Waves

$$\upsilon = \lambda f = \frac{\omega}{k} = \frac{2\pi}{Tk} = \frac{\lambda \omega}{2\pi}; \quad k = \frac{2\pi}{\lambda}; \quad \omega = \frac{2\pi}{T} = k \upsilon; \quad f = \frac{1}{T}$$

$$\frac{\partial^2 y}{\partial x^2} = \frac{1}{v^2} \frac{\partial^2 y}{\partial t^2}$$

$$y = A\cos(\kappa x \pm \omega t)$$

$$\bar{P} = \frac{1}{2}\mu\omega^2 A^2 V$$

$$v = \sqrt{\frac{T}{\mu}} = \sqrt{\frac{B}{\rho}}; \quad B = \rho v^2$$

$$\Delta p = -B \frac{\partial S(x)}{\partial x} = -\rho v^2 \frac{\partial S(x)}{\partial x}$$

$$\Delta p_{max} = \rho \omega v S_{max}$$

$$I = \frac{1}{2}\rho\omega^2 \ \upsilon \ S_{max}^2 = \eta\upsilon = \frac{1}{2}\frac{p_0^2}{\rho\upsilon}; \qquad \eta = \frac{1}{2}\rho\omega^2 S_0^2$$

$$I_{sp} = \frac{\rho}{4\pi r^2}$$

$$\upsilon = 331 \frac{m}{s} \sqrt{\frac{T}{273}}$$

$$\beta = 10\log\left(\frac{I}{I_0}\right) = 20\log\left(\frac{p}{p_0}\right) \qquad I_0 = 10^{12} W/m^2$$

$$f' = f \left[\frac{\upsilon - \upsilon_0}{\upsilon - \upsilon_s} \right]$$

$$A = \sqrt{A_1^2 + A_2^2 + 2A_1A_2\cos(\beta_2 - \beta_1)} = 2|A_1| \cos\left(\frac{\beta_2 - \beta_1}{2}\right)$$

$$\beta_2 - \beta_1 = 2n\pi$$
 (even)(constructive) $\beta_2 - \beta_1 = (2n+1)\pi$ (odd)(destructive)

$$A = 2A_1 \left| \sin \left(k \left(L - x \right) \right) \right|$$

$$X_m = L - m\frac{\lambda}{2} \qquad X_{m+1} - X_m = \frac{\lambda}{2}$$

$$\lambda_n = \frac{2L}{n} \qquad f_n = n f_1$$

$$\lambda_n = \frac{4L}{2n-1} \qquad f_n = (2n-1) f_1$$

$$\begin{split} \boldsymbol{f}_b &= \left| \boldsymbol{f}_2 - \boldsymbol{f}_1 \right| \\ \boldsymbol{y}_{net} &= 2A \cos \left[\left(\frac{K_1 - K_2}{2} \right) \boldsymbol{x} - \left(\frac{\omega_1 - \omega_2}{2} \right) \boldsymbol{t} \right] \cos \left[\left(\frac{K_1 + K_2}{2} \right) \boldsymbol{x} - \left(\frac{\omega_1 + \omega_2}{2} \right) \boldsymbol{t} \right] \end{split}$$

k: wave number

 λ : wave length

v: wave velocity

T: Period

f: frequency

ω: angular frequency

p: change in pressure

I: Intensity

η: average energy density

 β : intensity level (db)

 I_{sp} : wave intensity

Electric Charges and Fields

$$\vec{F} = k \frac{q_1 q_2}{r^2} \hat{e}_r = q \vec{E}$$
 $\hat{e}_r = \frac{\vec{r}}{r}$; $k = 8.99 \times 10^9 \ Nm^2 / C^2$

$$\vec{F}_{12} = -\frac{G \, m_1 m_2}{r_{12}^2} \hat{r}_{12} = k \frac{q_1 q_2}{r_{21}^2} \hat{e}_{21} \qquad \hat{r}_{12} = \frac{\vec{r}}{r}; \quad G = 6.67 \times 10^{-11} \, Nm^2 / kg^2$$

$$F = \frac{1}{4\pi\varepsilon_0} \frac{\left| q_1 q_2 \right|}{r^2} = k \frac{\left| q_1 \right| \left| q_2 \right|}{r^2} \qquad E = \frac{1}{4\pi\varepsilon_0} \frac{q}{R^2}$$

$$\vec{E} = k \frac{q}{r^2} \hat{e}_r = \frac{\vec{F}}{q}$$
 $\hat{e}_r = \frac{\vec{r}}{r}$

$$\overrightarrow{E_p} = k \int \frac{dr}{r^2} \, \hat{e}_r = k \int \frac{\overrightarrow{r_p} \, \rho}{r^2} \, dV = -\frac{kQ}{a[a+L]} \hat{i} \qquad \qquad E_p = E_{px} = \frac{kQx}{\sqrt[3]{x^2 + R^2}} = \frac{kQ}{a[a+L]}$$

