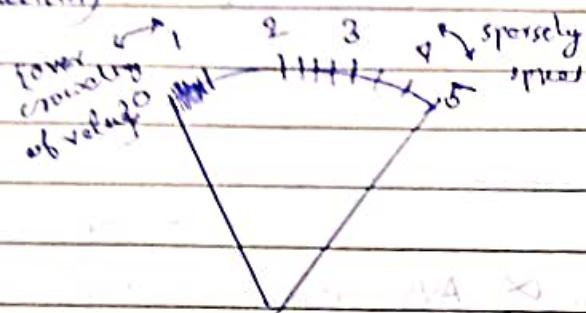
STEP A & B heating elements  
Heat  $\propto i^2 R$

CE & DE : Dissimilar metal joined at E.

Potential difference b/w C & D  $\propto$  Temperature of junction

$$\theta \propto i^2_{rms}$$

(deflection)



### Limitation

- Large current ( $i$ )
- Ambient temperature (How it is affected? How can it be avoided?)

### Meter movement

- (Q) If  $i_m$ , internal resistance  $\approx 100\Omega$  and required DC for full scale deflection  $\text{shunting Resistor}$  placed across movement has resistance  $> 100\Omega$ . If  $d_1$  and  $d_2$  has average forward resistance  $400\Omega$  and assume no resistance in reverse direction. For a 10V AC range calculate value of multiplier resistance  $R_g$  and voltmeter sensitivity on the AC range.

$$100 \times 1 = 100 \times \frac{1}{2}$$

$$i_T = 2 \text{ mA}$$

$$\cdot \times 10 - 2R_S - 400 \times 2 \times 10^3 - 100 \times 1 = 0$$

$$0.45 \times 10 - (800 + 100) \times 10^3 = 2R_S \times 10^3$$

$$4.5 \cancel{10} - 900 \times 10^3 = 2R_S \times 10^3$$

$$R_S = 10 - 0.9 \times 10^3$$

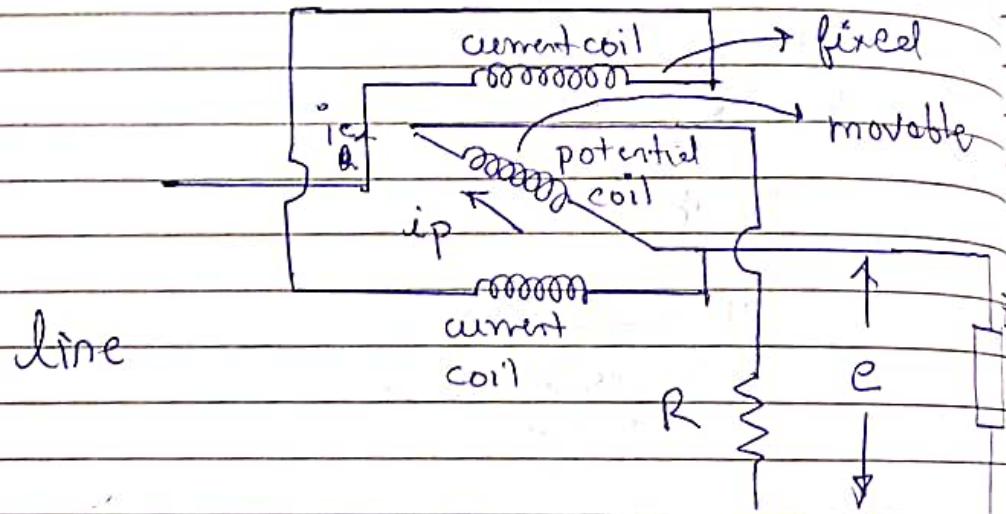
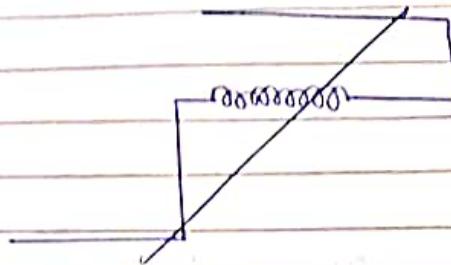
$$= \frac{8.1 \times 10^3}{2 \times 10^3}$$

$$= 4.05 \times 10^3$$

$$= 4.05 \text{ k}\Omega$$

$$S = \frac{2250 \Omega}{10V} = 225 \Omega/V$$

## Electrodynamometer in Power Measurement



$$\text{Deflection } \theta \propto i_p \times i_c$$

$$i_p = \frac{e}{R_p}$$

where

$$R_p = R + \text{resistance of potential coil}$$

$$\theta \propto i_p \cdot e$$

$$\theta_{avg} = k \cdot \frac{1}{T} \int_0^T \frac{i_c e}{R_p} dt$$

$$i_c \approx i \quad \{ R \text{ is very high} \}$$

$$\Theta_{avg} = \frac{k_2}{\Phi T} \int_0^T i_e dt$$

$$i = I \sin \omega t$$

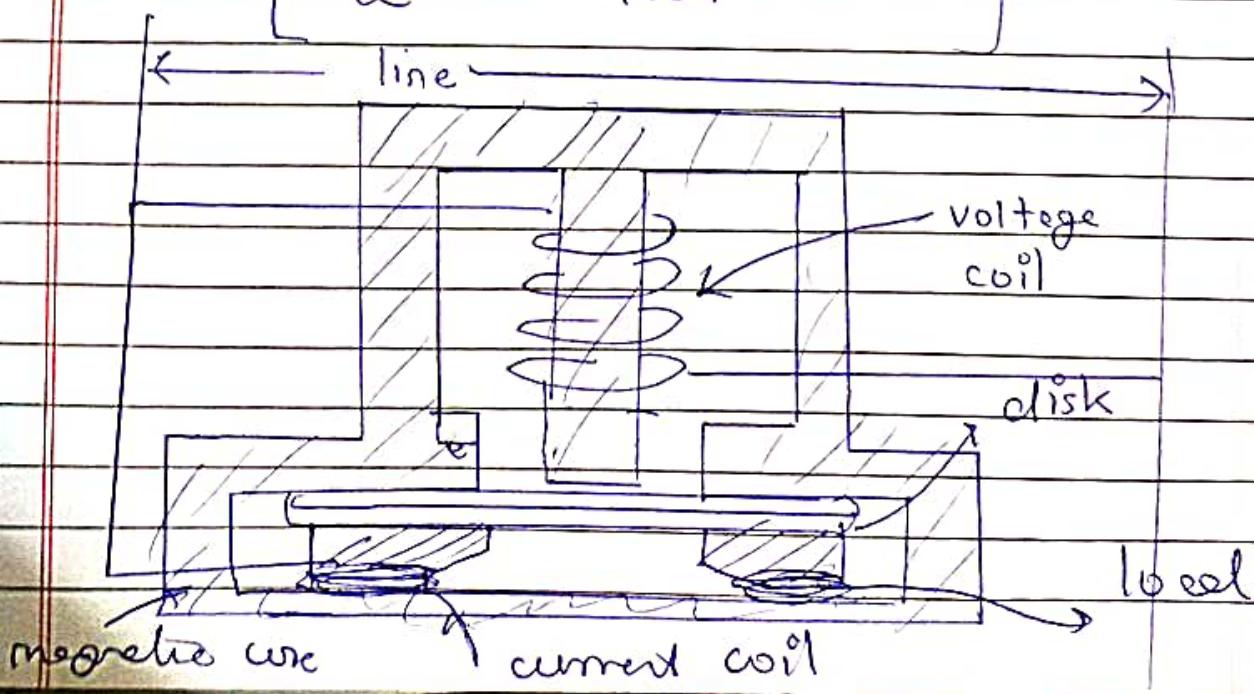
$$e = E \sin \omega t$$

$$\frac{k_2 IE}{T} \int_0^T 1 - \cos 2\omega t dt$$

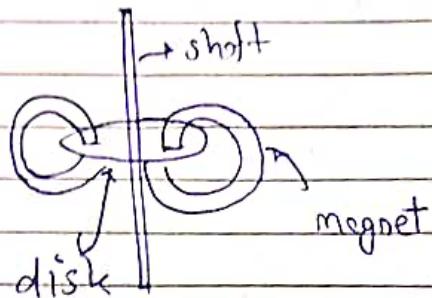
$$\frac{k_2 IE}{T} \left[ \frac{T}{2} - \frac{\sin 2\omega t}{2(2\omega)} \right]_0^T$$

$$\frac{k_2 IE}{T} \left( \frac{I}{2} - \frac{\sin 2\omega T}{4\omega} \right)$$

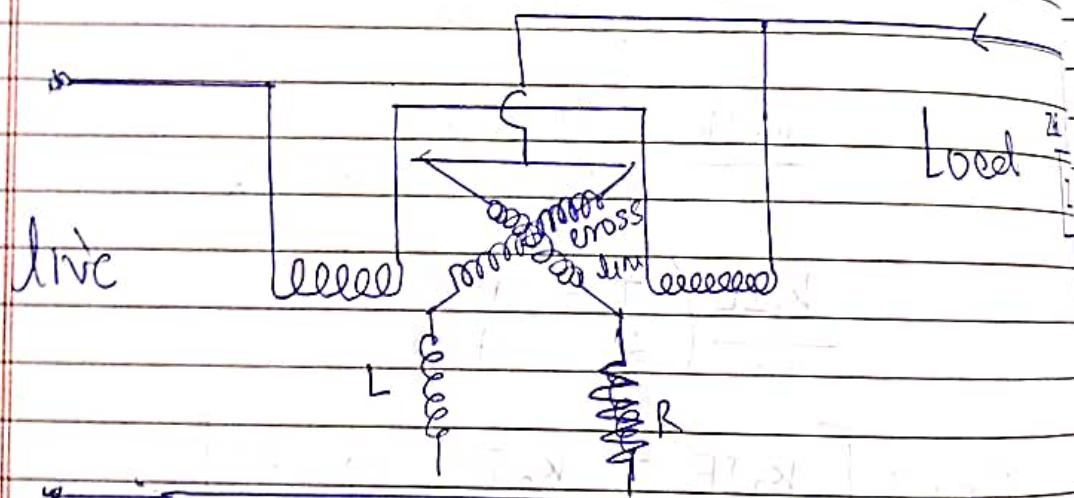
$$\Theta_{avg} = \left[ \frac{k_2 IE}{2} - \frac{k_2 IE}{4\omega T} \sin 2\omega T \right]$$



### Watt hour Meter



### Power Factor Meter



$$R_{th} = R_1 \parallel R_3$$

$$V_{Ho} = \frac{E}{R_1 + R_3}$$

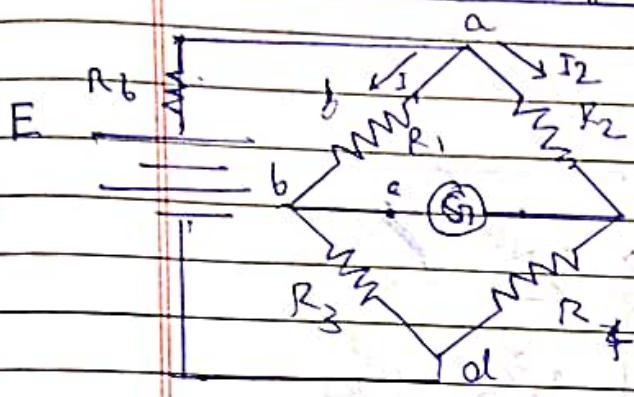
[Wheatstone]

Limit

- Lim
- eff

## Bridge Measurement

### Wheatstone Bridge



$$I_1 = \frac{E}{R_1 + R_3}$$

$$I_2 = \frac{E}{R_2 + R_4}$$

$$V_{ab} = V_{ac} \quad \left\{ \begin{array}{l} V_{bc} = 0 \\ V_b = V_c \end{array} \right.$$

$$\frac{ER_1}{R_1 + R_3} = \frac{ER_2}{R_2 + R_4}$$

$$R_{th} = R_1 || R_3$$

$$V_{th} = \frac{ER_3}{R_1 + R_3}$$

~~$$R_1 R_2 + R_1 R_4 = R_2 R_1 + R_2 R_3$$~~

~~$$R_1 R_4 = R_2 R_3$$~~

$$\left[ \begin{array}{l} R_1 = R_3 \\ R_2 = R_4 \end{array} \right]$$

[Wheatstone bridge : 1 Ω to few MΩ]

