

Module 22

Database Management Systems

Module 22: Relational Database Design/2

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Module Recap

Module 22

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Objectives & Outline

Dependencies

Armstrong's Axiom

- Identified the features of good relational design
- Familiarized with the First Normal Form

Module Objectives

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Objectives & Outline

Dependencies Armstrong's Axion

Module Summai

• To Introduce Functional Dependencies

Module Outline

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Objectives & Outline

Dependencies

Armstrong's Axion

Module Summar

Functional Dependencies



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Objectives of Outline

Functional Dependencies

Armstrong's Axion

Closure of FDs

Functional Dependencies

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Goal: Devise a Theory for Good Relations

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Objectives Outline Functional

Dependencies

Armstrong's Axioms

Closure of FDs

- Decide whether a particular relation *R* is in "good" form.
- In the case that a relation R is not in "good" form, decompose it into a set of relations $\{R_1, R_2, \ldots, R_n\}$ such that
 - each relation is in good form
 - o the decomposition is a lossless-join decomposition
- The theory is based on:
 - Functional dependencies
 - Multivalued dependencies
 - o Other dependencies



Functional Dependencies

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Functional Dependencies

- Constraints on the set of legal relations
- Require that the value for a certain set of attributes determines uniquely the value for another set of attributes
- A functional dependency is a generalization of the notion of a key

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Functional Dependencies (2)

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Objectives Outline

Functional Dependencies Armstrong's Axioms

Module Summa

• Let *R* be a relation schema

$$\alpha \subseteq \mathit{R}$$
 and $\beta \subseteq \mathit{R}$

The functional dependency or FD

$$\alpha \to \beta$$

holds on R if and only if for any legal relations r(R), whenever any two tuples t_1 and t_2 of r agree on the attributes α , they also agree on the attributes β . That is,

$$t_1[\alpha] = t_2[\alpha] \Rightarrow t_1[\beta] = t_2[\beta]$$

• Example: Consider r(A, B) with the following instance of r.

Α	В
1	4
1	5
3	7

• On this instance, $A \to B$ does **NOT** hold, but $B \to A$ does hold. So we cannot have tuples like (2, 4), or (3, 5), or (4, 7) added to the current instance.

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Functional Dependencies (3)

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Functional Dependencies

• K is a superkey for relation schema R if and only if $K \to R$

• K is a candidate key for R if and only if

- $\circ K \to R$ and
- \circ for no $\alpha \subset K$. $\alpha \to R$
- Functional dependencies allow us to express constraints that cannot be expressed using superkeys. Consider the schema:

inst_dept(ID, name, salary, dept_name, building, budget)

• We expect these functional dependencies to hold:

dept_name → building dept_name → budget

 $ID \rightarrow budget$

but would not expect the following to hold:

 $dept_name \rightarrow salary$



Functional Dependencies (4)

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Objectives Outline Functional

Dependencies Armstrong's Axioms

Closure of FDs

• We use functional dependencies to:

- o test relations to see if they are legal under a given set of functional dependencies.
 - ▶ If a relation r is legal under a set F of functional dependencies, we say that r satisfies F
- o specify constraints on the set of legal relations
 - ▶ We say that F holds on R if all legal relations on R satisfy the set of functional dependencies F
- **Note**: A specific instance of a relation schema may satisfy a functional dependency even if the functional dependency does not hold on all legal instances
 - \circ For example, a specific instance of instructor may, by chance, satisfy $name
 ightarrow \mathit{ID}$
 - \circ In such cases we do not say that F holds on R



Functional Dependencies (5)

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Objectives Outline

Functional Dependencies

Armstrong's Axioms

Closure of FDs

- A functional dependency is trivial if it is satisfied by all instances of a relation
 - o Example:
 - \triangleright *ID*, name \rightarrow *ID*
 - hd name
 ightarrow name
- In general, $\alpha \to \beta$ is trivial if $\beta \subseteq \alpha$.

Functional Dependencies (6)

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Objectives Outline Functional

Dependencies

Armstrong's Axioms

Closure of FDs

• Functional dependencies are:

StudentID	Semester	Lecture	TA
1234	6	Numerical Methods	John
1221	4	Numerical Methods	Smith
1234	6	Visual Computing Bob	
1201	2	Numerical Methods Peter	
1201	2	Physics II	Simon

 \circ StudentID \rightarrow Semester StudentID, Lecture \rightarrow TA $\{StudentID, Lecture\} \rightarrow \{TA, Semester\}$

Functional Dependencies (7)

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Objectives Outline

Functional Dependencies

Armstrong's Axioms

Module Summar

• Functional dependencies are:

Employee ID	Employee Name	Department ID	Department Name
0001	John Doe	1	Human Resources
0002	Jane Doe	2	Marketing
0003	John Smith	1	Human Resources
0004	Jane Goodall	3	Sales

 \circ EmployeeID \rightarrow EmployeeName

EmployeeID
ightarrow DepartmentID

 $DepartmentID \rightarrow DepartmentName$



Functional Dependencies (8): Armstrong's Axioms

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Objectives Outline

Functional Dependencies Armstrong's Axioms

- Given a set of Functional Dependencies F, we can infer new dependencies by the Armstrong's Axioms:
 - \circ **Reflexivity**: if $\beta \subseteq \alpha$, then $\alpha \to \beta$
 - **Augmentation**: if $\alpha \to \beta$, then $\gamma \alpha \to \gamma \beta$
 - \circ Transitivity: if $\alpha \to \beta$ and $\beta \to \gamma$, then $\alpha \to \gamma$
- These axioms can be repeatedly applied to generate new FDs and added to F
- A new FD obtained by applying the axioms is said to the logically implied by F
- The process of generations of FDs terminate after finite number of steps and we call it the Closure Set F⁺ for FDs F. This is the set of all FDs logically implied by F
- Clearly, $F \subseteq F^+$
- These axioms are
 - o Sound (generate only functional dependencies that actually hold), and
 - Complete (eventually generate all functional dependencies that hold)
- Prove the axioms from definitions of FDs
- Prove the soundness and completeness of the axioms
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Functional Dependencies (9): Closure of a Set of FDs

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Objectives Outline

Functional
Dependencies
Armstrong's Axion

- $F = \{A \rightarrow B, B \rightarrow C\}$
- $F^+ = \{A \rightarrow B, B \rightarrow C, A \rightarrow C\}$



Module Summary

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Objectives Outline

Functional
Dependencies
Armstrong's Axiom
Closure of FDs

Module Summary

• Introduced the notion of Functional Dependencies

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