

24/sep/17

Date: _____

Sr. No. _____

ECON

Assignment - 4

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pxk161130

Q.5.5a)

$$\begin{aligned} \text{Value} = & 28.4067 - 0.1834 \text{ Crime} \\ & - 22.8 \log \text{Nitex} + 6.3715 \text{ Rooms} \\ & - 0.0478 \text{ Age} - 1.3353 \text{ dist} \\ & + 0.2723 \text{ Access} - 0.0126 \text{ tax} \\ & - 1.1768 \text{ PT Ratio} \end{aligned}$$

Intercept $\rightarrow 28.4067$ when all other attributes are zero, the value of house will be \$28,406 which doesn't make any sense

Crime $\rightarrow -0.1834$

when all other things kept constant one unit increase in per capita ~~price~~ crime decreases the value of house by \$ 183.4

Nitex $\rightarrow -22.8 \log \rightarrow$ when all other things kept constant one ppm increase in concentration of Nitex decreases the value of house by \$ 22,810.

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Rooms $\rightarrow 6.3715 \rightarrow$ when all other things kept const one additional room in a dwelling will increase the value by \$6,371

Dist $\rightarrow -1.3353 \rightarrow$ when all things kept constant one unit increase in avg dist from employment center will reduce the price by \$1,335.

Age $\rightarrow -0.0478 \rightarrow$ When all other things kept const, one unit increase in proportion of owner-occupied units built prior to 1940 will decrease the value by \$47.8

Access $\rightarrow 0.2723 \rightarrow$ — // —
 — // — one additional unit in increase of ~~access~~ index of accessibility to radial highways will increase price by \$272.3

Tax $\rightarrow -0.0126 \rightarrow$ — // —
 one unit increase in full val. prop. tax rate per \$10,000 will decrease the value by \$12.6.

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Pratio $\rightarrow -1.1768 \rightarrow -10$
 one unit increase in pupil-teacher
 ratio by town will decrease
 the value by \$ 1,176.

b) P. Crime; $\beta_2 = -0.1833$

$$t(0.975, 497) = \pm 1.9647$$

$$\beta_2 = -0.1833 \pm 1.9647 \times 0.000$$

$$= \cancel{-2.1481} \text{ and } \cancel{-1.7813}$$

$$= \cancel{-0.1116} \text{ and } \cancel{-0.1116}$$

$$= -0.2551 \text{ and } -0.1116$$

Access $\beta_2 = 0.2723, 0.0723$

$$t_c = \pm 1.9647$$

$$= 0.1302 \text{ and } 0.4143$$

c) $\beta = 6.371, se = 0.3924$

$$t_{stat} = \frac{6.371 - 7}{0.3924}$$

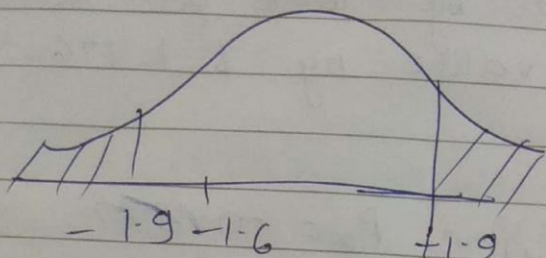
$$= -1.6029$$

$$H_0: \beta = 7$$

$$H_1: \beta \neq 7$$

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$$t_{\text{cri}} = \pm 1.9647$$



We fail to reject the null hyp that

increasing the no of rooms by one increases the value of house by \$7,000

d)

$$\checkmark H_0: \beta \geq -1$$

$$H_1: \beta < -1$$

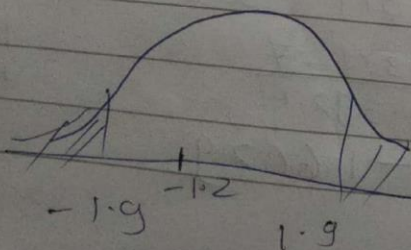
$$SE = 0.1394$$

$$\beta = -1.1768$$

$$t_{\text{stat}} = \frac{-1.1768 - (-1)}{0.1394}$$

$$= -1.2682$$

$$t_c = \pm 1.9647$$



We fail to reject the null hypothesis. Increasing PT ratio will not increase value by \$10,000