### Limitations -

- limiting error
- effect of change in temp. is not uniform

e.g.:  $R_1 = 1 \text{ M}\Omega \pm$  limiting error

$$R_2 = R_3 = 1 \text{ k}\Omega \pm \text{limiting error}$$

$$\frac{R_2}{R_1} = \frac{1}{2}$$

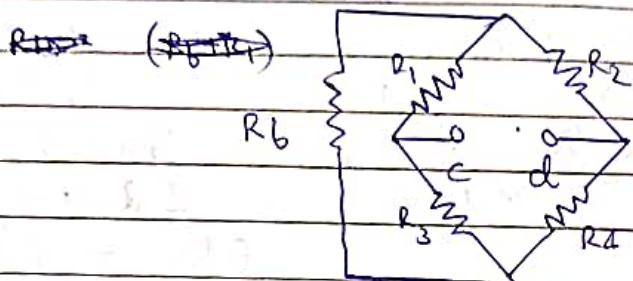
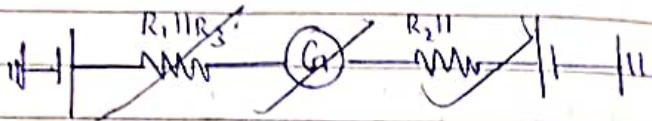
$$R_1 = 2 \text{ }\Omega$$

$$R_2 = 1 \text{ }\Omega$$

$$R_3 = 2 \text{ }\Omega$$

$$R_4 \approx ? \approx 1 \text{ }\Omega$$

• Lead resistance



Let  $R_1 = 0$

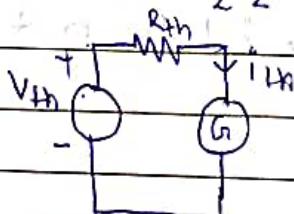
$$R_{Th} = (R_1 \parallel R_3) + (R_2 \parallel R_4)$$

$$E - i_1 R_1 - i_3 R_3 = 0$$

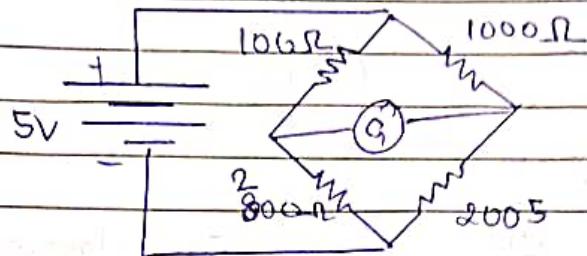
$$V_{Th} = V_C = i_1 R_1 - E \quad V_{OL} = i_2 R_2 - E$$

$$V_{Th} = V_C - V_{OL} = i_1 R_1 - i_2 R_2$$

$$V_{Th} = i_1 R_1 - i_2 R_2$$



- (1) The given figure has galvanometer sensitivity  $100 \text{ mV/V}$  and resistance of  $100 \Omega$ . Calculate deflection in galvanometer in terms of mm by unbalanced bridge.



$$R_{Th} = \left( 100 + \frac{2}{800} \right) \Omega \left( \frac{1000}{100 + 200} \right)$$

$$= \cancel{666.67} \cancel{277.78} \cancel{1888.89} \Omega \cancel{666.67} \Omega$$

$$V_{Th} = -i_1 R_1 - i_2 R_2$$

$$= -\frac{E}{R_1 + R_3} R_1 - \frac{E}{R_2 + R_4} R_2$$

$$= -1.083 - 2.773 \text{ mV}$$

$$I_g = 1.39 \text{ mA}$$

$$= 1.398 \times 10^{-3} \text{ A}$$

$$= 1.398 \times 10^{-3} \text{ A}$$

$$I_g = 1.398 \times 10^{-3} \text{ A}$$

$$= 1.398 \times 10^{-3} \text{ A}$$

$$= 1.398 \times 10^{-3} \text{ A}$$

$$R_{Th} = (100 || 200) + (1000 || 2005)$$

$$= 733.88 \Omega$$

$$V_{Th} = -i_1 R_1 - i_2 R_2$$

$$= -E \left( \frac{R_1}{R_1 + R_3} - \frac{R_2}{R_2 + R_4} \right)$$

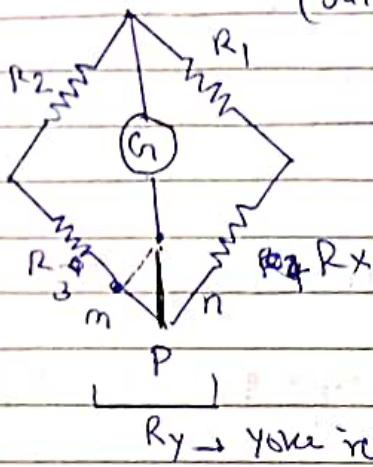
$$= 2.77 \times 10^3 \text{ V} = 2.77 \text{ mV}$$

$$I_{Th} = 3.32 \mu\text{A}$$

$$S = 33.21 \text{ mm}$$

### Kelvin Bridge

(suitable  $\leq 15\Omega$ )



$$(R_1)(R_3 + R_{mp}) = R_2(R_x)$$

$R_y \rightarrow$  true resistance

At point P,

$$\frac{R_{np}}{R_{mp}} = \frac{R_1}{R_2}$$

Balanced condition,

$$R_2 [R_x + R_{n-p}] = R_1 [R_3 + R_{mp}]$$

$$R_2 R_x + R_2 R_{n-p} = R_1 R_3 + R_1 R_{mp}$$

$$R_x = \frac{R_1 R_2}{R_2}$$

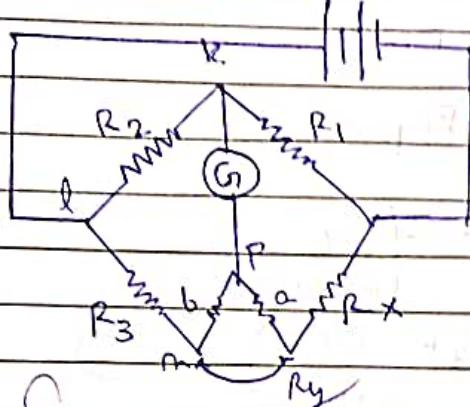
### Advantages

- Effect of lead resistance is eliminated

### Disadvantage

- Higher sensitivity galvanometer is required.

## Kelvin Double Bridge



Ratio Arms:  $R_1 \& R_2$  } [a, b are acting as]  
 Standard Arms:  $R_3 \& R_x$  } ratio arms

$$\frac{R_1}{R_2} = \frac{R_3}{R_x}$$

Balanced condition

$$R_1(R_3 + b) = R_2(R_x + a)$$

$$R_1R_3 + R_1b = R_2R_x + R_2a$$

$$R_x = \frac{R_1R_3}{R_2}$$

$$E_{KL} = E_{LMNP}$$

$$E_{KL} = R_2 \times \frac{E}{(R_1 + R_2) / (R_3 + a + b + R_x)}$$

$$= \frac{R_3 + a + b + R_x}{R_1 + R_2 + R_3 + R_x + a + b}$$

$$= R_2 \times \frac{E (R_1 + R_2 + R_3 + R_x + a + b)}{(R_1 + R_2)(R_3 + R_x + a + b)}$$

$$= \frac{R_3 + R_x + a + b}{R_1 + R_2 + R_3 + R_x + a + b}$$

$$E_{\text{in}} = B_0 \quad \frac{R_y E}{R_1 + R_2} = \frac{R_2}{R_1 + R_2} \Rightarrow I \left( R_3 + \frac{R_y}{a+b+R_y} \right) \quad (1)$$

$$E_{\text{imp}} = B_0 m + E_{\text{mp}}$$

$$IR_3 + I \left( \frac{R_y}{a+b+R_y} \right)$$

$$E_{\text{imp}} = I \left( R_3 + \frac{R_y}{a+b+R_y} \right) \quad (2)$$

equates (1) & (2)

$$\frac{R_2}{R_1 + R_2} \left[ R_3 + R_x + \frac{(a+b) R_y}{a+b+R_y} \right] = R_3 + \frac{R_x}{a+b}$$

$$\frac{R_x R_2}{R_1 + R_2} = R_3 + \frac{R_y}{a+b+R_y} - \frac{R_2 R_3}{R_1 + R_2} - \frac{R_2 (a+b)}{(R_1 + R_2) (a+b)}$$

$$(R_3 a + R_3 b + R_y R_3) / (R_1 + R_2)$$

$$\left\{ \begin{array}{l} a R_2 = b R_1 \\ \end{array} \right.$$

~~$$R_1 R_3 a + R_1 R_3 b + R_1 R_y R_3 + R_2 R_3 a + R_2 R_3 b + R_2 R_y$$~~

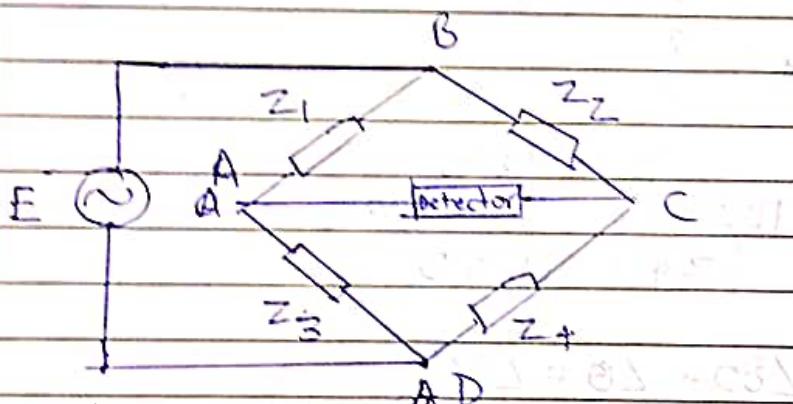
~~$$+ R_y R_1 + R_y R_2 - R_2 R_3 a - R_2 R_3 b - R_2 R_y$$~~

$$\frac{R_2 R_x}{R_1 + R_2} = - \frac{R_2 R_y a - R_2 R_y b}{(a+b+R_y)(R_1 + R_2)}$$

$$\frac{R_y R_1 + R_y R_2}{R_1 R_2} = \frac{R_1 R_3 (a+b+R_y)}{(a+b+f_y)}$$

$$\left\{ \begin{array}{l} R_x = \frac{R_1 R_3}{R_2} \\ \end{array} \right.$$

### AC bridges & their Applications



Balanced condition

$$\frac{E_{ba}}{E} = \frac{E_{bc}}{E}$$

$$\frac{z_1 i_1}{z_1 + z_3} = \frac{z_2 i_2}{z_2 + z_4}$$

$$i_1 = \frac{E}{z_1 + z_3} \quad i_2 = \frac{E}{z_2 + z_4}$$

$$\frac{z_1}{z_1 + z_3} = \frac{z_2}{z_2 + z_4}$$

$$z_1 z_4 = z_2 z_3$$

$$\frac{z_4}{z_3} = \frac{z_2}{z_1} \Rightarrow \frac{Y_3}{Y_4} = \frac{Y_1}{Y_2}$$

$$\{ Y_1 Y_4 = Y_2 Y_3 \}$$

$$z_1 = z \angle \theta$$

$$z_1 \angle \theta_1, z_4 \angle \theta_4 = z_2 \angle \theta_2, \Delta z_3 \angle \theta_3$$

$$z_1 z_4 \angle (\theta_1 + \theta_4) = z_2 z_3 \angle (\theta_2 + \theta_3)$$

To balance  $\{ z_1 z_4 = z_2 z_3 \}$   
 a bridge  $\{ \angle \theta_1 + \theta \angle \theta_4 = \angle \theta_2 + \angle \theta_3 \}$

