***Solution Section* 1.1 − Statistical Thinking**

***Exercise***

Giants best the Denver Broncos in the Super Bowl by a score of 120 to 98. Use common sense to determine whether the given event is (***a***) *impossible*; (***b***) *possible*, *but very unlikely*; (***c***) *possible and likely*.

***Solution***

(***b***) Possible, but very unlikely.

Possible because there are no physical constraints or rules of the game that would prohibit such scores.

***Exercise***

While driving to his home in Connecticut, David was ticketed for driving 205 *mi/h* on a highway with a speed limit of 55 *mi/h*. Use common sense to determine whether the given event is (***a***) *impossible*; (***b***) *possible*, *but very unlikely*; (***c***) *possible and likely*.

***Solution***

(***b***) Possible, but very unlikely.

Possible if he were driving a race car that could attain such a speed.

***Exercise***

Thanksgiving Day will fall on a Monday nest year. Use common sense to determine whether the given event is (***a***) *impossible*; (***b***) *possible*, *but very unlikely*; (***c***) *possible and likely*.

***Solution***

(***a***) Impossible, In the U.S., Thanksgiving Day always falls on a Thursday.

***Exercise***

When each of 25 statistics students turns on his or her TI-84 Plus calculator, all 25 calculators operate successfully. Use common sense to determine whether the given event is (***a***) *impossible*; (***b***) *possible*, *but very unlikely*; (***c***) *possible and likely*.

***Solution***

(***c***) Possible and likely

***Exercise***

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| *Nicotine Amounts from Menthol and King-Size Cigarettes* | | | | | |
| ***x*** | 1.1 | 0.8 | 1.0 | 0.9 | 0.8 |
| ***y*** | 1.1 | 1.7 | 1.7 | 1.1 | 1.1 |

The *x*-values are nicotine amounts (in *mg*) in different 100 *mm* filtered, non-light menthol cigarettes; the *y*-values are nicotine amounts (in mg) in different king-size non-filtered, non-menthol, and non-light cigarettes.

Each *x* value associated with the corresponding *y* value in some meaningful way? If the *x* and *y* values are not matched, does it make sense to use the difference between each *x* value and the *y* value that is the same column?

***Solution***

There is nothing in the data to suggest that the *x* and *y* values are matched. If the *x* and *y* values are not matched as presented, it does not make sense to calculate the differences between the *x* and *y* values – moving *x* values around, for example, would yield a different set of differences.

***Exercise***

The Federal Trade Commission obtained the measured amounts of nicotine in the table. Is the source of the data likely to be unbiased?

Note that the table lists measured nicotine amounts from two different types of cigarette. Given these data, what issue can be addressed by conducting a statistical analysis of the values?

***Solution***

Yes, since the Federal Trade Commission receives no financial or other benefit from a particular set of results, there is no reason for the data or the data selected to be biased.

***Exercise***

One of Gregor Mendel’s famous hybridization experiments with peas yielding 580 off spring with 152 of those peas (or 26%) having yellow pods. According to Mendel’s theory, 25% of the off spring peas should have yellow pods. Do the results of the experiment differ from Mendel’s claimed rate of 25% by an amount that is statistically significant?

***Solution***

Determining whether or not the difference between Mendel’s actual results (26%) and the results predicted by his theory (25%) is statistically significant properly requires applying some techniques.

Common sense suggests the 1% difference is of no practical difference. Considering the sample size, the actual difference between the observed and expected results is 152 – 145 = 7. Common sense suggests that a discrepancy of 7 (relative to an expected result of 145 plants from a total sample of 580 plants) is within the natural fluctuation inherent biological processes, and that the difference is not statistically significant.

***Exercise***

In a Gallup poll of 1038 randomly selected adults, 85% said that secondhand smoke is somewhat harmful or very harmful, but a representative of the tobacco industry claims that only 50% of adults believe that secondhand smoke is somewhat harmful or very harmful. Is there statistically significant evidence against the representative’s claim? Why or why not?

***Solution***

Determining whether or not the difference between the survey results (85%) and the statement of the industry representative (50%) is statistically significant properly. But common sense suggests that this is statistically significant evidence against the representative’s claim because (1) the observed result of 85% is so much greater than the stated claim of the 50% and (2) the sample of 1038 randomly selected adults appears to be properly chosen and large enough to provide reliable data.

***Solution*** ***Section* 1.2 − Types of Data**

***Exercise***

In a large sample of households, the median annual income per household for high school graduates is $19,856 (based on data from the U.S. Census Bureau). Determine if it is a statistic or a parameter.

***Solution***

Statistic, since it was determined from a sample of households.

***Exercise***

Among the Senators in the current Congress, 44% are Democrats. Is it a statistic or a parameter?

***Solution***

Parameter, since it is based on the population of all Senators.

***Exercise***

A study of all 2223 passengers aboard the Titanic found that 706 survived when it sank. Is it a statistic or a parameter?

***Solution***

Parameter, since it was determined from the population of all 2223 passengers.

***Exercise***

If the areas of the 50 states are added and the sum is divided by 50, the result is 196,533 square kilometers. Is it a statistic or a parameter?

***Solution***

Parameter, since it was determined from the population of all 50 states.

***Exercise***

The average (mean) atomic weight of all elements in the periodic table is 134,355 unified mass units. Is it a statistic or a parameter?

***Solution***

Parameter, since it was determined from the population of all elements in the periodic table.

***Exercise***

Determine whether the given value is parametric or a statistic

1. One of greatest baseball hitters of all time has a career batting average of 0.366
2. A sample of employees is selected and it is found that 50% own a vehicle
3. A survey of 42 out of hundreds in a dining hall showed that 17 enjoyed their meal

***Solution***

1. Parameter
2. Statistic because the value is a numerical measurement describing a characteristic of a sample
3. Statistic, because the data set of 42 people in a dining hall is a sample.

***Exercise***

Suppose a survey of 568 women in the U.S. found that more than 61% are the primary investor in their household.

1. Describe the survey represents the descriptive branch of statistic
2. Make an inference based on the results of the survey

***Solution***

1. 61% of women in the sample are the primary investor in their household
2. There is an association between U.S. women and being the primary investor in their household

***Exercise***

In the recent study, volunteers who had 8 hours of sleep were three times more likely to answer questions correctly on a math test than were sleep-deprived participaants.

1. Identify the sample used in the study
2. What is the sample’s population
3. Which part of the study represents the descriptive branch of statistics
4. Make an inference based on the results of the study

***Solution***

1. The sample is the responses of the volunteers in the study
2. The population is the collection of the responses of all individuals who completed the math test
3. The statement “three times more likely to answer questions correctly” is an example of descriptive statistics
4. Individuals who are not sleep deprived will be more likely to answer math questions correctly than individuals who are sleep deprived.

***Exercise***

Determine whether the data set is a population or a sample. Explain your reasoning

The salary if each baseball player in a league

***Solution***

Population, because it is a collection of salaries for all baseball players in the league

***Exercise***

In a poll, 1,004 adults in a country were asked whether they favor or oppose the use of “federal tax dollars to find medical research using stem cells obtained from human embryos.” Among the responders, 48% said that they were in favor. Describe the statistical study

1. What is the population?
2. Identify the sample

***Solution***

1. All adults in the country
2. The 1,004 adults selected

***Exercise***

A study shows that the obesity rate among boys ages 2 to 19 has increased over the past several years

1. Make an inference based on the results of this study?
2. What is wrong with this type of reasoning

***Solution***

1. The obesity rate among boys ages 2 to 19 is increasing
2. This inference may incorrectly imply that the trend will continue in future years.

***Exercise***

In the Literary Digest poll, Landon received 16,679,583 votes. Is it from a discrete or continuous data set?

***Solution***

Discrete, since the number of votes received must be a whole number.

***Exercise***

The amount of nicotine in a Marlboro cigarette is 1.2 mg. Is it from a discrete or continuous data set?

***Solution***

Continuous, since the amount of nicotine could be any value on a continuum; even though it is reported to the nearest 0.1 mg.

***Exercise***

The volume of cola in a can of regular coke is 12.3 oz. Is it from a discrete or continuous data set?

***Solution***

Continuous, since the volume could be any value on a continuum; even though it is reported to the nearest 0.1 oz.

***Exercise***

When a woman is randomly selected and measured for blood pressure, the systolic blood pressure is found to be 61 mm Hg.

***Solution***

Continuous, since the systolic pressure could be any value on a continuum; even though it is reported to the nearest 61 mm Hg.

***Exercise***

Types of movies (drama, comedy, adventure, documentary, etc.). Determine which of the four levels of measurement (nominal, ordinal, interval, ratio) is most appropriate.

***Solution***

Nominal, since the data give category names only and there is no natural ordering.

***Exercise***

Critic ratings of movies on a scale from 0 star to 4 stars. Determine which of the four levels of measurement (nominal, ordinal, interval, ratio) is most appropriate

***Solution***

Ordinal, since the categories have a natural ordering but the differences between the categories are not necessarily uniform.

***Exercise***

Ranks of cars evaluated by Consumer’s Union. Determine which of the four levels of measurement (nominal, ordinal, interval and ratio) is most appropriate

***Solution***

Ordinal, since the ranks have a natural ordering but the differences between the ranks are not necessarily uniform.

***Exercise***

The newspaper USA Today published a health survey, and some readers completed the survey and returned it. Identify the (*a*) sample and (*b*) population, also determine whether the sample likely to be representative of the population.

***Solution***

1. The sample is the readers who completed and returned the survey.
2. The population is all people who read USA Today.
3. No, since the sample is self-selected it is not likely to be representative of the population. Only those with special interest in health matters are likely to return the survey.

***Exercise***

A Gallup poll of 1012 randomly surveyed adults found that 9% of them said cloning of humans should be allowed. Identify the (*a*) sample and (*b*) population, also determine whether the sample likely to be representative of the population.

***Solution***

1. The sample is the 1012 randomly selected adults.
2. The population is all adults. This should probably be understood to be all adults living in the U.S.
3. Yes, since the adults were selected at random by an organization with experience in polling and with no vested interest in the results, the sample is likely to be representative of the population.

***Exercise***

Some people responded to this request: “Dial 1-900-PRO-LIFE to participate in a telephone poll on abortion. ($1.95 per minute. Average call: 2 minutes. You must be 18 years old.)” Identify the (*a*) sample and (*b*) population, also determine whether the sample likely to be representative of the population

***Solution***

1. The sample is the people who responded to the request.
2. The intended population is likely all persons over 18. The actual population is actually all persons over 18 who have opportunity to receive the request. If the request went out over the internet, for example, the population would be all internet users over 18. If the request went out over several radio and/or TV stations, the population would be all persons over 18 who tune in to those stations.
3. No, since the sample is self-selected it is not likely to be representative of the population. Only those with special interest in abortion issues are likely to spend the time and money to respond to the survey.

***Exercise***

In the Born Loser cartoon strip by Art Sansom, Brutus expresses joy over an increase in temperature from 1° to 2°. When asked what is so good about 2°, he answers that “it’s twice as warm as this morning.” explain why Brutus is wrong yet again.

***Solution***

Temperature ratios are not meaningful because a temperature of 0° does not represent the absence of temperature in the same sense that $0 represents the absence of money. The zero temperature in the exercise (whether Fahrenheit or Centigrade) was determined by a criterion other than “the absence of temperature.”

***Exercise***

A group of students develops a scale for rating the quality of cafeteria food, with 0 representing “neutral: not good and not bad.” Bad meals are given negative numbers and good meals are given positive numbers, with the magnitude of the number corresponding to the severity of badness or goodness. The first three meals are rated as 2, 4, and −5. What is the level of measurement for such rating? Explain your choice.

***Solution***

This is example of ordinal data. It is not interval data because differences are not meaningful. The difference between the ratings +4 and +5 does not necessarily represent the same differential in the quality of food as the difference between 0 and +1.

***Exercise***

Suppose that a study based on a sample from a targeted population shows that people who own a fax machine have more money than people who do not

1. Make an inference based on the results of this study?
2. What might this inference incorrectly imply?

***Solution***

1. People who own a fax machine have more money than people who do not
2. This inference may incorrectly inply that if you owned a fax machine, you would have more money than if you did not.

***Exercise***

Determine whether the statement is true or false, rewrite it as a true statement

1. Data at the ordinal level are quantitative only
2. More types of calculations can be performed with data at the nominal level than with data at the interval level

***Solution***

1. False. Data at the ordinal level can be qualitative or quantitative
2. False. More types of calculations can be performed with data at the interval level than with data at the nominal level.

***Exercise***

Determine whether the variable is qualitative or quantitative

1. Favorite film
2. Population of country of origin
3. Gallons of water in a swimming pool
4. Model of car driven
5. Distance in miles to nearest school
6. Time in hours that a light bulb lasts
7. Number of students at a high school

***Solution***

1. Qualitative
2. Quantitative
3. Quantitative
4. Qualitative
5. Quantitative
6. Quantitative
7. Quantitative

***Exercise***

The region of a country with the highest per capita income for the past six years is shown below

Northeast Southern Southwest Southeast Northern Western

1. Determine whether the data are qualitative or quantitative and identify the data set’s level of measurement
2. What is the data set’s level of measurement?

