# **Solution Section 7.6 – Polar Coordinates**

## Exercise

Convert to rectangular coordinates. (4, 30°)

#### **Solution**

$$x = r\cos\theta$$

$$= 4\cos 30^{\circ}$$

$$= 4\left(\frac{\sqrt{3}}{2}\right)$$

$$= 2\sqrt{3}$$

$$y = r\sin\theta$$

$$= 4\sin 30^{\circ}$$

$$= 4\left(\frac{1}{2}\right)$$

$$= 2$$

: The point  $(2\sqrt{3}, 2)$  in rectangular coordinates is equivalent to  $(4, 30^{\circ})$  in polar coordinates.

### Exercise

Convert to rectangular coordinates  $\left(-\sqrt{2}, \frac{3\pi}{4}\right)$ .

## **Solution**

$$x = -\sqrt{2} \cos \frac{3\pi}{4}$$
$$= -\sqrt{2} \left( -\frac{1}{\sqrt{2}} \right)$$
$$= 1$$
$$y = -\sqrt{2} \sin \frac{3\pi}{4}$$

$$y = -\sqrt{2} \sin \frac{1}{4}$$

$$= -\sqrt{2} \left( \frac{1}{\sqrt{2}} \right)$$

$$= -1$$

∴ The point (1, -1) in rectangular coordinates is equivalent to  $\left(-\sqrt{2}, \frac{3\pi}{4}\right)$  in polar coordinates.

Convert to rectangular coordinates (3, 270°).

#### **Solution**

```
x = 3\cos 270^{\circ}
= 3(0)
= 0
y = 3\sin 270^{\circ}
= 3(-1)
= -3
```

: The point (3, 270°) in polar coordinates is equivalent to (0, -3) in rectangular coordinates.

## Exercise

Convert to rectangular coordinates (2, 60°)

### **Solution**

$$x = 2\cos 60^{\circ}$$

$$= 2\left(\frac{1}{2}\right)$$

$$= 0$$

$$y = 2\sin 60^{\circ}$$

$$= 2\frac{\sqrt{3}}{2}$$

$$= \sqrt{3}$$

∴ The point  $(2, 60^{\circ})$  in polar coordinates is equivalent to  $(1, \sqrt{3})$  in rectangular coordinates.

## Exercise

Convert to rectangular coordinates  $(\sqrt{2}, -225^{\circ})$ 

$$x = \sqrt{2}\cos(-225^\circ)$$
$$= \sqrt{2}\left(-\frac{1}{\sqrt{2}}\right)$$
$$= -1$$
$$y = \sqrt{2}\sin(-225^\circ)$$

$$= \sqrt{2} \left( \frac{1}{\sqrt{2}} \right)$$

$$= 1$$

∴ The point  $(\sqrt{2}, -225^\circ)$  in polar coordinates is equivalent to (-1, 1) in rectangular coordinates.

### Exercise

Convert to rectangular coordinates  $\left(4\sqrt{3}, -\frac{\pi}{6}\right)$ 

#### **Solution**

$$x = 4\sqrt{3}\cos\left(-\frac{\pi}{6}\right)$$

$$= 4\sqrt{3}\left(\frac{\sqrt{3}}{2}\right)$$

$$= 6$$

$$y = 4\sqrt{3}\sin\left(-\frac{\pi}{6}\right)$$

$$= 4\sqrt{3}\left(-\frac{1}{2}\right)$$

$$= -2\sqrt{3}$$

 $\therefore$  The point  $\left(4\sqrt{3}, -\frac{\pi}{6}\right)$  in polar coordinates is equivalent to  $\left(6, -2\sqrt{3}\right)$  in rectangular coordinates.

#### Exercise

Change the polar coordinates to rectangular coordinates  $\left(-2, \frac{7\pi}{6}\right)$ 

#### **Solution**

$$x = -2\cos\left(\frac{7\pi}{6}\right)$$

$$= -2\left(-\frac{\sqrt{3}}{2}\right)$$

$$= \sqrt{3}$$

$$y = -2\sin\left(\frac{7\pi}{6}\right)$$

$$= -2\left(-\frac{1}{2}\right)$$

$$= 1$$

 $\therefore$  The point  $\left(-2, \frac{7\pi}{6}\right)$  in polar coordinates is equivalent to  $\left(\sqrt{3}, 1\right)$  in rectangular coordinates.

