

# Lecture 1 – Functions, Exponential & Logarithms

## Section 1.1 – Functions

A **set** is a collection of objects of some type, and the objects are called **elements** of the set.

<b>Notation or Terminology</b>	<b>Meaning</b>	<b>Example</b>
$a \in S$	$a$ is an element of $S$	$3 \in \mathbb{Z}$
$a \notin S$	$a$ is not an element of $S$	$\frac{3}{2} \notin \mathbb{Z}$
$S \subset T$	$S$ is a <b>subset</b> of $T$ Every element of $S$ is an element of $T$	$\mathbb{Z} \subset \mathbb{R}$
<b>Constant</b>	A letter or symbol that represents a specific element of a set.	5, $\sqrt{2}$ , $\pi$
<b>Variable</b>	A letter or symbol that represents any element of a set.	Let $x$ denote any $\mathbb{R}$

### Definition of a Function

A **function** is a relation between two variables such that to matches each element of a first set (called **domain**) to an element of a second set (called **range**) in such way that no element in the first set is assigned to two different elements in the second set.

The **domain** of the function is the set of all values of the independent variable for which the function is defined.

The **range** of the function is the set of all values taken on by the dependent variable.

### The **Domain** of a Function

1. Rational function:  $\frac{f(x)}{h(x)}$   $\Rightarrow$  **Domain:**  $h(x) \neq 0$

**Example:**  $f(x) = \frac{1}{x-3}$  **Domain:**  $x \neq 3$

2. Irrational function:  $\sqrt{g(x)}$   $\Rightarrow$  **Domain:**  $g(x) \geq 0$

**Example:**  $g(x) = \sqrt{3-x} + 5$  **Domain:**  $x \leq 3$

3. Otherwise: **Domain** all real numbers

**Example:**  $f(x) = x^3 + |x|$  **Domain:** All real numbers,  $\mathbb{R}$ , or  $(-\infty, \infty)$

(1) & (2) → Find the domain:  $f(x) = \frac{x+1}{\sqrt{x-3}} \Rightarrow \text{Domain: } x > 3$

$$\boxed{\begin{aligned} ax^2 + bx + c &\geq 0 \rightarrow \text{if } a > 0 \Rightarrow x \leq x_1, x \geq x_2 \\ ax^2 + bx + c &\leq 0 \rightarrow \text{if } a > 0 \Rightarrow x_1 \leq x \leq x_2 \end{aligned}}$$

### Example

Let  $g(x) = \frac{\sqrt{4+x}}{1-x}$ . Find the domain of  $g$ .

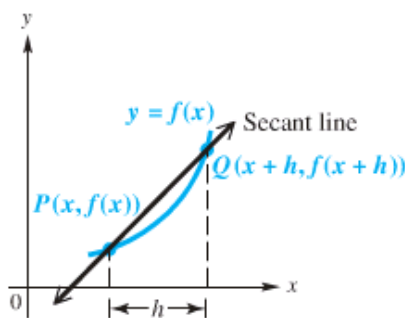
### Solution

$$\begin{cases} 4+x \geq 0 \Rightarrow x \geq -4 \\ 1-x \neq 0 \Rightarrow x \neq 1 \end{cases} \rightarrow [-4, 1) \cup (1, \infty)$$

### Difference Quotients

$$\frac{f(x+h)-f(x)}{(x+h)-x}$$

The difference quotient is given by:  $\frac{f(x+h)-f(x)}{h}$



### Example

For the function  $f$  given by  $f(x) = 2x^2 - 3x$ , find the difference quotient  $\frac{f(x+h)-f(x)}{h}$

### Solution

$$\begin{aligned} \frac{f(x+h)-f(x)}{h} &= \frac{\overbrace{2(x+h)^2 - 3(x+h)}^{f(x+h)} - \underbrace{(2x^2 - 3x)}_{f(x)}}{h} \\ &= \frac{2x^2 + 4xh + 2h^2 - 3x - 3h - 2x^2 + 3x}{h} \\ &= \frac{4xh + 2h^2 - 3h}{h} \\ &= \frac{4xh}{h} + \frac{2h^2}{h} - \frac{3h}{h} \\ &= \underline{4x + 2h - 3} \end{aligned}$$

