Professor: Fred Khoury

<u>Directions</u>: Show your work whenever possible: a correct answer is worth 0 point without any supporting work.

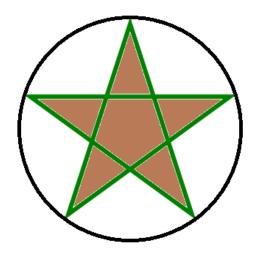
1. In any triangle *ABC*, prove that:

$$a = b\cos C + c\cos B$$

$$b = c \cos A + a \cos C$$

$$c = a\cos B + b\cos A$$

2. Find the area of the shaded star that is inscribed in a circle with a radius 1.



3. Evaluate:

$$\sin 1^{\circ} + \sin 2^{\circ} + \sin 3^{\circ} + \dots + \sin 357^{\circ} + \sin 358^{\circ} + \sin 359^{\circ}$$

 $\sin^{2} 1^{\circ} + \sin^{2} 2^{\circ} + \sin^{2} 3^{\circ} + \dots + \sin^{2} 357^{\circ} + \sin^{2} 358^{\circ} + \sin^{2} 359^{\circ}$

4. Find the solution(s) for: $\cos 2x + \cos 4x = \cos x$