

# GGNNMetrics, a package for optimizing and understanding MMD parametrization for evaluating generative GNNs on protein datasets.

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February 2, 2022

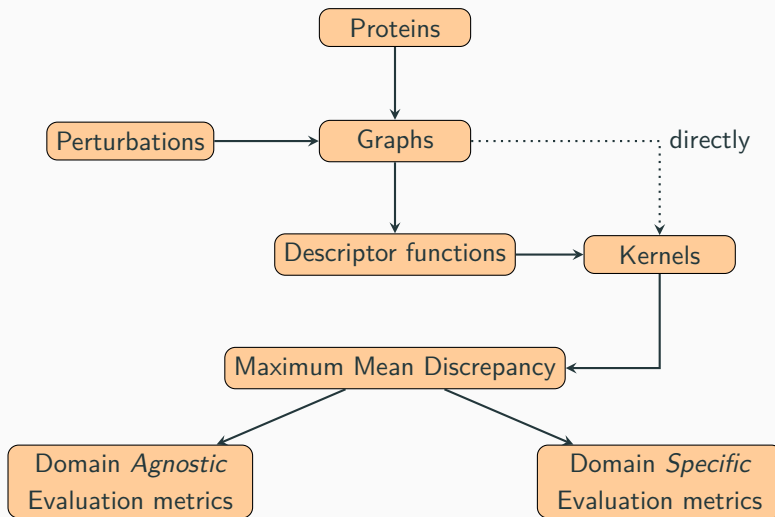


**DBSSE**

**ETH** zürich

- The following provides an overview of the plan for the thesis
- Aspirational/low priority items are [in blue](#).

# General workflow



**Figure 1:** Overview of the library

# Protein source datasets

- Start with human proteome from AlphaFold (23390 samples, [source](#))
- Expand to other experimentally datasets & add cleaning handlers

# Graph extraction from pdb file

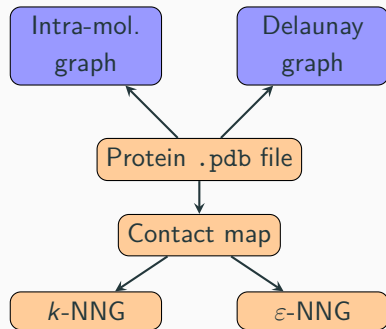
Granularity:

- CA-atom (1 point per amino acid)
- all atoms (loop through each residue to get atom coordinates)
- CB, C, O, ... see `Bio.PDB.Residue`

Graph extraction:

- Contact map (fully connected weighted graph).
- $\epsilon$ -neighborhood graph. [1]
- k-nearest neighbor graph. [10]
- **Intramolecular graphs** (hydrogen bonds, salt bridges, pi-cation bonds)
- **Delaunay graph** (through Delaunay triangulation, results in denser graph) [8].

Dependencies: only depend on Biopython.



**Figure 2:** Order of extraction of graphs from .pdb files.

# Descriptor functions & Kernels

## Descriptor functions

Domain agnostic graph descriptors [5]:

- Degree distribution histogram
- Clustering coefficient histogram
- Laplacian spectrum histogram

Topological descriptors (using the weighted, fully connected contact map):

- Persistence diagram, converted to Betti curves, persistence image, persistence landscapes. [7]
- Also possible to obtain vector representation from persistence diagram by applying a heat kernel to it. [6]

Domain specific: t.b.d

## Kernels

Conditions for selection: p.s.d & fast

General kernels [5]:

- RBF kernel
- Laplacian kernel
- Linear
- Neighborhood Subgraph Pairwise Distance graph kernel [3]

The last can be used when discrete edge features are employed.

Domain specific: t.b.d

# Maximum Mean Discrepancy

The Maximum Mean Discrepancy (MMD) [4, 2] is defined as follows:

$$\text{MMD}(X, Y) := \frac{1}{n^2} \sum_{i,j=1}^n k(x_i, x_j) + \frac{1}{m^2} \sum_{i,j=1}^m k(y_i, y_j) - \frac{2}{nm} \sum_{i=1}^n \sum_{j=1}^m k(y_i, y_j)$$

where:

- $x_i, x_j \sim \mathcal{X}$ ,  $n$  is the number of samples from non-empty set  $\mathcal{X}$ ;
- $y_i, y_j \sim \mathcal{Y}$ ,  $m$  is the number of samples from non-empty set  $\mathcal{Y}$ ;
- $k : \mathcal{X} \times \mathcal{X} \rightarrow \mathbb{R}$  is a valid kernel.

MMD is a kernelized proxy of the distance between two graph distributions  $G$  and  $G^*$  computed as  $d_{\text{MMD}}(G, G^*) = \text{MMD}(f(G), f(G^*))$ , where  $f$  is the descriptor function of the graph. A lower  $d_{\text{MMD}}(G, G^*)$  indicates a greater similarity between  $G$  and  $G^*$ . [Potentially look at other metrics for GNNs. \[9\]](#)

# Perturbations to graphs

Domain agnostic [5]:

- edge insertion
- edge removal
- edge rewiring
- node addition

Domain specific:

- t.b.d. (e.g. add edge “disrupting” binding pocket, how to do this?)



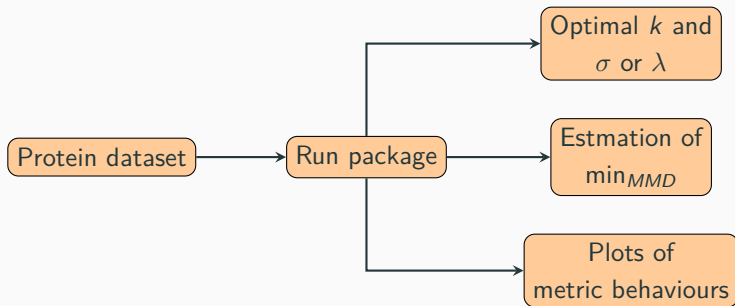
Domain agnostic [5]:

- Correlation with perturbation
- Correlation with graph edit distance

Domain specific:

- Alignment
- (estimated) folding energy
- Investigate what makes a “good” protein.





## Workflows enabled by the package









**Figure 3:** Workflows enabled by the package.

# Plots to understand the behaviour of MMD

- Distribution of  $\min_{MMD}$  for different random test/train splits.
- Correlation perturbation with MMD values with different parameters
- MMD vs. parameter

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