Machine Learning
Comp540 Spring 2016

This homework is due April 18 at 8 pm on Owlspace. The code base hw5.zip for the assignment is an attachment to Assignment 5 on Owlspace. You will add your code at the indicated spots in the files there. Place your answers to Problems 1 and 2 (typeset) in a file called writeup.pdf and add it to the zip archive. Upload the entire archive back to Owlspace before the due date and time.

1 Decision trees, entropy and information gain (10 points)

• (2 points) The entropy of a Bernoulli (Boolean 0/1) random variable X with P(X = 1) = q is given by

$$H(p) = -q \log q - (1-q) \log (1-q)$$

Suppose that a set S of examples contains p positive examples and n negative examples. The entropy H(S) of the set S is defined as H(p/(p+n)). Show that $H(S) \leq 1$ and that H(S) = 1 when p = n.

- (5 points) Consider a data set comprising 400 data points from class C_1 and 400 data points from class C_2 . Suppose that a decision stump model A splits these into two leaves at the root node; one containing (300,100) and the other containing (100,300) where (n,m) denotes n points are from class C_1 and m points are from class C_2 . Similarly a second decision stump model model B splits the examples as (200,400) and (200,0). What are the misclassification rates for model A and model B? Evaluate the entropy gain of the splits at the root node for the two models A and B. Also, evaluate the Gini index of the splits for the two models. Show that the entropy gain and Gini index are lower for the model B.
- (3 points) Can the misclassification rate ever increase when splitting on a feature? If so, give an example. If not, give a proof.

2 Bagging (10 points)

Consider a regression problem where we wish to learn a function f(x), where $x \in \mathbb{R}^d$. Suppose we learn L functions $h_1(x), \ldots, h_L(x)$. The predictions of each of these functions can be expressed as the sum of the true function plus an error term.

$$h_l(x) = f(x) + \epsilon_l(x)$$

where $\epsilon_l(x)$ is drawn from $N(0, \sigma_l^2)$. The expected squared-error of the function $h_l(x)$ is

$$E_X[\{f(x) + \epsilon_l(x) - f(x)\}^2] = E_X[\epsilon_l(x)^2]$$

The averaged error over the entire ensemble is

$$E_{av} = \frac{1}{L} \sum_{l=1}^{L} E_X [\epsilon_l(x)^2]$$

The prediction made by the bagger ensemble is the average over the L individual predictors:

$$h_{bag}(x) = \frac{1}{L} \sum_{l=1}^{L} h_l(x)$$

The error made by the bagged ensemble is:

$$\epsilon_{bag}(x) = h_{bag}(x) - f(x) = \frac{1}{L} \sum_{l=1}^{L} h_l(x) - f(x) = \left(\frac{1}{L} \sum_{l=1}^{L} (f(x) + \epsilon_l(x))\right) - f(x)$$

The expected squared-error of the bagged ensemble is:

$$E_{bag} = E_X[\epsilon_{bag}(x)^2]$$

• (5 points) Assuming that the individual errors $\epsilon_l(x)$ have zero mean and are uncorrelated, that is $E_X[\epsilon_l(x)] = 0$ and $E_X[\epsilon_m(x)\epsilon_l(x)] = 0$ for $m \neq l$, show that

$$E_{bag} = \frac{1}{L} E_{av}$$

• (5 points) In practice, however, the errors may be highly correlated. Nevertheless, using Jensens inequality for the special case of the convex function $f(x) = x^2$, show that the average expected squared-error E_{av} of the individual functions and the expected error of bagging E_{bag} satisfy $E_{bag} \leq E_{av}$, without any assumptions on $\epsilon_l(x)$. Jensen's equality states that for any convex function f(x), $\lambda_l \geq 0$ and $(\sum_{l=1}^L \lambda_l) = 1$,

$$f(\sum_{l=1}^{L} \lambda_l x_l) \le \sum_{l=1}^{L} \lambda_l f(x_l)$$

3 Fully connected neural networks and convolutional neural networks (100 points)

In this exercise, you will first develop a modular, fully connected neural net model and test it on the CIFAR-10 problem. Then, you will build a three layer convolutional neural net model and test it on the same CIFAR-10 problem. The purpose of this exercise is to give you a working understanding of neural net models and give you experience in tuning their (many) hyper-parameters. Download hw5.zip from Owlspace and unpack its contents. You will see the files as described in Table 1. A good reference for material on fully connected neural networks is the online text by Michael Nielsen available at http://neuralnetworksanddeeplearning.com/.

