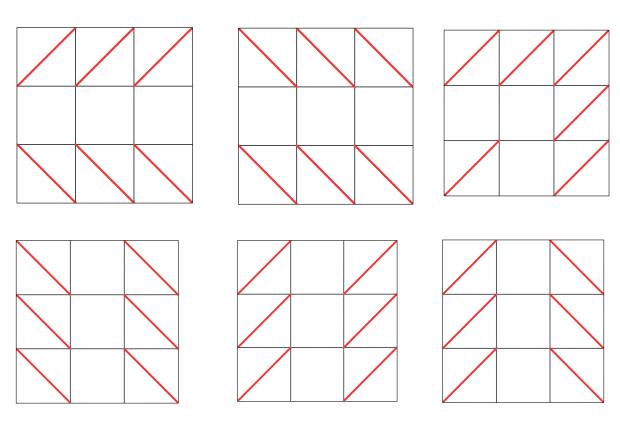
N Diagonals

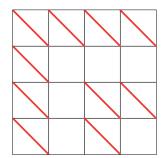
By clicking on squares, draw N diagonals that do not touch each other.

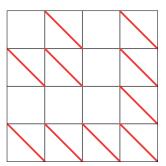
Mathematical Thinking in Computer Science by University of California San Diego & National Research University Higher School of Economics coursera.org

The case of 6 diagonals in a 3 by 3 grid. There are more...not shown Try the puzzle here: http://dm.compsciclub.ru/app/quiz-n-diagonals

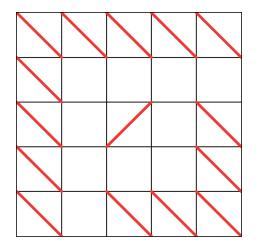


The case of 10 diagonals in a 4 by 5 grid.

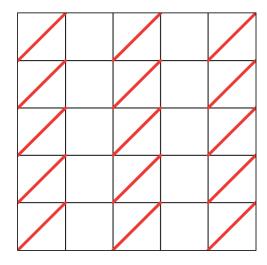




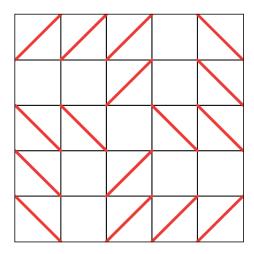
The case of 15 diagonals in a 5 by 5 grid. 15 diagonals is not difficult to obtain.



Or



To obtain 16 is a challenge...



Two algorithms are presented below. Interestingly the randomized algorithm is naturally slower than the backtracking algorithm, but not entirely without some useful value. $\frac{\text{https://oeis.org/A264041}}{\text{oeis.org/A264041}}$ predicts 21 as a max for n = 6 and 29 for n=7. Both algorithms find the solutions fairly quickly for n = 6. For n = 7, neither algorithm yielded an answer within a reasonable time.

