

## ***Solution***      ***Section 1.1 - Linear Equations and Rational Equations***

### ***Exercise***

Solve:       $5x - 8 = 72$

### **Solution**

$$5x - 8 + 8 = 72 + 8$$

$$5x = 80$$

$$\underline{x = 16}$$

### ***Exercise***

Solve:       $14 - 5x = -41$

### **Solution**

$$14 - 5x = -41$$

$$5x = 14 + 41$$

$$5x = 55$$

$$\underline{x = 11}$$

### ***Exercise***

Solve:       $2x + 6 = 3x - 2$

### **Solution**

$$2x + 6 - 3x - 6 = 3x - 2 - 3x - 6$$

$$-x = -8$$

$$\underline{x = 8}$$

### ***Exercise***

Solve:       $11x - (6x - 5) = 40$

### **Solution**

$$11x - 6x + 5 = 40$$

$$5x + 5 - 5 = 40 - 5$$

$$5x = 35$$

$$\underline{x = 7}$$

### ***Exercise***

Solve:  $9x + 11 = 7x + 1$

#### **Solution**

$$9x + 11 - 7x - 11 = 7x + 1 - 7x - 11$$

$$2x = -10$$

$$\underline{x = -5}$$

### ***Exercise***

Solve:  $2x - 7 = 6 + x$

#### **Solution**

$$2x - 7 - x + 7 = 6 + x - x + 7$$

$$\underline{x = 13}$$

### ***Exercise***

Solve:  $5x - 2 = 9x + 2$

#### **Solution**

$$5x - 2 - 9x + 2 = 9x + 2 - 9x + 2$$

$$-4x = 4$$

$$\underline{x = -1}$$

### ***Exercise***

Solve:  $3(x - 2) + 7 = 2(x + 5)$

#### **Solution**

$$3x - 6 + 7 = 2x + 10$$

$$3x = 9$$

$$\underline{x = 3}$$

### ***Exercise***

Solve:  $3x + 5 - 5(x + 1) = 6x + 7$

#### **Solution**

$$3x + 5 - 5x - 5 = 6x + 7$$

$$-8x = 7$$

$$\underline{x = -\frac{7}{8}}$$

### ***Exercise***

Solve:  $4(-2x + 1) = 6 - (2x - 4)$

#### **Solution**

$$-8x + 4 = 6 - 2x + 4$$

$$-6x = 6$$

$$\underline{x = -1}$$

### ***Exercise***

Solve:  $4(x + 7) = 2(x + 12) + 2(x + 1)$

#### **Solution**

$$4x + 28 = 2x + 24 + 2x + 2$$

$$4x - 4x = 26 - 28$$

$$0 = -2 \times$$

***No solution***

### ***Exercise***

Solve:  $6(3x - 1) = 8 - 10(10x - 14)$

#### **Solution**

$$18x - 6 = 8 - 100x + 140$$

$$118x = 154$$

$$x = \frac{154}{118}$$

$$\underline{= \frac{77}{59}}$$

### ***Exercise***

Solve:  $5x - (2x - 8) = 35$

#### **Solution**

$$5x - 2x + 8 = 35$$

$$3x = 27$$

$$\underline{x = 9}$$

### ***Exercise***

Solve:  $\frac{1}{14}(3x-2) = \frac{x+10}{10}$

### **Solution**

$$\frac{1}{14}(3x-2) = \frac{x+10}{10}$$

$$(70)\frac{1}{14}(3x-2) = (70)\frac{x+10}{10}$$

$$5(3x-2) = 7(x+10)$$

$$15x-10 = 7x+70$$

$$15x-7x = 10+70$$

$$8x = 80$$

$$\underline{x = 10}$$

### ***Exercise***

Solve:  $\frac{5}{6}x - 2x + \frac{4}{3} = \frac{5}{3}$

### **Solution**

$$6 \times \frac{5}{6}x - 2x + \frac{4}{3} = \frac{5}{3}$$

$$5x - 12x + 8 = 10$$

$$-7x = 2$$

$$\underline{x = -\frac{2}{7}}$$

### ***Exercise***

Solve:  $\frac{7}{4} + \frac{1}{5}x - \frac{3}{2} = \frac{4}{5}x$

### **Solution**

$$20 \times \frac{7}{4} + \frac{1}{5}x - \frac{3}{2} = \frac{4}{5}x$$

$$35 + 4x - 30 = 4x$$

$$5 = 4x$$

$$\underline{x = \frac{5}{4}}$$

### ***Exercise***

Solve:  $5(x+3)+4x-3=-(2x-4)+2$