Example

$$z_1 = 100 \angle 80^\circ \Omega$$

$$z_2 = ? \quad 250 \Omega$$

$$z_3 = 400 \angle 30^\circ$$

$$z_4 = ?$$

$$z_1 z_4 = z_2 z_3$$

$$100 \times z_4 = 250 \times 400$$

$$\{ z_4 = 1000 \Omega \}$$

$$80 + \angle \theta = 130^\circ$$

$$\{ \angle \theta = -50^\circ \}$$

$$\{ z_4 = 1000 \angle -50^\circ \Omega \}$$

Example :

$$z_{ab} = 400 \Omega$$

$$z_{bc} = ?$$

$$z_1 = 450 \Omega$$

$$z_2 = \cancel{900 \angle 53.13^\circ}$$

$$= 671.33 \angle -63.46^\circ + 600 \angle 58.1^\circ$$

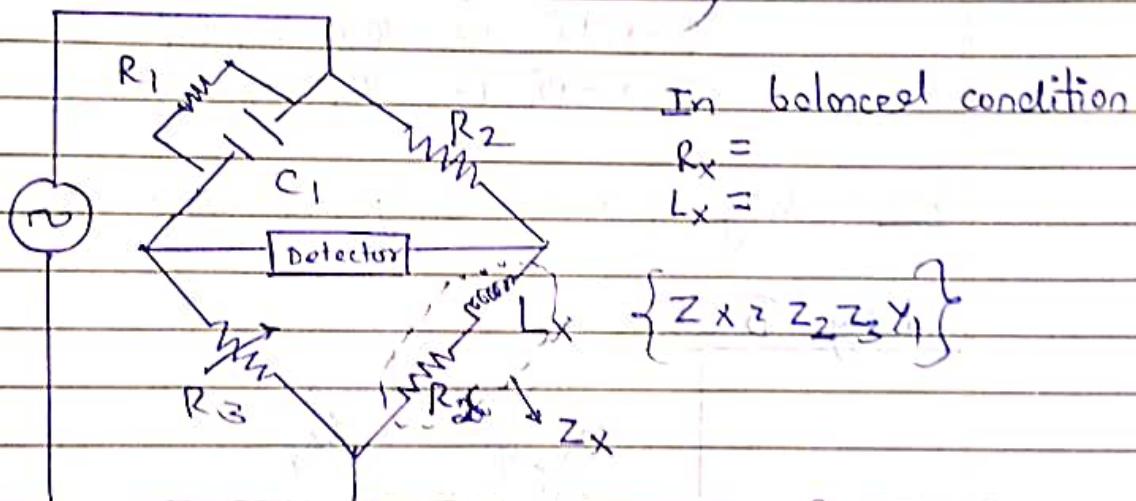
$$z_3 = 999.026 \Omega$$

$$z_4 = ? = 1018 \Omega$$

$$Z_4 = 1519.95 \angle 15.22^\circ$$

### Maxwell Bridge

It is used to find unknown inductance in terms of known capacitance. ( $1 < Q < 10$ )



$$\frac{R_1 X_C}{R_1 + X_C}, \quad R_2, \quad R_3, \quad \{R_x + X_L\}$$

$$\cancel{\frac{R_1 R_2}{R_2}} \frac{R_1 \cancel{+} X_{Cj}}{-R_1 X_{Cj}}$$

$$R_x + X_L = \frac{R_2 R_3 R_1}{-R_1 X_{Cj}} + \frac{R_2 R_3 X_{Cj}}{R_1 X_{Cj}}$$

$$R_x + X_L = \frac{R_2 R_3}{X_C} + \frac{R_2 R_3}{R_1}$$

$$\left\{ \begin{array}{l} R_x = \frac{R_2 R_3}{R_1} \\ X_L = \frac{R_2 R_3}{X_C} \end{array} \right.$$

$$R_x = \frac{R_1 R_2}{R_3}$$

$$L_x = R_2 R_3 C_1$$

$$\varphi = \frac{\omega X_L}{R} = \frac{\omega L}{R} \quad 1 < Q < 10$$

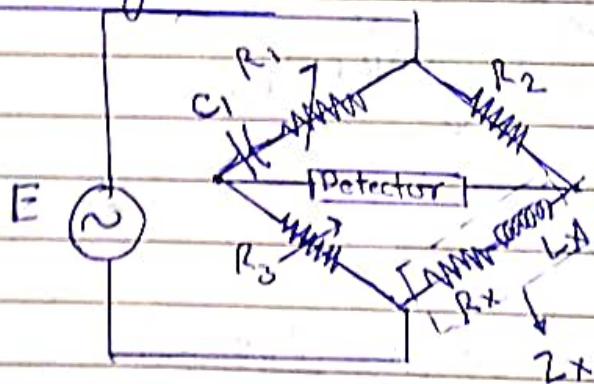
$$\begin{aligned} L_{Q_2} + L_{Q_3} &= 0, & \{ \text{Resistance} \} \\ L_{Q_1} + L_{Q_4} &= 0, \end{aligned}$$

$\varphi \rightarrow 90^\circ$  i.e.  $Q$  is very high

$\varphi \rightarrow -90^\circ$  i.e.  $R_j \rightarrow \infty$

Q.W.: Why Maxwell Bridge is unsuitable for  $Q < 1$

### Hay Bridge



$$\frac{i_1 (X_C + R_1)}{E (X_C + R_1)} = \frac{i_2 \cdot R_2}{R_2 + R_3}$$

$$- R_x X_C + R_1 R_x + X_C X_L + R_1 X_L \neq R_2 X_C + R_3 R_2$$

$$= R_2 R_1 - R_2 X_C + R_3 R_2$$

j

$$(-R_x X_C + R_1 X_L - R_2 X_C + R_3 X_C) j$$

$$+ (R_1 R_x + X_C X_L + R_1 R_2 - R_1 R_2 - R_3 R_2) = 0$$

$$R_1 R_x + X_C X_L = R_2 R_3$$

$$R_1 X_L - R_2 X_C - R_3 X_C = 0$$

$$\frac{X_L^2}{R_1} \frac{R_x X_C}{R_3}$$

$$R_1 R_x + X_C R_x X_C = 0$$

$$R_x = \frac{\omega^2 C_1^2 R_1 R_2 R_3}{1 + C_1^2 R_1^2 \omega^2}$$

$$R_{Lx} = \frac{R_2 R_3 C_1}{1 + \omega^2 C_1^2 R_1^2}$$

$$\phi = \tan \theta_L = \frac{\omega L_x}{R_x}$$

$$\frac{\tan \theta_L}{\omega L_x} = \frac{\tan \theta_C}{1}$$

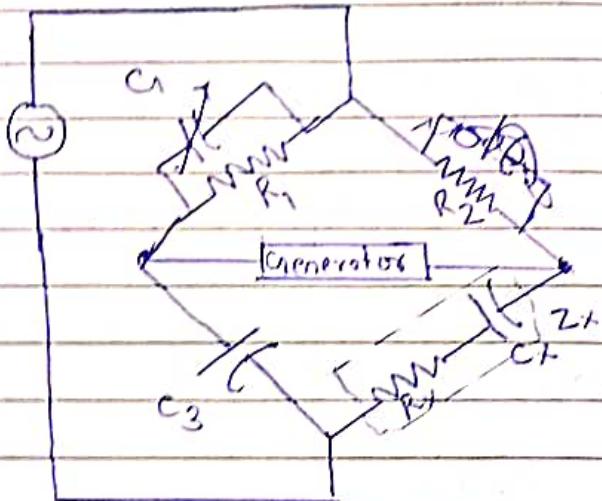
$$L_x = \frac{R_2 R_3 C_1}{1 + (1/\phi)^2}$$

$$\phi = 10 \\ (1/\phi) = 0.1$$

so  $\phi > 10$  does not affect  $L_x$

## Schering Bridge

- it is used for measurement of unknown copy.



$$\frac{R}{R_1 - (X_{C1} + X_C)} = \frac{R_2 R}{R_2 + R_X - C X_{C_X}}$$

$$\cancel{R_1^T R_2 + R_1 R_2} - (X C_{kj}) R_1 \neq -R_2 X C_{kj} - R_X X C_{kj} \neq 1.$$

$$= R_1 R_2 - x_{C1} R_2 \omega_j - x_{C3} R_2 j$$

$$R_1 R_{xy} - X_C_1 X_{C_y} = 0$$

$$\frac{R_1}{X_{C1}} = \frac{X_{C1}}{R_{0X}} \quad \textcircled{1}$$

$$-\text{RC}_1 - R_2 \cancel{\text{RC}_1} - R_3 \text{RC}_1 + \text{RC}_2 + \text{RC}_3$$

$$-\cancel{X_{C1}} \frac{R_1^2}{X_{C1} R_X} - R_X \cos^2 \theta + X_{C3} R_2^2 = 0$$

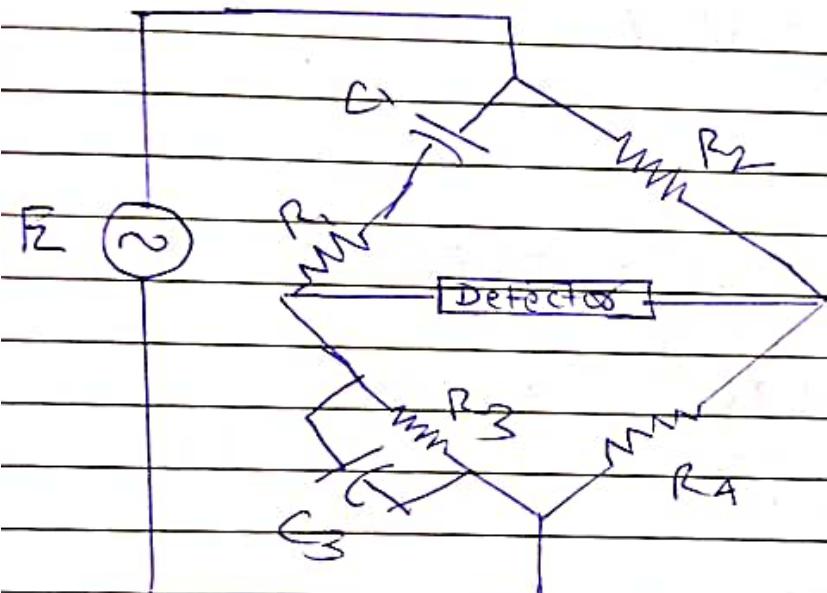
$$R_X R_1^2 - R_X X_{C1} + X_{C3} R_2^2 = 0$$

$$R_x = \frac{R_2 C_1}{C_3}$$

$$R_{Cx} = \frac{P_1 C_3}{P_2}$$

### Wien Bridge

Used to measure frequency



$$\left( R_3 + j \frac{1}{\omega C_3} \right) R_2 = \left( R_1 - j \frac{1}{\omega C_1} \right) R_4$$

$$\frac{R_3 R_2}{R_2 + j \frac{1}{\omega C_3}} = \frac{R_1 R_4}{R_1 R_4 + j \frac{1}{\omega C_1}}$$

$$R_2 = \frac{R_4}{j \frac{1}{\omega C_1}}$$

$$\left( -R_3 \frac{1}{\omega C_3} j \right) R_2 = R_1 R_4 - \frac{R_4}{\omega C_1} j$$

$$\frac{-R_3 \frac{1}{\omega C_3} j}{R_3 + j \frac{1}{\omega C_3}} R_2 = \frac{R_2 R_3 j}{R_3 C_3 \omega + j} = \frac{R_1 R_4 - R_4 j}{\omega C_1}$$

$$\frac{-\frac{R_2 R_3 j}{B_2} (R_3 C_3 \omega + j)}{\sqrt{(R_3 C_3 \omega)^2 + 1}} = R_1 R_4 - \frac{R_4}{C_1 \omega} j$$

$$\frac{\cancel{R_2 R_3}}{\sqrt{(R_3 C_3 \omega)^2 + 1}} - \frac{R_2 R_3^2 C_3 \omega j}{\sqrt{(R_3 C_3 \omega)^2 + 1}} = R_1 R_4 - \frac{R_4}{C_1 \omega}$$

$$\frac{(R_2 R_3)^2}{(R_3 C_3 \omega)^2 + 1} = (R_1 R_4)^2$$

$$\frac{(R_2 R_3)^2 = (R_1 R_4)^2 + \cancel{R_2 R_3} \cancel{C_3 \omega} (R_3 C_3 \omega)^2 (R_1 R_4)^2}{\sqrt{\frac{(R_2 R_3)^2 - (R_1 R_4)^2}{(R_3 C_3 R_1 R_4)^2}}} = \omega$$

$$\omega^2 = \frac{1}{R_1 R_4 R_2 C_3} \sqrt{R_2^2 R_3^2 - R_1^2 R_4^2}$$

(X)

