

Infix \Rightarrow

$A + B$

operand operand
operator

$$\begin{aligned} &A \\ &A+B \\ &(A+B)+(C+D) \end{aligned}$$

$(A+B) + (C+D) \Rightarrow \text{infinity}$
 $\underline{AB} + \textcircled{+} \underline{CD}$
 $\underline{AB} + \underline{CD} + \underline{+} \rightarrow \text{positive}$

Prefix \Rightarrow $A + B$ (infix) \rightarrow $+AB$ (Prefix)

operand operator operand

A
 $-AB \rightarrow A-B$

$A \rightarrow B \rightarrow +AD \rightarrow \text{Prüfung}$
 $AB \rightarrow + \rightarrow \text{position}$

$(A+B) + (C-D) \rightarrow \text{infix}$
 $+AB \text{ (+)} -CD$
 $\boxed{++AB-CD} \rightarrow \text{prefix}$

Diagram illustrating the conversion of an infix expression to postfix notation:

- Infix Expression:** $A + B$ (labeled "infix").
- Components:**
 - A and B are operands.
 - $+$ is the operator.
- Postfix Expression:** $AB +$ (labeled "postfix exp").
- Stack Structure:** A stack is shown with two cells:
 - Top cell: A
 - Bottom cell: $AB +$

| |
|-------------|
| A |
| AB + |
| AB + CO - + |

postfix expression

→ A \nearrow infix \nearrow postfix
 → $A+B \Rightarrow AB+$
 → $(A+B) + (C-D) \rightarrow \text{infix exp}$

$$\underline{AB+} + \underline{CD-}$$
 match

$$\boxed{AB+CD-+}$$

① $(A+B) * C-D$ $\rightarrow (L \rightarrow R)$
Prefix \Rightarrow exp $\Rightarrow (A+B) * C-D$

Step 1 $\rightarrow +AB \quad *C-D$
 $\downarrow \text{OP} \quad \downarrow \text{OP} \quad \downarrow \text{OP}$
 $\downarrow \text{OP}$

Step 2 $\rightarrow *+ABC - D$

Step 3 $\rightarrow - * + ABCD \rightarrow \underline{\text{prefix}}$

\odot \ominus
 \downarrow
 $A + B$
 $+ AB$
 $\frac{+AB}{L} \ominus \frac{*CD}{R}$
 $= \frac{+AB}{L} * \frac{CD}{R}$

$$\begin{array}{c} \text{op} \\ \text{L} \uparrow \text{R} \\ \text{A} + \text{B} \end{array} \Rightarrow \frac{\text{AB} +}{\text{output}}$$

Postfix \rightarrow exp \rightarrow $\frac{\text{int} \times \text{in}}{(A+B) * C - D}$

$$(A+B) * (C-D) \rightarrow \text{int} * \text{int}$$

exp $\rightarrow \underline{(A+B)^R} * C - D$

Step 1 $\rightarrow \underline{AB +} * C - D$

Step 2 $\hookrightarrow \underline{AB + C} * - D$

Step 3 $\rightarrow \underline{AB + C} * D -$

$\Rightarrow \text{step 1} \Rightarrow \underline{AB+} * \underline{CD-}$
 $\text{step 2} \Rightarrow \underline{AB+CD-} * \rightarrow \text{postfix}$

Input: $A * B + C / D$ →

→ infix exp

$A * B + C / D$
→ $*AB + /CD$
→ $+ *AB / CD$
→ postfix

$$\begin{aligned} & \underline{(A+B)} * C - D \\ & + \underline{AB} * C - D \\ & * + ABC - D \\ & - * + ABCD \end{aligned}$$

$\frac{A}{\rightarrow} \mid$
 $L \rightarrow R$
 $\frac{A * B + C \mid D}{*AB + C \mid D}$
 $\frac{*AB + \mid CD}{R}$
 $+ *AB \mid CD$
 $a + b + ab$
 $\rightarrow + *AB \mid CD$

$A * B + C / D \rightarrow \text{postfix}$
 $AB * + CD / \rightarrow \text{postfix}$
 $AB * CD / +$

Input: $(A - B/C) * (A/K - L)$ \rightarrow prefn and post fn

Postfix
 exp $\rightarrow (A - B / C) * (A / K - L)$
 Step 1 $\rightarrow (A - B / C) * (A / K - L)$
 Step 2 $\rightarrow \underline{-A / B C} * \underline{-A / K L}$
 Step 3 $\rightarrow * \underline{-A / B C - A / K L} \rightarrow$ Postfix
 exp

Postfix \Rightarrow

exp $\rightarrow (A - B / C) * (A / K - L)$

Step 1 $\rightarrow (A - B / C) * (A / K - L)$

Step 2 $\rightarrow A B C / - * A K / L -$

Step 3 $\rightarrow A B C / - A K / L - *$ \rightarrow Postfix exp

Rules for the conversion from infix to postfix expression

1. Print the operand as they arrive.
2. If the stack is empty or contains a left parenthesis on top, push the incoming operator on to the stack.
3. If the incoming symbol is '(', push it on to the stack.
4. If the incoming symbol is ')', pop the stack and print the operators until the left parenthesis is found.
5. If the incoming symbol has higher precedence than the top of the stack, push it on the stack.
6. If the incoming symbol has lower precedence than the top of the stack, pop and print the top of the stack. Then test the incoming operator against the new top of the stack.
7. If the incoming operator has the same precedence with the top of the stack then use the associativity rules. If the associativity is from left to right then pop and print the top of the stack then push the incoming operator. If the associativity is from right to left then push the incoming operator.
8. At the end of the expression, pop and print all the operators of the stack.