#### **Solution**

$$5x+15+4x-3=-2x+4+2$$

$$9x+12=-2x+6$$

$$9x+12+2x-12=-2x+6+2x-12$$

$$11x=-6$$

$$\underline{x = -\frac{6}{11}}$$

### ***Exercise***

Solve:  $2[x-(4+2x)+3]=2x+3$

#### **Solution**

$$2x-2(4+2x)+6=2x+3$$

$$2x-8-4x+6=2x+3$$

$$-2x-2=2x+3$$

$$-2x-2-2x+2=2x+3-2x+2$$

$$-4x=5$$

$$\underline{x = -\frac{5}{4}}$$

### ***Exercise***

Solve:  $2x-\{x-[3x-(8x+6)]\}=2x-2$

#### **Solution**

$$2x-x+[3x-(8x+6)]=2x-2$$

$$2x-x+3x-(8x+6)=2x-2$$

$$2x-x+3x-8x-6=2x-2$$

$$-4x-6=2x-2$$

$$-4x-2x-6+6=2x-2x-2+6$$

$$-6x=4$$

$$x = \frac{4}{-6}$$

$$\underline{= -\frac{2}{3}}$$

*Distribute the minus*

*Distribute the plus*

*Distribute the minus*

*Divide by -6*

### ***Exercise***

Solve:  $4(2x + 7) = 2x + 22 + 3(2x + 3)$

#### **Solution**

$$8x + 28 = 2x + 22 + 6x + 9$$

$$8x + 28 = 8x + 31$$

$$8x + 28 - 8x = 8x + 31 - 8x$$

$$28 = 31 \quad \text{False statement}$$

***No Solution***

### ***Exercise***

Solve:  $4[2x - (3 - x) + 5] = -7x - 2$

#### **Solution**

$$8x - 4(3 - x) + 20 = -7x - 2$$

$$8x - 12 + 4x + 20 = -7x - 2$$

$$12x - 8 = -7x - 2$$

$$12x - 8 + 7x + 8 = -7x - 2 + 7x + 8$$

$$19x = 6$$

$$\underline{x = \frac{6}{19}}$$

### ***Exercise***

Solve:  $3[2x - (4 - x) + 5] = 7x - 2$

#### **Solution**

$$6x - 3(4 - x) + 15 = 7x - 2$$

$$6x - 12 + 3x + 15 = 7x - 2$$

$$9x + 3 = 7x - 2$$

$$2x = -5$$

$$\underline{x = -\frac{5}{2}}$$

### ***Exercise***

Solve:  $-4(2x - 6) + 8x = 5x + 24 + x$

#### **Solution**

$$-8x + 24 + 8x = 5x + 24 + x$$

$$6x = 0$$

$$\underline{x = 0}$$

### ***Exercise***

Solve:  $-8(3x + 4) + 6x = 4(x - 8) + 4x$

#### **Solution**

$$-24x - 32 + 6x = 4x - 32 + 4x$$

$$-18x = 8x$$

$$26x = 0$$

$$\underline{x = 0}$$

### ***Exercise***

Solve:  $4(x + 7) = 2(x + 12) + 2(x + 1)$

#### **Solution**

$$4x + 28 = 2x + 24 + 2x + 2$$

$$4x + 28 = 4x + 26$$

$$4x - 4x = 26 - 28$$

$$0 = -2 \quad (\text{False})$$

$$\text{Solution: } \{\emptyset\}$$

### ***Exercise***

Solve:  $-6(2x + 1) - 3(x - 4) = -15x + 1$

#### **Solution**

$$-12x - 6 - 3x + 12 = -15x + 1$$

$$-15x + 6 = -15x + 1$$

$$6 = 1 \quad \text{False statement}$$

***No Solution***

### ***Exercise***

Solve:  $2(x - 1) + 3 = x - 3(x + 1)$

#### **Solution**

$$2x - 2 + 3 = x - 3x - 3$$

$$2x + 1 = -2x - 3$$

$$4x = -4$$

$$\underline{x = -1}$$

### ***Exercise***

$$\text{Solve: } 3(x-4) - 4(x-3) = x+3 - (x-2)$$

### **Solution**

$$3x - 12 - 4x + 12 = x + 3 - x + 2$$

$$-x = 5$$

$$\underline{x = -5}$$

### ***Exercise***

$$\text{Solve: } 2 - (7x + 5) = 13 - 3x$$

### **Solution**

$$2 - 7x - 5 = 13 - 3x$$

$$-7x - 3 = 13 - 3x$$

$$-4x = 16$$

$$\underline{x = -4}$$

### ***Exercise***

$$\text{Solve: } 16 = 3(x-1) - (x-7)$$

### **Solution**

$$16 = 3x - 3 - x + 7$$

$$16 = 2x + 4$$

$$2x = 12$$

$$\underline{x = 6}$$

### ***Exercise***

$$\text{Solve: } 5x - 2(x+1) = x + (3x-5)$$

