

### LOGICAL MACHINE

Kenny Jasmine Kunn Binn



George Boole

Formulated Boolean Algebra

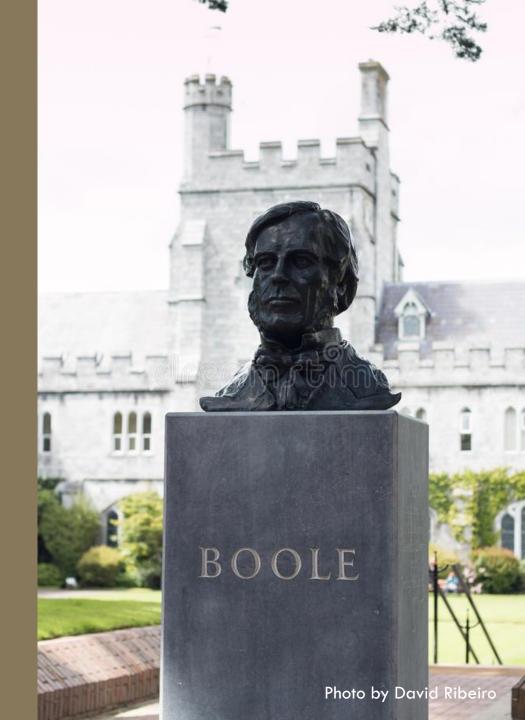
Based in Cork

CAN ANYONE RECOGNIZE WHO THIS IS?

### BOOLEAN ALGEBRA

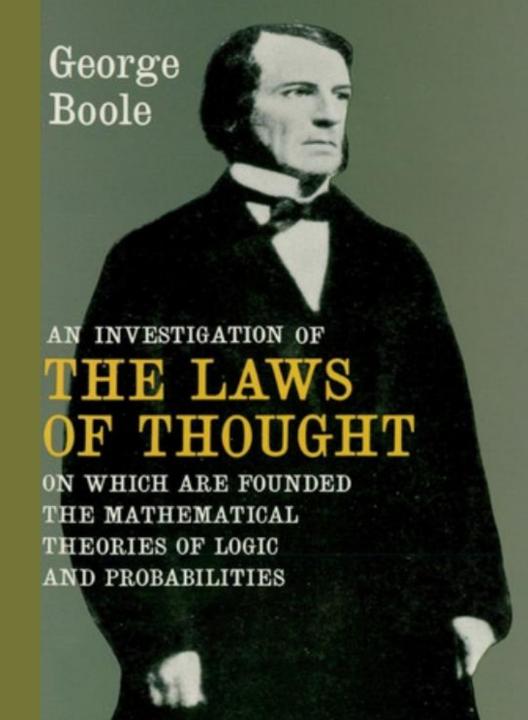
Building blocks behind the workings of a computer

Consist of two variables: TRUE or FALSE which can be denoted as 0 and 1 respectively



### LOGIC

Logic represents the systematic study of the form of argument and deductive reasoning.



## EX1. WHO CAN WE INVITE TO THE PARTY?

You have three friends: Claire, Daniel, and Eric, whom you would like to invite to your party. You can invite people according to the following rules:

- 1. If you invite Eric, you must invite Claire.
- 2. If you don't invite Daniel, you must invite both Claire and Eric.
- 3. You must invite either Claire or Eric, but not both.

Use your truth table to see who you can invite.

# TRUTH TABLE

	Claire	Daniel	Eric
1	0	0	0
2	0	0	1
3	0	1	0
4	0	1	1
5	1	0	0
6	1	0	1
7	1	1	0
8	1	1	1

1 = invite, 0 = do not invite

### 1. If you invite Eric, you must invite Claire.

	Claire	Daniel	Eric	
1	0	0	0	Keep
2	0	0	1	Discard
3	0	1	0	Keep
4	0	1	1	Discard
5	1	0	0	Keep
6	1	0	1	Keep
7	1	1	0	Keep
8	1	1	1	Keep

1 = invite, 0 = do not invite

### EX2. WHO IS WATCHING TV?

Abner, his wife Beryl and their three children, Cleo, Dale and Ellsworth.

- 1. If Abner is watching television, so is his wife.
- 2. Either Dale or Ellsworth, or both of them, are watching television.
- 3. Either Beryl or Cleo, but not both, is watching television.
- 4. Dale and Cleo are either both watching television or both not watching television.
- 5. If Ellsworth is watching television, then Abner and Dale are also watching.

