$$\frac{\cos n\pi}{5^{-n}}$$

$$\cos n\pi = (-1)^{n}$$

$$\frac{\cos n\pi}{5^{-n}} = \frac{1}{2} \left(-\frac{1}{5^{-n}}\right)^{n}$$

$$\frac{1}{2} \cos n\pi = \frac{1}{2} \left(-\frac{1}{5^{-n}}\right)^{n}$$

Katio Tests

I an

 $\lim_{n\to\infty}\frac{a_{n+1}}{a}=P$

1-if P < 1 - scries converges

" oliverses in conclusive.

<u>El</u> <u>2145</u>

unor - 2 +5 3 7 45

P= lum ang an -ilin 27+5

= + (2)

= = <1

By the Ratio Test, the given sens conveyes

 $\frac{2^{2}+5}{3^{2}}=\left(\frac{3}{3}\right)^{2}+5\left(\frac{1}{3}\right)^{2}$ \mathcal{E}_{X} $\sum_{n=1}^{\infty} \frac{(2n)!}{n!}$ 11=12...(1-01 (41) = 1.2. - . n. (A+1) $\frac{u_{n+1}}{a_n} = \frac{(a(n+1))!}{(n+1)!} \cdot \frac{n! n!}{(2n)!}$ = (2n+2)! / (n+1) (n+1) (2n)! $= \frac{(2n+1)(2n+2)}{(n+1)(n+1)}$ P= line (21+1) (21+2)
(1+1) (1+1) = lim 40 --

:. By the Ratio Yest, the given peurs durages

$$\frac{4^{n!} n!}{(2n)!}$$

$$\frac{(2n)!}{(2n+2)!} = \frac{4^{n!} (n+1)!}{(2n+2)!} \frac{(2n)!}{(2n+2)!}$$

$$= 4 \frac{(n+1)(n+1)}{(2n+2)}$$

$$= 4 \frac{(n+1)(n+1)(n+1)}{(2n+2)}$$

$$= 4 \frac{(n+1)(n+1)(n+1)}{(2n+2)}$$

$$= 4 \frac{(n+1)(n+1)(n+1)}{(2n+2)}$$

$$= 4 \frac{(n+$$

By the Ratio Test is inconclusive, since april and, the fiven senso diverses

Non 2 an = P Sens Conveyes C < 1 , a chivergeo C>1 in conclusing $\int_{-2\pi}^{\infty} \frac{n^2}{2^{n}}$ $\frac{1}{\sqrt{2n}} = \frac{\sqrt{n^2}}{2}$ P= lim 12/2 = 4 00 - = < Z :. By the Root Test, the given, sewes Conveyes

$$\frac{\alpha_{n+1}}{\alpha_n} = \frac{(n+1)^2}{2^{n+1}} = \frac{2^n}{n^2}$$

$$= \frac{1}{2} \left(\frac{n+1}{n} \right)^2$$

1/21 = -3/2 (27)3- >1 P= lim 2 13/1 By the Root Test, the given sens aboverses $\frac{2}{n+1} \left(\frac{1}{1+n}\right)^n$ 1/(1+n) = -1-P= lum - [s. By the Root Test, the given sewes convergen

(... There fore

1 Ratio Test. 2 27 $\frac{a_{n+1}}{a_n} = \frac{2^{n+1}}{(n+1)!} \cdot \frac{n!}{2^n}$ = -2 P= lum 2. :. By the Ratio Test the given series converges. $45 \int_{-1}^{2} \frac{n5^{n}}{(2n+3) \ln(n+1)}$ $\frac{a_{n+1}}{a_n} = \frac{(n+1).5^{-n+1}}{(2n+5)\ln(n+2)} \cdot \frac{(2n+3)\ln(n+1)}{n.5^n}$ $= 5 \frac{2n^2 + 5n + 3}{2n^2 + 5n} \frac{\ln(n+1)}{\ln(n+2)}$ P= 5 lum 212+51+3. lum lu(1+1)

= 5 lim 7 = 3 = 5 > 1

: By the Ratio Tests the given sewes diverses

root Test #24 2 (31) $\sqrt{\frac{4}{3n}} = \frac{4}{3n}$ P = lom 4 -. By the Roof Test, the given series converges 426) sin (1) 1/ sin 1/ = sin 1/0 P = lim sin do =0 <1

: By the Root Test, the given Devis Converges.

Sec 3.6 1-) lternating Sewes. + - + - - (-1)? $\sum_{n=1}^{\infty} (-1)^{n+1} u_n = u_1 - u_2 + u_3 - \dots$ Converges: 3steps (1) uns all prositive (2) # $\begin{array}{ccc} * & \mathcal{U}_n > \mathcal{U}_{n+1} \\ * & \mathcal{U}_n \longrightarrow 0 \end{array}$ Em U, = 5 EX = (-1) -1 1 da = 1 1 < 1+1 $\frac{1}{n} > \frac{1}{n+1}$ $u_n > u_{n+1} \sim$ 2) -- 0 .. By the afternating series, the given series converges.

- 8

Absolute convergence I an conveyes absolutely of Z/an/ comverges. Ex [-1) 1+1 Z/(-1) =] ______ 1-2>1 -> Converse The given series converges because it converges a b solutely I series Converges but doesn't converge absolutely Converges conditionally. #1 [-1] 1) da = 1 In < Vn+1 Vn > 1 Un > Unti 2) = >0~ . By the alternating series, The given series

Conviges.

#2 (-1) -4 (lun) 3 Un = (lun)? lun < lu(1+1) (lun)2 < (lu(1+1))2 (lun)2 > (lu(n+1))2 (lun)2 > 4 (lu(n+1))2 Un > Ung v (lyn)2 -> 0 -: By the Alternating Sens, the given series Converges. Un = 1 lun < lu(1+1) 1 lan < (1+1) lu (1+1) 1 / n lun > (n+1) lu (n+1) n Pun -> 0 ~ By the alterating Series, the given scurs converges.

2 nlun integral v Ration - 12004 ? alternating # $\int_{2}^{\infty} \frac{dx}{x \ln x} = \int_{2}^{\infty} \frac{d(\ln x)}{\ln x}$ = lu (lux) / 2 by the integral Test, the given series chineges 11 lnn >1 -11 m... - p=1 diverges by p-5 cies an = (n+1) lu (n+1) . 1 P: line 1 . lum lun
100 /11 = lim 1+1 = 1 l'aconclusine. Root Volum = 1 Van (lun) P- hom To lim Than = line Venn

lem lu $((lun)^{1/n} = loim lu(lun)$ = 0 $lin (lun)^{1/n} = 0$ = 1