

denotational semantics:

<STMT>:

$[[<STMT>]]: \text{Stmt} \rightarrow \text{Env} \rightarrow \text{Env}$

$[[<STMT>]] = [[<IF_STMT>]] \mid [[<BLOCK>]] \mid [[<ASSIGN>]] \mid [[<DECLARE>]] \mid [[<WHILE_LOOP>]]$

<STMT_LIST>:

$[[<STMT_LIST>]]: \text{List}<\text{Stmt}> \rightarrow \text{Env} \rightarrow \text{Env}$

<WHILE_LOOP>:

$[[<WHILE_LOOP>]]: \text{BExpr} \times \text{Stmt} \rightarrow \text{Env} \rightarrow \text{Env}$

$[\text{while } (b) \ S] = \text{if } ([b] = \text{true}) \text{ then } [[S]]([\text{while } (b) \ S]) \text{ else env}$

<IF_STMT>:

$[[<IF_STMT>]]: \text{BExpr} \times \text{Stmt} \times \text{Stmt} \rightarrow \text{Env} \rightarrow \text{Env}$

$[\text{if } (b) \ S1 \text{ else } S2] = \text{if } ([b] = \text{true}) \text{ then } [S1] \text{ else } [S2]$

<BLOCK>:

$[[<BLOCK>]]: \text{List}<\text{Stmt}> \rightarrow \text{Env} \rightarrow \text{Env}$

$\{ \{ \text{SL} \} \} = [<STMT_LIST>]$

<DECLARE>:

$[[<DECLARE>]]: \text{DataType} \times \text{List}<\text{ID}> \rightarrow \text{Env} \rightarrow \text{Env}$

$[\text{DataType ID1, ID2, ...}] = \text{env}[ID1 \leftarrow \text{DefaultValue}(\text{DataType}), ID2 \leftarrow \text{DefaultValue}(\text{DataType}), \dots]$

<ASSIGN>:

$[[<ASSIGN>]]: \text{ID} \times \text{Expr} \rightarrow \text{Env} \rightarrow \text{Env}$

$[ID = E] = \text{env}[ID \leftarrow [E]]$

<EXPR>:

$[[<EXPR>]]: \text{Expr} \rightarrow \text{Env} \rightarrow \text{Value}$

$[E1 + E2] = [E1] + [E2]$

$[E1 - E2] = [E1] - [E2]$

<TERM>:

$[[<TERM>]]: \text{Expr} \rightarrow \text{Env} \rightarrow \text{Value}$

$[E1 * E2] = [E1] * [E2]$

$[E1 / E2] = [E1] / [E2]$

$[E1 \% E2] = [E1] \% [E2]$

<FACT>:

$[[<FACT>]]: \text{Expr} \rightarrow \text{Env} \rightarrow \text{Value}$

$[ID] = \text{env}(ID)$

$[\text{INT_LIT}] = \text{INT_LIT}$

$[\text{FLOAT_LIT}] = \text{FLOAT_LIT}$
 $[(E)] = [E]$

<BOOL_EXPR>:

$[[<\text{BOOL_EXPR}>]]: \text{BExpr} \rightarrow \text{Env} \rightarrow \text{Bool}$

$[E1 > E2] = ([E1] > [E2])$

$[E1 < E2] = ([E1] < [E2])$

$[E1 \geq E2] = ([E1] \geq [E2])$

$[E1 \leq E2] = ([E1] \leq [E2])$

<BTERM>:

$[[<\text{BTERM}>]]: \text{BExpr} \rightarrow \text{Env} \rightarrow \text{Bool}$

$[E1 == E2] = ([E1] == [E2])$

$[E1 != E2] = ([E1] != [E2])$

<BAND>:

$[[<\text{BAND}>]]: \text{BExpr} \rightarrow \text{Env} \rightarrow \text{Bool}$

$[E1 \&\& E2] = ([E1] \&\& [E2])$

<BOR>:

$[[<\text{BOR}>]]: \text{BExpr} \rightarrow \text{Env} \rightarrow \text{Bool}$

$[E1 \parallel E2] = ([E1] \parallel [E2])$