***Solution***

1. Qualitative
2. Nominal

***Exercise***

The region of a country with the six highest level of food production last year are shown below

1. Eastern 2. Southwest 3. Western 4. Southeast 5. Northwest 6. Southern

1. Determine whether the data are qualitative or quantitative and identify the data set’s level of measurement
2. What is the data set’s level of measurement?

***Solution***

1. Quantitative
2. Ordinal

***Exercise***

The region of a country with the six highest level of food production last year are shown below

22.8 26.4 24.1 22.2 21.6 21.1 25.8 21.5 24.6

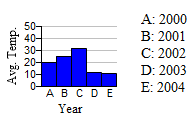
1. Determine whether the data are qualitative or quantitative and identify the data set’s level of measurement
2. What is the data set’s level of measurement?

***Solution***

1. Quantitative
2. Ratio

***Exercise***

The graph shows the average temperature in an artic city, in degree Fahrenheit, for certain years. Identify the level of measurement of the data listed on the horizontal axis in the graph



***Solution***

Interval

***Exercise***

Identify the level of measurement of the data:

|  |  |
| --- | --- |
| 1. Temperature 2. Age | 1. Family history of illness 2. Pain level (scale of 0 to 10) |

***Solution***

1. Interval
2. Ratio
3. Nominal
4. Ordinal

***Solution*** ***Section* 1.3 − Critical Thinking**

***Exercise***

Typical surveys involve about 500 people to 2000 people. When author Shere Hire wrote Woman and Love: A Cultural Revolution in Progress, she based conclusions on a relatively large sample of 4500 replies that she received after mailing 100,000 questionnaires to various women’s groups. Are her conclusions likely to be valid in the sense that they can applied to the general population of all women? Why or why not?

***Solution***

No. Since she used a voluntary response sample, the responses that she received are likely to be from those with strong feelings on the topic and not representative of the entire population. Even if she had not used a voluntary response sample, the results would apply only to women who were members of the different women’s groups that she surveyed, and not to the general population of all women.

***Exercise***

Based on a study showing that college graduates tend to live longer than those who do not graduate from college, a researcher concludes that studying causes people to live longer. Use critical thinking to develop an alternative or correct conclusion.

***Solution***

College graduates tend to earn more money than non-graduates, and people who have more money are able to purchase better health care. Having more money (whether or not it resulted from having a college degree) and not studying more is the primary contribution factor toward longer life.

***Exercise***

In the judicial case U.S. v. City of Chicago, a minority group failed the Fire Captain Examination at a much higher rate than the majority group. Conclusion: The exam is biased and causes members of the minority group to fail at a much higher rate. Use critical thinking to develop an alternative or correct conclusion.

***Solution***

It could be that the exam is a fair instrument to measure the aptitude for the job, but that larger percentages of the members of the minority group fail the test reasons other than the test breing biased. There may be fewer opportunities for the minorities, causing a larger number of them (including those who are lesser qualified) to unrealistically attempt the exam.

***Exercise***

When Harris Interactive surveyed 1013 adults, 91 % of them said that they washed their hands after using a public restroom. But when 6336 adults were observed, it was found that 82% actually did wash their hands. How can we explain the discrepancy? Which percentage is more likely to accurately indicate the true rate at which people wash their hands in a public restroom?

***Solution***

Self-reporting is not always a reliable method of gathering information. People tend to answer questions in a manner that will reflect well on them; they tend to give the answer they wish were true, or that they wish others to believe about them, rather than the true answer. The 82% rate is more likely to be accurate because it was based on objective observation rather than self-reporting.

***Exercise***

The Internet service provider AOL ran a survey of its users and asked if they preferred a real Christmas tree or a false one. AOL received 7073 responses, and 4650 of them preferred a real tree. Given that 4650 is 66% of the 7073 responses; can we conclude that about 66% of people who observe Christmas prefer a real tree? Why or why not?

***Solution***

No. Since the 66% figure is biased on a voluntary response sample, it might reflect only the views of those with strong feelings and not the views of the general population. In addition, the views of those using the internet are not necessarily representative of the views of the general population, particularly in matters involving tradition and technology.

***Exercise***

After the last national census was conducted, the Poughkeepsie Journal ran this front-page headline: “281,421,906 in America.” What is wrong with this headline?

***Solution***

The headline suggests a level of precision that is not warranted. While the national census attempts to be complete, various types of undercounts are known to occur. In addition, the data are collected over a period of time – during which people are constantly dying and being born. Even if the data collected were 100% correct, no single figure could claim to be the exact population at a specific given moment.

***Exercise***

The *Statistical Abstract of the United States* includes the average per capita income for each of the 50 states. When those 50 values are added, then divided by 50, the result is $29,672.52. Is $29,672.52 the average per capita income for all individuals in the U.S.? Why or why not?

***Solution***

No, this is not likely to be a good estimate of the average per capita income for all individuals in the U.S. States with small populations but high wages (due to the cost of living) like Alaska and Hawaii, for example, contribute 2/50 =4% of the average for the 50 states – but since they do not contain 4% of the U.S. wages earners, they inflate the estimate to make it higher than the true average of all US wage earners. In general, the average of averages does not give the overall average.

***Exercise***

The author surveyed students with this request: “Enter your height in inches,” Identify two major problems with this request.

***Solution***

One problem would be in obtaining the correct value: some people may not know their exact heights; some people may think they know their heights but be mistaken, and some people may deliberately exaggerate their heights. Another problem would be in recording the correct value: some people may record 6’ 2” and have it misread as 62”, some people who are not mathematical and/or not used to speaking in terms of inches only may mistakenly convert 6’ 2” into 62”, and some people of other cultures who know their exact height in another system my not be familiar with inches (centimeters).

***Exercise***

Convert the fraction  to an equivalent percentage.

***Solution***

***Exercise***

Convert the fraction  to an equivalent percentage. Express the answer to the near tenth of a percent.

***Solution***

***Exercise***

Convert 23.4% to an equivalent decimal.

***Solution***

***Exercise***

Convert 83% to an equivalent decimal.

***Solution***

***Exercise***

What is 37% of 500?

***Solution***

***Exercise***

What is 5% of 5020?

***Solution***

***Exercise***

Convert 0.127 to an equivalent percentage.

***Solution***

***Exercise***

Convert 0.045 to an equivalent percentage.

***Solution***

***Exercise***

In a Gallup poll, 49% of 734 surveyed Internet users said that they shop on the Internet frequently or occasionally. What is the actual number of Internet users who said that the shop on the internet frequently or occasionally.

***Solution***

***Exercise***

Ina a Gallup poll of 976 adults, 68 said that they have a drink every day. What is the percentage of respondents who said that they have a drink every day?

***Solution***

***Exercise***

Among 976 adults surveyed, 32% said that they never drink. What is the actual number of surveyed adults who said that they never drink?

***Solution***

***Exercise***

A New York Times editorial criticized a chart caption that described a dental rinse as one that “reduces plaque on teeth by over 300%.” What is wrong with that statement?

***Solution***

When plaque is reduced by 100%, there is none remaining. To reduce plaque by 300% would be to eliminate 3 times as much plaque as there is to begin with – which is not physically possible.

***Exercise***

In an ad for the Club, a device used to discourage car thefts, it was stated that “The club reduces your odds of car theft by 400%.” What is wrong with this statement?

***Solution***

To reduce something by 100% is to eliminate all of it. When the odds of the occurrence of some event are reduced by 100% the event becomes impossible, No further reduction is possible, The ad may have intended to say that “The Club makes car theft one-fourth as likely”.

***Solution*** ***Section* 1.4 − Collecting Sample Data**

***Exercise***

A Gallup poll surveyed 1018 adults by telephone, and 22% of them reported that they smoked cigarettes within the past year. Determine whether the description corresponds to an observation study or an experiment.

***Solution***

Observational study, since the poll involves collecting data from unmodified subjects.

***Exercise***

In a morally and criminally wrong study, 399 black men with syphilis were not given a treatment that could have cured them. The intent was to learn about the effects of syphilis on black men, The subjects were initially treated with small amounts of bismuth, neoarsphenamine, and mercury, but those treatments were replaced with aspirin. Determine whether the description corresponds to an observation study or an experiment.

***Solution***

Experiment, since the effect of an applied treatment (in this case a zero dose of the appropriate medicine) was measured.

***Exercise***

A student of the author collected measurements of arm lengths from her family members. Identify what type is used: random, systematic, convenience, stratified, or cluster.

***Solution***

Convenience, since the sample is those who happened to be in the student’s family.

***Exercise***

On the day of the last presidential election, ABC News organized an exit poll in which specific polling stations were randomly selected and all voters were surveyed as they left the premises. Identify what type is used: random, systematic, convenience, stratified, or cluster.

***Solution***

Cluster, since all the voters at randomly selected polling stations were surveyed.

***Exercise***

The author was an observer at a town of Poughkeepsic Police sobriety checkpoint at which every fifth driver was stopped and interviewed. (He witnessed the arrest of a former student.) Identify what type is used: random, systematic, convenience, stratified, or cluster.

***Solution***

Systematic, since every 5th driver was stopped

***Exercise***

You observed professional wine taster working at the Consumer’s Union testing facility in NY. Assume that a taste test involves three different wines randomly selected from each of five different wineries. Identify what type is used: random, systematic, convenience, stratified, or cluster.

***Solution***

Stratified, since the population of wines was subdivided into 5 different subgroups (wineries), and then samples were drawn from each subgroup.

***Exercise***

The U.S. Department of Corrections collects data about returning prisoners by randomly selecting five federal prisons and surveying all of the prisoners in each of the prisons. Identify what type is used: random, systematic, convenience, stratified, or cluster.

***Solution***

Cluster, since all the prisoners at five randomly selected prisons were surveyed.

***Exercise***

You instructor surveyed all of his students to obtain sample consisting of the number of credit cards students possess. Identify what type is used: random, systematic, convenience, stratified, or cluster.

***Solution***

Convenience, since the sample is those who happen to be students of the author.

***Exercise***

In a study of college programs, 820 students are randomly selected from those majoring in communications, 1463 students are randomly selected from those majoring in business, and 760 students are randomly selected from those majoring in history. Identify what type is used: random, systematic, convenience, stratified, or cluster.

***Solution***

Stratified, since the population was subdivided into 3 different subgroups, and then samples were drawn from each subgroup. The population of interest appears to be only communications, business and history majors – most likely because the programs being studied involved only those majors.

***Exercise***

Pharmacists typically fill prescriptions by scooping a sample of pills from a larger batch that is in stock. A pharmacist thoroughly mixes a large batch of Lipitor pills, then selects 30 of them. Does this sampling plan result in a random sample? Simple random sample? Explain.

***Solution***

Yes, it is a random sample because each pill has an equal chance of being selected.

Yes, it is a simple random sample because each sample of size 30 has an equal chance of being selected.

***Exercise***

A quality control engineer selects every 10,000*th* M&M plain candy that is produced. Does this sampling plan result in a random sample? Simple random sample? Explain.

***Solution***

Whether the sample is a random depends on how the first selection is made. If the engineer chooses the first one at random from 1 to 10,000 and every 10,000th one thereafter, then every M&M has an equal chance of being selected (namely 1 in 10,000) and the sample is a random sample. If the engineer determines to start with #1 and choose every 10,000th one thereafter, then some M&M’s have no chance of being selected (e.g., #2) and the sample is not a random sample.

No, no matter how the first selection is made the sample will not be a simple random sample of size *n*. All possible grouping of size *n* are not possible – any grouping containing #1 and #1, for example, could not occur.

***Exercise***

NBC News polled reactions to the last presidential election by surveying adults who were approached by a reporter at a location in N.Y. City. Does this sampling plan result in a random sample? Simple random sample? Explain.

***Solution***

No, this is not a random sample of all New Yorkers because persons who did not visit the location had not chance of being selected.

No it is not a simple random because it is not a random sample.

***Exercise***

A classroom consists of 36 students seated in six different rows, with six students in each row. The instructor rolls a die to determine a row, then rolls the die again to select a particular student in the row. This process is repeated until a sample of 6 students is obtained. Does this sampling plan result in a random sample? Simple random sample? Explain.

***Solution***

Yes, the results in a random sample because each student has an equal chance of being selected.

Yes, this results in a simple random sample of size 6 because each possible grouping of size 6 has an equal chance to occur.

***Exercise***

A computer company employs 100 software engineers and 100 hardware engineers. The personnel manager randomly selects 20 of the software engineers and 20 of the hardware engineers and questions them about career opportunities within the company. Does the sampling plan result in a random sample? Simple random sample? Explain.

***Solution***

Yes, the sample is random because all employees have the same chance of being selected.

No, it is not a simple random sample because some samples are possible, such as a sample consisting of 30 software engineers and 10 hardware engineers.

***Exercise***

A polling company obtains an alphabetical list of names of voters in a precinct. They select every 20th person from the list until a sample of 100 is obtained. They then call these 100 people. Does the sampling plan result in a random sample? Simple random sample? Explain.

