

$$\frac{a}{c} + \frac{b}{c} = \frac{a+b}{c}$$

$$\frac{a}{c} + \frac{b}{d} = \frac{ad+bc}{cd}$$

$$\frac{a}{c} - \frac{b}{d} = \frac{ad-bc}{cd}$$

$$\frac{a}{c} \cdot \frac{b}{d} = \frac{ab}{cd}$$

$$\frac{a}{c} \div \frac{b}{d} = \frac{a}{c} \cdot \frac{d}{b} = \frac{ad}{cb}$$

$$\frac{a}{b} = \frac{c}{d} \Leftrightarrow a = \frac{bc}{d} \Leftrightarrow ad = bc$$

$$\frac{\frac{a}{\frac{c}{b}}}{\frac{c}{b}} = \frac{a}{c}$$

$$\frac{\frac{a}{\frac{b}{c}}}{\frac{b}{c}} = \frac{a}{b}$$

$$a^0 = 1$$

$$a^m \cdot a^n = a^{m+n}$$

$$(a^m)^n = a^{mn}$$

$$\frac{a^m}{a^n} = a^{m-n}$$

$$a^{-n} = \frac{1}{a^n}$$

$$(ab)^m = a^m b^m$$

$$\left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}$$

$$\sqrt{xy} = \sqrt{x}\sqrt{y}$$

$$\sqrt{\frac{x}{y}} = \frac{\sqrt{x}}{\sqrt{y}}$$

$$\sqrt[n]{x} = x^{\frac{1}{n}}$$

$$\sqrt[n]{x^m} = x^{\frac{m}{n}}$$

$$(a-b)(a+b) = a^2 - b^2$$

$$(a-b)^2 = a^2 - 2ab + b^2$$

$$(a+b)^2 = a^2 + 2ab + b^2$$

$$(a-b)^3 = a^3 - 3a^2b + 3ab^2 - b^3$$

$$(a+b)^3 = a^3 + 3a^2b + 3ab^2 + b^3$$

$$x^2 + (a+b)x + ab = (x+a)(x+b)$$

$$a^2 + 2ab + b^2 = (a+b)^2$$

$$a^2 - b^2 = (a-b)(a+b)$$

$$a^2 + b^2 = (a - ib)(a + ib)$$

$$a^3 - b^3 = (a-b)(a^2 + ab + b^2)$$

$$a^3 + b^3 = (a+b)(a^2 - ab + b^2)$$

$$a^2 - 2ab + b^2 = (a-b)^2$$

$$\textcolor{red}{a}x^2 + \textcolor{blue}{b}x + \textcolor{green}{c} = 0 \Rightarrow \boxed{x = \frac{-\textcolor{blue}{b} \pm \sqrt{\textcolor{blue}{b}^2 - 4\textcolor{red}{a}\textcolor{green}{c}}}{2\textcolor{red}{a}}}$$

$$\checkmark \quad ax^2 + bx + c \geq 0 \rightarrow \text{if } a > 0 \Rightarrow x \leq x_1, \quad x \geq x_2$$

$$\checkmark \quad ax^2 + bx + c \leq 0 \rightarrow \text{if } a > 0 \Rightarrow x_1 \leq x \leq x_2$$

$|X| < \textcolor{blue}{c}$ are the numbers that satisfy $-\textcolor{blue}{c} < X < \textcolor{blue}{c}$.

$|X| > \textcolor{blue}{c}$ are the numbers that satisfy $X < -\textcolor{blue}{c}$ or $X > \textcolor{blue}{c}$.

