Assignment 2 - Alloy Corporation

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Introduction

The Manifacturing INC (MNC) makes four different metal alloys: A, B, C and D. The company is barely able to keep up with the increasing demand for these products. However, increasing raw material prices and foreign competition are forcing MNC to watch its margins to ensure it is operating in the most efficient manner possible.

Marketing Demands

To meet marketing demands for the coming week, MNC needs to produce

- at least 1,200 pounds of the A product,
- between 450 and 650 pounds of the B product,
- no more than 120 pounds of the C product, and
- no more than 150 pounds of D product.

Production Requirements

Each pound of the A, B, C, and D product contains, respectively, 55%, 45%, 25%, and 100% aluminum made up of copper.

The company has 1300 pounds of aluminum and 900 pounds of copper copper for use in the next week.

The various products are made using four different machines: forger, reamer, shaper, and planer. The following table summarizes the time required by each product on each machine. Each machine has 60 hours of time available in the coming week.

Financial summary

The controller recently presented management with the following financial summary of MNC's average weekly operations over the past quarter. From this report, the controller is arguing that the company should cease producing its B and C products.

Minutes required per pound

Machine	A	В	\mathbf{C}	D
Forger	1.20	1.00	1.00	1.5
Reamer	1.75	1.00	1.00	1.50
Shaper	1.30	0.60	0.40	0.00
Planer	2.50	1.20	2.00	1.50

Figure 1: Districts

	Product				
	A	В	С	D	Total
Sales Revenue	5769	2000	700	879	9348
Variables costs	3200	1550	300	350	5050
Fixed costs	600	500	250	300	1650
Net profit	1969	-50	150	229	2648
Pounds sold	1200	400	100	250	1950
Net profit per pound	1.64	-0.12	1.50	0.91	1.35

Figure 2: Financial summary

Questions

- a. Do you agree with the controller's recommendation? Why or why not?
- b. Formulate an LP model for this problem.
- c. Create a executable model in R for this problem and solve it.
- d. What is the optimal solution?
- e. Perform the sensitivity analysis for this solution and answer the following questions.
- f. Is the solution degenerate?
- g. Is the solution unique?
- h. If MNC wanted to decrease the production on any product, which one would you recommend and why?
- i. If MNC wanted to increase the production of any product, which one would you recommend and why?
- j. Which resources are preventing MNS from making more money? If they could acquire more of this resource how much should they acquire & how much should they be willing to pay to acquire it?
- k. How much should MNC be willing to pay to acquire more copper?
- 1. If the marketing department wanted to decrease the price of the A product by \$0.25, would the optimal solution change?

Solutions

a. Do you agree with the controller's recommendation? Why or why not?

We don't agree with the controller's recommendation, we have that using the current combination of Products, the $Product\ B$ has negative net profit (-0.12 per Pound) while the $Product\ C$ has positive net profit (1.5 per Pound). If we used the net profit as a performance measure of the products, which implies that the demand of the products will not change in the future, the controller would right on the cessation of the production of the $Product\ B$ but not of the $Product\ C$.

But as we can see that the demand of the *Product B* changed, using the current minimum amount for the product B we have that the net profit in this case would be $amount \cdot Margin\ per\ Pound$ (From the table below) – $Variable\ Costs = 1.125*450 - 500 = 6.25 > 0$ which is positive thus profitable, but comparatively a small profit. If we could allocate the resources spent for the Product B in other Products we will have a better profit since the marginal profit for the Product B is the lowest one (1.13).

The interruption in the production of the $Product\ B$ is still arguable and depends a lot also on the market request, but in the case of the $Product\ C$ we see that the marginal profit per Pound is 4.00, and it has a fixed cost of only 250, lowest one in all four products, thus we need to produce only 63 pounds of Product C to have a profit, as long as this demand is satisfied (in the last quarter it was satisfied) there is no need to interrupt the production of the Product C.

b. Formulate an LP model for this problem.

We create two different models one using the binary variable (called bin_model) and the other one without using the binary variables (called model)

Our objective is to maximize the profit, for that we define the *Margin Profit* as the *Sales Revenue-Variable Costs* and the Margin Profit per Pound as *Margin Profit/Pounds Sold*, we ignore the fixed costs because if we included them, since they are constant, they will go on the right hand side of the objective function and will not change the problem itself.

