## **Homework**

**1.** Show that *B* is the inverse of *A*. 
$$A = \begin{pmatrix} 2 & 1 \\ 5 & 3 \end{pmatrix}$$
;  $B = \begin{pmatrix} 3 & -1 \\ -5 & 2 \end{pmatrix}$ 

**2.** Find the inverse of the matrix 
$$\begin{pmatrix} 2 & 0 \\ 0 & 3 \end{pmatrix}$$

3. Find the inverse of the matrix 
$$\begin{pmatrix} 1 & 2 \\ 3 & 7 \end{pmatrix}$$

**4.** Find the inverse of the matrix 
$$\begin{pmatrix} -1 & 1 \\ 3 & -3 \end{pmatrix}$$

5. Find the inverse of the matrix 
$$\begin{pmatrix} 1 & 1 & 1 \\ 3 & 5 & 4 \\ 3 & 6 & 5 \end{pmatrix}$$

**6.** Find the inverse of the matrix 
$$\begin{pmatrix} -4 & -6 \\ 2 & 3 \end{pmatrix}$$

7. Find the inverse of the matrix 
$$A = \begin{pmatrix} \sin \theta & \cos \theta \\ -\cos \theta & \sin \theta \end{pmatrix}$$

**8.** Prove that is A is an invertible matrix, then 
$$(A^T)^{-1} = (A^{-1})^T$$

**9.** Prove if C is an invertible matrix such that 
$$CA = CB$$
, then  $A = B$ 

**10.** Prove that if 
$$A^2 = A$$
, then  $I - 2A = (I - 2A)^{-1}$ 

12. Prove that if A, B, and C are square symmetric matrices and 
$$ABC = I$$
, then B is an invertible and  $B^{-1} = CA$ .

**13.** Let 
$$A = \begin{pmatrix} 1 & 2 \\ -2 & 1 \end{pmatrix}$$

a) Show that 
$$A^2 - 2A + 5I = 0$$

b) Show that 
$$A^2 = \frac{1}{5}(2I - A)$$

c) Show that for any square matrix satisfying 
$$A^2 - 2A + 5I = 0$$
, the inverse of A is  $A^2 = \frac{1}{5}(2I - A)$