

**Hypothesis testing** is a procedure, based on sample evidence and probability, used to test statements regarding a characteristic of one or more populations.

**Null Hypothesis:** The *null hypothesis*, denoted  $H_0$ , is a statement to be tested. The null hypothesis is a statement of no change, no effect or no difference and is assumed true until evidence indicates otherwise.

**Alternative Hypothesis:** The *alternative hypothesis*, denoted  $H_1$ , is a statement that we are trying to find evidence to support.

### Three ways to set up the null and alternative hypotheses

1. Equal versus not equal hypothesis (two-tailed test)

$H_0$  : parameter = some value

$H_1$  : parameter  $\neq$  some value

2. Equal versus less than (left-tailed test)

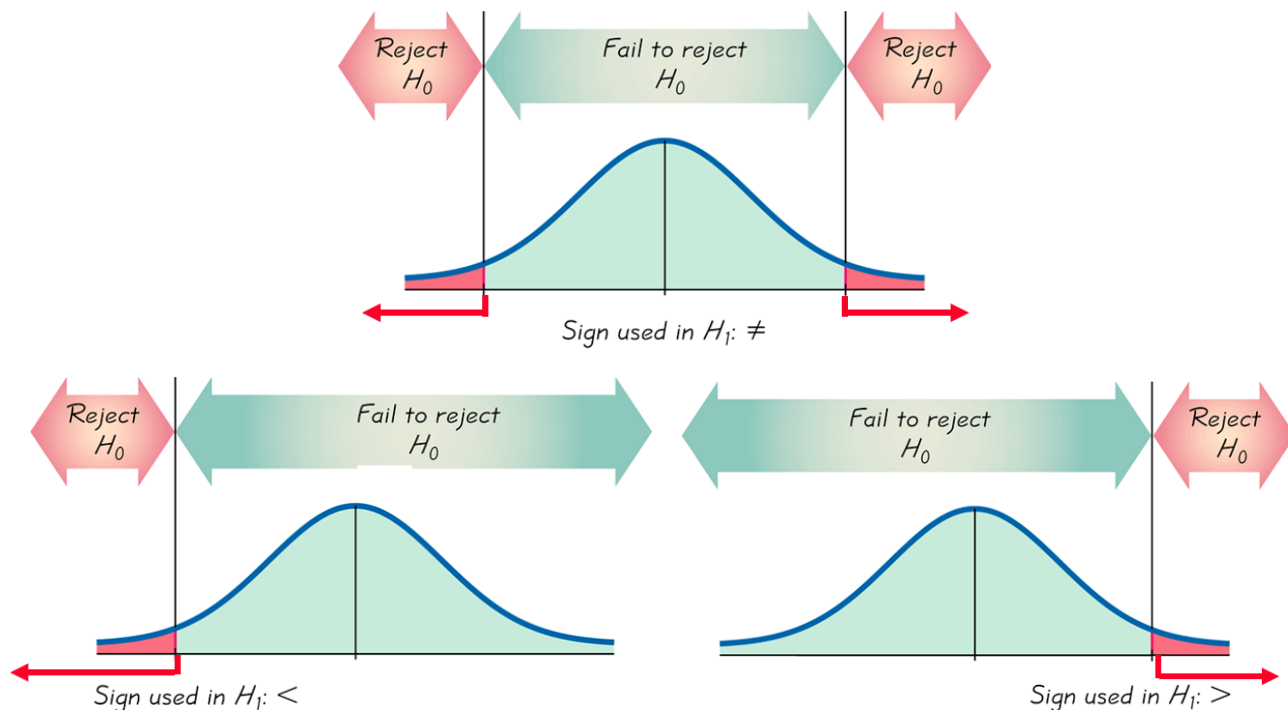
$H_0$  : parameter = some value

$H_1$  : parameter  $<$  some value

3. Equal versus greater than (right-tailed test)

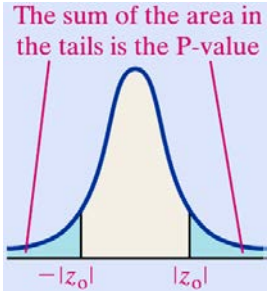
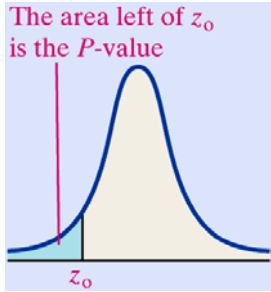
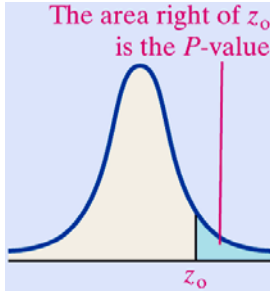
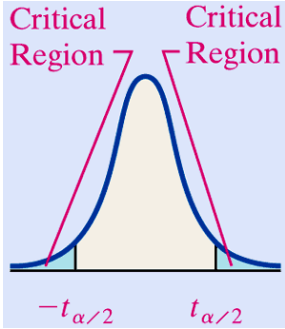
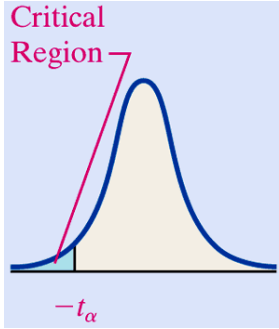
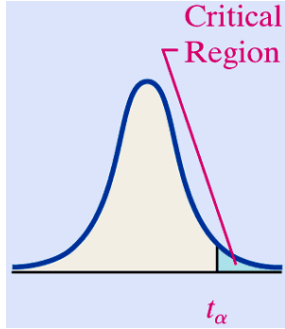
$H_0$  : parameter = some value

$H_1$  : parameter  $>$  some value



**If  $P\text{-value} < \alpha$ , reject the null hypothesis**

**If  $P\text{-value} > \alpha$ , fail to reject  $H_0$ .**

<i>Two-Tailed</i>	<i>Left-Tailed</i>	<i>Right-Tailed</i>
$H_1 : p \neq p_0$	$H_1 : p < p_0$	$H_1 : p > p_0$
$z_0 < -z_{\alpha/2} \text{ or } z_0 > z_{\alpha/2}$ <b>Reject the null hypothesis</b>	$z_0 < -z_{\alpha}$ <b>Reject the null hypothesis</b>	$z_0 > z_{\alpha}$ <b>Reject the null hypothesis</b>
		
$H_1 : \mu \neq \mu_0$	$H_1 : \mu < \mu_0$	$H_1 : \mu > \mu_0$
$t_0 < -t_{\alpha/2} \text{ or } t_0 > t_{\alpha/2}$ <b>Reject the null hypothesis</b>	$t_0 < -t_{\alpha}$ <b>Reject the null hypothesis</b>	$t_0 > t_{\alpha}$ <b>Reject the null hypothesis</b>
		
$H_1 : \sigma \neq \sigma_0$	$H_1 : \sigma < \sigma_0$	$H_1 : \sigma > \sigma_0$
$\chi_0^2 < \chi_{1-\alpha/2}^2 \text{ or } \chi_0^2 > \chi_{\alpha/2}^2$ <b>Reject the null hypothesis</b>	$\chi_0^2 < \chi_{1-\alpha}^2$ <b>Reject the null hypothesis</b>	$\chi_0^2 > \chi_{\alpha}^2$ <b>Reject the null hypothesis</b>
