

## ***Solution***

### ***Section 3.1– Introduction***

#### ***Exercise***

Indicate the angle if it is an acute or obtuse. Then give the complement and the supplement of each angle.

- a)  $10^\circ$       b)  $52^\circ$       c)  $90^\circ$       d)  $120^\circ$       e)  $150^\circ$

#### **Solution**

- a) Acute;  
Complement is  $90^\circ - 10^\circ = 80^\circ$ ;  
Supplement is  $180^\circ - 10^\circ = 170^\circ$ .
- b) Acute;  
Complement is  $90^\circ - 52^\circ = 38^\circ$ ;  
Supplement is  $180^\circ - 52^\circ = 128^\circ$ .
- c) Neither (*right angle*);  
Complement is  $90^\circ - 90^\circ = 0^\circ$ ;  
Supplement is  $180^\circ - 90^\circ = 90^\circ$ .
- d) Obtuse;  
Complement is  $90^\circ - 120^\circ = -30^\circ$ ;  
Supplement is  $180^\circ - 120^\circ = 60^\circ$ .
- e) Obtuse;  
Complement is  $90^\circ - 150^\circ = -60^\circ$ ;  
Supplement is  $180^\circ - 150^\circ = 30^\circ$ .

#### ***Exercise***

Change to decimal degrees

- a)  $10^\circ 45'$       c)  $274^\circ 18' 59''$       e)  $98^\circ 22' 45''$       g)  $1^\circ 2' 3''$   
b)  $34^\circ 51' 35''$       d)  $74^\circ 8' 14''$       f)  $9^\circ 9' 9''$       h)  $73^\circ 40' 40''$

#### **Solution**

- a)  $10^\circ 45' = 10^\circ + 45'$   
 $= 10^\circ + 45' \cdot \frac{1^\circ}{60'}$   
 $= 10^\circ + 0.75^\circ$   
 $= \underline{10.75^\circ}$
- b)  $34^\circ 51' 35'' = 34^\circ + 51' + 35''$   
 $= 34^\circ + 51' \cdot \frac{1^\circ}{60'} + 35'' \cdot \frac{1^\circ}{3600''}$   
 $= 34^\circ + 0.85^\circ + 0.00972^\circ$

$$= \underline{34.85972^\circ}$$

$$\begin{aligned} c) \quad 274^\circ 18' 59'' &= 274^\circ + 18' + 59'' \\ &= 274^\circ + 18' \cdot \frac{1^\circ}{60'} + 59'' \cdot \frac{1^\circ}{3600''} \\ &= 274^\circ + 0.3^\circ + 0.016389^\circ \\ &= \underline{274.316389^\circ} \end{aligned}$$

$$\begin{aligned} d) \quad 74^\circ 8' 14'' &= 74^\circ + \frac{8^\circ}{60} + \frac{14^\circ}{3600} \\ &= 74^\circ + 0.1333^\circ + 0.0039^\circ \\ &= \underline{74.137^\circ} \end{aligned}$$

$$\begin{aligned} e) \quad 98^\circ 22' 45'' &= 98^\circ + 22' + 45'' \\ &= 98^\circ + 22' \cdot \frac{1^\circ}{60'} + 45'' \cdot \frac{1^\circ}{3600''} \\ &= 98^\circ + 0.36667^\circ + 0.0125^\circ \\ &= \underline{98.37917^\circ} \end{aligned}$$

$$\begin{aligned} f) \quad 9^\circ 9' 9'' &= 9^\circ + 9' + 9'' \\ &= 9^\circ + 9' \cdot \frac{1^\circ}{60'} + 9'' \cdot \frac{1^\circ}{3600''} \\ &= 9^\circ + 0.15^\circ + 0.0025^\circ \\ &= \underline{9.1525^\circ} \end{aligned}$$

