

Practice Problems Set #1 - Definitions

- (1) Define Simple Harmonic Motion
- (2) Explain The relationship between Kinetic Energy and Potential Energy in a SHM system.
- (3) What is periodic motion?
- (4) What is the difference between frequency and angular frequency?
- (5) Describe at least 3 situations where an object would experience SHM.
- (6) Why does a pendulum only reflect SHM at small angles?
- (7) What experimental factors could contribute to a spring experiment not reflecting perfect SHM?

Practice Problems Set #2 - Understanding SHM

1. Given the equation $y=A(\sin(\omega t))$, derive velocity and acceleration showing all of your work. Does it show SHM? Why or why not? If we imagine that this formula is depicting the displacement of a spring system, what does this mean physically?
2. Consider the equation $x = Ae^{\omega x}$. Does this show SHM? Why or why not?
3. Why do we use $x=A(\cos(\omega t))$ instead of $x=A(\sin(\omega t))$ to show position of a spring system in time?
4. What happens to the Period of a spring system if we:
 - i. Increase the mass
 - ii. Decrease the mass
 - iii. Increase the spring constant
 - iv. Decrease the spring Constant
 - v. Increase the frequency
5. What happens to the Period of a pendulum system reflecting SHM if we:
 - i. Increase the mass
 - ii. Decrease the mass
 - iii. Increase length of the pendulum
 - iv. Decrease length of the pendulum
 - v. Increase gravity
 - vi. Decrease gravity
 - vii. Decrease the frequency

Practice Problems Set #3

For the following problems, find:

- i. Angular Frequency
- ii. Frequency
- iii. Position at the given time.
- iv. Velocity at that same time
- v. Acceleration at that same time
- vi. Maximum Velocity
- vii. Period

(:1:) A mass of 6.75kg is attached to a spring system with a spring constant of 29.0. It is then set to oscillate at an amplitude of 0.68m. Time for (iii. \rightarrow v.) : $t=1.13$

(:2:) A mass of 9.25kg is attached to a spring system with a spring constant of 74.0. It is then set to oscillate at an amplitude of 0.47m. Time for (iii. \rightarrow v.) : $t=2.12$

(:3:) A mass of 0.25kg is added to a vertical spring system and the spring extends 97.0m. It is then set to oscillate at an amplitude of 0.51m. Time for (iii. \rightarrow v.) : $t=1.81$

(:4:) A mass of 1.25kg is added to a vertical spring system and the spring extends 73.0m. It is then set to oscillate at an amplitude of 0.62m. Time for (iii. \rightarrow v.) : $t=1.5$

(:5:) A mass of 0.25kg is added to a vertical spring system and the spring extends 19.0m. You observe that the system has a maximum velocity of 5.4m/s. Time for (iii. \rightarrow v.) : $t=0.3$

(:6:) A mass of 8.75kg is added to a vertical spring system and the spring extends 65.0m. You observe that the system has a maximum velocity of 8.1m/s. Time for (iii. \rightarrow v.) : $t=2.41$

(:7:) A mass of 9.5kg is added to a vertical spring system and the spring extends 37.0m. The system has a maximum kinetic energy of 23.0J. Time for (iii. \rightarrow v.) : $t=1.08$

(:8:) A mass of 1.25kg is added to a vertical spring system and the spring extends 65.0m. The system has a maximum kinetic energy of 31.0J. Time for (iii. \rightarrow v.) : $t=2.41$

(:9:) A mass of 6.25kg is added to a vertical spring system and the spring extends 20.0m. The system has a maximum potential energy of 35.0J. Time for (iii. \rightarrow v.) : $t=0.05$

(:10:) A mass of 5.0kg is added to a vertical spring system and the spring extends 81.0m. The system has a maximum potential energy of 31.0J. Time for (iii. \rightarrow v.) : $t=0.07$

Practice Problems Set #4

(:1:) You explore a planet and bring a 35.0cm long pendulum with you. You find that at small angles, it has a period of 1.62seconds.

- i. What is the gravity on the planet?
- ii. If you had a 1.88m pendulum, what would its period be?

(:2:) You explore a planet and bring a 2.0cm long pendulum with you. You find that at small angles, it has a period of 1.03seconds.

- i. What is the gravity on the planet?
- ii. If you had a 4.19m pendulum, what would its period be?

(:3:) You explore a planet and bring a 59.0cm long pendulum with you. You find that at small angles, it has a period of 1.77seconds.

- i. What is the gravity on the planet?
- ii. If you had a 2.37m pendulum, what would its period be?

(:4:) You explore a different planet and bring a 63cm long pendulum with you. Each day at small angle oscillations, it completes 174500 complete oscillations.

- i. What is the period?
- ii. What is the gravity on the new planet?

