

Machine Learning

CS 539

Worcester Polytechnic Institute

Department of Computer Science

Instructor: Prof. Kyumin Lee

Upcoming Schedule

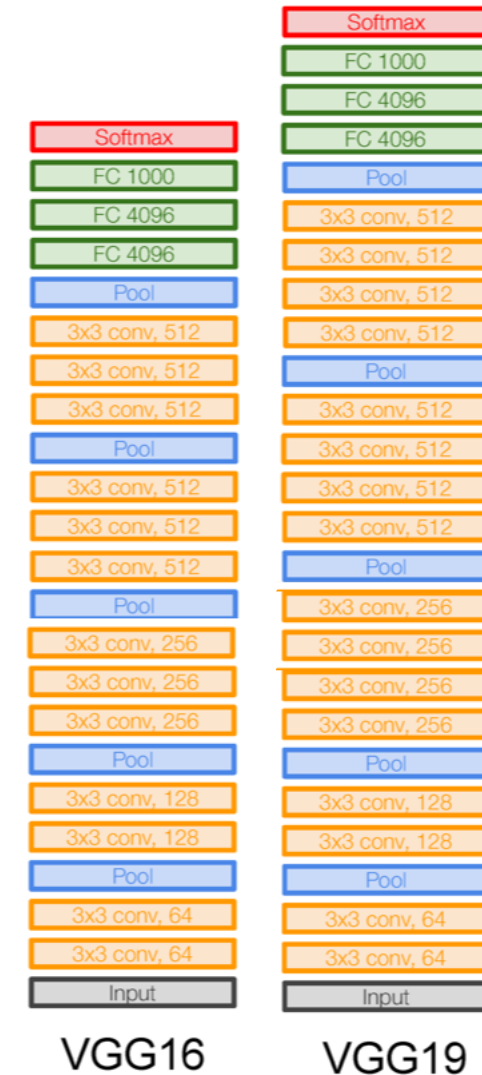
- Project Proposal
 - <https://canvas.wpi.edu/courses/58900/assignments/355606>
 - Due date is June 25
- HW 3
 - <https://canvas.wpi.edu/courses/58900/assignments/356655>
 - Due date is July 2

VGGNet

Small filters, Deeper networks

16 - 19 layers (VGG16Net)

Only 3x3 CONV stride 1, pad 1
and 2x2 MAX POOL stride 2



VGGNet

INPUT: [224x224x3] memory: $224 \times 224 \times 3 = 150\text{K}$ params: 0 (not counting biases)

CONV3-64: [224x224x64] memory: $224 \times 224 \times 64 = 3.2\text{M}$ params: $(3 \times 3 \times 3) \times 64 = 1,728$

CONV3-64: [224x224x64] memory: $224 \times 224 \times 64 = 3.2\text{M}$ params: $(3 \times 3 \times 64) \times 64 = 36,864$

POOL2: [112x112x64] memory: $112 \times 112 \times 64 = 800\text{K}$ params: 0

CONV3-128: [112x112x128] memory: $112 \times 112 \times 128 = 1.6\text{M}$ params: $(3 \times 3 \times 64) \times 128 = 73,728$

CONV3-128: [112x112x128] memory: $112 \times 112 \times 128 = 1.6\text{M}$ params: $(3 \times 3 \times 128) \times 128 = 147,456$

POOL2: [56x56x128] memory: $56 \times 56 \times 128 = 400\text{K}$ params: 0

CONV3-256: [56x56x256] memory: $56 \times 56 \times 256 = 800\text{K}$ params: $(3 \times 3 \times 128) \times 256 = 294,912$

CONV3-256: [56x56x256] memory: $56 \times 56 \times 256 = 800\text{K}$ params: $(3 \times 3 \times 256) \times 256 = 589,824$

CONV3-256: [56x56x256] memory: $56 \times 56 \times 256 = 800\text{K}$ params: $(3 \times 3 \times 256) \times 256 = 589,824$

POOL2: [28x28x256] memory: $28 \times 28 \times 256 = 200\text{K}$ params: 0

CONV3-512: [28x28x512] memory: $28 \times 28 \times 512 = 400\text{K}$ params: $(3 \times 3 \times 256) \times 512 = 1,179,648$