$$d\phi_E = \vec{E} \cdot d\vec{A} = E \cdot dA \cos \theta$$

$$\phi_{E} = \int E \cos \theta \ dA = \int \vec{E} \cdot d\vec{A} = \frac{Q_{encl}}{\varepsilon_{0}} = EA \cos \theta = \vec{E} \cdot \vec{A} = E_{n} A = \vec{E} \cdot \hat{n} A$$

$$\phi_{net} = \oint \vec{E} \cdot \vec{n} \, dA = \frac{kq}{R^2} \oint dA = 4\pi kq$$

$$\oint \vec{E} \ d\vec{A} = \frac{q}{\varepsilon_0} \qquad \varepsilon_0 = \frac{1}{4\pi k}; \quad k = \frac{1}{4\pi \varepsilon_0}$$

$$E = \frac{2k\lambda}{r} = 2\pi k\sigma = \frac{\sigma}{2\varepsilon_0} = \frac{1}{4\pi\varepsilon_0} \frac{Qr}{R^3} = \frac{1}{4\pi\varepsilon_0} \frac{Q}{r^2}$$

$$\rho = \frac{3Q}{4\pi R^3}$$

$$E = \frac{kq}{r^2}$$
 for $r > R$ $E = \frac{kq}{R^3}r$ for $r < R$

F: Force

G: Universal gravitational constant

 q_* : charge

r: distance

 \hat{e}_{r} : Unit vector

E: Electric field

 ε_0 : permittivity of free space = $8.85 \times 10^{-12} \, \text{C}^2 / \text{N-m}^2$

 ϕ : flux

σ: *charge density*

 $Q_{encl} = q_1 + q_2 + \cdots$: total charge enclosed by the surface

Electric Potential

$$\begin{split} w_e &= -\Delta u = u_f - u_i = q \int_{\vec{r}_i}^{\vec{r}_f} \vec{E} \ d\vec{r} = q \vec{E} \cdot \Delta \vec{r} = q \Delta V = q E d \cos \theta \\ \frac{1}{2} m v_i^2 + u_i &= \frac{1}{2} m v_f^2 + u_f \\ U &= \frac{1}{4 \pi \varepsilon_0} \frac{q q_0}{r} \\ W_e &= \int dW_e = \int_{\vec{r}_1}^{\vec{r}_2} \vec{F_r} \cdot d\vec{r} = q \int_{\vec{r}_1}^{\vec{r}_2} \vec{E} \cdot d\vec{r} = q \vec{E} \cdot \Delta \vec{r} = q E d \cos \theta = q \times E d \\ |\Delta u| &= |a| E d \end{split}$$

$$|\Delta u| = |q| Ed$$

$$\Delta v = \frac{\Delta u}{q} = -Ed$$

$$v(r) = \frac{kq}{r}$$

$$u = \frac{kq_1q_2}{r} = \frac{kq_1q_2}{r_{12}} + \frac{kq_2q_3}{r_{23}} + \frac{kq_1q_3}{r_{13}} = \frac{1}{2}\sum_{i=1}^n \sum_{j=i}^n \frac{kq_iq_j}{r_{ij}}$$

$$v_p = k\lambda \ln\left(\frac{a+L}{a}\right)$$

$$E = -\frac{v}{dx} = \frac{\sigma}{\varepsilon_0}$$

$$Q = c \Delta v$$

W: Work

U: potential energy

Electrical

$$I_{av} = \frac{Q}{\Delta t}$$
 $I = \frac{d\theta}{dt}$ $I(t) = I_{\text{max}} e^{-\frac{1}{RC}t}$

Ohm's Law:
$$V = I \cdot R$$

Resistance of a wire:
$$R = \frac{\rho \cdot l}{A} = \frac{\Delta V}{I} = R_0 \left[1 + \alpha \left(T - T_0 \right) \right]$$

Power
$$P = I^2 \cdot R = I \cdot V = \frac{V^2}{R} = \frac{\Delta u}{\Delta t}$$

$$P_S = \frac{W_S}{\Delta t} = I\varepsilon$$

$$P_d = P_S - P_r = \varepsilon I - I^2 r = \varepsilon I - I^2 r$$

$$P_R = \varepsilon I - I^2 r = I^2 r$$

$$\sum \Delta V_i = 0$$

$$\sum I_i = 0$$

Series Resistor
$$R_{eq} = R_1 + R_2 + R_3 + \cdots$$
 Parallel Resistor $\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \cdots + \frac{1}{R_n}$

Parallel Resistor
$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}$$

Series Capacitor
$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \dots + \frac{1}{C_n}$$
 Parallel Capacitor $C_{eq} = C_1 + C_2 + C_3 + \dots$

