

P : you have the flu

Q : you miss the final exam

a) $\neg P$: you don't have the flu

b) $P \wedge Q$ you have the flu and you miss the final

you miss the final exam because you have the flu

$$\neg P \wedge P \equiv P \wedge \neg P$$

P	$\neg P$	$\neg P \wedge P$
T	F	F
F	T	F

$$P \rightarrow \neg Q$$

P	Q	$\neg Q$	$P \rightarrow \neg Q$
T	T	F	F
T	F	T	T
F	T	F	T
F	F	T	T

$$p \leftrightarrow q \equiv (p \wedge q) \vee (\neg p \wedge \neg q)$$

p	q	$\neg p$	$\neg q$	$p \wedge q$	$\neg p \wedge \neg q$	$(p \wedge q) \vee (\neg p \wedge \neg q)$	$p \leftrightarrow q$
T	T	F	F	T	F	T	T
T	F	F	T	F	F	F	F
F	T	T	F	F	F	F	F
F	F	T	T	F	T	T	T

$$p \leftrightarrow q \equiv (p \wedge q) \vee (\neg p \wedge \neg q)$$

$N(x)$: ^{student} x has visited North Dakota

a) $\exists x N(x)$: there exists a student in your class has visited North Dakota

$\exists x \neg N(x)$: there exists a student in your class ^{has not} visited N.D.

$\neg \exists x N(x)$: No student in class has visited N.D.

$C(x)$: x has a cat x : student

$D(x)$: x has a dog

A student has a cat and a dog.

$$\exists x (C(x) \wedge D(x))$$

$$\forall x \forall y \exists z (x = y - z) \quad D: \mathbb{R}$$

for every x real number, and for every real numbers y , there exists a real number z such that $x = y - z$

Show square of even number is even number

$$n \text{ is even} \rightarrow n^2 \text{ is even}$$

$$n \text{ is even} \Rightarrow$$

$$n = 2k$$

$$n^2 = (2k)^2$$

$$= 4k^2$$

$$= 2(2k^2)$$

$$\therefore n \text{ is even} \Rightarrow n^2 \text{ is also even}$$

Venn diagram

A, B --- set

a_1, a_2, \dots or b_1, b_2, \dots are elements.