Who is watching television?

Obtained from Gardner (1969, p.20)

# Martin 2578 23 Gardner's 235579 New 23578 2356 Mathematical 23 Diversions 23 67 from 13578 1235 SCIENTIFIC 23579 AMERICAN 24578

From Binary magic to Topological games and the infinite pleasures of Pi

### REFERENCE

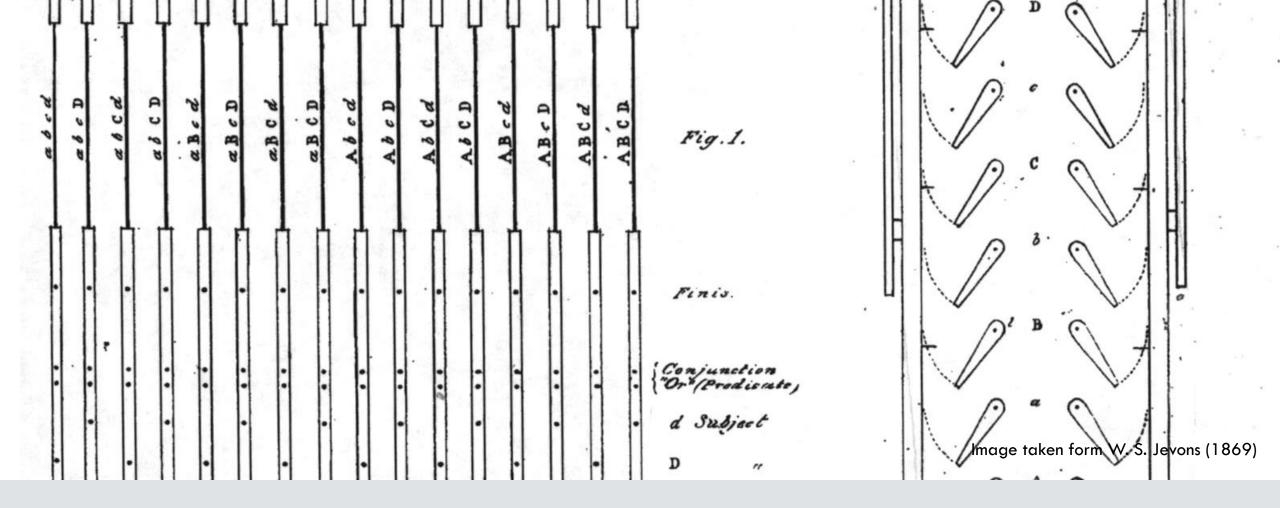
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### EXTRA MATERIALS

### SIMILAR TRIANGLES

"

- 1. Triangles whose corresponding angles are equal have their corresponding sides proportional, and vice versa.
- 2. Similar figures consist of all whose corresponding angles are equal, and whose corresponding sides are proportional.

AN INVESTIGATION

OF

### THE LAWS OF THOUGHT,

ON WHICH ARE FOUNDE

THE MATHEMATICAL THEORIES OF LOGIC AND PROBABILITIES.

BY

GEORGE BOOLE, LL.D.

PROFESSOR OF MATHEMATICS IN QUEEN'S COLLEGE, CORK.

#### LONDON:

WALTON AND MABERLY,

UPPER GOWER-STREET, AND IVY-LANE, PATERNOSTER-ROW.

CAMBRIDGE: MACMILLAN AND CO.

Courtesy of Bloomsbury Auctions

### EX. SIMILAR TRIANGLES

"

To represent these premises, let us make

s = similar.

t = triangles.

q = having corresponding agles equal.

r = having corresponding sides proportional.