$$\begin{aligned} g) \quad 1^\circ 2' 3'' &= 1^\circ + 2' + 3'' \\ &= 1^\circ + 2' \cdot \frac{1^\circ}{60'} + 3'' \cdot \frac{1^\circ}{3600''} \\ &= 1^\circ + 0.03333^\circ + 0.000833^\circ \\ &= \underline{1.034163^\circ} \end{aligned}$$

$$\begin{aligned} h) \quad 73^\circ 40' 40'' &= 73^\circ + 40' + 40'' \\ &= 73^\circ + 40' \cdot \frac{1^\circ}{60'} + 40'' \cdot \frac{1^\circ}{3600''} \\ &= 73^\circ + 0.6667^\circ + 0.0111^\circ \\ &= \underline{73.67778^\circ} \end{aligned}$$

### Exercise

Convert to degrees, minutes, and seconds.

a)  $89.9004^\circ$

c)  $122.6853^\circ$

e)  $44.01^\circ$

g)  $29.411^\circ$

b)  $34.817^\circ$

d)  $178.5994^\circ$

f)  $19.99^\circ$

h)  $18.255^\circ$

### Solution

$$\begin{aligned} a) \quad 89.9004^\circ &= 89^\circ + 0.9004^\circ \\ &= 89^\circ + 0.9004^\circ \cdot (60') \\ &= 89^\circ \quad 54.024' \\ &= 89^\circ \quad 54' + 0.024' \\ &= 89^\circ \quad 54' \quad 0.024' \cdot (60'') \\ &= \underline{89^\circ \quad 54' \quad 1.44''} \end{aligned}$$

$$\begin{aligned} b) \quad 34.817^\circ &= 34^\circ + 0.817^\circ \\ &= 34^\circ + 0.817 (60') \\ &= 34^\circ + 49.02' \\ &= 34^\circ + 49' + .02 (60'') \\ &= 34^\circ + 49' + 1.2'' \\ &= \underline{34^\circ \quad 49' \quad 1.2''} \end{aligned}$$

$$\begin{aligned} c) \quad 122.6853^\circ &= 122^\circ + .6853^\circ \\ &= 122^\circ + 0.6853 \cdot (60') \\ &= 122^\circ \quad 41.118' \\ &= 122^\circ \quad 41' + 0.118' \\ &= 122^\circ \quad 41' \quad 0.118 \cdot (60'') \\ &= \underline{122^\circ \quad 41' \quad 7.1''} \end{aligned}$$

$$\begin{aligned} d) \quad 178.5994^\circ &= 178^\circ + .5994^\circ \\ &= 178^\circ + .5994 \cdot (60') \\ &= 178^\circ \quad 35.964' \\ &= 178^\circ \quad 35' + .964' \\ &= 178^\circ \quad 35' \quad 0.964 \cdot (60'') \\ &= \underline{178^\circ \quad 35' \quad 57.84''} \end{aligned}$$

$$\begin{aligned} e) \quad 44.01^\circ &= 44^\circ + .01^\circ \\ &= 44^\circ + .01 \cdot (60') \\ &= 44^\circ \quad 0.6' \end{aligned}$$

$$= 44^\circ \quad 0.6 \cdot (60'') \\ = 44^\circ \quad 36''$$

$$\begin{aligned} f) \quad 19.99^\circ &= 19^\circ + .99^\circ \\ &= 19^\circ + .99 \cdot (60') \\ &= 19^\circ \quad 59.4' \\ &= 19^\circ \quad 59' + 0.4' \\ &= 19^\circ \quad 59' \quad 0.4 \cdot (60'') \\ &= 19^\circ \quad 59' \quad 24'' \end{aligned}$$

$$\begin{aligned} g) \quad 29.411^\circ &= 29^\circ + 0.411^\circ \\ &= 29^\circ + 0.411 \cdot (60') \\ &= 29^\circ \quad 24.66' \\ &= 29^\circ \quad 24' + 0.66' \\ &= 29^\circ \quad 24' \quad 0.66 \cdot (60'') \\ &= 29^\circ \quad 24' \quad 39.6'' \end{aligned}$$

$$\begin{aligned} h) \quad 18.255^\circ &= 18^\circ + 0.255^\circ \\ &= 18^\circ + 0.255 \cdot (60') \\ &= 18^\circ \quad 15.3' \\ &= 18^\circ \quad 15' + 0.3' \\ &= 18^\circ \quad 15' \quad 0.3 \cdot (60'') \\ &= 18^\circ \quad 15' \quad 18'' \end{aligned}$$

