

Directions: Show your work whenever possible: a correct answer is worth 0 point without any supporting work.

1. Evaluate $\int_1^{\ln 8} \int_0^{\ln 4} \int_0^{\ln 2} e^{-x-y-2z} dx dy dz$

2. Evaluate $\int_0^{\pi/2} \int_0^1 \int_0^{\pi/2} \sin \pi x \cos y \sin 2z dy dx dz$

3. Evaluate $\int_0^{2\pi} \int_0^{\pi/2} \int_0^{2\cos \varphi} \rho^2 \sin \varphi d\rho d\varphi d\theta$

4. Evaluate the integrals in cylindrical coordinates $\int_{-2}^2 \int_{-1}^1 \int_0^{\sqrt{1-z^2}} \frac{1}{(1+x^2+z^2)^2} dx dz dy$

5. Find the volume of the cap of a sphere of radius R with height h .

