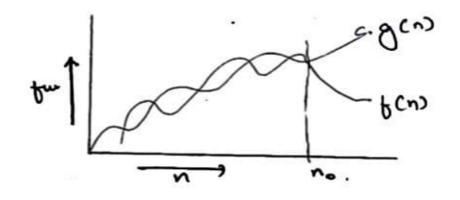
tssignment -1 are used to stell The notations that the comprenity of an algorithm when subre & very large i known at. asymtotic notation. havious types of asymbotic notation ore :-Big-OL (0):-\$ cw) = 0 (dcw) gen) is tight upper bound of f(u) = 0 (don)) f(n) <= c.g(n) + n>=no and c70.

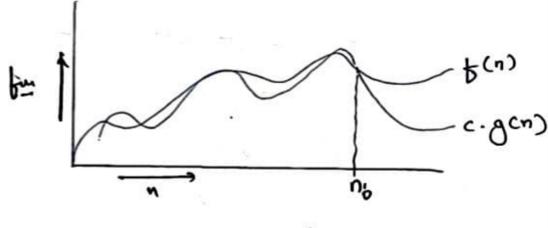
Big - Onega (SS) :f(n) = SL (g(n)) gens is 'tigut's lower bound of be fon) = 22 (gcm) iff. Theta (0):- It gives both upper flower be f(n) = & (g(cn)) O(q(n)) = f(n) .44. c1.8cm & fcw) & c5.8cm) + ages 1000 c1, c2 >0.0 man(n,, n2) > n

(ir) small - oh (o):
It gives du upper bound of tre't



f(n) = 0 (g(n)) iff. f(n) (eg(n) + n>no and c>0

(V) Small anega (ED) aka vho :
Tit gives the lower bound of the



fen) = co (devs)

f(n) > e.g(n) + n > no and c>0.

--- , n (k-tems).

$$T(n) = 3T(n-1) + n > 0. - 0$$
 $Pulting n = n-1 | m eq. (0).$
 $T(n-1) = 3T(n-2) - 0$
 $Pulting eq. (2) in (0).$
 $T(n) = 800 3 (3T(n-2))$
 $= 3^2 . T(n-2) - (3)$

pithing
$$n = n - 2$$
 on eq. (a) .
 $T(n-2) = 3T(n-3) - (a)$
putting eq. (a) on (a) .
 $T(n) = 3^3 T(n-3) - (5)$

a)
$$T(n) = 3^k T(n-1c)$$
 _ (6)

Base case

 $T(0) = 1$

a) $n - k = 0$
 $n = k$

pulting as as $k = n^{2}n = eq$ (6).

 $T(n) = 3^n T(n-n)$
 $= 3^n T(0)$
 $= 3^n$
 $T(n) = 0 (3^n)$
 $T(n) = 0 (3^n)$
 $T(n) = 2^n T(n-1) + 1 + n > 0$
 $T(n) = 2^n T(n-1) + 1 + n > 0$

putting $n = n - 1 = 2^n eq$ (6).

 $T(n-1) = 2^n T(n-2) - 1 = 3^n$

putting eq (3) in (1).

 $T(n) = 2 (2^n T(n-2) + 1) = 1$
 $= 2^n T(n-2) + 1 + 3 = 3$.

putting $n = n - 2 = 1 = eq$ (6).

 $T(n-2) = 2^n T(n-3) + 1 = 3^n$

putting eq (9) in eq (9).

 eq (1) eq (1)

 eq (2) eq (3)

 eq (1)

 eq (1)

 eq (2)

 eq (2)

 eq (3)

 eq (1)

 eq (1)

<u>Q4</u>

$$= 2^{k} T(n-k) - (1+2+2^{2}--+2^{k}).$$

$$= 2^{k} T(n) = 1$$

$$= 2^{n} T(n-n) - (1+2+2^{2}+---+2^{n})$$

$$= 2^{n} - (1+2+2^{2}+---+2^{n})$$

$$= 2^{n} - (2^{n}-1)$$

$$= 2^{n} (2^{n}-1)$$

$$= 2^{n} + 1 - 2^{n}$$

$$= (1+2+2^{n})$$

function (int n) { Pf (n==1) return; for (1=1 to m) ? for 4=1 +0 m) ? private ("*"); Z= Z fueton (n-3); T(n)=T(n-3)+n2-0. pulling n= n-3 is ear of T(n-3)=T(n-6)+(n-3)2 puty @· is eq O. T(n)=T(n-6)+(n++(n-3)2-3) putty n=n-6 is eq. 1. T(n-6)=T(n-9)+(n=6)2_ putly eq (9 is 3). T(n) = T(n-9) + n2+ (n-3)2+(n-6)2 =) T(n)= T(n-3k)+ n2+(n-3)2+ +(n + 3(k-1))2 T(1)= 0. $T(n) = n^2 + (n-3)^2 +$ =) $T(n) = n^3$

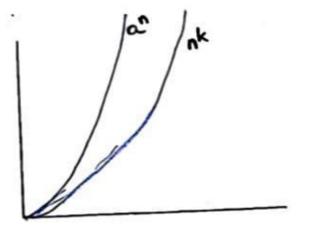
void furtion (but n) { for (i=1 ton) for (j-1; jen; jegti)

A= H(K+)C 1-1+1= K

$$\frac{2}{2}$$
 $\left(\frac{n-1}{2}+1\right)$

$$(n-1) \leq \frac{n}{i=1} 1 + \frac{1}{2} 1$$

(n-1). logn + n.