CONV3-512: [28x28x512] memory: $28 \times 28 \times 512 = 400\text{K}$ params: $(3 \times 3 \times 512) \times 512 = 2,359,296$

CONV3-512: [28x28x512] memory: $28 \times 28 \times 512 = 400\text{K}$ params: $(3 \times 3 \times 512) \times 512 = 2,359,296$

POOL2: [14x14x512] memory: $14 \times 14 \times 512 = 100\text{K}$ params: 0

CONV3-512: [14x14x512] memory: $14 \times 14 \times 512 = 100\text{K}$ params: $(3 \times 3 \times 512) \times 512 = 2,359,296$

CONV3-512: [14x14x512] memory: $14 \times 14 \times 512 = 100\text{K}$ params: $(3 \times 3 \times 512) \times 512 = 2,359,296$

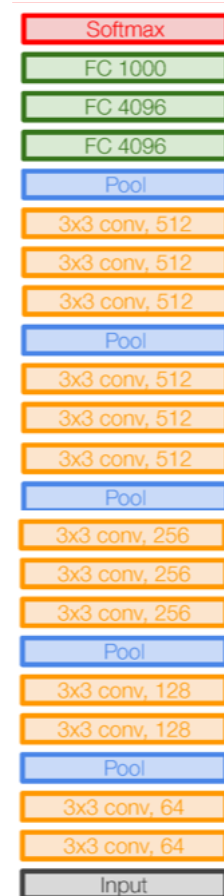
CONV3-512: [14x14x512] memory: $14 \times 14 \times 512 = 100\text{K}$ params: $(3 \times 3 \times 512) \times 512 = 2,359,296$

POOL2: [7x7x512] memory: $7 \times 7 \times 512 = 25\text{K}$ params: 0

FC: [1x1x4096] memory: 4096 params: $7 \times 7 \times 512 \times 4096 = 102,760,448$

FC: [1x1x4096] memory: 4096 params: $4096 \times 4096 = 16,777,216$

FC: [1x1x1000] memory: 1000 params: $4096 \times 1000 = 4,096,000$



VGG16

VGGNet

INPUT: [224x224x3] memory: $224*224*3=150K$ params: 0 (not counting biases)

CONV3-64: [224x224x64] memory: $224*224*64=3.2M$ params: $(3*3*3)*64 = 1,728$

CONV3-64: [224x224x64] memory: $224*224*64=3.2M$ params: $(3*3*64)*64 = 36,864$

POOL2: [112x112x64] memory: $112*112*64=800K$ params: 0

CONV3-128: [112x112x128] memory: $112*112*128=1.6M$ params: $(3*3*64)*128 = 73,728$

CONV3-128: [112x112x128] memory: $112*112*128=1.6M$ params: $(3*3*128)*128 = 147,456$

POOL2: [56x56x128] memory: $56*56*128=400K$ params: 0

CONV3-256: [56x56x256] memory: $56*56*256=800K$ params: $(3*3*128)*256 = 294,912$

CONV3-256: [56x56x256] memory: $56*56*256=800K$ params: $(3*3*256)*256 = 589,824$

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POOL2: [28x28x256] memory: $28*28*256=200K$ params: 0

CONV3-512: [28x28x512] memory: $28*28*512=400K$ params: $(3*3*256)*512 = 1,179,648$

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POOL2: [7x7x512] memory: $7*7*512=25K$ params: 0

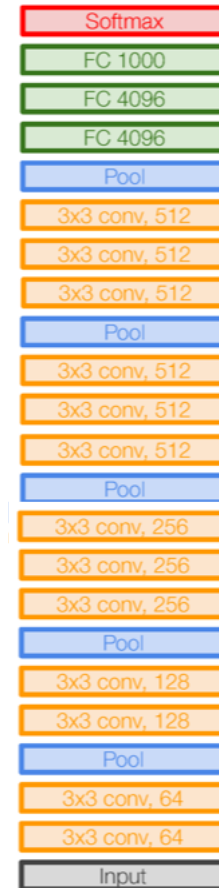
FC: [1x1x4096] memory: 4096 params: $7*7*512*4096 = 102,760,448$

FC: [1x1x4096] memory: 4096 params: $4096*4096 = 16,777,216$

FC: [1x1x1000] memory: 1000 params: $4096*1000 = 4,096,000$

TOTAL memory: $24M * 4 \text{ bytes} \approx 96MB$ / image (for a forward pass)