Name	Read?	Edit?	Description
fully_connected_nets.py	Yes	Yes	Script to run your fully connected networks.
convnets.py	Yes	Yes	Script to run your CNN functions.
fc_net.py	Yes	Yes	API for two-layer fully connected networks
			and networks of arbitrary depth.
cnn.py	Yes	Yes	API for three-layer CNN networks.
layers.py	Yes	Yes	Forward and backward functions for every
			layer type.
optim.py	Yes	Yes	Implementations of specific gradient descent
			rules.
layer_utils.py	Yes	No	Sandwich layer implementations.
utils.py	Yes	No	data loading utilities.
vis_utils.py	Yes	No	visualization utilities.
gradient_check.py	Yes	No	functions for checking gradients numerically.
fast_layers.py	Yes	No	fast versions of convolutional operations.
solver.py	Yes	No	gradient descent solver.
setup.py	No	No	code to setup fast layers implementation.
im2col.py	No	No	support for fast implementations of convolu-
			tional operations.
im2col_cython.c	No	No	support for fast implementations of convolu-
			tional operations.

Table 1: Code base for Assignment 5: fully connected neural networks

Before you begin the assignment, edit utils.py, providing it the path to CIFAR-10 data that we downloaded for Assignment 3 (to be specific, the directory datasets in that code base). Make sure you have the actual dataset there; else you might have to run the shell script I provided then to re-download it.

Fully connected feedforward neural networks: a modular approach

We will implement fully-connected networks using a modular approach. By this we mean that we will develop a backward and a forward function for each type of layer (affine, ReLU, pool, fully-connected). The forward function will receive inputs, weights, and other parameters and will return both an output and a cache object storing data needed for the backward pass,

```
def layer_forward(x, theta):
    """ Receive inputs x and weights theta """
    # Do some computations ...
    z = # ... some intermediate value
    # Do some more computations ...
    out = # the output

cache = (x, theta, z, out) # Values we need to compute gradients
    return out, cache
```

The backward pass will receive upstream derivatives and the cache object computed during the forward pass, and will return gradients with respect to the inputs and weights,

```
def layer_backward(dout, cache):
    """

Receive derivative of loss with respect to outputs and cache,
    and compute derivative with respect to inputs.
    """

# Unpack cache values
    x, theta, z, out = cache

# Use values in cache to compute derivatives
    dx = # Derivative of loss with respect to x
    dtheta = # Derivative of loss with respect to theta
```

After implementing a bunch of layers this way, we will be able to easily combine them to build classifiers with different architectures. In addition to implementing fully-connected networks of arbitrary depth, we will also explore different update rules for optimization especially suited for deep networks.

Problem 3.1.1: Affine layer: forward (5 points)

An affine layer computes a linear function of inputs in a fully connected network. An affine layer has h outputs, d inputs, and connection weights θ of size $d \times h$ connecting the outputs and inputs, as well as a bias weight vector θ_0 of size h. The forward function computes output a_j for every $j \in \{1, ..., h\}$ for an input $x \in \mathbb{R}^d$ by computing

$$a_j = \theta_j^T x + \theta_{0j}$$

where θ_j is the j^{th} column of the θ matrix and corresponds to the connections between the inputs and output unit j, and θ_{0j} is the j^{th} component of the bias vector θ_0 . To accommodate inputs shaped as a volume for convolutional networks, the function accepts $x \in \Re^{d_1 \times \dots d_n}$ by first reshaping it into a vector of size d equal to the product of the d_i 's.