Change the polar coordinates to rectangular coordinates  $\left(6, \arctan \frac{3}{4}\right)$ 

**Solution** 

$$\arctan \frac{3}{4} = \beta \implies \tan \beta = \frac{3}{4}$$

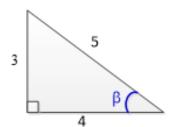
$$x = 2\cos\beta$$
$$= 2\left(\frac{4}{5}\right)$$

$$=\frac{8}{5}$$

$$y = 2\sin \beta$$

$$=2\left(\frac{3}{5}\right)$$

$$=\frac{6}{5}$$



∴ The point  $\left(6, \arctan \frac{3}{4}\right)$  in polar coordinates is equivalent to  $\left(\frac{8}{5}, \frac{6}{5}\right)$  in rectangular coordinates.

## Exercise

Change the polar coordinates to rectangular coordinates  $\left(10, \arccos\left(-\frac{1}{3}\right)\right)$ 

**Solution** 

$$\arccos\left(-\frac{1}{3}\right) = \alpha \implies \cos\alpha = -\frac{1}{3} \quad (QII)$$

$$x = 10\cos\alpha$$

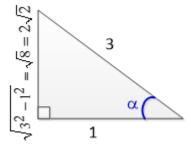
$$=10\left(-\frac{1}{3}\right)$$

$$=-\frac{10}{3}$$

$$y = 10\sin\alpha$$

$$=10\left(\frac{2\sqrt{2}}{3}\right)$$

$$=\frac{20\sqrt{2}}{3}$$



∴ The point  $\left(10, \arccos\left(-\frac{1}{3}\right)\right)$  in polar coordinates is equivalent to  $\left(-\frac{10}{3}, \frac{20\sqrt{2}}{3}\right)$  in rectangular coordinates.

Convert to polar coordinates (3, 3).

#### **Solution**

$$r = \sqrt{3^2 + 3^2}$$

$$= \sqrt{18}$$

$$= 3\sqrt{2}$$

$$\theta = \tan^{-1}\left(\frac{3}{3}\right)$$

$$= \tan^{-1}(1)$$

$$= 45^{\circ}$$

∴ The point (3, 3) in rectangular coordinates is equivalent to  $(3\sqrt{2}, 45^{\circ})$  in polar coordinates.

#### Exercise

Convert to polar coordinates (-2, 0).

#### **Solution**

$$r = \pm \sqrt{4+0}$$

$$= \pm 2$$

$$\theta = \tan^{-1} \frac{0}{-2}$$

$$= 0^{\circ}$$

∴ The point (-2, 0) in rectangular coordinates is equivalent to  $(-2, 0^\circ)$   $(2, 180^\circ)$  in polar coordinates.

### Exercise

Convert to polar coordinates  $(-1, \sqrt{3})$ .

#### **Solution**

$$r = \pm \sqrt{1+3}$$

$$= \pm 2$$

$$\theta = \tan^{-1} \left( \frac{\sqrt{3}}{-1} \right)$$

$$= 120^{\circ}$$

∴ The point  $\left(-1, \sqrt{3}\right)$  in rectangular coordinates is equivalent to  $\left(2, 120^{\circ}\right)$  in polar coordinates.

Convert to polar coordinates (-3, -3)  $r \ge 0$   $0^{\circ} \le \theta < 360^{\circ}$ 

#### **Solution**

$$r = \sqrt{(-3)^2 + (-3)^2}$$

$$= 3\sqrt{2}$$

$$\widehat{\theta} = \tan^{-1}\left(\frac{3}{3}\right)$$

$$= \tan^{-1}(1)$$

= 45°

The angle is in quadrant III

Therefore, 
$$\theta = 180^{\circ} + 45^{\circ}$$
  
=  $225^{\circ}$ 

∴ The point (-3, 3) in rectangular coordinates is equivalent to  $(3\sqrt{2}, 225^{\circ})$  in polar coordinates.

#### Exercise

Convert to polar coordinates  $\left(2, -2\sqrt{3}\right)$   $r \ge 0$   $0^{\circ} \le \theta < 360^{\circ}$ 

## Solution

$$r = \sqrt{2^2 + \left(-2\sqrt{3}\right)^2}$$

$$= 4$$

$$\hat{\theta} = \tan^{-1}\left(\frac{2\sqrt{3}}{2}\right)$$

$$= \tan^{-1}\left(\sqrt{3}\right)$$

$$= 60^{\circ}$$

The angle is in quadrant *IV* 

Therefore, 
$$\theta = 360^{\circ} - 60^{\circ}$$
  
=  $300^{\circ}$ 

∴ The point  $(2, -2\sqrt{3})$  in rectangular coordinates is equivalent to  $(4, 300^\circ)$  in polar coordinates.