Parallel Capacitor
$$C_{eq} = C_1 + C_2 + C_3 + \cdots$$

Heat of a phase $Q = m \cdot L$

$$C = \frac{Q}{V} = \frac{\kappa \varepsilon_0 A}{l} = \frac{\varepsilon_0 A}{d} = \frac{L}{2k \ln\left(\frac{b}{a}\right)} = \frac{ab}{k(b-a)} = kC_0$$

$$V_c = V_0 e^{-t/RC}$$

$$V_c - IR = 0$$

$$E = \rho J = -\frac{dV}{dr}$$

$$J = \sigma E = \frac{I}{A_{\perp}}; \qquad \rho = \frac{1}{\sigma}$$

$$U = \frac{1}{2}CV^2 = \frac{1}{2}\frac{Q^2}{C} = \frac{1}{2}QV$$

$$\mathcal{E} = -L\frac{dI}{dt} = -\frac{d\phi_m}{dt}$$

$$\phi_m = \int B \cdot dA$$

$$\Delta v = \frac{\Delta v_0}{k} = kQ\left(\frac{1}{a} - \frac{1}{b}\right)$$

$$\left| \Delta v \right| = 2k\lambda \ln \frac{b}{a}$$

$$u = \frac{1}{2}C\Delta v^2 = \frac{1}{2}Q\Delta v = \frac{1}{2}\frac{Q^2}{C}$$

$$\frac{1}{2}\varepsilon_0^{}E^2=u_E^{}$$

$$k = \frac{E_0}{E}$$

$$\Delta \rho = \alpha \rho_0 \Delta T \quad \rightarrow \quad \rho = \rho_0 \left[1 + \alpha \left(T - T_0 \right) \right]$$

V: voltage

I: current

R: resistance

C: Capacitance

L: Inductance

Q: charge

P: power

ρ: resistivity of wire material

σ: *conductivity*

r: distance

J: current density

l: length of wire

A: cross-sectional area of the wire

U: potential or stored energy

κ: dielectric constant

 ε : emf

 ϕ_m : magnetic flux

B: magnetic field

 $\Delta \rho = \rho - \rho_0$: Change in resistivity

 ρ_0 : Initial resistivity

 $\Delta T = T - T_0$: Change in temperature

α: Temperature coefficient of resistivity

 $P_{\rm c}$: Power of a source

 W_{ς} : Work done by a source in transporting charges from

one to the other in a time Δt

 P_d : Power delivered to the external resistance

 $P_{\scriptscriptstyle R}$: Power dissipated in the external resistance

$$\vec{F}_B = I \Delta \vec{\ell} \times \vec{B} \qquad F_B = |q|VB \sin \theta$$

$$\vec{\tau} = I(\vec{A} \times \vec{B}) \rightarrow \tau = IAB \sin \theta$$

$$\vec{\mu} = I\vec{A} \qquad u = -\vec{\mu} \cdot \vec{B}$$

$$\vec{F}_{em} = q\vec{E} + q\vec{v} \times \vec{B}$$

$$v = \frac{qRB}{m}$$

$$E = \frac{1}{2m}q^2R^2B^2$$

$$B = \frac{\Delta V_H}{v_{\perp} d} = \frac{nqt\Delta V_H}{I} = \frac{I\mu_0}{2\pi r_{\perp}} = \frac{\mu_0 NI}{\ell}$$

$$d\vec{B} = \frac{\mu_0 I \, d\vec{s} \times \vec{r}_p}{4\pi r_p^3} \qquad \vec{B} = \frac{\mu_0}{4\pi} I \frac{d\vec{s} \times (\vec{r} - \vec{r'})}{\left|\vec{r} - \vec{r'}\right|^3} = \frac{\mu_0 I \, R^2}{2\left(a^2 + R^2\right)^{3/2}} \, \hat{k} = \frac{\mu_0 NI}{2R} \, \hat{k}$$

$$\frac{F_{12}}{\ell} = \frac{\mu_0 I_1 I_2}{2\pi d}$$

$$\oint_{\text{closed}} \vec{B} \cdot d\vec{s} = \mu_0 I = \mu_0 NI = \mu_0 \left(I + I_0 \right) = \mu_0 \left(I + \varepsilon_0 \frac{d\phi_E}{dt} \right)$$

$$B = \frac{\mu_0 I}{2\pi r_\perp} \quad if \quad r_\perp > R \qquad \quad B = \frac{\mu_0 r_\perp I}{2\pi R^2} \quad if \quad r_\perp < R$$

 F_R : Magnitude of magnetic force

V: Magnitude of velocity

B: Magnitude of magnetic field

 $\vec{\tau}$: Magnetic torque

 $\vec{\mu}$: Magnetic moment

 $d\vec{B} \rightarrow$ Magnetic field due to current *I* in a small path element $d\vec{s}$

 $\vec{r}_p \rightarrow$ Position vector of the point (P) with respect to the path element $d\vec{i}$

 $r_n \rightarrow$ Distance between path element and the point.

 $\mu_0 = 4\pi \times 10^{-7} \frac{Tm}{A} \rightarrow \text{A universal constant called magnetic permeability in vacuum.}$

 $r_{\perp} \rightarrow \bot$ distance between the wire and the point

 $\frac{F_{12}}{\ell}$ \rightarrow Force (magnetic) per unit length exerted by wire 2

 $\vec{B} \rightarrow$ Magnetic field at the location of $d\vec{s}$

 $I \rightarrow \text{Current crosses the closed path}$

 $N \rightarrow$ Number of turns

 ℓ \rightarrow Length of solenoid