### **Solution**

$$5x - 2x - 2 = x + 3x - 5$$

$$3x - 2 = 4x - 5$$

$$-x = -3$$

$$\underline{x = 3}$$



### ***Exercise***

Solve:  $7(x+1) = 4[x - (3-x)]$

#### **Solution**

$$7x + 7 = 4x - 4(3 - x)$$

$$3x = -7 - 12 + 4x$$

$$-x = -19$$

$$\underline{x = 19}$$

### ***Exercise***

Solve:  $2[3x - 2(2x - 3)] = 5(x - 6)$

#### **Solution**

$$6x - 4(2x - 3) = 5x - 30$$

$$6x - 8x + 12 = 5x - 30$$

$$-2x - 5x = -42$$

$$-7x = -42$$

$$\underline{x = 6}$$

### ***Exercise***

Solve:  $.2x - .5 = .1x + 7$

#### **Solution**

$$10 \times .2x - .5 = .1x + 7$$

$$2x - 5 = x + 70$$

$$\underline{x = 75}$$

### ***Exercise***

Solve:  $.01x + 3.1 = 2.03x - 2.96$

#### **Solution**

$$100 \times .01x + 3.1 = 2.03x - 2.96$$

$$x + 310 = 203x - 296$$

$$202x = 606$$

$$x = \frac{606}{202}$$

$$\underline{= 3}$$

### ***Exercise***

Solve:  $.08x - .06(x + 12) = 7.72$

#### **Solution**

$$100 \times .08x - .06(x + 12) = 7.72$$

$$8x - 6(x + 12) = 772$$

$$8x - 6x - 72 = 772$$

$$2x = 700$$

$$x = 350$$

### ***Exercise***

Solve:  $.04(x - 12) + .06x = 1.52$

#### **Solution**

$$100 \times .04(x - 12) + .06x = 1.52$$

$$4(x - 12) + 6x = 152$$

$$4x - 48 + 6x = 152$$

$$10x = 200$$

$$x = 20$$

### ***Exercise***

Solve:  $.3(x + 2) - .5(x + 2) = -.2x - .4$

#### **Solution**

$$10 \times .3(x + 2) - .5(x + 2) = -.2x - .4$$

$$3(x + 2) - 5(x + 2) = -2x - 4$$

$$3x + 6 - 5x - 10 = -2x - 4$$

$$-2x - 4 = -2x - 4$$

$$0 = 0 \text{ True statement}$$

$$\text{Solution: } \mathbb{R}$$

### ***Exercise***

Solve:  $.6(x - 5) + .8(x - 6) = .2x - 1.8$

#### **Solution**

$$10 \times .6(x - 5) + .8(x - 6) = .2x - 1.8$$

$$6(x-5) + 8(x-6) = 2x - 18$$

$$6x - 30 + 8x - 48 = 2x - 18$$

$$14x - 78 = 2x - 18$$

$$12x = 60$$

$$\underline{x = 5}$$

### ***Exercise***

Solve:  $.5x + \frac{4}{3}x = x + 10$

### **Solution**

$$30 \times .5x + \frac{4}{3}x = x + 10$$

$$15x + 40x = 30x + 300$$

$$55x = 30x + 300$$

$$25x = 300$$

$$x = \frac{300}{25}$$

$$\underline{x = 12}$$

***Or***

$$\frac{1}{2}x + \frac{4}{3}x = x + 10$$

$$6 \times \frac{1}{2}x + \frac{4}{3}x = x + 10$$

$$3x + 8x = 6x + 60$$

$$5x = 60$$

$$\underline{x = 12}$$

### ***Exercise***

Solve:  $.25x + \frac{2}{3}x = x + 2$

### **Solution**

$$\frac{1}{4}x + \frac{2}{3}x = x + 2$$

$$12 \times \frac{1}{4}x + \frac{2}{3}x = 12x + 24$$

$$3x + 8x = 12x + 24$$

$$-x = 24$$

$$\underline{x = -24}$$

### ***Exercise***

Solve:  $\frac{1}{4}(x-2) = \frac{1}{6}(x-5)$

#### **Solution**

$$6(x-2) = 4(x-5)$$

$$6x - 12 = 4x - 20$$

$$2x = -8$$

$$\underline{x = -4}$$

### ***Exercise***

Solve:  $\frac{1}{4}(3x-2) = \frac{1}{5}(x+5)$

#### **Solution**

$$5(3x-2) = 4(x+5)$$

$$15x - 10 = 4x + 20$$

$$11x = 30$$

$$\underline{x = \frac{30}{11}}$$

### ***Exercise***

Solve:  $\frac{1}{9}(x+2) = \frac{1}{15}(2x+5)$

