

The average rate of change:  $\frac{\Delta y}{\Delta x} = \frac{f(x+h) - f(x)}{h}$ ,  $h \neq 0$

**Sandwich Theorem**  $g(x) \leq f(x) \leq h(x) \Rightarrow \lim_{x \rightarrow c} g(x) = \lim_{x \rightarrow c} h(x) = L$  then  $\lim_{x \rightarrow c} f(x) = L$

Let  $f(x)$  be defined on an open interval about  $x_0$ , except possibly at  $x_0$  itself. We say that **the limit of  $f(x)$  as  $x$  approaches  $x_0$  is the number  $L$** , and write:  $\lim_{x \rightarrow x_0} f(x) = L$

If, for every number  $\varepsilon > 0$ , there exists a corresponding number  $\delta > 0$  such that for all  $x$ ,

$$0 < |x - x_0| < \delta \Rightarrow |f(x) - L| < \varepsilon$$

**Continuity:**  $\lim_{x \rightarrow c} f(x) = f(c)$

**Horizontal Asymptote:**  $f(x) = \frac{p(x)}{q(x)} = \frac{a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0}{b_m x^m + b_{m-1} x^{m-1} + \dots + b_1 x + b_0} = \frac{a_n x^n}{b_m x^m}$

$$n < m \Rightarrow y = 0$$

$$n = m \Rightarrow y = \frac{a_n}{b_m}$$

$$n > m \Rightarrow \text{No horizontal asymptote}$$

**Vertical Asymptote** - Think Domain