Convert to polar coordinates (-2, 0)  $r \ge 0$   $0 \le \theta < 2\pi$ 

#### **Solution**

$$r = \sqrt{(-2)^2 + 0^2}$$

$$= 2 \rfloor$$

$$\hat{\theta} = \tan^{-1} \left(\frac{0}{2}\right)$$

$$= 0 \rfloor$$

$$\theta = \pi \rfloor$$

 $\div$  The point (-2, 0) in rectangular coordinates is equivalent to  $(2, \pi)$  in polar coordinates.

#### Exercise

Convert to polar coordinates  $\left(-1, -\sqrt{3}\right)$   $r \ge 0$   $0 \le \theta < 2\pi$ 

### **Solution**

$$r = \sqrt{(-1)^2 + (-\sqrt{3})^2}$$

$$= 2 \rfloor$$

$$\hat{\theta} = \tan^{-1} \left(\frac{\sqrt{3}}{1}\right)$$

$$= \frac{\pi}{3}$$

The angle is in quadrant *III* 

Therefore, 
$$\theta = \pi + \frac{\pi}{3}$$

$$= \frac{4\pi}{3}$$

 $\therefore$  The point  $\left(-1, -\sqrt{3}\right)$  in rectangular coordinates is equivalent to  $\left(2, \frac{4\pi}{3}\right)$  in polar coordinates.

### Exercise

Change the rectangular coordinates to polar coordinates  $(7, -7\sqrt{3})$  r > 0  $0 \le \theta < 2\pi$ 

$$r = \sqrt{(7)^2 + (-7\sqrt{3})^2}$$

$$=\sqrt{196}$$

$$\widehat{\theta} = \tan^{-1} \left( \frac{7\sqrt{3}}{7} \right)$$
$$= \frac{\pi}{3}$$

The angle is in quadrant IV; therefore,

$$\theta = 2\pi - \frac{\pi}{3}$$

$$= \frac{5\pi}{3}$$

 $\therefore$  The point  $\left(7, -7\sqrt{3}\right)$  in rectangular coordinates is equivalent to  $\left(14, \frac{5\pi}{3}\right)$  in polar coordinates.

## Exercise

Change the rectangular coordinates to polar coordinates  $\left(-2\sqrt{2}, -2\sqrt{2}\right)$  r > 0  $0 \le \theta < 2\pi$ 

## **Solution**

$$r = \sqrt{\left(-2\sqrt{2}\right)^2 + \left(-2\sqrt{2}\right)^2}$$

$$= 4$$

$$\hat{\theta} = \tan^{-1}\left(\frac{-2\sqrt{2}}{-2\sqrt{2}}\right)$$

$$= \tan^{-1}(1)$$

$$= \frac{\pi}{4}$$

The angle is in quadrant III; therefore,

$$\theta = \pi + \frac{\pi}{4}$$

$$= \frac{5\pi}{4}$$

 $\therefore$  The point  $\left(7, -7\sqrt{3}\right)$  in rectangular coordinates is equivalent to  $\left(4, \frac{5\pi}{4}\right)$  in polar coordinates.

The point (0, -3) in rectangular coordinates is equivalent to  $(3, 270^{\circ})$  in polar coordinates.

#### Solution

$$r = \sqrt{0 + (-3)^2}$$

$$= 3$$

$$\hat{\theta} = \tan^{-1} \frac{0}{3}$$

$$= 90^{\circ}$$

The polar point is  $(3, 270^{\circ})$ 

### Exercise

The point (1, -1) in rectangular coordinates is equivalent to  $\left(-\sqrt{2}, \frac{3\pi}{4}\right)$  in polar coordinates.