TOTAL params: 138M parameters



VGG16

VGGNet

INPUT: [224x224x3] memory: $224*224*3=150K$ params: 0 (not counting biases)

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CONV3-64: [224x224x64] memory: $224*224*64=3.2M$ params: $(3*3*64)*64 = 36,864$

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CONV3-128: [112x112x128] memory: $112*112*128=1.6M$ params: $(3*3*128)*128 = 147,456$

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FC: [1x1x4096] memory: 4096 params: $7*7*512*4096 = 102,760,448$

FC: [1x1x4096] memory: 4096 params: $4096*4096 = 16,777,216$

FC: [1x1x1000] memory: 1000 params: $4096*1000 = 4,096,000$

Note:

Most memory is in early CONV

Most params are in late FC

TOTAL memory: $24M * 4 \text{ bytes} \sim 96MB$ / image (only forward! ~ 2 for bwd)

TOTAL params: 138M parameters

VGGNet

INPUT: [224x224x3] memory: $224*224*3=150K$ params: 0 (not counting biases)

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FC: [1x1x4096] memory: 4096 params: $4096*4096 = 16,777,216$

FC: [1x1x1000] memory: 1000 params: $4096*1000 = 4,096,000$

TOTAL memory: 24M * 4 bytes ~= 96MB / image (only forward! ~*2 for bwd)

TOTAL params: 138M parameters

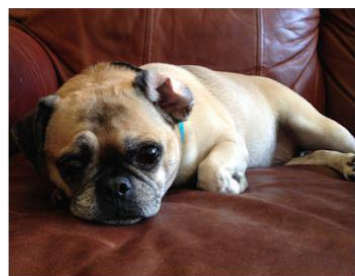


VGG16

Common names

[Zeiler and Fergus 2013]

Visualization of VGG-16 by Lane McIntosh. VGG-16 architecture from [Simonyan and Zisserman 2014].