***Solution***

No. The sample is not random because not all voters have the same chance of being selected.

No, the second person on the list has no chance of being selected. It is not a simple random sample because some samples are not possible, such as a sample containing the second person on the list.

***Exercise***

What is an inherent zero? Describe three examples of data sets that have inherent zeroes and three that do not.

***Solution***

An inherent zero is a zero that implies none.

1. Average age of college students in years
2. Maximum wing speed during a hurricane
3. Average monthly precipitation in inches

***Exercise***

What is the different between a random sample and a simple random sample?

***Solution***

With a random sample, each individual has the same chance of being selected. With a simple random sample, all samples of the same size have the same chance of being selected.

***Exercise***

Determine whether the statement is true or false. If false, rewrite it as a true statement

1. In a randomized block design, subjects with similar characteristics are divided into blocks, and then, within each block, randomly assigned to treatment groups.
2. Using a systematic sample guarantees that members of each group within a population will be sampled.
3. The method for selected a stratified sample is to order a population in some way and then select members of the population at regular intervals.

***Solution***

1. True
2. False. Using a stratified sample guarantees that members of each group within a population will be sampled.
3. False. The method for selecting systematic sample is to order a population in some way and then select members of the population at regular intervals.

***Exercise***

Which method of data collection should be used to collect data for the following study

1. A study of the health of 148 kidney transplant patients at a hospital.
2. A study of the effect on the taste of a snack food made with a sugar substitute
3. A study of how fast a virus would spread in a herd of cattle.

***Solution***

1. Census
2. Experiment
3. Simulation

***Exercise***

A pharmaceutical company wants to test the effectiveness of a new allergy drug. The company identifies 250 females 30-35 years old who suffer from severe allergies. The subjects are randomly assigned into two groups. One group is given the new allergy drug and the other is given a placebo that looks exactly like the new allergy drug. After six months, the subjects’ symptoms are studied and compared

1. Identify the experimental units and treatment used in this experiment.
2. Identify a potential problem with the experiment design being used and suggest a way to improve it.
3. How could this experiment be designed to be a double-blind?

***Solution***

1. The experiment units are the 30- to 35- year old females being given the treatment is the new allergy drug.
2. There may be a bias on the part of the researcher knows which patients were given the real drug.
3. The study would be a double-blind study if both the researcher and the patient did not know which patient received the real drug or the placebo

***Exercise***

What type of sampling is used: random, stratified, convenience, cluster, systematic, in the following?

1. Toyota wants to administer a satisfaction survey to its current customers. Using their customer database, the company randomly selects 80 customers and asks them about their level of satisfaction with the company
2. To determine her power usage, Dan divides up his day into three parts: morning, afternoon, and evening. He then measures his power usage at 3 randomly selected times during each part of the day.
3. A newspaper asks its readers to call in their opinion regarding the number of books they have read this month.
4. Toshiba wants to administer a satisfaction survey to its current customers. Using their customer database, the company randomly selects 80 customers and asks them about their level of satisfaction with the company.
5. An education researcher randomly selects 48 middle schools and interviews all the teachers at each school.
6. A market researcher selects 500 drivers under 30 years of age and 500 drivers over 30 years of age.
7. To avoid working late, a quality control analyst simply inspects the first 100 items produced in a day.

***Solution***

1. Simple random
2. Stratified
3. Convenience
4. Simple random
5. Cluster
6. Stratified
7. Convenience

***Exercise***

Determine whether you would take a census or use a sampling to collect data for the study described:

1. The average credit card debt of the 65 employees of a company
2. The most popular grocery store among the 40,000 employees of a company

***Solution***

1. Census
2. Sampling

***Exercise***

Determine if the survey question is biased. If the question is biased, suggest a better wording

1. Why drinking fruit juice good for you?
2. Why is eating ice cream bad for you?

***Solution***

1. Yes. How do you think drinking fruit juice affects your health?
2. Yes. How do you think eating ice cream affects your health?

***Exercise***

A company has been rating television programs for more than 60 years. It uses several sampling procedures, but its main one is to track the viewing patterns of 20,000 households. These contain more than 45,000 people and are chosen to form a cross section of the overall population. The households represent various locations, ethnic groups, and income brackets. The data gathered from the sample of 20,000 households are used to draw inferences about the population of all households in the U.S.

1. What strata are used in the sample?
2. Why is it important to have a stratified sample for these ratings?
3. Observation studies are sometimes referred to as natural experiments. Explain what this means

***Solution***

1. The various locations, ethnic groups, and income brackets that are represented.
2. Stratified sampling ensures that each segment of the population is represented.
3. In an observation study, a researcher measures characteristics of interest of a part of a population but does not change existing conditions.

***Exercise***

Some polling agencies ask people to call a telephone number and give their response to a question

1. What is an advantage of this type of survey?
2. What is disadvantage of this type of survey?
3. Identify the sampling technique used.

***Solution***

1. This usually results in a savings in the survey cost.
2. There tends to be a lower response rate and this may introduce a bias into the sample. Only a certain segment of the population might respond.
3. Convenience sampling.

***Exercise***

A computer company employs 100 software engineers and hardware engineers. The personnel manager randomly selects 20 of the software engineers and 20 of the hardware and questions them about career opportunities within the company. Does this sampling plan result in a random sample? Simple random sample? Explain.

***Solution***

Yes it is random sample and it is not a simple random sample.

The sample is random because all employees have the same chance of being selected. It is not a simple random sample because some examples are not possible, such as a sample consisting of 30 software engineers and 10 hardware engineers

***Solution*** ***Section* 1.5 − Frequency Distributions and Histograms**

***Exercise***

Identify the class width, class midpoints, and class boundaries for the given frequency distribution. Then construct the cumulative frequency distribution that corresponds to the frequency distribution.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| *a*) | |  |  | | --- | --- | | ***Tar (mg) in Nonfiltered Cigarettes*** | ***Frequency*** | | 10 – 13 | 1 | | 14 – 17 | 0 | | 18 – 21 | 15 | | 22 – 25 | 7 | | 26 – 29 | 2 | | *b*) | |  |  | | --- | --- | | ***Tar (mg) in Filtered Cigarettes*** | ***Frequency*** | | 2 – 5 | 2 | | 6 – 9 | 2 | | 10 – 13 | 6 | | 14 – 17 | 15 | |
| *c*) | |  |  | | --- | --- | | ***Weights (lb) of Discarded Metal*** | ***Frequency*** | | 0.00 – 0.99 | 5 | | 1.00 – 1.99 | 26 | | 2.00 – 2.99 | 15 | | 3.00 – 3.99 | 12 | | 4.00 – 4.99 | 4 | | *d*) | |  |  | | --- | --- | | ***Weights (lb) of Discarded Plastic*** | ***Frequency*** | | 0.00 – 0.99 | 14 | | 1.00 – 1.99 | 20 | | 2.00 – 2.99 | 1 | | 3.00 – 3.99 | 4 | | 4.00 – 4.99 | 2 | | 5.00 – 5.99 | 1 | |

***Solution***

1. *Class width*:  (***Subtracting the first two lower class limits***)

*Class midpoints*:  adding **4** to obtain the rest: 11.5, 15.5, 19.5, 23.5, 27.5.

*Class boundaries*:  (boundary between the first and second class). The other can be obtained by adding 4: 9.5, 13.5, 17.5, 21.5, 25.5, 29.5.

1. *Class width*:  (***Subtracting the first two lower class limits***)

*Class midpoints*:  adding **4** to obtain the rest: 3.5, 7.5, 11.5, 15.5.

*Class boundaries*:  (boundary between the first and second class). The other can be obtained by adding 4: 1.5, 5.5, 9.5, 13.5, 17.5.

1. *Class width*:  (***Subtracting the first two lower class limits***)

*Class midpoints*:  adding **1.00** to obtain the rest: 0.495, 1.495, 2.495, 3.495, 4.495.

*Class boundaries*:  (boundary between the first and second class). The other can be obtained by adding or subtracting **1.00**: -0.005, 0.995, 1.995, 2.995, 3.995, 4.995.

1. *Class width*:  (***Subtracting the first two lower class limits***)

*Class midpoints*:  adding **1.00** to obtain the rest: 0.495, 1.495, 2.495, 3.495, 4.495, 5.495.

*Class boundaries*:  (boundary between the first and second class). The other can be obtained by adding or subtracting **1.00**: -0.005, 0.995, 1.995, 2.995, 3.995, 4.995, 5.995.

***Exercise***

In a study, researchers treated 570 people who smoke with either nicotine gum or a nicotine patch. Among those treated with nicotine gum, 191 continued to smoke and the other 59 stopped smoking. Among those treated with nicotine patch, 263 continued to smoke and the other 57 stopped smoking (based on data from the Center for Disease Control and Prevention). Construct the relative frequency distribution.

***Solution***

Obtain the relative frequencies by dividing the given frequencies by the total of 570.

|  |  |  |
| --- | --- | --- |
| ***Those whose smoking*** |  | ***Relative Frequency*** |
| Continued after the gum |  | 33.5 % |
| Stopped after the gum |  | 10.4 % |
| Continued after the patch |  | 46.1 % |
| Stopped after the patch |  | 10.0 % |
|  | | 100.0 % |

***Exercise***

Heights of statistics students were obtained by the author as part of a study conducted for class. The last digits of those heights are listed below. Construct a frequency distribution with 10 classes. Based on the distribution, do the heights appear to be reported or actually measured? What do you know about the accuracy of the results?

0 0 0 0 0 0 0 0 0 1 1 2 3 3 3 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 6 6 8 8 8 9

***Solution***

|  |  |
| --- | --- |
| ***Digit*** | ***Frequency*** |
| 0 | 9 |
| 1 | 2 |
| 2 | 1 |
| 3 | 3 |
| 4 | 1 |
| 5 | 15 |
| 6 | 2 |
| 7 | 0 |
| 8 | 3 |
| 9 | 1 |
|  | 37 |

The heights are not actually measured because the data have been round off and showed unusually high numbers of 0’s and 5’s.

***Exercise***

Listed below are amounts of strontium-90 (in millibecquerels) in a simple random sample of baby teeth obtained from Pennsylvania residents born after 1979, Construct a frequency distribution with eight classes. Begin with a lower class limit of 110, and use a class width of 0. Cite a reason why such data are important.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 155 | 142 | 149 | 130 | 151 | 163 | 151 | 142 | 156 | 133 | 138 | 161 | 128 | 144 |
| 172 | 137 | 151 | 166 | 147 | 163 | 145 | 116 | 136 | 158 | 114 | 165 | 169 | 145 |
| 150 | 150 | 150 | 158 | 151 | 145 | 152 | 140 | 170 | 129 | 188 | 156 |  |  |

***Solution***

Lowest number: 114 Highest number: 188

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| |  |  | | --- | --- | | ***level*** | ***Frequency*** | | 110 – 119 | 2 | | 120 – 129 | 2 | | 130 – 139 | 5 | | 140 – 149 | 9 | | 150 – 159 | 13 | | 160 – 169 | 6 | | 170 – 179 | 2 | | 180 – 189 | 1 | |  | 40 | | Such data are important because they can be helpful in detecting potentially dangerous situations and in making recommendations for future action |

***Exercise***

Refer to the data below and use the 40 voltage measurements from the generator. Construct a frequency distribution with seven classes. Begin with a lower class limit of 123.9 volts, and use a class width of 0.20 volt. Using a very loose interpretation of the relevant criteria, does the result appear to have a normal distribution?

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 124.8 | 124.3 | 125.2 | 124.5 | 125.1 | 124.8 | 125.1 | 125.0 | 124.8 | 124.7 | 124.5 | 125.2 | 124.4 | 124.7 |
| 124.9 | 124.5 | 124.8 | 124.8 | 124.5 | 124.6 | 125.0 | 124.7 | 124.9 | 124.9 | 124.7 | 124.2 | 124.7 | 124.8 |
| 124.4 | 124.6 | 124.4 | 124.0 | 124.7 | 124.4 | 124.6 | 124.6 | 124.6 | 124.8 | 124.3 | 124.0 |  |  |

***Solution***

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| |  |  | | --- | --- | | ***Voltage (volts)*** | ***Frequency*** | | 123.9 – 124.0 | 2 | | 124.1 – 124.2 | 1 | | 124.3 – 124.4 | 6 | | 124.5 – 124.6 | 9 | | 124.7 – 124.8 | 13 | | 124.9 – 125.0 | 5 | | 125.1 – 125.2 | 4 | | Yes;  The voltages do appear to follow a normal distribution.  There are many values near the center of the distribution, and the frequencies diminish toward either end. |

***Exercise***

As part of the Garbage Project at the University of Arizona, the discarded garbage for 62 households was analyzed. Refers to the 62 weights from table below and construct a frequency distribution. Begin with a lower class of 1.00 lb., and use a class width of 4.00 lb. Do the weights of discarded paper appear to have a normal distribution?