Real parts

$$\frac{R_2}{R_4} = \frac{R_1}{R_3} + \frac{C_3}{C_1}$$

Imag. parts

$$\omega C_3 R_1 R_4 = \frac{R_4}{\omega C_1 R_3}$$

$$\omega^2 \sqrt{\frac{1}{C_3 C_1 R_3 R_1}}$$

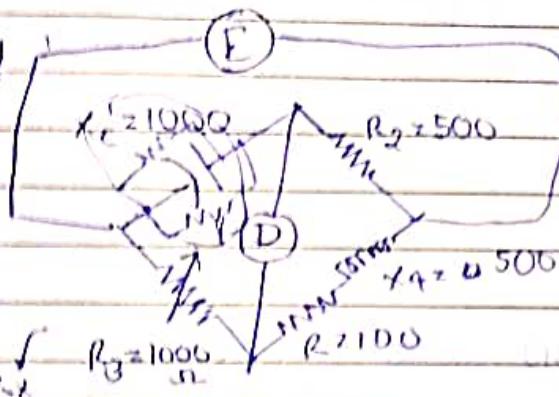
$$\int \omega = 1$$

$$2\pi \sqrt{R_1 R_3 C_1 C_3}$$

$$\text{if } R_1 = R_3$$

$$C_1 = C_3$$

$$\left\{ \begin{array}{l} \int \omega = 1 \\ 2\pi R_1 C_1 \end{array} \right.$$

HW

Determine whether  
bridge is completely  
balanced.  
if not find 2  
ways to make it  
balanced

$$\frac{1000 \times 500}{10} = (100 + 500j) \left( \frac{-1000j R_2}{R_2 - 1000j} \right)$$

$$5 \times 10^5 = \left( \frac{10^4 j R_2}{R_2 - 1000j} \right) + \left( \frac{5 \times 10^4 j R_2}{R_2 - 1000j} \right)$$

$$1 = \frac{2j R_2 + R_2}{R_2 - 1000j}$$

$$R_2 - 1000j = 2j R_2 + R_2$$

$$\left\{ R_2 = 5k\Omega \right.$$

$$Z_4 = Z_2 Z_3 Y_1$$

$$Z_4 = Z_2 Z_3 \left( 1 + j \omega C \right)$$

$$\frac{Y_1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{(j\omega C)^2}$$

$$\left\{ Y = \frac{Y_1}{R_1} + \omega C j \right\}$$

$$500R_x = 1 \times (16j + 50j) \left[ \frac{(-10j)(5+j)}{50j - 10j} \right]$$

$$R_x = (1+5j) \left( \frac{-50j}{5-j} \right)$$

$$R_x = \frac{-10 - 50j}{5-j}$$

$$= \frac{(-10 - 50j)(5+j)}{5j^2 + 1}$$

$$= \frac{-50 - 10j - 250j + 50}{5j^2 + 1}$$

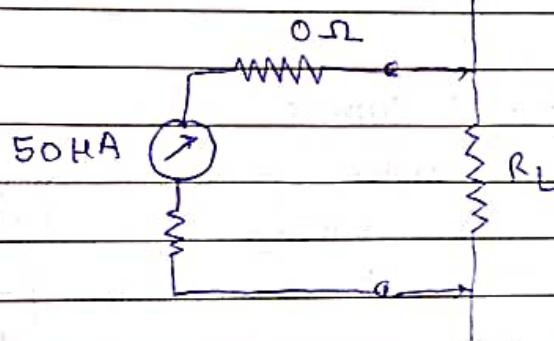
$$\text{B2} \rightarrow \text{B2D} \quad Z_3 = Z_1 Z_4 Y_2 \\ 100 \times 1000 \quad \{$$

## Electronic Instruments for measuring basic parameters

$$FSD = 50 \mu A$$

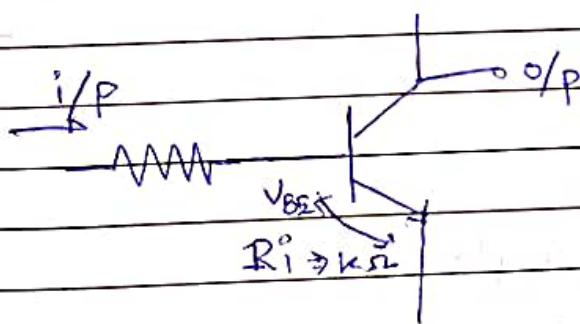
$$R_m = 160 \Omega$$

$$V_m = 5 \text{ mV}$$

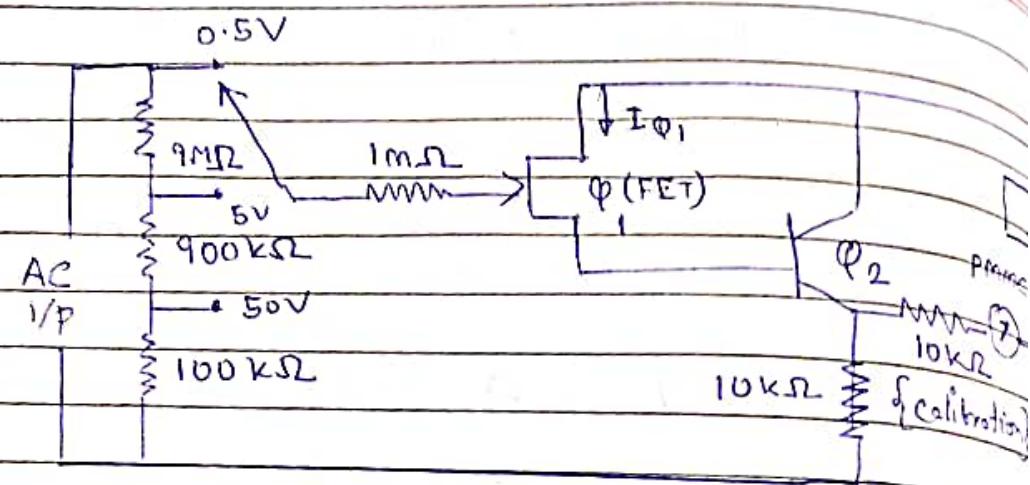


### Requirements -

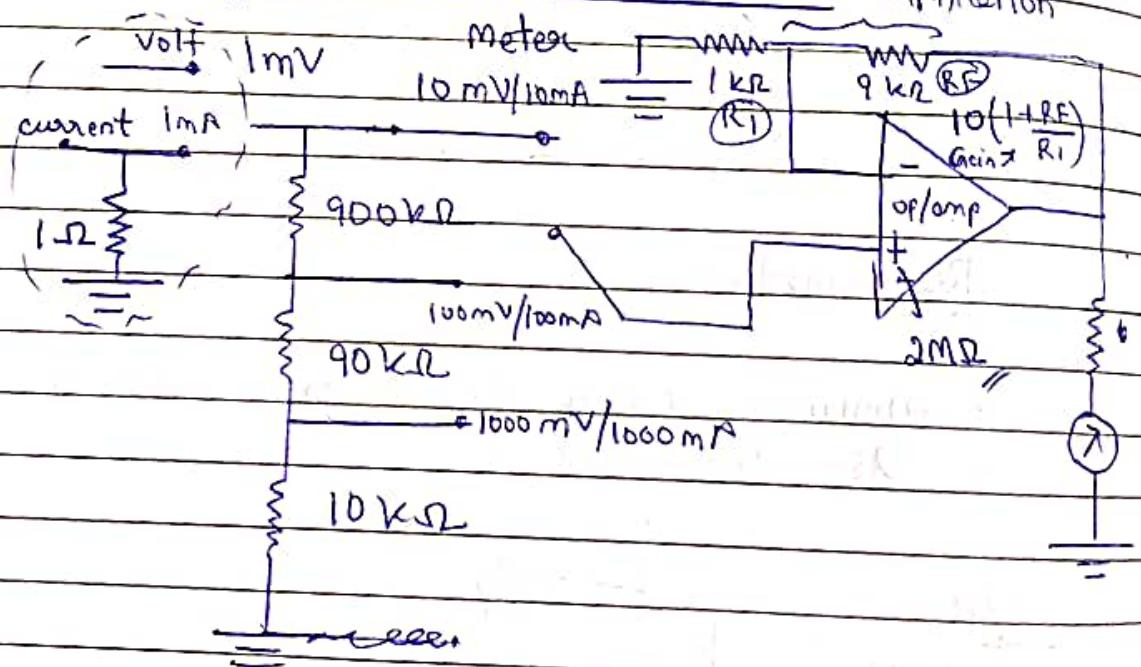
- minimum energy drawn from measurement
- Use the same PIMC



### Amplified DC Voltmeter



Amplified DC Voltage & Current meter Amplification



## OP-AMP (Operational Amplifier)

\* IC 741

\* Amplification

\* high i/p resistances

\* low o/p impedance

\* high gain (upto  $10^4$ )

\* ckt diagram of op-amp

- \* min power drawn from measured
- \* must provide sufficient current to produce deflection.
- \* sufficient o/p current to produce deflection in PMMC.

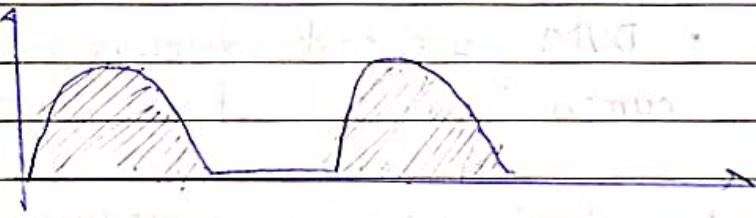
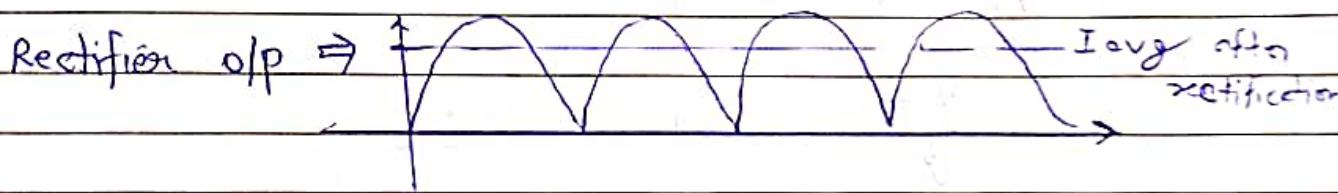
45V

(Q) How to measure small value AC signal?

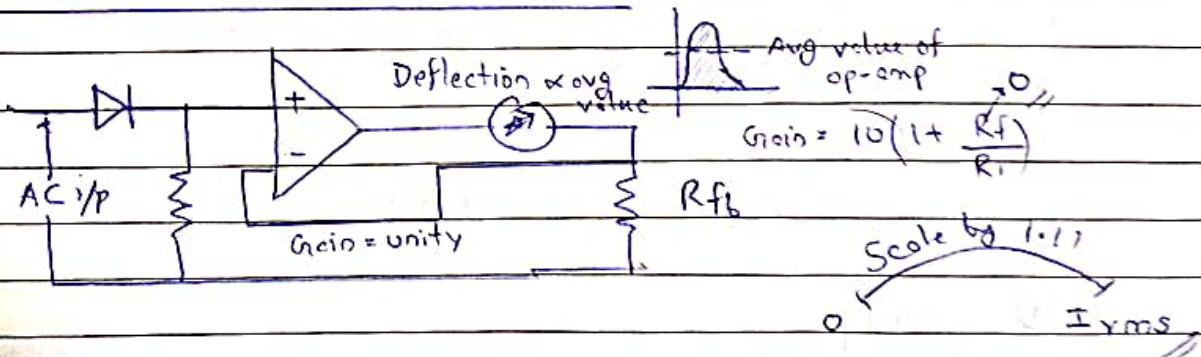
We have → Amplifier box

→ PMMC  $[θ \propto I_{avg}]$

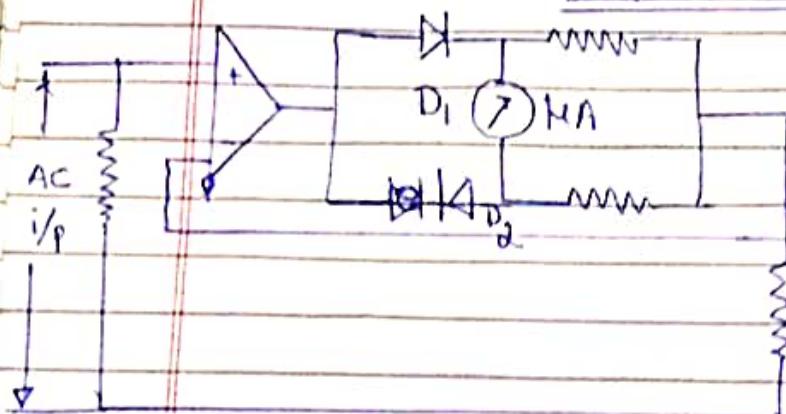
We require a rectifier type arrangement to convert bidirectional AC to DC.



### AC Voltmeter with Rectification



Rectifier Amplify → rectify



rectification after amplification -

- average responding type meter
- meter markings are corrected by a factor =  $F = \frac{1}{\pi}$
- full wave rectification

$$\frac{V_{pp}}{\sqrt{2}R_m}$$

### Digital Voltmeter

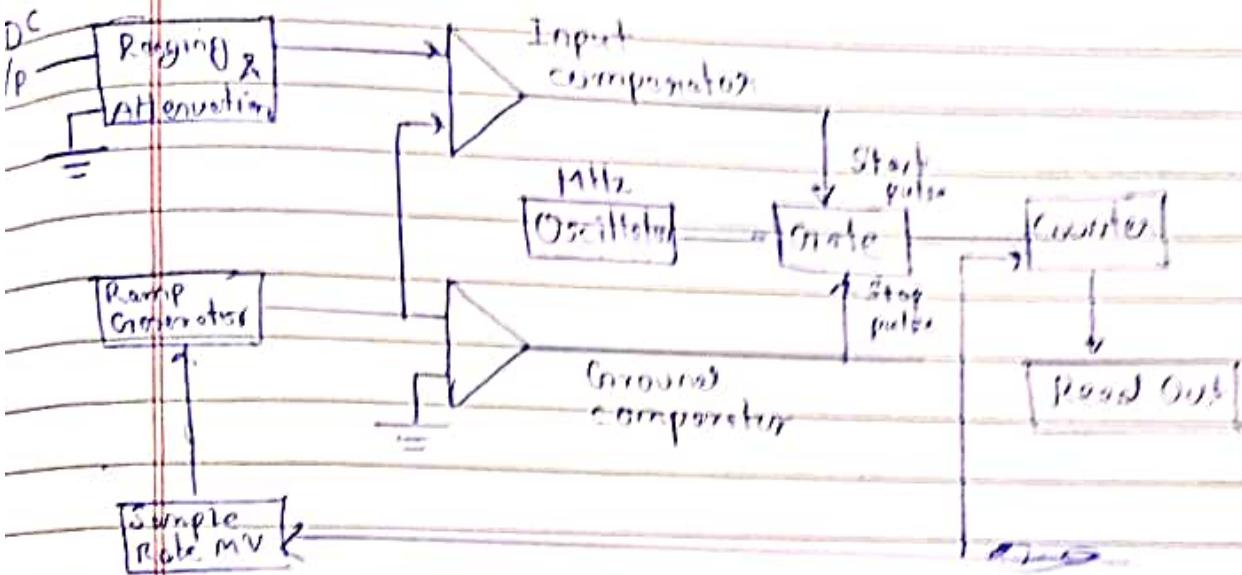
$$\frac{2V_{pp}}{R_m}$$

- DVM represent displays measurement as a digital numerical instead of a pointer deflection.
- reduces parallax, reduces time requirement for noting
- o/p is suitable for further processing or recording.