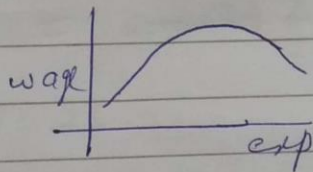
Q. 59

$$a) \quad \frac{\partial(\text{Wage})}{\partial(\text{Exper})} = \beta_3 + 2\beta_4 \text{ Exper}$$

b) $\beta_2 \rightarrow +ve \rightarrow$ more education
more wage

$\beta_3 \rightarrow +ve \rightarrow$ more experience, more wage

$\beta_4 \rightarrow -ve \rightarrow$ wages will start to decline after certain age as worker nears retirement



$$c) \quad \frac{\partial(\text{wage})}{\partial(\text{exper})} = \beta_3 + 2\beta_4 \text{ exper}$$

wages decline when

$$\beta_3 + 2\beta_4 \text{ exper} = 0$$

$$\text{exper} = \frac{-\beta_3}{2\beta_4}$$

A exp will start declining after it hits the maximum value

d) $Wage = \beta_1 + \beta_2 \text{Edu} + \beta_3 \text{Exp} + \beta_4 \text{Exp}^2$

i) $\frac{\partial(Wage)}{\partial(Edu)} = \beta_2 = 2.2774$

$N = 1000$

$t_c(0.975, 994) = \pm 1.9623$

$se = 0.1394$

95% CI = $2.274 \pm (1.9623 \times 0.1394)$
 $= (2.0004, 2.5475)$

ii) $c_{exp} = 4$

$\frac{\partial(Wage)}{\partial(Exp)} = \beta_3 + 2\beta_4 \text{Exp}$

$= \beta_3 + 2 \times 4 \beta_4$

$= \beta_3 + 8\beta_4$

CI = $(\beta_3 + 8\beta_4) \pm t_{crit} \times se(\beta_3 + 8\beta_4)$

$se(\beta_3 + 8\beta_4) = \sqrt{\text{var } \beta_3 + 8^2 \text{var } \beta_4 + 2 \times 8 \text{cov}(\beta_3, \beta_4)}$

$$= \sqrt{(0.1048)^2 + 64 \times (0.0019)^2 + 16(-0.000189)}$$

$$= 0.09045$$

95% CI

$$= -0.6821 + 8 \times 0.00$$

$$= 0.6821 - 8 \times 0.0101 \pm (1.9623 \times 0.09045)$$

$$= 0.4238 \pm 0.7789$$

Exp = 25

$$\text{iii)} (\beta_3 + 2 \times 25 \beta_1) \pm t_c \times Se$$

$$= 0.6821 + 50 \times 0.0101 \pm (1.9623 \times 0.09045)$$

$$Se = \sqrt{(0.1048)^2 + 50^2 (0.0019)^2 + 100(-0.000189)}$$

$$= 0.03329$$

$$= (0.6821 - 50 \times 0.0101) \pm (1.9623 \times 0.03329)$$

$$= 0.1117 \pm 0.2424$$

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5.12
a)

$\beta_2 \rightarrow$ negative
more the quantity, less
the price.

$\beta_3 \rightarrow +ve$
more the quality more
the price.