## ***Even and Odd Functions***

Given the function  $f(x)$  then find  $f(-x)$  and simplify:

- If  $f(-x) = f(x) \Rightarrow f$  is ***even***, or
- If  $f(-x) = -f(x) \Rightarrow f$  is ***odd***
- ***Neither***

### ***Example***

Decide whether each function is even, odd, or neither

a)  $f(x) = 8x^4 - 3x^2$

$$\begin{aligned}f(-x) &= 8(-x)^4 - 3(-x)^2 \\&= 8x^4 - 3x^2 \\&= f(x)\end{aligned}$$

Function is *Even*

b)  $f(x) = 6x^3 - 9x$

$$\begin{aligned}f(-x) &= 6(-x)^3 - 9(-x) \\&= -6x^3 + 9x \\&= -(6x^3 - 9x) \\&= -f(x)\end{aligned}$$

Function is *Odd*

c)  $f(x) = 3x^2 + 5x$

$$\begin{aligned}f(-x) &= 3(-x)^2 + 5(-x) \\&= 3x^2 - 5x\end{aligned}$$

Function is *Neither*

## Piecewise-Defined Functions

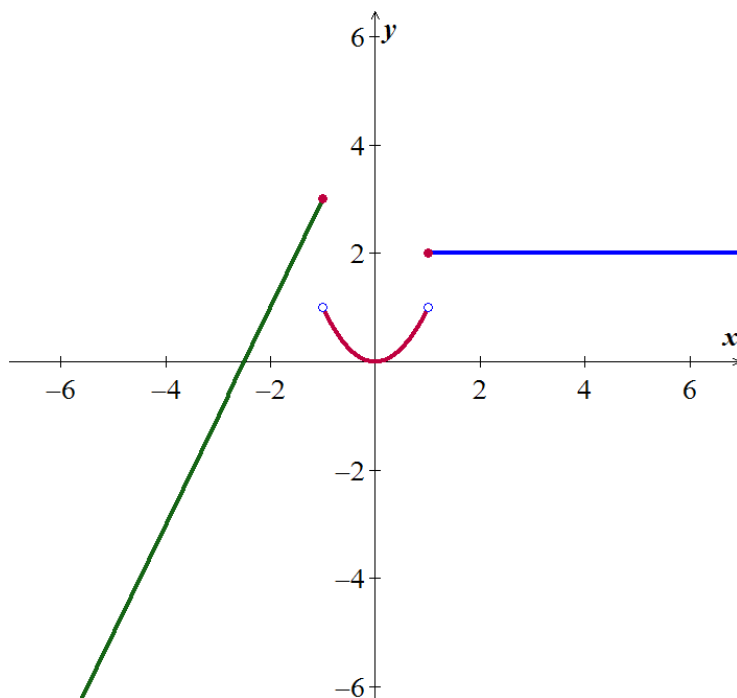
Function are sometimes described by more than one expression, we call such functions *piecewise-defined functions*.

### Example

Graph each function

$$f(x) = \begin{cases} 2x+5 & \text{if } x \leq -1 \\ x^2 & \text{if } |x| < 1 \\ 2 & \text{if } x \geq 1 \end{cases}$$

### Solution

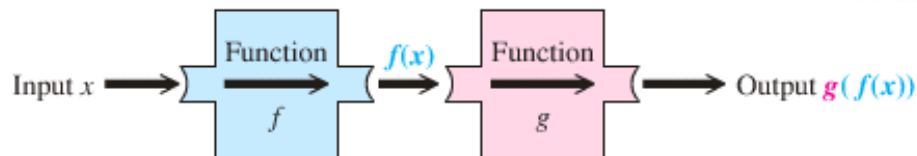
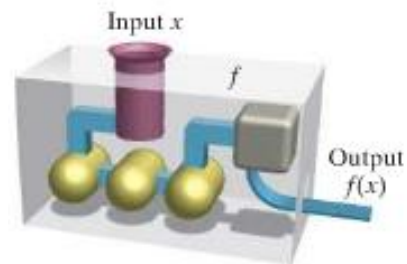


## Composition of Functions

The composite function  $f \circ g$ , the composite of  $f$  and  $g$ , is defined as

$$(f \circ g)(x) = f(g(x))$$

Where  $x$  is in the domain of  $g$   
and  $g(x)$  is in the domain of  $f$



### Example

Let  $f(x) = x^2 - 1$  and  $g(x) = 3x + 5$

- Find  $(f \circ g)(x)$  and the domain of  $f \circ g$
- Find  $(g \circ f)(x)$  and the domain of  $g \circ f$
- Find  $(f(g))(2)$  in two different ways: first using the functions  $f$  and  $g$  separately and second using the composite function  $f \circ g$ .

