

ENEL 671 Adaptive Signal Processing Project Report

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Abstract—The purpose of this project is to analyze the performance of three different adaptive algorithms. These algorithms, which can be used for a variety of applications such as echo cancellation and beamforming, are implemented for the purposes of equalizing a dispersive channel. The first algorithm investigated is the Least Mean Squares (LMS). The LMS filter uses a search method to minimize the mean square error. The performance of the LMS is then compared to the Recursive Least Squares (RLS) method, which minimizes a weighted linear least squares cost function. Finally the Recursive Least Squares Lattice algorithm is implemented in the third project for joint process estimation. The algorithms are tested against multiple channels with varying eigenvalue spreads. Furthermore different design parameters such as step size and filter order are evaluated. The performance with regards to convergence speed and complexity is discussed. The RLSL appears to have performance advantages in terms of convergence speed at the cost of significant increase in complexity.

I. INTRODUCTION

ADAPTIVE filtering is used for a variety of applications. When communicating across a dispersive channel, a signal is distorted by effects of multipath, noise etc REFERENCE. To recover the correct message at the receiver, an adaptive filter is implemented to equalize the channel. In general, an algorithm is used to calculate the optimum filter coefficients to minimize the error between transmit and receive. In practice, a signal transmitted along a channel contains a preamble, which is a known sequence of data that is used to estimate the parameters of the channel. The statistics are assumed to be stationary in the window of time that each preamble is sent.

The most common adaptive equalizers involve the LMS, RLS, and RLSL algorithms. The performance of these methods varies and they each have their advantages and drawbacks. The LMS is relatively simplistic in terms of hardware/software resources. However, its drawback is that it uses a stochastic search gradient and which limits its ability to find an optimum solution, is inefficient and not practically capable of removing all distortions. The RLS algorithm is typically an order of magnitude faster because it whitens the input data by using the inverse correlation matrix of the data, assumed to be of zero mean REF. The RLSL algorithm uses a lattice predictor along with a stage that estimates the error of the next filter order at each time step.

The methodology used for designing of the filters in this project will be discussed. Afterwards a detailed analysis of the

results for each project and a summary of their implications will be discussed. Finally a conclusions section will highlight the general results drawn from each experiment.

II. EQUALIZATION METHODOLOGY

ADAPTIVE equalization is designed to remove unwanted signals from a channel output which can be caused by multipath or other distortions. In Figure 1 the general block diagram that is simulated in these experiments is outlined. A data source that generates a random BPSK signal goes through a dispersive channel that has three paths and white noise. The adaptive filter reduces the effects of these signal distortions to generate the output. Before the specifics of this block diagram is discussed a few general principles of Wiener filter theory will be discussed. The autocorrelation matrix is defined as

$$\mathbf{R} = E[\mathbf{u}(n)\mathbf{u}(n)^T]$$

and the autocovariance:

$$\mathbf{p} = E[\mathbf{u}(n)d(n)]$$

it can be shown from REF that the Wiener-Hopf or Normal Equation can be solved for the optimum tap weights:

$$\mathbf{R}\mathbf{w} = \mathbf{p}$$

although this is computationally wasteful and the matrix \mathbf{R} may not always be invertible therefore adaptive algorithms are used to determine the tap weight vector.

$$\mathbf{w} = [w_0 \quad w_1 \quad \dots \quad w_{M-1}]^T$$

The output of the channel, which is the input to the adaptive filter is defined as:

$$\begin{aligned} \mathbf{u}(n) &= [u(n) \quad u(n-1) \quad \dots \quad u(n-M+1)]^T \\ &= \mathbf{h}^T(n)\mathbf{a}(n) + \mathbf{v}(n) \end{aligned}$$

where \mathbf{h} is known as the channel impulse response. The impulse response for the four channels with varying distortion are defined as

Channel	\mathbf{h}_1	\mathbf{h}_2	\mathbf{h}_3
1	0.2194	1	0.2194
2	0.2798	1	0.2798
3	0.3365	1	0.3365
4	0.3887	1	0.3887

