Sec 4.1

2) 
$$\vec{u} = (2, -4)$$
 $\vec{x} = (1, 2)$ 
 $\vec{x} + \vec{y} = (1, 2) + (2, -2)$ 
 $= (1+2, 2-2)$ 
 $= (3, 1)$ 
 $\vec{x} + \vec{k} = (2, -3)$ 
 $\vec{x} + \vec{k} = (2, -3) + (-2, -1)$ 
 $\vec{x} + \vec{k} = (2, -3) + (-2, -1)$ 
 $= (-1, -4)$ 

#11.

 $\vec{u} = (-2, 3)$ 
 $\vec{x} = (-3, 3)$ 

び== (3は+四)

= = (-9, 7)

=(-皇, 圭)

 $=\frac{1}{2}(3(-2,3)+(-3,-2)$ 

19/ il= (1,2,3) N=(2,2,-1) U- F= (1,2,3) - (2,2,-1) = (-1,0,4) N-1= (2, 2, -1) - (1, 2,3) = (1,0,-4)) 2/ T= (1,2,3) N= (2,2,-1) W= (4,0,-4) 20 +41 -0 = 2(1,2,3)+4(2,2,-1)-(4,0,-4) =(6,12,6) 立=(1,2,3) 成=(4,0,-4) 32 -42 = 3 4 2 = 3 u - w == 1 (3(1,2,3) - (4,0,-4)) = = (-1,6,13) =(-1, 3, 12) a) u-1 = (4,0,-2,5) - (0,2,5,4) =(4,-2,-8,1)b) 2(1+31)=2((4,0,-3,5)+3(0,0,5,4)) =2(4,6,12,17) = (8, 12, 24, 34) c) 2N-1= 2 (0,2,54) - (4,0,-3,5) = (-4, 4, 13, 3) |

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sec 4.1 cont
33 \vec{u} = (1, 2, -3, 1) \vec{k} = (0, 2, -1, -2)
     \vec{\omega} = (2, -2, 1, 3)
 a) u+ov=(1,0,-3,1)+2(0,2,-1,-2)
           = (1,6,-5,-3)
  b) 1 -3 th = (2, -2, 1, 3) -3 (1, 2, -3, 1)
             =(-1,-8,10,0)
  C) 4 12-13-4 (0, 2,-1,-2)++(1, 2,-3,1)-(2,-2,1,3)
               = (-3, 11, -12, -21)
35  = (1,-1,0,1)  = (0,2,3,-1) - =?
   30 = 20-20
     成二十 [(1,-1,0,1)-2(0,2,3,-1)]
       == 1(1,-5,-6,3)
        = (3, -5, -2, 1)
41 R=(1,2) W=(1,-1)
  N=(2,1)
   (2,1) = (a,2a) + (b,-b)
       = (a+b, 2a-b)
    \frac{1}{2}a+b=2 \Rightarrow b=1
        30=3 => 0=11
     が= は+が1
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$$Sec 4.( | cont | d) = (1,2,4)$$

