# Ions in an AC Electric Field: Strong Long-Range Repulsion between Oppositely Charged Surfaces

# Data S2

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# The Data S2 Content

The Data set S2 should contain

- shortManual.pdf this file. The short manual on how to use the code;
- electrokinFOAM the folder containing the OpenFOAM solver for solving the coupled Poisson-Nernst-Planck equations for two ions in solution;
- electrokinBC the folder containing the no flux boundary conditions
- oneDimCase the folder containing the case.

The solver and the boundary conditions were written, tested and used under foam-ext-3.2 distribution of the OpenFOAM library.

# Installation guide

To install the solver and the boundary conditions and to use them it is advised to have the foam-ext-3.2 version of the OpenFOAM. The has not been tested under other OpenFOAM distributions. Next, it is sufficient to first enter the electrokinFOAM folder and execute

#### wmake

command as for every standard OpenFOAM utility. The place of the installation can be changed by manipulating the content of

#### electrokinFOAM/Make/files

file. Similarly, the installation of the boundary conditions is done. It is sufficient to enter the electrokinBC folder and execute the

# wmake libso

command. To clean installation commands wclean in the electrokinFOAM folder and wlcean libso in the electrokinBC folder need to be executed.

# electrokinFOAM

The solver electrokinFOAM is written to solve the Poisson-Nernst-Planck system of PDEs for the evolution of the ion concentrations  $n_{\sigma}$  ( $\sigma = \pm$ )

$$\frac{\partial n_{\sigma}}{\partial t} = \nabla \cdot D_{\sigma} \left( \nabla n_{\sigma} + \sigma \frac{ez_{\sigma}}{k_B T} n_{\sigma} \nabla \phi \right), \tag{1a}$$

under the influence of the electric field with potential  $\phi$ 

$$\Delta \phi = -\frac{e}{\epsilon} \left( z_+ n_+ - z_- n_- \right), \tag{1b}$$

with diffusion constants  $D_{\sigma}$ , ionic valency  $z_{\sigma}$ , T is the temperature, e is the elementary charge and  $k_B$  Boltzmann's constant. The electric field is described by Poisson's equation.

The solver works iteratively in the time loop. The time step can be either fixed or controlled by the analog of Courant number Co, that is calculated based on the flux of ions through the boundaries of the computational cells. We found that the optimal performance of the code is when the time step is piecewise constant. In the case of adjustable time step we chose to modify it as it takes the value outside the interval  $(\hat{\text{Co}}/2,\hat{\text{Co}})$ , where  $\hat{\text{Co}}$  is the desired analog of Courant number. It can be specified as maxCo in the contolDict file.

In every time step the solver enters into the loop for solving the equations.

subdictionary in the fvSolution dictionary. For nOuterCorrIons= 1 the solver behaves in similar manner to the PISO algorithm for iterative solution of pressure-velocity coupling. In case nOuterCorrIons> 1 the solver becomes similar to PIMPLE algorithm.

The solver needs an additional dictionary physicalProperties in the constant folder specified. This dictionary contains physical constants necessary for the solution

```
epsilon0 [ -1 -3 4 0 0 2 0 ] <dielectric constant>;
epsilon0
           e [ 0 0 1 0 0 1 0]
                                         <elementary charge>;
nRef
           nRef [ 0 0 0 0 0 0 0]
                                         <reference concentration number n0>;
           muPlus [ -1 0 2 0 0 1 0]
muPlus
                                         <mobility coefficient of plus ion>;
muMinus
           muMinus [ -1 0 2 0 0 1 0]
                                         <mobility coefficient of plus ion>;
DPlus
           DPlus [ 0 2 -1 0 0 0 0]
                                         <diffusion coefficient of the plus ion>;
           DMinus [ 0 2 -1 0 0 0 0]
                                         <diffusion coefficient of the minus ion>;
DMinus
           ZPlus [ 0 0 0 0 0 0 0 ]
ZPlus
                                         <unsigned valency of the plus ion>;
ZMinus
           ZMinus [ 0 0 0 0 0 0 0 ]
                                         <unsigned valency of the minus ion>;
nMinimal
           nMinimal [ 0 -3 0 0 0 0 0 ]
                                         <lower boundary for the density fields>;
```

The nRef stands for the reference number that unit concentration has to be multiplied in order to get a real concentration value. For example in case of desired 1 mM concentration nRef should equal to  $6.022 \times 10^{23}$ . The relation between the mobility  $\mu$  and the diffusion coefficient D is given by

$$\mu_{\pm} = \frac{z_{\pm}eD}{k_BT}.\tag{2}$$

The nMinimal is used as the lower boundary of the concentration for the calculation of the analog of Co number.

All other parameters are specified in the same way as in other OpenFOAM solvers.

# electrokinBC

The no flux boundary conditions

$$\mathbf{j} = -D_{\sigma} \left( \nabla n_{\sigma} + \sigma \frac{z_{\sigma} e}{k_{B} T} n_{\sigma} \nabla \phi \right) = 0.$$
 (3)

are specified using the electrokinBC library. After successful compilation one has to add the

```
libs ( "electrokinBC.so" );
```

line at the end of the controlDict dictionary. After specifying the name of the additional library, the boundary condition can be used in the following form

```
type fixedFlux;
n <name of the corresponding ion concentration>;
sign <sign of the ion charge>;
D <diffusion coefficient>;
mu <mobility coefficient>;
gradient uniform 0.0;
value calculated;
}
```

Please use the values that correspond to the values specified in the physicalProperties dictionary. Otherwise the results will be wrong.

# oneDimCase

The oneDimCase is a complete example with already meshed geometry. It is sufficient to enter the folder and run

#### electrokinFOAM

The geometry is a non uniformly meshed realization of 1D segment. The mesh gets denser near the plateOne wall where no flux boundary conditions are applied. The total length of the segment is 0.5  $\mu$ m. At the plateOne boundary we apply the no flux boundary conditions for the ions and the oscillatory electric potential. At the plateTwo boundary we apply the bulk concentration boundary condition for the ions and constant zero potential. The oscillatory boundary condition for the potential is defined in the plateOne.dat source file for the timeVaryingUniformFixedValue boundary conditions.

The system is filled with the 1 mM solution of NaNO<sub>3</sub> salt. Specified are the physical values of valencies, diffusion coefficients and mobility coefficients. The concentration nRef is equal to  $6.022 \times 10^{23}$ . The initial concentration fields are specified in initial condition files for the ion concentrations 0/nPlus and 0/nMinus to be equal 1. In the case of the divalent electrolyte like  $\rm H_2SO_4$  this should be in the desired ratio e.g., 1 for nPlus and 0.5 for nMinus. During the calculations the ionic concentration fields are multiplied by the nRef.

In addition to the files needed for the solution we also provide a exemplary sampleDict file for probing the fields along the line.