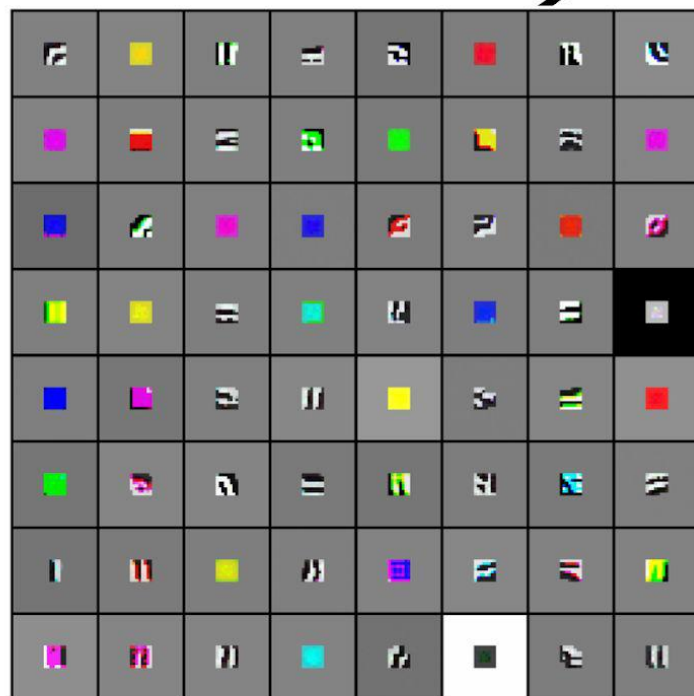


Low-level features

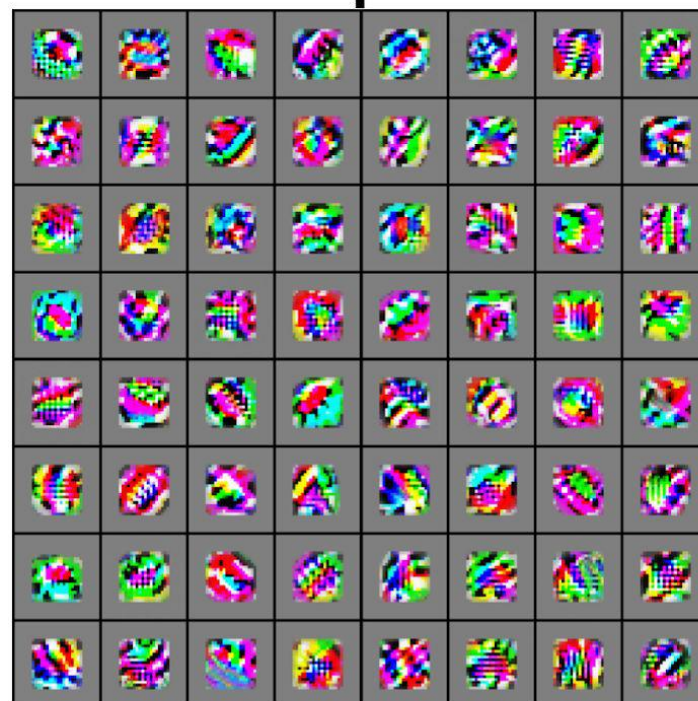
Mid-level features

High-level features

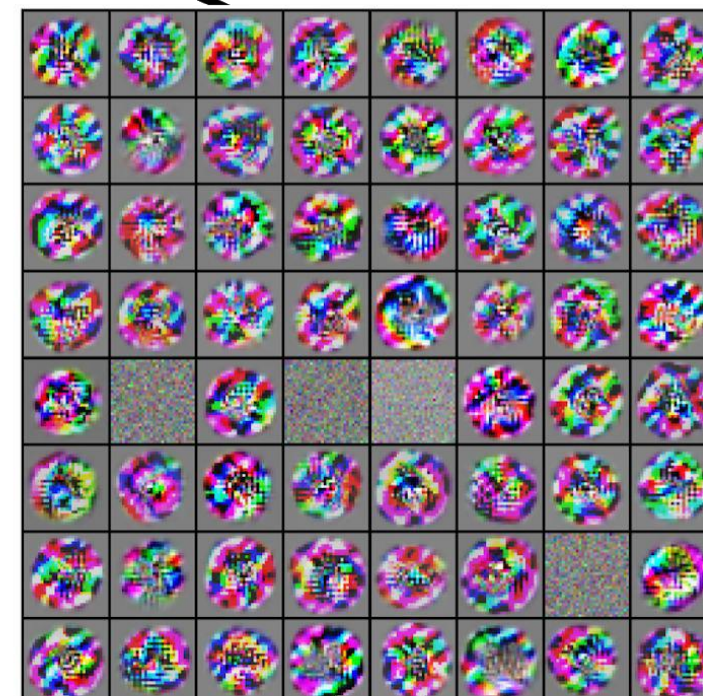
Linearly separable classifier



VGG-16 Conv1_1



VGG-16 Conv3_2

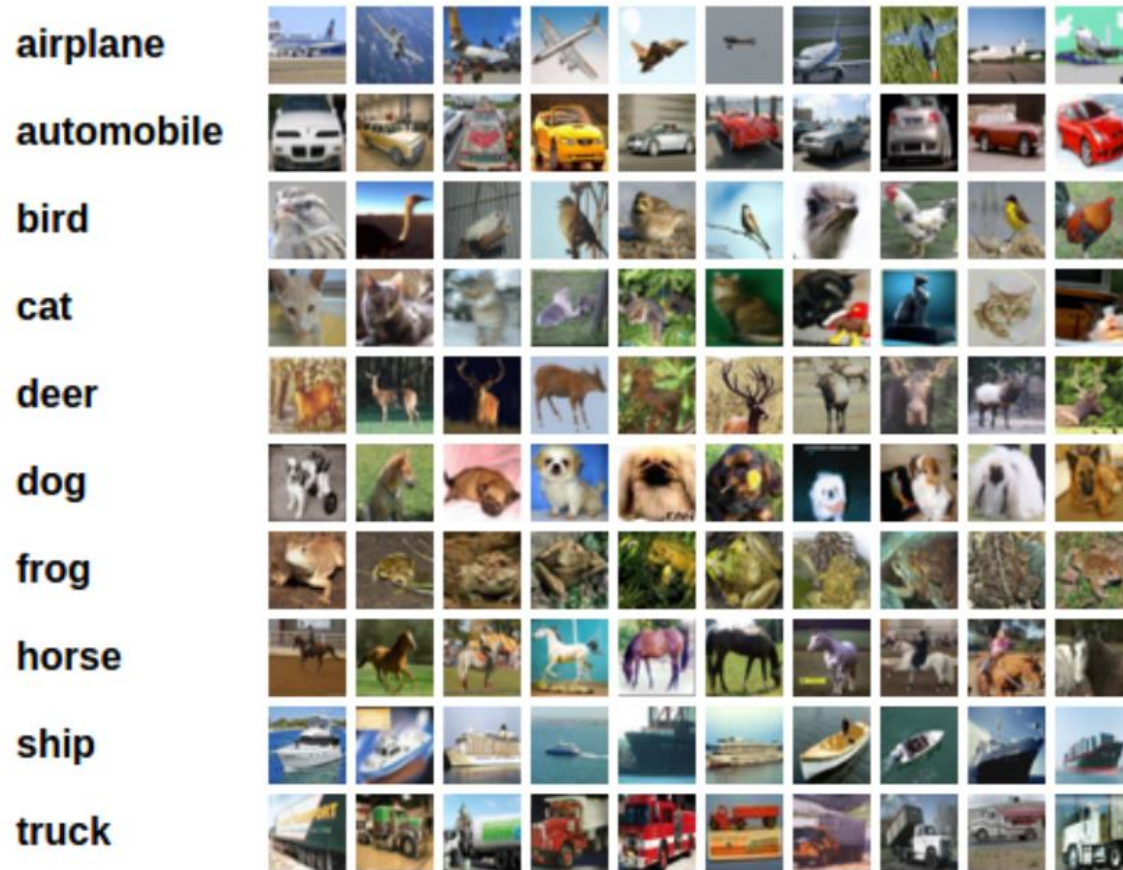


VGG-16 Conv5_3

Pytorch Basics and Example

Implementation of CNN in PyTorch

For this tutorial, we will use the CIFAR10 dataset. It has the classes: 'airplane', 'automobile', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse', 'ship', 'truck'. The images in CIFAR-10 are of size 3x32x32, i.e. 3-channel color images of 32x32 pixels in size.



cifar10

https://pytorch.org/tutorials/beginner/blitz/cifar10_tutorial.html

Implementation of CNN in PyTorch

```
class Net(nn.Module):
    def __init__(self):
        super().__init__()
        self.conv1 = nn.Conv2d(3, 6, 5)
        self.pool = nn.MaxPool2d(2, 2)
        self.conv2 = nn.Conv2d(6, 16, 5)
        self.fc1 = nn.Linear(16 * 5 * 5, 120)
        self.fc2 = nn.Linear(120, 84)
        self.fc3 = nn.Linear(84, 10)

    def forward(self, x):
        x = self.pool(F.relu(self.conv1(x)))
        x = self.pool(F.relu(self.conv2(x)))
        x = torch.flatten(x, 1) # flatten all dimensions except batch