In the file layers.py implement the affine_forward function. Once you are done, you should test your implementation of affine_forward by running the script fully_connected_nets.py.

Problem 3.1.2: Affine layer: backward (5 points)

The affine_backward function propagates derivatives from the outputs back to the inputs of an affine layer. Let the error derivative vector at the output of the layer be $\frac{\partial J}{\partial a_j}$. We now need to calculate $\frac{\partial J}{\partial x_i}$, $\frac{\partial J}{\partial \theta_j}$ and $\frac{\partial J}{\theta_{0j}}$. Use the chain rule of derivatives together with the linear relationship between a_j and x to derive the formulas for these three partial derivatives. Hint: $\frac{\partial J}{\partial x} = \frac{\partial J}{\partial y} \frac{\partial y}{\partial x}$.

In the file layers.py implement the affine_backward function. Once you are done, you should test your implementation of affine_backward by running the script fully_connected_nets.py.

Problem 3.1.3: ReLU layer: forward (2 points)

A ReLU layer constitutes a non-linear layer in a fully-connected network. It takes input $x \in \mathbb{R}^d$ and produces output $a \in \mathbb{R}^d$ such that

$$a_j = \begin{cases} x_j & \text{if } x_j > 0\\ 0 & \text{otherwise} \end{cases}$$

In the file layers.py implement the relu_forward function. Once you are done, you should test your implementation of relu_forward by running the script fully_connected_nets.py.

The relu_backward function propagates derivatives from the outputs back to the inputs of an ReLU layer. Let the error derivative vector at the output of the layer be $\frac{\partial J}{\partial a_j}$. We now need to calculate $\frac{\partial J}{\partial x_i}$ for the ReLU layer. As before, use the chain rule to compute it.

In the file layers.py implement the relu_backward function. Once you are done, you should test your implementation of relu_backward by running the script fully_connected_nets.py.

Sandwich layers

There are some common patterns of layers that are frequently used in neural nets. For example, affine layers are frequently followed by a ReLU nonlinearity. To make these common patterns easy, we define several convenience layers in the file layer_utils.py. For now take a look at the affine_relu_forward and affine_relu_backward functions. The script fully_connected_nets.py will numerically gradient check the backward pass.

Loss layers: softmax and SVM

You implemented these loss functions in the last assignment, so we will give them to you for free here. You should still make sure you understand how they work by looking at the implementations in layers.py. The script fully_connected_nets.py will make sure that the implementations are correct.

Problem 3.1.5: Two layer network (5 points)

Now that you have built modular versions of the necessary layers, you will implement a two layer fully connected network using these modular implementations. In particular, you will implement a two-layer fully-connected neural network with ReLU nonlinearity and softmax loss. The architectural layers are affine - relu - affine - softmax. Open the file fc_net.py and complete the implementation of the TwoLayerNet class. This class will serve as a model for the other networks you will implement in this assignment, so read through it to make sure you understand the API. The script fully_connected_nets.py will test your implementation, including your network initialization, forward and backward computations.

Problem 3.1.6: Overfitting a two layer network (5 points)

Open the file solver.py and read through it to familiarize yourself with the API for the Solver class. The documentation includes sample calls to create a Solver instance with default parameters that are a good starting point for this problem. Then, use a Solver instance at the indicated spot in fully_connected_nets.py to train a TwoLayerNet on the

CIFAR-10 data. Select the size of the hidden layer and the regularization parameter $t\overline{b}$ achieve at least 50% accuracy on the validation set.

Problem 3.1.7: Multilayer network (10 points)

Next you will implement a fully-connected network with an arbitrary number of hidden layers. Read through the FullyConnectedNet class in fc_net.py. Implement the initialization, the forward pass, and the backward pass. As a sanity check, we have code in fully_connected_nets.py to check the initial loss and gradients of the network both with and without regularization. Do the initial losses seem reasonable? For gradient checking, you should expect to see errors around 1e-6 or less.