#### **Solution**

$$15(x+2) = 9(2x+5)$$

$$15x + 30 = 18x + 45$$

$$3x = -15$$

$$\underline{x = -5}$$

### ***Exercise***

Solve:  $\frac{1}{2}(4x+8) - 16 = -\frac{2}{3}(9x-12)$

#### **Solution**

$$6 \times \frac{1}{2}(4x+8) - 16 = -\frac{2}{3}(9x-12)$$

$$3(4x+8) - 96 = -4(9x-12)$$

$$12x + 24 - 96 = -36x + 48$$

$$12x + 36x = 48 + 72$$

$$48x = 120$$

$$x = \frac{120}{48}$$

$$= \frac{5}{2}$$

### Exercise

Solve:  $\frac{3}{4}(24 - 8x) - 16 = -\frac{2}{3}(6x - 9)$

#### Solution

$$12 \times \frac{3}{4}(24 - 8x) - 16 = -\frac{2}{3}(6x - 9)$$

$$9(24 - 8x) - 192 = -8(6x - 9)$$

$$216 - 72x - 192 = -48x + 72$$

$$24x = 24 - 72$$

$$24x = -48$$

$$x = -2$$

### Exercise

Solve:  $\frac{x-3}{4} = \frac{5}{14} - \frac{x+5}{7}$

#### Solution

$$(28)\frac{x-3}{4} = (28)\frac{5}{14} - (28)\frac{x+5}{7}$$

$$LCD : 4 \quad 14 \quad 7 \rightarrow 28$$

$$7(x - 3) = 2(5) - 4(x + 5)$$

$$7x - 21 = 10 - 4x - 20$$

$$7x + 4x = 21 - 10$$

$$11x = 11$$

$$x = 1$$

### Exercise

Solve:  $\frac{x+1}{4} = \frac{1}{6} + \frac{2-x}{3}$

#### Solution

$$12\frac{x+1}{4} = 12\frac{1}{6} + 12\frac{2-x}{3}$$

$$3(x+1) = 2 + 4(2-x)$$

$$3x + 3 = 2 + 8 - 4x$$

$$3x + 4x = 2 + 8 - 3$$

$$7x = 7$$

$$\underline{x = 1}$$

### Exercise

Solve  $\frac{x-8}{3} + \frac{x-3}{2} = 0$

### Solution

$$(6)\frac{x-8}{3} + (6)\frac{x-3}{2} = 0(6)$$

**LCD: 2, 3: 6**

$$2(x-8) + 3(x-3) = 0$$

$$2x - 16 + 3x - 9 = 0$$

$$5x - 25 = 0$$

$$5x = 25$$

$$\underline{x = 5}$$

### Exercise

Solve:  $\frac{5}{2x} - \frac{8}{9} = \frac{1}{18} - \frac{1}{3x}$

### Solution

**Restriction:  $x \neq 0$**

$$18x \frac{5}{2x} - 18x \frac{8}{9} = 18x \frac{1}{18} - 18x \frac{1}{3x}$$

$$2x \quad 9 \quad 18 \quad 3x \quad \rightarrow 18x$$

$$9(5) - 2x(8) = x - 6$$

$$45 - 16x = x - 6$$

$$45 + 6 = x + 16x$$

$$51 = 17x$$

$$x = \frac{51}{17}$$

$$\underline{= 3}$$

### Exercise

Solve:  $\frac{1}{x+4} + \frac{1}{x-4} = \frac{22}{x^2-16}$

### Solution

**Restrictions:**  $x \neq \pm 4$

$$(x+4)(x-4)\frac{1}{x+4} + (x+4)(x-4)\frac{1}{x-4} = (x+4)(x-4)\frac{22}{x^2-16}$$

$$x - 4 + x + 4 = 22$$

$$2x = 22$$

$$\underline{x = 11}$$

### Exercise

Solve:  $\frac{3x-1}{3} - \frac{2x}{x-1} = x$

### Solution

**Condition (Restriction):**  $x - 1 \neq 0 \Rightarrow x \neq 1$

$$3(x-1)\frac{3x-1}{3} - 3(x-1)\frac{2x}{x-1} = 3(x-1)x$$

$$3x^2 - x - 3x + 1 - 6x = 3x^2 - 3x$$

$$3x^2 - x - 3x + 1 - 6x - 3x^2 + 3x = 0$$

$$-7x + 1 = 0$$

$$-7x = -1$$

$$\underline{x = \frac{1}{7}}$$

### Exercise

Solve:  $\frac{x}{x-2} = \frac{2}{x-2} + 2$

### Solution

**Restriction:**  $x - 2 \neq 0 \Rightarrow x \neq 2$

$$(x-2)\frac{x}{x-2} = (x-2)\frac{2}{x-2} + 2(x-2)$$

$$x = 2 + 2x - 4$$

$$-x = -2$$

$$x = 2$$

$\Rightarrow$  No Solution or  $\{\emptyset\}$  because of the restriction.

