



# Assessing the predictions of a NO<sub>x</sub> kinetic mechanism on recent hydrogen and syngas experimental data



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## ABSTRACT

A detailed chemical kinetic mechanism has been developed to describe the pyrolysis and oxidation of the hydrogen/NO<sub>x</sub> and syngas/NO<sub>x</sub> systems. The thermodynamic data of nitrogenous compounds have been updated based on the study of Bugler et al. (2016). The rate constants of individual elementary reactions associated with the Zeldovich mechanism, the N/O sub-mechanism (NO<sub>2</sub>, N<sub>2</sub>O and NO<sub>3</sub>), the H/N/O sub-mechanism (HNO/HON, HNO<sub>2</sub>/HONO and HONO<sub>2</sub>) and the NH<sub>3</sub> mechanism (NNH and NH<sub>2</sub>OH) have been selected through a synthetic comparison of the data available in the literature and the adoption of the latest available published rate constant data. The proposed mechanism has been validated against a large number of experimental data including pyrolysis histories, ignition delay time data, species profile versus time and temperature and flame speed measurements over a wide range of initial combustion conditions and various experimental devices including shock tubes, flow reactors, jet-stirred reactors and spherical combustion bombs.

The simulations of the proposed model have also been compared to those from five recently published kinetic models available in the literature. It was found that although these mechanisms generally reproduced well the data for which they were validated, they did not globally capture the combustion characteristics of all of the hydrogen/NO<sub>x</sub> and syngas/NO<sub>x</sub> systems.

Finally, the proposed model has been used to simulate the formation of NO at practical gas-turbine relevant conditions. A detailed flux analysis has been performed to kinetically explore the NO formation mechanism under various combustion conditions.

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## 1. Introduction

Worldwide interest in emissions from gas turbine and internal combustion engines and the enactment of legislation to limit emissions has resulted in the need to understand the effect of exhaust emission control methods on engine performance [1]. Nitrogen oxides (NO<sub>x</sub>), essentially the sum of nitric oxide (NO), nitrogen dioxide (NO<sub>2</sub>) and nitrous oxide (N<sub>2</sub>O), originate primarily from the oxidation of molecular nitrogen by the oxygen present in fuel/air mixtures at high temperatures ( $T > 2100$  K). This is the so-called Zeldovich/Thermal NO<sub>x</sub> mechanism. It is well known that in a diffusion flame combustor, the primary way to control thermal NO<sub>x</sub> formation is to reduce the flame temperature in the combustor. To this end, over the past number of years, a large num-

ber of combustion technologies [2–7] have emerged to limit NO<sub>x</sub> production during combustion. Nevertheless, it remains difficult to limit thermal NO<sub>x</sub> formation to a zero level due to the presence of air in the reactant mixtures. Previous work suggests that even small amounts of nitrogen species can have a dramatic impact on fuel oxidation and combustion at low to high temperatures [8–12]. This effect is more noticeable in supersonic combustion tests where vitiated air streams are doped with NO<sub>x</sub> species and can be introduced into the reaction chamber. Therefore, an advanced combustor design not only requires an understanding of the NO<sub>x</sub> formation mechanisms, but also the exploration of the chemical interaction between the fuel and NO<sub>x</sub>. For a hydrocarbon flame however, the interaction is reflected in part in Fenimore's prompt NO route via the reaction sequence  $\text{CH} + \text{N}_2 = \text{NCN} + \text{H}$  and  $\text{NCN} + \text{H}/\text{O}/\text{OH}/\text{O}_2 = \text{NO} + \text{CN}/\text{HCN}/\text{NCO}$  [13,14]. Ahmed et al. [15] indicated that a different subset of any available hydrocarbon mechanism can induce an obvious difference in the description of CH chemistry, leading to a significant effect on NO<sub>x</sub>

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formation through Fenimore's prompt mechanism. They also confirmed that for hydrogen and syngas combustion considerable uncertainty still remained in model predictions of both  $\text{NO}_x$  formation and the kinetic interaction between the fuel and  $\text{NO}_x$  species. It would appear that researchers have not come to a consensus with respect to a quantitative description of the interaction of  $\text{NO}_x$  with the free radical pool established, even by simple fuels such as hydrogen and syngas. In order to simplify the complexity of the reaction system, we have chosen the hydrogen/syngas/ $\text{NO}_x$  system as the target to omit the prompt-NO mechanism from the analysis enabling us to isolate and better expound the relative importance of the various  $\text{NO}_x$  formation routes such as the Zeldovich NO, the nitrous-oxide, the nitrous oxide and the NNH mechanism.

To investigate these processes at a more fundamental level, a number of studies involving the pyrolysis of  $\text{N}_2\text{O}$  and the oxidation of hydrogen/ $\text{NO}_x$  and syngas/ $\text{NO}_x$  have been performed in shock tubes [8,16–27], jet-stirred reactors (JSR) [28–30], flow reactors (FR) [9,10,31,32] and spherical expanding laminar flames [33,34]. Simultaneously, many relative kinetic mechanisms [9,10,13,28,32,35–43] have also been proposed to improve our understanding of  $\text{NO}_x$  formation and to develop  $\text{NO}_x$  control strategies. A very good review of nitrogen combustion chemistry before 1989 was carried out by Miller and Bowman [44] and only a brief summary based on recent publications is presented herein.

Glarborg et al. [32] conducted an experimental and theoretical work of impact of  $\text{NO}_x$  on moist CO oxidation under post-flame conditions ( $p = 1.05$  atm,  $T = 800 - 1400$  K,  $x_{\text{NO}} = 0 - 1\%$ , and  $x_{\text{NO}_2} = 0 - 622$  ppm). The concentrations of the major species including CO,  $\text{CO}_2$ , NO and  $\text{NO}_2$  were measured and used for model development. The rate constants for the  $\text{NO}_x$  subset were mainly adopted from the recommendations of Tsang and Herron [38] and updated portions of rate constants using literature recommendations, mainly including radical recombination reactions, NO formation recycled by reactions of HNO,  $\text{NO}_2$ , HONO and  $\text{NO}_3$  with chain carriers. The model showed a general good agreement with the data. Glarborg et al. [32] pointed out that the presence of NO and  $\text{NO}_2$  significantly affects CO consumption. In particular, NO represented a two-fold impact with respect to CO oxidation at lower temperatures through 1) enhancing CO consumption by converting  $\text{HO}_2$  radicals into OH radicals via the reaction  $\text{NO} + \text{HO}_2 = \text{NO}_2 + \text{OH}$  at low NO concentrations and 2) inhibiting CO consumption by catalyzing chain-carrier recombination via  $\text{OH}/\text{H}/\text{O} + \text{NO} (+\text{M}) = \text{HONO}/\text{HNO}/\text{NO}_2 (+\text{M})$ . In contrast,  $\text{NO}_2$  was observed to be more efficient in scavenging reactive radicals. However, in the shock tube measurements, the experimental observations showed the opposite effect of  $\text{NO}_2$  with either hydrogen [8] or a hydrocarbon fuel [45], because of the higher temperatures ( $>1400$  K) relative to the flow reactor experiments (600–1400 K).

To further supplement early atmospheric-pressure flow reactor studies [32,46,47], Mueller et al. [10] conducted an experimental and modeling study of  $\text{H}_2/\text{O}_2$  and  $\text{CO}/\text{H}_2\text{O}/\text{O}_2$  reaction kinetics in the presence of trace quantities of NO and  $\text{NO}_2$  at conditions relevant to auto-ignition and post-combustion expansion processes ( $p = 0.5 - 14$  atm,  $T = 750 - 1100$  K,  $\varphi = 0.25 - 1.0$ ,  $x_{\text{NO}} = 12 - 532$  ppm, and  $x_{\text{NO}_2} = 85$  ppm). This work confirmed the experimental observations of Glarborg et al. [32] and also clarified the fact that the effect of the addition of NO on fuel oxidation and NO to  $\text{NO}_2$  conversion not only depends strongly on NO concentration but also depends on pressure and on equivalence ratio. The inter-conversion of NO with  $\text{NO}_2$  can consume  $\text{H}_2$  and CO at much lower temperatures relative to that which occurs in the absence of  $\text{NO}_x$  species. The measurements of the concentrations of  $\text{H}_2$ , CO,  $\text{O}_2$ ,  $\text{H}_2\text{O}$ ,  $\text{CO}_2$ , NO,  $\text{NO}_2$ , HONO and temperature were used to develop a detail kinetic mechanism which was capable of reproducing their experimental measurements.

Konnov et al. [48,49] constructed a detail H/N/O mechanism to computationally investigate the NO production rate for fuel-lean, stoichiometric and fuel-rich hydrogen/air reaction systems in well-stirred reactors over a temperature range of 1500–2200 K. They clarified the validity of steady-state assumptions used in the development of explicit expressions used to predict the instantaneous NO formation rate in a hydrogen flame at residence times of 1–25 ms. Furthermore, Konnov et al. identified a possible new route to NO formation in fuel-rich hydrogen combustion via a sequence of reactions relating to  $\text{N}_2\text{H}_3$  radicals, and also emphasized the importance of NNH chemistry to form NO that was first proposed by Bozzelli and Dean [50]. Subsequently, Konnov [13] released a revised model with an update of an additional implementation of kinetic pathways to prompt-NO formation via NCN chemistry.

Dayma and Dagaut [28] explored the oxidation of a diluted hydrogen system perturbed with various concentrations of NO and  $\text{NO}_2$  at typical JSR conditions ( $p = 1.0 - 10$  atm,  $T = 700 - 1150$  K,  $\varphi = 0.1 - 2.5$ ,  $x_{\text{NO}} = 220 - 250$  ppm, and  $x_{\text{NO}_2} = 65 - 70$  ppm). They proposed a detailed kinetic model to interpret their experimental data and indicated that the mutual sensitization effect of NO and/or  $\text{NO}_2$  on hydrogen oxidation can be attributed to 1) the conversion of unreactive  $\text{HO}_2$  radicals into reactive OH radicals via the reaction  $\text{NO} + \text{HO}_2 = \text{NO}_2 + \text{OH}$  which promotes hydrogen oxidation via  $\text{H}_2 + \text{OH} = \text{H}_2\text{O} + \text{H}$ , and 2) the recycled generation of NO via  $\text{NO}_2 + \text{H} = \text{NO} + \text{OH}$  together with the release of OH radicals. Moreover, the sensitization of relative importance reflected by these reactions presented a different pressure dependence in the range 1–10 atm. Unfortunately, the Dayma and Dagaut model disagreement significantly with the ignition delay times of  $\text{H}_2/\text{O}_2/\text{NO}_2$  reported by Slack and Grillo [51].

Rasmussen et al. [9] conducted a well-defined experimental investigation of homogeneous  $\text{CO}/\text{H}_2/\text{O}_2/\text{NO}_x$  mixtures in a high-pressure laminar flow reactor at the following conditions:  $p = 20 - 100$  atm,  $T = 600 - 900$  K,  $\varphi = 0.063$ ,  $x_{\text{NO}}/x_{\text{NO}_2} = 36/113$  ppm, 125/26 ppm and 145/6 ppm corresponding to 20, 50 and 100 atm, respectively. The concentrations of major species, CO,  $\text{CO}_2$ ,  $\text{O}_2$ , NO and  $\text{NO}_2$ , were recorded. Furthermore, a detailed kinetic model was proposed with updated rate constants and thermodynamic properties using either *ab initio* CBS-QBS calculations or new literature recommendations. The model reproduced the species histories for  $\text{H}_2/\text{CO}/\text{O}_2/\text{NO}_x$  oxidation at high pressures pretty well, and was in reasonable agreement with literature flow reactor data, but trended to over-predict the reactivity of syngas ignition.

Mathieu et al. [8,18] assessed the validity of both the  $\text{H}_2/\text{O}_2$  chemistry and  $\text{NO}_x$  sub-mechanisms incorporated respectively in the literature models [9,13,28] against their own measured ignition delay times. The simulations showed that, although these models were in part in reasonable agreement with the new data for the  $\text{H}_2/\text{O}_2/\text{NO}_x$  system, none of them could reproduce correctly the ignition trend for the neat  $\text{H}_2/\text{O}_2$  system. Ahmed et al. [15] and Watson et al. [52] found that the discrepancy of the  $\text{NO}_x$  subset was particularly more important in predicting species evolution at high-pressure flow reactor conditions.

Considering the shortcomings of the mechanisms [9] used by Mathieu et al. [8,18] to simulate their pure  $\text{H}_2/\text{O}_2$  system, most recently Ahmed et al. [15] proposed a detailed mechanism to describe  $\text{H}_2/\text{CO}/\text{NO}_x$  oxidation. They integrated the literature  $\text{NO}_x$  reaction schemes [9,13,28,49,53] with the  $\text{H}_2/\text{O}_2$  reaction scheme published by Burke et al. [54]. They also updated several of the rate constants for reactions recommended by Klippenstein et al. [39] relating to the  $\text{NH}_2$ , HNO and  $\text{NH}_2\text{OH}$  species. The assembled model generally showed a reasonable agreement with recent experimental data measured in various facilities including a shock tube, a FR and a JSR over a wide range of conditions. Nevertheless, the model still over-predicted the ignition delay times reported by Mathieu et al. [8] even considering H atom impurity condensa-

tion, especially more notably at high pressures and high  $\text{NO}_2$  levels. We have therefore re-evaluated the Burke et al. [54] model against recent data measured by Hashemi et al. [55] in a high-pressure FR for neat  $\text{H}_2/\text{O}_2/\text{N}_2$  mixtures. Results show that the Burke et al. model presents slow  $\text{H}_2$  consumption at 800–900 K, and the deviation tends to be more dramatic transitioning from fuel-rich to fuel-lean mixtures, see Fig. S1 of the Supplementary material.

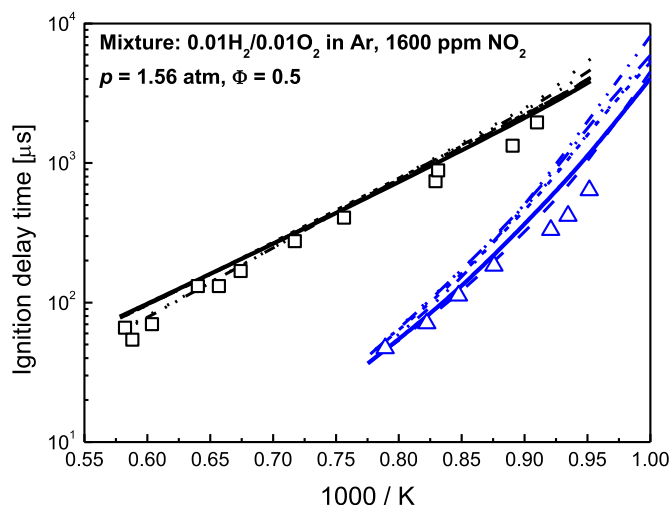
Extensive kinetic modeling studies have been carried out for hydrogen/ $\text{NO}_x$  and syngas/ $\text{NO}_x$  combustion. Such studies however, have not systematically addressed the combined effects of all of the reactions. In fact, each individually recommended rate constant and species thermochemistry have an associated uncertainty, which can propagate through the complete model and can eventually produce an undesirable simulation result [56]. With this in mind, the aim of *this study* is 1) to evaluate the effect of important reactions on the kinetic interaction of the hydrogen/syngas sub-mechanism with the  $\text{NO}_x$  subset at different physical operating conditions (ambient temperature, ambient pressure, equivalence ratio, and concentrations of  $\text{NO}_x$ ); 2) to develop a mechanism with significant updates based on recent thermodynamic and kinetic data. The aim is to produce a model capable of reproducing the combustion characteristics of both neat hydrogen/syngas and hydrogen/syngas/ $\text{NO}_x$  systems over a wide range of experimental targets and conditions measured using shock tube pyrolysis data, ignition delay times, JSR species profiles, laminar and turbulent FR speciation data and flame speeds; and 3) to attempt to provide a promising strategy controlling NO formation through a preliminary kinetic exploration of NO at practical gas-turbine conditions. We expect that the model can be predictive in nature with the ultimate goal of advancing the design and optimization of practical fuel-flexibility engine systems to control  $\text{NO}_x$  formation.

## 2. Mechanism development

### 2.1. Thermochemistry

As mentioned above, erroneous or inconsistent use of both chemical kinetic and thermochemical data may result in a series of compensating errors which may result in an eventual good prediction of a limited number of targets. To avoid possible uncertainties stemming from thermochemistry, an accurate and consistent set of thermodynamic data is certainly necessary. In *this study*, thermodynamic data for hydrogen, carbon monoxide and related radicals are adopted from the NUI Galway hydrogen/syngas mechanism [57]. Moreover, thermodynamic data of nitrogen-containing compounds are taken from the recent work of Bugler et al. [58], where a new gas-phase thermochemistry database was calculated using high-level *ab initio* calculations for 60 nitrogenous compounds that exist in practical combustion environments. Three quantum-chemical compound methods (CBS-APNO, G3 and G4) were used to derive heats of formation, while the B3LYP/cc-pVTZ level of theory was used to calculate entropies and heat capacities. Simulated results showed that the thermochemistry database presented a decrease of 10% and 20% in NO and  $\text{N}_2\text{O}$  concentrations, respectively, and an increase of 20% in the concentration of  $\text{NO}_2$  compared to literature data. However, Bugler et al. reported the deviation archives to be approximately a factor of three for some important intermediates such as HONO and  $\text{HNO}_2$ .

As we mentioned above, the coupled nature of the kinetics and the thermochemistry can impact on modeling results. To clarify the effect of thermochemistry, we have combined our current kinetic model with the thermochemical parameters from difference sources (Ahmed\_2016 [15], Konnov\_2009 [13], SJK/PG\_2015 [31, 39], Mével\_2009 [19], and Dagaut\_2008 [59]), to simulate com-



**Fig. 1.** Effect of choice of thermochemistry on ignition delay time simulations at typical shock tube conditions. Symbols represent Mathieu et al. [8] measurements. Lines denote model simulations with the current model (solid line), Ahmed\_2016 [15] (dash line), Konnov\_2009 [13] (dot line), SJK/PG\_2015 [31,39] (dash dot line), Mével\_2009 [19] (dash dot dot line) and Dagaut\_2008 [59] (short dash line).

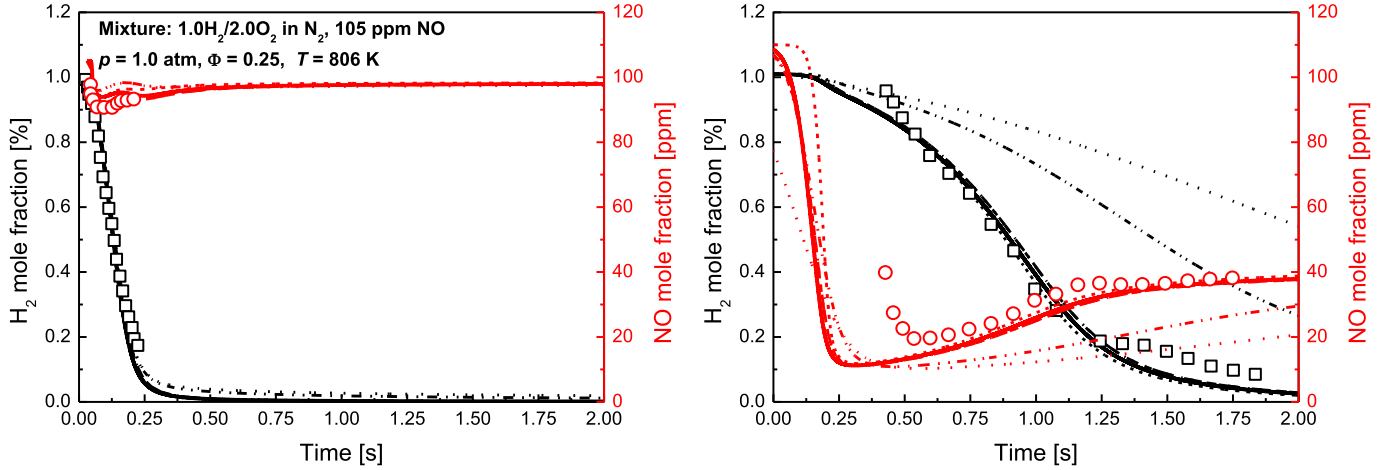
mon targets including ignition delay times (Fig. 1), FR speciation (Fig. 2), and JSR species concentrations (Fig. 3).

For ignition delay times the impact of thermochemistry is generally limited at low pressures, Fig. 1. At high pressures, however, the effect becomes more prominent, particularly at lower temperatures ( $< 1150$  K). The simulations using the Ahmed et al. thermochemistry are consistent with those predicted by our model and both are in excellent agreement with the experiments. In contrast, the other three are similar to the data but slightly over-predict the ignition delay times.