### Solution

$$\begin{aligned} a) \quad (f \circ g)(x) &= f(g(x)) \\ &= f(3x + 5) \\ &= (\underline{\quad})^2 - 1 \\ &= (3x + 5)^2 - 1 \\ &= 9x^2 + 30x + 25 - 1 \\ &= 9x^2 + 30x + 24 \end{aligned}$$

$$\text{Domain} : (3x + 5) \rightarrow \mathbb{R}$$

$$\text{Domain} : (9x^2 + 30x + 24) \rightarrow \mathbb{R}$$

**Domain** of  $f \circ g : \mathbb{R}$

$$\begin{aligned} b) \quad (g \circ f)(x) &= g(f(x)) \\ &= g(x^2 - 1) \\ &= 3(x^2 - 1) + 5 \\ &= 3x^2 - 3 + 5 \\ &= 3x^2 + 2 \end{aligned}$$

$$\text{Domain} : (x^2 - 1) \rightarrow \mathbb{R}$$

$$\text{Domain} : (3x^2 + 2) \rightarrow \mathbb{R}$$

**Domain** of  $g \circ f : \mathbb{R}$

$$c) \quad g(2) = 3(2) + 5 = 11$$

$$\begin{aligned}(f \circ g)(2) &= f(g(2)) \\ &= f(11) \\ &= 11^2 - 1 \\ &= 120\end{aligned}$$

$$(f \circ g)(x) = 9x^2 + 30x + 24$$

$$(f \circ g)(\textcolor{red}{2}) = 9(\textcolor{red}{2})^2 + 30(\textcolor{red}{2}) + 24 = \underline{\textcolor{blue}{120}}$$

### ***Example***

Let  $f(x) = x^2 - 16$  and  $g(x) = \sqrt{x}$

a) Find  $(f \circ g)(x)$  and the domain of  $f \circ g$

b) Find  $(g \circ f)(x)$  and the domain of  $g \circ f$

### **Solution**

$$\begin{aligned}a) \quad (f \circ g)(x) &= f(g(x)) \\ &= f(\sqrt{x}) \\ &= (\sqrt{x})^2 - 16 \\ &= x - 16\end{aligned}$$

$$\text{Domain} : (\sqrt{x}) \rightarrow x \geq 0$$

$$\text{Domain} : (x - 16) \rightarrow \mathbb{R}$$

**Domain** of  $f \circ g : x \geq 0$

$$\begin{aligned}b) \quad (g \circ f)(x) &= g(f(x)) \\ &= g(x^2 - 16) \\ &= \sqrt{x^2 - 16}\end{aligned}$$