The Binomial Theorem

$$(a+b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + \binom{n}{k}a^{n-k}b^k + \dots + \binom{n}{n-1}ab^{n-1} + b^n$$

$$\text{Slope} = m = \frac{\text{Vertical Change}}{\text{Horizontal Change}} = \frac{\text{Rise}}{\text{Run}} = \frac{y_2 - y_1}{x_2 - x_1}$$

Equation of a line: $y = mx + b$ (b : y - intercept)

$$y = m(x - x_1) + y_1 \quad (\text{Given: slope and one point})$$

Two slopes m_1 and m_2 are: **Parallel** (//) if $m_1 = m_2$

Perpendicular (\perp) $m_1 \cdot m_2 = -1$

Two points (x_1, y_1) and (x_2, y_2)

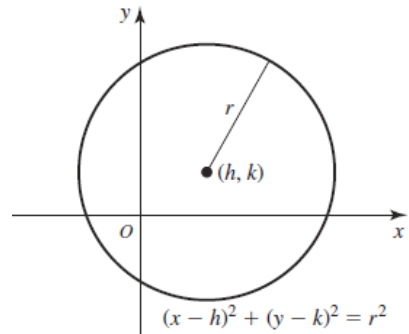
Distance between 2 points: $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

$$\textbf{Midpoint} = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

Equation of a circle with a center (h, k) and radius r :

$$(x-h)^2 + (y-k)^2 = r^2$$

(Diameter = 2.r)



Reflected across y -axis

Reflected across x -axis

$$y = -a f(-c(x \pm b)) \pm d$$

$\begin{cases} |a| > 1 & \Rightarrow \text{Stretching Vertically} \\ 0 < |a| < 1 & \Rightarrow \text{Shrinking Vertically} \end{cases}$
 $\begin{cases} |c| > 1 & \Rightarrow \text{Shrinking Horizontally} \\ 0 < |c| < 1 & \Rightarrow \text{Stretching Horizontally} \end{cases}$
 $\begin{cases} +b & \text{Shifted Left} \\ -b & \text{Shifted Right} \end{cases}$
 $\begin{cases} +d & \text{Shifted up} \\ -d & \text{Shifted Down} \end{cases}$

$e^0 = 1$	$e^1 = 2.7183$	$\ln e = 1$
$\log_a a = 1$	$\log_b 1 = 0$	$\ln 1 = 0$
$\log_b b^x = x$	$\log_a a^x = x$	
$e^x e^y = e^{x+y}$	$\frac{e^x}{e^y} = e^{x-y}$	$a^x = a^y \Leftrightarrow x = y$

$$y = \log_b x \Leftrightarrow x = b^y$$

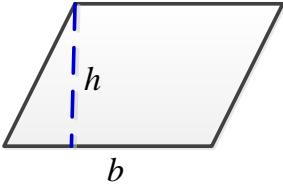
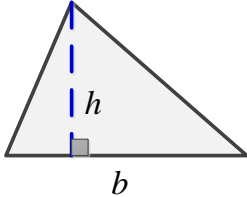
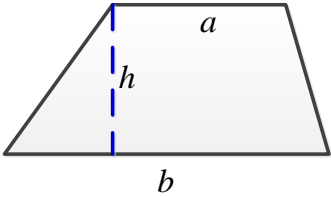
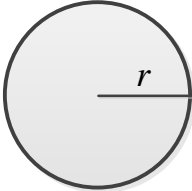
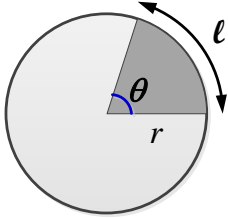
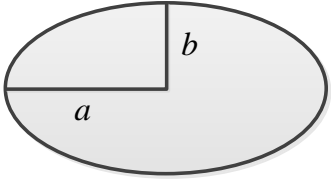
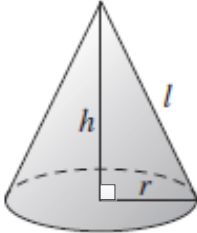
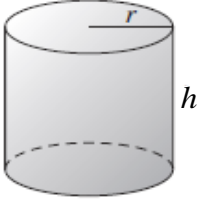
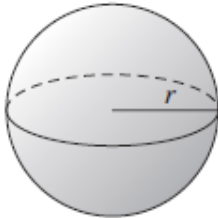
$$\log_b M = \frac{\log_a M}{\log_a b} \Rightarrow \log_b M = \frac{\log M}{\log b} = \frac{\ln M}{\ln b}$$

