$$y' + 3y = e^{2x}$$

$$f(0) = -1$$

$$f(y' + 3y) = f(0) + 3/(5) = \frac{1}{5-2}$$

$$(5+3) / (5) = \frac{1}{5-2} - 1 = \frac{5+3}{(5+3)(5-2)}$$

$$/ (5) = \frac{1}{(5-2)(5+3)} - \frac{1}{(5+3)}$$

$$\frac{1}{5-1} + \frac{1}{5+3} \Rightarrow f(5+3) + 105 - 20 = 1$$

$$\frac{1}{5-1} + \frac{1}{5-2} \Rightarrow \frac{1}{5-2} = 1$$

$$\frac{1}{5-2} + \frac{1}{5-2} = \frac{1}{5-2}$$

$$\frac{1}{5-2} + \frac{1}{5-2} = \frac{1}{5-2} = \frac{1}{5-2} = \frac{1}{5-2}$$

$$\frac{1}{5-2} + \frac{1}{5-2} = \frac{1}{$$

 $X'' + 4x' + 4x = t^2$  X(0) = X'(0) = 0£ } x"+4x"+4x3 = £ { +23 (-52+45-4) X (5) = -2  $\chi(s) = \frac{2}{5^3 + 5 + 21^2}$  $\frac{17}{5} + \frac{15}{5^2} + \frac{1}{5^2} + \frac{1}{5+2} + \frac{1}{(5+2)^2} = \frac{2}{3}$ A52(5,48+4)+B5(52+45+4) + C(52+45+4) + D 53(5+2) + E 53=2 +D 53 4A +B +2D+6:00 52 4A+4B+C =0 0 +4B+4C = 0 > 13=-131 +40 22 ~ C=1 D=-3 (2) 5 = - 3 + 1 + 3 = -4) 1 7x(s)3= 31/3-1 2(43-1 27/4) - 3 x-1/5-2) - 4 x / 5-2)

$$\begin{cases}
y'' + uy' + by = sin f \\
y'(0) = 0
\end{cases}$$

$$\begin{cases}
y'' + uy' + by = f \\
y'' + by + f \\
y'' + by = f \\
y'' + by + f \\
y''$$

$$\frac{1}{5} = \frac{4}{5} \frac{5}{5^{2}+1} + \frac{7}{65} \frac{1}{5^{2}+1} + \frac{1}{65} \frac{695 + 269}{(5+2)^{2}+44}$$

$$\frac{1}{5} \frac{1}{5} \frac{1}{5} \frac{1}{5} + \frac{7}{65} \frac{1}{5} \frac{1}{5^{2}+1} + \frac{7}{65} \frac{1}{5} \frac{1}{5^{2}+1} \frac{1}{5} \frac{1}{5$$

$$X_{1}'(A) = 2X_{1} + 2X_{2}$$

$$X_{2}'(A) = X_{1} + 3X_{2}$$

$$1 = \begin{pmatrix} 2 & 2 \\ 1 & 3 \end{pmatrix}$$

$$|A - \lambda I|^{2} = |A - \lambda I|$$

$$= \lambda^{2} - 5\lambda + 4 = 0$$

$$C'' \text{ fon value}: \ A_{1,2} = 1, 4$$

$$Fin \ A_{1} = 1 \Rightarrow (A - \lambda I) V_{1} = 0$$

$$\begin{pmatrix} 1 & 2 \\ 2 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \Rightarrow x = -2y$$

$$V_{1}' = \begin{pmatrix} A \\ 1 \end{pmatrix}$$

$$V_{1}' = \begin{pmatrix} A \\ 1 \end{pmatrix}$$

$$V_{2}' = \begin{pmatrix} A \\ 1 \end{pmatrix} = \begin{pmatrix} 0 \\ 1 \end{pmatrix} \Rightarrow x = -2y$$

$$X(A) = \begin{pmatrix} -2 \\ 1 \end{pmatrix} e^{4} + C \begin{pmatrix} 1 \\ 1 \end{pmatrix} e^{4}$$

$$X(B) = \begin{pmatrix} -2 \\ 1 \end{pmatrix} e^{4} + C \begin{pmatrix} 1 \\ 1 \end{pmatrix} e^{4}$$

$$X(B) = \begin{pmatrix} -2 \\ 1 \end{pmatrix} e^{4} + C \begin{pmatrix} 1 \\ 1 \end{pmatrix} e^{4}$$

$$C(A) = \begin{pmatrix} -2 \\ 1 \end{pmatrix} e^{4} + C \begin{pmatrix} 1 \\ 1 \end{pmatrix} e^{4}$$

$$C(A) = \begin{pmatrix} -2 \\ 1 \end{pmatrix} e^{4} + C \begin{pmatrix} 1 \\ 1 \end{pmatrix} e^{4}$$

$$C(A) = \begin{pmatrix} -2 \\ 1 \end{pmatrix} e^{4} + C \begin{pmatrix} 1 \\ 1 \end{pmatrix} e^{4}$$

$$|X_{1}| = 3x_{1} - X_{2} \qquad X_{1}(0) = 2$$

$$|X_{2}| = X_{1} + X_{2} \qquad X_{2}(0) = -1$$

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$$\begin{pmatrix} C_{1}+1 \\ C_{2} \end{pmatrix} = \begin{pmatrix} 2 \\ -1 \end{pmatrix} \Rightarrow C_{2} = -1$$

$$X(t) = \begin{pmatrix} -t + 2 \\ -1 \end{pmatrix} e^{2t}$$

$$(1-2I) V_{i} = 0$$

$$(1-1) (x) = (0) \qquad x = y$$

$$(1-1) (y) = (0) \qquad x = y$$

$$V_{i} = (1) e^{2k}$$

$$x(t) : \left( C_{1} \begin{pmatrix} 1 \\ 1 \end{pmatrix} + C_{2} \begin{pmatrix} 1 \\ 1 \end{pmatrix} t + \begin{pmatrix} 1 \\ 1 \end{pmatrix} \right) = 2t$$

$$= \left( C_{2}t + C_{1} + C_{2} \right) e^{2t}$$

$$C_{2}t + C_{1}$$

$$\begin{pmatrix} C_1 + C_2 \\ C_1 \end{pmatrix} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$\begin{pmatrix} C_1 + C_2 \\ C_1 \end{pmatrix} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$\begin{pmatrix} C_1 = -1 \\ C_2 = 3 \\ 3+ -1 \end{pmatrix}$$

$$= \begin{pmatrix} 3+2 \\ 3+2 \end{pmatrix}$$

$$(2) \quad (3)$$

$$\begin{cases}
 \lambda_{1}(A) = 6x_{1} - x_{2} \\
 X_{2}(A) = 5x_{1} + 2x_{2}
 \end{cases}$$

$$\begin{cases}
 A = 6 - 1 \\
 A = 6 - 2
 \end{cases}$$

$$\begin{cases}
 A - 72/ = 6 - 2 - 1 \\
 A = 6 - 2
 \end{cases}$$

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