$\beta_4 \rightarrow$ positive or negative
~~the~~ trend could be +ve or
-ve depending on other
circumstances

b)

Intercept	90.8466	
quant	-0.0599	
qual	0.1162	\rightarrow pval not significant
trend	-2.354	

~~one gram~~

Holding all other things constant
 \rightarrow one gram increase in quantity
will decrease price by \$0.06 or 6
cents

\rightarrow one percent increase in quality will
increase price by \$0.116 or 11.6 cents

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→ one unit increase in trend will reduce price by \$2.35

Signs are as expected

$$c) R^2 = 0.509$$

$$Adj R^2 = 0.4814$$

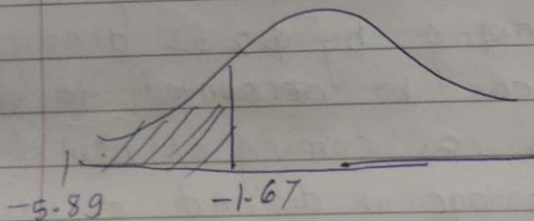
Roughly 48% variation in cocaine price is explained by quantity, quality, time

$$d) H_0: \beta_2 \geq 0$$

$$\checkmark H_1: \beta_2 < 0$$

$$t_{critical} = (t_{0.05, 52}) = -1.674$$

$$t_{stat} = -5.89 \rightarrow \text{from reg. output}$$

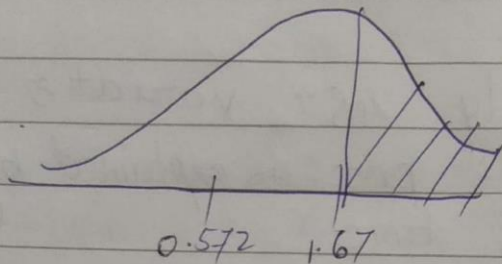


∴ we can reject the null hypothesis that ~~the~~ Higher the quantity higher the price

e) $H_0: \beta_3 = 0$
 $H_1: \beta_3 > 0$

$$t_c = -1.674$$

$$t_{stat} = 0.572$$



We fail to reject the null hypothesis
 that no premium is paid for the
 high ~~value~~ quality of cocaine

f) the parameter for trend is
 -2.354 so the price of cocaine
 is changing by \$2.35 annually.
 this can be accounted to various
 factors as coming of new drugs,
 or shortage in demand or excess
 in production or many other things

5.13

a) Intercept -41947
 sqft 90.90
 age -755.041

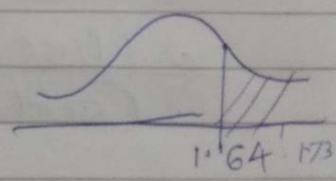
Keep all other thing const

- Intercept → price of house will be ~~at~~ \$-41947 with ~~not~~ zero sqft + age which don't make any sense
- sqft → every additional sqft will increase by \$ ~~90.90~~ 90.90
- Every one year addition in age will decrease price by \$755.

b)

~~85~~
 86.254 & 95.68
 → calculated using R

c) $H_0: \beta_3 \geq 1000$
 $H_1: \beta_3 < -1000$



$$t_{critical} = t(0.95, 1077) = \pm 1.6462$$

$$t_{stat} = \frac{-755 + 1000}{140.89} = \frac{245}{140.89} = 1.73$$

Signature 1.73

we fail to reject the null hypothesis that having a house a year older decreases price by 1000 or less

b)

$$\text{Price} = \beta_1 + \beta_2 \text{sqft} + \beta_3 \text{Age} + \beta_4 \text{sqft}^2 + \beta_5 \text{Age}^2$$

i)

$$\frac{\partial(\text{Price})}{\partial(\text{sqft})} = \beta_2 + 2\beta_4 \text{sqft}$$

$$\text{Max} = 7897$$

$$\text{Min} = 662$$

$$\beta_2 = -55.78$$

$$\beta_4 = 0.02315$$

$$\frac{\partial(\text{Price})}{\partial(\text{sqft})}_{\text{min}} = -55.78 + 0.02315 \times 662$$

$$= -25.1294$$

$$\frac{\partial(\text{Price})}{\partial(\text{sqft})}_{\text{max}} = 309.85$$

$$\frac{\partial(\text{Price})}{\partial(\text{sqft})}_{2300} = 50.71$$

for smaller house, change of sqft seems unrealistic but as size increases price also increases

$$ii) \frac{\partial(\text{Price})}{\partial(\text{Age})} = \underset{-2798}{\beta_3} + 2 \times \underset{30.16}{\beta_5} \text{ Age}$$

$$\text{Max Age} = 80 \quad \text{Min Age} = 1$$

$$\left. \frac{\partial(\text{Price})}{\partial(\text{Age})} \right|_{\text{Min}} = -2737.68$$

$$\left. \frac{\partial(\text{Price})}{\partial(\text{Age})} \right|_{\text{max}} = 2027.6$$

$$\left. \frac{\partial(\text{Price})}{\partial(\text{Age})} \right|_{80} = -1591.6$$