$$\vec{u}_3 = (10,1,4) \quad \vec{u}_1 = (2,3,5) \quad u_2 = (1,2,4)$$

$$\vec{u}_3 = (-2,2,2)$$

$$\vec{n} = x_1 \vec{u}_1 + x_2 \vec{u}_2 + x_3 \vec{u}_3$$

$$(10,1,4) = (2x_1 + x_2 - 2x_3) 2x_1 + 2x_2 + 2x_3, 5x_1 + 4x_2 + 3x_3$$

$$\begin{cases} 2x_1 + x_2 - 2x_3 = 10 \\ 3x_1 + 2x_2 + 2x_3 = 1 \end{cases}$$

$$5x_1 + 4x_2 + 3x_3 = 4$$

$$5x_1 + 2x_2 + 2x_3 = 1$$

$$5x_1 + 2x_2 + 2x_3 = 1$$

$$5x_1 + 2x_2 + 2x_3 = 21 = -3$$

$$5x_1 + 2x_2 + 2x_3 = 21 = -3$$

$$5x_1 + 2x_2 + 2x_3 = 21 = -3$$

$$5x_1 + 2x_2 + 2x_3 = 21 = -3$$

$$5x_1 + 2x_2 + 2x_3 = 21 = -3$$

$$5x_1 + 2x_2 + 2x_3 = 1$$

$$6x_1 + 2x_2 + 2x_3 + 2x_3 = 1$$

$$6x_1 + 2x_2 + 2x_3 + 2x_3 = 1$$

$$6x_1 + 2x_2 + 2x_3 + 2x$$

Sec 4.2 Y R": (0,0,0,0) 0 + 0x + 0x 2 + 0x3 3 R: (NI, NZ, NI)  $-(N_1, N_2, N_3) = (-N_1, -N_2, -N_3)$ 15/ P(G) = X + X = X D PO(x) =- x3-x2+2x (P, +P2)(x) = x3+x2-x2-x3-x+3x = x is not 3rd dag polyn. i. This set is not a rector space #31 } (x,0): ×≥0, 7 ∈ R3 Axiom 6: CUEV. Assume C=-1-0 -1 (2,7) = (-2,7) => -2 \$0 Axiom 6 failed i. This set is not a vector space 25 selica 57 >Maxz let M = (ab) M2 = (de) M3 = (2 b) Axiom 1: M, +M2 = (a b) + (d e) = (a+d b+c) & Maxz Axima: M,-M2=(a b)-(de) = (a-d b-e) E Man Axiom3: (1-+1/2+1/2= (2. 3)+(d e)+(2 0) = (a+d b+e) + (a b) = (a+d) + (a+b) + (a+b) = (a+d) + (a+b) + (a+b) = (a+d) + (a+b) + (a+b) $= \begin{pmatrix} a + (d+2) & b + (e+h) \\ c + (f+i) & 0 \end{pmatrix}$ = (a b) + (d+2 e+4) = M, + [ (d &) + (2 3)] Axiom 41 0=[00]

Axiom 41 0=[00] M, + 0 = (a 5) + (00) = (a 5) = M, Axim 5: M,+ (-M1) = (a b)+ (-a -5) = (0-0 5-5) = (0 0) 5 Max2

kM, = & ( a b) = (ak bk) & Marc = (an anz) = (an o) Axion 7, k. (M,+1/2)=k (a b)+(de) = k (a+d b+e) = (ak+dk bk+ek)
ck+fk o = (ah bk) + (dk -ek) = k(a b) + k(d e) = kM, + kM2 ~ Axiom 8: (k, +k2) M, = (k,+k2) (a b)  $= \begin{pmatrix} a(k_1+k_1) & b(k_1+k_2) \\ e(k_1+k_2) & 0 \\ = \begin{pmatrix} ak_1+ak_2 & bk_1+bk_2 \\ ck_1+ck_2 & 0 \end{pmatrix}$ = (ak, bk,) + (akz bkz) = k1(a b) + k2(a b) = k, M, + K2 M2 ~

Axiom 9: (k, k2) ( , = (k, k2) ( a b) = (akika bkika) = (ckika oki) = ki (aki bki) = k, (k, (a 5)) = k, (k2 Mi) ~. Axiom 101 1M, = 1 (a b) : set is a vector space

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Sec 4.2
39 N= (x, 2x): XER3
   Axiom 1: u=(x, 2x,) N=(x2, 2x2) W(x3, 2x3)
          U+N=(X1, 2X1)+(X2,2X2)
                = (x,+x2,2 (x,+x2)) let x = x,+x2
                = (x, 2x) EV.
    Axiom 2: U+N = (x,,2x1) + (x2) 2x2)
                   = (x,+x2 ) 2x,+2xx
                   = (x2 +x1, 2x2 +2x1)
                   = (x2,2x2) + (x,, 2x,)
                   = N+U =
    Axiem4:
            U+0= (x1,2x1)+ (0,0)
                  = (x,+0, 2x,+0)
                  =(x_{1}, 2x_{1})
   Axiom3: (u+N+W=((x,2x,)+(x2,2x2))+(x3+2x3)
                   = (x,+x2, 2x,+2x2)+ (x2, 2x3)
                   = ((x,+x2)+x3, (2x,+2x2)+2x3)
                   = (x,+(x,+x), 2x,+(2x))
                   = (x1,2x1)+ (x2+x3,2x2+2x3)
                    = 4+ ((x2,2x2) + (x3,2x3))
                    = u + (N+w) V.
   Axiom 5, U+(-U) = (x, 12x,) + (-(x, 2x,))
                    =(x_1, 2x_1)+(-x_1, -2x_1)
                     = (x,-x, , 2x,-2x)
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conf
  Sec 4. 2
39 cont
  Axiom 61 Ca=c(x, + 2x,)
                   = (cx, , 2cx,) let x=cx,
                   = (x1,2x1) EV.
 Axiom 7, C (u+w) = c ((x,,2x1)+(x2,2x2))
                     = ((x_1 + x_2, 2x_1 + 2x_2)
                      = (c(x,+x2), c(2x,+2x2))
                      = (cx, +cx2, 2cx, +2cx2)
                      = (CX, 2CX,) + (CX2, 2CX2)
                      = c(x,, 2x,) + c(x2, 2x2)
                       = CU+CNV
  Axiom 8: (c+d) u = (c+d) (x,, 2x,)
                   = ((c+d)x, , 2(c+d)x,)
                   = (cx, +dx, , 2cx, + 2dx,)
                    = (cx_1, 2cx_1) + (dx_1, 2dx_1)
= c(x_1, 2x_1) + d(x_1, 2x_1)
                     = cu +du ~
 Axiom9: (cd) u= (cd) (x,, 2x,)
                 = ((cd)x, , (cd)(2x,))
                 = (c(dx1) / c(2dx1))
                 = c (dx, 12dx,)
                  = ( [d(x1, 2x1)]
                 = c (du) ~
 Axiom 10 1 1 u = 1 (x1, 2x1) = (1x1, 1(2x1))
                  = (x,, 2x,)
: Theset is a vector space
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