$$\text{Domain} : (x^2 - 16) \rightarrow \mathbb{R}$$

$$\text{Domain} : (\sqrt{x^2 - 16}) \rightarrow |x| \geq 4$$

**Domain** of  $g \circ f : |x| \geq 4$  *or*  $(-\infty, -4] \cup [4, \infty)$

# Exercises

## Section 1.1 – Functions

(1 – 80) Find the Domain

1.  $f(x) = 7x + 4$

2.  $f(x) = |3x - 2|$

3.  $f(x) = 3x + \pi$

4.  $f(x) = \sqrt{7}x + \frac{1}{2}$

5.  $f(x) = -2x^2 + 3x - 5$

6.  $f(x) = x^3 - 2x^2 + x - 3$

7.  $f(x) = x^2 - 2x - 15$

8.  $f(x) = 4 - \frac{2}{x}$

9.  $f(x) = \frac{1}{x^4}$

10.  $g(x) = \frac{3}{x-4}$

11.  $y = \frac{2}{x-3}$

12.  $y = \frac{-7}{x-5}$

13.  $f(x) = \frac{x+5}{2-x}$

14.  $f(x) = \frac{8}{x+4}$

15.  $f(x) = \frac{1}{x+4}$

16.  $f(x) = \frac{1}{x-4}$

17.  $f(x) = \frac{3x}{x+2}$

18.  $f(x) = x - \frac{2}{x-3}$

19.  $f(x) = x + \frac{3}{x-5}$

20.  $f(x) = \frac{1}{2}x - \frac{8}{x+7}$

21.  $f(x) = \frac{1}{x-3} - \frac{8}{x+7}$

22.  $f(x) = \frac{1}{x+4} - \frac{2x}{x-4}$

23.  $f(x) = \frac{3x^2}{x+3} - \frac{4x}{x-2}$

24.  $f(x) = \frac{1}{x^2 - 2x + 1}$

25.  $f(x) = \frac{x}{x^2 + 3x + 2}$

26.  $f(x) = \frac{x^2}{x^2 - 5x + 4}$

27.  $f(x) = \frac{1}{x^2 - 4x - 5}$

28.  $g(x) = \frac{2}{x^2 + x - 12}$

29.  $h(x) = \frac{5}{\frac{4}{x} - 1}$

30.  $y = \sqrt{x}$

31.  $f(x) = \sqrt{8-3x}$

32.  $y = \sqrt{4x+1}$

33.  $y = \sqrt{7-2x}$

34.  $f(x) = \sqrt{8-x}$

35.  $f(x) = \sqrt{3-2x}$

36.  $f(x) = \sqrt{3+2x}$

37.  $f(x) = \sqrt{5-x}$

38.  $f(x) = \sqrt{x-5}$

39.  $f(x) = \sqrt{6-3x}$

40.  $f(x) = \sqrt{3x-6}$

41.  $f(x) = \sqrt{2x+7}$

42.  $f(x) = \sqrt{x^2-16}$

43.  $f(x) = \sqrt{16-x^2}$

44.  $f(x) = \sqrt{9-x^2}$

45.  $f(x) = \sqrt{x^2-25}$

46.  $f(x) = \sqrt{x^2-5x+4}$

47.  $f(x) = \sqrt{x^2+5x+4}$

48.  $f(x) = \sqrt{x^2+3x+2}$

49.  $f(x) = \sqrt{x^2-3x+2}$

50.  $f(x) = \sqrt{x-4} + \sqrt{x+1}$

51.  $f(x) = \sqrt{3-x} + \sqrt{x-2}$

52.  $f(x) = \sqrt{1-x} + \sqrt{4-x}$

53.  $f(x) = \sqrt{1-x} - \sqrt{x-3}$

54.  $f(x) = \sqrt{x+4} - \sqrt{x-1}$

55.  $f(x) = \frac{\sqrt{x+1}}{x}$

56.  $g(x) = \frac{\sqrt{x-3}}{x-6}$

57.  $f(x) = \frac{\sqrt{x+4}}{\sqrt{x-1}}$

58.  $f(x) = \frac{\sqrt{5-x}}{x}$

59.  $f(x) = \frac{x}{\sqrt{5-x}}$

$$60. f(x) = \frac{1}{x\sqrt{5-x}}$$

$$61. f(x) = \frac{x+1}{x^3-4x}$$

$$62. f(x) = \frac{\sqrt{x+5}}{x}$$

$$63. f(x) = \frac{x}{\sqrt{x+5}}$$

$$64. f(x) = \frac{1}{x\sqrt{x+5}}$$

$$65. f(x) = \frac{x+3}{\sqrt{x-3}}$$

$$66. f(x) = \frac{\sqrt{x+3}}{\sqrt{x-3}}$$