The values seems to be unrealistic the older the house, lesser should be the price

$$\text{soft} = 2300$$

$$\text{iii)} \quad t_c = 1.9621$$

$$s_e = \sqrt{40.82 + 2 \times (2300)^2 \times 0.0050 - 2 \times 2300 \times 2 \times 0.0050}$$

$$= 2.544$$

$$\text{C.I.} = \beta_2 + 2\beta_1 \pm t_c \times s_e$$

$$= \underline{\underline{5.5}}$$

$$= -55.78 + 2 \times 0.023 \times 2300 \\ \pm 1.9621 \times 2.544$$

$$= 45.718 \text{ \& } 55.70158$$

$$\text{iv)} \quad \frac{\partial(\text{Price})}{\partial(\text{Age})} = b_3 + 2b_5 \text{ Age} \\ \text{Age} = 20$$

$$s_e = \sqrt{9.309 \times 10^4 + 2^2 \times 20^2 \times 25.7155 \\ + 2 \times 2 \times 20 \times (-1.4345 \times 10^3)}$$

$$= 139.5521$$

$$H_0: \frac{\partial(\text{Price})}{\partial \text{Age}} \geq 1000$$

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$$H_1: \frac{\partial(\text{Price})}{\partial(\text{Age})} < -1000$$

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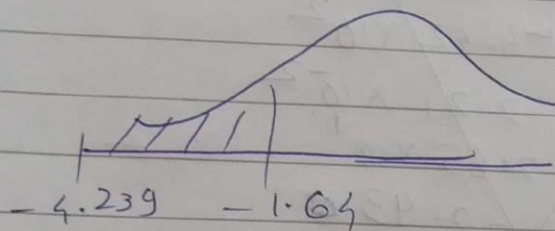
$$t_{\text{stat}} = \frac{(b_3 + 2b_5) - (-1000)}{SE}$$

$$= -2788$$

$$= \frac{-2788 + 40 \times 30.16 + 1000}{139.5521}$$

$$= -4.239$$

$$t_c = -1.64$$



We ~~reject~~ reject the null hypothesis that is for a 20 year old house, an extra year in ^{age} ~~price~~ decreases the price by is more than \$1000.

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$$c) \text{ Price} = 1.146 \times 10^5 - 3.073 \times 10^1 \text{ sqft} \\ - 4.42 \times 10^2 \text{ Age} + 2.21 \times 10^{-2} \text{ sqft}^2 \\ + 2.65 \times 10^1 \text{ Age}^2 - 9.3 \times 10^{-1} \text{ sqft} \times \text{Age}$$

$$i) \frac{\partial(\text{Price})}{\partial(\text{sqft})} = \beta_2 + 2 \times \beta_3 \text{ sqft} \\ + \beta_6 \text{ Age}$$

$$\text{Age} = 20, \text{ sqft} = 2300$$

~~$$\begin{aligned} \beta_2 &= -30.73 \\ \beta_3 &= -4.42 \times 10^{-2} \\ \beta_4 &= 2.21 \times 10^{-2} \\ \beta_5 &= 2.65 \times 10^1 \\ \beta_6 &= -0.93 \end{aligned}$$~~