$\log_b MN = \log_b M + \log_b N$	$\log_b M^p = p \log_b M$	$\log_b \frac{M}{N} = \log_b M - \log_b N$
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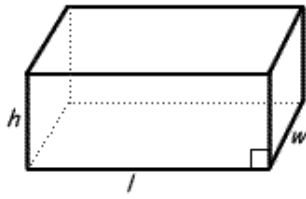
Exponential Growth / Decay: $P(t) = P_o e^{kt}$

Growth Rate and Doubling Time: $kT = \ln 2$; $k = \frac{\ln 2}{T}$; $T = \frac{\ln 2}{k}$

Geometry

<p style="text-align: center;">Parallelogram</p>  <p style="text-align: center;">$A = bh$</p>	<p style="text-align: center;">Triangle</p>  <p style="text-align: center;">$A = \frac{1}{2}bh$</p>	<p style="text-align: center;">Trapezoid</p>  <p style="text-align: center;">$A = \frac{1}{2}(a + b)h$</p>
<p style="text-align: center;">Circle</p>  <p style="text-align: center;">$A = \pi r^2$ $C = 2\pi r$</p>	<p style="text-align: center;">Sector</p>  <p style="text-align: center;">$A = \frac{1}{2}r^2\theta$ $S = r\theta \quad \theta \text{ in rad}$ $\ell = 2\pi r^2$</p>	<p style="text-align: center;">Ellipse</p>  <p style="text-align: center;">$A = \pi ab$</p>
<p style="text-align: center;">Cone</p>  <p style="text-align: center;">$V = \frac{1}{3}\pi r^2 h$ $A = \pi r\ell \quad (\text{cone})$ $\text{Surface Area} = \pi r\ell + \pi r^2$</p>	<p style="text-align: center;">Cylinder</p>  <p style="text-align: center;">$V = \pi r^2 h$ $A = 2\pi rh \quad (\text{side})$ $\text{Surface Area} = 2\pi rh + 2\pi r^2$</p>	<p style="text-align: center;">Sphere</p>  <p style="text-align: center;">$V = \frac{4}{3}\pi r^3$ $A = 4\pi r^2$</p>

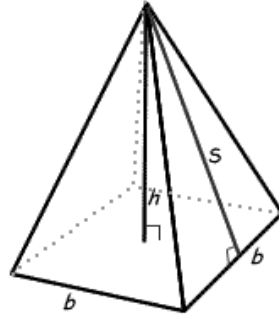
Rectangular Prism



$$A = 2(wh + lw + lh)$$

$$V = lwh$$

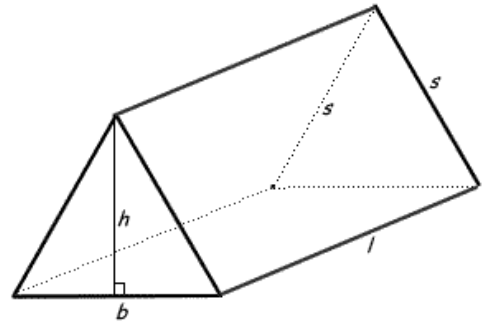
Square Based Pyramid



$$A = 2bs + b^2$$

$$V = \frac{1}{3}b^2h$$

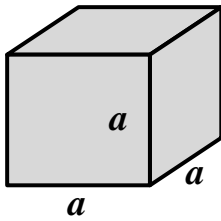
Triangular Prism



$$A = bh + 2ls + lb$$

$$V = \frac{1}{2}(bh)l$$

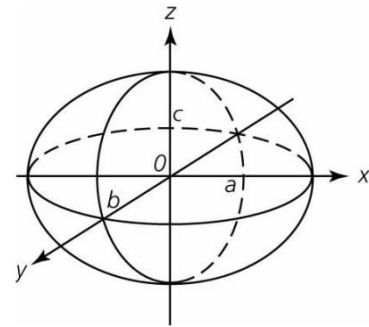
Cube



$$\text{Surface Area} = 6a^2$$

$$V = a^3$$

Ellipsoid



$$V = \frac{4}{3}\pi abc$$