        x = F.relu(self.fc1(x))
        x = F.relu(self.fc2(x))
        x = self.fc3(x)
        return x

net = Net()
print(net)
```

```
Net(
  (conv1): Conv2d(3, 6, kernel_size=(5, 5), stride=(1, 1))
  (pool): MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1, ceil_mode=False)
  (conv2): Conv2d(6, 16, kernel_size=(5, 5), stride=(1, 1))
  (fc1): Linear(in_features=400, out_features=120, bias=True)
  (fc2): Linear(in_features=120, out_features=84, bias=True)
  (fc3): Linear(in_features=84, out_features=10, bias=True)
)
```

https://pytorch.org/tutorials/beginner/blitz/cifar10_tutorial.html

Implementation of CNN in PyTorch

```
class Net(nn.Module):
    def __init__(self):
        super().__init__()
        self.conv1 = nn.Conv2d(3, 6, 5)
        self.pool = nn.MaxPool2d(2, 2)
        self.conv2 = nn.Conv2d(6, 16, 5)
        self.fc1 = nn.Linear(16 * 5 * 5, 120)
        self.fc2 = nn.Linear(120, 84)
        self.fc3 = nn.Linear(84, 10)

    def forward(self, x):
        x = self.pool(F.relu(self.conv1(x)))
        x = self.pool(F.relu(self.conv2(x)))
        x = torch.flatten(x, 1) # flatten all dimensions except batch
        x = F.relu(self.fc1(x))
        x = F.relu(self.fc2(x))
        x = self.fc3(x)
        return x

net = Net()
print(net)
```

