CONTENTS

1

1

2

- 1 **Stability**
- 2 **Routh Hurwitz Criterion**
- 3 **Compensators**
- 4 2 **Nyquist Plot**

Abstract—This manual is an introduction to control systems based on GATE problems. Links to sample Python codes are available in the text.

Download python codes using

1 STABILITY

2 ROUTH HURWITZ CRITERION

2.1. **Question** In the feedback system given below

$$G(s) = \frac{1}{(s+1)(s+2)(s+3)}$$
 (2.1.1)

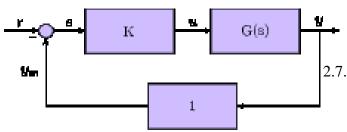
The positive value of k for which the gain margin of system is exactly 0 dB and phase margin of system is exactly 0 degree is?

Fig. 2.1

2.1

2.2. Theory

Gain Margin The gain margin is defined as the change in open-loop gain required to make the closed-loop system unstable. Systems with greater gain margins can withstand greater changes in system parameters before becoming unstable in closed-loop.



Phase Margin The phase margin is defined as the change in open-loop phase shift required to make the closed-loop system unstable. The phase margin also measures the system's tolerance to time delay

1

2.3. **Technique description** As given in question we see that gain margin is 0 dB and phase margin is 0 degrees. This implies that system is just enough stable and will become destabilized on just small increase in gain. Hence the system is marginbally stable.

The stability of the system can be checked by Routh-Hurwitz Stability Criterion

2.4. Routh Hurwitz Criterion Necessary condition for Routh-Hurwitz Stability Criterion: The necessary condition is that the coefficients of the characteristic polynomial should be positive. This implies that all the roots of the characteristic equation should have negative real parts.

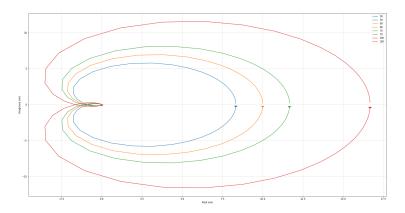
Sufficient condition for Routh-Hurwitz Stability Criterion: The sufficient condition is that all the elements of the first column of the Routh array should have the same sign. This means that all the elements of the first column of the Routh array should be either positive or negative.

2.5. The Routh array for characteristic equation

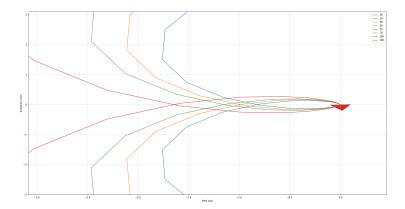
2.5. The Routh array for characteristic equation
$$a_0s^n + a_1s^{n-1} + a_2s^{n-2} + \dots + a_{n-1}s + a_n = 0$$

$$\begin{vmatrix} s^n & a_0 & a_2 & a_4 & \cdots \\ s^{n-1} & a_1 & a_3 & a_5 & \cdots \\ b_1 & b_2 & b_3 & \cdots \\ b_1 & b_2 & b_3 & \cdots \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ a_1c^1 & b_1c^2 &$$

2.7. Now since the system is marginally stable therefore s^1 row is ≥ 0 Hence $\frac{66-(6+K)}{6}$ Hence k=60



2.8. Verification using Plots



- 3 Compensators
- 4 Nyquist Plot