$$K_{114} = 1 \underbrace{x_1}_{A_{114}} \cdot \underbrace{x_2}_{500} = \underbrace{x_1}_{500}$$

$$K_{104} = 1 \cdot \underbrace{x_1}_{500} = \underbrace{x_1}_{500}$$

$$X_1'dt = \underbrace{x_2}_{500} - \underbrace{x_1}_{500}$$

$$X_1' = \underbrace{x_1}_{500} \times \underbrace{x_2}_{500} = \underbrace{x_2}_{500}$$

$$K_{2111} = \underbrace{x_1}_{500} \times \underbrace{x_2}_{500} = \underbrace{x_2}_{500}$$

$$X_1' = \underbrace{x_1}_{500} \cdot \underbrace{x_1}_{500} + \underbrace{x_2}_{500} = \underbrace{x_2}_{500}$$

$$X_2' = \underbrace{x_1}_{500} \cdot \underbrace{x_1}_{500} + \underbrace{x_2}_{500} \times \underbrace{x_2}_{500} = \underbrace{x_2}_{500}$$

$$X_2' = \underbrace{x_1}_{500} \cdot \underbrace{x_1}_{500} + \underbrace{x_2}_{500} \times \underbrace{x_2}_{500} = \underbrace{x_2}_{500}$$

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$$X_1' = \underbrace{x_1}_{500} \cdot \underbrace{x_1}_{500} + \underbrace{x_2}_{500} \times \underbrace{x_2}_{500} = \underbrace{x_$$

For
$$\lambda_{1} = -\frac{1}{260} \Rightarrow (\lambda - \lambda_{1}) |_{1} = 0$$

$$(500 |_{1} = -\frac{1}{260}) \Rightarrow (\lambda_{1} - \lambda_{1}) |_{1} = 0$$

$$(500 |_{2} = 0) \Rightarrow (\lambda_{1} - \lambda_{1}) |_{2} = 0$$

$$(-\frac{1}{500} |_{2} = 0) \Rightarrow (\lambda_{1} - \lambda_{1}) |_{2} = 0$$

$$(-\frac{1}{500} |_{2} = 0) \Rightarrow (\lambda_{1} - \lambda_{1}) |_{2} = 0$$

$$(\lambda_{1} - \frac{1}{500} |_{2} = 0) \Rightarrow (\lambda_{2} - \lambda_{1}) |_{2} = 0$$

$$(\lambda_{1} - \frac{1}{500} |_{2} = 0) \Rightarrow (\lambda_{1} - \lambda_{1}) |_{2} = 0$$

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$$(\lambda_{1} - \frac{1}{500} |_{2} = 0) \Rightarrow (\lambda_{1} - \lambda_{1})$$

1: (2) 1.7.1. /5-7 2 11 8 17 -01 de - 3 + + " " (h) - 4/ 1 () FOR 7, = 11+1 105 (-1-7, AV, -) (-2' -1-i) (xi) = (0) li= (-1+c) (1-i)x, =-x2 (6-1)X1 = X2 t = (-1-1i) (4+i) t. (a+bi) (-1-i) = ((-1)+i(0) (cost+isint) c48 eit = cont + c'smo

$$= \left[\begin{pmatrix} 1 \\ -1 \end{pmatrix} + i \begin{pmatrix} 0 \\ 1 \end{pmatrix} \right] (cost + i sint) e^{4t}$$

$$= \left[\begin{pmatrix} 1 \\ -1 \end{pmatrix} cost - \begin{pmatrix} 0 \\ 1 \end{pmatrix} sint + i \begin{pmatrix} 1 \\ -1 \end{pmatrix} sint + \begin{pmatrix} 0 \\ 1 \end{pmatrix} cost \right] e^{4t}$$

$$= \left[\begin{pmatrix} cost \\ -cost - sint \end{pmatrix} + i \begin{pmatrix} sint \\ -cost \end{pmatrix} \right] e^{4t}$$

$$X(t) = \left[\begin{pmatrix} cost \\ -cost - sint \end{pmatrix} e^{4t} + \left[cost - cost - cost \right] e^{4t}$$

$$X(t) = \left[\begin{pmatrix} cost + c_1 sint \end{pmatrix} e^{4t} + c_2 (cost - cost - c$$

Kuco= (-C, cost-C, sintle 4t + C2 (cost sintle 4t

1 ez en value (mult) $\begin{cases} x_{1}(t) = C_{1}(v_{1} + v_{2})e^{\lambda t} \\ x_{2}(t) = C_{1}(v_{1} + v_{2})e^{\lambda t} \end{cases}$

$$\begin{aligned} EX & A = \begin{pmatrix} -1 & -1 \\ 1 & -3 \end{pmatrix} \\ & A = A = \begin{pmatrix} -1 & -1 \\ 1 & -3 - A \end{pmatrix} \\ & = A^{2} + 4A + 44 \\ & = (A + 2)^{2} = 0 \\ & A_{1,2} = -2 \end{bmatrix} \\ For & A = -2 \Rightarrow (A - A_{2} I)V_{2} = 0 \\ & \begin{pmatrix} 1 & -1 \\ 1 & -1 \end{pmatrix} \begin{pmatrix} 1 & -1 \\ 1 & -1 \end{pmatrix} \begin{pmatrix} x_{1} \\ x_{2} \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \Rightarrow V_{2} = \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ & \begin{pmatrix} A + 2I \end{pmatrix} V_{2} = V_{2} \\ & \begin{pmatrix} V_{1} & -1 \\ 1 & -1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \begin{pmatrix} 1 \\ 1 \end{pmatrix} \\ & X(H) = \begin{pmatrix} 1 & -1 \\ 1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} \begin{pmatrix} 1 \\$$