2.41 11.08 9.45 5.88 7.57 12.43 12.32 8.26 9.55 6.05 20.12 12.45

8.82 13.61 7.72 10.58 8.72 6.98 6.16 5.87 6.96 14.33 7.98 8.78

6.83 13.31 9.64 11.03 11.42 3.27 8.08 12.29 16.08 6.67 10.99 20.58

6.38 17.65 13.11 12.56 13.05 12.73 3.26 9.92 11.36 9.83 1.65 3.45

15.09 16.39 10 9.09 2.8 6.33 8.96 3.69 6.44 9.19 9.46 2.61

5.86 9.41

***Solution***

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| |  |  | | --- | --- | | ***Weight (lbs)*** | ***Frequency*** | | 1.00 – 4.99 | 8 | | 5.00 – 8.99 | 21 | | 9.00 – 12.99 | 22 | | 13.00 – 16.99 | 8 | | 17.00 – 20.99 | 3 | |  | 62 | | Yes,  The weights appear to have a distribution that is approximately normal. |

***Exercise***

*a*) Refer to the data below for the FICO credit rating scores. Construct a frequency distribution beginning with a lower class limit of 400, and use a class width of 50. Does the result appear to have a normal distribution? Why or why not?

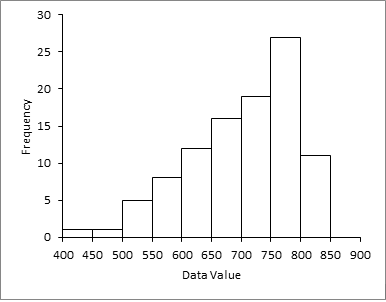
|  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 708 | 713 | 781 | 809 | 797 | 793 | 711 | 681 | 768 | 611 | 698 | 729 | 829 |
| 836 | 768 | 532 | 657 | 559 | 741 | 792 | 701 | 753 | 745 | 681 | 594 | 744 |
| 598 | 693 | 743 | 444 | 502 | 739 | 755 | 835 | 714 | 517 | 787 | 706 | 752 |
| 714 | 497 | 636 | 637 | 797 | 568 | 714 | 618 | 830 | 579 | 818 | 722 | 783 |
| 751 | 731 | 850 | 591 | 802 | 756 | 689 | 789 | 654 | 617 | 849 | 604 | 630 |
| 628 | 692 | 779 | 756 | 782 | 760 | 503 | 784 | 798 | 611 | 709 | 661 | 579 |
| 591 | 834 | 694 | 795 | 660 | 651 | 696 | 638 | 697 | 732 | 796 | 753 | 782 |
| 635 | 795 | 519 | 682 | 824 | 603 | 709 | 777 | 664 |  |  |  |  |

*b*) Use the table to construct a histogram. Does the result appear to be normal distribution? Why or why not?

***Solution***

|  |  |
| --- | --- |
| ***FICO score*** | ***Frequency*** |
| 400 – 449 | 1 |
| 450 – 499 | 1 |
| 500 – 549 | 5 |
| 550 – 599 | 8 |
| 600 – 649 | 12 |
| 650 – 699 | 16 |
| 700 – 749 | 19 |
| 750 – 799 | 27 |
| 800 – 849 | 10 |
| 850 – 899 | 1 |
|  | 100 |

*b*)



The data appear to have a distribution that is not normal. While there is a maximum value with progressively smaller frequencies on either side of the maximum, the distribution is definitely not symmetric.

***Exercise***

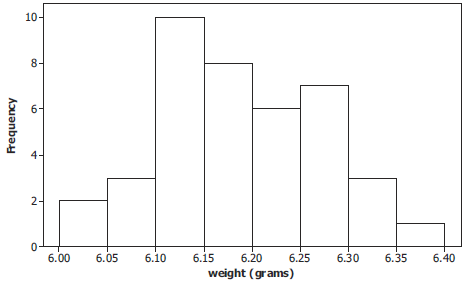
Refer to the data in the table below. Construct a frequency distribution. Begin with lower class limit of 6.0000 g, and use a class width of 0.0500 g.

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| 6.2771 | 6.2371 | 6.1501 | 6.0002 | 6.1275 | 6.2151 |
| 6.2866 | 6.0760 | 6.1426 | 6.3415 | 6.1309 | 6.2412 |
| 6.1442 | 6.1073 | 6.1181 | 6.1352 | 6.2821 | 6.2647 |
| 6.2908 | 6.1661 | 6.2674 | 6.2718 | 6.1949 | 6.2465 |
| 6.3172 | 6.1487 | 6.0829 | 6.1423 | 6.1970 | 6.2441 |
| 6.3669 | 6.0775 | 6.1095 | 6.1787 | 6.2130 | 6.1947 |
| 6.1940 | 6.0257 | 6.1719 | 6.3278 |  |  |

***Solution***

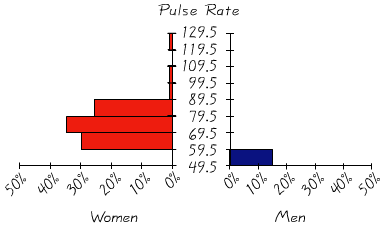
|  |  |
| --- | --- |
| ***Weight* (*g*)** | ***Frequency*** |
| 6.0000 – 6.04999 | 2 |
| 6.0500 – 6.0999 | 3 |
| 6.1000 – 6.1499 | 10 |
| 6.1500 – 6.1999 | 8 |
| 6.2000 – 6.2499 | 6 |
| 6.2500 – 6.2999 | 7 |
| 6.3000 – 6.3499 | 3 |
| 6.3500 – 6.3999 | 1 |
|  | 40 |

b)



***Exercise***

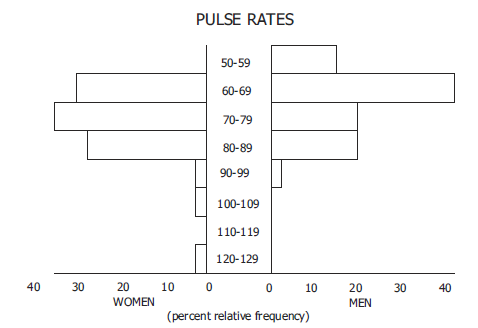
When using histograms to compare two data sets, it is sometimes difficult to make comparisons by looking back and forth between the two histograms. A back-to-back relative frequencies histogram uses a format that makes the comparison much easier. Instead of frequencies, we should use relative frequencies (percentages or proportions) so that the comparisons are not distorted by different sample sizes. Complete the back-to-back relative frequency histograms shown below by using the data below. Then use the result to compare the two data sets.



|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| **Pulse Rates (*beats per minute*) of Females and Males** | | | | | | | | | | | | | | | | | | | |
| ***Females*** | | | | | | | | | | | | | | | | | | | |
| 76 | 72 | 88 | 60 | 72 | 68 | 80 | 64 | 68 | 68 | 80 | 76 | 68 | 72 | 93 | 72 | 68 | 72 | 64 | 80 |
| 64 | 80 | 76 | 76 | 76 | 80 | 104 | 88 | 60 | 76 | 72 | 72 | 88 | 80 | 60 | 72 | 88 | 88 | 124 | 64 |
| ***Males*** | | | | | | | | | | | | | | | | | | | |
| 68 | 64 | 88 | 72 | 64 | 72 | 60 | 88 | 76 | 60 | 96 | 72 | 56 | 64 | 60 | 64 | 84 | 76 | 84 | 88 |
| 72 | 56 | 68 | 64 | 60 | 68 | 60 | 60 | 56 | 84 | 72 | 84 | 88 | 56 | 64 | 56 | 56 | 60 | 64 | 72 |

***Solution***

The back-to-back relative frequency histograms are given below. The pulse rates of the males tend to be lower than those of the females.



***Solution Section* 1.6 − Statistical Graphics**

***Exercise***

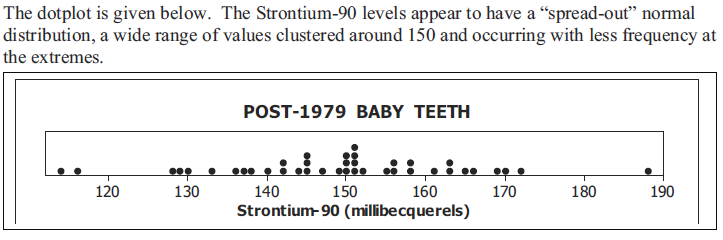
Given listed amounts of Strontium-90 (in millibecquerels) in a simple random sample of baby teeth.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 155 | 142 | 149 | 130 | 151 | 163 | 151 | 142 | 156 | 133 | 138 | 161 | 128 | 144 | 172 |
| 137 | 151 | 166 | 147 | 163 | 145 | 116 | 136 | 158 | 114 | 165 | 169 | 145 | 150 | 150 |
| 150 | 158 | 151 | 145 | 152 | 140 | 170 | 129 | 188 | 156 |  |  |  |  |  |

1. Construct a dot plot of the amounts of Strontium-90. What does the dot plot suggest about the distribution of those amounts?
2. Construct a stemplot of the amounts of Strontium-90. What does the stemplot suggest about the distribution of those amounts?
3. Construct a frequency polygon of the amounts of Strontium-90. For the horizontal axis, use the midpoints of the class intervals in the frequency distribution: 110-119, 120-129, 130-139, …, 180-189.
4. Construct an ogive of the amounts of Strontium-90. For the horizontal axis, use the class boundaries corresponding to the class limits. How many of the amounts are below 150 millibecquerels?

***Solution***

1. The dotplot is given below.



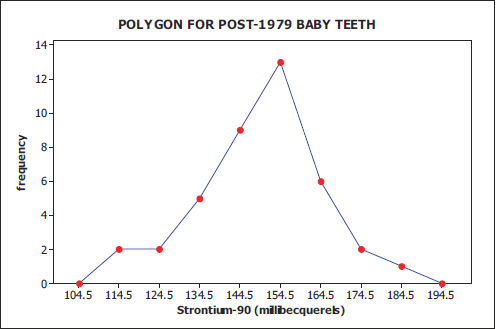
The strontium-90 levels appear to have a normal distribution clusters around 150.

1. The stemplot is given:

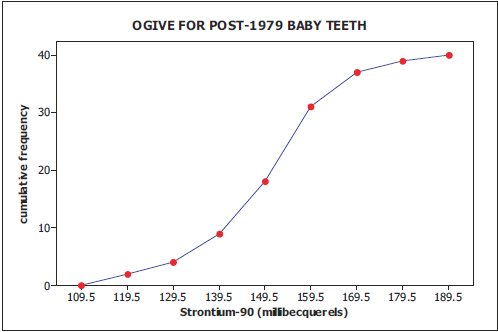
|  |  |
| --- | --- |
| ***Strontium* – 90** | |
| 11 | 46 |
| 12 | 89 |
| 13 | 03678 |
| 14 | 022455579 |
| 15 | 0001111256688 |
| 16 | 133569 |
| 17 | 02 |
| 18 | 8 |

The strontium-90 levels appear to have a normal distribution clusters around 150.

1. The frequency polygon is given:



1. The ogive is given:



Using the figure: move up from 150 on the horizontal scale to intersect the graph, then move left to intersect the vertical scale at 18. This indicates there were approximately 18 data values which would have been recorded as being below 150, which agrees with the actual data values.

***Exercise***

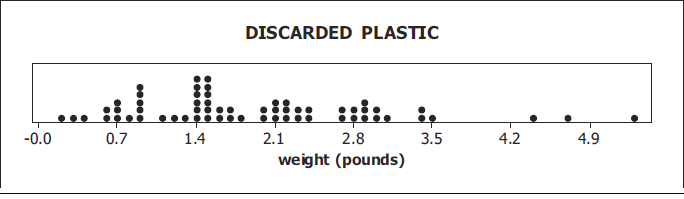
Use the 62 weights if discarded plastic listed in Data set below

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 0.27 | 1.41 | 2.19 | 2.83 | 2.19 | 1.81 | 0.85 | 3.05 | 3.42 | 2.10 | 2.93 | 2.44 | 2.17 | 1.41 | 2.00 |
| 0.93 | 2.97 | 2.04 | 0.65 | 2.13 | 0.63 | 1.53 | 4.69 | 0.15 | 1.45 | 2.68 | 3.53 | 1.49 | 2.31 | 0.92 |
| 0.89 | 0.80 | 0.72 | 2.66 | 4.37 | 0.92 | 1.40 | 1.45 | 1.68 | 1.53 | 1.44 | 1.44 | 1.36 | 0.38 | 1.74 |
| 2.35 | 2.30 | 1.14 | 2.88 | 2.13 | 5.28 | 1.48 | 3.36 | 2.83 | 2.87 | 2.96 | 1.61 | 1.58 | 1.15 | 1.28 |
| 0.58 | 0.74 |  |  |  |  |  |  |  |  |  |  |  |  |  |

1. Construct a dot plot of the weights of discarded plastic. What does the dot plot suggest about the distribution of the weights?
2. Construct a stemplot of the weights of discarded plastic. What does the stemplot suggest about the distribution of the weights?
3. Construct a frequency polygon of the weights of discarded plastic. For the horizontal axis, use the midpoints of the class intervals: 0.00-0.99, 1.00-1.99, 2.00-2.99, 3.00-3.99, 4.00-4.99, 5.00-5.99.
4. Construct an ogive of the weights of discarded plastic. For the horizontal axis, use these classes boundaries: −0.005, 0.995, 1.995, 2.995, 3.995, 4.995, 5.995. How many of the weights are below 4 lb.?