77

Obtain form Boole (1854, p.96)

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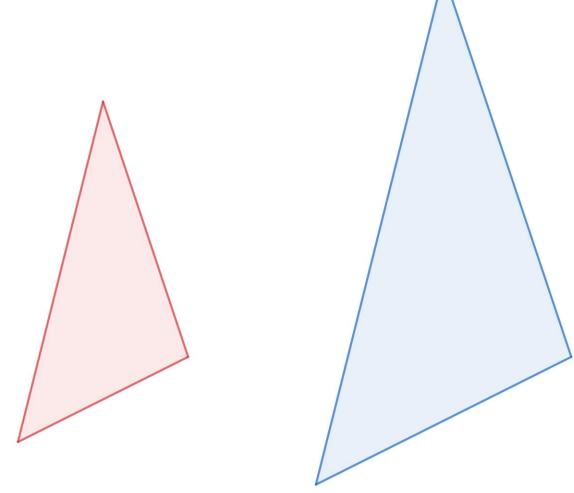
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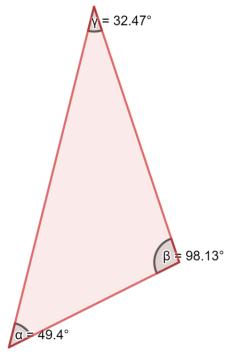
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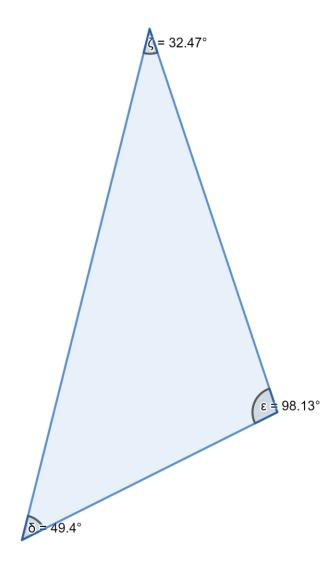
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## 1. Triangles ...

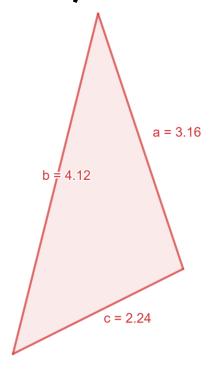


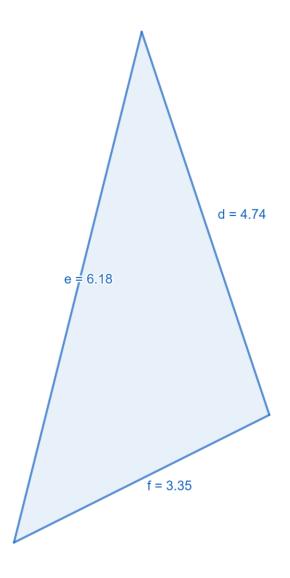
... whose corresponding angles are equal ...



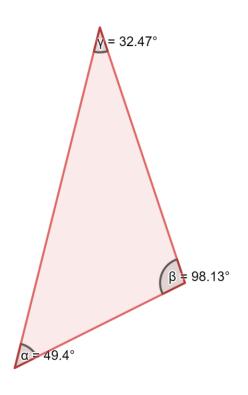


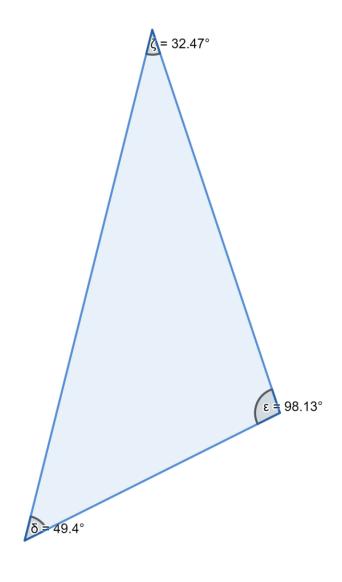
... have their corresponding sides proportional, ...