Product	A	В	С	D
Sales Revenue	5769	2000	700	879
Variable Costs	3200	1550	300	350
Margin	2569	450	400	529
Pounds Sold	1200	400	100	250
Margin per Pound	2.14	1.13	4.00	2.12

We start by the one **without** the binary variables:

So, indicated with A the pound sold of Product A (same for B, C and D) , the objective function is:

$$2.14 \cdot A + 1.13 \cdot B + 4 \cdot C + 2.12 \cdot D$$

The domain of the variables are:

$$\begin{aligned} 1200 & \le A < +\infty \\ 450 & \le B \le 650 \\ 0 & \le C \le 120 \\ 0 & \le D \le 150 \end{aligned}$$

Based on the composition of the material in each Product and the limited resources we also have that:

$$0.55 \cdot A + 0.45 \cdot B + 0.25 \cdot C + 1.00 \cdot D \le 1300 \qquad \longrightarrow \text{Maximum Alminium}$$

$$0.45 \cdot A + 0.55 \cdot B + 0.75 \cdot C + 0.00 \cdot D \le 900 \qquad \longrightarrow \text{Maximum Copper}$$

We also have a time limit on each Machine, so the following constraint is also valid:

$$\begin{array}{ll} 1.20 \cdot A + 1.00 \cdot B + 1.00 \cdot C + 1.50 \cdot D \leq 3600 & \to \text{Forger} \\ 1.75 \cdot A + 1.00 \cdot B + 1.00 \cdot C + 1.50 \cdot D \leq 3600 & \to \text{Reamer} \\ 1.30 \cdot A + 0.60 \cdot B + 0.40 \cdot C + 0.00 \cdot D \leq 3600 & \to \text{Shaper} \\ 2.50 \cdot A + 1.20 \cdot B + 2.00 \cdot C + 1.50 \cdot D \leq 3600 & \to \text{Planer} \\ \end{array}$$

The model with the binary variables:

The **objective function** in this case is:

$$2.14 \cdot A + 1.13 \cdot B + 4 \cdot C + 2.12 \cdot D - 600 \cdot Y_A - 500 \cdot Y_B - 250 \cdot Y_C - 300 \cdot Y_D$$

The domain of the variables are:

$$1200 \le A < +\infty$$

$$450 \le B \le 650$$

$$0 \le C \le 120$$

$$0 \le D \le 150$$

$$Y_i \in \{0, 1\} \text{ with } i = A, B, C, D$$

Based on the composition of the material in each Product and the limited resources we also have that:

$$0.55 \cdot A + 0.45 \cdot B + 0.25 \cdot C + 1.00 \cdot D \leq 1300 \qquad \qquad \rightarrow \text{Maximum Alminium}$$

$$0.45 \cdot A + 0.55 \cdot B + 0.75 \cdot C + 0.00 \cdot D \leq 900 \qquad \qquad \rightarrow \text{Maximum Copper}$$

We also have a time limit on each Machine, so the following constraint is also valid:

$$\begin{array}{ll} 1.20 \cdot A + 1.00 \cdot B + 1.00 \cdot C + 1.50 \cdot D \leq 3600 & \to \text{Forger} \\ 1.75 \cdot A + 1.00 \cdot B + 1.00 \cdot C + 1.50 \cdot D \leq 3600 & \to \text{Reamer} \\ 1.30 \cdot A + 0.60 \cdot B + 0.40 \cdot C + 0.00 \cdot D \leq 3600 & \to \text{Shaper} \\ 2.50 \cdot A + 1.20 \cdot B + 2.00 \cdot C + 1.50 \cdot D \leq 3600 & \to \text{Planer} \\ \end{array}$$

Lastly we have the binary constraints:

$$A \leq M_A Y_A \text{ with } M_A = \min(1300/0.55, 900/0.45, 3600/1.2, 3600/1.75, 3600/1.3, 3600/2.5) = 1440$$

$$B \leq M_B Y_B \text{ with } M_B = \min(1300/0.45, 900/0.55, 3600/1, 3600/1, 3600/0.6, 3600/1.2) = 1636.36$$

$$C \leq M_C Y_C \text{ with } M_C = \min(1300/0.25, 900/0.75, 3600/1, 3600/1, 3600/0.4, 3600/2) = 1200$$

$$D \leq M_D Y_D \text{ with } M_D = \min(1300/1, 3600/1.5, 3600/1.5, 3600/1.5) = 1300$$

Additionally we want to produce a certain Product only if it is profitable after deducting the fixed cost so we will have:

$$A \ge 600/2.14 \cdot Y_A = 280.24Y_A$$

$$B \ge 500/1.13 \cdot Y_B = 444.44Y_B$$

$$C \ge 250/4 \cdot Y_C = 62.5Y_C$$

$$D \ge 300/2.12 \cdot Y_D = 141.78Y_D$$

c. Create a executable model in R for this problem and solve it.