$$67. f(x) = \frac{\sqrt{x-2}}{\sqrt{x+2}}$$

$$68. f(x) = \frac{\sqrt{2-x}}{\sqrt{x+2}}$$

$$69. f(x) = \frac{x-4}{\sqrt{x-2}}$$

$$70. f(x) = \frac{1}{(x-3)\sqrt{x+3}}$$

$$71. f(x) = \sqrt{x+2} + \sqrt{2-x}$$

$$72. f(x) = \sqrt{(x-2)(x-6)}$$

$$73. f(x) = \sqrt{x+3} - \sqrt{4-x}$$

$$74. f(x) = \frac{\sqrt{4x-3}}{x^2-4}$$

$$75. f(x) = \frac{4x}{6x^2+13x-5}$$

$$76. f(x) = \frac{\sqrt{2x-3}}{x^2-5x+4}$$

$$77. f(x) = \frac{x^2}{\sqrt{x^2-5x+4}}$$

$$78. f(x) = \frac{x+2}{\sqrt{x^2+5x+4}}$$

$$79. f(x) = \frac{\sqrt{x+2}}{\sqrt{x^2+3x+2}}$$

$$80. f(x) = \frac{\sqrt{2x+3}}{x^2-6x+5}$$

(81 – 97) Find and simplify the difference quotient  $\frac{f(x+h)-f(x)}{h}$  for the given function

$$81. f(x) = 9x + 5$$

$$82. f(x) = 6x + 2$$

$$83. f(x) = 4x + 11$$

$$84. f(x) = 3x - 5$$

$$85. f(x) = -2x - 3$$

$$86. f(x) = -4x + 3$$

$$87. f(x) = 3x - 6$$

$$88. f(x) = -5x - 7$$

$$89. f(x) = 2x^2$$

$$90. f(x) = 5x^2$$

$$91. f(x) = 3x^2 - 4x$$

$$92. f(x) = 2x^2 - 3x$$

$$93. f(x) = 2x^2 - x - 3$$

$$94. f(x) = x^2 - 2x + 5$$

$$95. f(x) = 3x^2 - 2x + 5$$

$$96. f(x) = -2x^2 - 3x + 7$$

$$97. f(x) = \sqrt{x-3}$$

98. Let  $f(x) = 4x - 3$  and  $g(x) = 5x + 7$ . Find each of the following and give the domain

$$a) (f+g)(x)$$

$$b) (f-g)(x)$$

$$c) (fg)(x)$$

$$d) \left(\frac{f}{g}\right)(x)$$

99. Let  $f(x) = 2x^2 + 3$  and  $g(x) = 3x - 4$ . Find each of the following and give the domain

$$a) (f+g)(x)$$

$$b) (f-g)(x)$$

$$c) (fg)(x)$$

$$d) \left(\frac{f}{g}\right)(x)$$

100. Let  $f(x) = x^2 - 2x - 3$  and  $g(x) = x^2 + 3x - 2$ . Find each of the following and give the domain

$$a) (f+g)(x)$$

$$b) (f-g)(x)$$

$$c) (fg)(x)$$

$$d) \left(\frac{f}{g}\right)(x)$$



**101.** Let  $f(x) = \sqrt{4x-1}$  and  $g(x) = \frac{1}{x}$ . Find each of the following and give the domain

a)  $(f+g)(x)$       b)  $(f-g)(x)$       c)  $(fg)(x)$       d)  $\left(\frac{f}{g}\right)(x)$

**102.** Find  $(f+g)(x)$ ,  $(f-g)(x)$ ,  $(f \cdot g)(x)$ , and  $(f/g)(x)$  and the domain of

$$f(x) = \sqrt{3-2x}, \quad g(x) = \sqrt{x+4}$$

**103.** Find  $(f+g)(x)$ ,  $(f-g)(x)$ ,  $(f \cdot g)(x)$ , and  $(f/g)(x)$  and the domain of

$$f(x) = \frac{2x}{x-4}, \quad g(x) = \frac{x}{x+5}$$

**104.** Let  $f(x) = \sqrt{4x-1}$  and  $g(x) = \frac{1}{x}$ . Find each of the following and give the domain

e)  $(f+g)(x)$       f)  $(f-g)(x)$       g)  $(fg)(x)$       h)  $\left(\frac{f}{g}\right)(x)$

