HW-2-1-clean

September 21, 2023

1 Computer Assignment 2 Problem 1

```
[23]: import numpy as np import matplotlib.pyplot as plt import os
```

2 Maximum Likelihood

From previous homework, used for comparison

```
[24]: # Step 1: Estimate Parameters (Mean vectors and Covariance matrices)
      def estimate_parameters(data):
          num_features = len(data[0]) - 1 # Exclude the last column (class label)
          num_classes = int(max(data, key=lambda x: x[-1])[-1]) # Assuming class_
       ⇔labels are 1-indexed
          mean_vectors = {i: np.zeros(num_features) for i in range(1, num_classes +
       →1)}
          covariance_matrices = {i: np.zeros((num\_features, num\_features))) for i in_{LL}
       →range(1, num_classes + 1)}
          class_counts = {i: 0 for i in range(1, num_classes + 1)}
          # Calculate the sum of feature values for each class
          for row in data:
              class_label = int(row[-1])
              class_counts[class_label] += 1
              for i in range(num_features):
                  mean_vectors[class_label][i] += row[i]
          # Calculate the mean vectors
          for class label in mean vectors:
              mean_vectors[class_label] /= class_counts[class_label]
          # Calculate the covariance matrices
          for row in data:
              class_label = int(row[-1])
              x_minus_mean = row[:-1] - mean_vectors[class_label]
```

```
x_minus_mean = x_minus_mean.reshape((-1, 1)) # Convert to column vector
        covariance matrices[class_label] += np.dot(x_minus_mean, x_minus_mean.T)
    for class_label in covariance_matrices:
        covariance matrices[class_label] /= (class_counts[class_label] - 1)
    return mean_vectors, covariance_matrices
# Step 2: Minimum Risk Bayes Decision Theoretic Classifier
def multivariate_normal_pdf(x, mean, covariance_matrix):
    # Calculate the multivariate normal probability density function (PDF) for
 \hookrightarrowa given test sample 'x'
    # with the given mean and covariance matrix.
    k = len(x)
    coefficient = 1.0 / ((2 * np.pi) ** (k / 2) * np.linalg.

→det(covariance_matrix))
    \# Calculate (x - mean)
    x_{minus_mean} = x - mean
    # Calculate the inverse of the covariance matrix
    inv_covariance = np.linalg.inv(covariance_matrix)
    # Calculate the Mahalanobis distance squared
    mahalanobis_dist_sq = np.dot(x minus_mean, np.dot(inv_covariance,_
 →x_minus_mean))
    # Calculate the exponent
    exponent = -0.5 * mahalanobis_dist_sq
    return coefficient * np.exp(exponent)
def minimum risk classifier(test sample, mean vectors, covariance matrices, u
 →prior_probabilities):
    num classes = len(mean vectors)
    risks = [0] * num_classes
    for class_label in range(1, num_classes + 1):
        mean_vector = np.array(mean_vectors[class_label])
        covariance_matrix = np.array(covariance_matrices[class_label])
        # Calculate the multivariate normal PDF for the current class
        pdf = multivariate_normal_pdf(test_sample, mean_vector,__
 # Calculate the risk for the current class, which is the negative \Box
 \hookrightarrow log-PDF plus the log-prior probability.
```

```
risks[class_label - 1] = -np.log(pdf) + np.
log(prior_probabilities[class_label])

# Choose the class with the minimum risk as the predicted class label.
predicted_label = np.argmin(risks) + 1
return predicted_label
```

3 k-NN classifier

```
[25]: class KNNClassifier:
          # k-Nearest Neighbors Classifier
          # first, initial the class with k value
          # then, call the class with test sample and train data
          def init (self, k num=3):
              self.k = k_num
          def __call__(self, test_sample, train_data):
              k nearest neighbors = self.compute k nearest neighbors(test sample,
       →train_data) # Get the k nearest neighbors
              class_labels = [sample[-1] for sample in k_nearest_neighbors] # Get the__
       ⇔class labels of the k nearest neighbors
              predicted label = int(max(set(class labels), key=class labels.count)) #__
       → Majority voting
              return predicted_label
          def euclidean_distance(self, x1, x2):
              # Calculate the Euclidean distance between two vectors
              return np.sqrt(np.sum((x1 - x2) ** 2))
          def compute k nearest neighbors(self, test sample, train data):
              # Compute the k nearest neighbors of the given test sample
              distances = []
              for train_sample_features in train_data:
                  test_sample_ = test_sample[:-1] # Exclude the last column (class_
       \hookrightarrow label)
                  train_sample_features_ = train_sample_features[:-1] # Exclude the_
       ⇒last column (class label)
                  distance = self.euclidean_distance(test_sample_,_
       →train_sample_features_) # Calculate the Euclidean distance
                  distances.append((train_sample_features, distance)) # Add the_
       ⇔distance along with the sample features to the list
              distances.sort(key=lambda x: x[1]) # Sort the list by the distances
              k_nearest_neighbors = [sample[0] for sample in distances[:self.k]] #__
       \hookrightarrow Get the k nearest neighbors
```

4 10-fold cross validation

```
[26]: # perform 10-fold cross validation on maximum likelihood classifier and KNNu
      \hookrightarrow classifier
     def cross validation(data, fold=10, k=3, name='Twoclass', plot=False):
        print(f"Performing \{fold\}-fold cross validation with k = \{k\}")
         # shuffle data before cross validation
        np.random.shuffle(data)
        fold_size = len(data) // fold
        accuracy scores knn = []
        accuracy_scores_mlc = []
        for i in range(fold):
            # split data into training and test data
            start = i * fold_size
            end = (i + 1) * fold_size
            data_test_fold = data[start:end]
            data_train_fold = np.concatenate([data[:start], data[end:]])
            y_test_fold = data_test_fold[:, -1]
            ########## k-NN classifier
      print(f"\nFold {i+1}")
            knn = KNNClassifier(k_num=k) # Initialize the k-NN classifier with k = 3
            y_pred = [knn(x, data_train_fold) for x in data_test_fold] # Predict_
      →the class labels of the test data
            # display results for each test sample
            print(f"Predicted labels: {y_pred}")
            accuracy = np.sum(y_pred == y_test_fold) / len(y_test_fold) # Calculate__
      → the accuracy
            # Display results for the current fold
            print(f"Number of misclassified samples: {np.sum(y_pred !=_

y_test_fold)}")
            accuracy_scores_knn.append(accuracy) # Store the accuracy for the
      ⇔current fold
            print(f"k-NN accuracy: {100*accuracy:.2f} %")
            # calculate prior probabilities from data_train_fold
            y_train_fold = data_train_fold[:, -1]
            prior_probabilities = {i: np.sum(y_train_fold == i) / len(y_train_fold)_u
      →for i in np.unique(y_train_fold)}
```

```
# print(f"Prior probabilities: {prior_probabilities}")
      mean_vectors, covariance_matrices = estimate_parameters(data_train_fold)
      mlc_predicted_labels = [] # List to store the predicted labels for the ___
\hookrightarrow current fold
      for sample in data test fold:
          test sample = sample[:-1]
          # true_label = int(sample[-1])
          predicted_label = minimum_risk_classifier(test_sample,__

mean_vectors, covariance_matrices, prior_probabilities)

          mlc_predicted_labels.append(predicted_label) # Store the predicted_
→ label for the current sample
      mlc_accuracy = 1 - (np.sum(mlc_predicted_labels != y_test_fold) /__
→len(y_test_fold))
      # Display results for the current fold
      print(f"MLC accuracy: {100*mlc accuracy:.2f} %")
      accuracy_scores_mlc.append(mlc_accuracy)
      if not plot:
          continue
      else:
          # plot the results of each fold, comparing the two classifiers
          # using 2 subplots
          # x axis: feature 3
          # y axis: feature 4
          # title: fold i
          # subplot 1: k-NN classifier
          # subplot 2: MLC classifier
          plt.figure(figsize=(10, 5))
          plt.suptitle(f"Fold {i+1}")
          plt.subplot(1, 2, 1)
          plt.title(f"k-NN classifier (k = {k}): {accuracy:.2f}")
          plt.xlabel("Feature 3")
          plt.ylabel("Feature 4")
          plt.scatter(data_train_fold[:, 2], data_train_fold[:, 3],__
⇔c=data_train_fold[:, -1])
          # test data as star with increasing size
          plt.scatter(data_test_fold[:, 2], data_test_fold[:, 3], s=150,__
→marker="*", c=y_pred)
          plt.subplot(1, 2, 2)
          plt.title(f"MLC classifier: {mlc_accuracy:.2f}")
          plt.xlabel("Feature 3")
```

