

FAST EXPONENTIATION

(ITERATIVE) (BINARY EXPONENTIATION)

B times
(ans $\leftarrow A$)

$5^{117} \bmod 19$

$1110101 \rightarrow$

$5^{(2^0 + 2^2 + 2^4 + 2^5 + 2^6)}$

$5^{2^0} \cdot 5^{2^2} \cdot 5^{2^4} \cdot 5^{2^5} \cdot 5^{2^6}$

$5^1 \cdot 5^4 \cdot 5^{16} \cdot 5^{32} \cdot 5^{64}$

$(2^k)^2 = 2^{2k}$

$2^k \cdot 2^k = 2^{2k}$

$A^B \bmod C$

A^{2^k}

$A^{2^0} \cdot A^{2^1} \cdot \dots \cdot A^{2^k}$

$2^k \leq B$

$k \leq \log_2 B$

$5^{117} \bmod 19$

$1110101 \rightarrow$

$5^{(2^0 + 2^2 + 2^4 + 2^5 + 2^6)}$

$5^{2^0} \cdot 5^{2^2} \cdot 5^{2^4} \cdot 5^{2^5} \cdot 5^{2^6}$

$2^{2^k} \rightarrow 2^{2^{k+1}}$

$\log_2 B$

0
2
4
6
3

hreeRam! | @csalgo

```

#include <iostream>

using namespace std;

int fastexpo(int a, int b, int mod)
{
    int ans = 1;
    while (b)
    {
        if (b % 2 == 1) // 1011 this is binary form eg then this is used to check whether the last bit is zero or 1 if 1 it means to multiply the ans with a
        {
            ans = (1LL * ans * a % mod);
        }
        a = 1LL * a * a % mod; //eg 1001 means 2^0*2^3 only
        b = b / 2; //divide each time to go to next bit it can be done using bit manipulation
    }
    return ans;
}

int main()
{
    int a, b;
    cin >> a >> b;
    cout << fastexpo(a, b, 1e9 + 7) << "\n";
    //calculating mod inverse
    cout << fastexpo(a, 1e9 + 7 - 2, 1e9 + 7); //a^(p-2) by little theorem
}

```