### ***Exercise***

Solve the equation  $\frac{x}{x-7} = \frac{7}{x-7} + 8$

### **Solution**

Restriction:  $x - 7 \neq 0 \Rightarrow \boxed{x \neq 7}$

$$(x-7)\frac{x}{x-7} = (x-7)\frac{7}{x-7} + 8(x-7)$$

$$x = 7 + 8x - 56$$

$$x - 8x = -49$$

$$-7x = -49$$

$$x = \frac{-49}{-7} = \underline{7}$$

But  $x \neq 7$  (restriction), therefore there is ***no solution***

### ***Exercise***

Solve:  $\frac{3x}{5} - x = \frac{x}{10} - \frac{5}{2}$

### **Solution**

$$10 \times \frac{3x}{5} - x = \frac{x}{10} - \frac{5}{2}$$

$$6x - 10x = x - 25$$

$$-4x = x - 25$$

$$-5x = -25$$

$$\underline{x = 5}$$

### ***Exercise***

Solve:  $2x - \frac{2x}{7} = \frac{x}{2} + \frac{17}{2}$

### **Solution**

$$\frac{14x - 2x}{7} = \frac{x + 17}{2}$$

$$\frac{12x}{7} = \frac{x + 17}{2}$$

$$24x = 7x + 119$$

$$17x = 119$$

$$\underline{x = 7}$$



### ***Exercise***

Solve:  $\frac{x+3}{6} = \frac{2}{3} + \frac{x-5}{4}$

#### **Solution**

$$12 \times \frac{x+3}{6} = \frac{2}{3} + \frac{x-5}{4}$$

$$2x + 6 = 8 + 3x - 15$$

$$2x - 3x = 8 - 15 - 6$$

$$-x = -13$$

$$\underline{x = 13}$$

### ***Exercise***

Solve:  $\frac{x+1}{4} = \frac{1}{6} + \frac{2-x}{3}$

#### **Solution**

$$12 \times \frac{x+1}{4} = \frac{1}{6} + \frac{2-x}{3}$$

$$3x + 3 = 2 + 8 - 4x$$

$$7x = 7$$

$$\underline{x = 1}$$

### ***Exercise***

Solve:  $\frac{x}{4} = 2 + \frac{x-3}{3}$

#### **Solution**

$$12 \times \frac{x}{4} = 2 + \frac{x-3}{3}$$

$$3x = 24 - 4x - 12$$

$$7x = 12$$

$$\underline{x = \frac{12}{7}}$$

### ***Exercise***

Solve:  $5 + \frac{x-2}{3} = \frac{x+3}{8}$

#### **Solution**

$$24 \times 5 + \frac{x-2}{3} = \frac{x+3}{8}$$

$$120 + 8x - 16 = 3x + 9$$

$$5x = 9 - 104$$

$$5x = -95$$

$$\underline{x = -19}$$

### ***Exercise***

$$\text{Solve: } \frac{x+1}{3} = 5 - \frac{x+2}{7}$$

### **Solution**

$$21 \times \frac{x+1}{3} = 5 - \frac{x+2}{7}$$

$$7x + 7 = 105 - 3x - 6$$

$$10x = 92$$

$$\underline{x = \frac{46}{5}}$$

### ***Exercise***

$$\text{Solve: } \frac{3x}{5} - \frac{x-3}{2} = \frac{x+2}{3}$$

### **Solution**

$$30 \times \frac{3x}{5} - \frac{x-3}{2} = \frac{x+2}{3}$$

$$18x - 15x + 45 = 10x + 20$$

$$3x - 10x = 20 - 45$$

$$-7x = -25$$

$$\underline{x = \frac{25}{7}}$$

### ***Exercise***

$$\text{Solve: } \frac{3x+2}{x-2} + \frac{1}{x} = \frac{-2}{x^2-2x}$$

### **Solution**

$$\text{Restriction: } \begin{cases} x-2 \neq 0 \Rightarrow x \neq 2 \\ x \neq 0 \end{cases}$$

$$x(x-2) \frac{3x+2}{x-2} + x(x-2) \frac{1}{x} = x(x-2) \frac{-2}{x^2-2x}$$

$$3x^2 + 2x + x - 2 = -2$$

$$3x^2 + 3x = 0$$

$$3x(x+1) = 0$$

$$3x = 0 \quad x+1 = 0$$

$$x = 0 \quad x = -1$$

$x = -1$  is the only solution

### Exercise

Solve:  $\frac{-4x}{x-1} + \frac{4}{x+1} = \frac{-8}{x^2-1}$

### Solution

Restriction:  $x \neq \pm 1$

$$(x-1)(x+1) \frac{-4x}{x-1} + (x-1)(x+1) \frac{4}{x+1} = (x-1)(x+1) \frac{-8}{x^2-1}$$