~~$$\frac{\partial(\text{Price})}{\partial(\text{sqft})} =$$~~

$$\text{Age } 20, \text{ sqft} = 2300$$

$$\begin{aligned}
 \beta_2 &= -30.73 & \text{soft} \\
 \beta_3 &= -420442 & \text{Age} \\
 \beta_4 &= 2.218 \times 10^{-2} & \text{soft}^2 \\
 \beta_5 &= 26.52 & \text{Age}^2 \\
 \beta_6 &= -0.09306 & \text{soft} \times \text{age}
 \end{aligned}$$

$$\begin{aligned}
 \frac{\partial(\text{Price})}{\partial(\text{soft})} &= -30.73 + 2 \times 2.218 \times 10^{-2} \times 2300 \\
 &\quad - 0.09306 \times 20 \\
 &= 52.708
 \end{aligned}$$

$$\text{Age} = 20, \text{ Min soft} = 662$$

$$\frac{\partial(\text{Price})}{\partial(\text{soft})} = -19.975$$

$$\text{Age} = 20, \text{ biggest house} = 7897$$

$$\frac{\partial(\text{Price})}{\partial(\text{soft})} = 300.96$$

ii) effect of age & price

$$\frac{\partial(\text{Price})}{\partial(\text{Age})} = \beta_3 + 2\beta_5 \text{Age} + \beta_6 \text{seft}$$

$$\text{seft} = 2300 \quad \text{Age} = 1$$

$$\frac{\partial(\text{Price})}{\partial(\text{Age})} = -25,29.33$$

$$\text{Age} = 80, \text{seft} = 2300$$

$$\frac{\partial(\text{Price})}{\partial(\text{Age})} = 1660.82$$

$$\text{Age} = 20, \text{seft} = 2300$$
$$\frac{\partial(\text{Price})}{\partial(\text{Age})} = -1521.58$$

Newer the house less the price
Older the house more the price

iii) $\text{Sqft} = 2300, \text{Age} = 20$
 $t_c = t(0.95, 1074) = 1.962$

$$\frac{\frac{\partial(\text{Price})}{\partial(\text{sqft})}}{\frac{\partial(\text{Price})}{\partial(\text{sqft})}} + t_c \text{se}\left(\frac{\partial(\text{Price})}{\partial(\text{sqft})}\right)$$

from part i)

$$= 52.708 + (1.962 \times 2.4825)$$

$$= 57.84 \text{ \& } 57.58$$

iv) ~~$H_0: \beta_4 \neq 5$~~

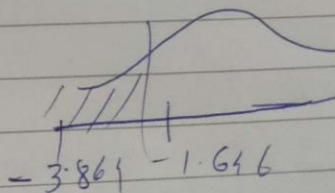
$$H_0: \beta_3 + 40\beta_5 + 2300\beta_6 \geq -1000$$

$$H_1: \beta_3 + 40\beta_5 + 2300\beta_6 \leq -1000$$

$$t_{\text{stat}} = \frac{b_3 + 40b_5 + 2300b_6 - (-1000)}{\text{se}(b_3 + 40b_5 + 2300b_6)}$$

$$t_{\text{stat}} = \frac{-5.21701}{13.60} = -3.846$$

$$t_c = -1.646$$



We reject the null hypothesis that for house 20 yr old price reduction is more than or equal to \$1000.

d) The linear model is not sufficient to fit the data. the addition of quadratic term $sqft^2 + age^2$ increases the model fit. the further addition of the ~~term~~ interaction term $age \times sqft$ increases the model fit. *

R version 3.2.5 (2016-04-14) -- "Very, Very Secure Dishes"
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Platform: x86_64-w64-mingw32/x64 (64-bit)