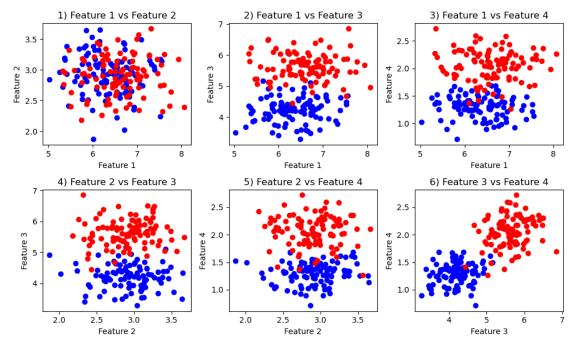
5 Two class dataset

```
[27]: file_path = "TWOCLASS.dat"
      try:
          with open(file_path, "r") as file:
              content = file.read()
              data = content.split()
              # print(data)
      except FileNotFoundError:
          print("File not found!")
      # drop the first 6 elements from list 'data'
      data = data[6:]
      data_processed = []
      for i in range(0, len(data), 5):
          data_processed.append([float(data[i]), float(data[i+1]), float(data[i+2]), \
                                 float(data[i+3]), int(data[i+4])])
      # print length of data
      print("Length of data: ", len(data_processed))
```

Length of data: 200

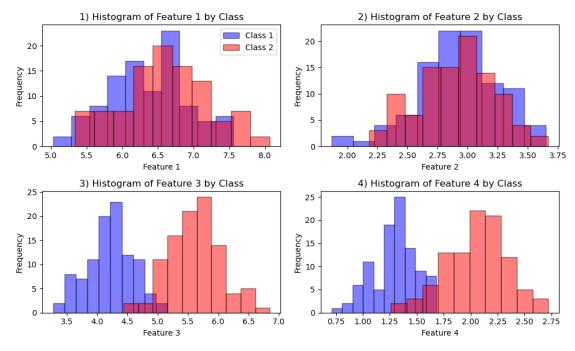
```
[28]: # make subplots of scatter plot of data with class labels for all pairs of \rightarrow features # 1 vs 2, 1 vs 3, 1 vs 4, 2 vs 3, 2 vs 4, 3 vs 4
```

```
# 6 subplots in total
# use 2 for loops to plot
# plot the data
plt.figure(figsize=(10, 6))
# plt.suptitle("Scatter plot of data with class labels")
count = 1
for i in range(0, 4):
   for j in range(i+1, 4):
       plt.subplot(2, 3, count)
       plt.title(f"{count}) Feature {i+1} vs Feature {j+1}")
       plt.xlabel(f"Feature {i+1}")
       plt.ylabel(f"Feature {j+1}")
       plt.scatter([sample[i] for sample in data_processed], [sample[j] for__
 ⇔sample in data_processed], \
                    c=[sample[-1] for sample in data_processed], cmap="bwr")
        count += 1
plt.tight_layout()
```



```
[29]: # Separate data by class
class1_data = [sample[:-1] for sample in data_processed if sample[-1] == 1]
class2_data = [sample[:-1] for sample in data_processed if sample[-1] == 2]
```

```
# Features (replace these labels with your actual feature names)
feature_labels = ['Feature 1', 'Feature 2', 'Feature 3', 'Feature 4']
# Create a subplot of 2x2 graphs, each with a size of 10x10
fig, axs = plt.subplots(2, 2, figsize=(10, 6))
# Plot histograms for each feature
for i in range(len(feature_labels)):
    ax = axs[i // 2, i \% 2] # Get the appropriate subplot
    ax.hist([x[i] for x in class1_data], bins=10, alpha=0.5, color='blue',__
 →label='Class 1', edgecolor='black')
    ax.hist([x[i] for x in class2_data], bins=10, alpha=0.5, color='red', __
 ⇔label='Class 2', edgecolor='black')
    ax.set_xlabel(feature_labels[i])
    ax.set_ylabel('Frequency')
    ax.set_title(f'{i+1}) Histogram of {feature_labels[i]} by Class')
    if i == 0:
        ax.legend()
    # ax.grid(True)
plt.tight_layout()
plt.show()
```



5.1 Results

```
[30]: \# cross_validation(np.array(data_processed), k = 3, plot = True, name = ___
       → 'Twoclass')
[31]: # run cross validation from k = 2 to 10
      # collect the average accuracy for each k
      k_{list} = [2, 3, 4, 5, 6, 7, 8, 9, 10]
      avg_accuracy_knn_list = []
      avg accuracy mlc list = []
      for k in k_list:
          avg_accuracy_knn, avg_accuracy_mlc = cross_validation(np.
       array(data_processed), fold=10, k=k, name='Twoclass', plot=False)
          avg_accuracy_knn_list.append(avg_accuracy_knn)
          avg_accuracy_mlc_list.append(avg_accuracy_mlc)
      print(f'\nk: {k_list}')
      print(f'Average accuracy for k-NN classifier: {100*np.
       →array(avg_accuracy_knn_list)} "')
      print(f'Average accuracy for MLC classifier: {100*np.
       →mean(avg_accuracy_mlc_list)} %\n')
     Performing 10-fold cross validation with k = 2
     Fold 1
     Predicted labels: [1, 2, 1, 2, 1, 2, 2, 1, 1, 1, 1, 2, 1, 1, 2, 1, 1, 1, 1, 2]
     Number of misclassified samples: 2
     k-NN accuracy: 90.00 %
     MLC accuracy: 90.00 %
     Fold 2
     Predicted labels: [1, 2, 2, 2, 1, 2, 2, 1, 1, 1, 1, 2, 2, 1, 2, 1, 2, 1, 2]
     Number of misclassified samples: 0
     k-NN accuracy: 100.00 %
     MLC accuracy: 95.00 %
     Fold 3
     Predicted labels: [2, 1, 2, 2, 1, 2, 1, 1, 1, 1, 2, 1, 1, 2, 1, 2, 2, 1, 1]
     Number of misclassified samples: 2
     k-NN accuracy: 90.00 %
     MLC accuracy: 90.00 %
     Fold 4
     Predicted labels: [2, 1, 2, 2, 1, 1, 1, 2, 1, 2, 2, 2, 1, 2, 2, 1, 2, 1, 2, 1]
     Number of misclassified samples: 0
     k-NN accuracy: 100.00 %
     MLC accuracy: 100.00 %
```

Fold 5

Predicted labels: [1, 1, 2, 2, 2, 1, 2, 1, 1, 2, 1, 1, 1, 2, 2, 1, 1, 2, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 6

Predicted labels: [2, 1, 1, 1, 2, 1, 2, 2, 2, 2, 1, 2, 1, 1, 2, 1, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 7

Predicted labels: [2, 1, 1, 2, 2, 2, 2, 2, 2, 2, 1, 2, 1, 1, 2, 1, 1, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 100.00 %

Fold 8

Predicted labels: [1, 1, 1, 2, 1, 2, 1, 1, 2, 1, 1, 2, 1, 2, 1, 1, 2, 2, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 9

Predicted labels: [2, 2, 2, 1, 2, 1, 2, 2, 2, 1, 2, 1, 1, 1, 1, 1, 1, 2, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 10

Predicted labels: [2, 1, 2, 2, 2, 1, 2, 2, 1, 1, 1, 1, 1, 1, 2, 2, 1, 2, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 100.00 %

k-NN average accuracy: 97.00 % MLC average accuracy: 97.50 %

Performing 10-fold cross validation with k = 3

Fold 1

Predicted labels: [2, 1, 2, 2, 2, 2, 1, 1, 2, 2, 1, 1, 1, 2, 1, 1, 2, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 2