$$-4x(x+1) + 4(x-1) = -8$$

$$-4x^2 - 4x + 4x - 4 = -8$$

$$-4x^2 = -4$$

$$x^2 = 1$$

$x = \pm 1$  The solution is  $\{\emptyset\}$

### Exercise

Solve:  $\frac{4x+3}{x+1} + \frac{2}{x} = \frac{1}{x^2+x}$

### Solution

Restriction:  $x+1 \neq 0 \rightarrow x \neq -1, 0$

$$x(x+1) \frac{4x+3}{x+1} + x(x+1) \frac{2}{x} = x(x+1) \frac{1}{x^2+x}$$

$$x(4x+3) + 2(x+1) = 1$$

$$4x^2 + 3x + 2x + 2 = 1$$

$$4x^2 + 5x + 2 - 1 = 1 - 1$$

$$4x^2 + 5x + 1 = 0$$

$$(4x+1)(x+1) = 0$$

$$4x+1=0 \quad x+1=0$$

$$\underline{x = -\frac{1}{4}} \quad \cancel{x = -1}$$

### Exercise

Solve:  $\frac{6}{x+3} - \frac{5}{x-2} = \frac{-20}{x^2+x-6}$

### Solution

$$\frac{6}{x+3} - \frac{5}{x-2} = \frac{-20}{x^2+x-6}$$

**Restriction:**  $x \neq -3, 2$

$$(x+3)(x-2) \frac{6}{x+3} - (x+3)(x-2) \frac{5}{x-2} = (x+3)(x-2) \frac{-20}{x^2+x-6}$$