## ***Exercise***

Perform each calculation

$$a) \quad 51^\circ 29' + 32^\circ 46' \quad b) \quad 90^\circ - 73^\circ 12' \quad c) \quad 90^\circ - 36^\circ 18' 47'' \quad d) \quad 75^\circ 15' + 83^\circ 32'$$

## **Solution**

$$\begin{aligned} a) \quad &51^\circ 29' + 32^\circ 46' \\ &\begin{array}{r} 51^\circ \quad 29' \\ + 32^\circ \quad 46' \\ \hline 83^\circ \quad 75' \end{array} \\ &83^\circ \quad 75' = 1^\circ 15' \quad \boxed{84^\circ \quad 15'} \end{aligned}$$

$$b) \quad 90^\circ - 73^\circ 12'$$

$$\begin{array}{r} 89^\circ \ 60' \\ -73^\circ \ 12' \\ \hline 16^\circ \ 48' \end{array}$$

$$c) \ 90^\circ - 36^\circ 18' 47''$$

$$\begin{array}{r} 90^\circ \\ -36^\circ \ 18' \ 47'' \\ \hline \end{array} \Rightarrow \begin{array}{r} 89^\circ \ 59' \ 60'' \\ -36^\circ \ 18' \ 47'' \\ \hline 53^\circ \ 41' \ 13'' \end{array}$$

$$d) \ 75^\circ 15' + 83^\circ 32'$$

$$\begin{array}{r} 75^\circ \ 15' \\ 83^\circ \ 32' \\ \hline 158^\circ \ 47' \end{array}$$

### ***Exercise***

Find the angle of least possible positive measure coterminal with an angle of

$$a) \ -75^\circ$$

$$b) \ -800^\circ$$

$$c) \ 270^\circ$$

### **Solution**

$$a) \ 360^\circ - 75^\circ = \underline{285^\circ}$$

$$b) \ 3(360^\circ) - 800^\circ = \underline{280^\circ}$$

$$c) \ 360^\circ + 270^\circ = \underline{630^\circ}$$

### Exercise

A vertical rise of the Forest Double chair lift 1,170 *feet* and the length of the chair lift as 5,570 *feet*. To the nearest foot, find the horizontal distance covered by a person riding this lift.

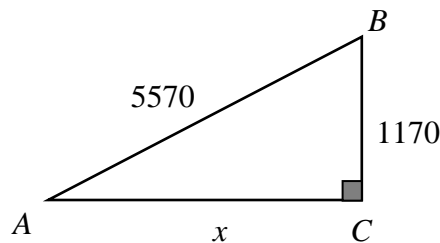
#### Solution

$$x^2 + 1170^2 = 5570^2$$

$$x^2 = 5570^2 - 1170^2$$

$$x = \sqrt{5570^2 - 1170^2}$$

$$x = 5,445.73 \text{ ft}$$



### Exercise

A tire is rotating 600 times per minute. Through how many degrees does a point of the edge of the tire move in  $\frac{1}{2}$  second?

#### Solution

$$\frac{1}{2} 600 \frac{\text{rev}}{\text{min}} \cdot \frac{1 \text{ min}}{60 \text{ sec}} \cdot \frac{360^\circ}{1 \text{ rev}} = 1800 \text{ deg / sec}$$

### Exercise

A windmill makes 90 revolutions per minute. How many revolutions does it make per second?