Problem 3.1.8: Overfitting a three layer network (2 points)

As another sanity check, make sure you can overfit a small dataset of 50 images. First we will try a three-layer network with 100 units in each hidden layer. You will need to tweak the learning rate and initialization scale in fully_connected_nets.py at the indicated point, and you should be able to achieve 100% training accuracy within 20 epochs.

Problem 3.1.9: Overfitting a five layer network (3 points)

Now try to use a five-layer network with 100 units on each layer to overfit 50 training examples. Again you will have to adjust the learning rate and weight initialization, and you should be able to achieve 100% training accuracy within 20 epochs. Did you notice anything about the comparative difficulty of training the three-layer net vs training the five layer net?

Update rules

So far we have used vanilla stochastic gradient descent (SGD) as our update rule. More sophisticated update rules can make it easier to train deep networks. We will implement a few of the most commonly used update rules and compare them to vanilla SGD.

Problem 3.1.10: SGD+Momentum (5 points)

Open the file optim.py and read the documentation at the top of the file to make sure you understand the API. Implement the SGD+momentum update rule in the function sgd_momentum and run the script fully_connected_nets.py to check your implementation. You should see errors less than 1e-8.

The SGD+momentum rule is parameterized by momentum μ and it maintains a velocity

variable v updated as follows:

$$v \leftarrow \mu v - \alpha \frac{\partial J}{\partial \theta}$$

where α is the learning rate. Then, θ is updated as

$$\theta \leftarrow \theta + v$$

Then we train a six-layer network with both SGD and SGD+momentum. You should see the SGD+momentum update rule converge faster.

Problem 3.1.11: RMSProp (5 points)

RMSProp is an update rule that sets per-parameter learning rates by using a running average of the second moments of gradients. In the file optim.py, implement the RM-SProp update rule in the rmsprop function check your implementations using the tests in fully_connected_nets.py. The RMSProp rule is parameterized by a decay rate γ , and an ϵ . It maintains a cache c of squared gradients which is updated as follows:

$$c \leftarrow \gamma c + (1 - \gamma) \frac{\partial J}{\partial \theta} * \frac{\partial J}{\partial \theta}$$

Then, θ is updated as

$$\theta \leftarrow \theta - \alpha \frac{\partial J}{\partial \theta} \frac{1}{(\sqrt{c} + \epsilon)}$$

where the ϵ is added to the denominator to keep it from being zero.

Problem 3.1.12: Training a fully connected network for the CIFAR-10 dataset (5 points)

Use the FullyConnectedNet class that you have developed and the new gradient descent rules to train a model that achieves greater than 50% accuracy on the validation set of the full CIFAR-10 dataset. You will need to find the number of hidden layers, the number of units in each layer, the weight scale, the learning rule, the learning rate, batch size, number of training epochs, and batch size to achieve this training goal. Use the show_net_weights function to visualize the first level weights.

Convolutional neural networks

So far we have worked with deep fully-connected networks, using them to explore different optimization strategies and network architectures. Fully-connected networks are a good testbed for experimentation because they are very computationally efficient, but in practice all state-of-the-art results use convolutional networks instead. First you will implement several layer types that are used in convolutional networks. You will then use these layers to train a convolutional network on the CIFAR-10 dataset.

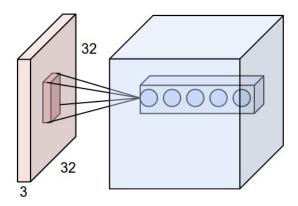


Figure 1: An example input volume in red (e.g. a 32x32x3 CIFAR-10 image), and an example volume of neurons in the first convolutional layer. Each neuron in the convolutional layer is connected only to a local region in the input volume spatially, but to the full depth (i.e. all color channels). Note, there are multiple neurons (5 in this example) along the depth, all looking at the same region in the input. The neurons compute a dot product of their weights with the input followed by a non-linearity, but their connectivity is now restricted to be local spatially.