$$|X_{1}| = 4X_{1} + 5X_{2}$$

$$X_{2}| = -2X_{1} + 6X_{2}$$

$$A = \begin{bmatrix} 4 & 5 \\ -2 & 6 \end{bmatrix}$$

$$|A - AI| = \begin{vmatrix} 4 - A & 5 \\ -2 & 6 - A \end{vmatrix}$$

$$= A^{2} - 10A + 34 = 0$$

$$A_{1,1} = +5 + \frac{1}{2} \sqrt{100 - 136}$$

$$= 5 + 3C$$

$$For A_{1} = 5 + 3C \Rightarrow (A - A, I) V_{1} = 0$$

$$\begin{pmatrix} -1 - 3C & 5 \\ -2 & 1 + 3C \end{pmatrix} \begin{pmatrix} x_{1} \\ y_{2} \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

$$- (1 + 3C) X_{1} + 5X_{2} = 0$$

$$(1 + 3C) X_{1} = 5y_{1} \Rightarrow V_{1} = \begin{pmatrix} 5 \\ 1 + 3C \end{pmatrix}$$

$$I(5) + I(3) = \begin{bmatrix} 5 \\ 1 \end{bmatrix} + I(3) = \begin{bmatrix} 5 \\ 1 \end{bmatrix} + I(3) = \begin{bmatrix} 5 \\ 1 \end{bmatrix} + I(3) = \begin{bmatrix} 5 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} 5 \\ 1 \end{bmatrix} + I(3) = \begin{bmatrix} 5 \\ 1 \end{bmatrix} + I(3)$$

 $= e^{5t} \left(\binom{6}{1} \cos_3 t + \binom{0}{3} \sin_3 t + i \left(\binom{0}{3} \cos_3 t + \binom{5}{3} \sin_3 t \right) \right)$ $\times (t) = C_1 \left(\frac{5 \cos_3 t}{\cos_3 t} - 3 \sin_3 t \right) \cdot e^{5t} + C_2 \left(\frac{5 \sin_3 t}{3 \cos_3 t + \sin_3 t} \right) \cdot e^{5t}$

$$\begin{cases} x_{1}'(t) = -6x_{1} + 5x_{2} \\ x_{2}'(t) = -5x_{1} + 4x_{2} \\ .t = \begin{pmatrix} -6 & 5 \\ -5 & 4 \end{pmatrix} \\ |A - \partial I| = \begin{pmatrix} -6 - \lambda & 5 \\ -5 & 4 \end{pmatrix} \\ = \lambda^{2} + 2\lambda + 1 = 0 \\ \frac{\lambda_{12}}{12} = -1 \} \text{ evgen values} \\ for \lambda = -1 = s \quad (A - \lambda I)^{2} V_{2} = 0 \\ \begin{pmatrix} -5 & 5 \\ -5 & 5 \end{pmatrix} \begin{pmatrix} -5 & 5 \\ -5 & 5 \end{pmatrix} \begin{pmatrix} x_{2} \\ y_{1} \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \\ \begin{pmatrix} x_{1} \\ y_{2} \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \\ V_{1} = \begin{pmatrix} -5 \\ -5 \end{pmatrix} \\ V_{2} = \begin{pmatrix} -5 \\ -5 \end{pmatrix} \\ V_{3} = \begin{pmatrix} -5 \\ -5 \end{pmatrix} \\ V_{4} = \begin{pmatrix} -5 \\ -5 \end{pmatrix} \\ V_{5} = \begin{pmatrix} -$$

$$|-\delta| = -1 \implies (A - \partial_{x}) V_{i} = 0$$

$$(-5 - 5) \begin{pmatrix} x_{1} \\ -5 - 5 \end{pmatrix} \begin{pmatrix} x_{1} \\ y_{1} \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \implies x_{i} = y_{i}$$

$$V_{i} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$A V_{2} = V_{1}$$

$$(-6 - 5) \begin{pmatrix} x_{1} \\ y_{2} \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \implies 1^{3K}$$

$$-6 x_{2} + 5 y_{2} = 1 \qquad x_{2} = 0 \implies y_{2} = \frac{1}{5}$$

$$-5 x_{2} + 6 y_{2} = 1 \implies x_{2} = 0 \implies x_{1} = -1$$

$$x_{2} = -1 \qquad y_{2} = -1 \implies x_{2} = -1$$

$$V_{2} = \begin{pmatrix} 0 \\ y_{5} \end{pmatrix}$$

$$x(t) = \begin{pmatrix} 0 \\ y_{5} \end{pmatrix}$$

$$x(t) = \begin{pmatrix} 0 \\ y_{5} \end{pmatrix} = -1$$

$$= C_{i} \begin{pmatrix} 1 \\ 1 \end{pmatrix} e^{-t} + C_{2} \begin{pmatrix} 1 \\ 1 \end{pmatrix} + \begin{pmatrix} 0 \\ y_{5} \end{pmatrix} e^{-t}$$

$$= C_{i} \begin{pmatrix} 1 \\ 1 \end{pmatrix} e^{-t} + C_{2} \begin{pmatrix} 1 \\ 1 \end{pmatrix} + \begin{pmatrix} 0 \\ y_{5} \end{pmatrix} e^{-t}$$

