

6.1 Right Triangles.

cosine } hyp \rightarrow adj.
sine } \rightarrow opp.
tangent \rightarrow no hyp

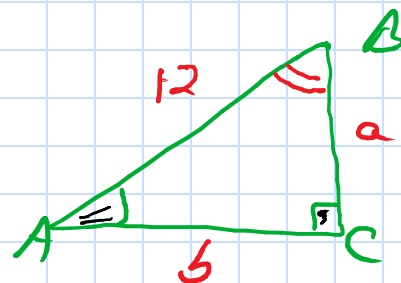


Ex $\triangle ABC$ $C = 90^\circ$ $c = 12$ $A = 40^\circ$

$$\begin{aligned} B &= 90^\circ - A \\ &= 90^\circ - 40^\circ \\ &= 50^\circ \end{aligned}$$

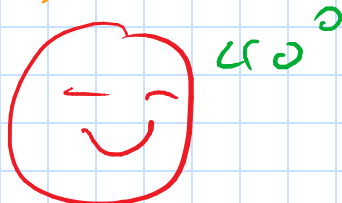
$$\cos A = \frac{b}{12}$$

$$b = 12 \cos 40^\circ \approx 9.2 \text{ cm}$$



$$\sin 40^\circ = \frac{a}{12} \Rightarrow a = 12 \sin 40^\circ \approx 7.7 \text{ cm}$$

$$\begin{aligned} \frac{1}{2} \\ 30^\circ \frac{1}{2} \\ 0^\circ \end{aligned}$$

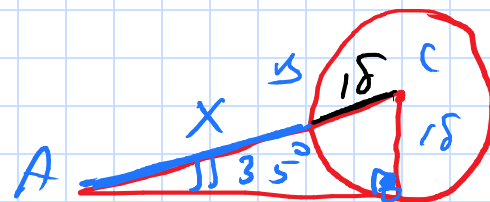


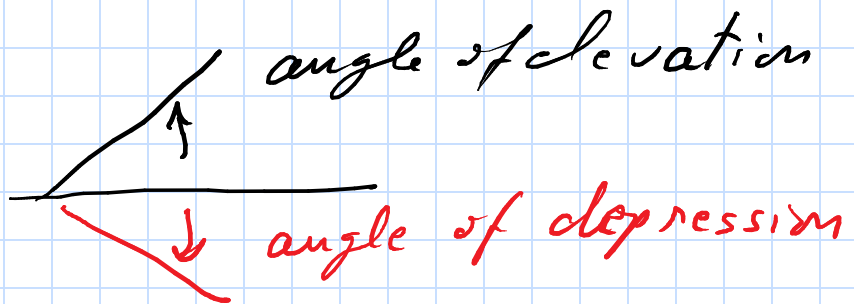
$$\begin{aligned} \sin 0^\circ &= 0 \\ \sin 30^\circ &= \frac{1}{2} \\ \sin 45^\circ &\approx .707 \end{aligned}$$

Ex $\sin 35^\circ = \frac{18}{x+18}$

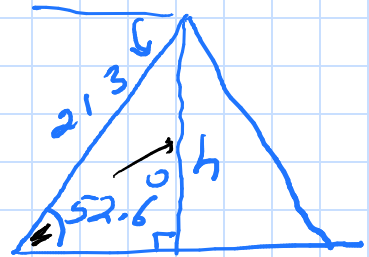
$$x+18 = \frac{18}{\sin 35^\circ}$$

$$x = \frac{18}{\sin 35^\circ} - 18 \approx 13 \text{ cm}$$





ex $\sin 52.6^\circ = \frac{h}{213}$
 $h = 213 \sin 52.6^\circ$



$\triangle ACB \Rightarrow \tan 36.7^\circ = \frac{h}{x}$
 $h = x \tan 36.7^\circ$ ①

$\triangle DCB \Rightarrow \tan 22.2^\circ = \frac{h}{x+50}$

$h = (x+50) \tan 22.2^\circ = x \tan 36.7^\circ$

$x \tan 22.2^\circ + 50 \tan 22.2^\circ = x \tan 36.7^\circ$
 $x (-\tan 22.2^\circ + \tan 36.7^\circ) = +50 \tan 22.2^\circ$

$x = \frac{50 \tan 22.2^\circ}{\tan 36.7^\circ - \tan 22.2^\circ}$

① $h = \frac{50 \tan 22.2^\circ \cdot \tan 36.7^\circ}{\tan 36.7^\circ - \tan 22.2^\circ}$

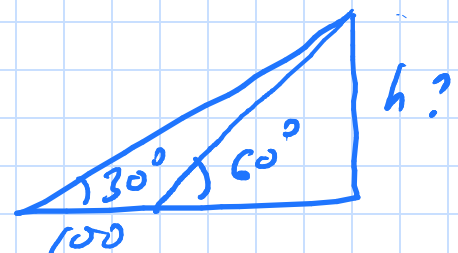
$h = \frac{x \tan \theta \tan \phi}{\tan \theta - \tan \phi}$