#### Solution

$$90 \frac{\text{rev}}{\text{min}} \cdot \frac{1 \text{ min}}{60 \text{ sec}} = 1.5 \text{ rev / sec}$$

### Exercise

Convert to radians

- a)  $256^\circ 20'$     b)  $-78.4^\circ$     c)  $330^\circ$     d)  $-60^\circ$     e)  $-225^\circ$

#### Solution

$$\begin{aligned} \text{a) } 256^\circ 20' &= 256^\circ + \frac{20^\circ}{60} \\ &= 256^\circ + \frac{2^\circ}{6} \\ &= \frac{1538^\circ}{6} = \left( \frac{769}{3} \right)^\circ \end{aligned}$$

$$\frac{769^\circ}{3} \cdot \frac{\pi}{180^\circ} = \frac{769\pi}{540} \text{ rad} \approx 4.47 \text{ rad}$$

$$b) \quad -78.4^\circ = -78.4^\circ \left( \frac{\pi}{180^\circ} \right) rad$$

$$\underline{\approx -1.37 \text{ rad}}|$$

$$c) \quad 330^\circ = 330^\circ \left( \frac{\pi}{180^\circ} \right) rad$$

$$\underline{= \frac{11\pi}{6} \text{ rad}}|$$

$$d) \quad -60^\circ = -60^\circ \left( \frac{\pi}{180^\circ} \right) rad$$

$$\underline{= -\frac{\pi}{3} \text{ rad}}|$$

$$e) \quad -225^\circ = -225^\circ \left( \frac{\pi}{180^\circ} \right) rad$$

$$\underline{= -\frac{5\pi}{4} \text{ rad}}|$$

### **Exercise**

Convert to degrees

$$a) \quad \frac{11\pi}{6}$$

$$c) \quad \frac{\pi}{6}$$

$$e) \quad \frac{\pi}{3}$$

$$g) \quad -4\pi$$

$$b) \quad -\frac{5\pi}{3}$$

$$d) \quad 2.4$$

$$f) \quad -\frac{5\pi}{12}$$

$$h) \quad \frac{7\pi}{13}$$

### **Solution**

$$a) \quad \frac{11\pi}{6} \text{ (rad)} = \frac{11\pi}{6} \cdot \frac{180^\circ}{\pi}$$

$$\underline{= 330^\circ}|$$

$$b) \quad -\frac{5\pi}{3} \text{ (rad)} = -\frac{5\pi}{3} \cdot \frac{180^\circ}{\pi}$$

$$\underline{= -300^\circ}|$$

$$c) \quad \frac{\pi}{6} \text{ (rad)} = \frac{\pi}{6} \left( \frac{180}{\pi} \right)^\circ$$

$$\underline{= 30^\circ}|$$

$$d) \quad 2.4 \text{ rad} = 2.4 \cdot \frac{180^\circ}{\pi}$$

$$= \frac{432^\circ}{\pi}$$

$$\underline{\approx 137.5^\circ}|$$

$$e) \quad \frac{\pi}{3}(\text{rad}) = \frac{\pi}{3} \left( \frac{180}{\pi} \right)^{\circ}$$

$$\underline{= 60^{\circ}} \quad |$$

$$f) \quad -\frac{5\pi}{12}(\text{rad}) = -\frac{5\pi}{12} \left( \frac{180}{\pi} \right)^{\circ}$$

$$\underline{= -75^{\circ}} \quad |$$

$$g) \quad -4\pi(\text{rad}) = -4\pi \left( \frac{180}{\pi} \right)^{\circ}$$

$$\underline{= -720^{\circ}} \quad |$$

$$h) \quad \frac{7\pi}{13}(\text{rad}) = \frac{7\pi}{13} \left( \frac{180}{\pi} \right)^{\circ}$$

$$\underline{\approx 96.923^{\circ}} \quad |$$