First solution a randomized algorithm

```
https://math.stackexchange.com/questions/339387/how-to-solve-5x5-grid-
with-16-diagonals
The link inspired the randomized solution below. Not the fastest,
but nonetheless an amusing way to find solutions.
import random
#displays the grid
def printGrid(grid):
    for i in range(len(grid)):
        print()
        for j in range(len(grid)):
           print(grid[i][j],end=' ')
   print()
Given a list of moves, randomly return one move from the list
def randomMove(moves):
    random.shuffle(moves)
    temp = moves.pop()
    return temp
Counts the number of +1, -1 in a grid
def getNumDiag(grid):
    count = 0
    for i in range(len(grid)):
        for j in range(len(grid)):
            if(qrid[i][j] == 1 \text{ or } qrid[i][j] == -1):
                count+=1
    return count
 0 , +1 , -1
                   represent empty cell , \ , /
The cells sharing an edge with a cell with a \pm 1 cannot contain a \mp 1.
If a cell contains a 1, the adjacent cells to the top-left
and bottom-right cannot also contain a 1.
If a cell contains a -1, the adjacent cells to the bottom-left
and top-right cannot also contain a -1.
Here, cells containing a "1" have a diagonal running top-left to bottom-
right,
and cells containing a "-1" have a diagonal running the other way.
```

```
Cells containing _ do not have a diagonal at all.
def getMoves(grid,i,j):
    #All moves are intially possible
    moves = [0, 1, -1]#All moves are intially possible
    #Check west and remove
    if j - 1>=0:
        if(grid[i][j-1] == 1):
            if -1 in moves:
                moves.remove(-1)
        if(grid[i][j-1] == -1):
            if 1 in moves:
                moves.remove(1)
    #Check north and remove
    if i - 1>=0:
        if(grid[i-1][j] == 1):
            if -1 in moves:
                moves.remove(-1)
        if(grid[i-1][j] == -1):
            if 1 in moves:
                moves.remove(1)
    #Check west north west and remove
    if i - 1 >= 0 and j - 1 >= 0:
        if(grid[i-1][j-1] == 1):
            if 1 in moves:
                moves.remove(1)
    #Check east north east and remove
    if ((i -1 >= 0) \text{ and } (j+1 < len(grid))):
        if(grid[i-1][j+1] == -1):
            if -1 in moves:
                moves.remove(-1)
    return moves
. . .
Randomly updates an grid and returns this updated grid
def fillGrid(grid):
    for i in range(len(grid)):
        for j in range(len(grid)):
            moves = getMoves(grid,i,j)
            grid[i][j] =randomMove(moves)
    return grid
#run until a solutions are found and then display
size = 5
while (True):
    #intialize grid
    grid = [[0 for i in range(size)] for j in range(size)]
    temp = fillGrid(grid)
    if(getNumDiag(temp) == 16):
        print(printGrid(temp))
```

```
Two solutions found after a few minutes
-1 0 1 1 1
-1 0 1 0 0
-1 -1 0 -1 -1
0 0 1 0 -1
1 1 1 0 -1
-1 -1 -1 0 1
0 0 -1 0 1
1 1 0 1 1
1 0 -1 0 0
1 0 -1 -1 -1
Second solution a backtracking algorithm
Backtracking Algorithm to solve the NDiagonals Puzzle
Adapted from https://github.com/mattcollier/diagonals#sample-output
Try the puzzle here: http://dm.compsciclub.ru/app/quiz-n-diagonals
#Ultility displays the grid
def printGrid(grid):
    for i in range(len(grid)):
        print()
        for j in range(len(grid)):
            print(grid[i][j],end=' ')
        print()
    print()
. . .
Use the following encoding
 \_ , +1 , -1 represent empty cell , \backslash , /
The cells sharing an edge with a cell with a \pm 1 cannot contain a \mp 1.
If a cell contains a 1, the adjacent cells to the top-left
and bottom-right cannot also contain a 1.
If a cell contains a -1, the adjacent cells to the bottom-left
and top-right cannot also contain a -1.
. . .
```

```
#Check 4 directions: West, West North West, North, Eest North East
def check neighbors (row, col, value):
    global grid
    # check West
    if(col > 0):
        W = grid[row][col - 1]
        if (W != 0 \text{ and } W != \text{value}):
            return False
    # check WNW, N, ENE
    if row > 0:
        # check North
        N = grid[row - 1][col];
        if (N != 0 \text{ and } N != \text{value}):
            return False
        # check North West North cannot be -1
        if (value == 1 and col > 0):
            NWN = grid[row - 1][col -1];
            if (NWN != 0 and NWN != -1):
                return False
        # check East North East cannot be +1
        if (value == -1 and col < size -1):
            ENE = grid[row - 1][col + 1]
            if (ENE != 0 and ENE != 1):
                return False
    return True
. . .
Backtrack until reminaing diagonals equals 0
def extend(row, col, remainingDiags):
    global size
    global grid
    global ct
    if remainingDiags == 0:
        ct+=1
        print('Solution:',ct)
        printGrid(grid)
        return
    if row == size:
        return
    nextRow = row
    nextCol = col + 1
    if nextCol == size:
        nextRow += 1
        nextCol = 0
    # putting -1 first here optimizes for the known solution
    \# -1 is /, 1 is \, 0 is blank cell
    for diagonalType in [1, -1, 0]:
```

```
# zero (blank cell) always works, no need to test
        if diagonalType == 0:
            grid[row][col] = diagonalType
            extend(nextRow, nextCol, remainingDiags)
            if check neighbors(row, col, diagonalType):
                # the diagonal works, put it in
                grid[row][col] = diagonalType
                extend(nextRow, nextCol, remainingDiags - 1)
# setup a grid size X size
size = 5
ct = 0
grid = [[5 for i in range(size)] for j in range(size)]
extend(0, 0, 16)
. . .
Solution: 1
-1 -1 -1 0 1
0 0 -1 0 1
1 1 0 1 1
1 0 -1 0 0
1 0 -1 -1 -1
Solution: 2
-1 0 1 1 1
-1 0 1 0 0
-1 -1 0 -1 -1
0 0 1 0 -1
1 1 1 0 -1
```