Predicted labels: [2, 2, 2, 2, 1, 2, 2, 1, 1, 2, 2, 1, 2, 2, 2, 2, 2, 1, 1]

Number of misclassified samples: 2

k-NN accuracy: 90.00 % MLC accuracy: 95.00 %

Fold 3

Predicted labels: [1, 2, 2, 2, 1, 1, 2, 2, 1, 1, 1, 1, 2, 2, 1, 1, 2, 1, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 100.00 %

Fold 4

Predicted labels: [2, 2, 2, 2, 2, 1, 1, 1, 1, 2, 2, 2, 1, 2, 2, 1, 2, 1, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 5

Predicted labels: [1, 2, 1, 1, 2, 1, 1, 2, 2, 1, 2, 1, 2, 2, 1, 1, 2, 1, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 95.00 %

Fold 6

Predicted labels: [2, 2, 1, 1, 2, 2, 1, 2, 1, 1, 1, 1, 1, 1, 2, 2, 1, 1, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 7

Predicted labels: [1, 1, 1, 2, 2, 2, 1, 1, 1, 2, 2, 2, 1, 2, 2, 1, 2, 1, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 95.00 %

Fold 8

Predicted labels: [1, 2, 2, 2, 1, 2, 1, 2, 1, 1, 1, 1, 2, 2, 1, 2, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 9

Predicted labels: [1, 1, 1, 2, 1, 2, 2, 2, 2, 2, 1, 1, 2, 1, 2, 1, 1, 2, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 10

Predicted labels: [2, 2, 1, 1, 1, 1, 1, 2, 1, 1, 2, 1, 1, 2, 1, 1, 1, 1, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 95.00 %

k-NN average accuracy: 97.00 % MLC average accuracy: 98.00 %

Performing 10-fold cross validation with k = 4

Fold 1

Predicted labels: [2, 1, 1, 1, 2, 2, 2, 2, 1, 1, 2, 2, 2, 2, 1, 1, 1, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 95.00 %

Fold 2

Predicted labels: [1, 2, 2, 2, 1, 1, 1, 1, 2, 1, 2, 2, 2, 2, 1, 1, 1, 1, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 3

Predicted labels: [1, 2, 1, 1, 1, 1, 1, 2, 2, 1, 2, 1, 1, 1, 1, 1, 2, 1, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 95.00 %

Fold 4

Predicted labels: [1, 1, 1, 1, 1, 1, 2, 1, 2, 2, 1, 1, 1, 2, 1, 1, 2, 2, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 5

Predicted labels: [1, 2, 2, 1, 1, 1, 2, 1, 1, 2, 2, 1, 1, 2, 2, 1, 1, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 6

Predicted labels: [1, 1, 2, 1, 2, 2, 2, 2, 1, 1, 2, 1, 1, 2, 2, 1, 2, 2, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 95.00 %

Fold 7

Predicted labels: [1, 2, 2, 1, 2, 1, 1, 1, 1, 1, 1, 2, 2, 2, 2, 2, 2, 2, 1, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 95.00 %

MLC accuracy: 95.00 % Fold 8 Predicted labels: [1, 2, 1, 2, 1, 2, 1, 1, 2, 1, 2, 2, 1, 2, 2, 1, 2, 2, 1, 1] Number of misclassified samples: 1 k-NN accuracy: 95.00 % MLC accuracy: 100.00 % Fold 9 Predicted labels: [2, 2, 1, 2, 2, 1, 1, 1, 1, 1, 2, 2, 1, 2, 1, 2, 2, 2, 1, 2] Number of misclassified samples: 1 k-NN accuracy: 95.00 % MLC accuracy: 95.00 % Fold 10 Predicted labels: [2, 2, 1, 1, 1, 2, 2, 2, 2, 2, 2, 1, 2, 1, 1, 2, 2, 1, 1, 1] Number of misclassified samples: 0 k-NN accuracy: 100.00 % MLC accuracy: 100.00 % k-NN average accuracy: 97.00 % MLC average accuracy: 97.50 % Performing 10-fold cross validation with k = 5Fold 1 Predicted labels: [1, 1, 2, 2, 1, 2, 1, 2, 1, 1, 1, 2, 2, 2, 1, 1, 1, 1, 1] Number of misclassified samples: 0 k-NN accuracy: 100.00 % MLC accuracy: 100.00 % Fold 2 Predicted labels: [2, 1, 2, 2, 1, 1, 2, 1, 1, 2, 1, 2, 2, 1, 2, 1, 1, 2, 1] Number of misclassified samples: 1 k-NN accuracy: 95.00 % MLC accuracy: 95.00 % Fold 3 Predicted labels: [2, 2, 2, 1, 2, 1, 1, 2, 2, 2, 2, 2, 2, 1, 2, 1, 2, 1, 1, 1] Number of misclassified samples: 1 k-NN accuracy: 95.00 % MLC accuracy: 100.00 % Fold 4

Predicted labels: [2, 1, 2, 2, 1, 1, 1, 2, 1, 2, 1, 1, 1, 2, 1, 2, 1, 1, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 95.00 %

Fold 5

Predicted labels: [1, 2, 2, 2, 1, 2, 2, 1, 2, 2, 2, 1, 2, 2, 2, 1, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 6

Predicted labels: [2, 1, 2, 2, 2, 1, 1, 1, 2, 1, 1, 1, 2, 2, 1, 2, 1, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 95.00 %

Fold 7

Predicted labels: [2, 2, 1, 1, 1, 2, 1, 2, 2, 1, 1, 1, 1, 2, 1, 2, 1, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 8

Predicted labels: [2, 2, 1, 1, 1, 2, 2, 1, 2, 2, 2, 1, 2, 1, 1, 1, 1, 1, 2, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 100.00 %

Fold 9

Predicted labels: [2, 1, 1, 1, 1, 2, 2, 2, 2, 1, 2, 2, 1, 2, 1, 1, 2, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 95.00 %

Fold 10

Predicted labels: [2, 1, 2, 2, 1, 1, 2, 1, 2, 1, 2, 2, 2, 2, 1, 2, 1, 1, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

k-NN average accuracy: 97.00 % MLC average accuracy: 98.00 %

Performing 10-fold cross validation with k = 6

Fold 1

Predicted labels: [1, 1, 1, 1, 1, 2, 2, 2, 1, 1, 2, 2, 2, 1, 1, 1, 2, 2, 2]

Number of misclassified samples: 2

k-NN accuracy: 90.00 % MLC accuracy: 90.00 %

Fold 2

Predicted labels: [2, 1, 1, 2, 2, 1, 2, 1, 1, 2, 1, 1, 2, 1, 1, 2, 2, 2, 1, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 3

Predicted labels: [1, 2, 1, 1, 1, 1, 1, 1, 1, 1, 2, 1, 2, 1, 1, 1, 1, 2, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 4

Predicted labels: [2, 2, 1, 2, 1, 1, 1, 1, 2, 1, 2, 2, 2, 2, 2, 1, 1, 1, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 5

Predicted labels: [1, 2, 1, 1, 2, 2, 2, 1, 1, 1, 1, 2, 2, 2, 1, 2, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 6

Predicted labels: [2, 1, 1, 2, 2, 1, 1, 2, 2, 1, 1, 1, 2, 1, 1, 2, 1, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 100.00 %

Fold 7

Predicted labels: [2, 1, 1, 1, 2, 1, 2, 2, 2, 1, 1, 1, 2, 2, 2, 1, 2, 1, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 8

Predicted labels: [2, 1, 2, 1, 1, 2, 1, 2, 2, 2, 2, 2, 1, 2, 1, 1, 2, 2, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 100.00 %

Fold 9

Predicted labels: [2, 1, 2, 1, 2, 2, 2, 1, 2, 1, 1, 1, 2, 2, 2, 2, 1, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 95.00 %

Fold 10

Predicted labels: [1, 1, 1, 2, 2, 2, 2, 1, 1, 2, 1, 1, 1, 2, 1, 2, 1, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 95.00 %

k-NN average accuracy: 97.00 % MLC average accuracy: 98.00 %

Performing 10-fold cross validation with k = 7

Fold 1

Predicted labels: [2, 1, 2, 1, 2, 2, 2, 2, 1, 2, 2, 2, 1, 1, 2, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 2