Convolutional layer

The convolutional layer is the core building block of a convolutional network, and its output volume can be interpreted as holding neurons arranged in a 3D volume. The convolutional layer's parameters consist of a set of learnable filters. Every filter is small spatially (along width and height), but extends through the full depth of the input volume as shown in Figure 1. During the forward pass, we slide (more precisely, convolve) each filter across the width and height of the input volume, producing a 2-dimensional activation map of that filter. As we slide the filter, across the input, we are computing the dot product between the entries of the filter and the input. Intuitively, the network will learn filters that activate when they see some specific type of feature at some spatial position in the input. Stacking these activation maps for all filters along the depth dimension forms the full output volume. Every entry in the output volume can thus also be interpreted as an output of a neuron that looks at only a small region in the input and shares parameters with neurons in the same activation map (since these numbers all result from applying the same filter).

When dealing with high-dimensional inputs such as images, as we saw above it is impractical to connect neurons to all neurons in the previous volume. Instead, we will connect each neuron to only a local region of the input volume. The spatial extent of this connectivity is a hyperparameter called the receptive field of the neuron (also called filter size). The extent of the connectivity along the depth axis is always equal to the depth of the input volume. It is important to note this asymmetry in how we treat the spatial dimensions (width and height) and the depth dimension: The connections are local in space (along width and height), but always full along the entire depth of the input volume.

We have explained the connectivity of each neuron in the convolutional layer to the input volume, but we haven't yet discussed how many neurons there are in the output volume or how they are arranged. Three hyperparameters control the size of the output volume: the depth, stride and zero-padding.

- First, the depth of the output volume is a hyperparameter that we can pick; It controls the number of neurons in the convolutional layer that connect to the same region of the input volume. This is analogous to a regular neural network, where we had multiple neurons in a hidden layer all looking at the exact same input. As we will see, all of these neurons will learn to activate for different features in the input. For example, if the first convolutional layer takes as input the raw image, then different neurons along the depth dimension may activate in presence of various oriented edged, or blobs of color. We will refer to a set of neurons that are all looking at the same region of the input as a depth column.
- Second, we must specify the stride with which we allocate depth columns around the spatial dimensions (width and height). When the stride is 1, then we will allocate a new depth column of neurons to spatial positions only 1 spatial unit apart. This will lead to heavily overlapping receptive fields between the columns, and also to large output volumes. Conversely, if we use higher strides then the receptive fields will overlap less and the resulting output volume will have smaller dimensions spatially.
- Sometimes it will be convenient to pad the input with zeros spatially on the border of the input volume. The size of this zero-padding is a hyperparameter. The nice feature of zero padding is that it will allow us to control the spatial size of the output volumes. In particular, we will sometimes want to exactly preserve the spatial size of the input volume.

We can compute the spatial size of the output volume as a function of the input volume size (W), the receptive field size of the convolutional layer neurons (F), the stride with which they are applied (S), and the amount of zero padding used (P) on the border. The formula for calculating how many neurons "fit" is given by 1+(W-F+2P)/S. If this number is not an integer, then the strides are set incorrectly and the neurons cannot be tiled so that they "fit" across the input volume neatly, in a symmetric way. In general, setting zero padding to be P=(F-1)/2 when the stride is S=1 ensures that the input volume and output volume will have the same size spatially. It is very common to use zero-padding in this way in designing convolutional network architectures.

Note that the spatial arrangement hyperparameters have mutual constraints. For example, when the input has size W=10, no zero-padding is used P=0, and the filter size is F=3, then it would be impossible to use stride S=2, since 1+(W-F+2P)/S=1+(10-3+0)/2=4.5, i.e. not an integer, indicating that the neurons don't "fit" neatly and symmetrically across the input. Therefore, this setting of the hyperparameters is considered to be invalid, and a convolutional network library would likely throw an exception.

Here is a real-world example. The Krizhevsky et al. architecture that won the ImageNet challenge in 2012 accepted images of size [227x227x3]. On the first Convolutional Layer, it used neurons with receptive field size F = 11, stride S = 4 and no zero padding P = 0. Since 1 + (227 - 11)/4 = 55, and since the convolutional layer had a depth of K = 96, the convolutional layer output volume had size [55x55x96]. Each of the 55*55*96 neurons in this volume was connected to a region of size [11x11x3] in the input volume. Moreover, all 96 neurons in each depth column are connected to the same [11x11x3] region of the input, but of course with different weights.