Here is the implementation of problem defined above in point **b.** of model in R:

```
if(require(lpSolveAPI)==FALSE) install.packages("lpSolveAPI")
model = make.lp(0,4)
                                                 # 4 Variables (A,B,C,D)
lp.control(model, sense = "max")
                                                 #Maximazing Problem
set.objfn(model,obj = c(2.141,1.125,4,2.116)) #Objective function coefficients
row.add.mode(model, "on")
add.constraint(model,
               xt = c(0.55, 0.45, 0.25, 1),
               type = "<=",
               rhs = 1300,
               indices = c(1:4)) #Aluminium Constraint
add.constraint(model,
               xt = c(0.45, 0.55, 0.75, 0),
               type = "<=",
               rhs = 900,
               indices = c(1:4)) #Copper Constraint
add.constraint(model,
               xt = c(1.2,1,1,1.5),
               type = "<=",
               rhs = 3600,
               indices = c(1:4)) #Forger Time Constraint
add.constraint(model,
               xt = c(1.75,1,1,1.5),
               type = "<=",
               rhs = 3600,
               indices = c(1:4)) #Reamer Time Constraint
add.constraint(model,
               xt = c(1.3, 0.6, 0.4, 0),
               type = "<=",
               rhs = 3600,
               indices = c(1:4)) #Shaper Time Constraint
add.constraint(model,
               xt = c(2.5,1.2,2,1.5),
               type = "<=",
               rhs = 3600,
               indices = c(1:4)) #Planer Time Constraint
#Setting lower and upper bounds
set.bounds(model,lower = c(1200,450,0,0), upper = c(Inf,650,120,150))
row.add.mode(model, "off")
#Giving names to the contraints and variables
dimnames(model)<- list(c("Aluminium", "Copper", "Forger", "Reamer", "Shaper", "Planer"),</pre>
                       c("A", "B", "C", "D"))
name.lp(model, "Alloy Corporation")
```

```
print(model) #To see to model
## Model name: Alloy Corporation
                                      D
##
                        В
                           C
                 Α
## Maximize 2.141 1.125
                              4 2.116
## Aluminium 0.55
                    0.45
                            0.25
                                      1 <= 1300
## Copper
              0.45 0.55
                            0.75
                                      0 <=
                                              900
                                    1.5 <= 3600
## Forger
              1.2
                    1
                             1
## Reamer
             1.75
                       1
                                    1.5 <= 3600
                              1
## Shaper
              1.3
                    0.6
                            0.4
                                    0 <= 3600
                                    1.5 <= 3600
## Planer
              2.5 1.2
                             2
## Kind
              Std
                    Std
                           Std
                                   Std
## Type
              Real
                     Real
                            Real
                                   Real
## Upper
              Inf
                      650
                             120
                                    150
## Lower
              1200
                      450
                               0
Here is the implementation of problem defined above in point b. of bin_model in R:
bin_model = make.lp(0,8)
                                                   # 8 Variables (A,B,C,D)
set.type(bin_model, c(5:8), "binary")
lp.control(bin_model, sense = "max")
                                                   #Maximazing Problem
set.objfn(bin_model,obj = c(2.141,1.125,4,2.116,-600,-500,-250,-300))
                                                                     #Objective function coefficient
row.add.mode(bin_model, "on")
add.constraint(bin_model,
              xt = c(0.55, 0.45, 0.25, 1),
              type = "<=",
              rhs = 1300,
              indices = c(1:4)) #Aluminium Constraint
add.constraint(bin_model,
              xt = c(0.45, 0.55, 0.75, 0),
              type = "<=",
              rhs = 900.
              indices = c(1:4)) #Copper Constraint
add.constraint(bin_model,
              xt = c(1.2,1,1,1.5),
              type = "<=",
              rhs = 3600,
              indices = c(1:4)) #Forger Time Constraint
add.constraint(bin_model,
              xt = c(1.75,1,1,1.5),
              type = "<=",
              rhs = 3600,
              indices = c(1:4)) #Reamer Time Constraint
add.constraint(bin_model,
              xt = c(1.3, 0.6, 0.4, 0),
              type = "<=",
              rhs = 3600,
```