$$6(x-2) - 5(x+3) = -20$$

$$6x - 12 - 5x - 15 = -20$$

$$x = -20 + 12 + 15$$

$$\underline{x = 7}$$

### Exercise

Solve:  $\frac{6}{x+1} - \frac{5}{x+2} = \frac{10}{x^2+3x+2}$

### Solution

**Restriction:**  $x \neq -1, -2$

$$6(x+2) - 5(x+1) = 10$$

$$6x + 12 - 5x - 5 = 10$$

$$\underline{x = 3}$$

### Exercise

Solve:  $3(x-4) - 5(x+2) = 3[2 - (x+24)] - 2(x-2)$

### Solution

$$3x - 12 - 5x - 10 = 6 - 3(x+24) - 2x + 4$$

$$-2x - 22 = -3x - 72 - 2x + 10$$

$$3x = -62 + 22$$

$$3x = -42$$

$$\underline{x = -14}$$

### Exercise

Solve:  $(2x+3)(6x-1) - 9 = 15x^2 - (3x-2)(x-2)$

### Solution

$$12x^2 + 16x - 3 - 9 = 15x^2 - (3x^2 - 8x + 4)$$

$$12x^2 + 16x - 12 = 15x^2 - 3x^2 + 8x - 4$$

$$12x^2 + 16x - 8x = 12x^2 - 4 + 12$$

$$8x = 8$$

$$\underline{x = 1}$$

### ***Exercise***

Solve:  $(3x - 1)^2 - 2x(x - 1) = 7x^2 - 5x + 2$

#### **Solution**

$$9x^2 - 6x + 1 - 2x^2 + 2x = 7x^2 - 5x + 2$$

$$7x^2 - 4x + 1 = 7x^2 - 5x + 2$$

$$\underline{x = 1}$$

### ***Exercise***

Solve:  $(2x + 3)(x - 1) + (x + 1)(x - 4) = 3x^2$

#### **Solution**

$$2x^2 + x - 3 + x^2 - 3x - 4 = 3x^2$$

$$3x^2 - 2x - 7 = 3x^2$$

$$2x = 7$$

$$\underline{x = \frac{7}{2}}$$

### ***Exercise***

Solve:  $4x + 13 - \{2x - [4(x - 3) - 5]\} = 2(x - 6)$

#### **Solution**

$$4x + 13 - 2x + 4(x - 3) - 5 = 2x - 12$$

$$2x + 8 + 4x - 12 = 2x - 12$$

$$4x = -8$$

$$\underline{x = -2}$$

### ***Exercise***

Solve:  $-2\{7 - [4 - 2(1 - x) + 3]\} = 10 - [4x - 2(x - 3)]$

#### **Solution**

$$-14 + 2[7 - 2 + 2x] = 10 - 4x + 2x - 6$$

$$-14 + 2(5 + 2x) = 2 - 2x$$

$$-14 + 10 + 4x = 2 - 2x$$

$$6x = 6$$

$$\underline{x = 1}$$

### ***Exercise***

Solve:  $2(y + 2) + (y + 3)^2 = y(y + 5) + 2\left(\frac{17}{2} + y\right)$

#### **Solution**

$$2y + 4 + y^2 + 6y + 9 = y^2 + 5y + 17 + 2y$$

$$8y + 13 = 7y + 17$$

$$\underline{y = 4}$$

### ***Exercise***

Solve:  $(y + 1)(y - 1) = (y + 2)(y - 3) + 4$

#### **Solution**

$$y^2 - 1 = y^2 - y - 6 + 4$$

$$-1 = -y - 2$$

$$\underline{y = -1}$$

### ***Exercise***

Solve:  $45 - [4 - 2y - 4(y + 7)] = -4(1 + 3y) - [4 - 3(y + 2) - 2(2y - 5)]$

#### **Solution**

$$45 - [4 - 2y - 4y - 28] = -4 - 12y - [4 - 3y - 6 - 4y + 10]$$

$$45 - 4 + 2y + 4y + 28 = -4 - 12y - 4 + 3y + 6 + 4y - 10$$

$$69 + 6y = -12 - 5y$$

$$6y + 5y = -12 - 69$$

$$11y = -81$$

$$\underline{y = -\frac{81}{11}}$$

### ***Exercise***

Solve:  $35 - [2 - 3y - 4(y + 7)] = -3(1 + 3y) + 4 - 3(y + 2) - 2(2y - 5)$

### **Solution**

$$35 - 2 + 3y + 4(y + 7) = -33 - 9y + 4 - 3y - 6 - 4y + 10$$

$$33 + 3y + 4y + 28 = -25 - 16y$$

$$61 + 7y = -25 - 16y$$

$$23y = -86$$

$$\underline{y = -\frac{86}{23}}$$

### ***Exercise***

Solve:  $25 - [2 + 5y - 3(y + 2)] = -3(2y - 5) - [5(y - 1) - 3y + 3]$

### **Solution**

$$25 - [2 + 5y - 3y - 6] = -6y + 15 - [5y - 5 - 3y + 3]$$

$$25 - (2y - 4) = -6y + 15 - (2y - 2)$$

$$25 - 2y + 4 = -6y + 15 - 2y + 2$$

$$-2y + 29 = -8y + 17$$

$$6y = -12$$

$$\underline{y = -2}$$

### ***Exercise***

Solve:  $V = lwh$ , for  $h$

### **Solution**

$$\underline{h = \frac{V}{lw}}$$

### ***Exercise***

Solve:  $A = \frac{1}{2}h(B + b)$  for  $B$

### **Solution**

$$2A = h(B + b) \quad \text{Multiply both sides by 2}$$

$$\frac{2A}{h} = B + b \quad \text{Divide both sides by } h$$

$$\underline{B = \frac{2A}{h} - b}$$

### ***Exercise***

Solve:  $A = \frac{1}{2}h(a + b)$  for  $a$

### **Solution**

$$2A = 2 \cdot \frac{1}{2}h(a + b)$$

$$2A = h(a + b)$$

$$\frac{2A}{h} = \frac{h}{h}(a + b)$$

$$\frac{2A}{h} = a + b$$

$$\frac{2A}{h} - b = a$$

$$\underline{a = \frac{2A}{h} - b} \quad \text{or} \quad a = \frac{2A - bh}{h}$$

### ***Exercise***

Solve:  $S = 2\pi rh + 2\pi r^2$  for  $h$

### **Solution**

$$2\pi rh = S - 2\pi r^2$$

$$\underline{h = \frac{S - 2\pi r^2}{2\pi r}}$$

### ***Exercise***

Solve:  $A = \frac{1}{2}h(b_1 + b_2)$ , for  $h$

### **Solution**

$$2A = h(b_1 + b_2)$$

$$\underline{h = \frac{2A}{b_1 + b_2}}$$



### ***Exercise***

Solve:  $A = \frac{1}{2}h(b_1 + b_2)$ , for  $b_2$

### **Solution**

$$2A = h(b_1 + b_2)$$

$$\frac{2A}{h} = b_1 + b_2$$

$$b_2 = \frac{2A}{h} - b_1$$

### ***Exercise***

Solve:  $A = \frac{1}{2}h(b_1 + b_2)$ , for  $b_1$

### **Solution**

$$\frac{2A}{h} = b_1 + b_2$$

$$b_1 = \frac{2A}{h} - b_2$$

### ***Exercise***

Solve:  $S = P + Prt$  for  $t$ .