TABLE I: Problem 1 Calculations

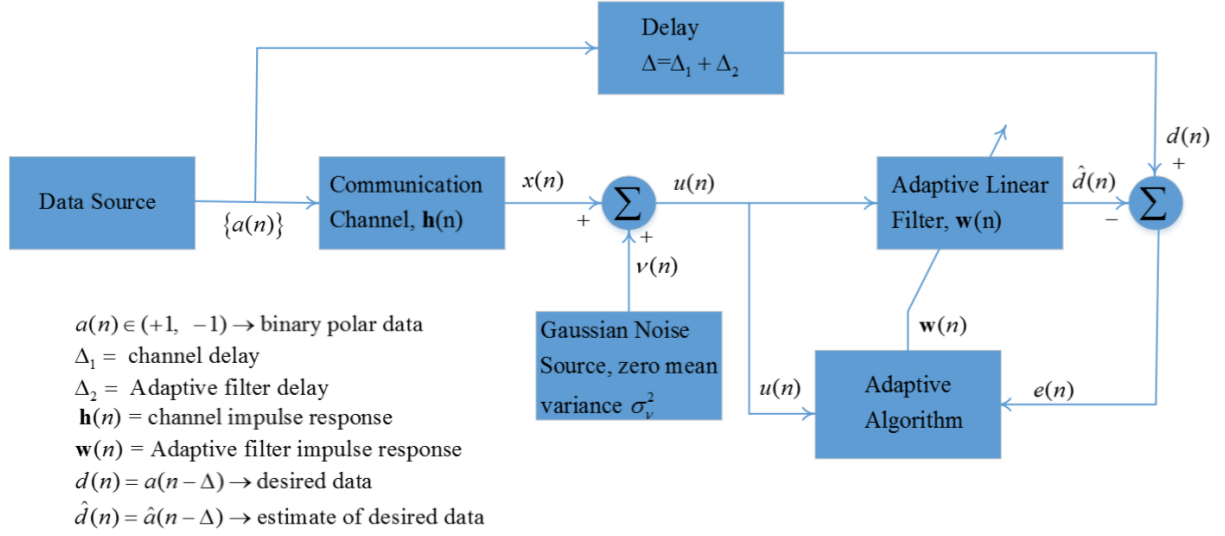


Fig. 1: Block Diagram for Equalization

To compare the output of the filter to the truth data source adequate delay must be added to the BPSK data. The optimal delay is given by half the filter order, that is:

$$\Delta = \frac{M}{2}$$

III. PRE EXPERIMENT CALCULATIONS

$$R = \begin{bmatrix} r(0) & r(1) & r(2) & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ r(1) & r(0) & r(1) & r(2) & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ r(2) & r(1) & r(0) & r(1) & r(2) & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & r(2) & r(1) & r(0) & r(1) & r(2) & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & r(2) & r(1) & r(0) & r(1) & r(2) & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & r(2) & r(1) & r(0) & r(1) & r(2) & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & r(2) & r(1) & r(0) & r(1) & r(2) & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & r(2) & r(1) & r(0) & r(1) & r(2) & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & r(2) & r(1) & r(0) & r(1) & r(2) \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & r(2) & r(1) & r(0) & r(1) \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & r(1) & r(0) & 0 \end{bmatrix}$$

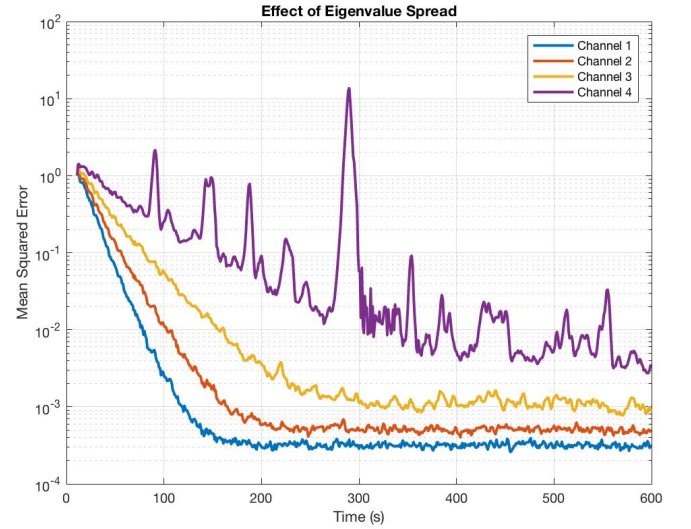


Fig. 2: BLAH BLAH

IV. PROJECT 1: LEAST MEAN SQUARES ALGORITHM

$$\mathbf{w}(n) = \mathbf{w}(n-1) + \mu \mathbf{u}(n) e(n)$$

$$\hat{d}(n) = y(n) = \mathbf{w}^T(n) \mathbf{u}(n) = \mathbf{u}^T(n) \mathbf{w}(n)$$

$$e(n) = d(n) - \hat{d}(n) = d(n) - \mathbf{w}^T(n) \mathbf{u}(n)$$

$$\mathbf{J}(n) = \sigma_d^2 - 2\mathbf{w}^T \mathbf{p} + \mathbf{w}^T \mathbf{R} \mathbf{w}$$