indices = c(1:4)) #Shaper Time Constraint

```
add.constraint(bin_model,
               xt = c(2.5, 1.2, 2, 1.5),
               type = "<=",
               rhs = 3600,
               indices = c(1:4)) #Planer Time Constraint
add.constraint(bin_model,
               xt = c(1,-1440),
               type = "<=",
               rhs = 0,
               indices = c(1,5)) #binary contraint for A
add.constraint(bin_model,
               xt = c(1, -1636.36),
               type = "<=",
               rhs = 0,
               indices = c(2,6)) #binary contraint for B
add.constraint(bin_model,
               xt = c(1,-1200),
               type = "<=",
               rhs = 0,
               indices = c(3,7)) #binary contraint for C
add.constraint(bin model,
               xt = c(1,-1300),
               type = "<=",
               rhs = 0,
               indices = c(4,8)) #binary contraint for D
add.constraint(bin_model,
               xt = c(-1,280.24),
               type = "<=",
               rhs = 0,
               indices = c(1,5)) #min contraint for A
add.constraint(bin_model,
               xt = c(-1,444.44),
               type = "<=",
               rhs = 0,
               indices = c(2,6)) #min contraint for B
add.constraint(bin_model,
               xt = c(-1,62.5),
               type = "<=",
               rhs = 0,
               indices = c(3,7)) #min contraint for C
add.constraint(bin_model,
               xt = c(-1,141.78),
               type = "<=",
               rhs = 0,
               indices = c(4,8)) #min contraint for D
```

```
#Setting lower and upper bounds
set.bounds(bin_model,lower = c(1200,450,0,0,0,0,0), upper = c(Inf,650,120,150,1,1,1,1))
row.add.mode(bin model, "off")
#Giving names to the contraints and variables
dimnames(bin_model)<- list(c("Aluminium", "Copper", "Forger", "Reamer", "Shaper", "Planer",</pre>
                               "Binary A", "Binary B", "Binary C", "Binary D",
                                "Min Bin A", "Min Bin B", "Min Bin C", "Min Bin D"),
                             c("A", "B", "C", "D", "YA", "YB", "YC", "YD"))
name.lp(bin_model, "Alloy Corporation Binary Problem")
print(bin_model)
## Model name: Alloy Corporation Binary Problem
                                                                 YΑ
                                                                            YΒ
                                                                                       YC
                                                                                                  YD
                                            C
                                                       D
                                                                                                -300
                  2.141
                             1.125
                                            4
                                                   2.116
                                                               -600
                                                                          -500
                                                                                     -250
## Maximize
## Aluminium
                   0.55
                              0.45
                                         0.25
                                                       1
                                                                  0
                                                                             0
                                                                                                   0
                                                                                                       <=
                                                                                                           1300
## Copper
                   0.45
                              0.55
                                         0.75
                                                                  0
                                                                                                   0
                                                                                                      <=
                                                                                                            900
                                                       0
                                                                             0
                                                                                        0
## Forger
                    1.2
                                 1
                                            1
                                                     1.5
                                                                  0
                                                                             0
                                                                                        0
                                                                                                   0
                                                                                                       <=
                                                                                                           3600
## Reamer
                   1.75
                                                     1.5
                                                                  0
                                                                             0
                                                                                        0
                                                                                                   Λ
                                                                                                       <=
                                                                                                           3600
                                 1
                                            1
## Shaper
                    1.3
                               0.6
                                          0.4
                                                       0
                                                                  0
                                                                             0
                                                                                        0
                                                                                                   0
                                                                                                       <=
                                                                                                           3600
## Planer
                                                                  0
                                                                             0
                                                                                        0
                                                                                                   0
                                                                                                      <=
                                                                                                           3600
                    2.5
                               1.2
                                            2
                                                     1.5
## Binary A
                      1
                                 0
                                            0
                                                       0
                                                              -1440
                                                                             0
                                                                                        0
                                                                                                   0
                                                                                                              0
                                                                     -1636.36
                                                                                                   0
                                                                                                      <=
                                                                                                              0
## Binary B
                      0
                                 1
                                            0
                                                       0
                                                                  0
                                                                                        0
## Binary C
                                                                                                              0
                      0
                                 0
                                            1
                                                       0
                                                                  0
                                                                             0
                                                                                    -1200
                                                                                                   0
                                                                                                      <=
## Binary D
                      0
                                 0
                                                                                               -1300
                                                                                                      <=
                                                                                                              0
                                            0
                                                       1
                                                                  0
                                                                             0
                                                                                        0
## Min Bin A
                     -1
                                 0
                                            0
                                                       0
                                                             280.24
                                                                             0
                                                                                        0
                                                                                                   0
                                                                                                      <=
                                                                                                              0
                                                                                                              0
## Min Bin B
                      0
                                -1
                                            0
                                                       0
                                                                  0
                                                                        444.44
                                                                                        0
                                                                                                   0
                                                                                                      <=
## Min Bin C
                      0
                                 0
                                           -1
                                                       0
                                                                  0
                                                                             0
                                                                                     62.5
                                                                                                   0
                                                                                                      <=
                                                                                                              0
## Min Bin D
                                 0
                                                                  0
                                                                                              141.78 <=
                                                                                                              0
                      0
                                            0
                                                      -1
                                                                             0
                                                                                        0
                                                     Std
## Kind
                    Std
                               Std
                                          Std
                                                                Std
                                                                           Std
                                                                                      Std
                                                                                                 Std
## Type
                              Real
                                         Real
                                                    Real
                                                                Int
                                                                           Int
                                                                                      Int
                                                                                                 Int
                   Real
## Upper
                               650
                                          120
                                                     150
                    Inf
                                                                  1
                                                                             1
                                                                                        1
                                                                                                   1
## Lower
                   1200
                               450
                                            0
                                                       0
                                                                  0
                                                                             0
                                                                                        0
                                                                                                   0
```

