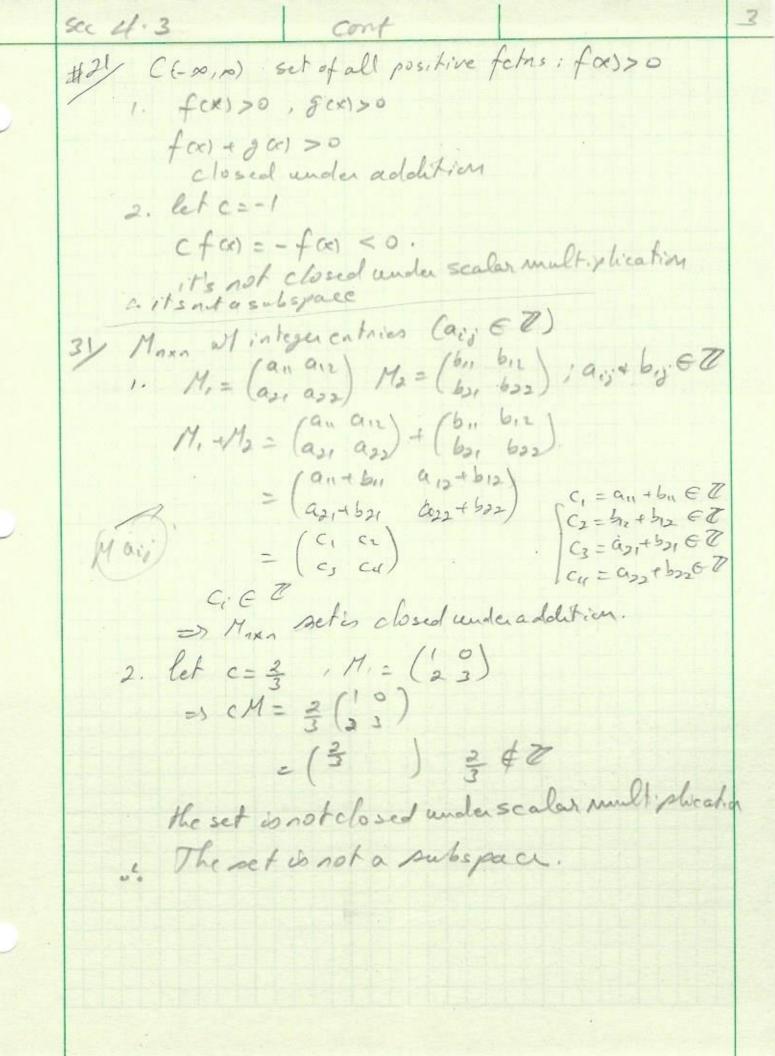
```
sec 4.3
V W= {(x1, x2, x3, 0) 1 X1, x2, x3 6 Ry
      let u= (x, x2, x3,0) N=(4, 3, 1/2,0)
   1- u+N= (x1, x2, x3,0)+(7, 12,13,10)
             = (x1+4, x2+2, x3+4, 0) | Z1=x1+4, 
= (x1+4, x2+2, x3+4, 0) | Z2=x2+2,
              = (Z1, 72, 7, 0) EW.
                                               73 = x3+73
       Set is closed under addition
    2. let c scalar ER.
        cu = c(x_1, x_2, x_3, 0)
= (cx_1, cx_2, cx_3, 0)
                                             CX, = 7,
                                             ( CX2= 2,
                                              Cx3 = 23
              = (2, ,72, 73,0) EW
        set is closed under scalar multiplication
   .: Set wis a subspace of Ry
3/ W: Mb = 10 a
     let M, = (0 a) Mo = (0 a)
    1- M,+M2 = (0 a1) + (0 a2)
                                            a = a_1 + \dot{a}_1
               = \begin{pmatrix} 0 & a_1 + a_2 \\ b_1 + b_2 & 0 \end{pmatrix}
                                           b = b + b2
               = (0 a) EW
         set is closed under addition
        let CER
          CM, = C (6,0)
                                       ca, = a
                                     ( Cb, = b
                 = (0 a) E W.
        setisclosed under scalar multiplication
  Since, the set is closed under addition & scalar multiplication
        Herfre, set is a subspace
```

```
7 W to the set of all vector IR3 3 cound =- 1
   let u= (0,1,1) + N= (1,0,-1)
     u+N= (0,1,1)+(1,0,-1)
         = (1,1,0) & W.
   1. it's not closed under addition
9 WERZ: X, y & Matimal
   let (1,3) & W
   let c=12 - 12 (1,3)= (1,3/2)
      3/2 6.0
    it's notebord under scalar multiplication
  M312 = | c | d |
     let M, = (010) M2 = (100)
      M,+M2=(010)+(010)
            = (200) -5 2+1
     it's not closed under addition
      (or c=2 => "
```