Predicted labels: [2, 2, 2, 2, 1, 2, 1, 1, 1, 1, 1, 1, 2, 1, 1, 2, 1, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 3

Predicted labels: [1, 2, 2, 2, 1, 1, 2, 1, 1, 2, 1, 2, 1, 2, 1, 1, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 4

Predicted labels: [1, 1, 2, 1, 2, 1, 1, 2, 1, 1, 1, 1, 1, 1, 1, 1, 2, 1, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 5

Predicted labels: [2, 2, 1, 2, 2, 1, 2, 2, 2, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 1]

Number of misclassified samples: 2

k-NN accuracy: 90.00 % MLC accuracy: 90.00 %

Fold 6

Predicted labels: [1, 1, 1, 2, 1, 2, 2, 1, 2, 2, 1, 1, 1, 1, 1, 1, 1, 2, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 100.00 %

Fold 7

Predicted labels: [1, 1, 1, 1, 2, 1, 1, 1, 2, 1, 1, 1, 1, 2, 2, 2, 2, 2, 1, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 95.00 %

MLC accuracy: 95.00 % Fold 8 Predicted labels: [1, 2, 2, 1, 1, 2, 2, 1, 2, 2, 1, 2, 2, 1, 2, 1, 2, 1, 2, 2] Number of misclassified samples: 1 k-NN accuracy: 95.00 % MLC accuracy: 100.00 % Fold 9 Predicted labels: [2, 2, 1, 1, 1, 1, 1, 1, 2, 1, 2, 1, 2, 1, 1, 1, 1, 2, 1, 1] Number of misclassified samples: 1 k-NN accuracy: 95.00 % MLC accuracy: 95.00 % Fold 10 Predicted labels: [2, 2, 2, 2, 1, 1, 2, 2, 2, 2, 2, 2, 2, 1, 1, 2, 2, 1, 2] Number of misclassified samples: 0 k-NN accuracy: 100.00 % MLC accuracy: 100.00 % k-NN average accuracy: 97.00 % MLC average accuracy: 98.00 % Performing 10-fold cross validation with k = 8Fold 1 Predicted labels: [2, 1, 1, 1, 1, 1, 2, 2, 1, 1, 1, 1, 1, 2, 1, 2, 1, 1, 1, 2] Number of misclassified samples: 0 k-NN accuracy: 100.00 % MLC accuracy: 100.00 % Fold 2 Predicted labels: [2, 2, 1, 1, 2, 1, 2, 1, 1, 1, 2, 2, 2, 1, 1, 2, 1, 2, 2] Number of misclassified samples: 1 k-NN accuracy: 95.00 % MLC accuracy: 95.00 % Fold 3 Predicted labels: [2, 1, 1, 1, 2, 2, 1, 2, 1, 2, 2, 1, 1, 2, 2, 1, 1, 1, 1, 2] Number of misclassified samples: 0 k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 4

Predicted labels: [2, 1, 2, 2, 2, 2, 2, 2, 1, 1, 1, 1, 1, 2, 2, 1, 1, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 5

Predicted labels: [1, 1, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 6

Predicted labels: [1, 1, 1, 2, 2, 1, 1, 2, 1, 1, 1, 1, 2, 1, 1, 2, 1, 2]

Number of misclassified samples: 3

k-NN accuracy: 85.00 % MLC accuracy: 95.00 %

Fold 7

Predicted labels: [2, 2, 2, 1, 1, 1, 1, 1, 1, 2, 2, 2, 1, 1, 1, 1, 2, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 95.00 %

Fold 8

Predicted labels: [2, 2, 1, 2, 2, 1, 1, 1, 1, 1, 2, 2, 2, 2, 2, 2, 1, 1, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 9

Predicted labels: [2, 2, 2, 2, 2, 1, 2, 1, 1, 1, 2, 1, 2, 2, 1, 2, 1, 1, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 10

Predicted labels: [2, 2, 2, 2, 2, 1, 1, 2, 2, 2, 2, 1, 1, 1, 1, 1, 2, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 95.00 %

k-NN average accuracy: 97.00 % MLC average accuracy: 98.00 %

Performing 10-fold cross validation with k = 9

Fold 1

Predicted labels: [1, 2, 1, 2, 1, 1, 1, 1, 2, 1, 1, 2, 1, 2, 1, 2, 2, 2, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 2

Predicted labels: [1, 1, 2, 1, 2, 1, 2, 2, 1, 1, 2, 1, 2, 2, 2, 1, 2, 2, 1, 2]

Number of misclassified samples: 2

k-NN accuracy: 90.00 % MLC accuracy: 90.00 %

Fold 3

Predicted labels: [2, 2, 2, 2, 1, 1, 1, 1, 2, 2, 1, 1, 2, 1, 2, 1, 1, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 95.00 %

Fold 4

Predicted labels: [2, 2, 1, 1, 1, 1, 2, 1, 1, 1, 2, 2, 1, 2, 1, 2, 1, 1, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 5

Predicted labels: [2, 2, 2, 2, 1, 1, 1, 1, 1, 1, 1, 2, 1, 1, 1, 1, 1, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 95.00 %

Fold 6

Predicted labels: [1, 1, 1, 1, 2, 2, 1, 2, 2, 1, 2, 2, 2, 2, 1, 2, 1, 2, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 95.00 %

Fold 7

Predicted labels: [2, 1, 2, 1, 2, 2, 2, 2, 2, 2, 2, 1, 1, 1, 1, 1, 1, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 8

Predicted labels: [1, 1, 2, 1, 2, 1, 2, 1, 2, 1, 1, 1, 1, 1, 2, 2, 2, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 100.00 %

Fold 9

Predicted labels: [2, 2, 2, 2, 1, 1, 2, 2, 1, 1, 2, 2, 2, 2, 1, 2, 1, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 10

Predicted labels: [2, 2, 1, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

k-NN average accuracy: 97.00 % MLC average accuracy: 97.50 %

Performing 10-fold cross validation with k = 10

Fold 1

Predicted labels: [2, 1, 1, 1, 2, 1, 1, 1, 1, 2, 2, 1, 2, 2, 1, 2, 2, 1, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 2

Predicted labels: [1, 2, 1, 1, 2, 1, 1, 1, 1, 1, 1, 2, 1, 2, 1, 2, 1, 2, 1]

Number of misclassified samples: 2

k-NN accuracy: 90.00 % MLC accuracy: 90.00 %

Fold 3

Predicted labels: [1, 2, 1, 2, 1, 1, 1, 2, 2, 1, 1, 1, 2, 1, 2, 1, 2, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 4

Predicted labels: [2, 1, 2, 2, 2, 2, 1, 1, 1, 2, 1, 2, 2, 1, 2, 1, 2, 2, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 95.00 % MLC accuracy: 95.00 %

Fold 5

Predicted labels: [2, 1, 1, 1, 1, 1, 1, 1, 2, 2, 1, 2, 1, 2, 2, 1, 1, 1, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 6

Predicted labels: [2, 1, 1, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 2, 2, 1, 1, 1, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 7

Predicted labels: [1, 2, 1, 2, 2, 1, 2, 2, 1, 1, 2, 1, 1, 2, 1, 2, 2, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 95.00 %

```
MLC accuracy: 100.00 %
Fold 8
Predicted labels: [1, 2, 2, 1, 1, 2, 1, 2, 1, 1, 2, 1, 1, 2, 2, 1, 2, 2, 1, 2, 2]
Number of misclassified samples: 0
k-NN accuracy: 100.00 %
MLC accuracy: 100.00 %
Fold 9
Predicted labels: [1, 2, 2, 2, 1, 2, 2, 1, 1, 1, 2, 1, 1, 1, 2, 1, 1, 2, 2, 2]
Number of misclassified samples: 1
k-NN accuracy: 95.00 %
MLC accuracy: 95.00 %
Fold 10
Predicted labels: [2, 2, 1, 1, 2, 2, 2, 1, 2, 2, 1, 1, 1, 1, 1, 1, 2, 2, 1, 2]
Number of misclassified samples: 1
k-NN accuracy: 95.00 %
MLC accuracy: 100.00 %
k-NN average accuracy: 97.00 %
MLC average accuracy: 98.00 %
k: [2, 3, 4, 5, 6, 7, 8, 9, 10]
Average accuracy for k-NN classifier: [97. 97. 97. 97. 97. 97. 97. 97. 97.] %
```