d. What is the optimal solution?

We use the solve() function to solve the model:

```
solve(model) #result = 0 -> solved

## [1] 0

solution <- get.variables(model)
fixed_cost <- 1650
cat("The optimal variables values are:","\n",
        "A <-",solution[1],", B <-",solution[2],
        ", C <-",solution[3],", D <-",solution[4])

## The optimal variables values are:
## A <- 1200 , B <- 450 , C <- 30 , D <- 0
cat("The optimal objective function value is: ",get.objective(model), "\n",
        "Thus the optimal net profit value is",get.objective(model) - fixed_cost)</pre>
```

```
## The optimal objective function value is: 3195.45
  Thus the optimal net profit value is 1545.45
We use the solve() function to solve the bin_model:
solve(bin_model) #result = 0 -> solved
## [1] 0
solution <- get.variables(bin_model)</pre>
cat("The optimal variables values are:","\n",
    "A <-", solution[1], ", B <-", solution[2],
    ", C \leftarrow", solution[3], ", D \leftarrow", solution[4], "\n",
    "Y_A <-", solution[5], ", Y_B <-", solution[6],
    ", Y_C <-", solution[7], ", Y_D <-", solution[8])
## The optimal variables values are:
## A <- 1200 , B <- 500 , C <- 0 , D <- 0 \,
## Y_A <- 1 , Y_B <- 1 , Y_C <- 0 , Y_D <- 0
cat("The optimal objective function value is: ",get.objective(bin_model))
## The optimal objective function value is: 2031.7
```

e. Perform the sensitivity analysis for this solution and answer the following questions.

```
printSensitivityObj(model)
```

Objs	Sensitivity
C1	$-\inf <= C1 <= 5$
C2	$-\inf <= C2 <= 2.4$
C3	$2.821 <= C3 <= \inf$
C4	$-\inf <= C4 <= 3$

We have that the base remains if the coefficient are in the following range:

$$-\infty < C_1 \le 5$$

$$-\infty < C_2 \le 2.4$$

$$2.821 \le C_3 < +\infty$$

$$-\infty < C_4 < 3$$

The fact that C_1 and C_2 can decrease all they want is due to the fact that the optimal solution satisfies the minimum constraint given for Product A and B, thus if we were to decrease the marginal profit per pound from how it is now, we will have that it still needs to satisfy the minimum quantity for Product A and B, so the solution will not change.