## **Solution**

$$r = \sqrt{(1)^2 + (-1)^2}$$

$$= \sqrt{2}$$

$$\widehat{\theta} = \tan^{-1}\left(\frac{1}{1}\right)$$

$$= \frac{\pi}{4}$$

$$\theta \in QIV \rightarrow \underline{\theta} = \frac{7\pi}{4}$$

$$\left(\sqrt{2}, \frac{7\pi}{4}\right) \Leftrightarrow \left(-\sqrt{2}, \frac{3\pi}{4}\right)$$

#### Exercise

A point lies at (4, 4) on a rectangular coordinate system. Give its address in polar coordinates  $(r, \theta)$ 

$$r = \sqrt{4^2 + 4^2}$$

$$= \sqrt{32}$$

$$= 4\sqrt{2}$$

$$\theta = \tan^{-1}\left(\frac{4}{4}\right)$$

$$= \tan^{-1}(1)$$

 $\therefore$  The point (4, 4) in rectangular coordinates is equivalent to  $(4\sqrt{2}, 45^{\circ})$  in polar coordinates.

## Exercise

Write the equation in rectangular coordinates  $r^2 = 4$ 

#### **Solution**

$$r^2 = 4$$
$$x^2 + y^2 = 4$$

#### Exercise

Write the equation in rectangular coordinates  $r = 6\cos\theta$ 

#### **Solution**

$$r = 6\cos\theta$$

$$r = 6\frac{x}{r}$$

$$r^2 = 6x$$

$$\frac{x^2 + y^2 = 6x}{r}$$

## Exercise

Write the equation in rectangular coordinates  $r^2 = 4\cos 2\theta$ 

$$r^{2} = 4\cos 2\theta$$

$$= 4\left(\cos^{2}\theta - \sin^{2}\theta\right)$$

$$= 4\left(\frac{x^{2}}{r^{2}} - \frac{y^{2}}{r^{2}}\right)$$

$$= 4\left(\frac{x^{2} - y^{2}}{r^{2}}\right)$$

$$r^{4} = 4\left(x^{2} - y^{2}\right)$$

$$\left(x^{2} + y^{2}\right)^{4} = 4x^{2} - 4y^{2}$$

Write the equation in rectangular coordinates  $r(\cos\theta - \sin\theta) = 2$ 

**Solution** 

$$r(\cos \theta - \sin \theta) = 2 \qquad \cos \theta = \frac{x}{r} \quad \sin \theta = \frac{y}{r}$$
$$r\left(\frac{x}{r} - \frac{y}{r}\right) = 2$$
$$r\left(\frac{x - y}{r}\right) = 2$$

x - y = 2

## Exercise

Write the equation in rectangular coordinates  $r^2 = 4\sin 2\theta$ 

**Solution** 

$$r^{2} = 4\sin 2\theta \qquad \sin 2\theta = 2\sin \theta \cos \theta$$

$$= 4(2\sin \theta \cos \theta) \qquad \cos \theta = \frac{x}{r} \sin \theta = \frac{y}{r}$$

$$= 8\left(\frac{y}{r}\right)\left(\frac{x}{r}\right)$$

$$= 8\frac{xy}{r^{2}}$$

$$r^{4} = 8xy \qquad r^{2} = x^{2} + y^{2}$$

$$\left(x^{2} + y^{2}\right)^{2} = 8xy$$

## Exercise

Find an equation in x and y that has the same graph as polar equation.  $r \sin \theta = -2$ 

$$r\sin\theta = -2$$

$$y = r\sin\theta$$

$$y = -2$$

Find an equation in x and y that has the same graph as polar equation.  $\theta = \frac{\pi}{4}$ 

## Solution

$$\tan \theta = \tan \frac{\pi}{4}$$

$$\frac{y}{r} = 1$$

$$y = x$$

## Exercise

Find an equation in x and y that has the same graph as polar  $r^2 \left( 4\sin^2 \theta - 9\cos^2 \theta \right) = 36$ 

## **Solution**

$$r^2 \left( 4\sin^2 \theta - 9\cos^2 \theta \right) = 36$$

$$\cos \theta = \frac{x}{r} \quad \sin \theta = \frac{y}{r}$$

$$r^2 \left( 4 \frac{y^2}{r^2} - 9 \frac{x^2}{r^2} \right) = 36$$

$$r^2\left(\frac{4y^2 - 9x^2}{r^2}\right) = 36$$

$$4y^2 - 9x^2 = 36$$

## Exercise

Find an equation in x and y that has the same graph as polar  $r^2 \left(\cos^2 \theta + 4\sin^2 \theta\right) = 16$ 

$$r^2\left(\cos^2\theta + 4\sin^2\theta\right) = 16$$

$$\cos\theta = \frac{x}{r} \quad \sin\theta = \frac{y}{r}$$

$$r^2 \left( \frac{x^2}{r^2} + 4 \frac{y^2}{r^2} \right) = 16$$

$$r^2\left(\frac{x^2+4y^2}{r^2}\right)=16$$

$$x^2 + 4y^2 = 16$$

Find an equation in x and y that has the same graph as polar  $r(\sin \theta - 2\cos \theta) = 6$ 