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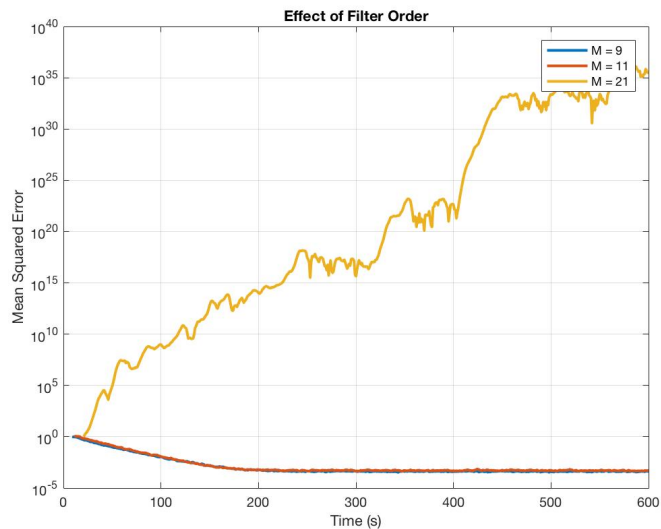


Fig. 3: BLAH BLAH

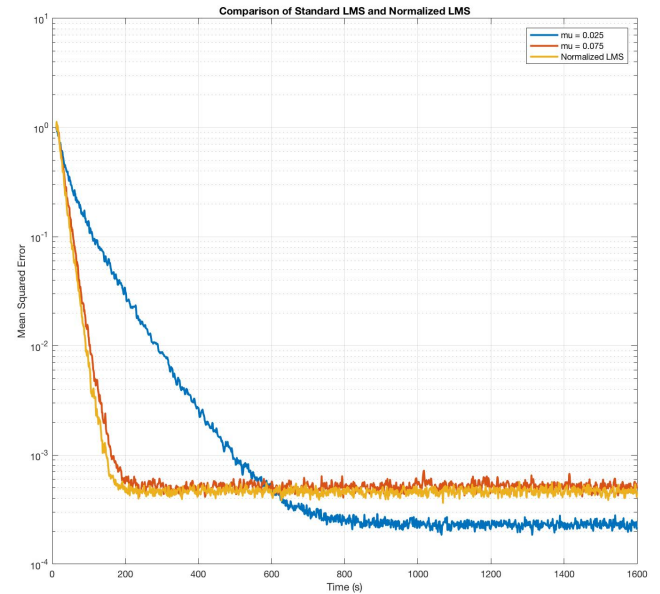


Fig. 5: BLAH BLAH

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V. CONCLUSION

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APPENDIX A

PROOF OF THE FIRST ZONKLAR EQUATION

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APPENDIX B

Appendix two text goes here.

ACKNOWLEDGMENT

The authors would like to thank...

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- [1] H. Kopka and P. W. Daly, *A Guide to L^AT_EX*, 3rd ed. Harlow, England: Addison-Wesley, 1999.

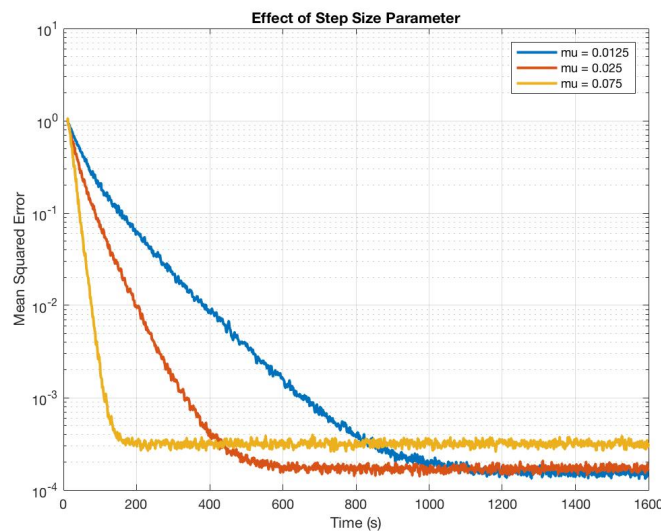


Fig. 4: BLAH BLAH

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