A similar argument applies for the coefficient C_4 of Product D, if we decrease C_4 the solution will not change since we will continue to not produce the Product C with the given constraints.

While for the coefficient C_3 if we increase it, since we produce only the product C, because the most profitable while satisfying the given contraints even if we increased the obtained profit we will have that the optimal solution will not change.

printSensitivityRHS(model)

Rhs	duals	Sensitivity
B1	0	-inf <= B1 <= inf
B2	0	$-\inf \le B2 \le \inf$
B3	0	$-\inf \le B3 \le \inf$
B4	0	$-\inf \le B4 \le \inf$
B5	0	$-\inf \le B5 \le \inf$
B6	2	$3540 \le B6 \le 3780$

So we have the dual variables are

$$y_i = 0, \forall i = 1, ..., 5$$

and

$$y_6 = 2$$

and the interval for the resources are:

$$-\infty < b_1 < +\infty \\ -\infty < b_2 < +\infty \\ -\infty < b_3 < +\infty \\ -\infty < b_4 < +\infty \\ -\infty < b_5 < +\infty \\ 3540 \le b_6 \le 3780$$

All the shadow prices except for the last one are 0 thus a small change in these contraints with null shadow prices will not affect the solution.

The last contraint (Planer Time) has a shadow price of 2, which means that every minute we add/subtract to the planer time (staying in the given interval [3540,3780]), the value of the optimal solution increases/decreases by 2.

f. Is the solution degenerate?

There are two was of checking if a solution is degenrate, the first one is using the theory: we have that since no constraint has an allowable increase or decrease = 0, the solution is not degenerate. Another way is using the value of the following function:

solve.lpExtPtr(model)

If the function has a value of 4 it means that the solution is degenerate, while 0 means that the optimal solution is found. In this case the value of the function confirms that the solution is not degenerate.

g. Is the solution unique?

get.solutioncount(model)

[1] 1

This function counts the number of solution for the model, in this case the result is 1, thus there is only one unique solution.

We could also see that the first two quantities for Product A and B are the minimum market's requirement and the rest of the resources are allocated for the Product C which is the most profitable one. So it is reasonable to think (but not obvious) that the obtained solution is the only best possibility. For example after satisfying the market's minimum requirement for the Product A and B, if we were to allocate the resources for any product but C, the net profit will not go up as much as with the Product C, given that the production time of C is more or less the same as the other products.

h. If MNC wanted to decrease the production on any product, which one would you recommend and why?

Variables	Final_Quantity	Reduced_Cost
A	1200	-2.859
В	450	-1.275
\mathbf{C}	30	0.000
D	0	-0.884

One would be tempted to use the marginal profit per Pound, in this case he/she would recommend decreasing the Production of the Product B, in order to allocate the resources for a more profitable Product, but using the Reduced Cost we can see that the Product which will gain us more value reducing its production is the Product A with a reduce cost of 2.859.

i. If MNC wanted to increase the production of any product, which one would you recommend and why?

In this case we would recommend the increase in production of the Product C, which is the most profitable one. All the other Products have a negative Reduced Cost.

j. Which resources are preventing MNS from making more money? If they could acquire more of this resource how much should they acquire & how much should they be willing to pay to acquire it?

```
get.constraints(model)
```

```
## [1] 870 810 1920 2580 1842 3600
```

The Planer time is the one which is preventing us to produce ant other product (because it's value is = 3600 which is the limit), since it's shadow price is 2, if we buy 180 minutes more the value of the function will increase by $y_6 \times \Delta_2 = 2 \times 180 = 360$. So the company must pay at most 360 to increase the time by 180 minutes in the Planer machine.

k. How much should MNC be willing to pay to acquire more copper?

From the point j. we can see that the quantity of Copper used is 810, while the company has an available quantity of 900, thus MNC doesn't need extra copper, so the answer is 0.

l. If the marketing department wanted to decrease the price of the A product by \$0.25, would the optimal solution change?

During the sensitivity analysis we saw that the the coefficient C_1 for the product A can decrease a lot without changing the optimal solution, so if we decrease it by 0.25 the optimal solution will not change, only the value of the function will change.

We can confirm it (even though it's unnecessary) creating a new model with the new coefficient for Product A.