

Research notes on metrics for GNNs applied to biological problems

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1 Graph Neural Networks

1.1 Reviews

1.1.1 Graph neural networks:

A review of methods and applications Zhou et al mention several GNN approaches in use today Generative models popular today:

Sequential graph generation process

- GraphRNN - generates the adjacency matrix of a graph by generating the adjacency vector of each node step by step, with graph outputs with different number of nodes.
- Li 2018 - also generates nodes and edges sequentially uses the hidden state to decide what to do at the next step
- GraphAF - also a sequential process, Conducts a validity check of each molecule generated at each step to see if it's valid.

Non-sequential graph generation process

- MolGAN - to generate small molecules. Uses a permutation-invariant to solve the node adjacency matrix at once. Also implements an RL-based optimization toward desired chemical properties
- Ma et al 2018 - constrained VAE for semantic validity of generated graph
- GCPN similar to MolGAN, uses RL based methods to ensure validity of domain-specific rules
- Graph Normalizing Flows

a common practice of applying Langevin dynamics. We chose the value of the hyper-parameters based on the **MMD** metrics on the validation set, which contains 32 samples from the training set.

$$\tilde{\mathbf{x}}_t \leftarrow \tilde{\mathbf{x}}_{t-1} + \frac{\alpha_i}{2} \mathbf{s}_{\theta}(\tilde{\mathbf{x}}_{t-1}, \sigma_i) + \epsilon_s \sqrt{\alpha_i} \mathbf{z}_t$$

Figure 2: MMD optimization strategy

2.1 Objective:

2.1.1 Generative graph dist close to the input graph dist

2.1.2 (pseudo)-metric to assess dissimilarity between G (generated graphs) and G^* (input graphs)

2.2 On images

2.2.1 Frechet Inception Distance

The idea here is to use deeper representational layers of an ANN and used the squared Wasserstein metric to compare two multinomial Gaussians. Introduced 2017

2.2.2 LPIPS Project page

Introduced 2017

2.2.3 Why comparing graphs is hard:

- Metrics need to deal with spatial invariances such as cycles.
- Graph edit distance is NP-hard (Zeng 2009) and therefore does not satisfy efficiency criterion.
- Other publications:

2.3 Desiderata for good metrics:

1. Robust to noise
2. Expressive, if they don't arise from the same dist, then metric should detect this.
3. Computationally efficient.

3 MMD - current accepted method to evaluate generative GNNs

- The MMD formula goes as follows:

$$\text{MMD}(X, Y) := \frac{1}{n^2} \sum_{i,j=1}^n k(x_i, x_j) + \frac{1}{m^2} \sum_{i,j=1}^m k(y_i, y_j) - \frac{2}{nm} \sum_{i=1}^n \sum_{j=1}^m k(y_i, y_j)$$

- use it for hypothesis/two-sample testing.
- In practice, we evaluate $d_{MMD}(\mathcal{G}, \mathcal{G}^*) := MMD(f(\mathcal{G}), f(\mathcal{G}^*))$ for a distribution \mathcal{G} . Given multiple distributions G_1, G_2, \dots , the values of d_{MMD} can be used to rank models, where smaller values are assumed to indicate a larger agreement with the original distribution \mathcal{G}^* .
- Commonly used kernels: first Wasserstein distance, total variation distance, radial basis function.
- Commonly used descriptor functions: degree distribution histogram, clustering coefficient, Laplacian spectrum histogram.

3.1 Potential pitfalls of descriptors

- Degree distributions are ok seemingly
- Clustering does not distinguish fully connected vs disconnected cliques
- Spectral methods are not clearly expressive. Does not seem to be for certain classes of graphs.
- Parameters and descriptors are set a priori in the best case
- Model performance is highly dependent on parameters and descriptor functions.

4 Research objectives

There are multiple objectives here:

1. Find optimal kernel/hyperparameter combination based on controlled experiments on a given dataset to evaluate a good MMD configuration.
 - For this we will need <https://www.alphafold.ebi.ac.uk/download>, because it's clean. Also filter single chain proteins to extract graphs in the first place.
 - This can be built as a first step to get the pipeline going.
2. Show which parameters influence evaluation and how?
 - Conduct perturbation experiments on graphs
3. Find novel domain-agnostic evaluation & domain-specific evaluation metrics
 - (a) Domain-agnostic evaluation measures
 - Correlation with graph-edit distance

- Correlation with perturbation
 - Topology/persistence based approaches could be useful for modelling features like binding pockets, etc?
- (b) Domain-specific evaluation measures
- Alignment
 - Energy?

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