6 IRIS dataset

```
file_path = "iris.pat"

try:
    with open(file_path, "r") as file:
        content = file.read()
        data = content.split()
        # print(data)

except FileNotFoundError:
    print("File not found!")

header = data[:5]
data = data[5:]

data_processed = []

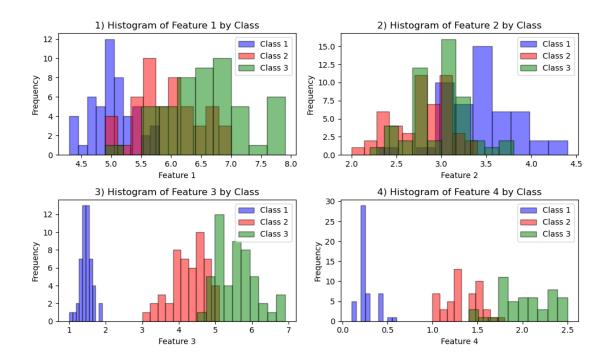
for i in range(0, len(data), 5):
    data_processed.append([float(data[i]), float(data[i+1]), float(data[i+2]), \
```

```
float(data[i+3]), int(data[i+4])])

# print length of data
print("Length of data: ", len(data_processed))
```

Length of data: 150

```
[33]: # Separate data by class
      class1_data = [sample[:-1] for sample in data_processed if sample[-1] == 1]
      class2_data = [sample[:-1] for sample in data_processed if sample[-1] == 2]
      class3_data = [sample[:-1] for sample in data_processed if sample[-1] == 3]
      # Features (replace these labels with your actual feature names)
      feature_labels = ['Feature 1', 'Feature 2', 'Feature 3', 'Feature 4']
      # Create a subplot of 2x2 graphs, each with a size of 10x10
      fig, axs = plt.subplots(2, 2, figsize=(10, 6))
      # Plot histograms for each feature
      for i in range(len(feature_labels)):
          ax = axs[i // 2, i \% 2] # Get the appropriate subplot
          ax.hist([x[i] for x in class1_data], bins=10, alpha=0.5, color='blue',
       ⇔label='Class 1', edgecolor='black')
          ax.hist([x[i] for x in class2 data], bins=10, alpha=0.5, color='red', __
       ⇔label='Class 2', edgecolor='black')
          ax.hist([x[i] for x in class3_data], bins=10, alpha=0.5, color='green', __
       →label='Class 3', edgecolor='black')
          ax.set xlabel(feature labels[i])
          ax.set_ylabel('Frequency')
          ax.set_title(f'{i+1}) Histogram of {feature_labels[i]} by Class')
          ax.legend()
          # ax.grid(True)
      plt.tight_layout()
      plt.show()
```



6.1 Results

```
# cross_validation(np.array(data_processed), k = 3, name='IRIS', plot = True)
[35]: # run cross validation from k = 2 to 10
      # collect the average accuracy for each k
      k_{list} = [2, 3, 4, 5, 6, 7, 8, 9, 10]
      avg_accuracy_knn_list = []
      avg_accuracy_mlc_list = []
      for k in k_list:
          avg_accuracy_knn, avg_accuracy_mlc = cross_validation(np.
       ⇔array(data_processed), \
                                                                 fold=10, k=k,

¬name='IRIS', plot=False)
          avg_accuracy_knn_list.append(avg_accuracy_knn)
          avg_accuracy_mlc_list.append(avg_accuracy_mlc)
      print(f'\nk: {k_list}')
      print(f'Average accuracy for k-NN classifier: {100*np.
       →array(avg_accuracy_knn_list)} %')
      print(f'Average accuracy for MLC classifier: {100*np.
       →mean(avg_accuracy_mlc_list)} %\n')
```

Performing 10-fold cross validation with k = 2

Fold 1

Predicted labels: [3, 1, 3, 2, 2, 3, 3, 2, 3, 3, 1, 3, 2, 3, 1]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 100.00 %

Fold 2

Predicted labels: [2, 2, 1, 1, 2, 2, 3, 2, 1, 2, 1, 1, 3, 3, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 3

Predicted labels: [1, 2, 2, 3, 3, 1, 2, 2, 3, 1, 1, 1, 1, 3, 2]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 100.00 %

Fold 4

Predicted labels: [1, 1, 1, 2, 2, 2, 2, 3, 1, 1, 1, 3, 1, 3, 2]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 100.00 %

Fold 5

Predicted labels: [2, 2, 3, 1, 3, 2, 2, 2, 1, 1, 3, 2, 2, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 6

Predicted labels: [3, 3, 3, 2, 3, 1, 3, 3, 3, 2, 3, 3, 1, 3, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 7

Predicted labels: [1, 1, 1, 2, 3, 2, 3, 1, 2, 1, 1, 3, 2, 1, 1]

Number of misclassified samples: 2

k-NN accuracy: 86.67 % MLC accuracy: 86.67 %

Fold 8

Predicted labels: [2, 2, 3, 3, 3, 1, 2, 3, 2, 1, 2, 2, 2, 3, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 9

Predicted labels: [1, 1, 3, 1, 2, 2, 3, 2, 3, 1, 3, 1, 3, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 100.00 %

Fold 10

Predicted labels: [3, 2, 1, 1, 2, 2, 2, 1, 3, 3, 3, 2, 2, 2, 2]

Number of misclassified samples: 2

k-NN accuracy: 86.67 % MLC accuracy: 93.33 %

k-NN average accuracy: 94.67 % MLC average accuracy: 98.00 %

Performing 10-fold cross validation with k = 3

Fold 1

Predicted labels: [1, 1, 3, 3, 2, 2, 3, 2, 2, 1, 3, 1, 3, 1, 3]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 2

Predicted labels: [1, 1, 2, 1, 2, 1, 3, 1, 1, 2, 2, 3, 2, 3, 3]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 100.00 %

Fold 3

Predicted labels: [2, 3, 2, 2, 3, 1, 2, 2, 3, 3, 2, 1, 2, 3, 3]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 93.33 %

Fold 4

Predicted labels: [3, 3, 3, 1, 3, 2, 2, 2, 2, 3, 1, 1, 2, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 5

Predicted labels: [3, 3, 1, 1, 1, 2, 2, 3, 3, 3, 2, 1, 3, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 93.33 %

Fold 6

Predicted labels: [3, 2, 3, 2, 1, 3, 3, 3, 3, 1, 1, 1, 1, 3, 3]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 7

Predicted labels: [2, 3, 2, 2, 2, 3, 2, 1, 1, 1, 1, 1, 3, 2, 3]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 8

Predicted labels: [2, 3, 1, 3, 1, 2, 1, 2, 2, 3, 2, 2, 1, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 100.00 %

Fold 9

Predicted labels: [1, 2, 1, 1, 1, 1, 3, 2, 1, 1, 1, 1, 3, 3, 2]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 93.33 %

Fold 10

Predicted labels: [2, 1, 2, 2, 1, 3, 2, 2, 1, 3, 1, 3, 3, 1, 3]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 93.33 %

k-NN average accuracy: 96.00 % MLC average accuracy: 97.33 %

Performing 10-fold cross validation with k = 4

Fold 1

Predicted labels: [1, 2, 2, 3, 2, 2, 3, 3, 3, 2, 3, 1, 2, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 2

Predicted labels: [3, 2, 2, 3, 3, 3, 2, 2, 1, 1, 2, 2, 3, 3]

Number of misclassified samples: 2

k-NN accuracy: 86.67 % MLC accuracy: 93.33 %

Fold 3

Predicted labels: [3, 1, 3, 1, 1, 1, 3, 2, 1, 2, 1, 3, 2, 1, 3]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 4

Predicted labels: [3, 1, 3, 2, 1, 3, 1, 3, 3, 2, 1, 2, 2, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 93.33 %