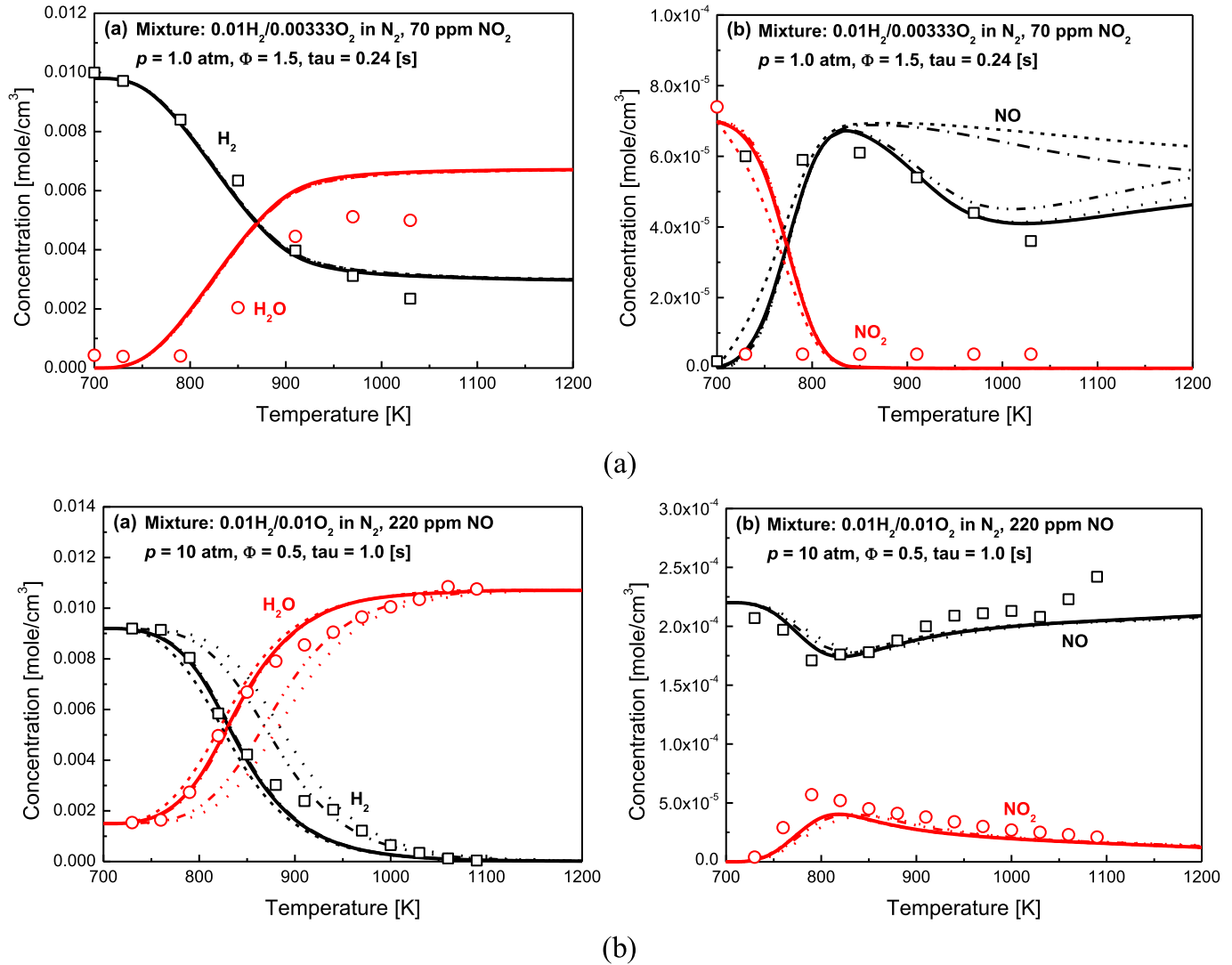
For FR species versus time prediction, likewise, the thermochemistry has a limited impact at low pressures but it is significant at higher pressures, Fig. 2. Specifically, the thermochemistry in current model, Ahmed\_2016, SJK/PG\_2015 and Dagaut\_2008 show almost the same predictions of the concentrations of the major species, and they are also in very good agreement with the Mueller et al. measurements. [10]. The thermochemistry from Konnov\_2009 and Mével\_2009 present an obvious deviation, particularly at late stages of oxidation ( $> 0.5$  s) where these two data sets lead to a slow prediction of the consumption of the fuel and formation of NO relative to the experiments.

In contrast, the effect of thermochemistry is fairly remarkable in the prediction of hydrogen/ $\text{NO}_x$  oxidation in a JSR, even at low pressure. At 1.0 atm, Fig. 3(a), the difference in thermochemistry has a negligible effect on the evolutions of both the hydrogen and water profiles but has a dramatic effect on NO to  $\text{NO}_2$  conversion. It is clear that the thermochemistry from Dagaut\_2009 and SJK/PG did not improve NO formation at higher temperatures ( $> 850$  K), while the other sets are in good agreement with the measurements [28]. At high pressures (10 atm), the conversion of NO to  $\text{NO}_2$  is reproduced well by all data sets for all conditions whereas using the data of Konnov\_2009 and Mével\_2009 result in slow predictions in H atom conversion from hydrogen to water at 800–1100 K, Fig. 3(b).

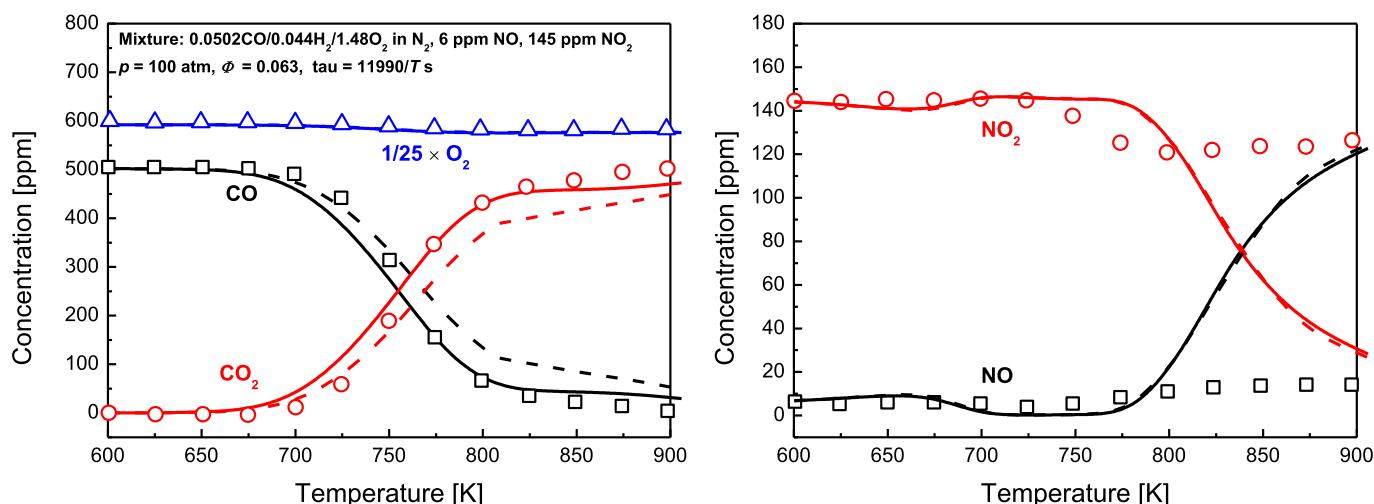
It is clear that the choice of thermochemistry does effect model simulations and that different sources result in different simulated results for commonly validated targets. Overall, simulations using the thermochemistry adopted here are in good agreement with that using the data from Ahmed et al. [15] and the experimental measurements as well.



**Fig. 2.** Effect of thermochemistry on simulating the oxidation of hydrogen/NO<sub>x</sub> at typical flow reactor conditions. Symbols represent Mueller et al. [10] measurements. Lines denote model simulations with the current model (solid line), Ahmed\_2016 [15] (dash line), Konnov\_2009 [13] (dot line), SJK/PG\_2015 [31,39] (dash dot line), Mével\_2009 [19] (dash dot dot line) and Dagaut\_2008 [59] (short dash line).



**Fig. 3.** Effect of thermochemistry on simulating oxidation of hydrogen/NO<sub>x</sub> at typical JSR conditions. Symbols represent Dayma and Dagaut experiments [28]. Lines denote model simulations with the current model (solid line), Ahmed\_2016 [15] (dash line), Konnov\_2009 [13] (dot line), SJK/PG\_2015 [31,39] (dash dot line), Mével\_2009 [19] (dash dot dot line) and Dagaut\_2008 [59] (short dash line). (a) Low pressure (1.0 atm); (b) high pressure (10 atm).



**Fig. 4.** Effect of HO•O chemistry on CO to CO<sub>2</sub> conversion in the H<sub>2</sub>/CO/O<sub>2</sub>/NO<sub>x</sub> reaction system at high pressures. Symbols represent flow reactor experimental measurements [9]; lines denote model predictions with HO•O chemistry (solid line) and without HO•O chemistry (dash line) at isothermal assumption.

## 2.2. Kinetic reaction mechanism

The proposed kinetic mechanism of hydrogen/NO<sub>x</sub> and syngas/NO<sub>x</sub> is developed upon the mechanism of hydrogen and syngas to hierarchically incorporate the sub-sets such as the Zeldovich mechanism, the N/O and H/N/O schemes and an NH<sub>3</sub> sub-mechanism, which are important to describe NO<sub>x</sub> formation and its interaction with hydrogen and syngas. The complete kinetic mechanism is available as Supplementary material.

### 2.2.1. H<sub>2</sub>/syngas sub-mechanism

Similar to the selection of thermochemistry data, the sub-mechanism of H<sub>2</sub>/CO is adopted from the work of Kéromnès et al. [57] with updates of several critical reactions based on recent experimental and theoretical data. This model has been validated widely using ignition delay times measured in both shock tubes and rapid compression machines, speciation data in both JSRs and FRs, laminar flame speeds, and mass burning rates.

### 2.2.2. HO•O radical chemistry

Due to the consideration of HO•O chemistry in terms of the kinetic importance of the conversion of CO to CO<sub>2</sub> in combustion environments, HO•O related reactions were added in the Kéromnès H<sub>2</sub>/CO/O<sub>2</sub> mechanism. Recently, Barker's group [60,61] applied *ab initio* Semi-Classical Transition State Theory (SCTST) to calculate the limiting low- and high-pressure rate coefficients for HO•O unimolecular dissociation reactions. The thermal rate constants calculated were in reasonable agreement with literature experimental data, and have been adopted in the current model.

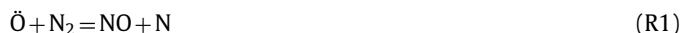
For bimolecular reactions of HO•O, Yu et al. conducted a series of quantum chemical calculations using an *ab initio* direct dynamics method for the reactions of HO•O + O<sub>2</sub> [62], HO•O + OH [63], HO•O + H [64], HO•O + O [65], HO•O + HO<sub>2</sub> [66] and HO•O + CH<sub>3</sub> [67]. For consistency, all of the rate constants of HO•O with free radicals are taken from Yu et al., including those provided in their recent review [68]. Moreover, the reactions of HO•O + NO/NO<sub>2</sub> are adopted from the theoretical calculations of Poggi et al. [69,70].

Figure 4 shows the effect of HO•O chemistry on the conversion of CO to CO<sub>2</sub> in the H<sub>2</sub>/CO/NO<sub>x</sub> reaction system at high pressures. Clearly, the new HO•O reaction pathways promote the conversion of CO to CO<sub>2</sub> at temperatures above 700 K, whereas there is a negligible effect on NO<sub>x</sub> formation. In fact, the conversion of NO to NO<sub>2</sub> at these conditions is most sensitive to the reactions:

NO + O (+M) = NO<sub>2</sub> (+M) and NO + O<sub>2</sub> = NO<sub>2</sub> + O, but it is not influenced by the HO•O chemistry. Note that the promoting effect of HO•O chemistry appears to be only important at high pressure ( $p > 50$  atm), while it is much more limited at lower pressures ( $p < 20$  atm).

### 2.2.3. Zeldovich mechanism

Thermal NO<sub>x</sub> is an important source of NO formation in combustors at high temperatures. The kinetic formation process has been well characterized in the Zeldovich mechanism [71] namely:



Due to the importance of the rate-limiting step, R1, Baulch et al. [72] reviewed the measurements of the rate constant of R1, and recommended a temperature-independent value of  $k_1$  of  $2.1 \times 10^{13} \text{ cm}^3 \text{ mol}^{-1} \text{ s}^{-1}$  and this rate constant has been widely used in most NO<sub>x</sub> kinetic mechanisms [9,13,15,29,39,53,73]. Nevertheless, the recent experiments reported by Abian et al. [31] indicated that adopting the rate constant recommended by Baulch et al. leads to an under-prediction of thermal NO formation, especially in the presence of high concentrations of O<sub>2</sub>. In contrast, using the Abian et al. rate constant shows excellent agreement with their own experimental data as well as with the literature data [17]. Therefore, we have adopted the recommendation of Abian et al. [31] to describe R1. Moreover, the rate constant of R2 is taken from Baulch et al. [36] since it is in excellent agreement with experimental literature data [74–77], while the rate constant of R3 is taken from the recommendation of Miller et al. [44,78], which is consistent with the direct measurement of Howard and Smith [79].

### 2.2.4. N/O sub-mechanism

Overall, the N/O sub-mechanism consists of four chemical species, namely nitric oxide (NO), nitrogen dioxide (NO<sub>2</sub>), nitrous oxide (N<sub>2</sub>O) and nitrogen trioxide (NO<sub>3</sub>). Owing to fact that NO acts to either eliminate free radicals to form stable species via recombination reactions, or it acts as a chain carrier, participating in other reactions of nitrogenous compounds. The NO scheme will be thus discussed along with above the four N/O schemes.

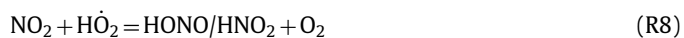


*NO<sub>2</sub> scheme:* NO<sub>2</sub> is initially formed via the recombination reaction between NO and  $\dot{\text{O}}$  atom,

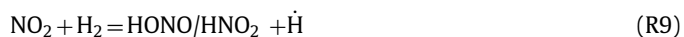


The rate constant of R4 is taken from the recommendation by Tsang and Herron [38]. The low- and high-pressure limits of R4 were derived, and were shown to be in good agreement with measurements. Third body collision efficiencies are adopted from Baulch et al. [72]. Considering the impact of the low pressure limit (LPL) on the consumption of CO under flow reactor conditions, we have increased the A-factor of the LPL by a factor of two which is within the uncertainty of a factor of three suggested by Tsang and Herron to better reproduce the CO species consumption profiles measured in a flow reactor.

NO<sub>2</sub> is mainly formed/consumed by reacting with either free radicals:



or with fuels, namely H<sub>2</sub> and CO in the current work.



The importance of R5 and R-7 with respect to inter-conversion of NO to NO<sub>2</sub> and accumulation of  $\dot{\text{OH}}$  radicals was identified in many reaction systems [8–10,28,45]. In this study, we have adopted the rate constants of R5 measured directly by Ko and Fontijn [80] which is close to the Baulch et al. [72] recommendation within an uncertainty by a factor of two. In order to accurately predict the species data from Mueller et al. [10] we have made a small (20%) adjustment in this rate constant which is well within the uncertainty limit mentioned above. The rate constant of R-7 is taken from Baulch et al. [72] evaluation based largely on experimental sets, and it is generally in good agreement with Howard [81] measurement and Tsang and Herron [38] recommendation. The rate constant of R6 is adopted from Tsang and Herron [38] recommendation due to its consistency with the experimental measurements [82–85] and high-level quantum chemistry calculation [86]. Glarborg et al. [87] in their study of the interaction of formaldehyde with NO<sub>x</sub> found that R8 can compete with the reaction of  $\dot{\text{H}}\text{O}_2 + \dot{\text{H}}\text{O}_2 = \text{H}_2\text{O}_2 + \text{O}_2$  and R-7 for  $\dot{\text{H}}\text{O}_2$  radicals, limiting the concentration of NO<sub>2</sub>. Rasmussen et al. [9] performed an *ab initio* study at the CBS-QB3 level of theory and clarified that the channel forming HNO<sub>2</sub> + O<sub>2</sub> dominates at typical combustion conditions. Here, we have adopted the rate constant of Rasmussen et al. [9] for R8. As proposed by Mathieu et al. [8], R9 plays a role in their brute force sensitivity analysis. However, previous modeling studies [10,13,29] rarely distinguish the HNO<sub>2</sub> isomer (*cis*-HONO, *trans*-HONO and HNO<sub>2</sub>) as the products of R9. Considering the lack of consensus regarding the rate constants for the channel forming the HNO<sub>2</sub> isomers, Chai and Goldsmith [40] conducted a high-accuracy electronic structure calculation on the rate constants. Their results show that, although *trans*-HONO represents the most stable state, the dominant product is *cis*-HONO, followed by HNO<sub>2</sub>. The total rate of R8 calculated by Chai and Goldsmith is in excellent agreement with that reported both in the Park et al. [88] measurement and the Rasmussen et al. [9] calculation,

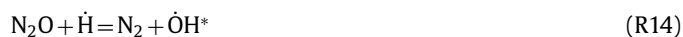
but it is an order of magnitude lower than the Tsang and Herron [38] recommendation. Here, we use the Chai and Goldsmith [40] calculations for R9. Fortunately, there appears to be little or no disagreement in the literature [38,89,90] in the recommended rate constant of R10. We have assigned the Tsang and Herron [38] recommendation for this reaction.

*N<sub>2</sub>O scheme:* The N<sub>2</sub>O mechanism can be important in high pressure flames or under fuel-lean conditions at low temperatures. Indeed, N<sub>2</sub>O is primarily formed via the recombination reaction of molecular nitrogen with  $\dot{\text{O}}$  atoms (R11), while its decomposition can also play a role in the release of active  $\dot{\text{O}}$  atoms at low pressures.



Mathieu et al. [18] indicated that an increase in reactivity can be attributed to the additional  $\dot{\text{O}}$  atoms released via R-11, as the  $\dot{\text{O}}$  atoms produced are free to undergo chain branching through the reaction of  $\text{H}_2 + \dot{\text{O}} = \dot{\text{H}} + \dot{\text{OH}}$ . Javoy et al. [20] experimentally determined the LPL of R-11 with an overall uncertainty of less than 18%. Their result are in good agreement with both the experimental measurements [91–93] and with the theoretical determination [94]. Moreover, Javoy et al. [20] adopted the high pressure limit (HPL) rate constant from Zuev and Starikovskii [95] for R-11 as the activation energy was consistent with the calculation of Chang and Yarkon [94]. Here, we select the Javoy et al. recommended expression in our model since the rate constant leads to a better prediction in both N<sub>2</sub>O decomposition and ignition delay time measurements. The third body efficiencies of the R-11 are taken from Konnov [13].

In a similar manner to the NO<sub>2</sub> scheme discussed above, N<sub>2</sub>O is also mainly consumed by free radical attack via the following sequence of reactions:



Using both sensitivity and flux analyses the reaction of N<sub>2</sub>O with  $\dot{\text{H}}$  atoms (R12) has been highlighted as the primary reaction channel in predicting laminar flame speed and energy release predictions in H<sub>2</sub>/N<sub>2</sub>O flames [33] and is the second most important reaction for ignition delay time predictions [96]. Marshall et al. [97] and Baulch et al. [72] determined the rate constant for R12 with a non-typical Arrhenius dependence with temperature. However, a more recent study of Klippenstein et al. [39] did not support the hypothesis that the change in activation energy in the low-temperature Arrhenius plot is due to a tunneling effect through an Eckart potential barrier as suggested by Marshall et al. [97], but is instead due to stabilization in the potential energy wells of *cis*- and *trans*-HONO. Together, they found that the reactions of R12 and R13 are to be essentially pressure-independent, at least up to

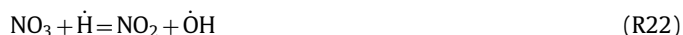
1 atm. In fact all of the aforementioned studies [39,72,97] are in relatively close agreement. In *this study*, we have adopted the most recent calculations from Klippenstein et al. [39] to describe R12 and R-13. Considering the effect of excited hydroxyl radicals ( $\text{OH}^*$ ) on the simulation of  $\text{N}_2\text{O}$  ignition times suggested by Mével et al. [96] and Mathieu et al. [18], we take the rate constant of R14 from the measurement of Hidaka et al. [24] which is in good agreement with the formation of  $\text{OH}^*$  measured in their  $\text{N}_2\text{O}/\text{H}_2$  system in the temperature range 1400–2000 K. Dean and Bozzelli [98] reviewed literature data [38,44,91,93,99] and found that most experiments were in good agreement for the rate constant of R16 whereas there was a considerable discrepancy in the rate constant for R15. In order to provide reliable information to interpret the deviations for R15 present in most of the previous studies, Meagher and Anderson [100] critically evaluated these literature data using detailed chemical modeling in terms of the product channels and confirmed the reliability of the rate constant of R15 measured by Davidson et al. [99]. Together, Meagher and Anderson also proposed a rate constants for R16 through combining the literature data with their direct measurements [101]. In this model, we have selected the rate constants resulting from the intensive study of Meagher and Anderson [100] and are also recommended by Baulch et al. [72] for R15 and R16. Moreover, Mebel et al. [102] calculations using TST and RRKM theories are adopted for R17–R19, while Kosarev et al. estimation is chosen to for R20.