#### **Solution**

$$r\left(\sin\theta - 2\cos\theta\right) = 6$$

$$r\left(\frac{y}{r} - 2\frac{x}{r}\right) = 6$$

$$r\left(\frac{y - 2x}{r}\right) = 6$$

y - 2x = 6

$$\cos\theta = \frac{x}{r} \quad \sin\theta = \frac{y}{r}$$

## Exercise

Find an equation in x and y that has the same graph as polar  $r(\sin\theta + r\cos^2\theta) = 1$ 

## **Solution**

$$r\left(\sin\theta + r\cos^2\theta\right) = 1$$
$$r\left(\frac{y}{r} + r\frac{x^2}{r^2}\right) = 1$$

$$\cos \theta = \frac{x}{r}$$
  $\sin \theta = \frac{y}{r}$ 

$$r\left(\frac{y}{r} + \frac{x^2}{r}\right) = 1$$

$$r\left(\frac{y+x^2}{r}\right)=1$$

$$y + x^2 = 1$$

#### Exercise

Find an equation in x and y that has the same graph as polar  $r = 8 \sin \theta - 2 \cos \theta$ 

$$r = 8\sin\theta - 2\cos\theta$$

$$\cos\theta = \frac{x}{r} \quad \sin\theta = \frac{y}{r}$$

$$r = 8\frac{y}{r} - 2\frac{x}{r}$$

$$r^2 = 8y - 2x$$

$$r^2 = x^2 + y^2$$

$$x^2 + y^2 = 8y - 2x$$

Find an equation in x and y that has the same graph as polar  $r = \tan \theta$ 

## **Solution**

$$r = \tan \theta$$

$$x^2 + y^2 = \frac{y^2}{x^2}$$

$$x^4 + x^2y^2 = y^2$$

$$\sqrt{x^2 + y^2} = \frac{y}{x}$$

#### Exercise

Find a polar equation that has the same graph as the equation in x and y.  $y^2 = 6x$ 

### **Solution**

$$v^2 = 6x$$

$$x = r \cos \theta$$
  $y = r \sin \theta$ 

$$(r\sin\theta)^2 = 6(r\cos\theta)$$

$$r^2\sin^2\theta = 6r\cos\theta$$

$$r = 6 \frac{\cos \theta}{\sin^2 \theta}$$

#### Exercise

Find a polar equation that has the same graph as the equation in x and y. xy = 8

## **Solution**

$$xy = 8$$

$$x = r \cos \theta$$
  $y = r \sin \theta$ 

$$(r\cos\theta)(r\sin\theta) = 8$$

$$r^2 = \frac{8}{\cos\theta\sin\theta}$$

## Exercise

Find a polar equation that has the same graph as the equation in x and y.  $(x+2)^2 + (y-3)^2 = 13$ 

$$x^2 + 4x + 4 + y^2 - 6y + 9 = 13$$

$$x^{2} + 4x + y^{2} - 6y = 13 - 9 - 4$$

$$x^{2} + 4x + y^{2} - 6y = 0$$

$$x^{2} + y^{2} = 6y - 4x$$

$$r^{2} = 6r \sin \theta - 4r \cos \theta$$

$$r^{2} = r(6 \sin \theta - 4 \cos \theta)$$

$$r = 6 \sin \theta - 4 \cos \theta$$

$$r = 6 \sin \theta - 4 \cos \theta$$
Divide by r

Find a polar equation that has the same graph as the equation in x and y.  $y^2 - x^2 = 4$ 