Fold 5

Predicted labels: [1, 1, 1, 1, 1, 2, 2, 2, 3, 1, 3, 2, 2, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 100.00 %

Fold 6

Predicted labels: [1, 3, 3, 3, 1, 1, 2, 3, 1, 3, 3, 2, 3, 3, 3]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 7

Predicted labels: [3, 1, 1, 1, 2, 1, 3, 2, 1, 3, 1, 3, 1, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 100.00 %

Fold 8

Predicted labels: [1, 1, 3, 3, 1, 2, 2, 1, 1, 2, 2, 1, 3, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 93.33 %

Fold 9

Predicted labels: [3, 3, 3, 3, 2, 2, 2, 3, 2, 2, 3, 2, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 10

Predicted labels: [2, 1, 1, 2, 1, 1, 3, 3, 1, 2, 3, 1, 3, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

k-NN average accuracy: 96.00 % MLC average accuracy: 98.00 %

Performing 10-fold cross validation with k = 5

Fold 1

Predicted labels: [3, 3, 1, 1, 1, 2, 3, 2, 3, 1, 2, 3, 2, 3, 2]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 93.33 %

Fold 2

Predicted labels: [1, 3, 1, 3, 1, 1, 1, 1, 2, 3, 3, 3, 1, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 3

Predicted labels: [1, 3, 3, 3, 2, 1, 1, 3, 2, 2, 2, 1, 1, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 4

Predicted labels: [2, 2, 1, 2, 3, 2, 2, 2, 1, 1, 1, 2, 3, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 100.00 %

Fold 5

Predicted labels: [2, 1, 1, 3, 3, 2, 3, 2, 3, 1, 1, 1, 1, 3, 2]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 93.33 %

Fold 6

Predicted labels: [3, 2, 3, 2, 1, 2, 1, 1, 3, 3, 2, 3, 2, 2, 2]

Number of misclassified samples: 2

k-NN accuracy: 86.67 % MLC accuracy: 93.33 %

Fold 7

Predicted labels: [2, 3, 2, 1, 1, 3, 3, 3, 2, 1, 2, 3, 3, 3, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 8

Predicted labels: [1, 3, 3, 3, 2, 2, 3, 2, 3, 1, 2, 3, 3, 2, 3]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 9

Predicted labels: [1, 3, 1, 1, 3, 1, 1, 2, 2, 2, 3, 1, 2, 3, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 10

Predicted labels: [1, 3, 2, 2, 1, 2, 1, 1, 3, 1, 3, 2, 1, 3, 3]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

k-NN average accuracy: 96.67 % MLC average accuracy: 98.00 %

Performing 10-fold cross validation with k = 6

Fold 1

Predicted labels: [2, 3, 1, 3, 3, 2, 3, 1, 3, 1, 1, 2, 1, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 2

Predicted labels: [1, 2, 2, 3, 2, 2, 1, 3, 1, 1, 1, 3, 2, 2, 3]

Number of misclassified samples: 2

k-NN accuracy: 86.67 % MLC accuracy: 93.33 %

Fold 3

Predicted labels: [3, 1, 2, 1, 2, 1, 3, 3, 3, 1, 3, 3, 2, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 100.00 %

Fold 4

Predicted labels: [1, 3, 2, 3, 1, 2, 1, 3, 1, 3, 2, 1, 2, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 5

Predicted labels: [3, 1, 1, 2, 1, 2, 3, 2, 2, 3, 2, 3, 1, 3, 2]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 93.33 %

Fold 6

Predicted labels: [2, 1, 3, 2, 3, 2, 1, 2, 1, 1, 3, 2, 2, 1, 3]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 7

Predicted labels: [2, 3, 3, 2, 3, 1, 2, 1, 1, 1, 2, 1, 3, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 93.33 %

Fold 8

Predicted labels: [3, 2, 3, 3, 1, 1, 3, 1, 1, 3, 2, 2, 1, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 9

Predicted labels: [3, 2, 1, 3, 2, 3, 2, 1, 2, 1, 3, 3, 3, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 93.33 %

Fold 10

Predicted labels: [2, 2, 1, 3, 1, 3, 1, 3, 3, 1, 3, 2, 2, 3, 2]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 100.00 %

k-NN average accuracy: 95.33 % MLC average accuracy: 97.33 %

Performing 10-fold cross validation with k = 7

Fold 1

Predicted labels: [1, 3, 2, 1, 2, 3, 3, 3, 1, 3, 3, 1, 1, 1, 3]

Number of misclassified samples: 2

k-NN accuracy: 86.67 % MLC accuracy: 93.33 %

Fold 2

Predicted labels: [1, 1, 2, 1, 2, 3, 3, 1, 3, 3, 2, 1, 2, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 3

Predicted labels: [3, 1, 3, 2, 3, 3, 1, 3, 2, 1, 3, 1, 1, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 100.00 %

Fold 4

Predicted labels: [2, 1, 1, 3, 1, 2, 2, 2, 2, 2, 2, 1, 3, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 93.33 %

Fold 5

Predicted labels: [3, 3, 1, 2, 1, 3, 3, 3, 3, 2, 2, 3, 2, 2, 3]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 93.33 %

Fold 6

Predicted labels: [2, 3, 2, 2, 1, 2, 1, 1, 3, 1, 3, 3, 1, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 7

Predicted labels: [3, 2, 3, 3, 2, 3, 1, 3, 2, 3, 3, 1, 1, 2, 3]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 8

Predicted labels: [3, 1, 2, 1, 3, 1, 3, 2, 3, 1, 1, 1, 2, 3, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 9

Predicted labels: [3, 2, 3, 1, 2, 1, 2, 2, 2, 2, 3, 1, 2, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 100.00 %

Fold 10

Predicted labels: [1, 2, 3, 1, 2, 2, 3, 3, 1, 1, 2, 3, 2, 3, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

k-NN average accuracy: 96.00 % MLC average accuracy: 98.00 %

Performing 10-fold cross validation with k = 8

Fold 1

Predicted labels: [2, 3, 3, 2, 1, 2, 3, 1, 3, 1, 2, 2, 2, 3, 1]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 100.00 %

Fold 2

Predicted labels: [3, 2, 3, 3, 3, 1, 1, 1, 1, 2, 2, 1, 3, 3, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 3

Predicted labels: [2, 1, 1, 3, 3, 1, 1, 3, 2, 1, 2, 2, 3, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 93.33 %

Fold 4

Predicted labels: [2, 1, 3, 3, 2, 1, 1, 3, 1, 1, 2, 3, 3, 3]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 5

Predicted labels: [3, 1, 1, 3, 2, 1, 1, 3, 2, 3, 1, 1, 3, 2, 2]

Number of misclassified samples: 2

k-NN accuracy: 86.67 % MLC accuracy: 100.00 %

Fold 6

Predicted labels: [3, 3, 2, 1, 2, 2, 3, 2, 2, 3, 2, 3, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 93.33 %

Fold 7

Predicted labels: [3, 1, 3, 2, 1, 2, 1, 2, 2, 3, 1, 2, 1, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 8

Predicted labels: [1, 1, 3, 2, 2, 2, 2, 2, 1, 2, 3, 1, 1, 1, 3]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 100.00 %

Fold 9

Predicted labels: [3, 1, 1, 1, 3, 3, 3, 3, 3, 1, 3, 2, 1, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 10

Predicted labels: [1, 2, 1, 2, 1, 2, 3, 3, 2, 2, 2, 2, 2, 3, 1]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 93.33 %

k-NN average accuracy: 96.00 % MLC average accuracy: 98.00 %

Performing 10-fold cross validation with k = 9

Fold 1

Predicted labels: [1, 2, 1, 1, 3, 1, 1, 1, 3, 3, 2, 2, 3, 2, 3]

Number of misclassified samples: 2

k-NN accuracy: 86.67 % MLC accuracy: 100.00 %

Fold 2

Predicted labels: [2, 2, 3, 1, 1, 1, 3, 3, 2, 1, 2, 2, 3, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 93.33 %

Fold 3

Predicted labels: [2, 1, 1, 2, 1, 1, 1, 3, 1, 1, 1, 1, 2, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 4