***Solution***

1. The dotplot is given below.



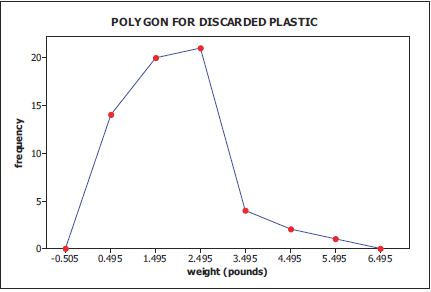
The weights appear to be approximately normally distributed, except for the presence of a few high values.

1. The stemplot is given:

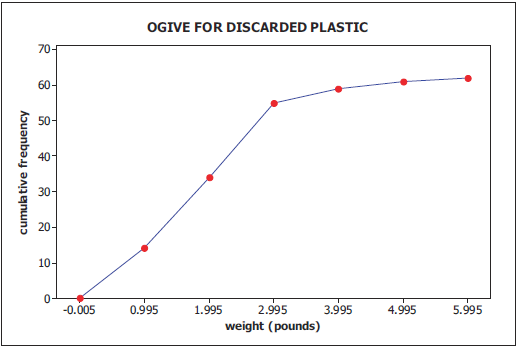
|  |  |
| --- | --- |
| ***Weight* (*lb.*)** | |
| 0. | 1256677888999 |
| 1. | 11234444444445556678 |
| 2. | 001111113334668888999 |
| 3. | 9345 |
| 4. | 36 |
| 5. | 2 |

The weights appear to be approximately normally distributed, except for the necessary lower truncation at zero.

1. The frequency polygon is given:



1. The ogive is given



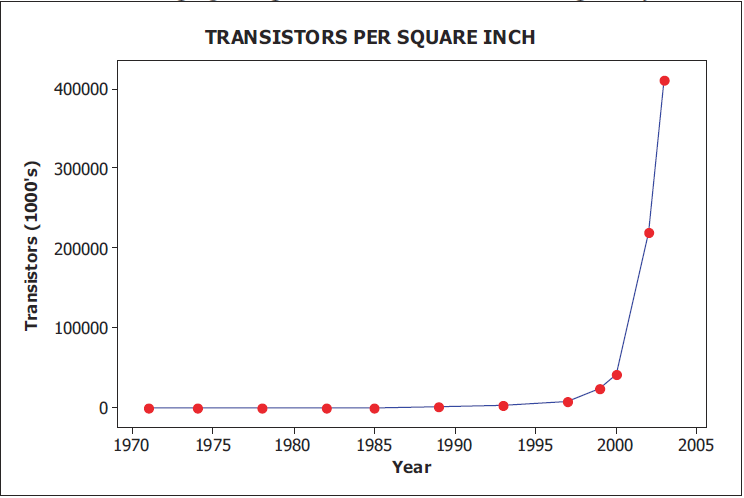
*Using the figure*: move up 3 on the horizontal scale to intersect the graph, then move left to intersect the vertical scale at 59. This indicates there were approximately 59 data values which would have been recorded as being below 4, which agrees with the actual data.

***Exercise***

In 1965, Intel cofounder Gordon Moore proposed what has since become known as Moore’s law: the number of transistors per square inch on integrated circuits with double approximately every 18 months. The table below lists the number of transistors per square inch (in thousands) for several different years. Construct a time-series graph of the data.

|  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| **Year** | 1971 | 1974 | 1978 | 1982 | 1985 | 1989 | 1993 | 1997 | 1999 | 2000 | 2002 | 2003 |
| **Transistors** | 2.3 | 5 | 29 | 120 | 275 | 1180 | 3100 | 7500 | 24,000 | 42,000 | 220,000 | 410,000 |

***Solution***



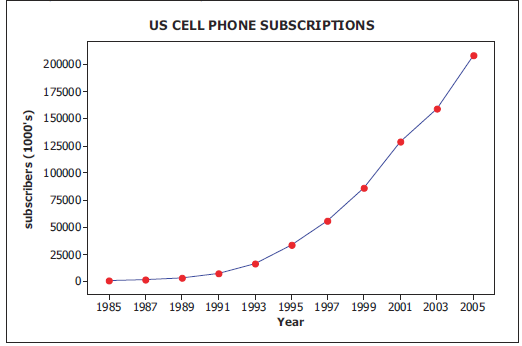
***Exercise***

The following table shows the numbers of cell phone subscriptions (in thousands) in the U.S. for various years. Construct a time-series graph of the data. “Linear” growth would result in a graph that is approximately a straight line. Does the time-series graph appear to show linear growth?

|  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| **Year** | 1985 | 1987 | 1989 | 1991 | 1993 | 1995 | 1997 | 1999 | 2001 | 2003 | 2005 |
| **Number** | 340 | 1231 | 3509 | 7557 | 16,009 | 33,786 | 55,312 | 86,047 | 128,375 | 158,722 | 207,900 |

***Solution***

The time series graph is given:



The graph does not appear to show linear growth (constant slope) over the entire time period, but does appear that there was linear growth during certain periods (since 1999)

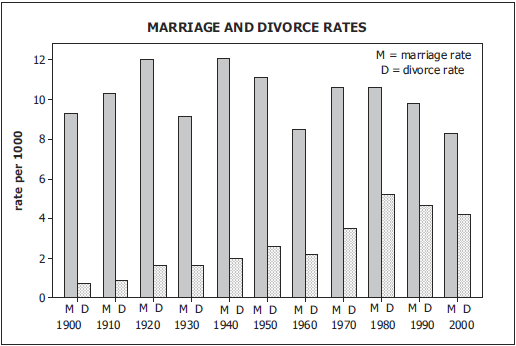
***Exercise***

The following table lists the marriage and divorce rates per 1000 people in the U.S. for selected years since 1900 (based on data from the Department of Health and Human Services). Construct a multiple bar graph of the data. Why do these data consist of marriage and divorce rates rather than total numbers of marriages and divorces? Comment on any trends that you observe in these rates, and give explanations for these trends.

|  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| **Year** | 1900 | 1910 | 1920 | 1930 | 1940 | 1950 | 1960 | 1970 | 1980 | 1990 | 2000 |
| **Marriage** | 9.3 | 10.3 | 12.0 | 9.2 | 12.1 | 11.1 | 8.5 | 10.6 | 10.6 | 9.8 | 8.3 |
| **Divorce** | 0.7 | 0.9 | 1.6 | 1.6 | 2.0 | 2.6 | 2.2 | 3.5 | 5.2 | 4.7 | 4.2 |

***Solution***

AS the population increases, the *numbers* of marriages and divorces will automatically increase. To identify any change in marriage and divorce patterns, one needs to examine the *rates*. This is analogous to using percents (or relative frequencies) instead of frequencies to compare categories for two samples of different sizes. The marriage rate appears to have remained fairly constant, with possible slight decrease in recent years. The divorce rate appears to have steadily grown, with a possible slight decrease in recent years.



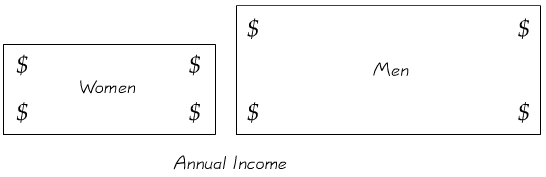
***Exercise***

Assume that, as a newspaper reporter, you must graph data showing that increased smoking causes an increased risk of lung cancer. Given that people might be helped and lives might be saved by creating a graph that exaggerates the risk of lung cancer, is it ethical to construct such a graph?

***Solution***

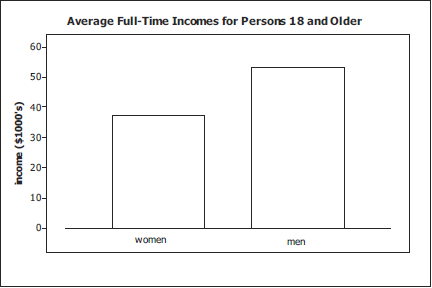
No. Results should be presented in a way that is fair and objective so that the reader has the reliable information necessary to reach his own conclusion.

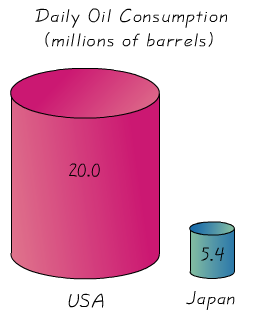
***Exercise***

The accompanying graph depicts average full-time incomes of women and men aged 18 and over. For a recent year, those incomes were $37,197 for women and $53,059 for men (based on data from the U.S. Census Bureau). Does the graph make a fair comparison of the data? Why or why not? If the graph distorts the data, construct a fair graph.

***Solution***

The average income for men is about 1.4 times the average income for women. Making the men’s pictograph 1.4 times as wide and 1.4 times as high as the women’s produces a men’s image with  the areas of the women’s image. Since it is the area that gives the visual impression in a two-dimensional figure, the men’s average income appears to be almost twice that of the women’s average income.

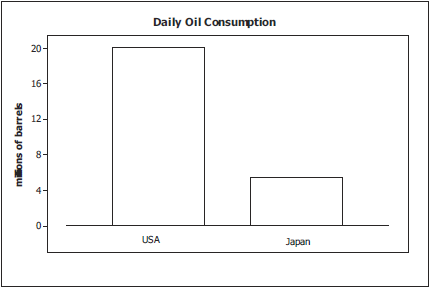


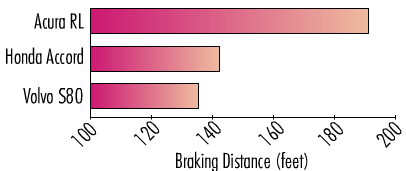
***Exercise***

The accompanying graph uses cylinders to represent barrels of oil consumed by the U.S. and Japan. Does the graph distort the data or doe it depict the data fairly? Why or why not? If the graph distorts the data, construct a graph that depicts the data fairly.

***Solution***

The oil consumption for the USA is about 3.7 times the oil consumption for Japan. Making the USA’s pictograph 3.7 times larger than Japan’s in three dimensional produces an image for the US with  times the volume of the image for Japan. Since it is perceived volume that gives the visual impression in the figure, the consumption for US appears 50 times that for Japan.

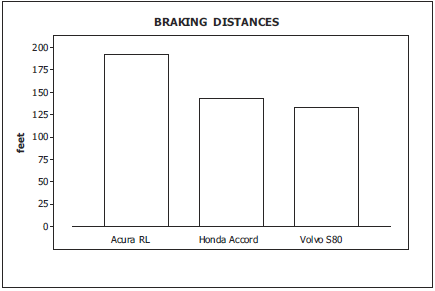


***Exercise***

The accompanying graph shows the braking distances for different cars measured under the same conditions. Describe the ways in which this graph might be deceptive. How much greater is the braking distance of the Acura RL than the braking distance of the Volvo S80? Draw the graph in a way that depicts the data more fairly.

***Solution***

It appears that the braking distance for the Acura RL is more than twice that of the Volvo S80. The actual difference is about 60 ft., and the Acura RL distance is about  times that of the Volvo. The exaggeration of differences is caused by the fact that the distance scale dies not start at zero.



***Exercise***

Use the data to create a stemplot

The midterm test scores for the seventh-period typing class are listed below

85 77 93 91 74 65 68 97 88 59 74 83 85 72 63 79

***Solution***



***Exercise***

Use the data to create a stemplot

Twenty-four workers were surveyed about how long it takes them to travel to work each day. The data below are given in minutes

20 35 42 52 65 20 60 49 24 37 23 24

22 20 41 25 28 27 50 47 58 30 32 48

***Solution***



***Exercise***

Find the original data from the stemplot



***Solution***

762, 766, 767, 772, 774, 779, 781, 787

***Solution Section* 1.7 − Measures of Center**

***Exercise***

In what sense are the mean, median, mode and midrange measures of “center”?

***Solution***

The mean, median, mode, and midrange are measures of “center” in the sense that they each attempt to determine (by various criteria – i.e., by using different approaches) what might be designated as a typical or representative value.

***Exercise***

A headline in USA Today stated that “Average family income drops 2.3%.” What is the role of the term average in statistics? Should another term be used in place of average?

***Solution***

The term *average* is not used in statistics because it is imprecisely used by the general public as a synonym for *typical* – as in, the average American had blue eyes. When referring to the result obtained by dividing a sum by the number of values contributing to that sum, the term ***mean*** should be used.

***Exercise***

In an editorial, the Poughkeepsie Journal printed this statement: “The median price – the price exactly in between the highest and lowest -- …” Does that statement correctly describes the median? Why or why not?

***Solution***

No. The price exactly in between the highest and the lowest would be the mean of the highest and lowest values – which is the midrange, and not the median.

***Exercise***

A simple random sample of pages from Merriam-Webster’s Collegiate Dictionary, 11th edition, was obtained. Listed below are the numbers of words defined on those pages. Given that this dictionary has 1459 pages with defined words, estimate the total number of defined words in the dictionary.