**105.** Given that  $f(x) = x+1$  and  $g(x) = \sqrt{x+3}$

- a) Find  $(f+g)(x)$
- b) Find the domain of  $(f+g)(x)$
- c) Find:  $(f+g)(6)$

**106.** Given that  $f(x) = x^2 - 4$  and  $g(x) = x+2$

- a) Find  $(f+g)(x)$  and its domain
- b) Find  $(f/g)(x)$  and its domain

**107.** Find  $(f \circ g)(x)$ ,  $(g \circ f)(x)$ ,  $f(g(-2))$  and  $g(f(3))$

$$f(x) = 2x^2 + 3x - 4, \quad g(x) = 2x - 1$$

**108.** Find  $(f \circ g)(x)$ ,  $(g \circ f)(x)$ ,  $f(g(-2))$  and  $g(f(3))$

$$f(x) = x^3 + 2x^2, \quad g(x) = 3x$$

**109.** Find  $(f \circ g)(x)$ ,  $(g \circ f)(x)$ ,  $f(g(-2))$  and  $g(f(3))$

$$f(x) = |x|, \quad g(x) = -7$$

(110 – 139) For the given function; find:

a) Find  $(f \circ g)(x)$  and the **domain** of  $f \circ g$

b) Find  $(g \circ f)(x)$  and the **domain** of  $g \circ f$

110.  $f(x) = x - 3$  and  $g(x) = x + 3$
111.  $f(x) = \frac{2}{3}x$  and  $g(x) = \frac{3}{2}x$
112.  $f(x) = x - 1$  and  $g(x) = 3x^2 - 2x - 1$
113.  $f(x) = 3x - 2$  and  $g(x) = x^2 - 5$
114.  $f(x) = x^2 - 2$  and  $g(x) = 4x - 3$
115.  $f(x) = 4x^2 - x + 10$  and  $g(x) = 2x - 7$
116.  $f(x) = \sqrt{x}$  and  $g(x) = x + 3$
117.  $f(x) = \sqrt{x}$  and  $g(x) = 2 - 3x$
118.  $f(x) = 3x + 2$  and  $g(x) = \sqrt{x}$
119.  $f(x) = x^4$  and  $g(x) = \sqrt[4]{x}$
120.  $f(x) = x^n$  and  $g(x) = \sqrt[n]{x}$
121.  $f(x) = x^2 - 3x$  and  $g(x) = \sqrt{x+2}$
122.  $f(x) = \sqrt{x-2}$  and  $g(x) = \sqrt{x+5}$
123.  $f(x) = x^2 + 2$  and  $g(x) = \sqrt{3-x}$
124.  $f(x) = x^5 - 2$  and  $g(x) = \sqrt[5]{x+2}$
125.  $f(x) = 1 - x^2$  and  $g(x) = \sqrt{x^2 - 25}$
126.  $f(x) = 2x + 3$  and  $g(x) = \frac{x-3}{2}$
127.  $f(x) = 4x - 5$  and  $g(x) = \frac{x+5}{4}$
128.  $f(x) = \frac{4}{1-5x}$  and  $g(x) = \frac{1}{x}$
129.  $f(x) = \frac{1}{x-2}$  and  $g(x) = \frac{x+2}{x}$
130.  $f(x) = \frac{1}{1+x}$  and  $g(x) = \frac{1-x}{x}$
131.  $f(x) = \frac{3x+5}{2}$  and  $g(x) = \frac{2x-5}{3}$
132.  $f(x) = \frac{x-1}{x-2}$  and  $g(x) = \frac{x-3}{x-4}$
133.  $f(x) = \frac{6}{x-3}$  and  $g(x) = \frac{1}{x}$
134.  $f(x) = \frac{6}{x}$  and  $g(x) = \frac{1}{2x+1}$
135.  $f(x) = 3x - 7$  and  $g(x) = \frac{x+7}{3}$
136.  $f(x) = \frac{2x+3}{x-4}$  and  $g(x) = \frac{4x+3}{x-2}$
137.  $f(x) = \frac{2x+3}{x+4}$  and  $g(x) = \frac{-4x+3}{x-2}$
138.  $f(x) = x + 1$  and  $g(x) = x^3 - 5x^2 + 3x + 7$
139.  $f(x) = x - 1$  and  $g(x) = x^3 + 2x^2 - 3x - 9$
140. Given that  $f(x) = 2x - 5$  and  $g(x) = x^2 - 3x + 8$ , find  $(f \circ g)(x)$ ,  $(g \circ f)(x)$  and their domain then find  $(f \circ g)(7)$
141. Given that  $f(x) = \sqrt{x}$  and  $g(x) = x - 1$ , find
- a)  $(f \circ g)(x) = f(g(x))$
- b)  $(g \circ f)(x) = g(f(x))$
- c)  $(f \circ g)(2) = f(g(2))$