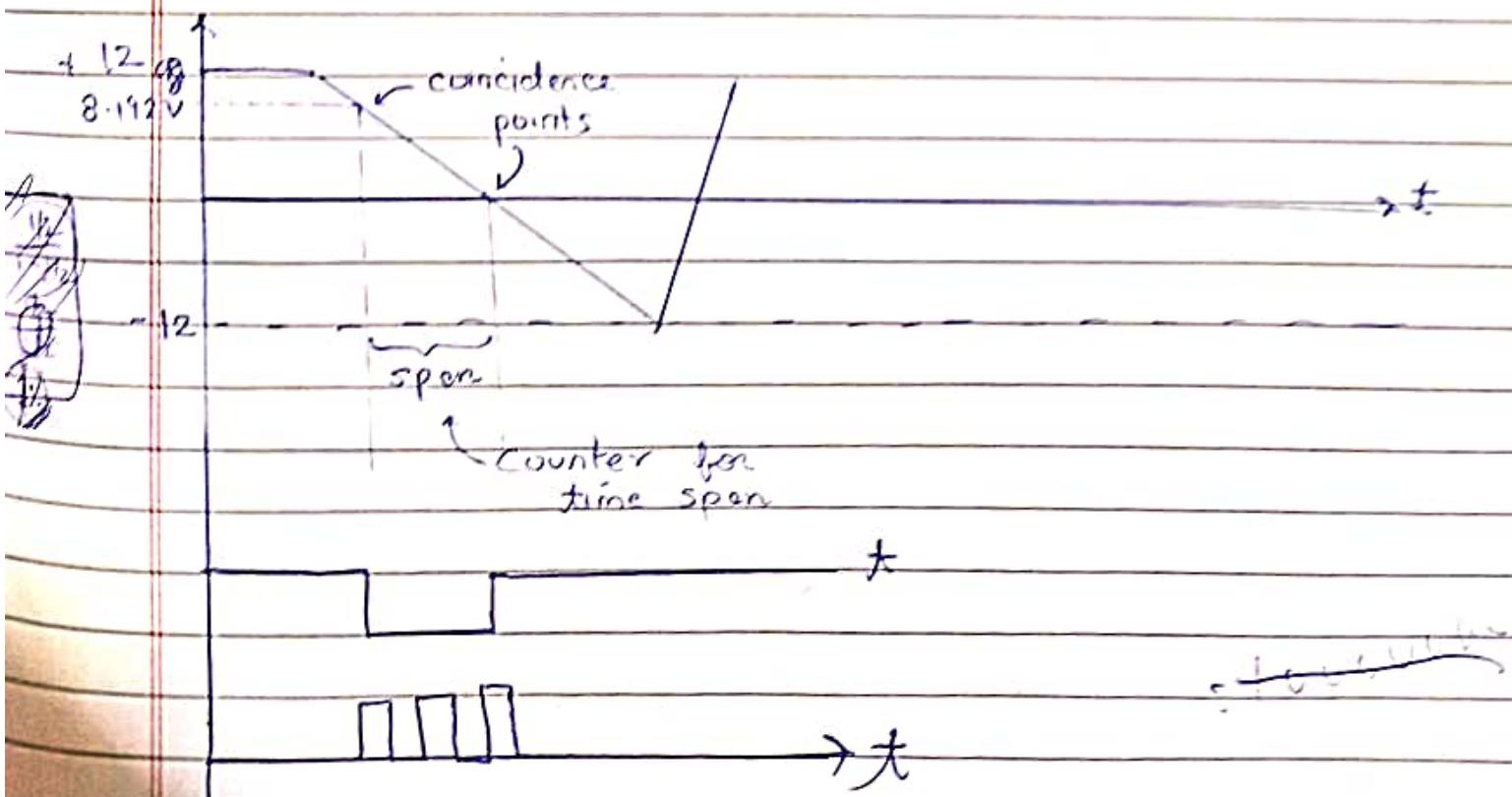
### DVM Classification

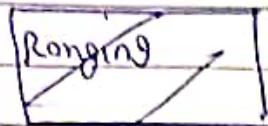
- ① Ramp
- ② Integrating
- ③ Continuous Balance
- ④ Successive Approximation

### Ramp-Type DVM

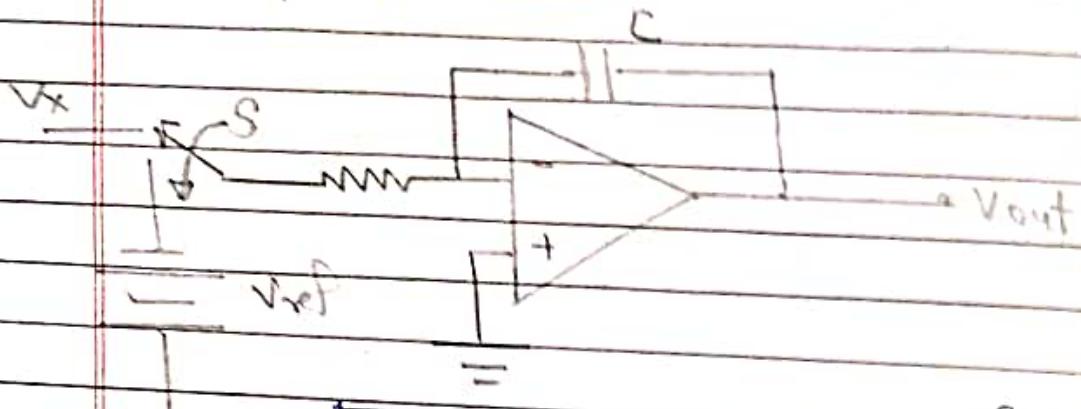


Operating principle : measure the time required for a linear ramp voltage to rise from 0V to the level of input voltage. This time interval is measured with an electronic counter.

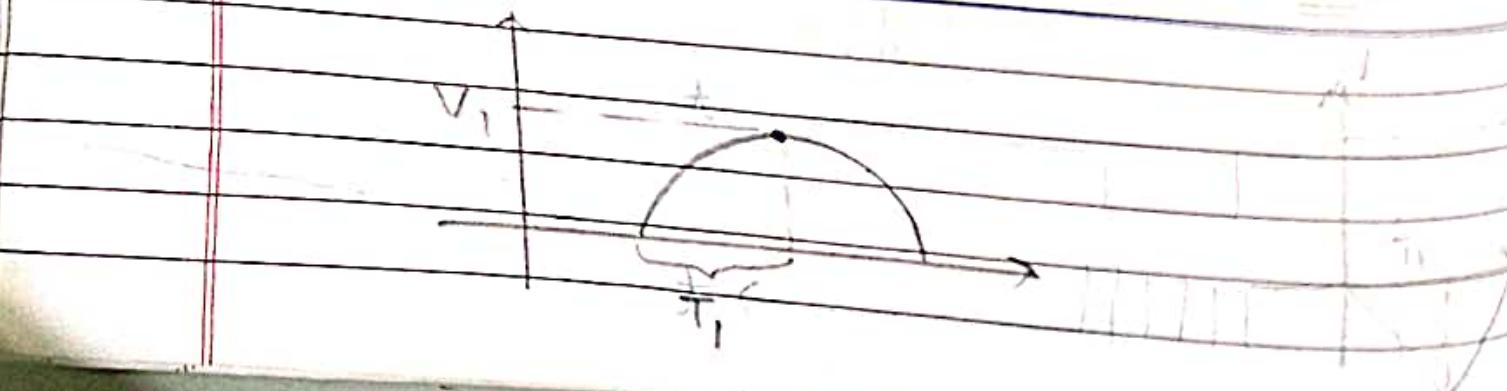
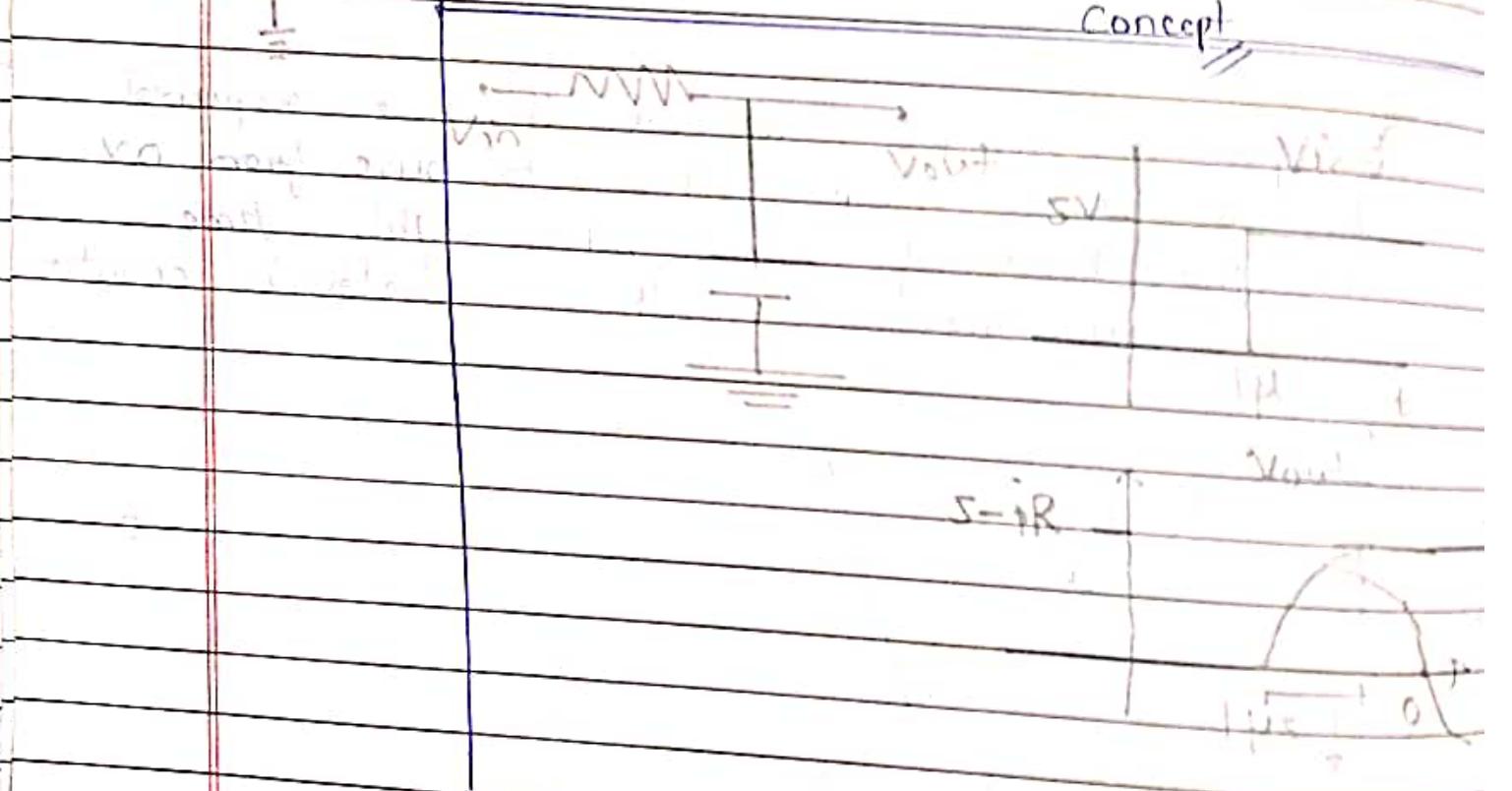


Ques  
08

## Integrating DVM



Concept



• OPAMP is used as integrator

O/p of OPAMP as integrator is

$$V_{out} = -\frac{1}{RC} t \cdot V_{in}$$

when  $V_x$  is applied

$$V_{out} = -\frac{1}{RC} t \cdot V_x$$

• we are connecting  $V_x$  only for ' $T_1$ ' duration  
and the o/p reaches ' $V_1$ ' volts within  $T_1$  time.

$$V_1 = -\frac{1}{RC} T_1 V_x$$

• at  $T_1$ , we are changing the position of  
switch 'S' from  $V_x$  to ' $-V_{ref}$ '.

$$V_{out} = -V_{ref} + \frac{1}{RC} (t - T_1)$$

$$= V_1 + \frac{1}{RC} t V_{ref}$$

$$\left. \begin{cases} V_{out} = V_1 + \frac{1}{RC} t V_{ref} \end{cases} \right\}$$

it takes ' $T_2$ ' time for  $V_{out}$  to go to OV.

$$0 = V_1 + \frac{1}{RC} T_2 V_{ref}$$

$$0 = -\frac{1}{RC} T_1 V_x + \frac{1}{RC} T_2 V_{ref}$$

$$\left. \begin{cases} V_x = \frac{T_2}{T_1} V_{ref} \end{cases} \right\}$$

## Successive Approximation Conversion

- assume that the "digital" no. to be determined is between 0 to 512.
- lets assume the voltage to be digitized is 4.99V.

e.g. Wheatstone Bridge Lab expt.