51 63 36 43 34 62 73 39 53 79

Find the

*a*) mean *b*) median *c*) mode *d*) midrange

*e*) Is that estimate likely to be an accurate estimate of the number of words in the English language?

***Solution***

34 36 39 43 51 53 62 63 73 79

1. *Mean*: 
2. *Median*: 
3. *Mode*: None
4. *Midrange*: 
5. Using the mean of 53.3 words per page, a reasonable estimate for the total number of words in the dictionary is . Since the sample is a simple random sample, it should be representative of the population and the estimate of 77,675 is a valid estimate for the number of words in the dictionary – but not for the total number of words in the English language, since the dictionary does not claim to contain every word.

***Exercise***

The National Highway Traffic Administration conducted crash tests of child booster seats for cars. Listed below are results from those teats, with the measurements given in *hic* (standard head injury condition units.

774 249 1210 546 431 612

Find the

*a*) mean *b*) median *c*) mode *d*) midrange

*e)* According to the safety requirement, the *hic* measurement should be less than 1000 *hic*. Do the results suggest that all of the child booster seats meet the specified requirement?

***Solution***

431 546 612 649 774 1210

1. *Mean*: 



1. *Median*: 
2. *Mode*: None
3. *Midrange*: 
4. No. Even though all four measures of center fall within with accepted guidelines, all the individual values do not. Since one result exceeds the guidelines, it is clear that all child booster seats do not meet the requirement.

***Exercise***

The insurance Institution for Highway Safety conducted tests with crashes of new cars traveling at 6 mi/h. The total cost of the damages was found for a simple random sample of the tested cars and listed below

$7448 $4911 $9051 $6374 $4277

Find the

*a*) mean *b*) median *c*) mode *d*) midrange

*e*) Do the different measures of center differ very much?

***Solution***

4277 4911 6374 7448 9051

1. *Mean*: 
2. *Median*: 
3. *Mode*: None
4. *Midrange*: 
5. No. Even though the sample values cover a fairly wide range, the measures of center do not differ very much.

***Exercise***

Listed below are the durations (in hours) of a simple random sample of all flights (as of this writing) of NASA’s Space Transport System (space shuttle).

73 95 235 192 165 262 191 376 259 235 381 331 221 244 0

Find the

*a*) mean *b*) median *c*) mode *d*) midrange

1. How might that duration time be explained?

***Solution***

0 73 95 165 191 192 221 235 235 244 259 262 331 376 381

1. *Mean*: 





1. *Median*: 
2. *Mode*: 235 ***hrs***.
3. *Midrange*: 
4. The duration of time of 0 appears to be very unusual. It likely represents Challenger disaster of Jan 1986, when the mission ended in an explosion shortly after takeoff.

***Exercise***

Listed below are the playing times (in seconds) of songs that were popular at the time of this writing.

448 242 231 246 246 293 280 227 213 262 239 213 258 255 257 244

Find the

*a*) mean *b*) median *c*) mode *d*) midrange

*e*) Is there on time that is very different from the others?

***Solution***

213 213 227 231 239 242 244 246 246 255 257 258 262 280 293 448

1. *Mean*: 





1. *Median*: 
2. *Mode*: 213, 246 ***sec***.
3. *Midrange*: 
4. Yes the time of 448 seconds appears to be very different from the others.

***Exercise***

Listed below are numbers of satellites in orbit from different countries.

158 17 15 17 7 3 5 1 8 3 4 2 4 1 2 3 1 1 1 1 1 1 1 1

Find the

*a*) mean *b*) median *c*) mode *d*) midrange

*e*) Does on country have an exceptional number of satellites?

*f*) Can you guess which country has the most satellites?

***Solution***

1 1 1 1 1 1 1 1 1 1 2 2 3 3 3 4 4 5 7 8 15 17 18 158

1. *Mean*: 





1. *Median*: 
2. *Mode*: 1 ******.
3. *Midrange*: 
4. Yes the country with 158 satellites has an exceptional number of them.
5. That country is most likely the United States.

***Exercise***

Listed below are costs (in dollars) of roundtrip flights from JFK airport in NY City to San Francisco. (All flights involve one stop and a two-week stay.) The airlines are US Air, Continental, Delta, United, American, Alaska, and Northwest.

|  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- |
| 30 Days in Advance | 244 | 260 | 264 | 264 | 278 | 318 | 280 |
| 1 Day in Advance | 456 | 614 | 567 | 943 | 628 | 1088 | 536 |

1. Find the mean and median for each then compare the two sets of results.
2. Does it make much difference if the tickets are purchased 30 days in advance or 1 day in advance?

***Solution***

|  |  |
| --- | --- |
| 30 Days in Advance | 244 260 264 264 278 280 318 |
| 1 Day in Advance | 456 536 567 614 628 943 1088 |

1. *Mean*: 

*Median*: 

*Mean*: 

*Median*: 

1. The tickets purchased 30 days in advance are considerably less expensive – they appear to cost less than half of the tickets purchased one day in advance.

***Exercise***

The trend of thinner Miss America winners has generated charges that the contest encourages unhealthy diet habits among young women. Listed below are body mass indexes (BMI) for Miss America winners from two different periods.

|  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| BMI (1920 – 1930) | 20.4 | 21.9 | 22.1 | 22.3 | 20.3 | 18.8 | 18.9 | 19.4 | 18.4 | 19.1 |
| BMI – (from recent winners) | 19.5 | 20.3 | 19.6 | 20.2 | 17.8 | 17.9 | 19.1 | 18.8 | 17.6 | 16.8 |

Find the mean and median for each then compare the two sets of results.

***Solution***

|  |  |
| --- | --- |
| BMI (1920 – 1930) | 18.4 18.8 18.9 19.1 19.4 20.3 20.4 21.9 22.1 22.3 |
| BMI – (*from recent winners*) | 16.8 17.6 17.8 17.9 18.8 19.1 19.5 19.6 20.2 20.3 |

1. *Mean*: 

*Median*: 

*Mean*: 

*Median*: 

1. The recent winners appear to have lower measures of BMI than do the former winners.

***Exercise***

Find the mean of the data summarized in the given frequency distribution.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| |  |  | | --- | --- | | ***Tar* (*mg*) *in Nonfiltered Cigarettes*** | ***Frequency*** | | 10 – 13 | 1 | | 14 – 17 | 0 | | 18 – 21 | 15 | | 22 – 25 | 7 | | 26 – 29 | 2 | | |  |  | | --- | --- | | ***Pulse Rates of Females*** | ***Frequency*** | | 60 – 69 | 12 | | 70 – 79 | 14 | | 80 – 89 | 11 | | 90 – 99 | 1 | | 100 – 109 | 1 | | 110 – 119 | 0 | | 120 – 129 | 1 | |

***Solution***

|  |  |  |
| --- | --- | --- |
| ***x*** | ***f*** |  |
| 11.5 | 1 | 11.5 |
| 15.5 | 0 | 0 |
| 19.5 | 15 | 292.5 |
| 23.5 | 7 | 164.5 |
| 27.5 | 2 | 55.0 |
|  | 25 | 523.5 |



This is close to the true value of 21.1 mg.

|  |  |  |
| --- | --- | --- |
| ***x*** | ***f*** |  |
| 64.5 | 12 | 774.0 |
| 74.5 | 14 | 1043.0 |
| 84.5 | 11 | 929.5 |
| 94.5 | 1 | 94.5 |
| 104.5 | 1 | 104.5 |
| 114.5 | 0 | 0.0 |
| 124.5 | 1 | 124.5 |
|  | 40 | 3070.0 |



This is close to the true value of 21.1 mg.

***Exercise***

A student of the author earned grades of B, C, B, A, and D. Those courses has these corresponding numbers credit hours: 3, 3, 4, 4, and 1. The grading system assigns quality points to letter grades as follows: A = 4; B = 3; C = 2; D = 1; F =0. Compute the grade point average (GPA) and round the result with two decimal places. If the Dean’s list requires a GPA 3.00 or greater, did this student make the Dean’s list?

***Solution***

The *x* values are the numerical values of the letter grades, and the corresponding weights are the numbers of credit hours.

|  |  |  |
| --- | --- | --- |
| ***x*** | ***w*** |  |
| 3 | 3 | 9 |
| 2 | 3 | 6 |
| 3 | 4 | 12 |
| 4 | 4 | 16 |
| 1 | 1 | 1 |
|  | 15 | 44 |



No; since 2.93 is below 3.00, the student did not make the Dean’s list.

***Exercise***

A student of the author earned grades of 92, 83, 77, 84, and 82 on her five regular tests. She earned grades of 88 on the final exam and 95 on her class projects. Her combined homework grade was 77. The five regular tests count for 60% of the final grade, the final exam counts for 10%, the project counts for 15%, and homework counts for 15%. What is her weighted mean grade? What letter grade did she earn? (A, B, C, D, or F)

***Solution***

|  |  |  |
| --- | --- | --- |
| ***x*** | ***w*** |  |
| 92 | 0.12 | 11.04 |
| 83 | 0.12 | 9.96 |
| 77 | 0.12 | 9.24 |
| 84 | 0.12 | 10.08 |
| 82 | 0.12 | 9.84 |
| 88 | 0.10 | 8.80 |
| 95 | 0.15 | 14.25 |
| 77 | 0.15 | 11.55 |
|  | 1.0 | 84.76 |

The *x* values are the individual grades, and the corresponding weights are the percent of the final grade.

Since the 5 regular tests count for 60% of the final grade, each regular test counts for:

 of the final grade.



Her weighted mean grade is 84.8. Within 90-80-70-60 grading system for A-B-C-D, that corresponds to B.

***Exercise***

You are taking a class in which your grade is determined from five sources: 50% from your test mean, 15% from your midterm, 20% from your final exam, 10% from your computer lab work, and 5% from your homework. Your scores are 86 (test mean), 96 (midterm), 82 (final exam), 98 (computer lab), and 100 (homework). What is the weighted mean of your scores? If the minimum average for an A is 90, did you get an A?

***Solution***

|  |  |  |  |
| --- | --- | --- | --- |
| ***Source*** | ***x*** | ***w*** |  |
| Test mean | 86 | 0.50 | 73.0 |
| Midterm | 96 | 0.15 | 14.4 |
| Final Exam | 82 | 0.20 | 16.4 |
| Computer lab | 98 | 0.10 | 9.8 |
| Homework | 100 | 0.05 | 5.0 |
|  |  | 1 | 88.6 |



Your weighted mean for the course is 88.6. So you did not get an *A*.

***Exercise***

During a quality assurance check, the actual coffee contents (in ounces) of six jars of instant coffee were recorded as 6.03, 5.59, 6.40, 6.00, 5.99, and 6.02.

1. Find the mean and the median of the coffee content.
2. The third value was incorrectly measured and is actually 6.04. Find the mean and median of the coffee content again.
3. Which measure of central tendency, the mean or the median, was affected more by the data entry error?

***Solution***

1. 





1. 





1. The mean was affected more

***Exercise***

The table below shows the U.S. exports (in billions of dollars) to 19 countries for a recent year.

|  |  |  |
| --- | --- | --- |
| ***U.S. Exports*** (in billions of dollars) | | |
| Canada: 261.1 | Mexico: 151.2 | Germany: 54.5 |
| Taiwan: 24.9 | Netherlands: 39.7 | China: 69.7 |
| Australia: 22.2 | Malaysia: 12.9 | Switzerland: 22.0 |
| Saudi Arabia: 12.5 | United Kingdom: 53.6 | Japan: 65.1 |
| South Korea: 34.7 | Singapore: 27.9 | France: 28.8 |
| Brazil: 32.3 | Belgium: 28.9 | Italy: 15.5 |
| Thailand: 9.1 |  |  |

1. Find the mean and the median.
2. Find the mean and median without the U.S. exports to Canada. Which measure of central tendency, the mean or the median, was affected more by the elimination of the Canadian exports?
3. The U.S. Exports to India were $17.7 billion. Find the mean and median with the Indian exports added to the original data set. Which measure of central tendency was affected more by adding the Indian exports?

***Solution***

1. 





1. 





The mean was affected more

1. 





The mean was affected more

***Solution Section* 1.8 − Measures of Variation**

***Exercise***

In statistics, how do variation and variance differ?

***Solution***

Variation is a general descriptive term that refers to the fact that all the items being measured are not identical. In Statistics, variance is a specific and well-defined measure of variation the has a particular mathematical formula.

***Exercise***

Collegiate Dictionary has 1459 pages of defined words. Listed below are the numbers of defined words per page for a simple random sample of those pages. If we use this sample as a basis for estimating the total number of defined words in the dictionary.

|  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 51 | 63 | 36 | 43 | 34 | 62 | 73 | 39 | 53 | 79 |

1. Find the range, variance, and standard deviation.
2. How does the variation of these numbers affect our confidence on the accuracy of the estimate?

|  |  |  |  |
| --- | --- | --- | --- |
| *x* |  |  |  |
| 34 | -19.3 | 372.49 | 1156 |
| 36 | -17.3 | 299.29 | 1296 |
| 39 | -14.3 | 204.49 | 1521 |
| 43 | -10.3 | 106.09 | 1849 |
| 51 | -2.3 | 5.29 | 2601 |
| 53 | -0.3 | 0.09 | 2809 |
| 62 | 8.7 | 75.69 | 3844 |
| 63 | 9.7 | 94.09 | 3969 |
| 73 | 19.7 | 388.09 | 5329 |
| 79 | 25.7 | 660.49 | 6241 |
| 533 | 0.0 | 2206.10 | 30615 |

***Solution***

1. 