**$\text{NO}_3$  scheme:**  $\text{NO}_3$  is initially formed by the recombination of  $\text{NO}_2$  with  $\dot{\text{O}}$  atoms via the following reaction:



Clearly, R21 competes with R6 for  $\dot{\text{O}}$  atoms, such that the ratio of the rate constants for R6 and R21 is important in determining the formation and consumption of  $\text{NO}_2$ . As mentioned by Hahn et al. [103], the reaction R21 may involve the same intermediate, similar to  $\text{HO}_2$  radicals in the reactions  $\dot{\text{H}} + \text{O}_2 = \dot{\text{O}} + \dot{\text{O}}\text{H}$  and  $\dot{\text{H}} + \text{O}_2 (+\text{M}) = \text{HO}_2 (+\text{M})$ . Hahn et al. measured the absolute rate for the sum of R6 and R21 over a wide range of pressure (1–900 bar). Meanwhile, they also theoretically calculated the HPL for R21 based on the Harding et al. [104] trajectory calculation approach, and the results are in agreement with the experimental data within a factor of two. Considering the fact that a small uncertainty in the rate constant of R6 can result in a large uncertainty in the LPL of R21, we use the rate constants determined by Hahn et al. [103] for R21 in order to be internally consistent because the same rate constant for R6 were used in our model and in that of Hahn et al.

Unlike  $\text{NO}_2$  and  $\text{N}_2\text{O}$ ,  $\text{NO}_3$  mainly undergoes O-atom abstraction by free radicals via the following reaction sequence to convert to  $\text{NO}_2$ .



Reactions 22–24 presented above do not appear to be important at combustion conditions and their rate constants have been adopted from the recommendations of Atkinson et al. [105] and Becker et al. [106] in this model.

### 2.2.5. H/N/O sub-mechanism

The H/N/O sub-mechanism essentially consists of five chemical species, namely nitroxyl (HNO), HON, nitrous acid isomers ( $\text{HONO}/\text{HNO}_2$ ), and nitric acid isomers ( $\text{HONO}_2$ ).

**HNO scheme:** The closed-shell species HNO plays a role in the conversion of reactive nitrogen, particularly for non-hydrocarbon

fuels such as CO and  $\text{H}_2$ , by reducing NO due to an important route from NO to nitrogen through the amine radical pool [107]. As mentioned above, NO can promote fuel oxidation by converting stable  $\text{HO}_2$  radicals into active  $\dot{\text{O}}\text{H}$  radicals via R-7. However, NO can also inhibit fuel oxidation through a catalyzing recombination process, followed by the removal of free radicals via the following reaction sequence:



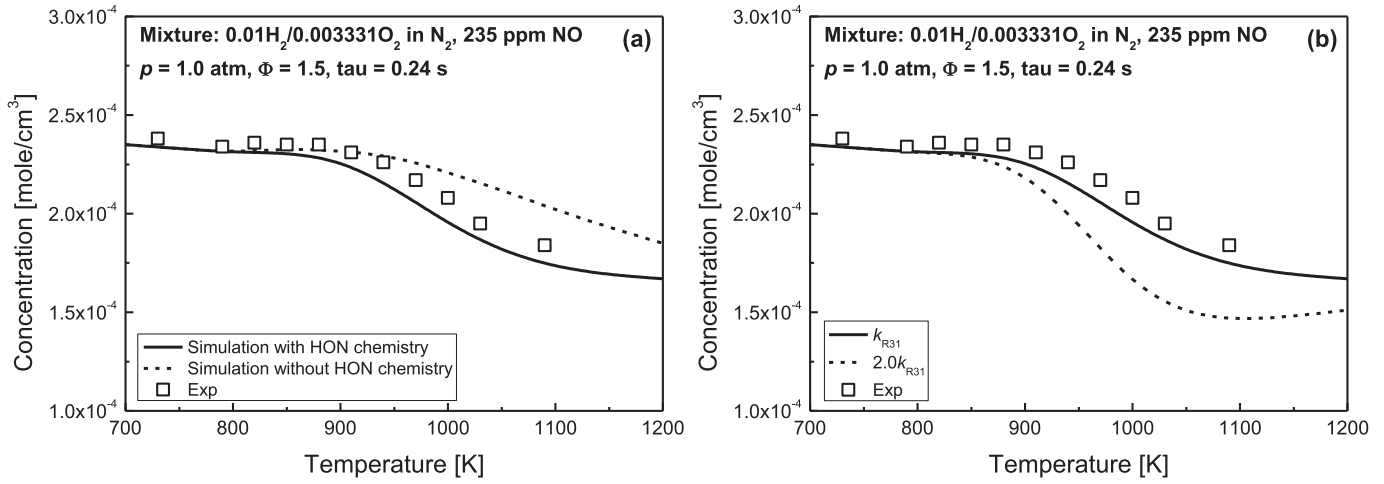
Overall, the HPL of R25 recommended by Tsang and Herron [107] is widely accepted and used in most combustion mechanisms. However, a large uncertainty remains in the LPL of R25. For instance, Allen et al. [108] estimated the LPL against their turbulent flow reactor experiments. It is three times lower than the recommendation of Tsang and Herron [38] but is in satisfactory agreement with the Glarborg et al. [107] experiments. Riley et al. [109] recently measured the rate constant of R25 with Ar as the collider. Their result generally confirmed the values derived by Allen et al. and Glarborg et al. We have therefore selected the recommendation of Tsang and Herron for the HPL, and the values of Glarborg et al. and Allen et al. for the LPL. The third body collision efficiencies are taken from Konnov's [13] estimation.

Soto and Page [110] calculated the potential energy surface (PES) for H-atom abstraction via reaction R26 at two levels of theory, multi-configurational self-consistent-field and configuration interaction involving all single and double substitutions. At 1000 K their calculated rate constant is 4.3 times faster than that recommended by Tsang and Herron [38]. Recently, Nguyen et al. [111] recalculated the rate constants for abstraction not only by  $\dot{\text{H}}$  atoms but also by  $\dot{\text{O}}$  atoms at temperatures of 200–2500 K. Their results confirmed Soto et al.'s calculation but they are considerably higher than the value recommended by Tsang and Herron. Compared to R26, H-atom abstraction via reaction R28 is a barrier-less reaction. Similarly, the rate constants determined by Nguyen et al. [111] are much lower than the recommendation of Tsang and Herron, and are within a factor of 1.6 of those calculated by Soto et al. [112]. We have used the values of Soto et al. to describe R26 and R28, and this is consistent with the literature models [9,10,13,15,39]. Moreover, the indirect measurement of Inomate et al. [113] is selected for R27. Similar to the study by Chain et al. [40], Mebel et al. [114] found that despite the fact that *trans*-HONO is the more stable species, the dominant products are *cis*-HONO + NO via R29 due to the lower energy barrier. In *this work*, we have adopted the expression calculated by Mebel et al. for R29. It is worth noting that the chemistry of HNO still has large uncertainties, as stated in the work of FaSheber et al. [115]. Direct measurements and theoretical calculation for R25–29 are still poorly investigated, particularly at high temperatures. Experimental/theoretical determinations of the temperature- and/or pressure-dependency of reactions involving HNO would be valuable to the combustion community.

**HON scheme:** In addition to R25,  $\dot{\text{H}}$  atoms can also be eliminated via the reaction:



Once HON is formed via R30 it can compete with HNO for free radicals via the following reactions:



**Fig. 5.** Effects of HON chemistry and reaction R31 on NO formation in the H<sub>2</sub>/O<sub>2</sub>/NO<sub>x</sub> reaction system at low pressure under fuel-rich condition. (a) Effect of HON chemistry. (b) Effect of rate constant of R31.



Amongst these, the branching ratio between R31 and R32 appears to be particularly important for NO formation. Figure 5 illustrates the effect of including HON chemistry in the simulations, and particularly R32, on NO formation at a typical JSR conditions. It can be seen that the prediction with HON chemistry presents a lower rate of NO formation at higher temperatures (> 850 K), and is closer to the experimental measurements, Fig. 5(a). It means that HON chemistry overall promotes the conversion of NO. Moreover, a sensitivity analysis of NO formation also reveals the importance of R32. The significant effect of an increase in the rate constant of R32 by a factor of two is shown by the solid black line, exhibiting a 30% lower prediction in NO concentration at 1050 K, Fig. 5(b). Note that HON chemistry only plays an important role at atmospheric pressures and at fuel-rich conditions. However, the effect appears to be negligible at higher pressures because the conversion of NO to NO<sub>2</sub> is primarily governed by R5 and R-7. In this study, all of the kinetic parameters for HON related reactions are adopted from the recommendations of Dean and Bozzelli [98]. Unfortunately, no further literature data are currently available and further theoretical and experimental studies on this system are warranted.

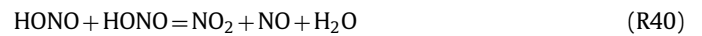
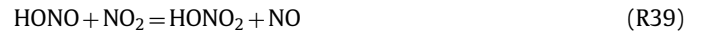
**HONO/HNO<sub>2</sub> scheme:** HONO can be formed by the reaction of HNO with NO<sub>2</sub> via R29, while HONO can rapidly equilibrate with NO and OH radicals via R34.



The flux analyses presented in the work of both Mueller et al. [10] and Rasmussen et al. [9] indicate that, the HONO formed in R29 dissociates directly to participate into the chain propagating sequence consisting of R25, R29 and R-34, as well as R30 (in our mechanism). Fulle et al. [116] measured the rate constant at pressures of 1–1000 bar and at temperatures of 250–400 K. The experimental measurements are generally in agreement with the LPL recommended by Tsang and Herron [38], whereas it appears to be over four times higher than that of Tsang and Herron for the HPL. Recently, Atkinson et al. [117] reviewed the rate constant measurements and derived both the LP and HPLs which are much closer to

the Fulle et al. measurements. On the basis of the more extensive review by Atkinson et al. in accordance with Fulle et al. measurements, we select the Atkinson et al. recommendation for R34. Note that the rate constants derived from either Atkinson et al. or Fulle et al. are only valid in the low temperature range (< 500 K), and thus further experimental/theoretical studies of R34 over a wider range temperature are recommended.

Again, the consumption of HONO mainly undergoes attack of free radicals via the following reactions:



Hsu et al. [118] theoretically calculated rate constants for the reactions of R35 and R36 using modified G2 and BAC-MP4 methods with TST and RRKM approaches, and the calculated rate constants have been successfully applied to reproduce their subsequent measurements for thermal reduction process of NO<sub>2</sub> by H<sub>2</sub> [88]. This thus gives us a confidence in using the Hsu et al. calculations in our mechanism. In contrast to the reactions R35 and R36, fewer studies of the reaction of HONO with  $\ddot{\text{O}}$  atoms, R37, have been performed, and Tsang and Herron [38] recommendation is used in our model due to its widely available temperatures. Mueller et al. [10] pointed out that the formation and consumption of HONO is quite sensitive to R38, especially at high-pressure, low temperature conditions. Recently, Xia and Lin [119] performed an *ab initio* calculation of the rate constant for R38 using orbital and variational TST theory. Their results indicated that R38 exhibits a noticeable negative temperature dependence at temperatures below 1000 K. Note that Xia and Lin calculation did not agree with the recommendation of Tsang and Herron [38], but it was consistently in excellent agreement with Burkholder et al. [120] experimental measurements and Wang et al. [121] theoretical calculations. We therefore use the rate constant from Xia and Lin for R38. Furthermore, Lu et al. [122] carried out an *ab initio* molecular-orbital calculation on R39 in association with TST theory. Here, we re-fit



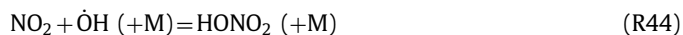
the total rate based on combining the three-parameter fit for *cis*-HONO and *trans*-HONO to assign a rate constant for R39. However, a slightly large uncertainty factor of three to four is present in the rate constant calculation due to the energy barrier uncertainty of 2–3 kcal mol<sup>-1</sup> resulting from the G2M (RCC, MP2) level of theory used in the determination of the transition state parameters. The bimolecular decomposition of HONO via R40 has been calculated by Mebel and Lin [123] with a consistent theory approach of their previous work [122] of R39. We have chosen their calculation in the current model.

As a structural isomer of HONO, the fate of the less stable HNO<sub>2</sub> species must also be established. At combustion conditions, two possibilities to form HNO<sub>2</sub> proceed through R8 and R9. HNO<sub>2</sub> consumption can proceed either via isomerization (R41) to form the more stable HONO isomer through inter-conversion of a H atom from N-atom to O-atom or H-atom abstractions by  $\dot{\text{O}}$  atoms via R42 and by  $\dot{\text{O}}\text{H}$  radicals via R43.



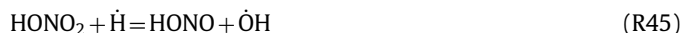
Rasmussen et al. [9] estimated the fall-off behavior for R41 using QRRK analysis based on their PES (47.3 kcal mol<sup>-1</sup> for HNO<sub>2</sub> and 55.3 kcal mol<sup>-1</sup> for HONO) which is generally consistent with the Takane and Fueno [124] calculations (45.7 kcal mol<sup>-1</sup> for HNO<sub>2</sub> and 56.6 kcal mol<sup>-1</sup> for HONO) and the determinations of Lu et al. [125] (46.5 kcal mol<sup>-1</sup> for HNO<sub>2</sub> and 55.2 kcal mol<sup>-1</sup> for HONO). Note that the LP and HPL expressions for R41 were reported by including a reduction of 17.4 kcal mol<sup>-1</sup> in the activation energy in light of an Eckart correction [126] for H-atom tunneling. However, in the recent work of Asatryan et al. [127], the heat of formation of HONO (−18.9 kcal mol<sup>-1</sup>) at 298 K calculated by high level composite methods is 8 kcal mol<sup>-1</sup> lower than for the HNO<sub>2</sub> isomer (−10.9 kcal/mol), while this difference in heat of formation for the isomerization is in excellent agreement with that of Rasmussen et al., and we therefore adopt their rate coefficient to describe R41. Furthermore, Rasmussen et al. calculated the rate constant for reaction R43 at the same level of theory and it is also used in this model. Compared to R41 and R43, R42 is much less important and its rate constant is taken from Dean and Bozzelli [98].

**HONO<sub>2</sub> scheme:** The formation of HONO<sub>2</sub> through the recombination of NO<sub>2</sub> with  $\dot{\text{O}}\text{H}$  radicals, R44, appears to be only important as an  $\dot{\text{O}}\text{H}$  radical-sink at atmospheric pressure. At typical combustion conditions, however, the generated HONO<sub>2</sub> is only an intermediate adduct of R-7 and is readily re-dissociation back to the formation of NO<sub>2</sub> and  $\dot{\text{O}}\text{H}$  radicals, as discussed by Rasmussen et al. [9].



We use the refined fall-off curves reported by Troe [128] as these results are consistent with his previously theoretical work [129] as well as with the experimental measurements [128,130].

HONO<sub>2</sub> is mostly consumed by attack by H atoms and  $\dot{\text{O}}\text{H}$  radicals via the following four reaction channels:



Here, we have used the recommended rate expressions from Boughton et al. [120] with quantum-mechanical tunneling corrections for the reactions of R45–R47. By contrast, R48 is more likely critical to combustion of energetic materials related to ammonia. Xia and Lin [131] recently explored the mechanism of R48 via an *ab initio* molecular orbital calculations at the G2M(cc3) level of theory. Their calculations reproduce well the experimental observation of a strong negative temperature coefficient behavior [132–135]. In this model, we have chosen the Xia and Lin calculation for R48. Note that the selected value is similar to the measurements of Lamb et al. [136] which have been widely used as a validation target in recent kinetic models [9,13,15,39] and is also consistent with the IUPAC recommendation [117] at 300 K, whereas it is approximately an order of magnitude faster than the Lamb et al. and IUPAC values at 1000 K.

## 2.2.6. NH<sub>3</sub> sub-mechanism

Ammonia (NH<sub>3</sub>) chemistry partially influences the sub-mechanisms of N/O and H/N/O and further effect the formation of NO<sub>x</sub> and thus we have added an NH<sub>3</sub> sub-mechanism in our model. The reactions involving NH<sub>3</sub> are mostly taken from the recent work of Mathieu and Petersen [137] where the NH<sub>3</sub> scheme was modified based on the model proposed by Dagaut et al. [59]. The updated model is capable of predicting the shock tube ignition delay time [137] and species profiles [59] for NH<sub>3</sub>/O<sub>2</sub>/Ar mixtures over a wide range of conditions. The sub-schemes of the NNH and NH<sub>2</sub>OH species recently reported by Klippenstein et al. [39,73] are adopted to describe thermal DeNO<sub>x</sub>.

## 3. Model performance

A great deal of experimental data measured using shock tubes, JSRs, flow reactors and spherical combustion bombs were collected to assess the performance of the mechanism developed in *this study*. In total, over 104 shock tube data sets, 87 JSR data sets, 87 flow reactor data sets and 6 laminar flame speed data sets have been used for the validation and comparison which are included as Supplementary material. The selected data are summarized in Table 1. Furthermore, five recent mechanisms available in the literature, namely the Ahmed\_2016 mechanism [15], the Konnov\_2009 mechanism [13], the SJK/PG\_2015 mechanism [31,39], the Mével\_2009 mechanism [19] and the Dagaut\_2008 mechanism [59] were also used to compared with the experimental targets as well as the model developed here.

### 3.1. Zeldovich NO formation

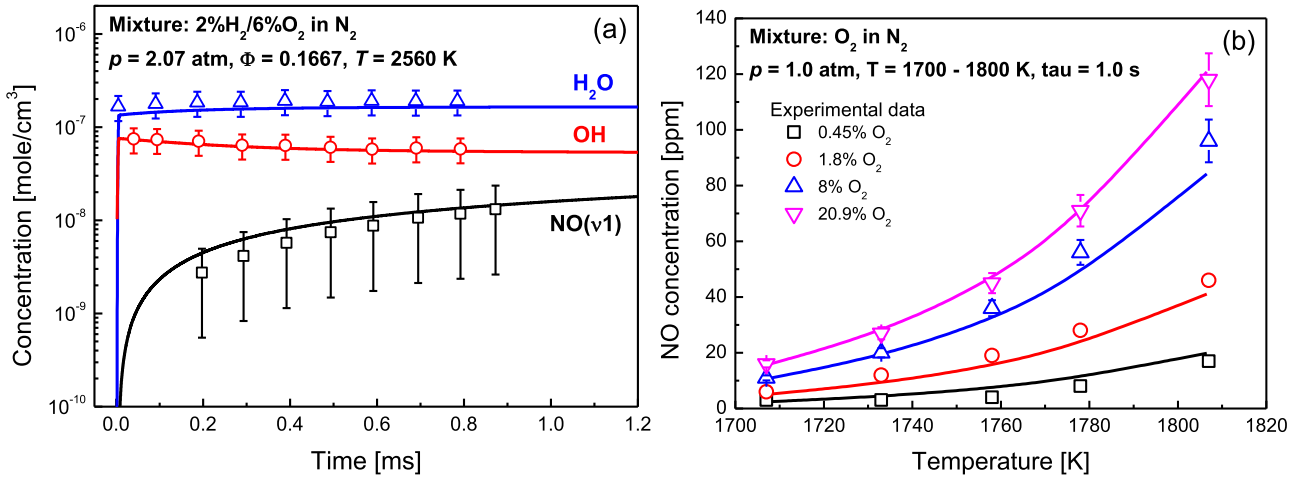
Bowman [17] conducted an investigation of thermal NO formation for H<sub>2</sub>/O<sub>2</sub>/N<sub>2</sub> combustion at an average pressure of 2.2 atm over temperature range 2150–2800 K using a shock tube and he provided the concentration of NO in two vibrational states ( $\nu = 1$  and  $\nu = 2$ ) corresponding to the absorption of incident radiation by both of the molecular bands ( $\gamma(0, 1)$  and  $\gamma(0, 2)$ ). Concentration profiles of  $\dot{\text{O}}\text{H}$  radicals, NO ( $\nu = 1$ ) and H<sub>2</sub>O were measured and were simulated using the current model. The results are in very good agreement with Bowman's measurements within his experimental uncertainty, Fig. 6(a).

