

1. Evaluate

a) $\int \frac{e^x}{4e^x + 6} dx$

d) $\int \frac{x+4}{x^2 + 8x + 25} dx$

g) $\int \frac{e^x}{\sqrt{e^{2x} + 4}} dx$

b) $\int_{e^2}^{e^8} \frac{dx}{x \ln x}$

e) $\int_{\ln 2}^{\ln 3} \coth x \, dx$

h) $\int_0^1 \frac{x^2}{9-x^6} dx$

c) $\int_1^4 \frac{10\sqrt{x}}{\sqrt{x}} dx$

f) $\int \frac{dx}{\sqrt{x^2 - 9}}, \quad x > 3$

2. The mass of radioactive material in a sample has decreased by 30% since the decay began. Assuming a half-life of 1500 years, how long ago did the decay begin?
3. Growing from an initial population of 150,000 at a constant annual growth rate of 4%/yr., how long will it take a city to reach a population of 1 million?
4. A savings account advertises an annual percentage yield (APY) of 5.4%, which means that the balance in the account increases at an annual growth rate of 5.4%/yr.
- a) Find the balance in the account for $t \geq 0$ with an initial deposit of \$1500, assuming the APY remains fixed and no additional deposits or withdrawals are made.
 - b) What is the doubling time of the balance?
 - c) After how many years does the balance reach \$5,000?

5. Compute the following derivatives

a) $\frac{d^6}{dx^6}(\cosh x)$

b) $\frac{d}{dx}(x \operatorname{sech} x)$

6. Find the area of the region bounded by the curves $f(x) = 8 \operatorname{sech}^2 x$ and $g(x) = \cosh x$

7. Evaluate $\lim_{x \rightarrow \infty} (\tanh x)^x$