Predicted labels: [2, 2, 3, 3, 3, 2, 3, 3, 3, 3, 3, 1, 1, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 93.33 %

Fold 5

Predicted labels: [3, 1, 1, 2, 1, 1, 2, 1, 1, 2, 2, 1, 1, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 6

Predicted labels: [2, 1, 3, 3, 3, 3, 3, 2, 3, 2, 3, 3, 3, 3]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 7

Predicted labels: [1, 2, 2, 2, 3, 1, 3, 1, 3, 3, 3, 1, 2, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 100.00 %

Fold 8

Predicted labels: [3, 1, 1, 3, 3, 1, 1, 2, 3, 3, 2, 3, 1, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 9

Predicted labels: [3, 2, 3, 1, 2, 1, 2, 2, 2, 1, 3, 3, 2, 3, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 93.33 %

Fold 10

Predicted labels: [3, 3, 3, 3, 2, 1, 2, 1, 2, 2, 2, 2, 1, 3, 2]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 100.00 %

k-NN average accuracy: 96.67 % MLC average accuracy: 98.00 %

Performing 10-fold cross validation with k = 10

Fold 1

Predicted labels: [2, 3, 3, 2, 3, 1, 3, 3, 3, 3, 3, 2, 3, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 93.33 %

Fold 2

Predicted labels: [3, 3, 1, 2, 2, 3, 2, 2, 2, 1, 3, 2, 3, 1, 3]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 3

Predicted labels: [3, 3, 1, 1, 1, 2, 1, 2, 3, 1, 2, 1, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 4

Predicted labels: [3, 2, 3, 2, 2, 1, 3, 3, 1, 2, 3, 1, 1, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 93.33 %

Fold 5

Predicted labels: [1, 2, 3, 1, 3, 2, 3, 1, 2, 3, 1, 1, 3, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 6

Predicted labels: [2, 3, 3, 1, 3, 1, 2, 1, 2, 1, 1, 2, 3, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 93.33 %

Fold 7

Predicted labels: [1, 1, 3, 1, 1, 3, 1, 1, 1, 1, 3, 3, 1, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 8

Predicted labels: [3, 1, 2, 3, 1, 2, 3, 2, 1, 3, 3, 1, 2, 3, 1]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

Fold 9

Predicted labels: [2, 2, 2, 2, 2, 1, 3, 2, 1, 2, 3, 2, 3, 2]

Number of misclassified samples: 1

k-NN accuracy: 93.33 % MLC accuracy: 100.00 %

Fold 10

Predicted labels: [1, 2, 1, 1, 1, 3, 2, 1, 2, 3, 2, 3, 1, 3, 3]

Number of misclassified samples: 0

k-NN accuracy: 100.00 % MLC accuracy: 100.00 %

k-NN average accuracy: 98.67 % MLC average accuracy: 98.00 %

k: [2, 3, 4, 5, 6, 7, 8, 9, 10]

Average accuracy for k-NN classifier: [94.66666667 96. 96.

```
96.6666667 95.33333333 96.

96. 96.66666667 98.66666667] %

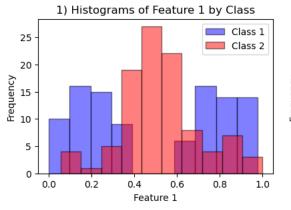
Average accuracy for MLC classifier: 97.85185185185186 %
```

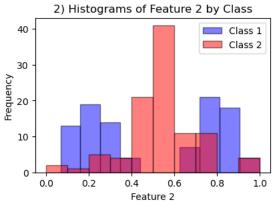
7 CROSS dataset

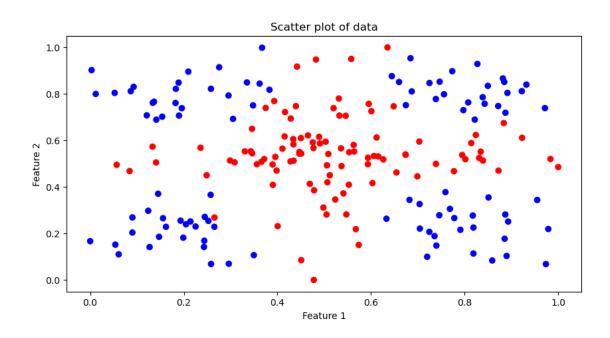
```
[36]: file_path = "cross.pat"
      try:
          with open(file_path, "r") as file:
              content = file.read()
              data = content.split()
              # print(data)
      except FileNotFoundError:
          print("File not found!")
      data = np.array(data).reshape(-1, 5).T
      print(data.shape)
      f1 = data[1].astype(float)
      f2 = data[2].astype(float)
      class_labels = data[4].astype(int) + 1 # Convert class labels from O-indexed to_
       \hookrightarrow 1-indexed
      data_processed = np.array([f1, f2, class_labels]).T
     (5, 200)
[37]: # Separate data by class
      class1_data = [sample[:-1] for sample in data_processed if sample[-1] == 1]
      class2_data = [sample[:-1] for sample in data_processed if sample[-1] == 2]
      # Features (replace these labels with your actual feature names)
      feature_labels = ['Feature 1', 'Feature 2']
      # Create a subplot of 2x2 graphs, each with a size of 10x10
      fig, axs = plt.subplots(1, 2, figsize=(10, 3))
      # Plot histograms for each feature
      for i in range(len(feature_labels)):
          ax = axs[i]
          ax.hist([x[i] for x in class1_data], bins=10, alpha=0.5, color='blue',_
       ⇔label='Class 1', edgecolor='black')
          ax.hist([x[i] for x in class2_data], bins=10, alpha=0.5, color='red', u
       ⇔label='Class 2', edgecolor='black')
          ax.set_xlabel(feature_labels[i])
          ax.set_ylabel('Frequency')
          ax.set_title(f'{i+1}) Histograms of {feature_labels[i]} by Class')
```

```
ax.legend()
  # ax.grid(True)

# plot scatter plot of data
plt.figure(figsize=(10, 5))
plt.title("Scatter plot of data")
plt.xlabel("Feature 1")
plt.ylabel("Feature 2")
plt.scatter(f1, f2, c=class_labels, cmap='bwr')
plt.show()
```







```
[38]: # define the function again because the structure of data is different (only ...
      ⇔plotting is changed)
     # perform 10-fold cross validation on maximum likelihood classifier and KNN
      \hookrightarrow classifier
     def cross_validation(data, fold=10, k=3, name='CROSS', plot=False):
         print(f"Performing {fold}-fold cross validation with k = {k}")
         # shuffle data before cross validation
         np.random.shuffle(data)
         fold_size = len(data) // fold
         accuracy_scores_knn = []
         accuracy_scores_mlc = []
         for i in range(fold):
            # split data into training and test data
            start = i * fold_size
            end = (i + 1) * fold_size
            data_test_fold = data[start:end]
            data_train_fold = np.concatenate([data[:start], data[end:]])
            y_test_fold = data_test_fold[:, -1]
            ########### k-NN classifier
      print(f"\nFold {i+1}")
            knn = KNNClassifier(k_num=k) # Initialize the k-NN classifier with k = 3
            y_pred = [knn(x, data_train_fold) for x in data_test_fold] # Predict_
      →the class labels of the test data
            # display results for each test sample
            print(f"Predicted labels: {y_pred}")
            accuracy = np.sum(y_pred == y_test_fold) / len(y_test_fold) # Calculate__
      → the accuracy
            # Display results for the current fold
            print(f"Number of misclassified samples: {np.sum(y_pred !=_
      y test fold)}")
            accuracy_scores_knn.append(accuracy) # Store the accuracy for the
      ⇔current fold
            print(f"k-NN accuracy: {accuracy:.2f}")
            # calculate prior probabilities from data_train_fold
            y_train_fold = data_train_fold[:, -1]
            prior_probabilities = {i: np.sum(y_train_fold == i) / len(y_train_fold)_u
      →for i in np.unique(y_train_fold)}
            # print(f"Prior probabilities: {prior_probabilities}")
            mean_vectors, covariance_matrices = estimate_parameters(data_train_fold)
```

```
mlc_predicted_labels = [] # List to store the predicted labels for the_
⇔current fold
      for sample in data test fold:
          test_sample = sample[:-1]
          # true label = int(sample[-1])
          predicted_label = minimum_risk_classifier(test_sample,__

¬mean_vectors, covariance_matrices, prior_probabilities)

          mlc_predicted_labels.append(predicted_label) # Store the predicted_
⇔label for the current sample
      mlc accuracy = 1 - (np.sum(mlc predicted labels != y test fold) / |
→len(y_test_fold))
      # Display results for the current fold
      print(f"MLC accuracy: {mlc_accuracy:.2f}")
      accuracy_scores_mlc.append(mlc_accuracy)
      if not plot:
          continue
      else:
          # plot the results of each fold, comparing the two classifiers
          # using 2 subplots
          # x axis: feature 1
          # y axis: feature 2
          # training data: class 1: red, class 2: blue
          # test data: class 1: orange, class 2: green
          # title: fold i
          \# subplot 1: k-NN classifier
          # subplot 2: MLC classifier
          plt.figure(figsize=(10, 5))
          plt.suptitle(f"Fold {i+1}")
          plt.subplot(1, 2, 1)
          plt.title(f"k-NN classifier (k = {k}): {accuracy:.2f}")
         plt.xlabel("Feature 1")
          plt.ylabel("Feature 2")
          plt.scatter(data_train_fold[:, 0], data_train_fold[:, 1],__
⇔c=data_train_fold[:, -1])
          # test data as star with increasing size
          plt.scatter(data_test_fold[:, 0], data_test_fold[:, 1], s=150,__
→marker="*", c=y_pred)
          plt.subplot(1, 2, 2)
          plt.title(f"MLC classifier: {mlc_accuracy:.2f}")
          plt.xlabel("Feature 1")
```

```
plt.ylabel("Feature 2")
    plt.scatter(data_train_fold[:, 0], data_train_fold[:, 1],
c=data_train_fold[:, -1])
    plt.scatter(data_test_fold[:, 0], data_test_fold[:, 1], s=150,
marker="*", c=mlc_predicted_labels) # PiYG
    plt.legend(("Training", "Test"))
    os.makedirs(f"HW1-{name}", exist_ok=True)
    plt.savefig(f"HW1-{name}/fold_{i+1}.png")
    # plt.show()
    plt.close()

avg_accuracy_knn = np.mean(accuracy_scores_knn)
    avg_accuracy_mlc = np.mean(accuracy_scores_mlc)
    print(f"\nk-NN average accuracy: {100*avg_accuracy_knn:.2f} %")
    print(f"MLC average accuracy: {100*avg_accuracy_mlc:.2f} %")
    return avg_accuracy_knn, avg_accuracy_mlc
```