0 | 5 | 0 | 1 | V ... 0 to 2V

0 | 0 | 3 | 8 | mV ... 0 to 500 mV

Steps:

(1) 1<sup>st</sup> guess: = 256

if  $x \Rightarrow > 256$

Yes

(2) 2<sup>nd</sup> guess  $256 + 128 = 384$

if  $x > 384$

Yes

(3) 3<sup>rd</sup> guess  $384 + 64 = 448$

if  $x > 448$

Yes

(4) 4<sup>th</sup> guess  $448 + 32 = 480$

if  $x > 480$

Yes

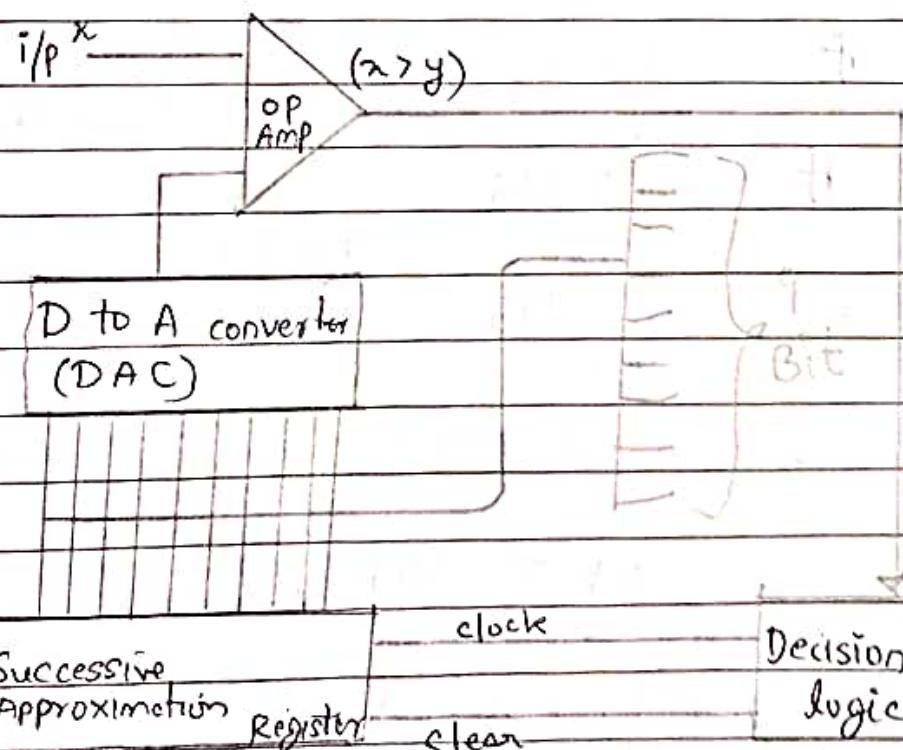
(5) 5<sup>th</sup> guess  $480 + 16 = 496$   
 $n > 496$  Yes

(6) 6<sup>th</sup> guess  $496 + 8 = 504$   
 $n > 504$  No

(7) 7<sup>th</sup> guess  $496 + 4 = 500$   
 $n > 500$  No

(8) 8<sup>th</sup> guess  $496 + 2 = 498$   
 $n > 498$  Yes

(9) 9<sup>th</sup> guess  $498 + 1 = 499$   
 $n = 499$



10 bit SAC, measured: 799

① if  $x > 512$

Yes  $512 + 256 = 768$

② if  $x > 768$

Yes  $768 + 128 = 896$

③ if  $x > 896$

No  $768 + 64 = 832$

④ if  $x > 832$

No  $768 + 32 = 800$

⑤ if  $x > 800$

No  $768 + 16 = 784$

⑥ if  $x > 784$

Yes  $784 + 8 = 792$

⑦ if  $x > 792$

Yes  $792 + 4 = 796$

⑧ if  $x > 796$

Yes  $796 + 2 = 798$

⑨ if  $x > 798$

Yes

⑩  $x = 798 + 1 = 799$

~~1100001111~~

~~1111000111~~

0	0	1	1	0	0	0	1	1	1
---	---	---	---	---	---	---	---	---	---

799
399
199

Quantization Error

499 V is to be converted by 9 bits

12 V is to be converted by 4 bits

$$12.3 \text{ V} \rightarrow 12 \text{ V}$$

$$\text{Error} = 0.3 \text{ V}$$

$$\text{Max. error} = 0.5 \text{ V}$$

For 499 V max error = 0.005 V

Max Error =  $\pm$  one half value of LSB

This is also called as Quantization error.

$$\text{Max error} = 0.005$$

(Q) What is quantization error while measuring voltage using DVM?

Ans: 2%

$$600 \text{ V} \rightarrow \cancel{9 \text{ bits}} \quad 0.05 \text{ V}$$

$$200 \times 10^3 \quad 200 \text{ V} \rightarrow 0.05 \text{ V}$$

$$20 \quad 20 \text{ V} \rightarrow \cancel{0.05 \text{ V}} \quad 0.005 \text{ V}$$

$$200 \quad 200 \text{ mV} \rightarrow 0.05 \text{ mV}$$

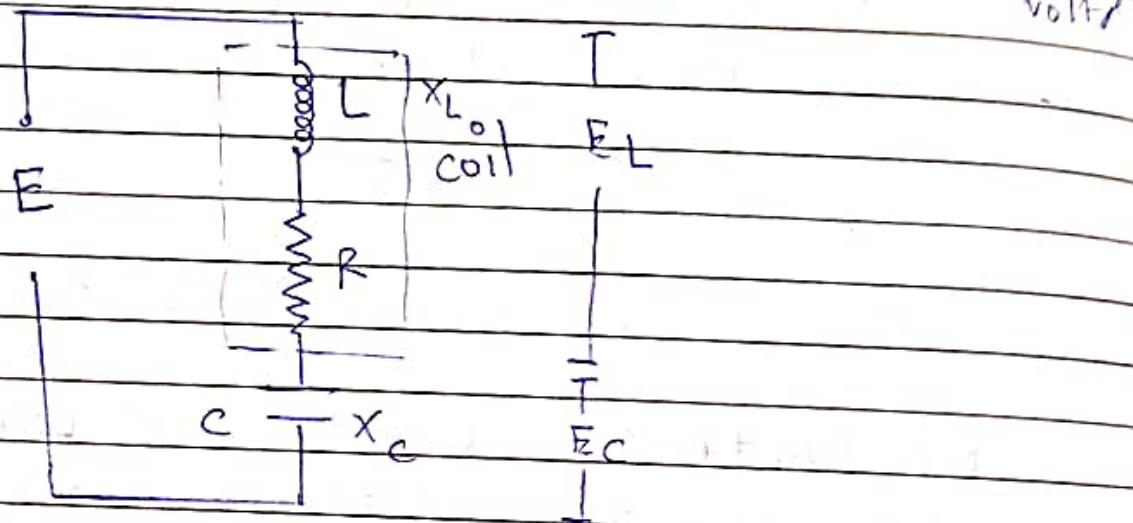
Q3

2  
3

## Q-Meter

Working principle : voltage across the coil of a series resonant ckt =  $Q \times$  Applied voltage ~~at resonance~~

voltage across the capacitor of a series resonant ckt =  $Q \times$  applied voltage



At resonance,

$$X_L = X_C$$

$$E_C = I X_C \quad E_L = I X_L$$

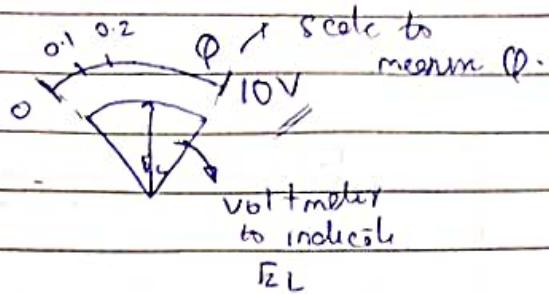
$$E = I R$$

$$E_L = Q E$$

$$\frac{E_L}{E} = Q = \frac{X_L}{R} = \frac{X_C}{R}$$

$E_L \Rightarrow$  can be measured using voltmeter

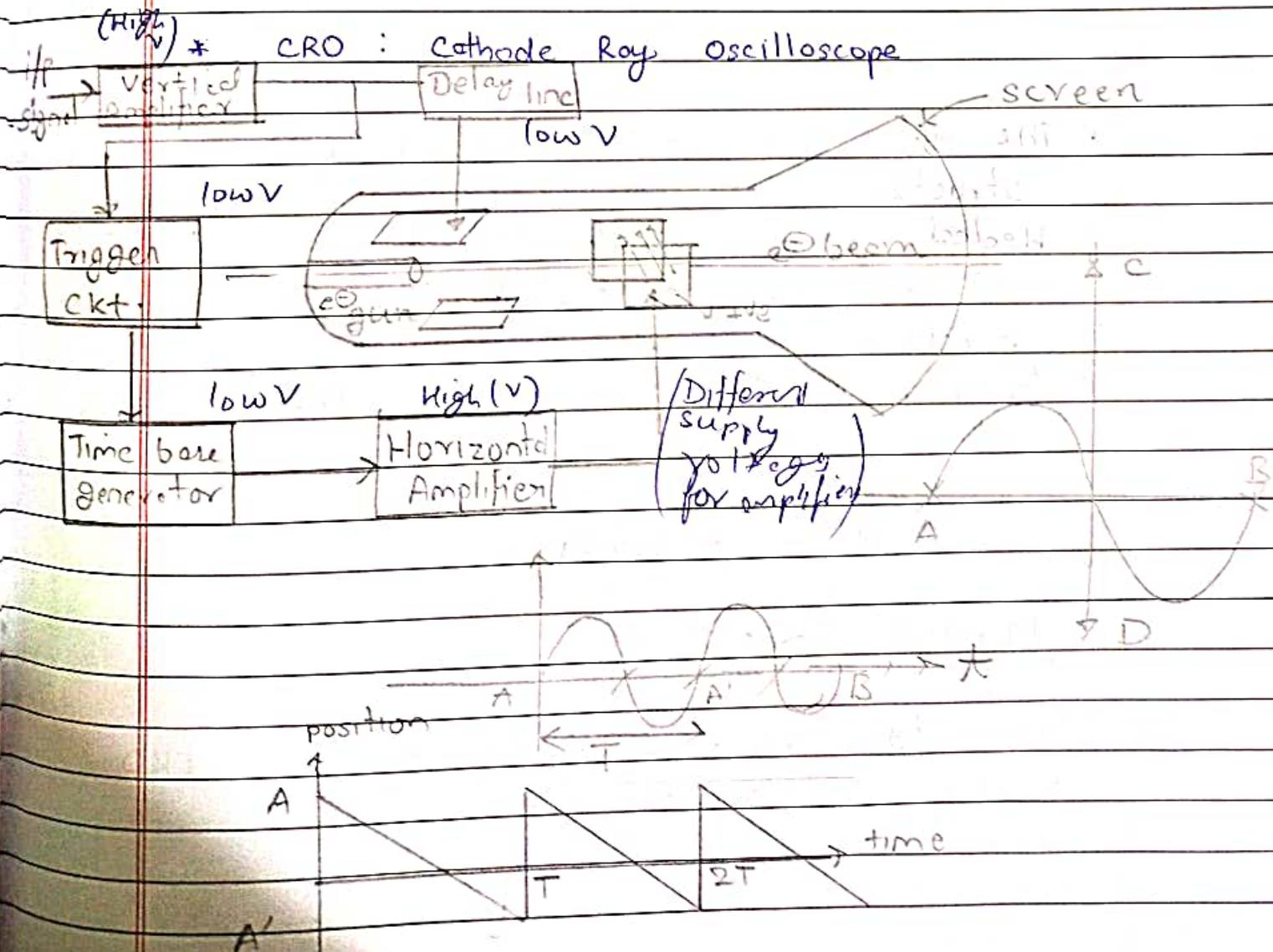
$$\varphi = \frac{x_L}{R} = \frac{x_C}{R}$$