$$\Rightarrow n^k = O(a^n)$$

: nk (a".c + c>0 and n.>, no

no (c. 3 ". K= a= 3 (say) =) C7/1 (no)1.

$$0 = 0, 1, 2, 3, 4, 5 -+ k - k$$

$$0 = 0 + 1 + 2 - - - k.$$

$$0 = \frac{k(k-1)}{2}$$

```
013
 (i)
      yor (int 2:0; i <= n; ++i)
                                        O Culer
        tor (in j=1; j<=n; j*=2)
              print ( " * ");
((,,)
       Put a=1, b=23
       while Cac=n) {
             a*=b;
             b*=25
       ζ.
رتنع
       Mor ( 1=1 +0 m) 8
           for Els, 40 m) &
              for (x=1 40 w)?
                                       0( n3)
               3
           3
```

$$T(n) = T(n|u) + T(n|z) + en^{2}$$

$$T(n|u) + T(n|z) - 2cn^{2} (3u|z) = T(n|u) + C(n|u) - 2cn^{2} (3)$$

$$T(n|u) + T(n|u) + T(n|u) + C(n|u) - 2cn^{2} (3)$$

$$T(n|u) + T(n|u) + T(n|u) + C(n|u) + C(n$$

I'mt fur Cint u) { for eint (=1; 1'<=1,++1) } for (int 1:1; 1 < " : 40). = 7.4;) & T(n)= 2 2 2 (1) = $\frac{1}{2}$ $\frac{n-1}{L}$ = (n-1) (++++++--~) (n-1) (ogu =) T (n) · O (nlog n) for (int == 2; ? = n; i=pow(i, k)) { i= 2 2 2 2 2 2 2 2 3 =) T(n) = O(logleg(n)) log (n) = Kr log2 log (n)= k log(regin))= Klog K

If
$$T(n) = T(\frac{qq}{100}n) + 1/100$$
 $T(1) = 0$

puthy $n = \frac{qq}{100}n$ is ear. 0 .

 $T(qq/100^n) = T(\frac{qq}{100})^2 n + 1/100$
 $T(n) = T(\frac{qq}{100})^n + 1/100$
 $T(n) = T(\frac{qq}{qq})^n + 1/100$

100 (loglogn (dogn (Th <n <
n < 22 < 22 < 22 < 4 < n!) <n < 4 < n! 1 < doglog (n) & Trogen < dog en) < *(P)* 2n < 4n < 2(2n) < log(2N) < 2 log(n) of n logn = log(n!) < (c). $96 < \log_2(n) = \log_8(n) < n \log_6(n) = n \log_8(n) < 5n < 8n^2 < 7n < 8^{2n}$. INPUT ARRENZ, KEY; for (?= 0 to u-1) & if (ARR[i]=key) { return 8; rehum -1)

```
1 20 Thrashue Inchon Sont
      void Tureston Sort (Put enr 92, 12hn)
           Put i, temp, ii.
          for (2=1 to m) {
               temb = arr (1)
               (= 2-1)
                Duile Cisso AND arreiss surp) {
                      our []+1]= over(]);
                     · Ú=j-1;
                our [ ]+1] = temp;
       3.
     Recursive See Insertion Sort
       vold Turntion Sort Club exx [3, int n)
            il ( ~ < 2 )
              ream.
           TisentionSout (arr, n-1);
            last = arx(n-1), j=n-1;
             while (j>=0 And arr cj3 > tup &
                       are fiti] = over [i];
                       1-1-1:
             ar 6;+1] = last;
```

be cause it process, the elements
one son one is a sorial faculor
whome considering the frame clus
whose sort are there as they require
merge sort are there as they can process
all inputs on which they can process
the data for correct suffer i.e there
algorithms want all the imput beforehen

_				
021	AdorAhu	Best Case	Ang. Case	Worst Gx
22.1	Bubble Sort	O(n2)	0(42)	O(n2)
	Selection Sout	0 Cm)	ocors	0(~,)
7.44400	Discretion Sove	0 (m)	O (u2)	O(n2)
3	Merge Sort	O(ulogn)	O(nlega)	OCudago
3	Ourch Sove	OCulogn)	OC (cog m)	000
	Heats Sove	O (nlogn)	OCU (codu)	OCNLOS
		•	1	1
022	Algoritus	Iu-place	Stable	Oulie.
0	Bushle Sort	~	~	×
Ø	Selection Some	/	×	×
		1		
0	Merge Sort	>		×
(5)	Ower Sout	مر	×	"×
	Heap Sort		×	M
0				

Iterastre Brum scarre Eur Brasy Stearth (Eur arrez, it 1, intr, 20 بهديد (در عد) ع Put w=((+r)12.) if (our [m]=x) return w. else if (anclud(x) L= mai; else r= m-1; retom - 1; Removine Brany Scarel the Binary Server (It and), inte, but , int. if (r>1) ine w = (0+1)12; if (arr[m]: n) return w. else if (aso Cuz (n) return Blueny Search (arr, m+1, v, r); else return Binery Search (cor, 1, W-1,

Iteratur Shay South Time Comprening Bust Cerse = O(1) Average corre= Oldog n) Worst Care = O((ogn). Space Comprenity = OCI) Eccurate Briany Search Time Complemely Best Corre= O(1) Average (ever = O(logu) Worst Care > O (logu) Space comprency: Bust come = O(1) Aways Carr = O(log ~) Dovet care = O(logu) アイハー エイルノナレ I(") = O(Tool ")