2 of them

ex 20

$h = \frac{100 \tan 60^\circ \tan 30^\circ}{\tan 60^\circ - \tan 30^\circ}$

X



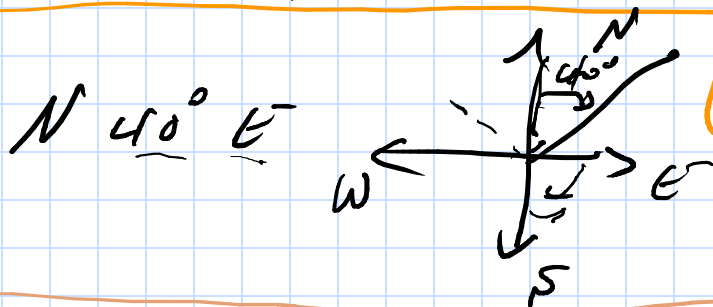
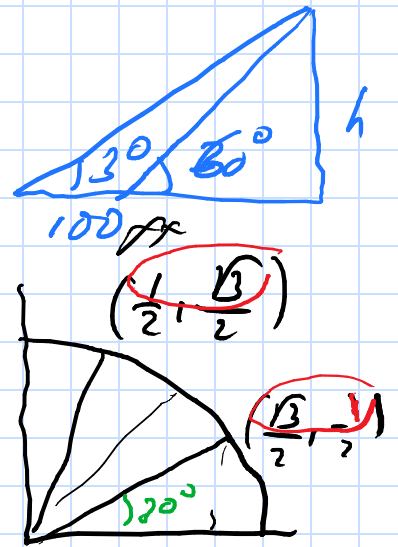
#120

$$h = \frac{100 \tan 60^\circ \tan 30^\circ}{\tan 60^\circ - \tan 30^\circ}$$

$$= \frac{100 \sqrt{3} \cdot \frac{1}{\sqrt{3}}}{\sqrt{3} - \frac{1}{\sqrt{3}}}$$

$$= \frac{100}{\frac{2}{\sqrt{3}}} \rightarrow 100 \cdot \frac{\sqrt{3}}{2}$$

$$= 50\sqrt{3} \text{ ft}$$



$$\tan 45^\circ = 1$$

$$\Delta AFC: \tan 13^\circ = \frac{y}{x} \quad (1)$$

$$\Delta BFC: \tan 19^\circ = \frac{y}{25-x} \quad (2)$$

$$(1) \quad y = x \tan 13^\circ \quad (3)$$

$$= (25-x) \tan 19^\circ$$

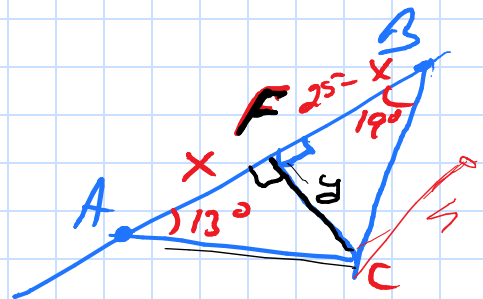
$$x \tan 13^\circ = 25 \tan 19^\circ - x \tan 19^\circ$$

$$x \tan 13^\circ + x \tan 19^\circ$$

$$x (\tan 13^\circ + \tan 19^\circ) = 25 \tan 19^\circ$$

$$x = \frac{25 \tan 19^\circ}{\tan 13^\circ + \tan 19^\circ}$$

$$y = \frac{25 \tan 19^\circ \tan 13^\circ}{\tan 13^\circ + \tan 19^\circ}$$



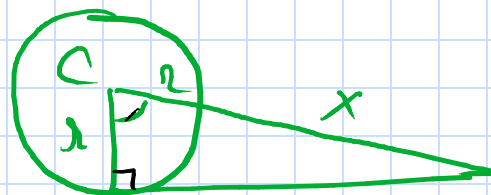
#6 $C = 30^\circ$ $r = 15$

$$\cos 30^\circ = \frac{r}{x+r}$$

$$\frac{\sqrt{3}}{2} = \frac{15}{x+15}$$

$$x+15 = \frac{30}{\sqrt{3}}$$

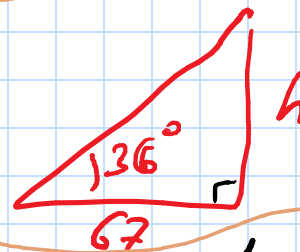
$$x = 10\sqrt{3} - 15$$



#10

$$\tan 36^\circ = \frac{h}{67}$$

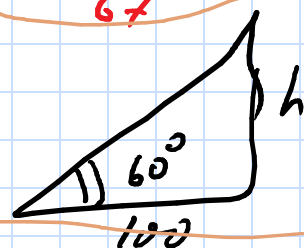
$$h = 67 \tan 36^\circ$$



#11

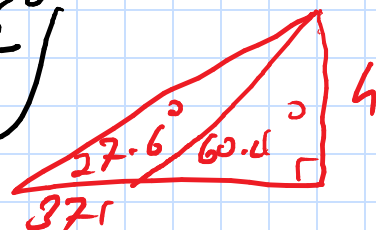
$$\tan 60^\circ = \frac{h}{100} = \sqrt{3}$$

$$h = 100\sqrt{3}$$



#17

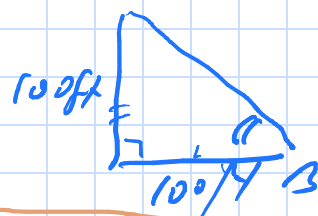
$$h = \frac{371 \tan 60.4^\circ \tan 37.6^\circ}{\tan 60.4^\circ - \tan 37.6^\circ}$$



