$$\frac{3^{2}}{90^{3}} - \frac{y^{2}}{130^{2}} = 1$$

$$y_{1} = \frac{1}{2} y_{2}$$

$$y_{2} = 2y_{1}$$

$$3g_{1} = 450$$

$$3g_{2} = 450$$

$$\frac{x^{2}}{70^{2}} = 1 + \frac{y^{2}}{170^{2}}$$

$$x^{2} = 90^{2} \left(\frac{130^{2} + y^{2}}{1300^{2}}\right)$$

$$x = \frac{90}{13} \sqrt{\frac{130^{2} + y^{2}}{130^{2}}}$$

$$= \frac{9}{13} \sqrt{\frac{9}{3} + \frac{130^{2}}{130^{2}}}$$

$$= \frac{90}{13} \sqrt{\frac{394}{1300^{2}}}$$
Topoliometa = $2x_{1} = \frac{180}{13} \sqrt{\frac{394}{1000^{2}}}$

$$= \frac{90}{13} \sqrt{\frac{1069}{1000^{2}}}$$
Bottom drameta = $\frac{100}{13} \sqrt{\frac{1069}{1000^{2}}}$

$$5.427 = 5.4272727 - 25.4 + .00027 + .$$

$$\begin{array}{l}
Q_1 = 18 \\
Q_2 = .98(18) \\
Q_3 = .98^2(18) \\
Q_{10} = (.98)^9 (18) \approx 15.007 \\
Q_{11} = 18 (.98)^{1-1} \\
T = \frac{18}{1-.98} = \frac{18}{1-\frac{98}{100}} \\
= \frac{1800}{2}$$

5.7 Mathematical Induction Assure Px is true sonced to prove Pk+, is also true Ex sum of isne 2+ Soln For n=1 => 1=1(2). 1=1 ~ Pristrue 9 Let Pk: 1+2+---+ k = k(k+1) is True Is $P_{k+1}: 1+\cdots+k+(k+1)=\frac{(k+1)(k+2)}{2}$ Copy $(k+1)=\frac{(k+1)}{2}+k+(k+1)=\frac{(k+1)(k+2)}{2}+(k+1)$ Compare = (k+1) (k= +1) $=\frac{(k+1)(k+2)}{2}$ The is also true. By the mathematical induction, the proof is completed

Ē.

 $e^{x}/^{2}+3^{2}+\cdots+(2n-1)^{2}=\frac{n(2n-1)(2n+1)}{3}$ For $n=1 \implies 1^2 = \frac{1(1)(3)}{3}$ 1=10 Priotive Let Pk: 12+--- + (2k-1)2 = k(2k-1)(2k+1) istrue Is P_{k+1} , $1^2 + \dots + (2k-1)^2 + (2(k+1)-1)^2$ $= \frac{(k+1)(2(k+1)-1)(2(k+1)+1)}{3}$ 12--- + (2k-1)+(2k+1)2=3 (k+1)(2k+1)(2k+3) 12 --- + (2k-1), + (2k+1) = 1k(2k-1)(2k+1)+(2k+1) = (2k+1) $\left(\frac{1}{3}k(2k-1) + .2k+1\right)$ $=(2k+1)\frac{2k^2k+6k+3}{3}$ $=\frac{1}{3}(2k+1)(k+1)(2k+3)$ 2k2+5k+3 Texi is also true : By the mathematical induction,

the proof is completed

For $n=1 \Rightarrow 1^2 + 5(1) = 6$ $= 2(3) / P_1 \text{ is true}$ $P_k : \text{ is true} \quad 2is a factor of k^2 + 5k$ $k^2 + 5k = 2K$ is $P_{k+1} (k+1)^2 + 5(k+1)$? $(k+1)^2 + 5(k+1) ?$ $= k^2 + 5k + 2k + 6$ = 2K + 2k + 6 = 2(K + k + 3) / R $2is a factor <math>\Rightarrow P_{k+1} \text{ is also true}$ $\therefore By the mathematical induction, the$

proof completed

tx a nonzew R a>-1 nonzero R = 1R - 103 Prove (1+a) > 1+na 17 >2 n=1 - (1+a) = 1+a 1+a > 1+a 1=2 => (1+a)2 3 1+2a 1+2a+a2 >1+2a a>-1 -> a2>1 (1+a)2> 1+2a = P2 is true Pk: (1+a) > 1+ka istrue is Pk+1 (1+a) > 1+ (k+1)a? (1+a) = (1+a)(1+a) k > (1+a) (1+ka) = 1+ ka+a+ka2 = 1+ (k+1)a +ka2 >1+ (k+1)a Tko is also true 2. By the mathematical induction, the proof is completed

 $\frac{1}{1} + 2^{3} + \dots + n^{3} = \frac{n^{2}(n+1)^{2}}{4}$ $for n=2 \Rightarrow 1^3 \stackrel{?}{=} \frac{1^2(2)^2}{U}$ 1=10 P, is true. Pk! 13+---+ k3 = k2 (k+1) do true. Is Pk+1! 13+ --- + k3+ (k+1)3= 1/4 (k+1)2 (k+2)2? 13 + -- + k3 + (k+1)3 = + k2(k+1)2+ (k+1)3 = (k+1)2(1/4k2+k+1) $= (k+1)^2 \frac{k^2 + uk + uk}{u}$ Pk+1 is also true. i. By the mathematical induction,

the proof is completed.