

$$\begin{aligned}
 1/ \int_{-2}^2 (3x^4 - 2x + 1) dx &= \frac{3}{5} x^5 - x^2 + x \Big|_{-2}^2 \\
 &= \frac{96}{5} - 4 + 2 - \left(-\frac{96}{5} - 4 - 2 \right) \\
 &= \frac{182}{5} + 4 \\
 &= \frac{202}{5}
 \end{aligned}$$

$$\begin{aligned}
 2/ \int_0^1 (4x^{21} - 2x^{16} + 1) dx &= \frac{2}{11} x^{22} - \frac{2}{17} x^{17} + x \Big|_0^1 \\
 &= \frac{2}{11} - \frac{2}{17} + 1 \\
 &= \frac{192}{187}
 \end{aligned}$$

$$3/ \quad f(x) = 16 - x^2 = 0 \quad x \in [-4, 4]$$

$x = \pm 4$

$$\begin{aligned}
 A &= \int_{-4}^4 (16 - x^2) dx \\
 &= 16x - \frac{1}{3} x^3 \Big|_{-4}^4 \\
 &= 4^3 - \frac{1}{3} 4^3 - \left(-4^3 + \frac{4^3}{3} \right) \\
 &= 64 \left(1 - \frac{1}{3} + 1 - \frac{1}{3} \right) \\
 &= 64 \left(2 - \frac{2}{3} \right) \\
 &= \frac{128}{3} \text{ unit}^2
 \end{aligned}$$

$$4/ \quad f(x) = x^3 - x \quad x \in [-1, 0]$$
$$x(x^2 - 1) = 0 \Rightarrow x = 0, \pm 1$$

$$A = \int_{-1}^0 (x^3 - x) dx$$
$$= \left. \frac{1}{4} x^4 - \frac{1}{2} x^2 \right|_{-1}^0$$
$$= -\left(\frac{1}{4} - \frac{1}{2} \right)$$
$$= \underline{\underline{\frac{1}{4} \text{ unit}^2}}$$

$$5/ \quad f(x) = x^2 - x = 0 \quad x \in [0, 3]$$
$$x = 0, 1$$

$$A = -\int_0^1 (x^2 - x) dx + \int_1^3 (x^2 - x) dx$$
$$= -\left(\frac{1}{3} x^3 - \frac{1}{2} x^2 \right) \Big|_0^1 + \left(\frac{1}{3} x^3 - \frac{1}{2} x^2 \right) \Big|_1^3$$
$$= -\left(\frac{1}{3} - \frac{1}{2} \right) + \left(9 - \frac{9}{2} - \frac{1}{3} + \frac{1}{2} \right)$$
$$= \frac{1}{6} - \frac{1}{3} + 5$$
$$= \frac{27}{6}$$
$$= \underline{\underline{\frac{9}{2} \text{ unit}^2}}}$$

$$6/ \quad f(x) = x^4 - x^2 = 0$$
$$x = \underline{0, 0}, \pm 1$$

$$[-1, 1]$$
$$x^2(x^2 - 1)$$

below x-axis.

$$A = \left| \int_{-1}^1 (x^4 - x^2) dx \right|$$

$$= \left| \frac{1}{5} x^5 - \frac{1}{3} x^3 \right|_{-1}^1$$

$$= \left| \frac{1}{5} - \frac{1}{3} + \frac{1}{5} - \frac{1}{3} \right|$$

$$= \underline{\underline{\frac{4}{15} \text{ unit}^2}}$$