Increase # of filters in deeper layers:

As we move forward in the layers, the patterns get more complex; **hence there are larger combinations of patterns to capture.**

```
Net(
  (conv1): Conv2d(3, 6, kernel_size=(5, 5), stride=(1, 1))
  (pool): MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1, ceil_mode=False)
  (conv2): Conv2d(6, 16, kernel_size=(5, 5), stride=(1, 1))
  (fc1): Linear(in_features=400, out_features=120, bias=True)
  (fc2): Linear(in_features=120, out_features=84, bias=True)
  (fc3): Linear(in_features=84, out_features=10, bias=True)
)
```

https://pytorch.org/tutorials/beginner/blitz/cifar10_tutorial.html

Implementation of CNN in Keras

```
from keras import layers
from keras import models

model = models.Sequential()
model.add(layers.Conv2D(32, (3, 3), activation='relu',
                        input_shape=(150, 150, 3)))
model.add(layers.MaxPooling2D((2, 2)))
model.add(layers.Conv2D(64, (3, 3), activation='relu'))
model.add(layers.MaxPooling2D((2, 2)))
model.add(layers.Conv2D(128, (3, 3), activation='relu'))
model.add(layers.MaxPooling2D((2, 2)))
model.add(layers.Conv2D(128, (3, 3), activation='relu'))
model.add(layers.MaxPooling2D((2, 2)))
model.add(layers.Flatten())
model.add(layers.Dense(512, activation='relu'))
model.add(layers.Dense(1, activation='sigmoid'))
```


Number of Parameters

```
from keras import layers
from keras import models

model = models.Sequential()
model.add(layers.Conv2D(32, (3, 3), activation='relu',
                        input_shape=(150, 150, 3)))
model.add(layers.MaxPooling2D((2, 2)))
model.add(layers.Conv2D(64, (3, 3), activation='relu'))
model.add(layers.MaxPooling2D((2, 2)))
model.add(layers.Conv2D(128, (3, 3), activation='relu'))
model.add(layers.MaxPooling2D((2, 2)))
model.add(layers.Conv2D(128, (3, 3), activation='relu'))
model.add(layers.MaxPooling2D((2, 2)))
model.add(layers.Flatten())
model.add(layers.Dense(512, activation='relu'))
model.add(layers.Dense(1, activation='sigmoid'))
```

Layer (type)	Output Shape	Param #
=====		
conv2d_1 (Conv2D)	(None, 148, 148, 32)	896
<hr/>		
max_pooling2d_1 (MaxPooling2D)	(None, 74, 74, 32)	0
<hr/>		
conv2d_2 (Conv2D)	(None, 72, 72, 64)	18496
<hr/>		
max_pooling2d_2 (MaxPooling2D)	(None, 36, 36, 64)	0
<hr/>		
conv2d_3 (Conv2D)	(None, 34, 34, 128)	73856
<hr/>		
max_pooling2d_3 (MaxPooling2D)	(None, 17, 17, 128)	0
<hr/>		
conv2d_4 (Conv2D)	(None, 15, 15, 128)	147584
<hr/>		
max_pooling2d_4 (MaxPooling2D)	(None, 7, 7, 128)	0
<hr/>		
flatten_1 (Flatten)	(None, 6272)	0
<hr/>		
dense_1 (Dense)	(None, 512)	3211776
<hr/>		
dense_2 (Dense)	(None, 1)	513
<hr/>		
=====		
Total params: 3,453,121		
Trainable params: 3,453,121		
Non-trainable params: 0		
<hr/>		

Number of parameters in a CONV layer would be : $((m * n * d)+1)* k$
m = shape of filter width
n = shape of filter height
d = number of filters/channels in the previous layer
1 = bias term
k = number of filters

CNN

- Video:
 - <https://www.youtube.com/watch?v=3JQ3hYko51Y&feature=youtu.be>
- Interactive visualization:
 - https://adamharley.com/nn_vis/cnn/3d.html