$$A \cap B, A \cup B, A - B, A \times B$$

$$A \cup \bar{A} = U \quad A \cap \bar{A} = \emptyset$$

$$A \subseteq B: \text{ let } x \in A, \text{ then } x \in B.$$

$$A = \{1, 2, 3, 4, 5\}$$

$$B = \{6, 7, 8, 9\}$$

$$A \cap B = \emptyset$$

$$A \cup B = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$$

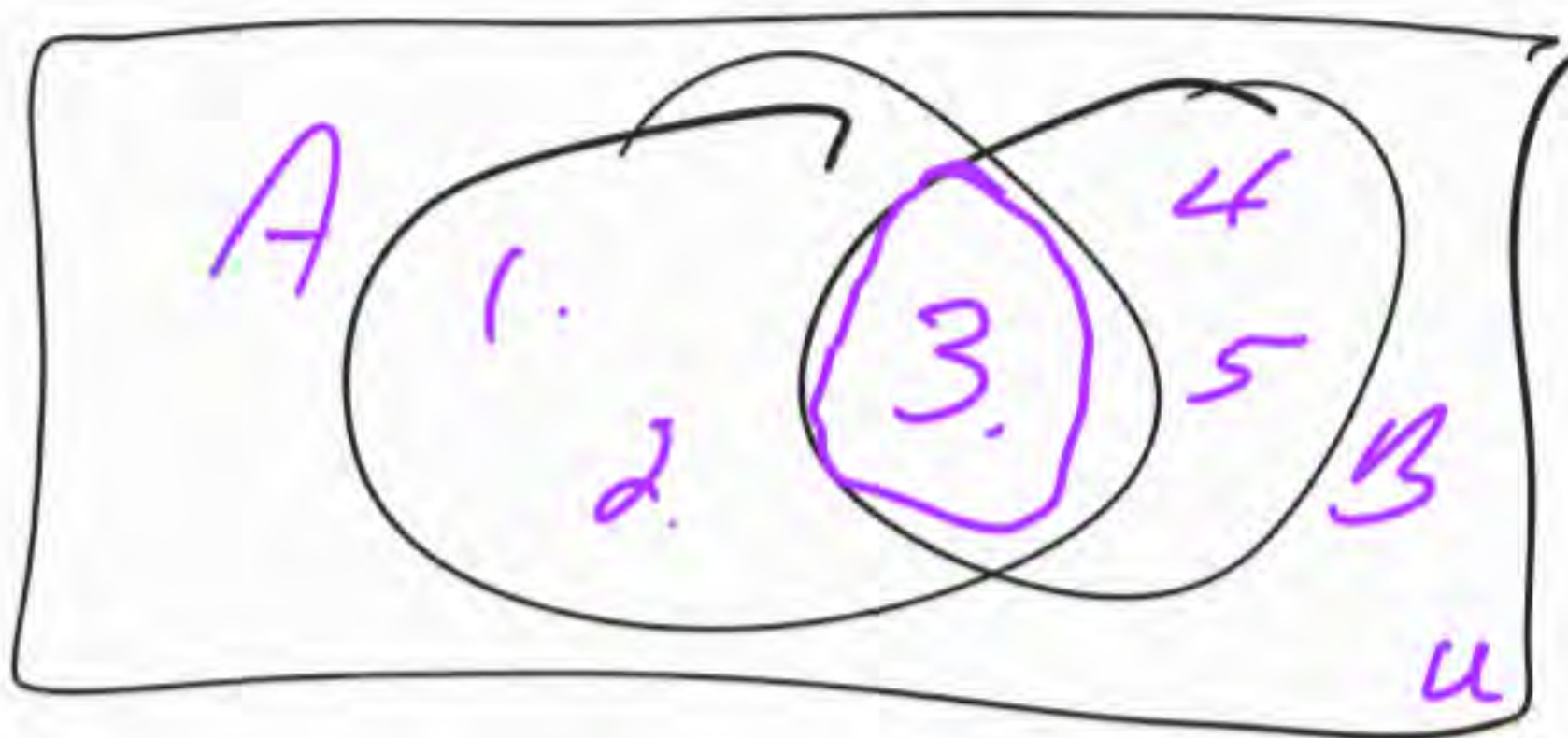
$$A = \{1, 2, 3\}$$

$$B = \{3, 4, 5\}$$

$$A - B = \{1, 2\}$$

$$B - A = \{4, 5\}$$

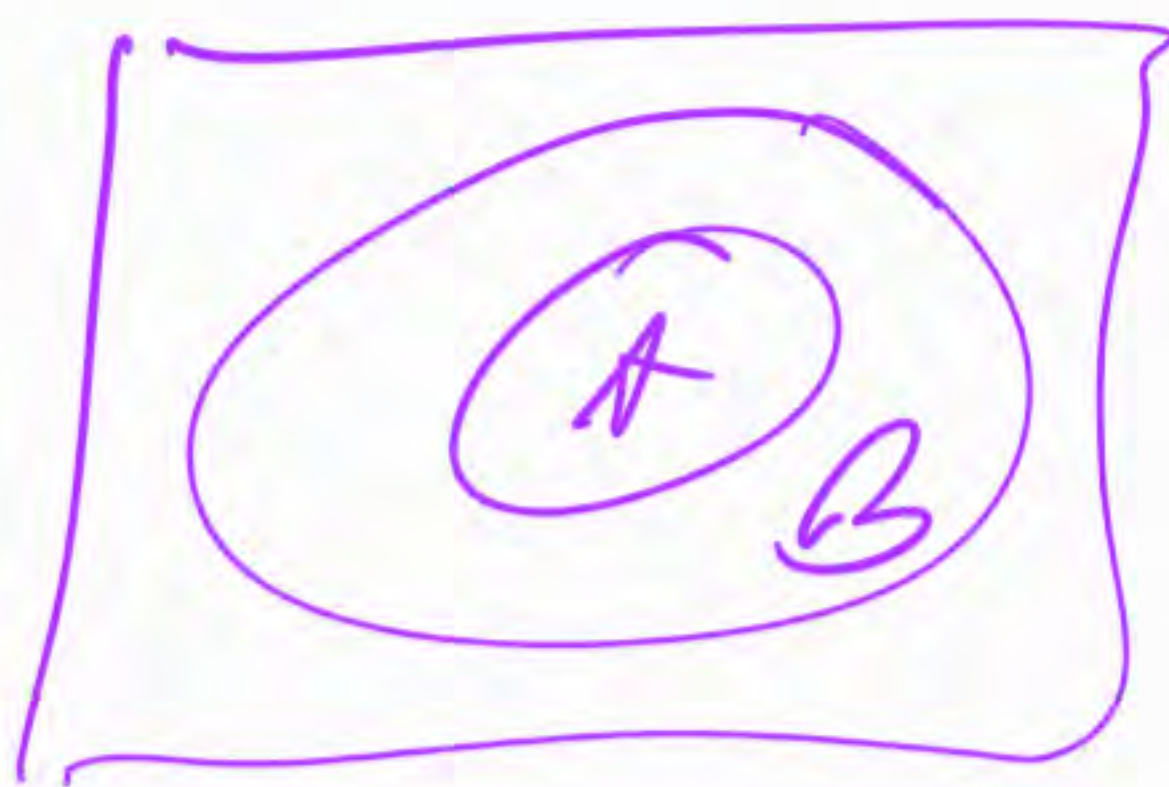
$$A \times B = \{(1, 3), (1, 4), (1, 5), (2, 3), (2, 4), (2, 5), (3, 3), (3, 4), (3, 5)\}$$



$$C \cap (B - A)$$



$$C \cap \bar{A}$$



$$A \subseteq B$$

you are not allowed to leave
Teams

Done → type conversation

Done, # pages.

< 1 minute

take pictures (low resolution)

wait email (?)? pages

that it is