In addition, Abian et al. [31] recently measured thermal NO formation in N<sub>2</sub>/O<sub>2</sub> oxidation using a flow reactor with various O<sub>2</sub> concentrations (0.45–20.9%) at temperatures in the range 1700–1800 K and at atmospheric pressure. To confirm the validity of the Zeldovich mechanism in our model the data reported by Abian are also used to validate model predictions. Likewise, the model gives excellent agreement with the experimental measurements, Fig. 6(b). More validations are provided in Figs. S2 and S3.

**Table 1**

Range of experimental devices and conditions used for mechanism improvement and validation.

Experimental device	Measured properties	Experimental conditions	Reference
Shock tube	Species profiles (2 data sets)	2.2 atm, 2150–2800 K, $\phi = 0.167$ –3.0 for $\text{H}_2/\text{O}_2/\text{N}_2$ mixtures	Bowman [17] 1971
Shock tube	Species profiles (29 data sets)	58–347 kPa, 1490–2490 K for $\text{N}_2\text{O}/\text{Ar}$ mixtures	Javoy et al. [20] 2009
Shock tube	Species profiles (4 data sets)	8.0–11.5 atm, 1800–2700 K for $\text{H}_2/\text{N}_2\text{O}/\text{Ar}$ mixtures	Zuev and Starikovskii [21] 1991
Shock tube	Ignition delay times (15 data sets)	1.5–30 atm, 1038–1744 K, $\phi = 0.3$ –1.0 for $\text{H}_2/\text{O}_2/\text{NO}_2/\text{Ar}$ mixtures	Mathieu et al. [8] 2013
Shock tube	Ignition delay times (12 data sets)	1.6–32 atm, 940–1675 K, $\phi = 0.5$ for $\text{H}_2/\text{O}_2/\text{N}_2\text{O}/\text{Ar}$ mixtures	Mathieu et al. [18] 2012
Shock tube	Ignition delay times (3 data sets)	1.8–32 atm, 993–1975 K, $\phi = 0.5$ for $\text{H}_2/\text{CO}/\text{O}_2/\text{NH}_3/\text{Ar}$ mixtures	Mathieu et al. [16] 2013
Shock tube	Ignition delay times (2 data sets)	0.14–0.47 atm, 1007–1574 K For $\text{H}_2/\text{N}_2\text{O}/\text{Ar}$ and $\text{H}_2/\text{O}_2/\text{N}_2\text{O}/\text{Ar}$ mixtures	Kosarev et al. [22] 2007
Shock tube	Ignition delay times (9 data sets)	300 kPa, 1300–2000 K, $\phi = 0.5$ –2.0 for $\text{H}_2/\text{N}_2\text{O}/\text{Ar}$ mixtures	Mével et al. [19] 2009
Shock tube	Ignition delay times and species profiles (7 data sets)	1.29–1.91 atm, 1700–2600 K, $\phi = 0.36$ –1.0 for $\text{H}_2/\text{N}_2\text{O}/\text{Ar}$ mixtures	Henrici and Bauer [23] 1969
Shock tube	Ignition delay times (3 data sets)	2.0 atm, 1400–2000 K, $\phi = 0.5$ –2.0 $\text{H}_2/\text{N}_2\text{O}/\text{Ar}$ mixtures	Hidaka et al. [24] 1985
Shock tube	Ignition delay times (2 data sets)	1.5 atm, 1919–2781 K, $\phi = 3.3$ –5.0 for $\text{H}_2/\text{N}_2\text{O}/\text{Ar}$ mixtures	Pamidimukkala and Skinner [25] 1982
Shock tube	Ignition delay times (2 data sets)	1.4–10.4 atm, 1654–2221 K for $\text{H}_2/\text{CO}/\text{N}_2\text{O}/\text{Ar}$ mixture	Kopp et al. [27] 2012
Shock tube	Ignition delay times (2 data sets)	3.0–12 atm, 1436–2287 K for $\text{N}_2\text{O}/\text{Ar}$ mixture	Borisov et al. [138] 1972
Shock tube	Ignition delay times (12 data sets)	1.4–30 atm, 1560–2455 K, $\phi = 0.5$ –2.0 for $\text{NH}_3/\text{O}_2/\text{Ar}$ mixtures	Mathieu and Petersen [137]
JSR	Species profiles (78 data sets)	1.0–10 atm, 700–1150 K, $\phi = 0.1$ –2.5 for $\text{H}_2/\text{O}_2/\text{NO}_x/\text{N}_2$ mixtures	Dayma and Dagaut [28] 2006
JSR	Species profiles (9 data sets)	1.0 atm, 800–1400 K, $\phi = 0.1$ –2.0 for $\text{H}_2/\text{CO}/\text{O}_2/\text{NO}_x/\text{N}_2$ mixtures	Dagaut et al. [30] 2003
Flow reactor	Species profiles (4 data sets)	50 atm, 702–900 K, $\phi = 0.0009$ –12 for $\text{H}_2/\text{O}_2/\text{N}_2$ mixtures	Hashemi et al. [55] 2015
Flow reactor	Thermal NO (4 data sets)	1.0 atm, 1700–1800 K, 0.45–20% $\text{O}_2$ for $\text{O}_2/\text{N}_2$ mixtures	Abian et al. [31] 2015
Flow reactor	Species profiles (15 data sets)	20–100 atm, 600–900 K, $\phi = 0.064$ for $\text{CO}/\text{H}_2/\text{O}_2/\text{NO}_x$ mixture	Rasmussen et al. [9] 2008
Flow reactor	Species profiles (41 data sets)	0.5–14 atm, 750–1100 K, $\phi = 0.25$ –1.0 for $\text{H}_2/\text{O}_2/\text{NO}_x$ and $\text{CO}/\text{H}_2\text{O}/\text{O}_2/\text{NO}_x$ mixtures	Mueller et al. [10] 1999
Flow reactor	Species profiles (23 data sets)	1.05 atm, 800–1400 K for $\text{NO}/\text{NO}_2/\text{CO}/\text{H}_2\text{O}/\text{N}_2$ mixtures	Glarborg et al. [32] 1995
Spherical combustion bomb	Laminar flame speeds (1 data set)	1.0 atm, 300 K, $\phi = 0.15$ –1.8 for $\text{H}_2/\text{N}_2\text{O}/\text{Ar}$ mixtures	Mével et al. [33] 2009
Spherical combustion bomb	Laminar flame speeds (5 data set)	0.2–0.8 atm, 298 K, $\phi = 0.15$ –1.0, 0–55% $\text{N}_2$ for $\text{H}_2/\text{N}_2\text{O}/\text{N}_2$ mixtures	Bane et al. [34] 2011



**Fig. 6.** Comparison of experiments and model predictions for Zeldovich NO formation in  $\text{O}_2/\text{N}_2$  system with different  $\text{O}_2$  concentrations. Symbols represent experimental measurements; lines denote model simulation with the current mechanism. (a) Shock tube data of Bowman [17]. (b) Flow reactor data of Abian et al. [31].

### 3.2. Ignition delay times

Shock tube measurements involving global combustion targets of ignition delay times and pyrolysis of nitrogenous species are primarily used to examine the validity of the current mechanism. These experiments were carried out over a wide range of pressure (0.14–33 atm), temperature (940–2600 K), equivalence ratio (0.3–5.0) and  $\text{NO}_x$  concentration (100 ppm – 10%) for different reaction systems such as pure  $\text{N}_2\text{O}$ ,  $\text{H}_2/\text{N}_2\text{O}$ ,  $\text{H}_2/\text{NO}_x/\text{O}_2$ , and  $\text{H}_2/\text{CO}/\text{N}_2\text{O}$  system. Complete validations are presented in Figs. S4–S17, and only typical cases will be discussed below.

#### 3.2.1. Model performance

**$\text{N}_2\text{O}$  pyrolysis and self-oxidation:** When a fuel and molecular oxygen are absent in a reaction system, the  $\text{N}_2\text{O}$  chemistry only involves its decomposition mechanism (i.e. R11, R15, R16 and R19) and the Zeldovich mechanism. Javoy et al. [20] explored the decomposition of  $\text{N}_2\text{O}$  by experimentally monitoring the formation of  $\dot{\text{O}}$  atoms behind reflected shock waves at pressures of 0.58–3.47 atm in the temperature range 1490–2490 K. Borisov and Skachkov [26] also used a shock tube to investigate the spontaneous ignition behavior of  $\text{N}_2\text{O}/\text{Ar}$  mixtures at pressures of 2.5–14 atm in the temperature range 1351–2326 K. The data measured

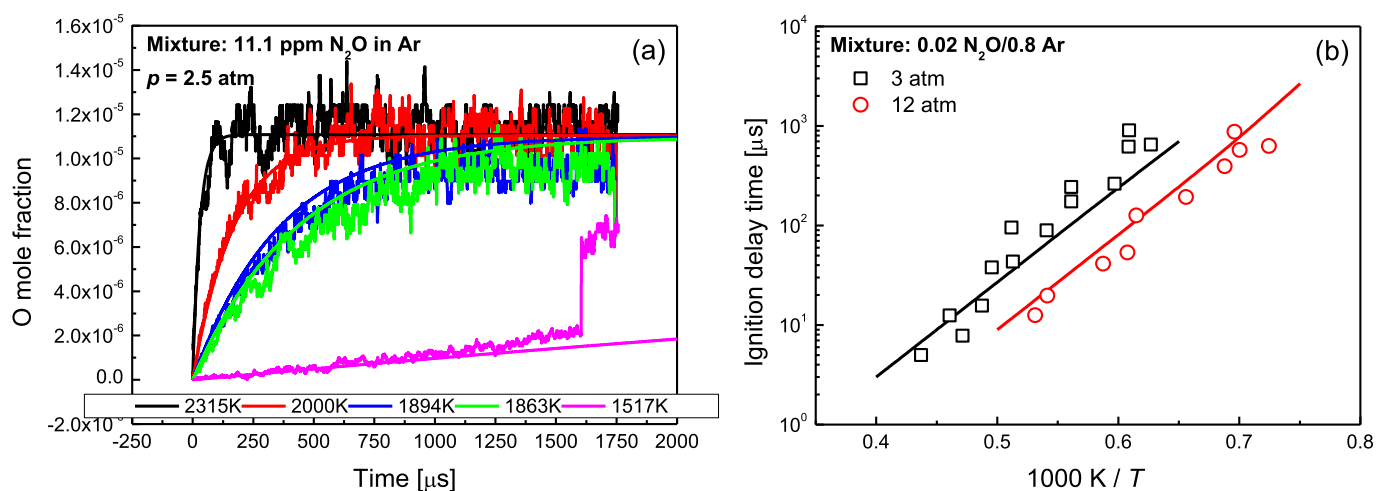


Fig. 7. Comparison of experiments and model predictions for the pyrolysis and oxidation of N<sub>2</sub>O/Ar mixtures at pressures of 2.5–12 atm. Symbols represent experimental measurements; lines denote model simulations with the current mechanism. (a) Shock tube absorption profiles of  $\dot{O}$  atoms taken from Javoy et al. [20]. (b) Shock tube ignition delay times taken from Borisov and Skachkov [26].

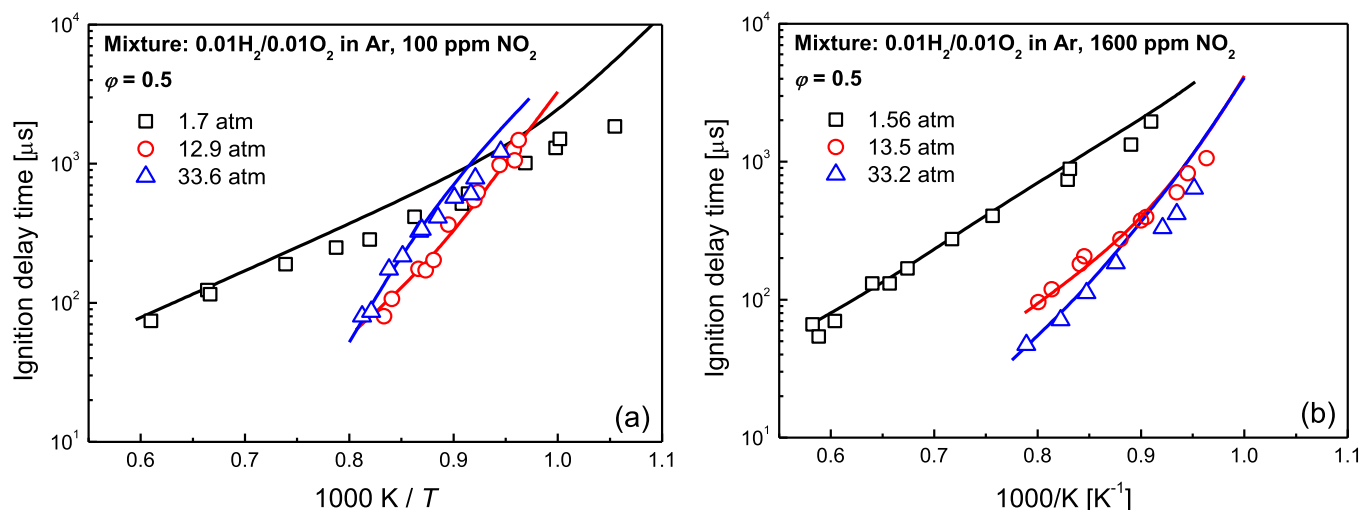


Fig. 8. Comparison of experiments and model predictions for ignition delay times of H<sub>2</sub>/O<sub>2</sub>/NO<sub>2</sub>/Ar mixtures. Symbols represent experimental measurements taken from Mathieu et al. [8]; lines denote model simulations with the current mechanism. (a) Effect of pressure at low concentration of NO<sub>2</sub>. (b) Effect of pressure at high concentration of NO<sub>2</sub>.

in both of these studies are compared to the current model predictions, Fig. 7. It can be seen that the current model reproduces well the temperature dependence of  $\dot{O}$  atom formation as well as the pressure dependence of the self-ignition delay times of N<sub>2</sub>O.

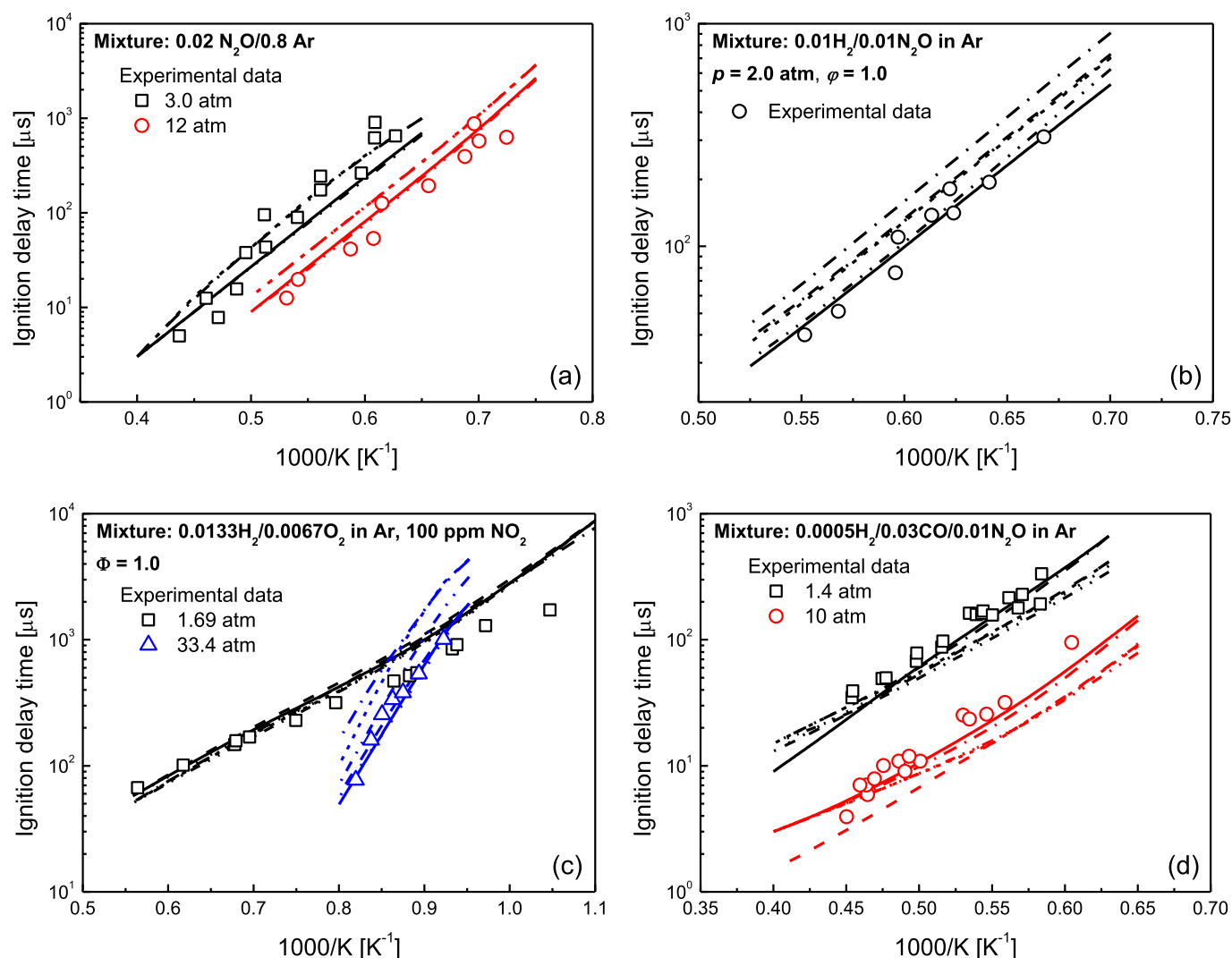
**H<sub>2</sub>/NO<sub>x</sub>/O<sub>2</sub> system:** The H<sub>2</sub>/NO<sub>2</sub>/O<sub>2</sub> and H<sub>2</sub>/N<sub>2</sub>O/O<sub>2</sub> systems are considered as the targets to explore the interaction of hydrogen and NO<sub>x</sub> in the presence of O<sub>2</sub>. Mathieu et al. [8,18] conducted a series of shock tube investigations on the effect of NO<sub>2</sub> and N<sub>2</sub>O addition on the ignition of H<sub>2</sub>/O<sub>2</sub> mixtures at various pressures (1.5–33 atm), equivalence ratios (0.5–2.0) and NO<sub>x</sub> concentrations (100–1600 ppm for NO<sub>2</sub> addition and 100–3200 ppm for N<sub>2</sub>O addition). The ignition delay time data of Mathieu et al. are therefore used to compare to the current model predictions. Results of the model simulations are in excellent agreement with the experimental data, Fig. 8. For the addition of low concentrations of NO<sub>2</sub>, the pressure-dependence of the ignition delay times is essentially consistent with that for pure hydrogen. This means that NO<sub>2</sub> only has a limited perturbation effect on the kinetics of hydrogen oxidation, Fig. 8(a).

For high levels of NO<sub>2</sub> addition, NO<sub>2</sub> has a strong pressure-dependence only at lower pressures (from 1.5 to 13.5 atm), whereas it was reported that there appeared to be a weak pressure

dependence at higher pressures (from 13.5 to 33.2 atm), Fig. 8(b). As discussed by Mathieu et al. [8], for high levels of NO<sub>2</sub> in the hydrogen system, reactions governing ignition change from a chain branching reaction ( $\dot{H} + O_2 = \dot{O} + \dot{O}H$  (R<sub>H1</sub>)) to a chain propagating reaction ( $H_2 + \dot{O}H = \dot{H} + H_2O$  (R<sub>H2</sub>)) due to the additional generation of  $\dot{O}H$  radicals, which results in an equilibrium of the radical-pool concentration.