## Oscilloscope

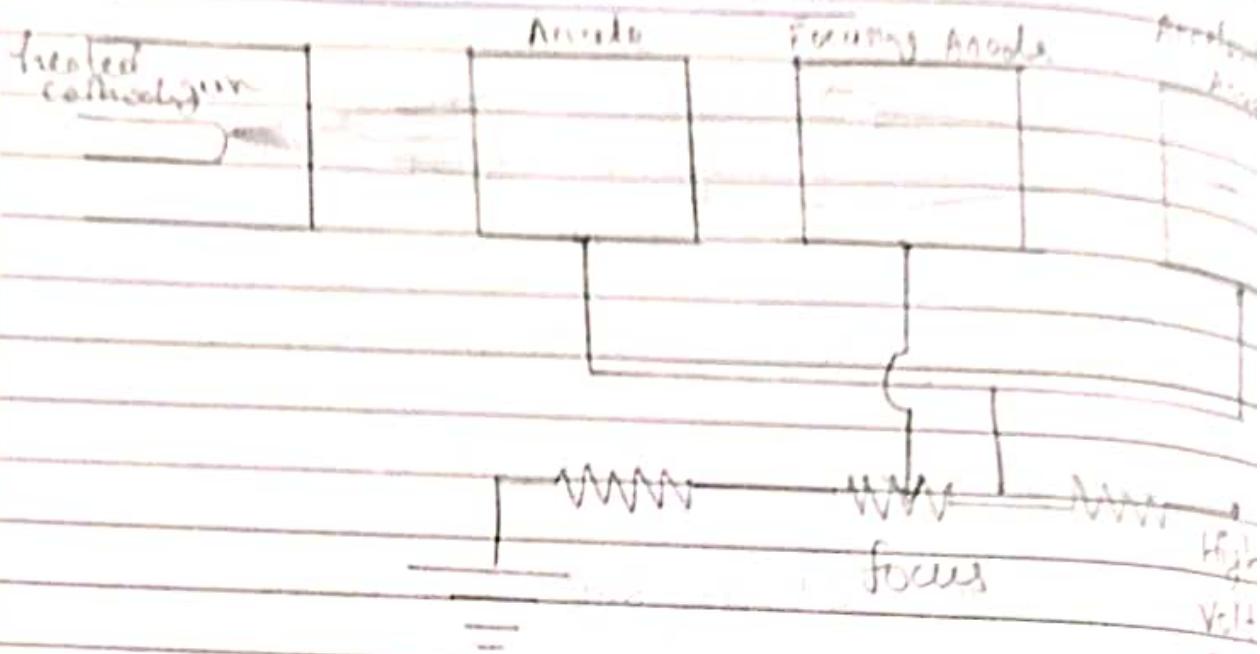
\* Ammeter/Voltmeter deflection  $\propto$  RMS

\* Oscilloscope : shape of waveform



## Cathode Ray Oscilloscope.

### Electron Beam Mechanism



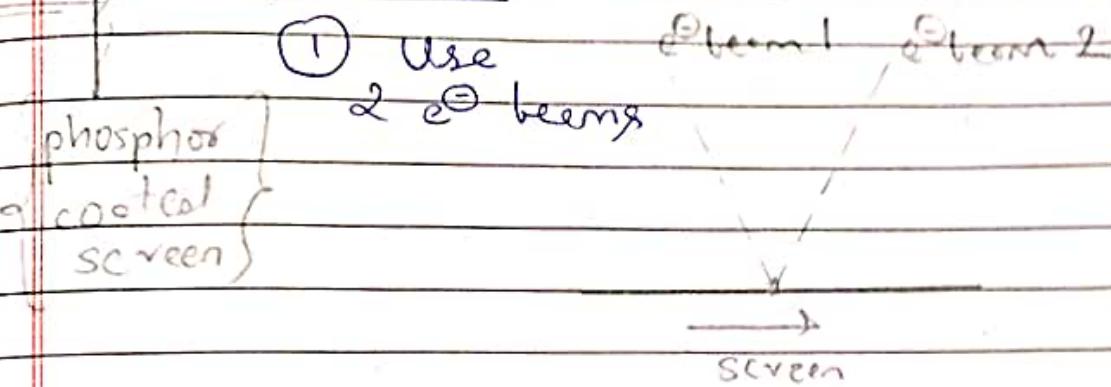
- The above 3 anode are hollow cylindrical structure
- Heated cathode emit the  $e^-$
- $e^-$  are first accelerated by pre-accelerating anode.
- focusing anode narrows down the  $e^-$  beam
- Electrostatic lens is formed
  - 1<sup>st</sup> lens aligns  $e^-(\delta)$ .
  - 2<sup>nd</sup> lens focus  $e^-(\delta)$ .

### Multiple Trace

- (Q) How to view 2 signals on the CRO screen simultaneously?



### Possibilities

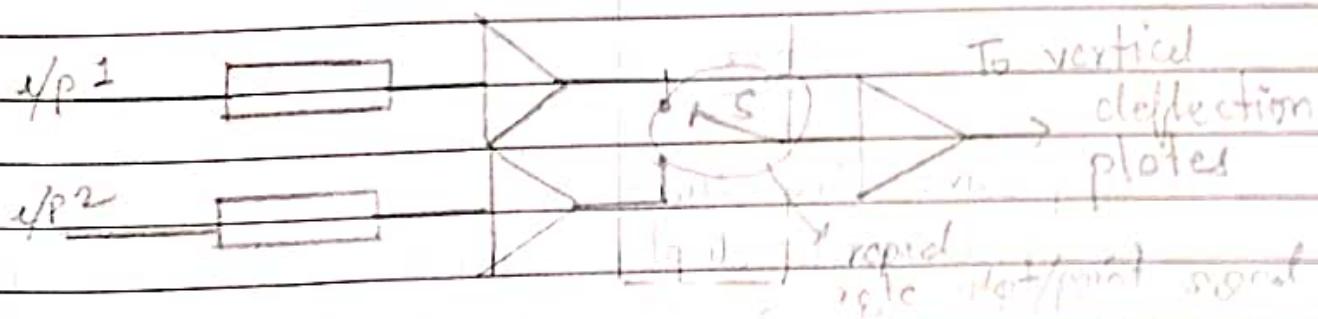


- each  $e^-$  beam would have its own set of components
- Dual beam CRO
- independent analysis of two signals
- costly
- larger size

② How to

### ② Using single $e^-$ beam

electronic switch



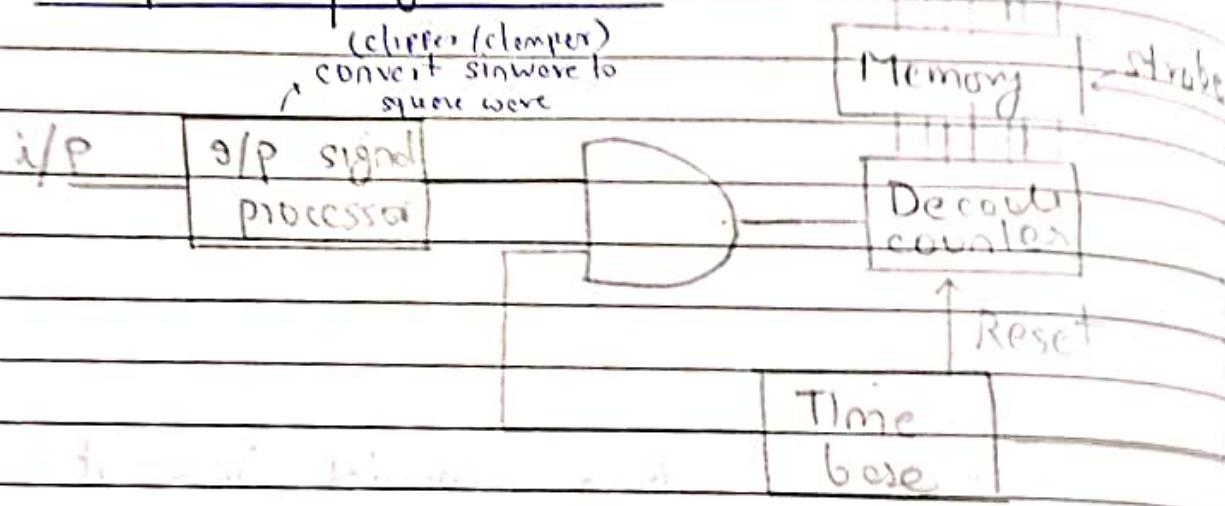
If signals are not multiples of each other's frequencies we cannot keep I/P1 out of the CRO box.

Drawback:

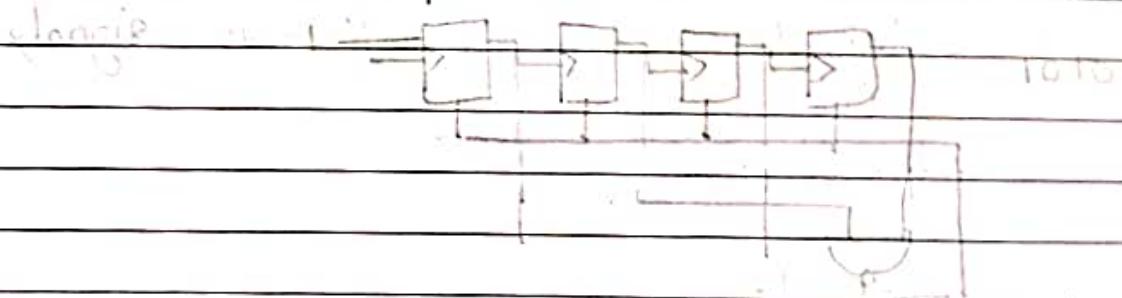
- non cyclic signals

Display

### Sample Frequency Counter



Decade counter → Asynchronous MOD = 10 counter



To determine frequency counter should give <sup>count</sup> pulses in 1 sec.

### Strain Gauge

- passive transducer
- mechanical displacement into change in resistance
- it is a thin wafer like device that can be attached or bonded to a variety of materials.

$R$ : Resistance of strain gauge

$\Delta R$ : change in resistance

$l$ : actual length

$\Delta l$ : change in length

$$k = \frac{\Delta R/R}{\Delta l/l} = \text{sensitivity}$$

$$\text{Strain } (\epsilon) = \frac{\Delta l}{l}$$

$$R = \frac{\rho l}{A} = \frac{\rho \times l}{\pi \times d^2 / 4} = \frac{4 \rho l}{\pi d^2}$$

where

$\rho$ : resistivity

$l$ : length

$A$ : area

$d$ : diameter

Now under stress

$$R_s = \rho \left( \frac{l + \Delta l}{(\pi/4) [d^2 - 2d\Delta d + (\Delta d)^2]} \right)$$

$$= \rho \cdot \frac{(l + \Delta l)}{d^2 (\pi/4) \left( 1 - \frac{2\Delta d}{d} \right)}$$

$$= \rho \cdot \frac{(l + \Delta l)}{d^2 (\pi/4) \left( 1 - \frac{2\mu d}{d} \right)}$$

$$\text{Poisson's ratio } \mu = \frac{\Delta d/d}{\Delta l/l}$$

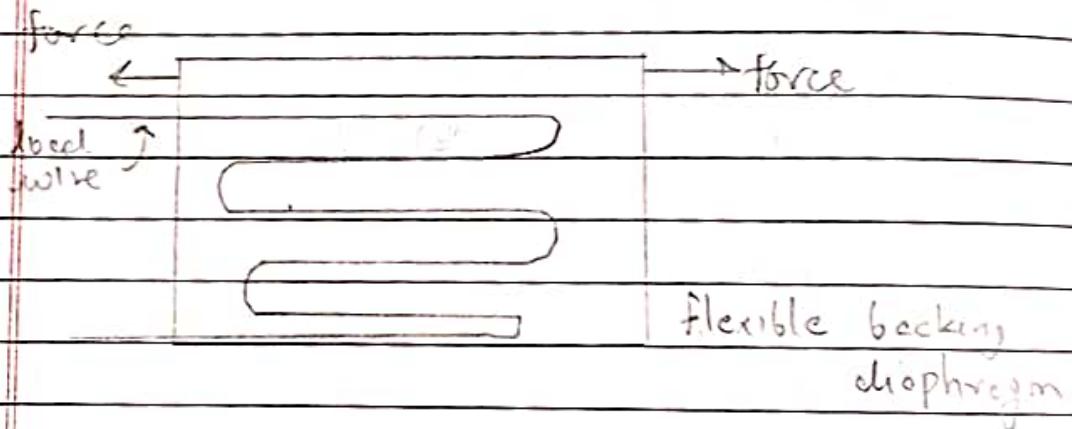
$$R_s = \frac{\rho l}{(\pi/4) d^2} \left[ \frac{1 + (\Delta l/l)}{1 + (1+2\mu) \frac{\Delta l}{l}} \right]$$

$$R_s = R + \Delta R$$

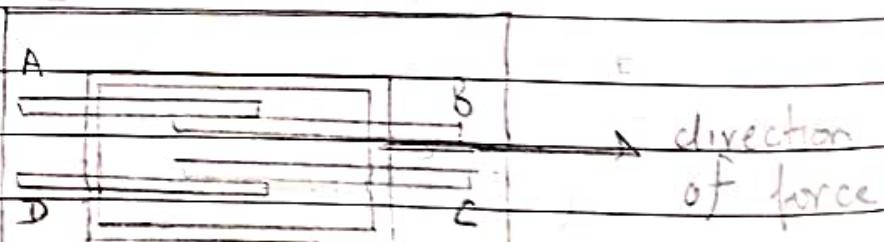
$$= R \left[ 1 + \frac{(2\mu)}{l} \Delta l \right]$$

$$k = \frac{\Delta R/R}{\Delta l/l} = 1 + 2\mu$$

### Bonded strain Gauge

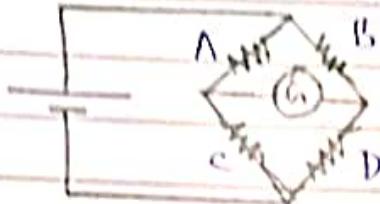


### Unbonded strain Gauge



marble armature stationary frame

$\Delta R$  can be measured using Wheatstone bridge



## Displacement Transducers

- Force  $\xrightarrow{\text{transducer}}$  displacement
- Pressure  $\xrightarrow{\text{transducer}}$  displacement

Once displacement is available, it can be measured using strain gauge.