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'help.start()' for an HTML browser interface to help.
Type 'q()' to quit R.

```
> qt(0.975,497)
[1] 1.964749
> qt(c(-0.1834,.975), df = 467)
[1]      NaN 1.965057
Warning message:
In qt(c(-0.1834, 0.975), df = 467) : NaNs produced
> a <- qt(0.975,497)
> -.1834+a
[1] 1.781349
> -.1834 - a
[1] -2.148149
> -.1834+ (a*0.0365)
[1] -0.1116867
> -.1834 - (a*0.0365)
[1] -0.2551133
> .2723 + (a*0.0723)
[1] 0.4143513
> .2723 - (a*0.0723)
[1] 0.1302487
> .2723 +- (a*0.0723)
[1] 0.1302487
> a <- qt(0.975,994)
> a
[1] 1.962353
> sqrt((.1048^2))
[1] 0.1048
> sqrt((.1048^2)+(64*.0019^2)+(16*-0.000189))
[1] 0.09049906
> 0.6821-(8*0.0101)+(1.9623*0.09045)
[1] 0.77879
> 0.6821-(8*0.0101)-(1.9623*0.09045)
[1] 0.42381
> 0.6821-(50*0.0101)-(1.9623*0.09045)
[1] -0.000390035
> sqrt((.1048^2)+(50^2*.0019^2)+(50*-0.000189))
[1] 0.1027523
> sqrt((.1048^2)+(50^2*.0019^2)+(100*-0.000189))
[1] 0.03328723
> 0.6821-(50*0.0101)+(1.9623*0.03329)
[1] 0.242425
> 0.6821-(50*0.0101)-(1.9623*0.03329)
[1] 0.111775
> sqrt((.1048^2)+(50^2*.0019^2)+(100*-0.000189))
[1] 0.03347566
> 0.6821-(8*.0101)+(1.96*23*.09045)
[1] 4.678786
```

```

> 0.6821-(8*.0101)+(1.9623*.09045)
[1] 0.77879
> 0.6821-(8*.0101)-(1.9623*.09045)
[1] 0.42381
> sqrt((.1048^2)+(50^2*.0019^2)+(100*-0.000189))
[1] 0.03328723
> sqrt((.1048^2)+(50^2*.0019^2)+(100*-0.000189259))
[1] 0.0328959
> sqrt((.1048^2)+(50^2*.0019^2)-(100*+0.000189259))
[1] 0.0328959
> 06821-(50*.0101)
[1] 6820.495
> 0.6821-(50*.0101)
[1] 0.1771
> .1771+(1.9623*.03329)
[1] 0.242425
> .1771-(1.9623*.03329)
[1] 0.111775
> library(haven)
> cocaine <- read_dta("D:/Class Notes/Fall 17 Classes/ECON/Data_sets/cocaine.dta")
> View(cocaine)
> model <- lm(price ~ quant qual trend, data = cocaine)
Error: unexpected symbol in "model <- lm(price ~ quant qual"
> model <- lm(price ~ quant +qual+ trend, data = cocaine)
> summary(model)

```

Call:

```
lm(formula = price ~ quant + qual + trend, data = cocaine)
```

Residuals:

Min	1Q	Median	3Q	Max
-43.479	-12.014	-3.743	13.969	43.753

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	90.84669	8.58025	10.588	1.39e-14 ***
quant	-0.05997	0.01018	-5.892	2.85e-07 ***
qual	0.11621	0.20326	0.572	0.5700
trend	-2.35458	1.38612	-1.699	0.0954 .

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 20.06 on 52 degrees of freedom

Multiple R-squared: 0.5097, Adjusted R-squared: 0.4814

F-statistic: 18.02 on 3 and 52 DF, p-value: 3.806e-08

```

> qt(0.05,52)
[1] -1.674689
> library(haven)
> br2 <- read_dta("D:/Class Notes/Fall 17 Classes/ECON/Data_sets/br2.dta")
> View(br2)
> model <- lm(price ~ sqft + age, data = br2)
> summary(model)

```

Call:

```
lm(formula = price ~ sqft + age, data = br2)
```

Residuals:

