

1. Prove that the statement is true: $1 \cdot 1! + 2 \cdot 2! + 3 \cdot 3! + \dots + n \cdot n! = (n+1)! - 1$
2. Prove that the statement is true: $1^2 + 2^2 + 3^2 + \dots + n^2 = \frac{n(n+1)(2n+1)}{6}$
3. Prove that the statement is true: $1 + 2 + 3 + \dots + n + (n+1) = \frac{1}{2}(n+1)(n+2)$