#### **Solution**

$$y^{2} - x^{2} = 4$$

$$r^{2} \sin^{2} \theta - r^{2} \cos^{2} \theta = 4$$

$$r^{2} \left(\sin^{2} \theta - \cos^{2} \theta\right) = 4$$

$$\cos 2\alpha = \cos^{2} \alpha - \sin^{2} \alpha$$

$$r^{2} \left(-\cos 2\theta\right) = 4$$

$$\frac{r^{2} - \frac{4}{\cos 2\theta}}{\cos 2\theta}$$

#### Exercise

Write the equation in polar coordinates x + y = 5

#### **Solution**

$$x + y = 5$$

$$r\cos\theta + r\sin\theta = 5$$

$$r(\cos\theta + \sin\theta) = 5$$

$$r = \frac{5}{\cos\theta + \sin\theta}$$

#### Exercise

Write the equation in polar coordinates  $x^2 + y^2 = 9$ 

$$x^{2} + y^{2} = 9$$

$$r^{2} = 9$$

$$r^{2} = 9$$

Write the equation in polar coordinates  $x^2 + y^2 = 4x$ 

## **Solution**

$$x^2 + y^2 = 4x$$

$$r^2 = x^2 + y^2 \qquad x = r\cos\theta$$

$$r^2 = 4r\cos\theta$$

$$\frac{r^2}{r} = \frac{4r\cos\theta}{r}$$

$$r = 4\cos\theta$$

### Exercise

Write the equation in polar coordinates y = -x

## **Solution**

$$y = -x$$

$$x = r\cos\theta$$
  $y = r\sin\theta$ 

$$r\sin\theta = -r\cos\theta$$

$$\sin \theta = -\cos \theta$$

## Exercise

Write the equation in polar coordinates x + y = 4

$$x + y = 4$$

$$x + y = 4$$

$$r\cos\theta + r\sin\theta = 4$$

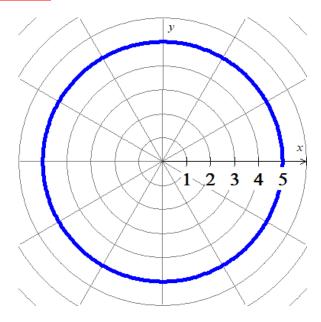
$$x = r\cos\theta$$
  $y = r\sin\theta$ 

$$r(\cos\theta + \sin\theta) = 4$$

$$r = \frac{4}{\cos\theta + \sin\theta}$$

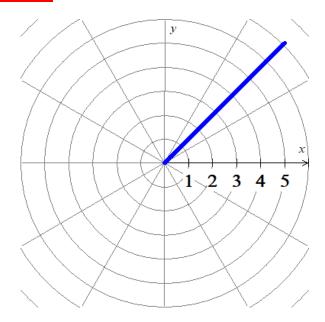
Sketch the graph of the polar equation r = 5

# **Solution**



# Exercise

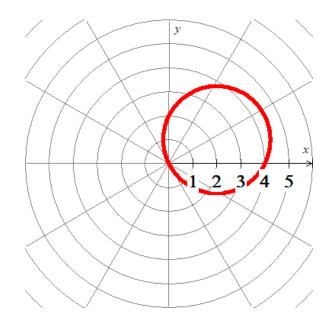
Sketch the graph of the polar equation  $\theta = \frac{\pi}{4}$ 



Sketch graph  $r = 4\cos\theta + 2\sin\theta$ 

# **Solution**

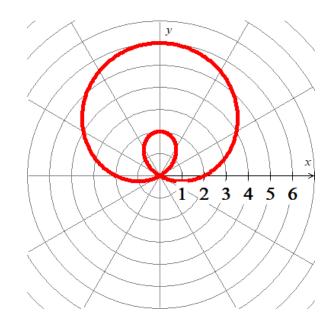
$\boldsymbol{\theta}$	r
0	4
$\frac{\pi}{4}$	$3\sqrt{2}$
$\frac{\pi}{2}$	2
$\frac{3\pi}{4}$	$-\sqrt{2}$
$\pi$	-4
$\frac{3\pi}{2}$	-2



# Exercise

Sketch the graph of the polar  $r = 2 + 4 \sin \theta$ 

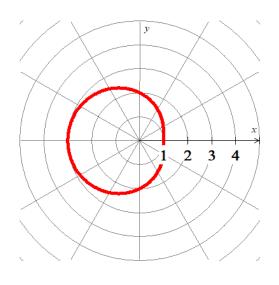
$\boldsymbol{\theta}$	r
0	2
$\frac{\pi}{6}$	4
$\frac{\pi}{4}$	$2+2\sqrt{2}$
$\frac{\pi}{2}$	6
$\frac{5\pi}{6}$	4
$\pi$	2
$\frac{7\pi}{6}$	0
$\frac{3\pi}{2}$	-2
$\frac{11\pi}{6}$	0