### 3.2.2. Comparison with literature models

Figure 9 shows a comparison of the current model prediction with the performances of five literature models against the experimental measurements for the five typical systems mentioned above. Overall, the different models predict the ignition delay times reasonable well and this conclusion is in consensus with Ahmed et al. [15]. The SJK/PG\_2015 mechanism over-predicts the reactivity of the H<sub>2</sub>/N<sub>2</sub>O/Ar system (Fig. 9(b)) at low pressures while the SJK/PG\_2015 and Dagaut\_2008 mechanisms over-predict the reactivity of the H<sub>2</sub>/O<sub>2</sub>/NO<sub>x</sub>/Ar system at high pressures (Fig. 9(c)). It should be noted that the different models present different predictions of the experimentally observed global activation energy for the H<sub>2</sub>/CO/N<sub>2</sub>O/Ar system at 10.4 atm. The SJK/PG\_2015



**Fig. 9.** Current model and selected literature model predictions compared to literature data. Symbols represent experimental measurements; lines denote model simulations with the current model (solid line), Ahmed\_2016 [15] (dash line), Konnov\_2009 [13] (dot line), SJK/PG\_2015 [31,39] (dash dot line), Mével\_2009 [19] (dash dot dot line) and Dagaut\_2008 [59] (short dash line). (a)  $\text{N}_2\text{O}$  self-oxidation without fuel and  $\text{O}_2$  [26]. (b)  $\text{H}_2/\text{N}_2\text{O}$  oxidation without  $\text{O}_2$  [24]. (c)  $\text{H}_2/\text{NO}_2/\text{O}_2$  oxidation [8]. (d)  $\text{H}_2/\text{CO}/\text{N}_2\text{O}$  oxidation [27].

model and our mechanism are in good agreement with the experimental data whereas the other five models give slightly lower activation energy value, Fig. 9(d). The reason for the difference may be a combination of a) the different base chemistry ( $\text{H}_2$  and  $\text{CO}$ ), b) the different sub-mechanisms for  $\text{N}_2\text{O}$  and  $\text{NO}_2$  chemistry and c) the different sources of thermochemistry used.

### 3.3. Flow reactor species versus time data

In an attempt to further illustrate the model performance, the evolution profiles of major species versus reaction time and/or temperature measured in FRs have been simulated using the current model. These flow reactor experiments were performed over a wide range of pressure (0.5–100 atm), temperature (600–1800 K), equivalence ratio (0.0009–12) and  $\text{NO}_x$  concentration (12–10,000 ppm) for different reaction systems including  $\text{H}_2/\text{NO}_x/\text{O}_2$ ,  $\text{CO}/\text{H}_2\text{O}/\text{NO}_x/\text{O}_2$  and  $\text{H}_2/\text{CO}/\text{H}_2\text{O}/\text{NO}_x/\text{O}_2$ . Complete validations are provided in Figs. S18–S20, and only representative cases are selected for the discussion in the following section.

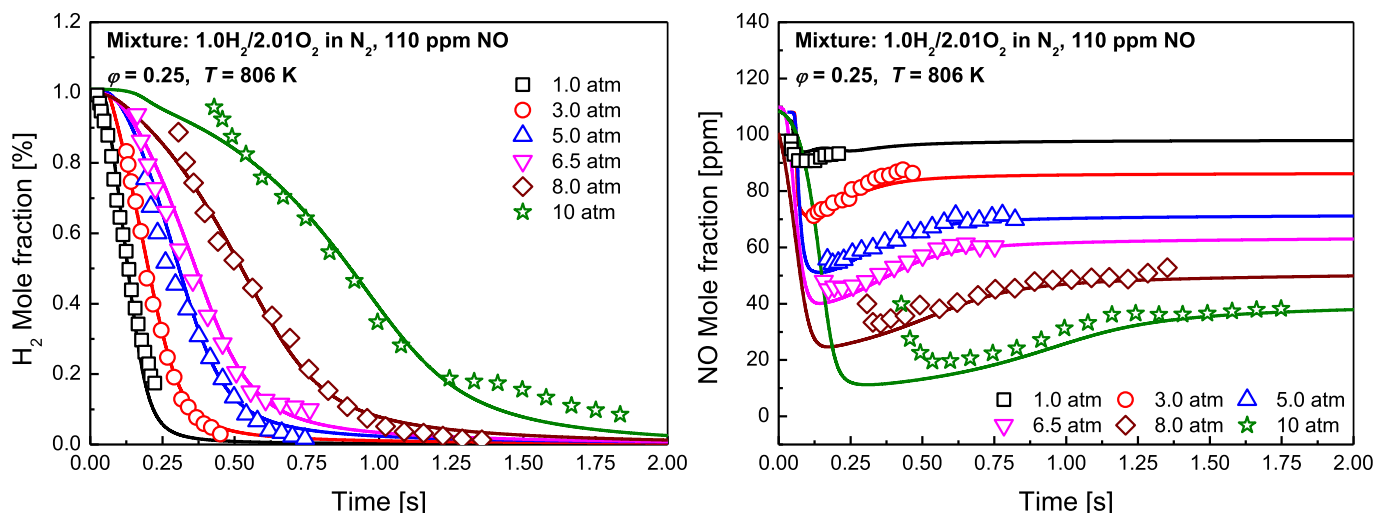
#### 3.3.1. Model performance

**$\text{H}_2/\text{NO}_x/\text{O}_2$  system:** Figure 10 depicts detailed comparisons of model predictions of species profile data [10] as a function of time

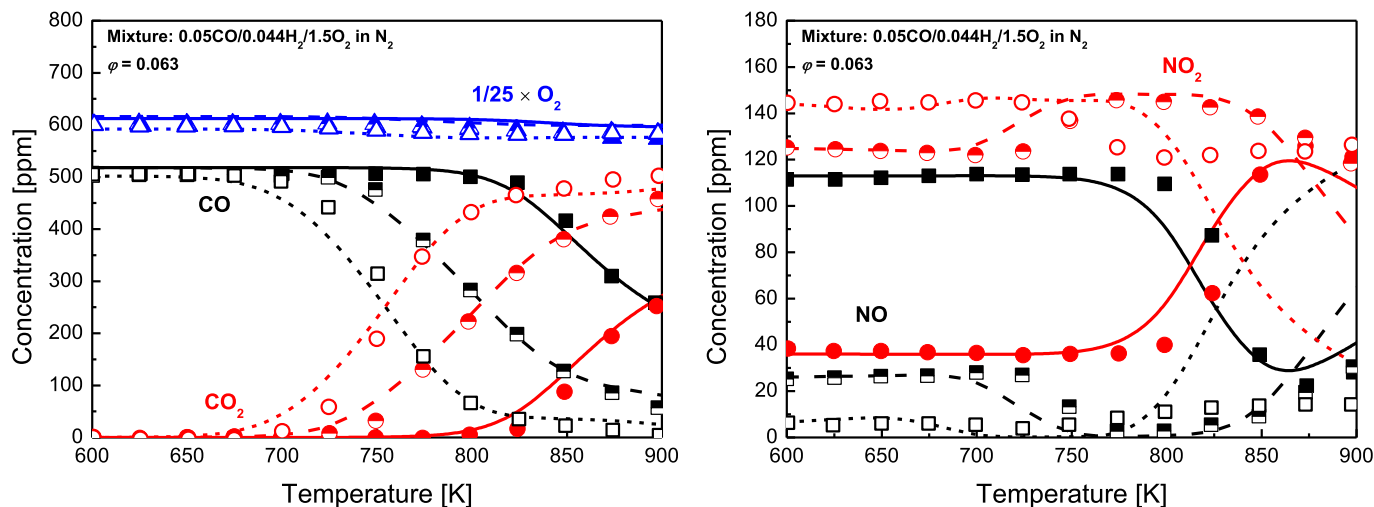
taken over a series of experimental conditions where the pressure was varied from 1.0 to 10 atm. It indicates that increasing the pressure inhibits  $\text{H}_2$  consumption and promotes the  $\text{NO}$  to  $\text{NO}_2$  inter-conversion. The model accurately captures the pressure-dependent behavior throughout the entire reaction time scale. Note that the effect of pressure appears to be more noticeable at higher pressures due to the fact that the third-body recombination reaction  $\dot{\text{H}} + \text{O}_2 (+\text{M}) = \text{HO}_2 (+\text{M})$  ( $\text{R}_{\text{H}3}$ ) dominates the reactivity at elevated pressures and at intermediate temperatures, namely 806 K in this study. The abundant  $\text{HO}_2$  radicals preferentially react with  $\text{NO}$  to form  $\text{NO}_2$  via  $\text{R-7}$ .

**$\text{H}_2/\text{CO}/\text{H}_2\text{O}/\text{NO}_x/\text{O}_2$  system:** For the  $\text{H}_2/\text{CO}/\text{H}_2\text{O}/\text{NO}_x/\text{O}_2$  system model predictions are compared with the high pressure FR species profiles of Rasmussen et al. [9] at pressures of 20–100 atm, Fig. 11. Again, the model thoroughly reproduces the pressure dependence of the  $\text{CO}$  to  $\text{CO}_2$  conversion as well as the evolution of the  $\text{NO}_x$  species. In general, increasing the pressure reduces the initial temperature of the  $\text{CO}$  to  $\text{CO}_2$  conversion process. The effect of pressure on the initial temperature of  $\text{CO}$  consumption reduces with increasing pressure. This is as expected as indicated by Rasmussen et al. [9] and Ahmed et al. [15]. Note that the results simulated with the current model are quite similar to the numerical values of Rasmussen et al, meaning the current model are largely consistent





**Fig. 10.** Comparison of experiments and model predictions for the species profiles in  $\text{H}_2/\text{O}_2/\text{NO}/\text{N}_2$  mixture at 806 K and elevated pressures in a flow reactor [10]. Symbols represent experimental measurements; lines denote model simulations with the current mechanisms.



**Fig. 11.** Comparison of experiments and model predictions for the species profiles in  $\text{CO}/\text{H}_2/\text{NO}_x/\text{N}_2$  mixture at 100 atm over 600–900 K in a flow reactor [9]. Symbols represent experimental measurements (solid: 20 atm, half-solid: 50 atm, open: 100 atm); lines denote model simulations with the current mechanism (solid line: 20 atm, dash line: 50 atm, short dash line: 100 atm).

with Rasmussen et al. with respect to considering real temperature profiles.

### 3.3.2. Comparison with literature models

Unlike the comparison of the model performance in predicting ignition delay times, the current model is considerably different to other literature models in simulating either the  $\text{H}_2/\text{NO}_x/\text{O}_2$  system or the  $\text{CO}/\text{H}_2\text{O}/\text{O}_2$  system. Figure 12 shows detailed comparisons of the model performance at 10 atm. For the  $\text{H}_2/\text{NO}_x/\text{O}_2$  system, Fig. 12(a), both the SJK/PG\_2015 and Mével\_2009 mechanisms over-predict the consumption of hydrogen, especially at intermediate and late reaction times. As a result, the two models present unreasonable predictions of NO to  $\text{NO}_2$  conversion, particularly the SJK/PG\_2015 mechanism. Note that the predictions by the Ahmed\_2016 mechanism are not presented at this condition due to convergence issues. However, for the  $\text{CO}/\text{H}_2\text{O}/\text{O}_2$  system, all of the models generally agree in the prediction of NO formation but they significantly diverge in predicting CO oxidation. Specifically, the Mével\_2009 mechanism predicts the slowest consumption of CO whereas the SJK/PG\_2015 mechanism presents the fastest consumption. The Ahmed\_2016 and Kon-

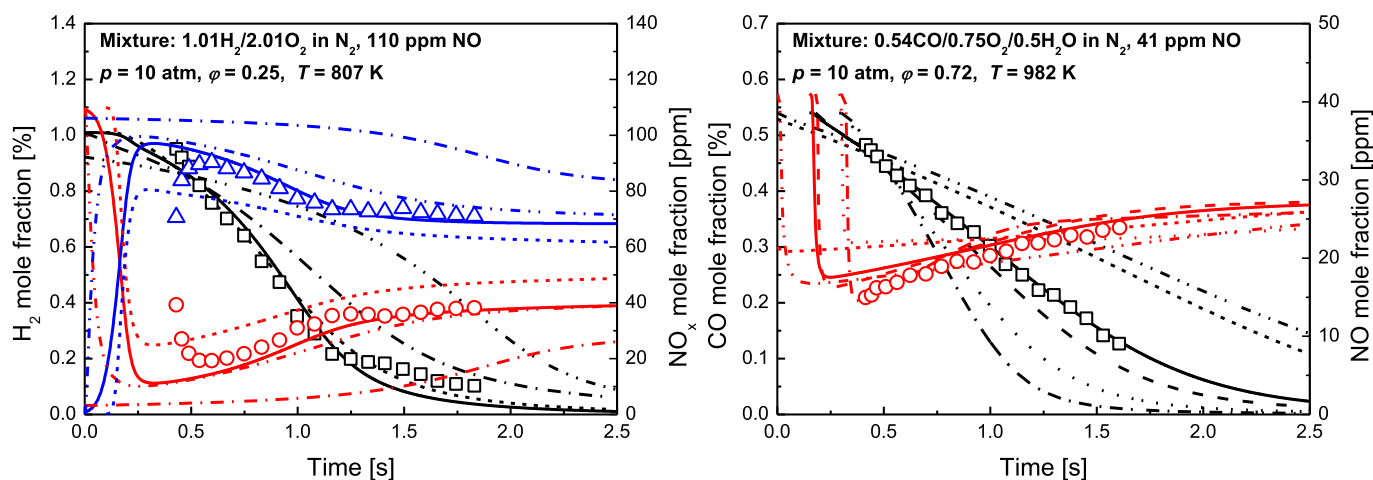
nov\_2009 mechanisms also predict a slightly fast consumption of CO.

### 3.4. Jet-stirred reactor species versus temperature profiles

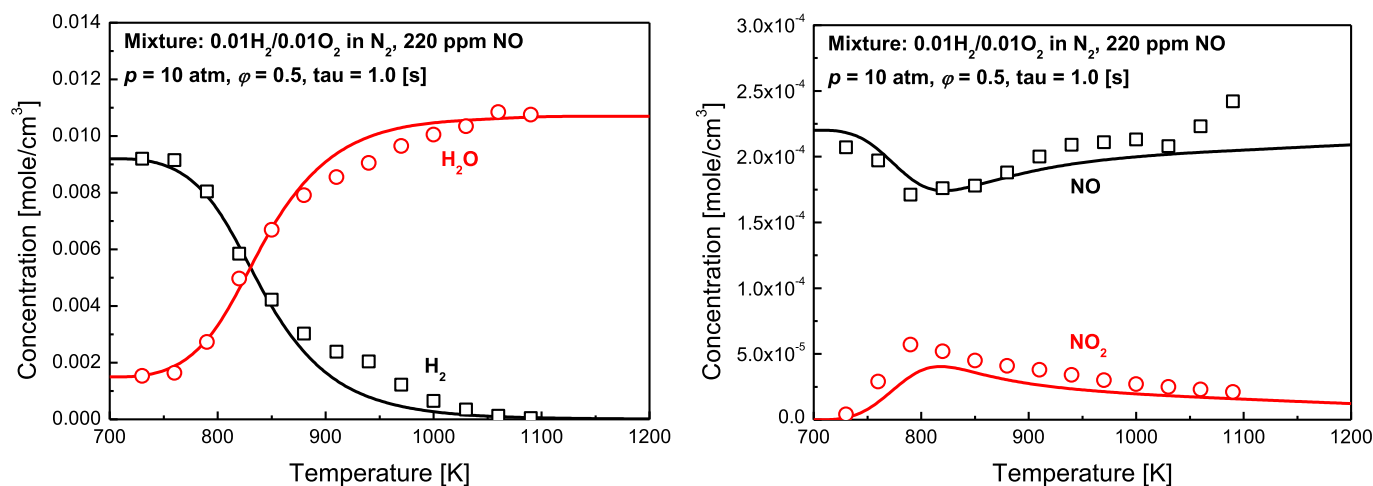
JSR species versus temperature data are used to test the ability of the proposed model by comparing its predictions to major species concentration profiles measured by Dagaut et al. [28,30]. These JSR experiments were performed over a wide range of pressures (1.0–10 atm), temperatures (700–1400 K), equivalence ratios (0.1–2.5) and  $\text{NO}_x$  concentrations (70–1000 ppm) for different reaction systems including  $\text{H}_2/\text{NO}/\text{O}_2$ ,  $\text{H}_2/\text{NO}_2/\text{O}_2$  and  $\text{H}_2/\text{CO}/\text{NO}_x/\text{O}_2$ . All of the data are valuable to provide further insight into the kinetic mechanisms including  $\text{NO}_x$  formation, NO to  $\text{NO}_2$  inter-conversion and the kinetics of interaction of  $\text{NO}_x$  species with fuel. Complete validations are available in Figs. S21 and S22. Likewise, we only chose several illustrative cases herein to discuss in the following section.

#### 3.4.1. Model performance

Figure 13 shows the detailed comparisons of experimental and model predicted species versus temperature profiles for the  $\text{H}_2/\text{O}_2$



**Fig. 12.** Current model and selected literature model predictions compared to literature data. Symbols represent experimental measurements [10]; lines denote model simulations with current model (solid line), Ahmed\_2016 [15] (dash line), Konnov\_2009 [13] (dot line), SJK/PG\_2015 [31,39] (dash dot line), Mével\_2009 [19] (dash dot dot line) and Dagaut\_2008 [59] (short dash line).



**Fig. 13.** Comparison of experiments and model predictions for the species profiles in  $\text{H}_2/\text{O}_2/\text{NO}/\text{N}_2$  system at 1.0 and 10 atm over 700–1100 K in a jet-stirred reactor [28]. Symbols represent; lines denote model simulations with the current mechanism.

system in the presence of 220 ppm NO at  $p = 10$  atm and  $\phi = 0.5$ . It is clear that the conversion rate of NO to  $\text{NO}_2$  first promotes and then inhibits reactivity with increasing temperature, with the reactivity reaching a peak value at approximately 800 K. The transformation in the conversion rate of NO to  $\text{NO}_2$  can be kinetically interpreted by considering the concentration of  $\text{HO}_2$  radicals generated at different temperatures. At lower temperatures ( $< 800$  K),  $\text{HO}_2$  radicals are formed via  $\text{R}_{\text{H}3}$ , which promotes the conversion of NO into  $\text{NO}_2$ . However, as the temperature increases  $\text{R}_{\text{H}3}$  is inferior in competition with  $\text{R}_{\text{H}1}$  resulting in a lower concentration of  $\text{HO}_2$  radicals and low rate of  $\text{R}_7$ . Meanwhile, additional H atoms yielded by reaction sequence  $\text{R}_{\text{H}1}$  and  $\text{R}_{\text{H}2}$  accelerates the rate of  $\text{R}_5$  leading to the conversion of  $\text{NO}_2$  back to NO. As expected, the current model accurately captures the NO to  $\text{NO}_2$  inter-conversion as well as  $\text{H}_2$  to  $\text{H}_2\text{O}$  conversion.