Parameter sharing scheme is used in convolutional layers to control the number of parameters. Using the real-world example above, we see that there are 55*55*96 = 290,400 neurons in the first convolutional layer, and each has 11*11*3 = 363 weights and 1 bias. Together, this adds up to 290400 * 364 = 105,705,600 parameters on the first layer of the convolutional network alone. Clearly, this number is very high.

It turns out that we can dramatically reduce the number of parameters by making one reasonable assumption: That if one patch feature is useful to compute at some spatial position (x, y), then it should also be useful to compute at a different position (x2, y2). In other words, denoting a single 2-dimensional slice of depth as a depth slice (e.g. a volume of size [55x55x96] has 96 depth slices, each of size [55x55]), we are going to constrain the neurons in each depth slice to use the same weights and bias. With this parameter sharing scheme, the first convolutional layer in our example would now have only 96 unique set of weights (one for each depth slice), for a total of 96*11*11*3 = 34,848 unique weights, or 34,944 parameters (+96 biases). Alternatively, all 55*55 neurons in each depth slice will now be using the same parameters. In practice during backpropagation, every neuron in the volume will compute the gradient for its weights, but these gradients will be added up across each depth slice and only update a single set of weights per slice.

Notice that if all neurons in a single depth slice are using the same weight vector, then the forward pass of the convolutional layer can in each depth slice be computed as a convolution of the neuron's weights with the input volume (Hence the name: convolutional layer). Therefore, it is common to refer to the sets of weights as a filter (or a kernel), which is convolved with the input. The result of this convolution is an activation map (e.g. of size [55x55]), and the set of activation maps for each different filter are stacked together along the depth dimension to produce the output volume (e.g. [55x55x96]).

The backward pass for a convolution operation (for both the data and the weights) is also a convolution. Use the chain rule to propagate the upstream derivatives across each filter.

Pooling layer

It is common to periodically insert a pooling layer in-between successive convolutional layers in a convolutional network architecture. Its function is to progressively reduce the spatial size of the representation to reduce the amount of parameters and computation in the network, and hence to also control overfitting. The pooling layer operates independently on every

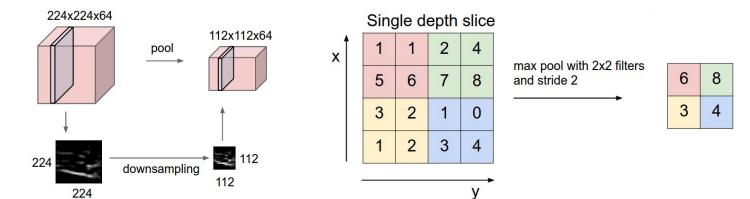


Figure 2: Pooling layer downsamples the volume spatially, independently in each depth slice of the input volume. Left: In this example, the input volume of size [224x224x64] is pooled with filter size 2, stride 2 into output volume of size [112x112x64]. Notice that the volume depth is preserved. Right: The most common downsampling operation is max, giving rise to max pooling, here shown with a stride of 2. That is, each max is taken over 4 numbers (little 2x2 square).

depth slice of the input and resizes it spatially, using the maxoperation. The most common form is a pooling layer with filters of size 2x2 applied with a stride of 2 to downsample every depth slice in the input by 2 along both width and height, discarding 75% of the activations. Every max operation would in this case be taking a max over 4 numbers (little 2x2 region in some depth slice). The depth dimension remains unchanged. More generally, the pooling layer, accepts a volume of size $W1 \times H1 \times D1$ and produces a volume of size $W2 \times H2 \times D1$ where W2 = 1 + (W1 - F)/S and H2 = 1 + (H1 - F)/S. The parameters F and S are the filter size and stride respectively.

