3. If
$$\frac{1}{4}$$
 $\frac{1}{2}$ $\frac{1}{2}$

$$\lim_{x \to 0} \frac{x - \sin x}{x^{2}} = \frac{0}{0}$$

$$= \lim_{x \to 0} \frac{1 - \cos x}{3x^{2}} = \frac{0}{0}$$

$$= \lim_{x \to 0} \frac{\sin x}{6x} = 0$$

$$= \lim_{x \to 0} \frac{\cos x}{6}$$

$$= \frac{1}{6}$$

$$\lim_{x \to 0} \frac{\sin x}{6} = \frac{1}{6}$$

$$\lim_{x \to 0} \frac{\cos x}{6} = \frac{1}{6}$$

$$\lim_{x \to 0} \frac{1 - \cos x}{x + x^{2}} = \frac{1 - 1}{0} = \frac{0}{0}$$

$$\lim_{X\to 0} \frac{1-Cos_X}{X+x^2} = \frac{1-1}{o} = \frac{o}{o}$$

$$= \lim_{X\to 0} \frac{\sin x}{1+2x}$$

$$= \frac{o}{1}$$

$$= 0$$

$$\lim_{x \to 0} \frac{\sin x}{x^{2}} = \frac{0}{0}$$

$$= \lim_{x \to 0} \frac{\cos x}{2x}$$

$$= \frac{1}{0}$$

$$= \lim_{x \to 0^{-}} \frac{\sin x}{x^{2}} = \frac{0}{0}$$

$$= \lim_{x \to 0^{-}} \frac{\cos x}{2x}$$

$$= \lim_{x \to 0^{-}} \frac{\cos x}{2x}$$

$$= \lim_{x \to 0^{-}} \frac{\sec x}{x^{2}} = \frac{\sin x}{\sec x}$$

$$= \lim_{x \to 0^{-}} \frac{\sin x}{\sec x}$$

$$= \lim_{x \to 0^{-}} \frac{\sin x}{\cos x} \cdot \frac{\cos x}{\cos x}$$

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$$= \lim_{x \to 0^{-}} \frac{\sin x}{\cos x} \cdot \frac{\cos x}{\cos x}$$

$$\lim_{x \to \infty} \frac{1}{2\sqrt{x}} = \frac{1}{20}$$

$$= \lim_{x \to \infty} \frac{1}{\sqrt{x}}$$

$$\lim_{x \to 0^{+}} \sqrt{x} \ln x = 0 \ (-\infty)$$

$$= \lim_{x \to 0^{+}} \frac{\ln x}{\sqrt{x}}$$

$$= \lim_{x \to 0^{+}} \frac{1}{\sqrt{x}}$$

$$= \lim_{x \to 0^{+}} \frac{1}{\sqrt{x}} \frac{x^{2}}{x}$$

$$= -2 \lim_{x \to 0^{+}} x^{2}$$

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$$= -2 \lim_{x \to 0^{+}} x^{2}$$

$$= \lim_{x \to 0} \frac{x - \sin x}{x}$$

$$= \lim_{x \to 0} \frac{1 - \cos x}{2 \sin x + x \cos x} = 0$$

$$= \lim_{x \to 0} \frac{\sin x}{\cos x + \cos x - x \sin x}$$

$$= \lim_{x \to 0} \frac{\sin x}{2 \cos x - x \sin x}$$

$$= 0$$

$$= 0$$

In determinate Fower If him in for = L lum f(x) = lum e luf(x) x-sa x+a = 64 lim (1+x) = e Prove lim (1+x) = 100 f (x) = (/+x) 1/x lum lu fa) = limbre (1+x) = lim + lu(1+x) }# $=\lim_{x\to 0^+}\frac{\ln(1+x)}{x}=\frac{0}{n}$ = lim 1+x lim la (1+x) = 1 lum (1+x) = e 1 x > 0+.