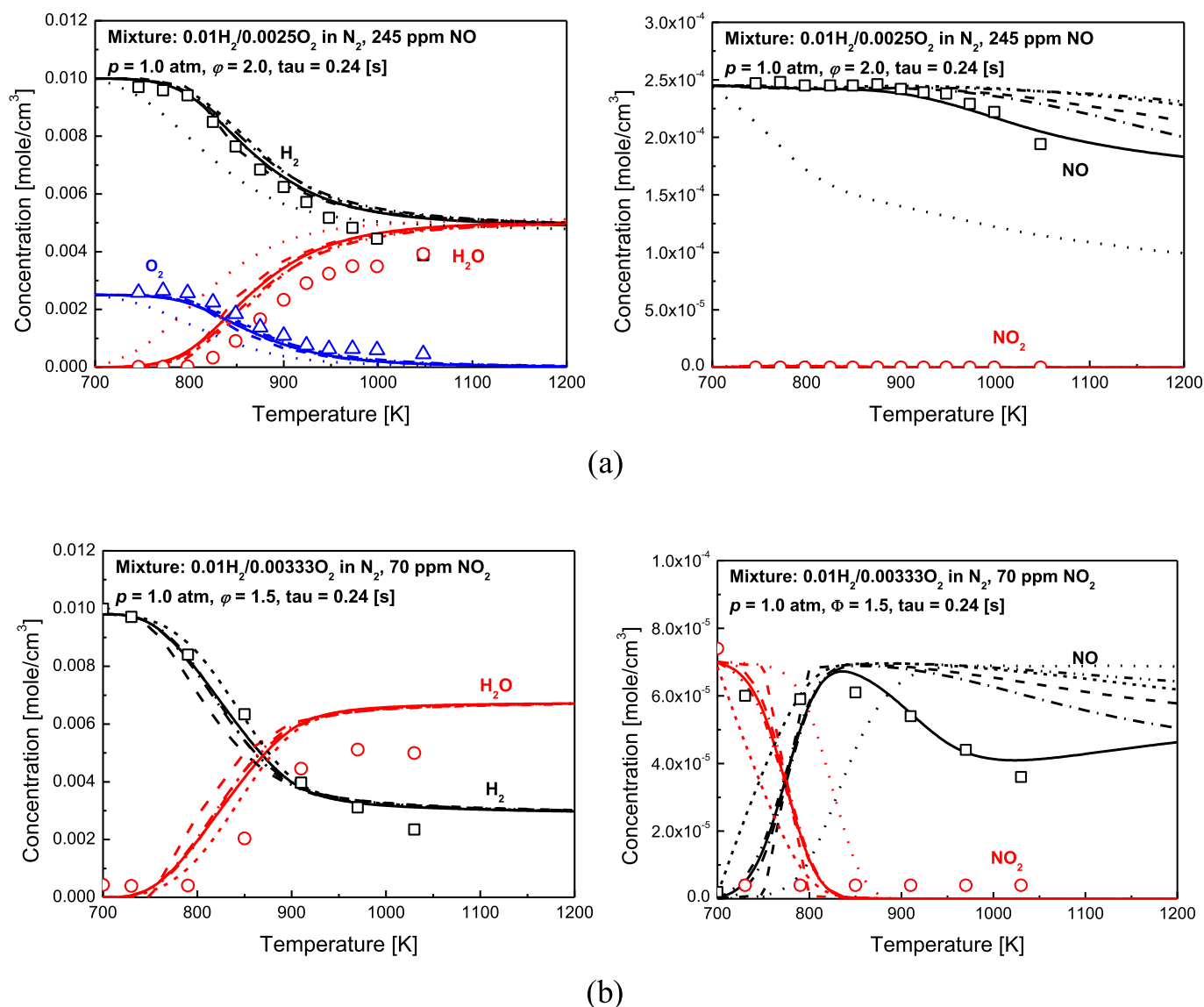
### 3.4.2. Comparison with literature models

Here, only two JSR conditions ( $p = 1.0$  atm,  $\phi = 2.0$  for the  $\text{H}_2/\text{O}_2/\text{NO}$  system and  $p = 1.0$  atm,  $\phi = 1.5$  for the  $\text{H}_2/\text{O}_2/\text{NO}_2$  system) reported by Dayma and Dagaut [28] are taken as representative cases to test the performance of our proposed model and others in the literature, Fig. 14.

For fuel oxidation, all of the models are in good agreements with the experimental measurements for the addition of both NO

and  $\text{NO}_2$  except the Konnov\_2009 mechanism which shows an under-prediction in the consumptions of reactants resulting in an over-prediction in the formation of  $\text{H}_2\text{O}$  in the  $\text{H}_2/\text{O}_2/\text{NO}$  system but the model is in reasonable agreement for the  $\text{H}_2/\text{O}_2/\text{NO}_2$  system.

For the NO to  $\text{NO}_2$  conversion process however, noticeable discrepancies in the model simulations can be clearly observed in either the  $\text{H}_2/\text{O}_2/\text{NO}$  or the  $\text{H}_2/\text{O}_2/\text{NO}_2$  systems. All of the literature models do not predict the decline in the NO concentration at higher temperatures— $> 950$  K for the  $\text{H}_2/\text{O}_2/\text{NO}$  system and  $> 850$  K for the  $\text{H}_2/\text{O}_2/\text{NO}_2$  system. Dayma and Dagaut [28] attempted to modify their model's shortcoming by modifying the rate constant of the reactions  $\text{HNO} + \text{H}_2 = \text{NH} + \text{H}_2\text{O}$  and  $\text{NH} + \text{NO} = \text{N}_2 + \text{OH}$ , but this change does not appear to be a satisfactory explanation/improvement as the modified model results in poorer predictions of the experiments at high pressures. They thus suggested that more kinetic analysis was needed to clarify this issue. In the current model, we have added the new reaction scheme for HON oxidation as discussed in section “HON scheme”, and identified its importance in predicting NO formation/consumption at low pressures. Clearly, the addition of HON chemistry greatly improves the NO conversion kinetics at low pressures yet maintains the model's good predictability at high pressures.



**Fig. 14.** Current model and selected literature model predictions compared to literature data. Symbols represent experimental measurements [28]; lines denote model simulations with the current model (solid line), Ahmed\_2016 [15] (dash line), Konnov\_2009 [13] (dot line), SJK/PG\_2015 [31,39] (dash dot line), Mével\_2009 [19] (dash dot dot line) and Dagaut\_2008 [59] (short dash line). (a) H<sub>2</sub>/O<sub>2</sub> oxidation under NO perturbation. (b) H<sub>2</sub>/O<sub>2</sub> oxidation under NO<sub>2</sub> perturbation.

### 3.5. Spherical flame speeds

Finally, spherical flame data are used to test the fidelity of the proposed model by comparing its predictions to laminar flame speeds measured by Mével et al. [33] and Bane et al. [34]. These experiments were performed over a range of pressures (0.2–1.0 atm), equivalence ratios (0.15–1.8) and dilutions (0 – 55% for N<sub>2</sub> and 60% for Ar). All of the data are helpful in testing the high temperature chemistry of the H<sub>2</sub>/N<sub>2</sub>O system. More validations are presented in Figs. S23 and S24.

#### 3.5.1. Model performance

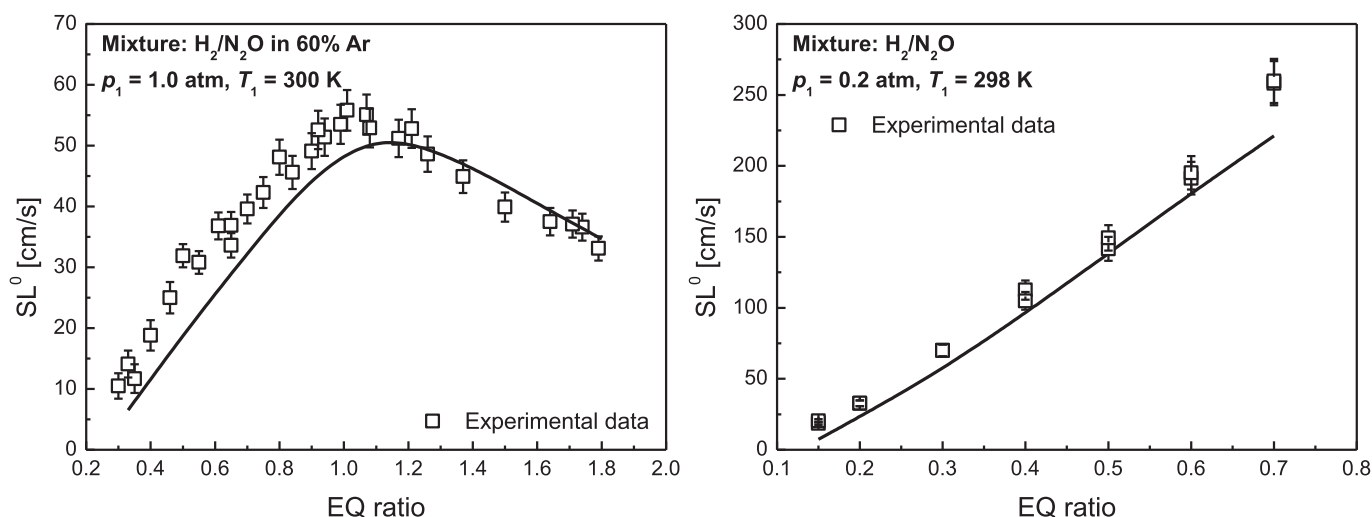
Figure 15 shows an example case of model predictions of measured laminar flame speed data for two different systems. For the case of the H<sub>2</sub>/N<sub>2</sub>O system diluted in Ar, the proposed model generally agrees with the experimental data over the range of equivalence ratios available, Fig. 15(a). It slightly under-estimates the flame speeds on the fuel-lean side but it is in better agreement on the fuel-rich side. Moreover, our current model is in excellent agreement with the data taken in the undiluted H<sub>2</sub>/N<sub>2</sub>O system,

Fig. 15(b). The comparative results suggests that the rate constants of the most important reactions R12 ( $\text{N}_2\text{O} + \text{H} = \text{N}_2 + \text{OH}$ ) and R13 ( $\text{N}_2\text{O} + \text{H} = \text{NH} + \text{NO}$ ) in the flame conditions highlighted by Mével et al. [33] are reliable in our proposed mechanism.

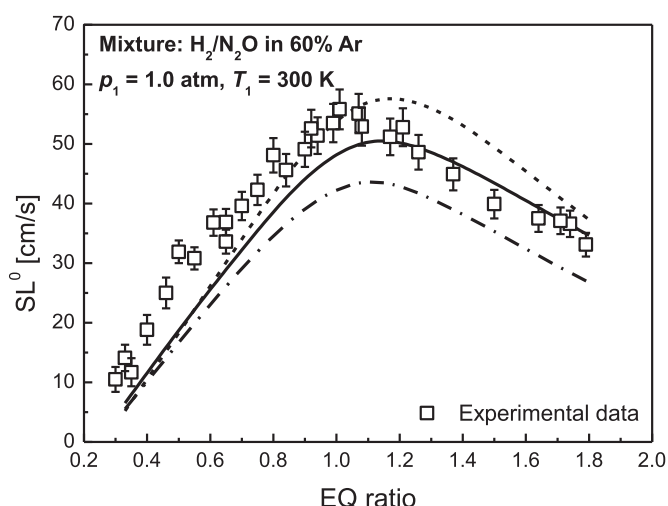
#### 3.5.2. Comparison with literature models

The conditions associated with the experiments presented in Fig. 15(a) have been selected as a representative case to compare the ability of literature models to predict flame speeds. Detailed comparisons are provided in Fig. 16.

The results indicate that all of the models tested here predict well the measured flame speeds but the consensus tends to be worse with increasing equivalence ratios. The SJK/PG\_2015 mechanism shows an under-prediction while the Dagaut\_2008 mechanism over-predicts the flame speeds at richer conditions. Note that the current mechanism and the SJK/PG\_2015 mechanism predict a peak value of flame speed at  $\phi = 1.1$  which is consistent with the experimental observations, whereas the Dagaut\_2008 mechanism predicts the peak at  $\phi = 1.2$ .



**Fig. 15.** Comparison of experiments and model predictions for the laminar flame speeds in  $H_2/N_2O$ /dilution system; lines denote model simulation with the current mechanism. Symbols represent experimental measurements for (a)  $H_2/N_2O$  diluted by 60% Ar at 1.0 atm and 300 K taken from Mével et al. [33] and for (b)  $H_2/N_2O$  undiluted at 0.2 atm and 298 K taken from Bane et al. [34].



**Fig. 16.** Comparison between current model and selected models against literature data. Symbols represent experimental measurements; lines denote model simulations with the current model (solid line), SJK/PG\_2015 [31,39] (dash-dot line), and Dagaut\_2008 [59] (short-dash line).

It is noted that, we only added part of error bars to the experimental data due to such the reasons: a) the authors did not pointed out clearly the uncertainty of their data and b) the data can be more clearly depicted and compared with modeling without error bars. Mueller et al. data [10] for example, although they gave the uncertainties of measured species ( $H_2O$ : 10%;  $O_2$ : 3%;  $CO$ : 2%;  $CO_2$ , 2%;  $H_2$ : 5%;  $NO$ : 5% and  $NO_2$ : 5%), to better distinguish the comparison of different models and the comparison of experimental data and model predictions, we have chosen not to include error bars for clarity as they are already very busy plots.

#### 4. Mechanism application to gas-turbine relevant condition

To provide more kinetic information for combustor design, we have used the proposed model to simulate the pressure-, temperature- and equivalence ratio-dependence of NO concentration for the selected mixture, 50%  $H_2$ /50% CO diluted in air, at practical engine-relevant conditions of pressures in the range 10–80 atm, at temperatures of 750–1050 K and at equivalence ratios

of 0.1–2.0. Detailed flux analyses were then carried out to better understand the effect of equivalence ratio on NO formation.

##### 4.1. Effect of engine combustion conditions on NO formation

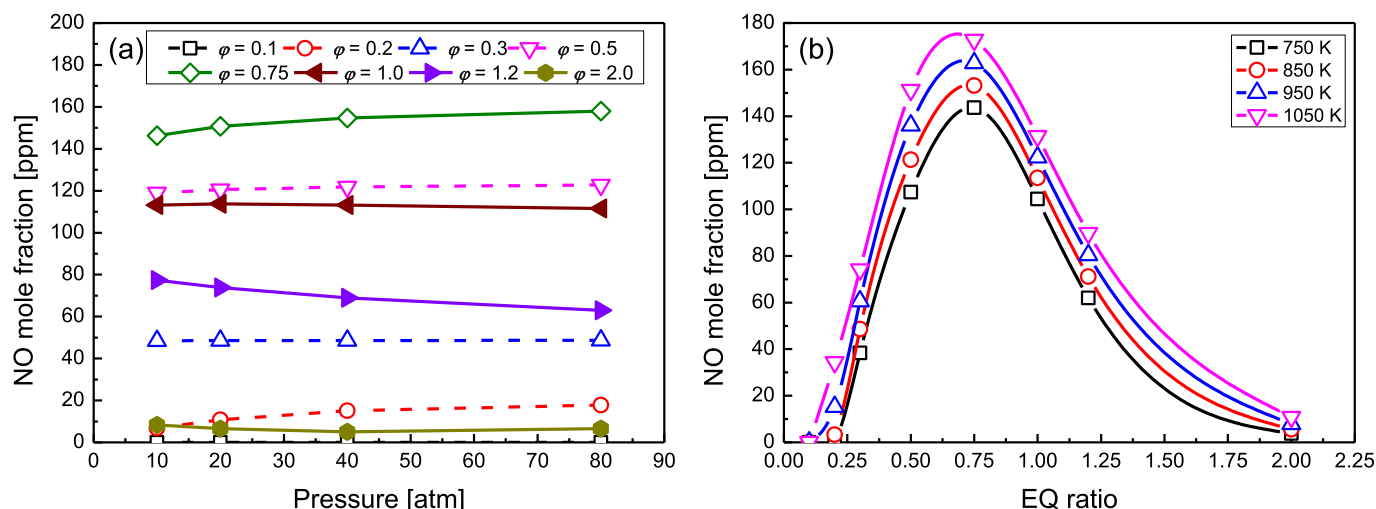
Figure 17(a) shows the NO concentration as a function of pressure at  $T = 850$  K and at various equivalence ratios. It is clear that NO exhibits a weak pressure-dependence at a given equivalence ratio meaning that the ignition pressure within an operating range of between 10 and 80 bar does not appear to have any effect on the concentration of NO formed. In contrast, the effects of temperature and equivalence ratio are more prominent, especially the latter, Fig. 17(b). For a given equivalence ratio, decreasing the temperature leads to a proportional reduction in NO concentration. At  $\varphi = 0.5$  for example, a 10 K decrease in temperature reduces the NO concentration by 10 ppm over the temperature range investigated. For a given temperature however, increasing the equivalence ratio first promotes and then inhibits NO formation. The NO concentration reaches a maximum value at  $\varphi \approx 0.75$ . On either side of this peak value, either fuel-lean or fuel-rich, there is a dramatic reduction in the observed NO concentration. Compared to controlling the pressure and temperature in the reactor, controlling the equivalence ratio of the reactant mixtures in the reactor appears to be more a promising way to control NO formation.

##### 4.2. Flux analysis

Based on the analysis above, flux analyses were carried out for the same mixtures at  $p = 30$  atm and  $T = 850$  K to provide an overview of the critical NO formation/consumption pathways at equivalence ratios of 0.3, 0.75 and 2.0, Fig. 18. In the system investigated here, NO is formed from molecular nitrogen.  $N_2$  is therefore selected as the initial reactant to explore the critical reaction pathway governing NO formation/consumption.

At all of the conditions investigated  $N_2$  is consumed by recombining with either  $H$  atoms forming NNH (over 99.7%) via R49 ( $N_2 + H (+M) = NNH (+M)$ ) or with  $O$  atoms forming  $N_2O$  (less 0.3%) via R11 ( $N_2 + O (+M) = N_2O (+M)$ ). Despite the fact that the former pathway consumes most of the  $N_2$ , the latter pathway appears to be a dominant channel in producing NO since 100% of the NNH generated from R49 can react with molecular oxygen to re-form  $N_2$  together with the release of  $HO_2$  radicals via R50 ( $NNH + O_2 = N_2 + HO_2$ ), especially at  $\varphi = 0.3$  and 0.75. The  $N_2O$





**Fig. 17.** NO formations calculated using the proposed model for  $H_2/CO/O_2/N_2$  system at practical engine conditions. (a) NO formation as a function of pressure at 850 K at various equivalence ratios; (b) NO formation as a function of equivalence ratio at 30 atm and different temperatures.

formed from R11 mainly undergoes O-atom abstractions by the fuel molecules via R20 and R51 ( $N_2O + CO = N_2 + CO_2$ ), resulting in the regeneration of  $N_2$ . Only a very small amount of  $N_2O$  reacts with H atoms via R13 resulting in NO formation. The amount of NO formed less than 100 ppm at  $\phi = 0.3$  but increases to 300 ppm at  $\phi = 0.75$  and to 1.88% at  $\phi = 2.0$ . Even though NO has similar formation pathways at different equivalence ratios, there are quite different kinetic mechanisms involved in its consumption at different equivalence ratios. At  $\phi = 0.3$ , 100% of NO is converted to  $NO_2$  by reacting with  $HO_2$  radicals via R-7 due to the abundance of  $HO_2$  radicals present in this lean environment. Most of the  $NO_2$  subsequently reacts with either H atoms (75.4%) via R5 or with CO (6.0%) via R10 to reproduce NO resulting in an inter-conversion of NO into  $NO_2$ . Only 15.9% of the  $NO_2$  is further oxidized by  $HO_2$  radicals via R8 forming  $HNO_2$ , followed by isomerization to HONO, which finally decomposes to NO and OH radicals via R-34. However, at  $\phi = 0.75$  NO consumption occurs either by its reaction with  $\dot{O}$  atoms (61.7%) via R4 forming  $NO_2$  or by reaction with H atoms (38.3%) via R25 forming HNO. Both  $NO_2$  and HNO can be converted into NO via O-atom abstraction and H-atom abstraction reactions respectively, until they reach an equilibrium concentration. Although the NO consumption pathways are somewhat different at  $\phi = 0.3$  and 0.75, the NO to  $NO_2$  inter-conversion pathways continue to play a dominant role rather than NO to HNO conversion, suggesting that there is a comparable NO consumption rate at both equivalence ratios. Thus, there is a two-fold reason for the higher NO concentration presented at  $\phi = 0.75$ , Fig. 17(b). Namely, 1) there is a faster NO formation rate due to the rate of R13 being accelerated due to an increased concentration of H atoms generated at  $\phi = 0.75$  and 2) there are similar NO consumption rates due to the dominant role of  $NO_2$  to NO conversion in NO consumption at both equivalence ratios.