*Range* = 79 – 34 = 45 ***words***

*Variance*: 



*Standard deviation*: 

1. There seems to be considerable variation from page to page. For small samples with n = 10, there could be considerable variation in the sample mean and, therefore, considerable variation in the projected totals for the entire dictionary. It appears that there would be a question about the accuracy of an estimate based on this sample for the total number of words.

***Exercise***

The National Highway Traffic Administration conducted crash tests of child booster seats for cars. Listed below are results from those teats, with the measurements given in hic (standard head injury condition units.

774 649 1210 546 431 612

1. Find the range, variance, and standard deviation
2. According to the safety requirement, the hic measurement should be less than 1000 hic. Do the results suggest that all of the child booster seats meet the specified requirement?

***Solution***

|  |  |
| --- | --- |
| *x* |  |
| 431 | 185761 |
| 546 | 298116 |
| 612 | 374544 |
| 649 | 421201 |
| 774 | 599076 |
| 1210 | 1464100 |
| 4222 | 3342798 |

1. 

*Range* = 1210 – 431 = 779 ***hic***

*Variance*: 



*Standard deviation*: 

1. Yes, there seems to be much variation – mainly due to the largest value, which appears to be substantially different from the others.

***Exercise***

The insurance Institution for Highway Safety conducted tests with crashes of new cars traveling at 6 mi/h. The total cost of the damages was found for a simple random sample of the tested cars and listed below

$7448 $4911 $9051 $6374 $4277

1. Find the range, variance, and standard deviation
2. Do the different measures of center differ very much?

***Solution***

|  |  |
| --- | --- |
| *x* |  |
| 4277 | 18292729 |
| 4911 | 24117921 |
| 6374 | 40627876 |
| 7448 | 55472704 |
| 9051 | 81920601 |
| 32061 | 220431831 |

1. *Range* = 9051 – 4277 = $4744

*Variance*: 



*Standard deviation*: 

1. A value is considered unusual if it differs from the mean by more than two standard deviations. Since $10,000 differs from the mean by  standard deviations, in this context it would not be considered an unusual value.

***Exercise***

Listed below are the durations (in hours) of a simple random sample of all flights (as of this writing) of NASA’s Space Transport System (space shuttle).

73 95 235 192 165 262 191 376 259 235 381 331 221 244 0

1. Find the range, variance, and standard deviation

|  |  |
| --- | --- |
| *x* |  |
| 0 | 0 |
| 73 | 5329 |
| 95 | 9025 |
| 165 | 27225 |
| 191 | 36481 |
| 192 | 36864 |
| 221 | 48841 |
| 235 | 55225 |
| 235 | 55225 |
| 244 | 59536 |
| 256 | 65536 |
| 262 | 68644 |
| 331 | 109561 |
| 376 | 141376 |
| 381 | 145161 |
| 3260 | 865574 |

1. How might that duration time be explained?

***Solution***

1. *Range* = 381 – 0 = 381 ***hrs***.

*Variance*: 



*Standard deviation*: 



1. A value is considered unusual if it differs from the mean by more than two standard deviations. Since 0 hours differs from the mean by  standard deviations, in this context it would not be considered an unusual value.

***Exercise***

|  |  |
| --- | --- |
| *x* |  |
| 213 | 45369 |
| 213 | 45369 |
| 227 | 51529 |
| 231 | 53361 |
| 239 | 57121 |
| 242 | 58564 |
| 244 | 59536 |
| 246 | 60516 |
| 246 | 60516 |
| 255 | 65025 |
| 257 | 66049 |
| 258 | 66564 |
| 262 | 68644 |
| 280 | 78400 |
| 293 | 85849 |
| 448 | 200704 |
| 4154 | 1123116 |

Listed below are the playing times (in seconds) of songs that were popular at the time of this writing.

448 242 231 246 246 293 280 227 213

262 239 213 258 255 257 244

1. Find the range, variance, and standard deviation
2. Is there on time that is very different from the others?

***Solution***

1. *Range* = 448 – 213 = 235 ***sec***

*Variance*: 



*Standard deviation*: 



1. If the highest playing time is omitted, then

 .

The change is substantial.

***Exercise***

Listed below are numbers of satellites in orbit from different countries.

158 17 15 17 7 3 5 1 8 3 4 2 4 1 2 3 1 1 1 1 1 1 1 1

|  |  |
| --- | --- |
| *x* |  |
| 1 | 1 |
| 1 | 1 |
| 1 | 1 |
| 1 | 1 |
| 1 | 1 |
| 1 | 1 |
| 1 | 1 |
| 1 | 1 |
| 1 | 1 |
| 1 | 1 |
| 2 | 4 |
| 2 | 4 |
| 3 | 9 |
| 3 | 9 |
| 3 | 9 |
| 4 | 16 |
| 4 | 16 |
| 5 | 25 |
| 7 | 49 |
| 8 | 64 |
| 15 | 225 |
| 17 | 289 |
| 18 | 328 |
| 158 | 24964 |
| 259 | 26017 |

1. Find the range, variance, and standard deviation
2. Does on country have an exceptional number of satellites?

***Solution***

1. *Range* = 158 – 1 = 157 ***satellites***

*Variance*: 



*Standard deviation*: 



1. A values is considered unusual if it differs from the mean by more than two standard deviations. Since 0 satellites differs from the mean by  standard deviations, in this context it would not be considered an unusual value.

There are many countries with 0 satellites, and since the original data included no 0’s, it appears that the data was gathered only from countries that had at least one satellite.

***Exercise***

Listed below are costs (in dollars) of roundtrip flights from JFK airport in NY City to San Francisco. (All flights involve one stop and a two-week stay.) The airlines are US Air, Continental, Delta, United, American, Alaska, and Northwest.

|  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- |
| 30 Days in Advance | 244 | 260 | 264 | 264 | 278 | 318 | 280 |
| 1 Day in Advance | 456 | 614 | 567 | 943 | 628 | 1088 | 536 |

Find the coefficient of variation for each of the two sets of data, then compare the variation.

***Solution***

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| *x* |  |  | *x* |  |
| 244 | 59536 |  | 456 | 207936 |
| 260 | 67600 |  | 536 | 287296 |
| 264 | 69696 |  | 567 | 321489 |
| 264 | 69696 |  | 614 | 376996 |
| 278 | 77284 |  | 628 | 394384 |
| 280 | 78400 |  | 943 | 889249 |
| 318 | 101124 |  | 1088 | 1183744 |
| 1908 | 523336 |  | 4832 | 3661094 |

*For* 30 days:







Coefficient of variation: 

*For* 1 day:







Coefficient of variation: 

There is considerably more variation among the costs for tickets purchased one day in advance.

***Exercise***

The trend of thinner Miss America winners has generated charges that the contest encourages unhealthy diet habits among young women. Listed below are body mass indexes (BMI) for Miss America winners from two different periods.

|  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| BMI (1920 – 1930) | 20.4 | 21.9 | 22.1 | 22.3 | 20.3 | 18.8 | 18.9 | 19.4 | 18.4 | 19.1 |
| BMI – (*from recent winners*) | 19.5 | 20.3 | 19.6 | 20.2 | 17.8 | 17.9 | 19.1 | 18.8 | 17.6 | 16.8 |

Find the coefficient of variation for each of the two sets of data, then compare the variation.

***Solution***

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| *x* |  |  | *x* |  |
| 18.4 | 338.56 |  | 16.8 | 282.24 |
| 18.8 | 353.44 |  | 17.6 | 309.76 |
| 18.9 | 357.21 |  | 17.8 | 316.84 |
| 19.1 | 364.81 |  | 17.9 | 320.41 |
| 19.4 | 376.36 |  | 18.8 | 353.44 |
| 20.3 | 412.09 |  | 19.1 | 364.81 |
| 20.4 | 416.16 |  | 19.5 | 380.25 |
| 21.9 | 479.61 |  | 19.6 | 384.16 |
| 22.1 | 488.41 |  | 20.2 | 408.04 |
| 22.3 | 497.29 |  | 20.3 | 412.09 |
| 201.6 | 4083.94 |  | 187.6 | 3532.04 |

*For* BMI (1920 – 1930):







Coefficient of variation: 

*For* BMI – (from recent winners):







Coefficient of variation: 

The BMI values for the two time period appear to exhibit about the same amount of variation.

***Exercise***

Find the Standard Deviation from the frequency distribution and find the standard deviation of sample summarized in a frequency distribution table by using the formula, where *x* represents the class midpoint, *f* represents the class frequency, and *n* represents the total number of sample values.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| |  |  | | --- | --- | | ***Tar* (*mg*) *in Nonfiltered Cigarettes*** | ***Frequency*** | | 10 – 13 | 1 | | 14 – 17 | 0 | | 18 – 21 | 15 | | 22 – 25 | 7 | | 26 – 29 | 2 | | |  |  | | --- | --- | | ***Pulse Rates of Females*** | ***Frequency*** | | 60 – 69 | 12 | | 70 – 79 | 14 | | 80 – 89 | 11 | | 90 – 99 | 1 | | 100 – 109 | 1 | | 110 – 119 | 0 | | 120 – 129 | 1 | |

***Solution***

1. The *x* values are the class midpoints from the given frequency table.

|  |  |  |  |
| --- | --- | --- | --- |
| ***x*** | ***f*** |  |  |
| 11.5 | 1 | 11.5 | 132.25 |
| 15.5 | 0 | 0 | 0 |
| 19.5 | 15 | 292.5 | 5703.75 |
| 23.5 | 7 | 164.5 | 3867.75 |
| 27.5 | 2 | 55.0 | 1512.50 |
|  | 25 | 523.5 | 11214.25 |





This is the same as the true value of 3.2 mg.

1. The *x* values are the class midpoints from the given frequency table.

|  |  |  |  |
| --- | --- | --- | --- |
| ***x*** | ***f*** |  |  |
| 64.5 | 12 | 774.0 | 49923.00 |
| 74.5 | 14 | 1043.0 | 77703.5 |
| 84.5 | 11 | 929.5 | 78542.75 |
| 94.5 | 1 | 94.5 | 8930.25 |
| 104.5 | 1 | 104.5 | 10920.25 |
| 114.5 | 0 | 0 | 0 |
| 124.5 | 1 | 124.5 | 15500.25 |
|  | 40 | 3070.0 | 241520.00 |





This is close to the true value of 12.5 beats/min.

***Exercise***

Heights of women have a bell-shaped distribution with a mean of 161 cm and a standard deviation of 7 cm. Using the empirical rule, what is the approximate percentage of women between

1. 154 cm and 168 cm?
2. 147 cm and 175 cm?

***Solution***

1. The range from 154 to 168 is  . The empirical rule suggests that about 68% of the data values should fall within those limits.
2. The range from 147 to 175 is  . The empirical rule suggests that about 95% of the data values should fall within those limits.

***Exercise***

The author’s Generac generator produces voltage amounts with a mean of 125.0 volts and standard deviation of 0.3 volts, and the voltages have a bell-shaped distribution. Using the empirical rule, what is the approximate percentage of voltage amounts between

1. 124.4 volts and 125.6 volts?
2. 124.1 volts and 125.9 volts?

***Solution***

1. The range from 124.4 to 125.6 is  . The empirical rule suggests that about 95% of the data values should fall within those limits.
2. The range from 124.1 to 125.9 is  . The empirical rule suggests that about 99.7% of the data values should fall within those limits.

***Exercise***

The mean value of land and buildings per acre from a sample of farms is $1,500, with a standard deviation of $200. Using the empirical rule, estimate the percent of farms whose land and building values per acre are between $1,300 and $1,700. (Assume the data set has a bell-shaped distribution.)

***Solution***





68% of the farms have values between $1,300 and $1,700 per acre

***Exercise***

The mean value of land and buildings per acre from a sample of farms is $2,400, with a standard deviation of $450. Using the empirical rule, between what two values do about 95% of the data lie? (Assume the data set has a bell-shaped distribution.)

***Solution***





95% of the farms have values between $1,500 and $3,300 per acre

***Exercise***

Heights of women have a bell-shaped distribution with a mean of 161 cm and a standard deviation of 7 cm. Using Chebyshev’s Theorem, what do we know about the percentage of women with heights that are within 2 standard deviations of the mean? What are the minimum and maximum heights that are within 2 standard deviations of the mean?

***Solution***

Chebyshev’s Theorem states that for any set of data there must be at least  (75%) of the data values within 2 standard deviations of the mean. In this context, the limits are : there must be at least 75% of the heights between 147 cm and 175 cm.