Sketch the graph  $r = 2 - \cos \theta$ 

# **Solution**

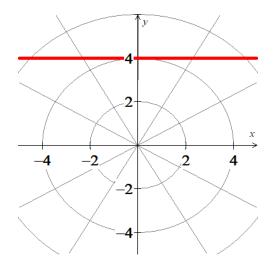
$\theta$	r
0	1
$\frac{\pi}{3}$	$\frac{3}{2}$
$\frac{\frac{\pi}{3}}{\frac{\pi}{2}}$ $\frac{2\pi}{3}$	2
$\frac{2\pi}{3}$	$\frac{5}{2}$
$\pi$	3
$\frac{4\pi}{3}$	3 <u>5</u> 2
$ \frac{4\pi}{3} $ $ \frac{3\pi}{2} $ $ \frac{5\pi}{3} $	2
$\frac{5\pi}{3}$	$\frac{3}{2}$



# Exercise

Sketch the graph  $r = 4 \csc \theta$ 

$$r = 4\csc\theta$$
$$= \frac{4}{\sin\theta}$$
$$r\sin\theta = \underline{4 = y}$$



Sketch the graph  $r^2 = 4\cos 2\theta$ 

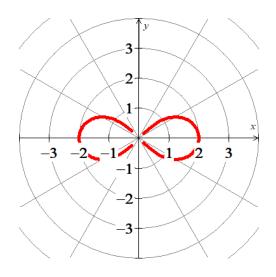
# **Solution**

$$r^{2} = 4\cos 2\theta \ge 0$$

$$-\frac{\pi}{2} \le 2\theta \le \frac{\pi}{2}$$

$$-\frac{\pi}{4} \le \theta \le \frac{\pi}{4} \quad \& \quad \frac{3\pi}{4} \le \theta \le \frac{5\pi}{4}$$

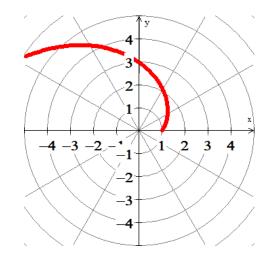
$\theta$	r
0	2
$\frac{\pi}{6}$	$\sqrt{2}$
$\frac{\pi}{4}$	0
$\frac{3\pi}{4}$	0
$\pi$	2
$\frac{5\pi}{4}$	0
$\frac{7\pi}{4}$	0

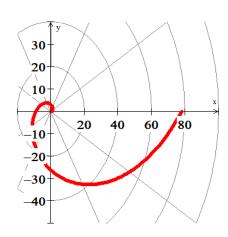


# Exercise

Sketch the graph  $r = 2^{\theta}$   $\theta \ge 0$ 

$\theta$	r
0	1
$\frac{\pi}{2}$	$2^{\pi/2}$

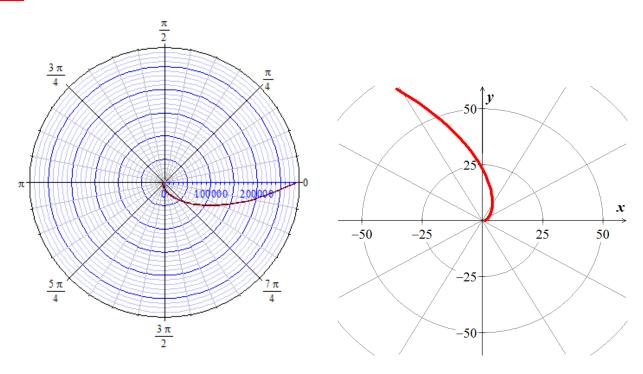




Sketch the graph of the polar equation

$$r = e^{2\theta} \quad \theta \ge 0$$

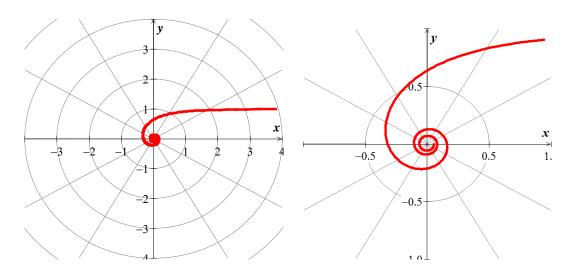
# **Solution**



# Exercise

Sketch the graph of the polar equation

$$r\theta = 1 \quad \theta > 0$$



Sketch the graph of the polar equation  $r = 2 + 2 \sec \theta$ 