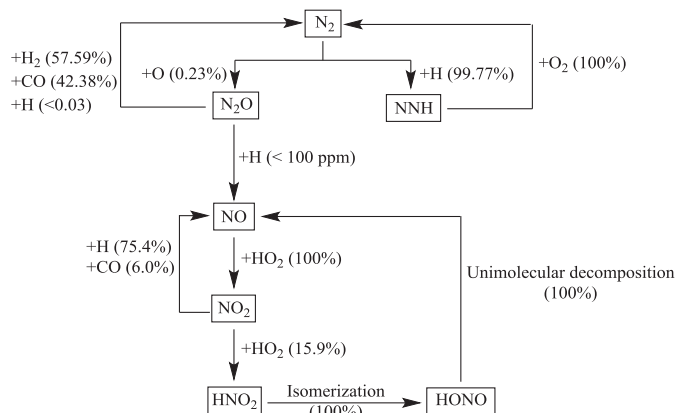
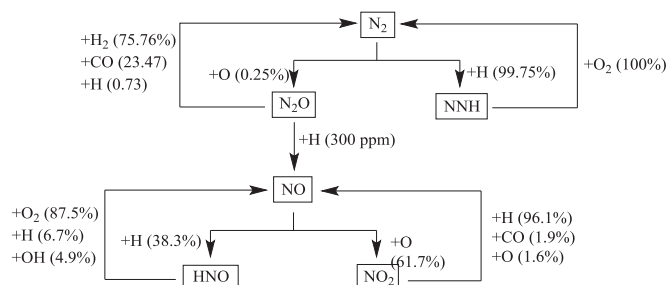
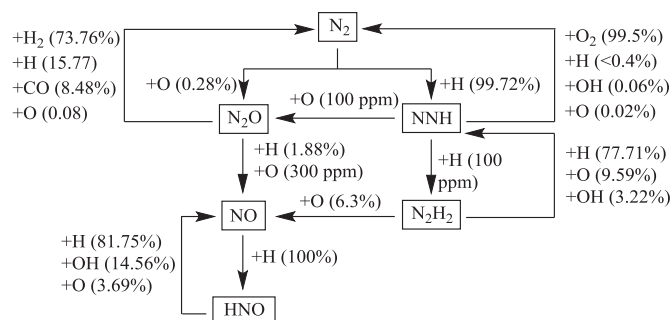
At  $\phi = 2.0$ ,  $N_2O$  can be formed by the reaction of NNH with  $\dot{O}$  atoms (100 ppm) via R52 ( $NNH + \dot{O} = N_2O + H$ ) in addition to the direct oxidation of  $N_2$  via R11. Likewise,  $N_2O$  is mainly consumed by R13 resulting in NO formation. Unlike the case for fuel-lean conditions, a small amount of NNH (100 ppm) can also contribute to NO formation by recombining with H atoms via R53 ( $NNH + H (+M) = N_2H_2 (+M)$ ) followed by the reaction of  $N_2H_2$  with  $\dot{O}$  atoms via R54 ( $N_2H_2 + \dot{O} = NO + NH_2$ ). All (100%) of the NO formed is then converted to HNO via R25 due to the relatively high concentration of H atoms and low concentrations of  $HO_2$  radicals and  $\dot{O}$  atoms at fuel-rich conditions. All of the HNO can react back to NO through H-atom abstraction reactions via H atoms (81.75%) in R26, via OH

radicals (14.56%) in R28 and via  $\dot{O}$  atoms (3.69%) in R27. It is worth noting that, despite the seemingly high percentage of NO that is observed at  $\phi = 2.0$ , the lower total amount of  $N_2$  at fuel-rich conditions results in a lower rate of formation of  $N_2O$  and NNH precursors relative to fuel-lean conditions. Additionally, the reaction rate of R26, which predominantly converts HNO into NO, is essentially unfavorable due to the rate constant being several times lower than that of R25 as well as a higher concentration of  $H_2$  at fuel-rich conditions. As a result, the conversion efficiency of HNO into NO is much slower than that of NO into HNO resulting in a lower rate of NO production.

## 5. Conclusions

In this study, we have developed a detailed kinetic mechanism to describe the hydrogen/ $NO_x$  and syngas/ $NO_x$  systems. Critically important reactions associated with the Zeldovich mechanism, the N/O sub-mechanism involving nitrogen dioxide, nitrous oxide, nitrogen trioxide, the H/N/O sub-mechanism involving nitroxyl isomer, nitrous acid isomers, and nitric acid isomers, and the  $NH_3$  mechanism have been described. Additionally, some missing reaction pathways involving  $HO_2$  kinetics of the CO chemistry sub-mechanism have also been considered in the current model. The rate constants used for these important reactions associated with the pyrolysis and oxidation of each  $NO_x$  sub-mechanism have been selected by comparison with literature values and integrating the latest published values. We have optimized several rate constants that had a large uncertainty by testing against the experimental data but did not further modify the rate constants obtained from either directly experimental measurements or high-level theoretically calculation in the literature.

The ability of the mechanism developed in this study to simulate a wide-range of experimental data for various reaction systems including  $H_2/O_2/N_2$ ,  $N_2O$  pyrolysis,  $H_2/N_2O$ ,  $H_2/NO_x/O_2$ ,  $CO/H_2O/NO_x/O_2$ ,  $H_2/CO/NO_x/O_2$  and the  $H_2/CO/H_2O/NO_x/O_2$  system. A large number of experimental data including 104 shock tube data sets, 87 JSR data sets, 87 FR data sets and 6 laminar flame speed data sets over 3000 experimental points were used. Overall, the current model gives a satisfactory representation of the experimental data over a wide range of conditions for each of the selected data sets considered here. Through the comparisons of the proposed mechanism and a selection of available literature mechanisms, we found that each literature mechanism performed well for certain systems but exhibited relatively noticeable deviations

(a)  $\phi = 0.3$ ,  $p = 30$  atm,  $T = 850$  K(b)  $\phi = 0.75$ ,  $p = 30$  atm,  $T = 850$  K(c)  $\phi = 2.0$ ,  $p = 30$  atm,  $T = 850$  K

**Fig. 18.** Flux analysis of NO formations for 50% H<sub>2</sub>/50% CO in air mixtures at 30 atm under different equivalence ratios. The reaction time corresponds to 20% of hydrogen consumption. (a)  $\phi = 0.3$ ; (b)  $\phi = 0.75$ ; (c)  $\phi = 2.0$ .

compared to others. It is suggested that the reason for the different simulation results by different mechanisms may be three-fold: a) different hydrogen/CO chemical kinetics, b) different NO<sub>x</sub> chemistry and c) different thermochemistry for the species. Therefore, only updating one of these either the kinetic parameters as part of the sub-mechanisms or the thermochemistry of the species may not result in a high-fidelity model.

An open question proposed by Dayma and Dagaut [28] in 2008 was that the kinetic model was not able to capture the fall-off behavior of NO concentration with increasing temperatures at low pressures (1.0 atm) and this issue also pertains to the current literature models. We found that HON chemistry ap-

pears to be a promising way to resolve this problem through R32:  $\text{HON} + \text{H} = \text{OH} + \text{NH}$  in competition for H atoms with R26 ( $\text{HNO} + \text{H} = \text{NO} + \text{H}_2$ ) which reduces the rate of NO formation at low pressures. However, further experimental and/or theoretical research of HON chemistry is recommended to better explore its kinetic role in combustion mechanisms.

The proposed mechanism was also used to simulate NO formation at practical gas-turbine conditions. We found that a change in pressure does not effectively control the formation of NO during fuel oxidation/ignition rather that changes in temperature and equivalence ratio appear to provide a better strategy. By contrast, controlling the equivalence ratio appears to be a more efficient way of controlling NO formation, because the kinetic pathways that lead to its formation/consumption are more sensitivity to the variations in equivalence ratio.

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## Supplementary materials

Supplementary material associated with this article can be found, in the online version, at [doi:10.1016/j.combustflame.2017.03.019](https://doi.org/10.1016/j.combustflame.2017.03.019).

## References

- [1] S. Bhaduri, B. Berger, M. Pochet, H. Jeanmart, F. Contino, HCCI engine operated with unscrubbed biomass syngas, *Fuel Process. Technol.* 157 (2017) 52–58.
- [2] J. Wünnig, J. Wünnig, Flameless oxidation to reduce thermal NO-formation, *Prog. Energy Combust. Sci.* 23 (1997) 81–94.
- [3] H. Omidvarborna, A. Kumar, D.-S. Kim, NO<sub>x</sub> emissions from low-temperature combustion of biodiesel made of various feedstocks and blends, *Fuel Process. Technol.* 140 (2015) 113–118.
- [4] R. Burch, J. Breen, F. Meunier, A review of the selective reduction of NO<sub>x</sub> with hydrocarbons under lean-burn conditions with non-zeolitic oxide and platinum group metal catalysts, *Appl. Catal. B* 39 (2002) 283–303.
- [5] L. Muzio, G. Quartucci, J. Cichanowicz, Overview and status of post-combustion NO<sub>x</sub> control: SNCR, SCR and hybrid technologies, *Int. J. Environ. Pollut.* 17 (2002) 4–30.
- [6] T. Yamamoto, M. Okubo, K. Hayakawa, K. Kitaura, Towards ideal NO<sub>x</sub> control technology using a plasma-chemical hybrid process, *IEEE Trans. Ind. Appl.* 37 (2001) 1492–1498.
- [7] X. Tazua, A. Maiboom, S.R. Shah, Experimental study of inlet manifold water injection on combustion and emissions of an automotive direct injection Diesel engine, *Energy* 35 (2010) 3628–3639.
- [8] O. Mathieu, A. Levacque, E. Petersen, Effects of NO<sub>2</sub> addition on hydrogen ignition behind reflected shock waves, *Proc. Combust. Inst.* 34 (2013) 633–640.
- [9] C.L. Rasmussen, J. Hansen, P. Marshall, P. Glarborg, Experimental measurements and kinetic modeling of CO/H<sub>2</sub>/O<sub>2</sub>/NO<sub>x</sub> conversion at high pressure, *Int. J. Chem. Kinet.* 40 (2008) 454–480.
- [10] M. Mueller, R. Yetter, F. Dryer, Flow reactor studies and kinetic modeling of the H<sub>2</sub>/O<sub>2</sub>/NO<sub>x</sub> and CO/H<sub>2</sub>O/O<sub>2</sub>/NO<sub>x</sub> reactions, *Int. J. Chem. Kinet.* 31 (1999) 705–724.
- [11] J.-B. Masurier, F. Foucher, G. Dayma, P. Dagaut, Investigation of iso-octane combustion in a homogeneous charge compression ignition engine seeded by ozone, nitric oxide and nitrogen dioxide, *Proc. Combust. Inst.* 35 (2015) 3125–3132.
- [12] F. Contino, F. Foucher, P. Dagaut, T. Lucchini, G. D'Errico, C. Mounaïm-Rousselle, Experimental and numerical analysis of nitric oxide effect on the ignition of iso-octane in a single cylinder HCCI engine, *Combust. Flame* 160 (2013) 1476–1483.
- [13] A. Konnov, Implementation of the NCN pathway of prompt-NO formation in the detailed reaction mechanism, *Combust. Flame* 156 (2009) 2093–2105.
- [14] L. Moskaleva, M. Lin, The spin-conserved reaction CH+N→H+NCN: a major pathway to prompt NO studied by quantum/statistical theory calculations and kinetic modeling of rate constant, *Proc. Combust. Inst.* 28 (2000) 2393–2401.
- [15] S.F. Ahmed, J. Santner, F.L. Dryer, B. Padak, T.I. Farouk, Computational Study of NO<sub>x</sub> Formation at Conditions Relevant to Gas Turbine Operation, Part 2: NO<sub>x</sub> in High Hydrogen Content Fuel Combustion at Elevated Pressure, *Energy Fuels* 30 (2016) 7691–7703.
- [16] O. Mathieu, M. Kopp, E. Petersen, Shock-tube study of the ignition of multi-component syngas mixtures with and without ammonia impurities, *Proc. Combust. Inst.* 34 (2013) 3211–3218.

- [17] C.T. Bowman, Investigation of nitric oxide formation kinetics in combustion processes: the hydrogen-oxygen-nitrogen reaction, *Combust. Sci. Technol.* 3 (1971) 37–45.
- [18] O. Mathieu, A. Levacque, E. Petersen, Effects of  $N_2O$  addition on the ignition of  $H_2$ - $O_2$  mixtures: experimental and detailed kinetic modeling study, *Int. J. Hydrogen Energy* 37 (2012) 15393–15405.
- [19] R. Mével, S. Javoy, F. Lafosse, N. Chaumeix, G. Dupré, C.-E. Paillard, Hydrogen-nitrous oxide delay times: Shock tube experimental study and kinetic modelling, *Proc. Combust. Inst.* 32 (2009) 359–366.
- [20] S. Javoy, R. Mével, C. Paillard, A study of  $N_2O$  decomposition rate constant at high temperature: Application to the reduction of nitrous oxide by hydrogen, *Int. J. Chem. Kinet.* 41 (2009) 357–375.
- [21] A. Zuev, A.Y. Starikovskii, Reactions involving nitrogen oxides. Unimolecular  $N_2O$  decomposition, *Sov. J. Chem. Phys.* 10 (1992) 80–99.
- [22] I. Kosarev, S. Starikovskaia, A.Y. Starikovskii, The kinetics of autoignition of rich  $N_2O$ - $H_2$ - $O_2$ -Ar mixtures at high temperatures, *Combust. Flame* 151 (2007) 61–73.
- [23] H. Henrici, S. Bauer, Kinetics of the nitrous oxide-hydrogen reaction, *J. Chem. Phys.* 50 (1969) 1333–1342.
- [24] Y. Hidaka, H. Takuma, M. Suga, Shock-tube study of the rate constant for excited hydroxyl ( $OH^*(2, \Sigma, \text{SIGMA}^+)$ ) formation in the nitrous oxide-molecular hydrogen reaction, *J. Chem. Phys.* 89 (1985) 4903–4905.
- [25] K.M. Pamidimukkala, G.B. Skinner, Resonance absorption measurements of atom concentrations in reacting gas mixtures. VIII. Rate constants for  $O+H_2 \rightarrow OH+H$  and  $O+D_2 \rightarrow OD+D$  from measurements of O atoms in oxidation of  $H_2$  and  $D_2$  by  $N_2O$ , *J. Chem. Phys.* 76 (1982) 311–315.
- [26] A. Borisov, G. Skachkov, Spontaneous ignition of nitrous oxide, *Kinet. Catalysis* 13 (1972) 42–47.
- [27] M. Kopp, M. Brower, O. Mathieu, E. Petersen, F. Güthe,  $CO_2^*$  chemiluminescence study at low and elevated pressures, *Appl. Phys. B* 107 (2012) 529–538.
- [28] G. Dayma, P. Dagaut, Effects of air contamination on the combustion of hydrogen—effect of NO and  $NO_2$  addition on hydrogen ignition and oxidation kinetics, *Combust. Sci. Technol.* 178 (2006) 1999–2024.
- [29] P. Dagaut, A. Nicolle, Experimental study and detailed kinetic modeling of the effect of exhaust gas on fuel combustion: mutual sensitization of the oxidation of nitric oxide and methane over extended temperature and pressure ranges, *Combust. Flame* 140 (2005) 161–171.
- [30] P. Dagaut, F. Lecomte, J. Mieritz, P. Glarborg, Experimental and kinetic modeling study of the effect of NO and  $SO_2$  on the oxidation of CO- $H_2$  mixtures, *Int. J. Chem. Kinet.* 35 (2003) 564–575.
- [31] M. Abian, M.U. Alzueta, P. Glarborg, Formation of NO from  $N_2/O_2$  Mixtures in a Flow Reactor: Toward an Accurate Prediction of Thermal NO, *Int. J. Chem. Kinet.* 47 (2015) 518–532.
- [32] P. Glarborg, D. Kubel, P.G. Kristensen, J. Hansen, K. Dam-Johansen, Interactions of CO,  $NO_x$ , and  $H_2O$  under post-flame conditions, *Combust. Sci. Technol.* 110 (1995) 461–485.
- [33] R. Mével, F. Lafosse, N. Chaumeix, G. Dupré, C.-E. Paillard, Spherical expanding flames in  $H_2$ - $N_2O$ -Ar mixtures: flame speed measurements and kinetic modeling, *Int. J. Hydrogen Energy* 34 (2009) 9007–9018.
- [34] S. Bane, R. Mével, S. Coronel, J. Shepherd, Flame burning speeds and combustion characteristics of undiluted and nitrogen-diluted hydrogen-nitrous oxide mixtures, *Int. J. Hydrogen Energy* 36 (2011) 10107–10116.
- [35] P. Dagaut, F. Lecomte, S. Chevailler, M. Cathonnet, Experimental and detailed kinetic modeling of nitric oxide reduction by a natural gas blend in simulated reburning conditions, *Combust. Sci. Technol.* 139 (1998) 329–363.
- [36] D. Baulch, C. Cobos, R. Cox, P. Frank, G. Hayman, T. Just, J. Kerr, T. Murrells, M. Pilling, J. Troe, Evaluated kinetic data for combustion modeling. Supplement I, *J. Phys. Chem. Ref. Data* 23 (1994) 847–848.
- [37] W. Tsang, Chemical kinetic data base for propellant combustion. II. Reactions involving CN, NCO, and HNC, *J. Phys. Chem. Ref. Data* 21 (1992) 753–791.
- [38] W. Tsang, J.T. Herron, Chemical kinetic data base for propellant combustion I. Reactions involving NO,  $NO_2$ , HNO,  $HNO_2$ , HCN and  $N_2O$ , *J. Phys. Chem. Ref. Data* 20 (1991) 609–663.
- [39] S.J. Klippenstein, L.B. Harding, P. Glarborg, J.A. Miller, The role of NNH in NO formation and control, *Combust. Flame* 158 (2011) 774–789.
- [40] J. Chai, C.F. Goldsmith, Rate coefficients for fuel+  $NO_2$ : Predictive kinetics for HONO and  $HNO_2$  formation, *Proc. Combust. Inst.* 36 (2017) 617–626.
- [41] A. Frassoldati, T. Faravelli, E. Ranzi, The ignition, Combust. Flame structure of carbon monoxide/hydrogen mixtures. Note 1: Detailed kinetic modeling of syngas combustion also in presence of nitrogen compounds, *Int. J. Hydrogen Energy* 32 (2007) 3471–3485.
- [42] G.P. Smith, D.M. Golden, M. Frenklach, N.W. Moriarty, B. Eiteneer, M. Goldenberg, C.T. Bowman, R.K. Hanson, S. Song, W.C. Gardiner Jr, URL: [http://www.me.berkeley.edu/gri\\_mech](http://www.me.berkeley.edu/gri_mech), 51 (1999) 55.
- [43] U.C.S. Diego, Chemical-Kinetic Mechanisms for Combustion Applications, San Diego Mechanism web page, Mechanical and Aerospace Engineering (Combustion Research), University of California at San Diego (<http://combustion.ucsd.edu>).
- [44] J.A. Miller, C.T. Bowman, Mechanism and modeling of nitrogen chemistry in combustion, *Prog. Energy Combust. Sci.* 15 (1989) 287–338.
- [45] F. Deng, F. Yang, P. Zhang, Y. Pan, J. Bugler, H.J. Curran, Y. Zhang, Z. Huang, Towards a kinetic understanding of the NO<sub>x</sub> promoting-effect on ignition of coalbed methane: A case study of methane/nitrogen dioxide mixtures, *Fuel* 181 (2016) 188–198.
- [46] J.F. Roessler, R.A. Yetter, F.L. Dryer, Kinetic interactions of CO, NO<sub>x</sub>, and HCl emissions in postcombustion gases, *Combust. Flame* 100 (1995) 495–504.
- [47] J. Bromly, F. Barnes, P. Nelson, B. Haynes, Kinetics and modeling of the  $H_2$ - $O_2$ - $NO_x$  system, *Int. J. Chem. Kinet.* 27 (1995) 1165–1178.
- [48] A.A. Konnov, J.D. Ruyck, A Possible new route for NO formation via  $N_2H_3$ , *Combust. Sci. Technol.* 168 (2001) 1–46.
- [49] A. Konnov, G. Colson, J. De Ruyck, NO formation rates for hydrogen combustion in stirred reactors, *Fuel* 80 (2001) 49–65.
- [50] J.W. Bozzelli, A.M. Dean, O+NNH: A possible new route for  $NO_x$  formation in flames, *Int. J. Chem. Kinet.* 27 (1995) 1097–1109.
- [51] M. Slack, A. Grillo, Investigation of hydrogen-air ignition sensitized by nitric oxide and by nitrogen dioxide, NASA Report CR-2896 (1977).
- [52] G.M. Watson, J.D. Munzar, J.M. Berghthorson, Diagnostics and modeling of stagnation flames for the validation of thermochemical combustion models for  $NO_x$  predictions, *Energy Fuels* 27 (2013) 7031–7043.
- [53] Z. Tian, Y. Li, L. Zhang, P. Glarborg, F. Qi, An experimental and kinetic modeling study of premixed  $NH_3/CH_4/O_2/Ar$  flames at low pressure, *Combust. Flame* 156 (2009) 1413–1426.
- [54] M.P. Burke, M. Chaos, Y. Ju, F.L. Dryer, S.J. Klippenstein, Comprehensive  $H_2/O_2$  kinetic model for high-pressure combustion, *Int. J. Chem. Kinet.* 44 (2012) 444–474.
- [55] H. Hashemi, J.M. Christensen, S. Gersen, P. Glarborg, Hydrogen oxidation at high pressure and intermediate temperatures: experiments and kinetic modeling, *Proc. Combust. Inst.* 35 (2015) 553–560.
- [56] W.K. Metcalfe, S.M. Burke, S.S. Ahmed, H.J. Curran, A hierarchical and comparative kinetic modeling study of C1–C2 hydrocarbon and oxygenated fuels, *Int. J. Chem. Kinet.* 45 (2013) 638–675.
- [57] A. Kéromnès, W.K. Metcalfe, K.A. Heufer, N. Donohoe, A.K. Das, C.-J. Sung, J. Herzler, C. Naumann, P. Griebel, O. Mathieu, An experimental and detailed chemical kinetic modeling study of hydrogen and syngas mixture oxidation at elevated pressures, *Combust. Flame* 160 (2013) 995–1011.
- [58] J. Bugler, K.P. Somers, J.M. Simmie, F. Güthe, H.J. Curran, Modeling Nitrogen Species as Pollutants: Thermochemical Influences, *J. Phys. Chem. A* 120 (2016) 7192–7197.
- [59] P. Dagaut, P. Glarborg, M.U. Alzueta, The oxidation of hydrogen cyanide and related chemistry, *Prog. Energy Combust. Sci.* 34 (2008) 1–46.
- [60] R.E. Weston Jr, T.L. Nguyen, J.F. Stanton, J.R. Barker, HO+CO reaction rates and H/D kinetic isotope effects: Master equation models with ab initio SCTST rate constants, *J. Phys. Chem. A* 117 (2013) 821–835.
- [61] T.L. Nguyen, B.C. Xue, R.E. Weston Jr, J.R. Barker, J.F. Stanton, Reaction of HO with CO: Tunneling is indeed important, *J. Phys. Chem. Lett.* 3 (2012) 1549–1553.
- [62] H.G. Yu, J.T. Muckerman, Quantum molecular dynamics study of the reaction of  $O_2$  with HOCO, *J. Phys. Chem. A* 110 (2006) 5312–5316.
- [63] H.G. Yu, J.T. Muckerman, J.S. Francisco, Direct ab initio dynamics study of the OH+ HOCO reaction, *J. Phys. Chem. A* 109 (2005) 5230–5236.
- [64] H.G. Yu, J.S. Francisco, Energetics and kinetics of the reaction of HOCO with hydrogen atoms, *J. Chem. Phys.* 128 (2008) 244315.
- [65] H.G. Yu, J.T. Muckerman, J.S. Francisco, Quantum force molecular dynamics study of the reaction of O atoms with HOCO, *J. Chem. Phys.* 127 (2007) 094302.
- [66] H.G. Yu, G. Poggi, J.S. Francisco, J.T. Muckerman, Energetics and molecular dynamics of the reaction of HOCO with  $HO_2$  radicals, *J. Chem. Phys.* 129 (2008) pp. 214307–214307.
- [67] H.G. Yu, J.S. Francisco, Theoretical Study of the Reaction of  $CH_3$  with HOCO Radicals, *J. Phys. Chem. A* 113 (2009) 3844–3849.
- [68] J.S. Francisco, J.T. Muckerman, H.G. Yu, HOCO radical chemistry, *Acc. Chem. Res.* 43 (2010) 1519–1526.
- [69] G. Poggi, J.S. Francisco, An ab initio study of the reaction of HOCO radicals with  $NO_2$ : addition/elimination mechanism, *J. Chem. Phys.* 130 (2009) 124306.
- [70] G. Poggi, J.S. Francisco, An ab initio study of the competing reaction channels in the reaction of HOCO radicals with NO and  $O_2$ , *J. Chem. Phys.* 120 (2004) 5073–5080.
- [71] Y.B. Zeldovich, The oxidation of nitrogen in combustion and explosions, *Acta Physicochim. URSS* 21 (1946) 577–628.
- [72] D. Baulch, C. Bowman, C. Cobos, R. Cox, T. Just, J. Kerr, M. Pilling, D. Stocker, J. Troe, W. Tsang, Evaluated kinetic data for combustion modeling: supplement II, *J. Phys. Chem. Ref. Data* 34 (2005) 757–1397.
- [73] S. Klippenstein, L. Harding, B. Ruscic, R. Sivaramakrishnan, N. Srinivasan, M.C. Su, J. Michael, Thermal Decomposition of  $NH_2OH$  and Subsequent Reactions: Ab Initio Transition State Theory and Reflected Shock Tube Experiments, *J. Phys. Chem. A* 113 (2009) 10241–10259.
- [74] K. Becker, W. Groth, D. Kley, The rate constant of the aeronomical reaction  $N+O_2$ , *Z. Naturforschung A* 24 (1969) 1280–1281.
- [75] W. Wilson, Rate constant for the reaction  $N+O_2 \rightarrow NO+O$ , *J. Chem. Phys.* 46 (1967) 2017–2018.
- [76] A.S. Vlastaras, C. Winkler, Reaction of active nitrogen with oxygen, *Can. J. Chem.* 45 (1967) 2837–2840.
- [77] M. Clyne, B. Thrush, Kinetics of the reactions of active nitrogen with oxygen and with nitric oxide, *Proceedings of the Royal Society of London A: Mathematical, Phys. Eng. Sci.* 261 (1961) 259–273.
- [78] J.A. Miller, M.C. Branch, W.J. McLean, D.V. Chandler, M.D. Smooke, R.J. Kee, The conversion of HCN to NO and  $N_2$  in  $H_2$ - $O_2$ -HCN-Ar flames at low pressure, *Symp. (Int.) Combust.* 20 (1985) 673–684.
- [79] M.J. Howard, I.W. Smith, Direct rate measurements on the reactions  $N+OH \rightarrow NO+H$  and  $O+OH \rightarrow O_2+H$  from 250 to 515 K, *J. Chem. Soc. Faraday Transactions 2: Molecular and Chemical Physics* 77 (1981) 997–1008.