**142.** Given that  $f(x) = \frac{x}{x+5}$  and  $g(x) = \frac{6}{x}$ , find

a)  $(f \circ g)(x) = f(g(x))$

b)  $(g \circ f)(x) = g(f(x))$

c)  $(f \circ g)(2) = f(g(2))$

**(143 – 167)** Determine whether  $f$  is even, odd, or neither

**143.**  $f(x) = 3x^4 + 2x^2 - 5$

**144.**  $f(x) = 8x^3 - 3x^2$

**145.**  $f(x) = \sqrt{x^2 + 4}$

**146.**  $f(x) = 3x^2 - 5x + 1$

**147.**  $f(x) = \sqrt[3]{x^3 - x}$

**148.**  $f(x) = |x| - 3$

**149.**  $f(x) = x^3 - \frac{1}{x}$

**150.**  $f(x) = -x^3 + 2x$

**151.**  $f(x) = x^5 - 2x^3$

**152.**  $f(x) = .5x^4 - 2x^2 + 6$

**153.**  $f(x) = .75x^2 + |x| + 4$

**154.**  $f(x) = x^3 - x + 9$

**155.**  $f(x) = x^4 - 5x + 8$

**156.**  $f(x) = x^3 + x$

**157.**  $g(x) = x^2 - x$

**158.**  $h(x) = 2x^2 + x^4$

**159.**  $f(x) = 2x^2 + x^4 + 1$

**160.**  $f(x) = \frac{1}{5}x^6 - 3x^2$

**161.**  $f(x) = x\sqrt{1-x^2}$

**162.**  $f(x) = x^2\sqrt{1-x^2}$

**163.**  $f(x) = 5x^7 - 6x^3 - 2x$

**164.**  $f(x) = 5x^6 - 3x^2 - 7$

**165.**  $f(x) = x^2 + 6$

**166.**  $f(x) = 7x^3 - x$

**167.**  $h(x) = x^5 + 1$

**168.**  $f(x) = \begin{cases} 2+x & \text{if } x < -4 \\ -x & \text{if } -4 \leq x \leq 2 \\ 3x & \text{if } x > 2 \end{cases}$

Find:  $f(-5)$ ,  $f(-1)$ ,  $f(0)$ , and  $f(3)$

**169.**  $f(x) = \begin{cases} -2x & \text{if } x < -3 \\ 3x-1 & \text{if } -3 \leq x \leq 2 \\ -4x & \text{if } x > 2 \end{cases}$

Find:  $f(-5)$ ,  $f(-1)$ ,  $f(0)$ , and  $f(3)$

**170.**  $f(x) = \begin{cases} x^3 + 3 & \text{if } -2 \leq x \leq 0 \\ x + 3 & \text{if } 0 < x < 1 \\ 4 + x - x^2 & \text{if } 1 \leq x \leq 3 \end{cases}$  Find:  $f(-5)$ ,  $f(-1)$ ,  $f(0)$ , and  $f(3)$

**171.**  $h(x) = \begin{cases} \frac{x^2 - 9}{x - 3} & \text{if } x \neq 3 \\ 6 & \text{if } x = 3 \end{cases}$  Find:  $h(5)$ ,  $h(0)$ , and  $h(3)$

**172.** Graph the piecewise function defined by  $f(x) = \begin{cases} 3 & \text{if } x \leq -1 \\ x - 2 & \text{if } x > -1 \end{cases}$

**173.** Sketch the graph  $f(x) = \begin{cases} x + 2 & \text{if } x \leq -1 \\ x^3 & \text{if } -1 < x < 1 \\ -x + 3 & \text{if } x \geq 1 \end{cases}$

**174.** Sketch the graph  $f(x) = \begin{cases} x - 3 & \text{if } x \leq -2 \\ -x^2 & \text{if } -2 < x < 1 \\ -x + 4 & \text{if } x \geq 1 \end{cases}$