#30

$$\tan B = \frac{100}{100} = 1$$

$$B = 45^\circ$$

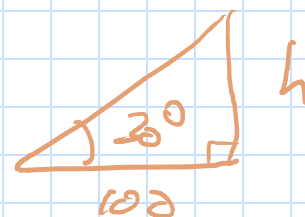


#37

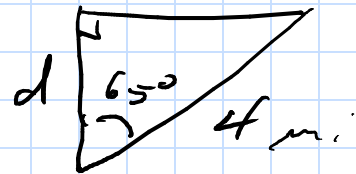
$$\tan 30^\circ = \frac{h}{100} = \frac{1}{\sqrt{3}}$$

$$h = \frac{100}{\sqrt{3}}$$

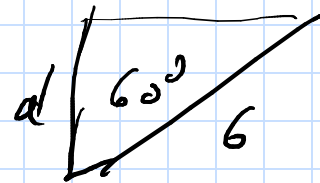
$$\frac{100\sqrt{3}}{3}$$



#39 $\cos 65^\circ = \frac{d}{4}$
 $d = 4 \cos 65^\circ$

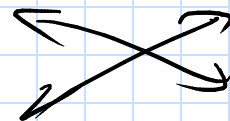
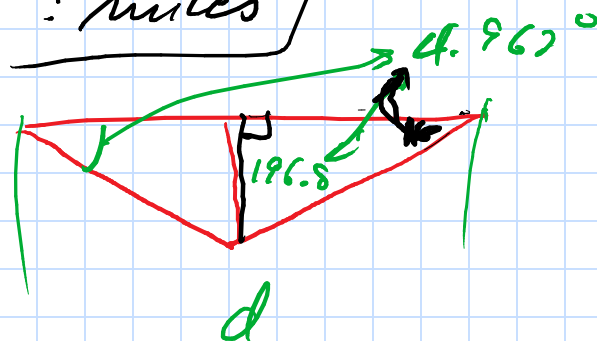


#10 $\cos 60^\circ = \frac{d}{6} = \frac{1}{2}$
 $d = 3 \text{ mi}$

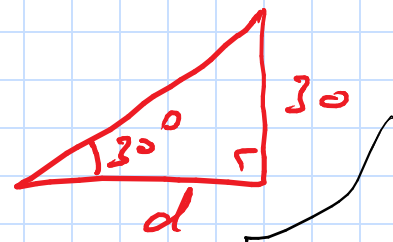


mi : miles

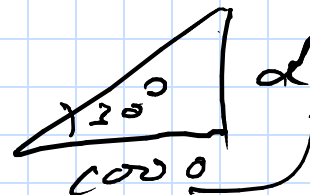
#112 $\tan 4.962^\circ = \frac{196.8}{d/2}$
 $\frac{d}{2} = \frac{196.8}{\tan 4.962^\circ}$
 $d = \frac{393.6}{\tan 4.962^\circ}$



#119 (29) $\tan 30^\circ = \frac{30}{d} = \frac{1}{\sqrt{3}}$
 $d = 30\sqrt{3}$



63 (73) $\tan 30^\circ = \frac{d}{1000} = \frac{1}{\sqrt{3}}$
 $d = \frac{1000}{\sqrt{3}}$



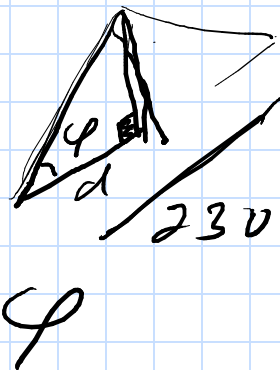
#166 $\tan 45^\circ = \frac{d}{30} = \frac{\sqrt{2}}{2}$
 $d = 15\sqrt{2}$



$$\underline{81} \quad h = 147 \quad d = 115$$

$$\tan \varphi = \frac{147}{115}$$

$$\underline{\varphi = \tan^{-1} \frac{147}{115}}$$



6.5 Law of Sines / Cosines

$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

angles

$$\frac{\sin A}{a} = \frac{\sin B}{b}$$

$$\sin A = \frac{a \sin B}{b}$$

Ex

$$A = 30^\circ \quad B = 70^\circ \quad a = 8$$

c?

$$C = 180^\circ - 30^\circ - 70^\circ$$

$$= 80^\circ$$

$$c = \frac{a \sin C}{\sin A} = \frac{8 \sin 80^\circ}{\sin 30^\circ}$$

$$\underline{c = 16 \sin 80^\circ}$$