***Exercise***

The author’s Generac generator produces voltage amounts with a mean of 125.0 volts and standard deviation of 0.3 volts. Using Chebyshev’s theorem, what do we know about the percentage of voltage amounts that are within 3 standard deviations of the mean? What are the minimum and maximum voltage amounts that are within 3 standard deviations of the mean?

***Solution***

Chebyshev’s Theorem states that for any set of data there must be at least



(89%) of the data values within 3 standard deviations of the mean.

In this context, the limits are : there must be at least 75% of the heights between 124.1 volts and 125.9 volts.

***Exercise***

The mean time in a women’s 400-meter dash is 57.07 seconds, with a standard deviation of 1.05 seconds. Apply Chebyshev’s Theorem to the data using . Interpret the results.

***Solution***



At least 75% of the 400-meter dash within 2 standard deviations of the mean

The limits are 

There must be at least 75% of the 400-meter dash between 54.97 and 59.17 seconds.

***Exercise***

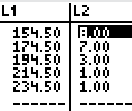
The number of gallons of water consumed per day by a small village are listed. Make a frequency distribution (using five classes) for the data set. Then approximate the population mean and the population standard deviation of the data set.

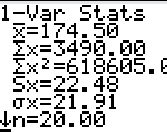
167 180 192 173 145 151 174 175 178 160

195 224 244 146 162 146 177 163 149 188

***Solution***



|  |  |  |  |
| --- | --- | --- | --- |
| ***Class*** | ***x*** | ***f*** |  |
| 145 – 164 | 154.5 | 8 | 1236.0 |
| 165 – 184 | 174.5 | 7 | 1221.5 |
| 185 – 204 | 194.5 | 3 | 583.5 |
| 205 – 224 | 214.5 | 1 | 214.5 |
| 225 – 244 | 234.5 | 1 | 234.5 |
|  |  | 20 | 3490.0 |



|  |  |  |  |
| --- | --- | --- | --- |
|  |  | ***f*** |  |
| −20 | 400 | 8 | 3200 |
| 0 | 0 | 7 | 0 |
| 20 | 400 | 3 | 1200 |
| 40 | 1600 | 1 | 1600 |
| 60 | 3600 | 1 | 3600 |
|  |  |  | 9600 |



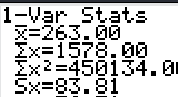




***Exercise***

To get the best deal on a microwave oven, Jeremy called six appliance stores and asked the cost of a specific model. The prices he was quoted are listed below:

$325 $384 $156 $210 $219 $284

Find the variance for the given data.

***Solution***





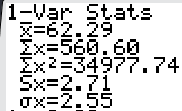
***Exercise***

Compare the variation in heights to the variation in weights of thirteen-year old girls. The heights (in inches) and weights (in pounds) of nine randomly selected thirteen-year old girls as listed below

Heights (inches): 59.3 61.2 62.6 64.7 60.1 58.3 64.6 63.7 66.1

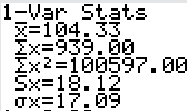
Weights (pounds): 87 96 91 119 96 90 123 98 139

Find the coefficient of variation for each of the two sets of data, then compare the variation

***Solution***

Heights: 

Coefficient of variation: 

Weights: 

Coefficient of variation: 

There is substantially more variation in the weights than in the heights of the girls

***Exercise***

The amount of Jen’s monthly phone bill is normally distributed with a mean of $56 and a standard deviation of $9. What percentage of her phone bills are between $29 and $83? Use the empirical rule to solve.

***Solution***





29 and 83 are each exactly 3 standard deviation away from the mean 56.

The empirical rule tells us that about 99.7% of all values are within 3 standard deviation of the mean, so about 99.7% of her phone bills are between 70 and 130.

***Solution Section* 1.9 − Measures of Relative Standing and Boxplots**

***Exercise***

When Reese Witherspoon won an Oscar as Best Actress for the movie *Walk the Line*, her age was converted to a *z*-score of −0.61 when included among the ages of all other Oscar-winning Best Actress at the time of this writing. Was her age above the mean or below the mean? How many standard deviations away from the mean is her age?

***Solution***

For a *z* score of −0.61, the negative sign indicates that her age is below the mean and the numerical portion indicates that her age is 0.61 standard deviations away from the mean.

***Exercise***

Hoffman was 38 years of age when he won a Best Actor Oscar for his role in Capote. The Oscar-winning Best Actors have a mean age of 43.8 years and a standard deviation of 8.9 years.

1. What is the difference between Hoffman’s age and the mean age?
2. How many standard deviations is that (the difference found in part (a))?
3. Convert Hoffman’s age to a *z*-score.
4. If we consider “usual” ages to be those that convert to *z*-scores between −2 and 2, is Hoffman’s age usual or unusual?

***Solution***

1. 





1. 
2. 



1. Since , Hoffman’s age is not considered unusual in this context.

***Exercise***

Eruptions of the Old Faithful geyser have duration times with a mean of 245.0 sec and a standard deviation of 36.4 sec. One eruption had a duration time of 110 sec.

1. What is the difference between a duration time of 110 sec and the mea?
2. How many standard deviations is that (the difference found in part (a))?
3. Convert duration time of 110 sec to a *z*-score.
4. If we consider “usual” ages to be those that convert to *z*-scores between −2 and 2, is a duration time of 110 sec usual or unusual?

***Solution***

1. 
2. 
3.  
4. Since , a duration time of 110 seconds is considered unusual in this context.

***Exercise***

Human body temperatures have a mean of 98.20°F and a standard deviation of 0.62°F. Convert each given temperature to a *z*-score and determine whether it is usual and unusual.

*a*) 101.00°F *b*) 96.90°F *c*) 96.98°F

***Solution***

1. ; since  it is unusual. 
2. ; since  it is unusual.
3. ; since  it is usual.

***Exercise***

Scores on SAT test have a mean of 1518 and a standard deviation of 325. Scores on the ACT test have a mean of 21.1 and standard deviation of 4.8. Which is relatively better: a score of 1840 on the SAT test or a score of 26.0 on the ACT test? Why?

***Solution***

SAT:  

ACT:  

Since 1.02 > 0.99, the ACT score of 26.0 is the relatively better score.

***Exercise***

Scores on SAT test have a mean of 1518 and a standard deviation of 325. Scores on the ACT test have a mean of 21.1 and standard deviation of 4.8. Which is relatively better: a score of 1190 on the SAT test or a score of 16.0 on the ACT test? Why?

***Solution***

SAT:  

ACT:  

Since −1.01 > −1.06, the SAT score of 119 is the relatively better score.

***Exercise***

Use the given sorted values, which are the numbers of points scored in the Super Bowl for a recent period of 24 years. Find the percentile corresponding to the given number of points

36 37 37 39 39 41 43 44 44 47 50 53 54 55 56 56 57 59 61 61 65 69 69 75

*a*) 47 *b*) 65 *c*) 54 *d*) 41

***Solution***

Let *b* to the number of scores below *x*; *n* is the total number of scores.

The percentile score of *x* is 

1. The percentile score of 47 is  
2. The percentile score of 65 is 
3. The percentile score of 54 is 
4. The percentile score of 41 is 

***Exercise***

For the given data, find the indicated percentile or quartile

36 37 37 39 39 41 43 44 44 47 50 53 54 55 56 56 57 59 61 61 65 69 69 75

1. 
2. 
3. 
4. 
5. 
6. 
7. 
8. 

***Solution***



1. . Since the 5th score is 39, then 
2. . Since the 20th score is 61, then 
3.  (it is a whole number).

The mean of the 12th and 13th score, then 

1.  (it is a whole number).

The mean of the 18th and 19th score, then 

1.  (it is a whole number).

The mean of the 6th and 7th score, then 

1. . Since the 23th score is 69, then 
2. , (it is a whole number).

The mean of the 6th and 7th score, then 

1. ,  (it is a whole number).

The mean of the 18th and 19th score, then 

***Exercise***

The number of hours of television watched per day by a sample of 28 people

2 4 1 5 7 2 5 4 4 2 3 6 4 3 5 2 0 3 5 9 4 5 2 1 3 6 7 2

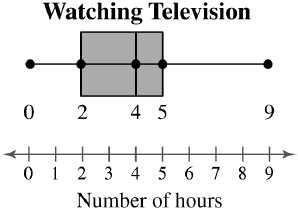
1. Find the data set’s first, second, and third quartiles.
2. Draw a box-and-whisker plot that represents the data set.
3. About 75% of the people watched no more than now many hours of television per day?
4. What percent of the people watched more than 4 hours of television per day?
5. If you randomly selected one person from the sample, what is the likelihood that the person watched less than 2 hours of television per day? Write your answer as a percent.

***Solution***



0 1 1 2 2 2 **2** 2 2 3 3 3 3 **4** 4 4 4 4 5 5 5 **5** 5 6 6 7 7 9

1. 



1. 
2. The percentage of the people watched more than 4 hours of television per day is 50%
3. Less than 2 hours of television per day is 25%

***Exercise***

The hourly earnings (in dollars) of a sample of 25 railroad equipment manufacturers

15.6 18.75 14.6 15.8 14.35 13.9 17.5 17.55 13.0 14.2 19.05 15.35 15.2

19.45 15.95 16.5 16.3 15.25 15.05 19.1 15.2 16.22 17.75 18.4 15.25

1. Find the data set’s first, second, and third quartiles.
2. Draw a box-and-whisker plot that represents the data set.
3. About 75% of the manufacturers made less than $15.80 per hour?
4. What percent of the manufacturers made more than $15.80 per hour?
5. If you randomly selected one manufacturer from the sample, what is the likelihood that the manufacturer made less than $15.80 per hour? Write your answer as a percent.

***Solution***

13.0 13.9 14.2 14.35 14.6 **15.05 15.2** 15.2 15.25 15.25 15.35 15.6 **15.8**

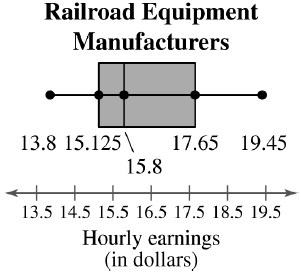
15.95 16.22 16.3 16.5 17.5 **17.55 17.75** 18.4 18.75 19.05 19.1 19.45

1. , , then 

, , then 

, , then 

1. Railroad equipment manufacturers



1. 
2. The percentage of the manufacturers made more than $15.80 per hour is 50%
3. The manufacturer made less than $15.80 per hour is 50%

***Exercise***

A certain brand of automobile tire has a mean life span of 35,000 miles, with a standard deviation of 2250 miles. (Assume the life spans of the tires have a bell-shaped distribution)

1. The life spans of three randomly selected tires are 34,000 miles, 37,000 miles, and 30,000 miles. Find the *z*-score that corresponds to each life span. According to the *z*-scores, would the life spans of any of these tires be considered unusual?
2. The life spans of three randomly selected tires are 30,500 miles, 37,250 miles, and 35,000 miles. Using the Empirical Rule, find the percentile that corresponds to each life span.

***Solution***

1. 



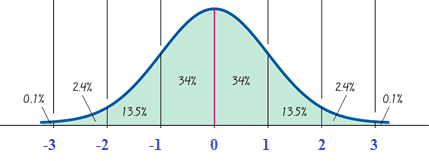


The tire with a life span of 30,000 miles has an unusual short life span.

1.  ⇒ 2.5th percentile

 ⇒ 84th percentile

 ⇒ 50th percentile

******

***Exercise***

The life spans of species of fruit fly have a bell shaped distribution, with mean of 33 days and a standard deviation of 4 days.

1. The life spans of three randomly selected fruit flies are 34 days, 30 days, and 42 days. Find the *z*-score that corresponds to each life span and determine if any of these life spans are unusual.
2. The life spans of three randomly selected fruit flies are 29 days, 41 days, and 25 days. Using the Empirical Rule, find the percentile that corresponds to each life span.

***Solution***

1. 



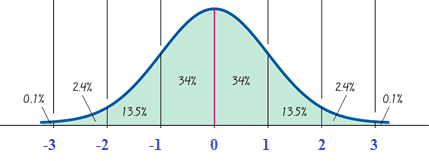


The fruit fly with a life span of 42 days has an unusual short life span.

1.  ⇒ 16th percentile

 ⇒ 97.5th percentile

 ⇒ 2.5th percentile

******

***Exercise***

Find the and  for the given data: 49 52 52 52 74 67 55 55

***Solution***







***Exercise***

Find the and  for the given weights (in pounds) of 30 newborn babies listed below:

5.5 5.7 5.8 6.0 6.1 6.1 6.3 6.4 6.5 6.6

6.7 6.7 6.7 6.9 7.0 7.0 7.0 7.1 7.2 7.2

7.4 7.5 7.7 7.7 7.8 8.0 8.1 8.1 8.3 8.7

***Solution***





***Exercise***

Find the percentile for the data value:

113 125 117 111 119 121 111 109 116 113 117 127 109 113 115 110

Data value: 119

***Solution***

Since there is 12 number less than 119



***Exercise***

The test scores of 40 students are listed below:

30 35 43 44 47 48 54 55 56 57 59 62 63 65 66 68 69 69 71 72

72 73 74 76 77 77 78 79 80 81 81 82 83 85 89 92 93 94 97 98

Find 

***Solution***