- [80] T. Ko, A. Fontijn, High-temperature photochemistry kinetics study of the reaction hydrogen atom+ nitrogen dioxide. *farw. hydroxyl+ nitric oxide* from 296 to 760 K, *J. Phys. Chem* 95 (1991) 3984–3987.
- [81] C.J. Howard, Kinetic study of the equilibrium  $\text{HO}_2 + \text{NO} \rightleftharpoons \text{OH} + \text{NO}_2$  and the thermochemistry of  $\text{HO}_2$ , *J. Am. Chem. Soc* 102 (1980) 6937–6941.
- [82] L.M. Avallone, Measurements of the temperature-dependent rate coefficient for the reaction  $\text{O}(^3\text{P}) + \text{NO}_2 \rightarrow \text{NO} + \text{O}_2$ , *J. Photochem. Photobiol. A* 157 (2003) 231–236.
- [83] P.P. Bemand, M.A. Clyne, R.T. Watson, Atomic resonance fluorescence and mass spectrometry for measurements of the rate constants for elementary reactions:  $\text{O}(^3\text{P}) + \text{NO}_2 \rightarrow \text{NO} + \text{O}_2$  and  $\text{NO} + \text{O}_3 \rightarrow \text{NO}_2 + \text{O}_2$ , *J. Chem. Soc. Faraday Trans. 2* 70 (1974) 564–576.
- [84] E. Estupinan, J. Nicovich, P. Wine, A temperature-dependent kinetics study of the important stratospheric reaction  $\text{O}(^3\text{P}) + \text{NO}_2 \rightarrow \text{O}_2 + \text{NO}$ , *J. Phys. Chem. A* 105 (2001) 9697–9703.
- [85] R. Geers-Müller, F. Stuhl, On the kinetics of the reactions of oxygen atoms with  $\text{NO}_2$ ,  $\text{N}_2\text{O}_4$ , and  $\text{N}_2\text{O}_3$  at low temperatures, *Chem. Phys. Lett* 135 (1987) 263–268.
- [86] B.A. Shiekh, D. Kaur, B. Seth, S. Mahajan, The theoretical-cum-statistical approach for the investigation of reaction  $\text{NO}_2 + \text{O}(^3\text{P}) \rightarrow \text{NO} + \text{O}_2$  using SCTST and a full anharmonic VPT2 model, *Chem. Phys. Lett* 662 (2016) 244–249.
- [87] P. Glarborg, M. Alzueta, K. Kjærgaard, K. Dam-Johansen, Oxidation of formaldehyde and its interaction with nitric oxide in a flow reactor, *Combust. Flame* 132 (2003) 629–638.
- [88] J. Park, N.D. Giles, J. Moore, M. Lin, A comprehensive kinetic study of thermal reduction of  $\text{NO}_2$  by  $\text{H}_2$ , *J. Phys. Chem. A* 102 (1998) 10099–10105.
- [89] H. Freund, H. Palmer, Shock-tube studies of the reactions of  $\text{NO}_2$  with  $\text{NO}_2$ ,  $\text{SO}_2$ , and  $\text{CO}$ , *Int. J. Chem. Kinet* 9 (1977) 887–905.
- [90] D. Milks, T. Adams, R. Matula, Single pulse shock tube study of the reaction between nitrogen dioxide ( $\text{NO}_2$ ) and carbon monoxide ( $\text{CO}$ ), *Combust. Sci. Technol* 19 (1979) 151–159.
- [91] S.K. Ross, J.W. Sutherland, S.-C. Kuo, R.B. Klemm, Rate Constants for the Thermal Dissociation of  $\text{N}_2\text{O}$  and the  $\text{O}(^3\text{P}) + \text{N}_2\text{O}$  Reaction, *J. Phys. Chem. A* 101 (1997) 1104–1116.
- [92] W.D. Breshers, Falloff behavior in the thermal dissociation rate of  $\text{N}_2\text{O}$ , *J. Phys. Chem* 99 (1995) 12529–12535.
- [93] M. Röhrig, E.L. Petersen, D.F. Davidson, R.K. Hanson, The pressure dependence of the thermal decomposition of  $\text{N}_2\text{O}$ , *Int. J. Chem. Kinet* 28 (1996) 599–608.
- [94] A.H. Chang, D.R. Yarkony, On the electronic structure aspects of spin-forbidden processes in  $\text{N}_2\text{O}$ , *J. Phys. Chem* 99 (1993) 6824–6831.
- [95] A. Zuev, A. Starikovskii, Reactions involving nitrogen oxides at high temperature: the unimolecular decay of  $\text{N}_2\text{O}$ , *Khim. Fiz* 10 (1991) 52–63.
- [96] R. Mevel, F. Lafosse, L. Catoire, N. Chaumeix, G. Dupre, C.E. Paillard, Induction delay times and detonation cell size prediction of hydrogen-nitrous oxide-diluent mixtures, *Combust. Sci. Technol* 180 (2008) 1858–1875.
- [97] P. Marshall, A. Fontijn, C.F. Melius, High-temperature photochemistry and BAC-MP4 studies of the reaction between ground-state H atoms and  $\text{N}_2\text{O}$ , *J. Chem. Phys* 86 (1987) 5540–5549.
- [98] A.M. Dean, J.W. Bozzelli, Combustion chemistry of nitrogen, Gas-phase combustion chemistry, Springer, 2000, pp. 125–341.
- [99] D. Davidson, M. DiRosa, A. Chang, R. Hanson, Shock tube measurements of the major product channels of  $\text{N}_2\text{O} + \text{O}$ , *Shock Waves* 2 (1992) 813–818.
- [100] N.E. Meagher, W.R. Anderson, Kinetics of the  $\text{O}(^3\text{P}) + \text{N}_2\text{O}$  Reaction. 2. Interpretation and Recommended Rate Coefficients, *J. Phys. Chem. A* 104 (2000) 6013–6031.
- [101] A. Fontijn, A. Goumri, A. Fernandez, W.R. Anderson, N.E. Meagher, Kinetics of the  $\text{O}(^3\text{P}) + \text{N}_2\text{O}$  Reaction. 1. Direct Measurements at Intermediate Temperatures, *J. Phys. Chem. A* 104 (2000) 6003–6012.
- [102] A. Mebel, M. Lin, K. Morokuma, C. Melius, Theoretical study of reactions of  $\text{N}_2\text{O}$  with NO and OH radicals, *Int. J. Chem. Kinet* 28 (1996) 693–703.
- [103] J. Hahn, K. Luther, J. Troe, Experimental and theoretical study of the temperature and pressure dependences of the recombination reactions  $\text{O} + \text{NO}_2 (+\text{M}) \rightarrow \text{NO}_3 (+\text{M})$  and  $\text{NO}_2 + \text{NO}_3 (+\text{M}) \rightarrow \text{N}_2\text{O}_5 (+\text{M})$ , *Phys. Chem. Chem. Phys* 2 (2000) 5098–5104.
- [104] L.B. Harding, H. Stark, J. Troe, V.G. Ushakov, New studies of the unimolecular reaction  $\text{NO}_2 + \text{NO}$ . Part 2. Relation between high pressure rate constants and potential parameters, *Phys. Chem. Chem. Phys* 1 (1999) 63–72.
- [105] R. Atkinson, D. Baulch, R. Cox, R. Hampson, J. Kerr, J. Troe, Evaluated kinetic and photochemical data for atmospheric chemistry: Supplement IV: IUPAC subcommittee on gas kinetic data evaluation for atmospheric chemistry, *Atmos. Environ. Part A: Gen. Top* 26 (1992) 1187–1230.
- [106] E. Becker, M. Rahman, R. Schindler, Determination of the rate constants for the gas phase reactions of  $\text{NO}_3$  with H, OH and  $\text{HO}_2$  radicals at 298 K, *Ber. Bunsenges. phys. Chem* 96 (1992) 776–783.
- [107] P. Glarborg, M. Østberg, M.U. Alzueta, K. Dam-Johansen, J.A. Miller, The recombination of hydrogen atoms with nitric oxide at high temperatures, *Symp. (Int.) Combust* 27 (1998) 219–226.
- [108] M.T. Allen, R.A. Yetter, F.L. Dryer, Hydrogen/nitrous oxide kinetics—Implications of the  $\text{N}_x\text{H}_y$  species, *Combust. Flame* 112 (1998) 302–311.
- [109] P.S. Riley, B. Cosic, A. Fontijn, The H+NO recombination reaction over a wide temperature range, *Int. J. Chem. Kinet* 35 (2003) 374–380.
- [110] M.R. Soto, M. Page, Ab initio variational transition-state-theory reaction-rate calculations for the gas-phase reaction  $\text{H} + \text{HNO} \rightarrow \text{H}_2 + \text{NO}$ , *J. Chem. Phys* 97 (1992) 7287–7296.
- [111] H.M.T. Nguyen, S. Zhang, J. Peeters, T.N. Truong, M.T. Nguyen, Direct ab initio dynamics studies of the reactions of HNO with H and OH radicals, *Chem. Phys. Lett* 388 (2004) 94–99.
- [112] M.R. Soto, M. Page, M.L. McKee, Theoretical study of the reaction of OH with HNO, *Chem. Phys* 153 (1991) 415–426.
- [113] S. Inomata, N. Washida, Rate constants for the reactions of  $\text{NH}_2$  and HNO with atomic oxygen at temperatures between 242 and 473 K, *J. Phys. Chem. A* 103 (1999) 5023–5031.
- [114] A. Mebel, M. Lin, K. Morokuma, Ab initio MO and TST calculations for the rate constant of the  $\text{HNO} + \text{NO}_2 \rightarrow \text{HONO} + \text{NO}$  reaction, *Int. J. Chem. Kinet* 30 (1998) 729–736.
- [115] N. Faßheber, M.C. Schmidt, G. Friedrichs, Quantitative HNO detection behind shock waves, *Proc. Combust. Inst* 36 (2017) 607–615.
- [116] D. Fulle, H. Hamann, H. Hippler, J. Troe, Temperature and pressure dependence of the addition reactions of HO to NO and to  $\text{NO}_2$ , *J. Chem. Phys* 108 (1998) 5391–5397.
- [117] R. Atkinson, D. Baulch, R. Cox, J. Crowley, R. Hampson, R. Hynes, M. Jenkin, M. Rossi, J. Troe, Evaluated kinetic and photochemical data for atmospheric chemistry: Volume I - gas phase reactions of  $\text{O}_x$ ,  $\text{HO}_x$ ,  $\text{NO}_x$  and  $\text{SO}_x$  species, *Atmos. Chem. Phys* 4 (2004) 1467–1738.
- [118] C.C. Hsu, M. Lin, A. Mebel, C. Melius, Ab initio study of the H+HONO reaction: direct abstraction versus indirect exchange processes, *J. Phys. Chem. A* 101 (1997) 60–66.
- [119] W. Xia, M. Lin, Ab initio MO/statistical theory prediction of the OH+HONO reaction rate: evidence for the negative temperature dependence, *PhysChemComm* 3 (2000) 71–78.
- [120] J.B. Burkholder, A. Mellouki, R. Talukdar, A. Ravishankara, Rate coefficients for the reaction of OH with HONO between 298 and 373 K, *Int. J. Chem. Kinet* 24 (1992) 711–725.
- [121] D.Q. Wang, J.L. Li, X.R. Huang, C.Y. Geng, C.C. Sun, OH+ HONO reaction: A theoretical study, *J. Mol. Struct. THEOCHEM* 847 (2007) 10–22.
- [122] X. Lu, J. Park, M. Lin, Gas phase reactions of HONO with  $\text{NO}_2$ ,  $\text{O}_3$ , and HCl: ab initio and TST study, *J. Phys. Chem. A* 104 (2000) 8730–8738.
- [123] A. Mebel, M. Lin, C. Melius, Rate constant of the  $\text{HONO} + \text{HONO} \rightarrow \text{H}_2\text{O} + \text{NO} + \text{NO}_2$  reaction from ab initio MO and TST calculations, *J. Phys. Chem. A* 102 (1998) 1803–1807.
- [124] S.-y. Takane, T. Fueno, Electronic structure and the hydrogen-shift isomerization of hydrogen nitril  $\text{HNO}_2$ , *Theor. Chim. Acta* 87 (1994) 431–439.
- [125] X. Lu, R.N. Musin, M. Lin, Gas-phase reactions of HONO with HNO and  $\text{NH}_3$ : an ab initio MO/TST study, *J. Phys. Chem. A* 104 (2000) 5141–5148.
- [126] C. Eckart, The penetration of a potential barrier by electrons, *Physical Review* 35 (1930) 1303.
- [127] R. Asatryan, J.W. Bozzelli, J.M. Simmie, Thermochemistry for enthalpies and reaction paths of nitrous acid isomers, *Int. J. Chem. Kinet* 39 (2007) 378–398.
- [128] J. Troe, Refined Representation of Falloff Curves for the Reaction  $\text{HO} + \text{NO}_2 + \text{N}_2 \rightarrow (\text{HONO}_2, \text{HOONO}) + \text{N}_2$ , *J. Phys. Chem. A* 116 (2012) 6387–6393.
- [129] J. Troe, Analysis of the temperature and pressure dependence of the reaction  $\text{HO} + \text{NO}_2 + \text{M} \rightleftharpoons \text{HONO}_2 + \text{M}$ , *Int. J. Chem. Kinet* 33 (2001) 878–889.
- [130] H. Hippler, S. Nasterlack, F. Striebel, Reaction of  $\text{OH} + \text{NO}_2 + \text{M}$ : Kinetic evidence of isomer formation, *Phys. Chem. Chem. Phys* 4 (2002) 2959–2964.
- [131] W. Xia, M. Lin, A multifacet mechanism for the  $\text{OH} + \text{HNO}_3$  reaction: An ab initio molecular orbital/statistical theory study, *J. Phys. Chem* 114 (2001) 4522–4532.
- [132] S.S. Brown, R.K. Talukdar, A. Ravishankara, Reconsideration of the rate constant for the reaction of hydroxyl radicals with nitric acid, *J. Phys. Chem. A* 103 (1999) 3031–3037.
- [133] S.S. Brown, J.B. Burkholder, R.K. Talukdar, A. Ravishankara, Reaction of hydroxyl radical with nitric acid: Insights into its mechanism, *J. Phys. Chem. A* 105 (2001) 1605–1614.
- [134] G. Poskrebyshev, P. Neta, R.E. Huie, Equilibrium constant of the reaction  $\text{OH} + \text{HNO}_3 \rightleftharpoons \text{H}_2\text{O} + \text{NO}_3$  in aqueous solution, *J. Geophys. Res.: Atmos* 106 (2001) 4995–5004.
- [135] R. Atkinson, D. Baulch, R. Cox, R. Hampson Jr, J. Kerr, M. Rossi, J. Troe, Evaluated kinetic and photochemical data for atmospheric chemistry: supplement VI. IUPAC subcommittee on gas kinetic data evaluation for atmospheric chemistry, *J. Phys. Chem. Ref. Data* 26 (1997) 1329–1499.
- [136] J.J. Lamb, M. Mozurkewich, S.W. Benson, Negative activation energies and curved Arrhenius plots. 3. Hydroxyl+ nitric acid and hydroxyl+peroxynitric acid, *J. Phys. Chem* 88 (1984) 6441–6448.
- [137] O. Mathieu, E.L. Petersen, Experimental and modeling study on the high-temperature oxidation of Ammonia and related  $\text{NO}_x$  chemistry, *Combust. Flame* 162 (2015) 554–570.
- [138] A. Borisov, V. Zamanskii, G. Skachkov, Kinetics and mechanism of reaction of hydrogen with nitrous oxide, *Kinet. Catal* 13 (1978) 42–47.