(:5:) You explore a different planet and bring a 90cm long pendulum with you. Each day at small angle oscillations, it completes 154300 complete oscillations.

- i. What is the period?
- ii. What is the gravity on the new planet?

(:6:) You explore a different planet and bring a 76cm long pendulum with you. Each day at small angle oscillations, it completes 198200 complete oscillations.

- i. What is the period?
- ii. What is the gravity on the new planet?

For problems (:7:) \rightarrow (:10:) find the gravity in City B

(:7:) A pendulum oscillating at small angles has a period of 1 second in city A, where the acceleration due to gravity is 9.92 m/s^2 . It is taken to city B where it is found to lose 321.0 seconds.

(:8:) A pendulum oscillating at small angles has a period of 1 second in city A, where the acceleration due to gravity is 9.67 m/s^2 . It is taken to city B where it is found to lose 211.0 seconds.

(:9:) A pendulum oscillating at small angles has a period of 1 second in city A, where the acceleration due to gravity is 9.68 m/s^2 . It is taken to city B where it is found to gain 315.0 seconds.

(:10:) A pendulum oscillating at small angles has a period of 1 second in city A, where the acceleration due to gravity is 9.69 m/s^2 . It is taken to city B where it is found to gain 171.0 seconds.

Practice Problems Set #5

For problems (:1:) \rightarrow (:3:) find:

- i. What is the total energy?
- ii. What is the maximum kinetic energy?
- iii. What is the maximum potential energy?
- iv. What is the minimum kinetic energy?
- v. What is the minimum kinetic energy?

(:1:) A mass of 8kg is added to a vertical spring system and the spring extends 10cm. It is then set to oscillate at an amplitude of 38cm.

(:2:) A mass of 6kg is added to a vertical spring system and the spring extends 18cm. It is then set to oscillate at an amplitude of 31cm.

(:3:) A mass of 7kg is added to a vertical spring system and the spring extends 11cm. It is then set to oscillate at an amplitude of 47cm.

For problems (:4:) → (:8:) find:

- i. What is the system's amplitude?
- ii. What is the system's total energy?
- iii. What is the mass of the object in the system?
- iv. What kinetic energy at this observed time?
- v. What is the potential energy at this time?

(:4:) At an observed time, you see that a spring system has a velocity of 1.25m/s at a position of 1.4cm from equilibrium. You also observe an angular frequency of 0.3 radians/sec. The spring also has a spring constant, $k=8.0$.

(:5:) At an observed time, you see that a spring system has a velocity of 0.5m/s at a position of 1.8cm from equilibrium. You also observe an angular frequency of 0.8 radians/sec. The spring also has a spring constant, $k=2.0$.

(:6:) At an observed time, you see that a spring system has a velocity of 1.5m/s at a position of 1.6cm from equilibrium. You also observe an angular frequency of 0.5 radians/sec. The spring also has a spring constant, $k=9.0$.

(:7:) At an observed time, you see that a spring system has a velocity of 1.0m/s at a position of 1.0cm from equilibrium. You also observe an angular frequency of 0.3 radians/sec. The spring also has a spring constant, $k=4.0$.

(:8:) At an observed time, you see that a spring system has a velocity of 0.5m/s at a position of 0.6cm from equilibrium. You also observe an angular frequency of 0.6 radians/sec. The spring also has a spring constant, $k=3.0$.

Practice Problems Set #6

For all the following problems, find:

- i. Amplitude of Oscillation
- ii. Angular Frequency
- iii. Maximum Velocity
- iv. Period
- v. Frequency

(:1:) A particle moving with SHM has velocities of 6.0cm/s and 8.0cm/s at distances of 8.0cm and 6.0cm respectively from its equilibrium position.

(:2:) A particle moving with SHM has velocities of 8.0cm/s and 15.0cm/s at distances of 15.0cm and 8.0cm respectively from its equilibrium position.

(:3:) A particle moving with SHM has velocities of 9.0cm/s and 12.0cm/s at distances of 4.0cm and 3.0cm respectively from its equilibrium position.

(:4:) A particle moving with SHM has velocities of 9.0cm/s and 12.0cm/s at distances of 12.0cm and 9.0cm respectively from its equilibrium position.

(:5:) A particle moving with SHM has velocities of 12.0cm/s and 16.0cm/s at distances of 4.0cm and 3.0cm respectively from its equilibrium position.

(:6:) A particle moving with SHM has velocities of 12.0cm/s and 16.0cm/s at distances of 8.0cm and 6.0cm respectively from its equilibrium position.

(:7:) A particle moving with SHM has velocities of 12.0cm/s and 16.0cm/s at distances of 16.0cm and 12.0cm respectively from its equilibrium position.