Min	1Q	Median	3Q	Max
-358116	-33259	-6111	27242	936754

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	-41947.696	6989.636	-6.001	2.67e-09 ***


```
sqft      90.970      2.403  37.855 < 2e-16 ***
age     -755.041    140.894  -5.359 1.02e-07 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 78810 on 1077 degrees of freedom
Multiple R-squared:  0.5896, Adjusted R-squared:  0.5888
F-statistic: 773.6 on 2 and 1077 DF, p-value: < 2.2e-16
```

```
> confint(model, sqft, level=0.95)
Error in confint.lm(model, sqft, level = 95) : object 'sqft' not found
> confint(model, 'sqft', level=0.95)
      -4700 % 4800 %
sqft      NaN      NaN
Warning message:
In qt(a, object$df.residual) : NaNs produced
> confint(model, 'sqft', level=0.95)
      2.5 % 97.5 %
sqft 86.25451 95.68509
> qt(.95,1077)
[1] 1.64627
> -755-1000
[1] -1755
> -17755/140.89
[1] -126.0203
> 1755/140.89
[1] 12.45653
> 1000-755
[1] 245
> 245/140.89
[1] 1.738945
```

```
> model <- lm(price ~ sqft + age + I(sqft*sqft) + I(age*age), data = br2)
> summary(model)
```

```
Call:
lm(formula = price ~ sqft + age + I(sqft * sqft) + I(age * age),
    data = br2)
```

```
Residuals:
    Min       1Q   Median       3Q      Max
-805011 -23873  -1375   18067  659703
```

```
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)  1.701e+05  1.043e+04  16.310 < 2e-16 ***
sqft        -5.578e+01  6.389e+00  -8.731 < 2e-16 ***
age         -2.798e+03  3.051e+02  -9.170 < 2e-16 ***
I(sqft * sqft)  2.315e-02  9.642e-04  24.013 < 2e-16 ***
I(age * age)   3.016e+01  5.071e+00   5.948 3.68e-09 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 63370 on 1075 degrees of freedom
Multiple R-squared:  0.7352, Adjusted R-squared:  0.7342
F-statistic: 746 on 4 and 1075 DF, p-value: < 2.2e-16
```

```
> .02315-55.78
[1] -55.75685
> 2*.02315
[1] 0.0463
> -55.78
[1] -55.78
> 0.0463-.5578
```

```

[1] -0.5115
> max(br2$sqft)
[1] 7897
> min(br2$sqft)
[1] 662
> (.02315*662)-55.78
[1] -40.4547
> (.02315**2662)-55.78
[1] -55.78
> (.02315**2*662)-55.78
[1] -55.42522
> (.02315*2*662)-55.78
[1] -25.1294
> (.02315*2*7897)-55.78
[1] 309.8511
> (.02315*2*2300)-55.78
[1] 50.71
> max(br2$age)
[1] 80
> min(br2$age)
[1] 1
> (2*30.16)-2798
[1] -2737.68
> (2*30.16*80)-2798
[1] 2027.6
> (2*30.16-2798
+ min(br2$age)
Error: unexpected symbol in:
"(2*30.16-2798
min"
> (2*30.16)-2798
[1] -2737.68
> (2*30.16*20)-2798
[1] -1591.6
> qc(.972,1075)
Error: could not find function "qc"
> qt(.972,1075)
[1] 1.913105
> qt(.975,1075)
[1] 1.962173
> vcov(model)

```

	(Intercept)	sqft	age	I(sqft * sqft)	I(age * age)
(Intercept)	1.088320e+08	-6.110570e+04	-1.340396e+06	8.152671e+00	1.601762e+04
sqft	-6.110570e+04	4.082499e+01	3.205761e+02	-5.870334e-03	-3.547411e+00
age	-1.340396e+06	3.205761e+02	9.309548e+04	-3.955193e-02	-1.434561e+03
I(sqft * sqft)	8.152671e+00	-5.870334e-03	-3.955193e-02	9.296015e-07	4.459434e-04
I(age * age)	1.601762e+04	-3.547411e+00	-1.434561e+03	4.459434e-04	2.571554e+01

```

> 23*10^2
[1] 2300
> 23*10^-2
[1] 0.23
> sqrt(40.82+((4600^2)*(9.29*10^-7)))+(2*2300*2*5.87*10^-3))
[1] 10.69961
> sqrt(40.82+((4600^2)*(9.29*10^-7)))-(2*2300*2*5.87*10^-3))
[1] 2.544335
> -55.78+(2*.023*2300)+(1.9621*2.544)
[1] 55.01158
> -55.78+(2*.023*2300)-(1.9621*2.544)
[1] 45.02842
> -55.78+(2*.02315*2300)-(1.9621*2.544)
[1] 45.71842
> -55.78+(2*.02315*2300)+(1.9621*2.544)
[1] 55.70158
> sqrt((9.309*10^4)+(4*400*25.7155)-(80*1.4345*10^3))
[1] 139.5521
> ((40*30.16)+1000-2798)/139.5521
[1] -4.239277
> qt(.95,1075)
[1] 1.646272
> model <- lm(price ~ sqft+ age + I(sqft * sqft) + I(age * age) + I(sqft * age), data= br2)
> summary(model)