To compute the backward pass for a $\max(x, y)$ operation we route the gradient to the input that had the highest value in the forward pass. Hence, during the forward pass of a pooling layer it is common to keep track of the index of the max activation so that gradient computation is efficient during backpropagation.

Problem 3.2.1: Convolution: naive forward pass (10 points)

The core of a convolutional network is the convolution operation, explained above. In the file layers.py, implement the forward pass for the convolution layer in the function conv_forward_naive. You don't have to worry too much about efficiency at this point; just write the function in whatever way you find most clear. You can test your implementation by running the convnets.py script.

Problem 3.2.2: Convolution: naive backward pass (10 points)

Implement the backward pass for the convolution operation in the function <code>conv_backward_naive</code> in the file <code>layers.py</code>. Again, you don't need to worry too much about computational efficiency. When you are done, run the <code>convnets.py</code> script to check your backward pass with a numeric gradient check.

Problem 3.2.3: Max pooling: naive forward pass (5 points)

Implement the forward pass for the max-pooling operation in the function max_pool_forward_naive in the file layers.py. Again, don't worry too much about computational efficiency. Check your implementation by running the convnets.py script.

Problem 3.2.4: Max pooling: naive backward pass (5 points)

Implement the backward pass for the max-pooling operation in the function max_pool_backward_naive in the file layers.py. You don't need to worry about computational efficiency. Check your implementation with numeric gradient checking by running convnets.py script.

Fast layers

Making convolution and pooling layers fast can be challenging. To spare you the pain, we've provided fast implementations of the forward and backward passes for convolution and pooling layers in the file fast_layers.py. The fast convolution implementation depends on a Cython extension; to compile it you need to run the following from the pa5 directory:

python setup.py build_ext --inplace

The API for the fast versions of the convolution and pooling layers is exactly the same as the naive versions that you implemented above: the forward pass receives data, weights, and parameters and produces outputs and a cache object; the backward pass receives upstream derivatives and the cache object and produces gradients with respect to the data and weights. The fast implementation for pooling will only perform optimally if the pooling regions are non-overlapping and tile the input. If these conditions are not met then the fast pooling implementation will not be much faster than the naive implementation. You can compare the performance of the naive and fast versions of these layers by running the convnets.py script.

Convolutional sandwich layers

Previously we introduced the concept of "sandwich" layers that combine multiple operations into commonly used patterns. In the file layer_utils.py you will find sandwich

layers that implement a few commonly used patterns for convolutional networks. The script convnets.py will test these implementations next.

Problem 3.2.5: Three layer convolutional neural network (10 points)

Now that you have implemented all the necessary layers, we can put them together into a simple convolutional network. Open the file cnn.py and complete the implementation of the ThreeLayerConvNet class.

Testing the CNN: loss computation

After you build a new network, one of the first things you should do is check the loss computation. When we use the softmax loss, we expect the loss for random weights (and no regularization) to be about log(C) for C classes. When we add regularization this should go up. The script convnets.py runs this check for you.

Testing the CNN: gradient check

After the loss looks reasonable, use numeric gradient checking to make sure that your backward pass is correct. When you use numeric gradient checking you should use a small amount of artificial data and a small number of neurons at each layer. The script convnets.py runs this check for you.

Testing the CNN: overfit small data

A nice trick is to train your model with just a few training samples. You should be able to overfit small datasets, which will result in very high training accuracy and comparatively low validation accuracy. Plotting the loss, training accuracy, and validation accuracy should show clear overfitting: The script convnets.py runs this check for you.

Problem 3.2.6: Train the CNN on the CIFAR-10 data (5 points)

By training a three-layer convolutional network with hidden dimension of 500 for one epoch, you should achieve greater than 40% accuracy on the CIFAR-10 training set. The script convnets.py sets up this CNN and runs it for you. It also visualizes the first-layer convolutional filters from the trained network. Play with the hyper parameters to achieve ξ 50% accuracy on the validation set.

Acknowledgement 15

This exercise would not be possible without the brilliant work of Andrej Karpathy and his team at Stanford University.