39 W=) (a, a-3b, b) : a, b & TR } let u= (x, x,-3 y, y) N= (x2, x2-3/2, 72) 1. U+N= (X1, X1-37, 7,)+(X27 X2-37, 75) = (x, +x2, x,-37,+x2-372, 7, +72) = (x,+1/2, x,+x2-3(3,+7,), y,-7,) = (a, a-3b, b) EW 1+1+ x2=a 1 3, 72 = 5 It's elised under addition 2. let CER. let cx = a cu= c(x,, x,-37, 7,) = (cx, cx, -3cy, cy) = (a, a-3b, b) E W It's closed under scalar multiplication the set w is a subspace.

Sec 4.3 4/ W=) (X1, X2, X1X2) ! X1, X2 ER3 1. let u = (u, u2, u, u2) = N= (N, N2, N, N2) U+N= (U,, U2, U, U2)+(N, N2, N, N2) = (u,+N, , u2+N2, u,u2+N,N2) let | X1 = u, +N, > X1X2 = (u,-1N) (us+N2) = 4,42+0,N2+NiU2 + U, U2+N, V2 1, ot's not closed under addition 2. let CER ca = c (u, u2, u, u2) let x, = c u, X2 = (U2 = (cu, cu, cu, u2) " it's not closed under scalar mit, es Since the set w is not closed reither under addition or scalar multiplication : set wis not subspace.

d) $\vec{u} = (1, 1, -1)$ $\begin{pmatrix} 2 & 5 & 1 \\ -1 & 0 & 1 \\ 3 & 4 & -1 \end{pmatrix} 2R_2 + R_1 \rightarrow \begin{pmatrix} 2 & 5 & 1 \\ 0 & 5 & 3 \\ 0 & -7 & -5 \end{pmatrix} C_2 = \frac{3}{5} + \frac{1}{4}$ No linear combination

2

a)
$$\vec{u} = (-1, 5, -6)$$

 $2 = (-1, 5, -6)$
 $2 = (-1, 5, -6)$
 $2 = (-1, 5, -6)$
 $4 = \begin{vmatrix} 2 & 2 & 2 \\ 0 & 4 & -12 \end{vmatrix} = 0$
 $4 = \begin{vmatrix} 2 & 2 & 2 \\ 0 & 4 & -12 \end{vmatrix} = 0$
 $4 = \begin{vmatrix} 2 & 2 & 2 \\ 2 & 5 & 13 \end{vmatrix} = 0$
 $4 = \begin{vmatrix} 2 & 2 & 2 \\ 2 & 5 & 13 \end{vmatrix} = 0$
 $4 = \begin{vmatrix} 2 & 2 & 2 \\ 2 & 5 & 13 \end{vmatrix} = 0$

(D)
$$2c_1 = -1 - 2c_2 = -1 - \frac{25}{2}$$

 $c_1 = -\frac{7}{4}$
 $\vec{u} = -\frac{7}{4}(2_10_17) + \frac{5}{4}(2_14_15) + o(2_1 - 12_113)$

b)
$$\vec{N} = (-3, 15, 18)$$

$$\Delta_3 = \begin{vmatrix} 2 & 2 - 3 \\ 0 & 4 & 15 \end{vmatrix} = 288 \pm 0 \text{ (wy)}$$

$$\Delta_3 = \begin{vmatrix} 2 & 4 & 15 \\ 7 & 5 & 18 \end{vmatrix} = 288 \pm 0 \text{ (wy)}$$

$$No linear combination for the vector $\vec{N}$$$

C)
$$\vec{\omega} = (\frac{1}{3}, \frac{1}{3}, \frac{1}{2})$$

$$\Delta_3 = \begin{vmatrix} 2 & 2 & 1/3 \\ 0 & 4 & 4/3 \\ 7 & 5 & 1/2 \end{vmatrix} = 0$$

$$\begin{pmatrix} 2 & 2 & 2 & 1/3 \\ 0 & 4 & -12 & 4/3 \\ 7 & 5 & 1/3 & 1/2 \end{pmatrix} \rightarrow 0$$

$$\vec{\omega} = -\frac{1}{6} (2,0,7) + \frac{1}{3} (2,4,5) + 0 (2,-12,13)$$

Sec 4,4 9 5= } (2,1),(-1,2)] 12-1/=> =0 S spans R2 13/ 5= {-3,5} 5 duesn't span R2 line 17/ 5= f(1,2), 1-2,-6), (u, 12)} 5 lies on a line 5 duesn't span R2 19 5= } (4,2,3), (-1,2,6), (2,-3,5)} | 2 -1 2 | = 228 ×0. 5 spans R3