$$\lim_{x\to\infty} x = \infty$$

$$\lim_{x\to\infty} \ln x = \lim_{x\to\infty} \frac{\ln x}{x} = \infty$$

$$= \lim_{x\to\infty} \frac{1}{x}$$

$$= \lim_{x\to\infty} \frac{3}{x}$$

= 3

#10
$$\lim_{x\to 0} \frac{x^2}{\ln(\sec x)} = \frac{0}{0}$$

$$= \lim_{x\to 0} \frac{2x}{\sec x}$$

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$$= \lim_{x\to 0} \frac{2x}{\sec x}$$

$$= \lim_{x\to 0} \frac{2}{\sec x}$$

$$= \lim_{x\to 0} \frac{(\cos x) \ln 3}{\sin x} = \lim_{x\to 0} \frac{(\cos x) \ln 3}{\sin x} = \lim_{x\to 0} \frac{(\cos x) \ln 3}{\sin x} = \lim_{x\to 0} \frac{2e^x(e^x - 1)}{\sin x + x \cos x} = 0$$

$$= \lim_{x\to 0} \frac{2e^x(e^x - 1)}{\sin x + x \cos x} = 0$$

$$= \lim_{x\to 0} \frac{2e^x - e^x}{\sin x + x \cos x}$$

$$= \lim_{x\to 0} \frac{2e^x - e^x}{\sin x + x \cos x}$$

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If
$$lon \frac{x^{2}-1}{x-1} = 0$$

$$= \lim_{x \to 1} \frac{nx^{n-1}}{1}$$

$$= n$$

$$= \lim_{x \to \infty} \frac{4x^{3}-2x^{3}+6}{7x^{3}+24} = \frac{x}{20}$$

$$= \lim_{x \to \infty} \frac{4x^{3}}{7x^{3}}$$

$$= \lim_{$$

X-s # (Deix) can x = 1 - lim lu (seix) tanx - lom faix fi (sinx) = lim (sinx) = 0 x = 1 t Cotx $= \lim_{X \to \overline{D}^+} \frac{\cos x}{-\csc^2 x} \to \frac{1}{\sin^2 x}$ =- lim (0)x sin3 = - lom Coox sinx

 $\lim_{x \to \frac{11}{x}} + (\sin x)^{\frac{1}{2}} = e^0 = 1$

Review

3.1 # 16
$$f(x) = x^3 - 3x^2$$
 [0,4]

 $f'(x) = 3x^2 - 6x = 0$
 $3x(x-2) = 0$

C.N: $x = 0, 2$
 $x \mid f^{(a)} \mid 0 \mid 0$
 $2 - 4 \rightarrow Abs. Min (2, -4)$
 $4 \mid 16 \rightarrow abs. Max (4, 16)$

10 $f(x) = \frac{1}{(x+2)^2} \neq 0$

Mo abs. extreme.

$$\begin{cases}
(x) = 2 \cos 2x = 0 \\
2x = \pm \frac{\pi}{2} \cdot \frac{(2nn)\pi}{2} \\
x = \pm \frac{\pi}{4} \cdot \frac{(2nn)\pi}{4} \\
x = -\frac{\pi}{4} \cdot \frac{\pi}{4} \cdot \frac{3\pi}{4} \cdot \frac{3\pi}{4}$$

11
$$\int cx = x^3 e^{-x} \left[-1, 5\right]$$

$$\begin{cases}
(x) = 3x^2 e^{-x} - x^3 e^{-x} \\
= (3x^2 - x^3)e^{-x} = 0
\end{cases}$$

$$x^2(3-x) = 0 \Rightarrow CN : x = 0, 3$$

$$\frac{x}{|x|} = 3abs. Min (-1, -e)$$

$$0 0$$

$$3 27/e^3$$

$$5 \frac{5^3}{5^3} = abs. Max (5, \frac{5^3}{6^3})$$

23 $f(x) = 2x \ln x + 10$ (0,4) $f'(x) = 2 \ln x + 2x \frac{1}{x}$ $= 2 \ln x + 2 = 0 \Rightarrow \ln x = -1$ $0.N : x = e^{-1}$ $f(\frac{1}{e}) = 2\frac{1}{e} \ln e^{-1} + 10$ $= 10 - \frac{2}{e}$ $abs Min : (\frac{1}{e}, 10 - \frac{2}{e})$