Find the critical points of the following functions on the given intervals. Identify the absolute maximum and minimum values (if they exist).

1. 
$$f(x) = 2x^3 - 3x^2 - 36x + 12$$
 on  $(-\infty, \infty)$ 

**2.** 
$$f(x) = 2x \ln x + 10$$
 on  $(0, 4)$ 

Sketch the graph

3. 
$$f(x) = \frac{1}{2}x^4 - 3x^2 + 4x + 1$$

**4.** 
$$f(x) = \frac{\cos \pi x}{1 + x^2}$$
 on  $[-2, 2]$ 

5. 
$$f(x) = x(x-1)e^{-x}$$