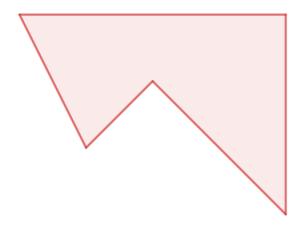


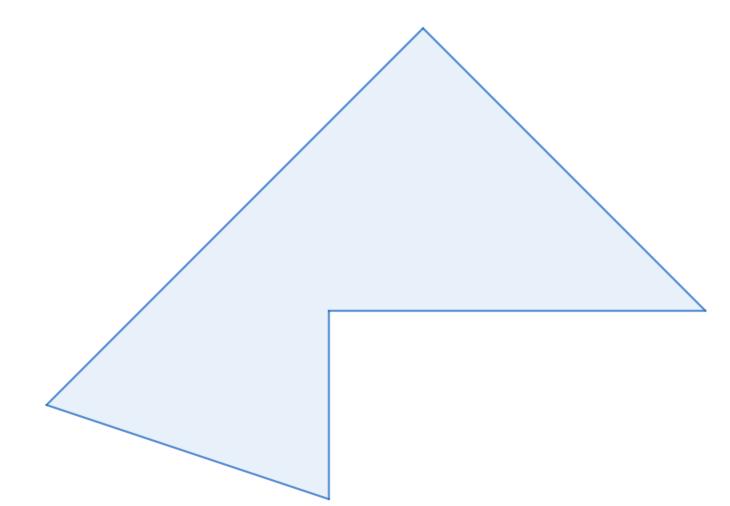
### ... and vice versa.



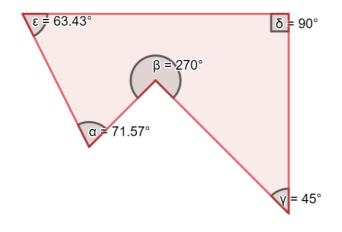


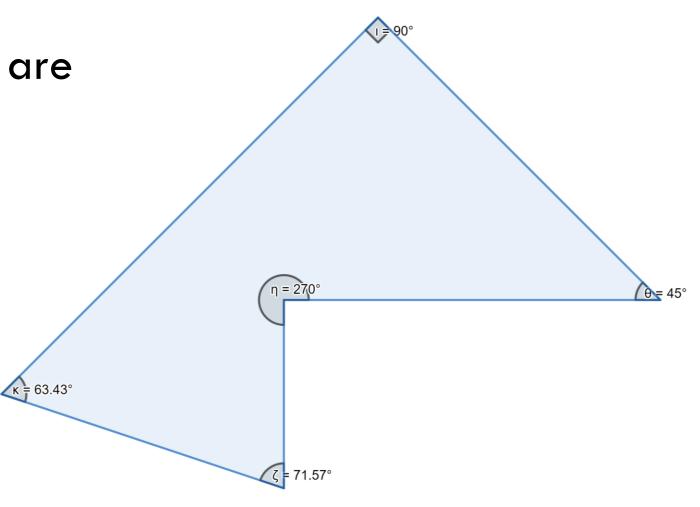
### 2. Similar figures ...



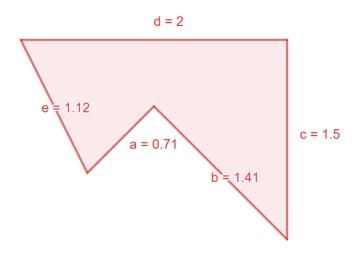


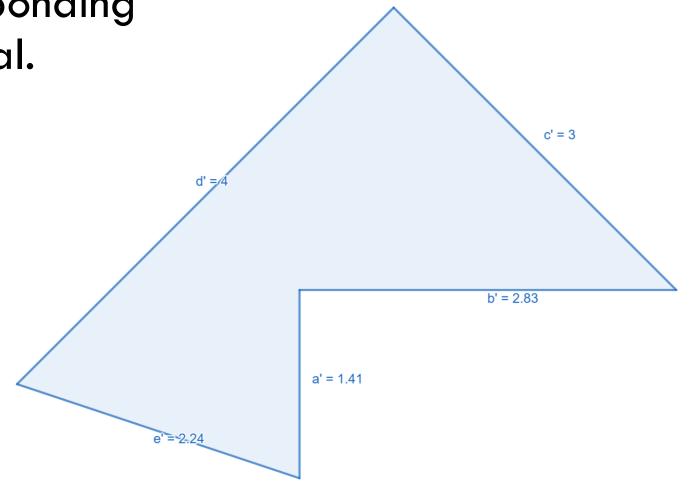
... consist of all whose corresponding angles are equal, ...





... and whose corresponding sides are proportional.





# Q: WHICH STATEMENT IS TRUE?

- **A.** Triangles, whose either corresponding sides are proportional, or corresponding angles are equal, but not both, are similar triangles.
- **B.** Dissimilar triangles, whose corresponding angles are equal, have corresponding sides disproportional.
- **C.** Figures whose corresponding sides are proportional and whose corresponding angles are equal, but not triangles, are similar.
- **D.** Non-triangular, dissimilar figures, could have corresponding sides proportional, and corresponding angles equal.