Geometric Seures: Zarn-1 5 = 1-2 if M = 1 -s converges. .7 M31 -> diverses 2 = 20 7 (-1)15 2 5 (-1)n \$ = 5 = 5 By the Geometric Sones, the given sewes Conveyes of Sum of 4 Divergent Series Zan conveyes, then (an)

Sy the obversent sens, the given sewes diverses

1 2/2 is By the diversent series, the given series diverses Es: \(\sum \text{(-1)}^{n+1} \), diverges because \(\text{g.ven seurs} \)
doesn't exist $\frac{\nabla x}{n=1} = \frac{n}{2n+5} = \frac{n}{2n+5} \longrightarrow -\frac{1}{2} + 0.$ By the divergent Series, the given sewes diverges $\frac{E}{1}$ $\frac{3^{n-1}}{6^{n-1}} = \frac{1}{6^{n-1}} \left(\frac{3^{n-1}}{6^{n-1}} - \frac{1}{6^{n-1}} \right)$ $= \sum_{n=1}^{\infty} \left(\frac{3}{6}\right)^{n-1} - \sum_{n=1}^{\infty} \left(\frac{1}{6}\right)^{n-1}$ = [(=)] - [(=)] - [(=)] - [(=)] - [(=)] |r|= 1/2 < 1 (N= = = = 1 $5 = \frac{1}{1 - \frac{7}{2}} - \frac{7}{1 - \frac{7}{6}}$ = 2 - 6 : By the Geometric serves, the given serves Converges w/ sum = #

3.3 Internal Test. $\int_{1}^{\infty} \frac{1}{n^2} conveyeo?$ $\int_{1}^{\infty} \frac{1}{x^2} dx = -\frac{1}{x} \int_{1}^{\infty}$ = -(o-1) = 1Premes. In 1 pt PXI s diverges. 2 / na 1 poast - By p-sens, the given sense converges $\int_{1}^{\infty} \frac{1}{n^2 + 1} = \int_{1}^{\infty} \frac{1}{x^2 + 1} = \int_{1}^{\infty} \frac{1}{x$ i. By the integral Test, the given series conveyes # 2 1

:. By p- serves, the given serves diverges

#17 5 15 2=5>1 :. By the p-sews, the green sewes conveyes 4) -1 (lun)2 So dx = So d(lux)2 = - (tus - tuz) = Eua By the integral Test, the given sense converges #5 5 2 5 x 2 = x/3 (3x 2 - 18x - 54) + 2 +27 EX/3 = 0 - e = (-3 - w-5u) = 75 :. By the integral Test, the given serves Converges.

3.4 Comparison Test Zan, Zen Zdin do san sca If I'm converges & Ian converges of Idn diverges - I an diverges Ex. I 5n-1 5n > 5n-1 $\frac{1}{5n}$ < $\frac{1}{5n-1}$ $\frac{5}{5n-1} > \frac{5}{5n}$ = 1; P=1 &1 diverges by p-suies -. By the Companison Test, the given senes diverses Limit Comparison Test. an >0 6n>0 1. If him an = C>0 - Zan + Zbn diverse an -> 0 Zb, conveyes as Za, conveyes diverses = s diverses

3. + 5 + 7 + 7 + --- = 2 = 20+1)2 (n+1)2 an= 21+1 (b) = 21 = 2) lum an - 1211. = him 202 Ib, = 1: P=131 dureyes by N-seurs 1. Bythe Limit Companison Ted, the given senes oliverses 21-1 < 2" $\frac{1}{2^{\frac{1}{2}}} \rightarrow \frac{1}{2^{n}} \qquad b_{n} = \frac{1}{2^{n}} \rightarrow 0$ lor an = lor 221 . 2 = lum 2" - By the Count Comparison Test, the gover

senes anverges

= x 1+ n En n an = 1+n lnn bn = n lnn = lnn > 1 P=151; Z-bn diverges by P-ser lum an = lum 1+1 lon . 1 = ling nalun = line lun : By the Limit Comparison Test, the given senes direges 1 = 2 n3/2 x -3/2 lux dx J: lux -> x=ed dx=e dy = fre dy $= \int y e^{-y/3} dy$ $= (-2y - u)e^{-x/2} \int_{-\infty}^{\infty}$ = 0 - (-4-4)e-1 = = | :. By the Integral Test, the given senes

(x2+1) Cos x × (x2+1) 12+30>n2 ip=2>1 conveyes n2430 < 1/2 by p-senes 1dy the Companison Test, the girica seves converges n4+2>n4 $\frac{1}{n^{4}12} < \frac{1}{n^{4}}$ $\frac{n-1}{n^{4}+2} < \frac{n-1}{n^{4}}$ - n 4 = 1/3 P=3>1 = converges by p-serving By Au Compaison Test, the given seico comoises

#60 JE1) k sin t -1 < sin & 5/ -k show + sk lom k = 20 . By Companison Test, the given serves diverges #63 <u>Coon</u> -1 < (00 n < 1 $-\frac{1}{n^3} \le \frac{\cos n}{n^3} \le \frac{1}{n^3}$ Ins: P=3>1 converges by P-sends . . Ag the Companison Test, the given senis converges.