### **Solution**

$$S - P = Prt$$

$$\frac{S - P}{Pr} = \frac{Pr}{Pr}t$$

$$t = \frac{S - P}{Pr}$$

### ***Exercise***

Solve:  $S = 2lw + 2wh + 2hl$  for  $h$

### **Solution**

$$S = 2lw + (2w + 2l)h$$

$$(2w + 2l)h = S - 2lw$$

$$h = \frac{S - 2lw}{2w + 2l}$$

### Exercise

Solve:  $S = 2lw + 2wh + 2hl$  for  $w$

### Solution

$$S = (2l + 2h)w + 2hl$$

$$(2l + 2h)w = S - 2hl$$

$$w = \frac{S - 2hl}{2l + 2h}$$

### Exercise

Solve:  $\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$  for  $R_1$

### Solution

1st Method

$$RR_1R_2 \frac{1}{R} = RR_1R_2 \frac{1}{R_1} + RR_1R_2 \frac{1}{R_2}$$

$$R_1R_2 = RR_2 + RR_1$$

$$R_1R_2 - RR_1 = RR_2$$

$$R_1(R_2 - R) = RR_2$$

$$R_1 = \frac{RR_2}{R_2 - R}$$

Multiply by the common denominator  $RR_1R_2$

Simplify

Move  $R_1$  to one side

Factor  $R_1$

Divide by  $R_2 - R$

2nd Method

$$\frac{1}{R} - \frac{1}{R_2} = \frac{1}{R_1}$$

$$\frac{R_2 - R}{RR_2} = \frac{1}{R_1}$$

$$R_1R_2 - RR_1 = RR_2$$

$$R_1(R_2 - R) = RR_2$$

$$R_1 = \frac{RR_2}{R_2 - R}$$

Common denominator on one side of the equality

Cross multiplication

Factor  $R_1$

Divide by  $R_2 - R$

3rd Method

$$\frac{1}{R} - \frac{1}{R_2} = \frac{1}{R_1}$$

$$\frac{R_2 - R}{RR_2} = \frac{1}{R_1}$$

Cross multiplication

$$\underline{R_1 = \frac{RR_2}{R_2 - R}}$$

*Flip*

### ***Exercise***

Solve:  $\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$  for  $R$

### **Solution**

$$\frac{1}{R} = \frac{R_1 + R_2}{R_1 R_2}$$

$$\underline{R = \frac{R_1 R_2}{R_1 + R_2}}$$

### ***Exercise***

Solve:  $V = \frac{d_1 - d_2}{t}$  for  $d_1$

### **Solution**

$$d_1 - d_2 = Vt$$

$$\underline{d_1 = Vt + d_2}$$

### ***Exercise***

Solve:  $V = \frac{d_1 - d_2}{t}$  for  $d_2$

### **Solution**

$$d_1 - d_2 = Vt$$

$$\underline{d_2 = d_1 - Vt}$$

### ***Exercise***

Solve:  $z = \frac{x - \mu}{s}$  for  $x$

### **Solution**

$$x - \mu = sz$$

$$\underline{x = sz + \mu}$$

### ***Exercise***

Solve:  $z = \frac{x - \mu}{s}$  for  $\mu$

#### **Solution**

$$x - \mu = sz$$

$$\mu = x - sz$$

### ***Exercise***

Solve:  $s = \frac{1}{2}at^2 + vt$  for  $v$

#### **Solution**

$$vt = s - \frac{1}{2}at^2$$

$$v = \frac{s}{t} - \frac{1}{2}at$$

### ***Exercise***

Solve:  $s = \frac{1}{2}at^2 + vt$  for  $a$

#### **Solution**

$$\frac{1}{2}at^2 = s - vt$$

$$at^2 = 2s - 2vt$$

$$a = \frac{2s - 2vt}{t^2}$$

### ***Exercise***

Solve:  $L = a + (n - 1)d$  for  $n$

#### **Solution**

$$(n - 1)d = L - a$$

$$n - 1 = \frac{L - a}{d}$$

$$n = \frac{L - a}{d} + 1$$

### Exercise

Solve:  $L = a + (n-1)d$  for  $d$

#### Solution

$$(n-1)d = L - a$$

$$d = \frac{L-a}{n-1}$$

### Exercise

Solve:  $A = \frac{x_1 + x_2 + x_3}{n}$  for  $x_2$

#### Solution

$$x_1 + x_2 + x_3 = nA$$

$$x_2 = nA - x_1 - x_3$$

### Exercise

Solve:  $A = \frac{x_1 + x_2 + x_3}{n}$  for  $n$

#### Solution

$$n = \frac{x_1 + x_2 + x_3}{A}$$

### Exercise

A sewage treatment plant has two inlet pipes to its settling pond. One can fill the pond in 10 hrs, the other in 12 hrs. If the first pipe is open for 5 hrs and then the second pipe is opened, how long will it take to fill the pond?

#### Solution

	Rate	Time	Job: $A = rt$
One	$\frac{1}{10}$	$x$	$\frac{x}{10}$
Other	$\frac{1}{12}$	$x - 5$	$\frac{x-5}{12}$

$$\frac{x}{10} + \frac{x-5}{12} = 1$$

$$(60)\frac{x}{10} + (60)\frac{x-5}{12} = 1(60)$$

$$6x + 5(x - 5) = 60$$

$$6x + 5x - 25 = 60$$

$$11x = 85$$

$$\underline{x = \frac{85}{11} \approx 7.72}$$

$$\begin{aligned} \text{The other} &= \frac{85}{11} - 5 \\ &= \frac{30}{11} \end{aligned}$$