```

```
Call:
lm(formula = price ~ sqft + age + I(sqft * sqft) + I(age * age) +
    I(sqft * age), data = br2)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-796617	-21537	-439	17825	623609

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	1.146e+05	1.214e+04	9.437	< 2e-16	***
sqft	-3.073e+01	6.898e+00	-4.455	9.27e-06	***
age	-4.420e+02	4.106e+02	-1.077	0.282	
I(sqft * sqft)	2.218e-02	9.425e-04	23.537	< 2e-16	***
I(age * age)	2.652e+01	4.939e+00	5.370	9.66e-08	***
I(sqft * age)	-9.306e-01	1.124e-01	-8.277	3.72e-16	***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 61470 on 1074 degrees of freedom
Multiple R-squared: 0.751, Adjusted R-squared: 0.7499
F-statistic: 648 on 5 and 1074 DF, p-value: < 2.2e-16

```
> -30.73+(2*2.218*10^-2*2300)-(.09306*20)
```

```
[1] 69.4368
```

```
> -30.73+(2*0.02218**2300)-(.09306*20)
```

```
[1] -32.5912
```

```
> -30.73+(2*0.02218*2300)-(.09306*20)
```

```
[1] 69.4368
```

```
> -30.73+(2*0.02218*662)-(.09306*20)
```

```
[1] -3.22488
```

```
> -30.73+(2*0.02218*662)-(.9306*20)
```

```
[1] -19.97568
```

```
> -30.73+(2*0.02218*2300)-(.9306*20)
```

```
[1] 52.686
```

```
> -30.73+(2*0.02218*662)-(.9306*20)
```

```
[1] -19.97568
```

```
> -30.73+(2*0.02218*7897)-(.9306*20)
```

```
[1] 300.9689
```

```
> -420+(2*26.52*1)-(0.9306*2300)
```

```
[1] -2507.34
```

```
> -442+(2*26.52*1)-(0.9306*2300)
```

```
[1] -2529.34
```

```
> -442+(2*26.52*80)-(0.9306*2300)
```

```
[1] 1660.82
```

```
> -442+(2*26.52*20)-(0.9306*2300)
```

```
[1] -1521.58
```

```
> vcov(model)
```

	(Intercept)	sqft	age	I(sqft * sqft)	I(age * age)	I(sqft * age)
(Intercept)	1.474488e+08	-7.781252e+04	-3.171479e+06	8.456068e+00	1.802396e+04	7.546407
sqft	-7.781252e+04	4.757635e+01	1.163214e+03	-5.877578e-03	-4.669568e+00	-3.403597
age	-3.171479e+06	1.163214e+03	1.686025e+05	-7.050846e-02	-1.475013e+03	-3.200138
I(sqft * sqft)	8.456068e+00	-5.877578e-03	-7.050846e-02	8.883579e-07	4.710565e-04	1.315232
I(age * age)	1.802396e+04	-4.669568e+00	-1.475013e+03	4.710565e-04	2.438964e+01	4.946518
I(sqft * age)	7.546407e+02	-3.403597e-01	-3.200138e+01	1.315232e-05	4.946518e-02	1.264187

```
>
```