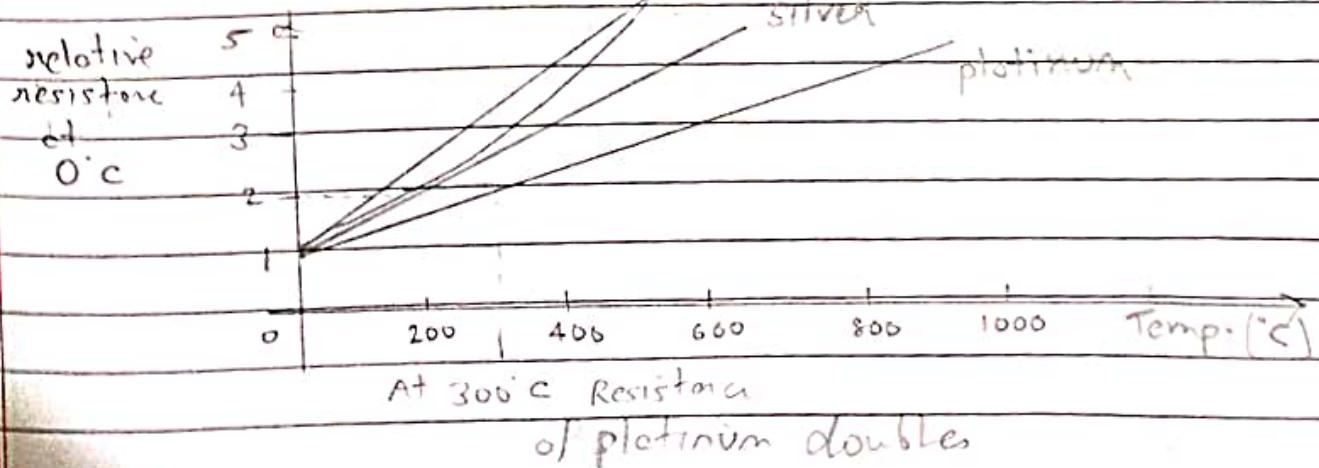
Chap 11  
Section

Assignment :-

Transducers

- 1) Capacitive
- 2) Inductive
- 3) LVDT
- 4) Oscillations
- 5) Piezoelectric
- 6) Potentiometric
- 7) Velocity

## Temperature Measurement



$$R_T = R_0 \left( 1 + \alpha \Delta T \right)$$

where

$R_T$  = resistance of conductor at temp  $T^{\circ}\text{C}$ .

$\alpha$  = temp coeff. of resistance

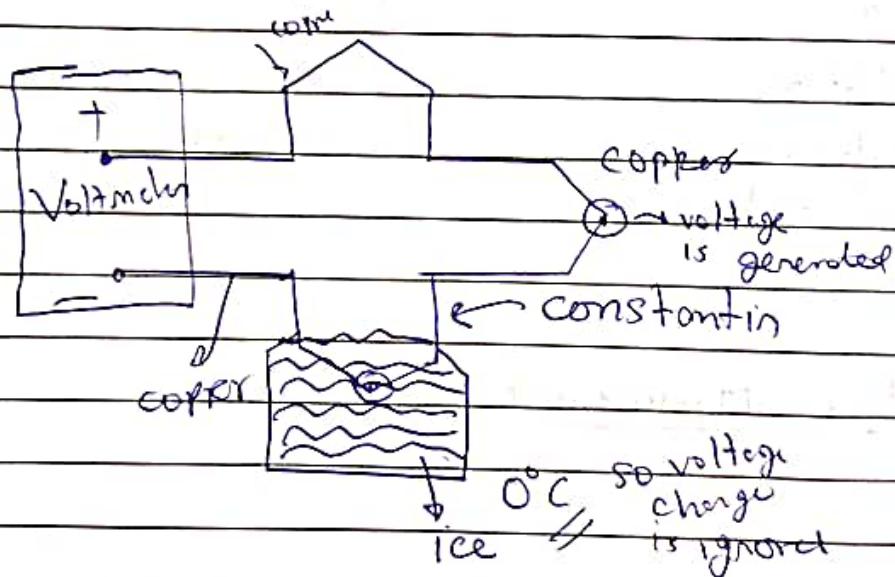
$R_{\text{ref}}$  = resistance at  $0^{\circ}\text{C}$ .

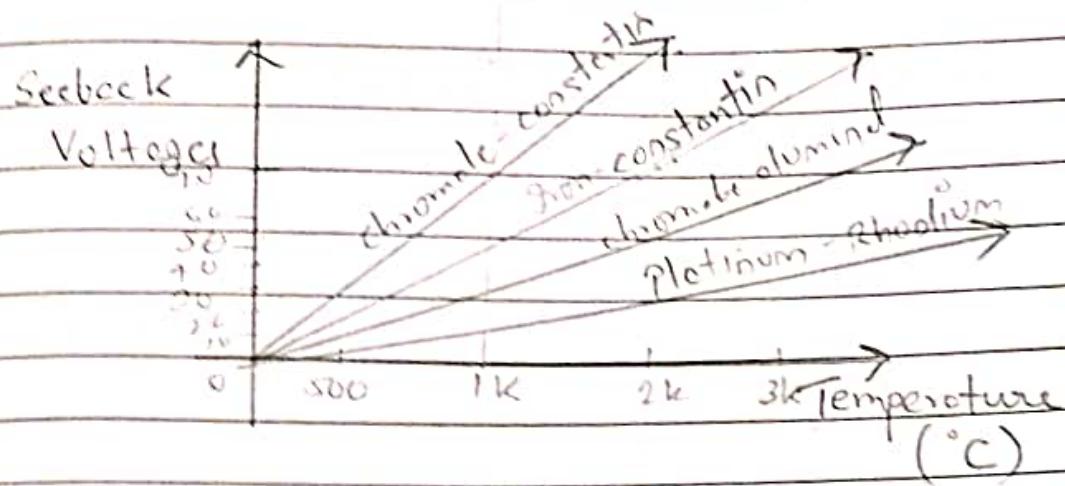
$$\Delta T = T^{\circ}\text{C} - T_{\text{ref}}$$

H.W: Read table 11.2 //

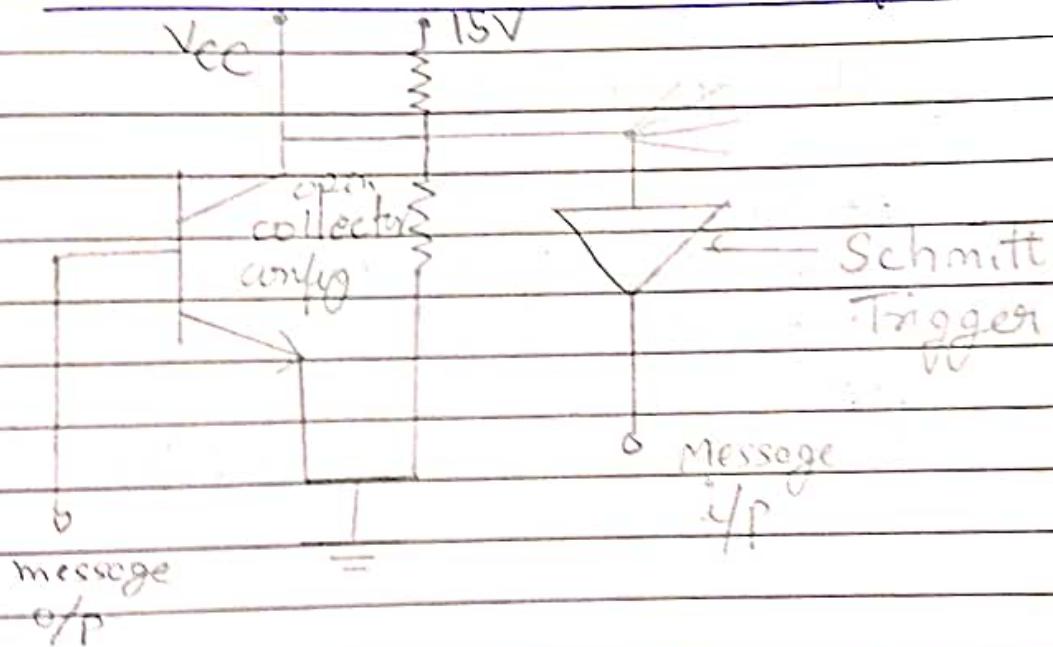
## Thermocouple

In 1821, Thomas Seebeck → discovered that when 2 dissimilar ~~method~~ metals are in contact a voltage is generated & the voltage is  $\propto$  temperature.



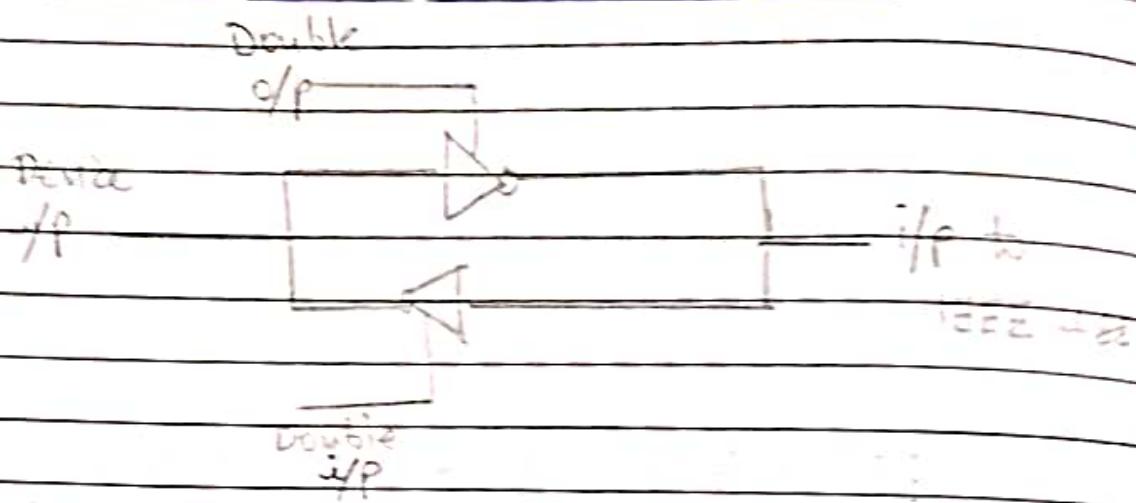


## IEEE 488 Electrical Interface



- Wireal communication for  $< 20 \text{ m}$ .
- logic '0'  $\rightarrow$  ~~approx~~  $< 0.8\text{V}$   
but driver should be less than  $< 0.5\text{V}$ .
- logic '1'  $\rightarrow$   $> 2.0\text{V}$  but driver should be  $> 2.4\text{V}$ .
- Noise margin =  $0.4$  for logic '1'  
 $= 0.3$  for logic '0'.

## Three State Bus Transceiver



## Cable requirements -

- ↳ conductor cables
  - ↳ & data lines
  - & power lines
  - ↳ remaining lines
- for other signals

Riley Textbook