

Determinant using *Diagonal Method*

$$\begin{array}{ccccc}
 a_{11} & a_{12} & a_{13} & a_{11} & a_{12} \\
 a_{21} & a_{22} & a_{23} & a_{21} & a_{22} \\
 a_{31} & a_{32} & a_{33} & a_{31} & a_{32}
 \end{array}
 \quad
 a_{11}a_{22}a_{33} + a_{12}a_{23}a_{31} + a_{13}a_{21}a_{32} \quad (1)$$

$$\begin{array}{ccccc}
 a_{11} & a_{12} & a_{13} & a_{11} & a_{12} \\
 a_{21} & a_{22} & a_{23} & a_{21} & a_{22} \\
 a_{31} & a_{32} & a_{33} & a_{31} & a_{32}
 \end{array}
 \quad
 -a_{13}a_{22}a_{31} - a_{11}a_{23}a_{32} - a_{12}a_{21}a_{33} \quad (2)$$

Determinant: $D = (1) + (2)$

$$\begin{vmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{vmatrix} = a_{11}a_{22}a_{33} + a_{12}a_{23}a_{31} + a_{13}a_{21}a_{32} - a_{13}a_{22}a_{31} - a_{11}a_{23}a_{32} - a_{12}a_{21}a_{33}$$

Second Method

$$\begin{vmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{vmatrix} = a_{11}(a_{22}a_{33} - a_{23}a_{32}) + a_{12}(a_{23}a_{31} - a_{21}a_{33}) + a_{13}(a_{21}a_{32} - a_{22}a_{31})$$