7.1 Results

```
[39]: \# cross validation(np.array(data processed), k = 3, name='CROSS', plot = True)
[40]: \# run cross validation from k = 2 to 10
      # collect the average accuracy for each k
      k_{list} = [2, 3, 4, 5, 6, 7, 8, 9, 10]
      avg_accuracy_knn_list = []
      avg_accuracy_mlc_list = []
      for k in k_list:
          avg_accuracy_knn, avg_accuracy_mlc = cross_validation(np.
       ⇔array(data_processed), fold=10, k=k, name='CROSS', plot=False)
          avg_accuracy_knn_list.append(avg_accuracy_knn)
          avg_accuracy_mlc_list.append(avg_accuracy_mlc)
      print(f'\nk: {k_list}')
      print(f'Average accuracy for k-NN classifier: {100*np.
       →array(avg_accuracy_knn_list)} %')
      print(f'Average accuracy for MLC classifier: {100*np.
       →mean(avg_accuracy_mlc_list)} %\n')
     Performing 10-fold cross validation with k = 2
     Fold 1
     Predicted labels: [2, 1, 2, 1, 1, 1, 1, 2, 1, 1, 2, 2, 1, 1, 1, 2, 2, 1, 1, 1]
     Number of misclassified samples: 2
     k-NN accuracy: 0.90
     MLC accuracy: 0.60
```

Predicted labels: [2, 1, 1, 2, 1, 2, 1, 1, 2, 2, 2, 1, 1, 2, 1, 2, 1, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.65

Fold 3

Predicted labels: [1, 1, 2, 1, 1, 1, 2, 1, 1, 2, 2, 1, 1, 1, 1, 2, 2, 2, 1, 2]

Number of misclassified samples: 4

k-NN accuracy: 0.80 MLC accuracy: 0.65

Fold 4

Predicted labels: [2, 2, 1, 2, 2, 1, 2, 2, 1, 1, 1, 2, 1, 1, 1, 1, 1, 1, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.95 MLC accuracy: 0.70

Fold 5

Predicted labels: [1, 1, 2, 2, 2, 1, 2, 1, 1, 1, 2, 2, 2, 1, 1, 2, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.75

Fold 6

Predicted labels: [2, 1, 1, 1, 1, 1, 2, 2, 1, 2, 1, 1, 1, 2, 1, 1, 1]

Number of misclassified samples: 2

k-NN accuracy: 0.90 MLC accuracy: 0.70

Fold 7

Predicted labels: [2, 1, 2, 2, 1, 1, 1, 1, 1, 2, 2, 1, 1, 1, 2, 1, 2, 2, 2]

Number of misclassified samples: 2

k-NN accuracy: 0.90 MLC accuracy: 0.65

Fold 8

Predicted labels: [2, 1, 2, 2, 1, 1, 2, 1, 1, 2, 2, 1, 1, 1, 1, 1, 2, 2, 1, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.95 MLC accuracy: 0.70

Fold 9

Predicted labels: [1, 2, 1, 1, 2, 1, 1, 1, 1, 1, 2, 2, 2, 2, 2, 1, 1, 2, 2, 2]

Number of misclassified samples: 2

k-NN accuracy: 0.90 MLC accuracy: 0.70

Predicted labels: [2, 1, 2, 1, 1, 2, 1, 1, 2, 2, 1, 1, 1, 1, 1, 2, 1, 1, 2, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.95 MLC accuracy: 0.60

k-NN average accuracy: 92.50 % MLC average accuracy: 67.00 %

Performing 10-fold cross validation with k = 3

Fold 1

Predicted labels: [1, 2, 1, 1, 1, 2, 2, 2, 1, 1, 1, 1, 1, 2, 2, 1, 2, 1, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.65

Fold 2

Predicted labels: [1, 1, 2, 1, 1, 1, 2, 2, 1, 2, 1, 2, 1, 2, 1, 2, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.70

Fold 3

Predicted labels: [2, 1, 2, 2, 1, 2, 1, 2, 1, 1, 2, 2, 2, 2, 1, 1, 2, 1, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.95 MLC accuracy: 0.75

Fold 4

Predicted labels: [1, 2, 1, 1, 1, 2, 2, 1, 2, 2, 2, 2, 1, 1, 1, 1, 1, 1, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.95 MLC accuracy: 0.80

Fold 5

Predicted labels: [2, 1, 1, 2, 2, 2, 2, 1, 1, 1, 1, 2, 2, 1, 1, 1, 1, 2, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.60

Fold 6

Predicted labels: [2, 1, 1, 2, 2, 2, 2, 1, 1, 1, 1, 1, 1, 1, 2, 1, 1, 1, 1]

Number of misclassified samples: 5

k-NN accuracy: 0.75 MLC accuracy: 0.50

Fold 7

Predicted labels: [2, 1, 2, 2, 2, 2, 1, 2, 1, 1, 2, 2, 2, 1, 2, 1, 2, 1, 2, 2]

```
Number of misclassified samples: 0
k-NN accuracy: 1.00
MLC accuracy: 0.75
Fold 8
Predicted labels: [2, 2, 1, 2, 1, 1, 1, 1, 1, 1, 1, 2, 2, 1, 1, 1, 2, 1, 2, 2]
Number of misclassified samples: 0
k-NN accuracy: 1.00
MLC accuracy: 0.40
Fold 9
Predicted labels: [2, 1, 2, 2, 2, 1, 2, 2, 2, 2, 2, 1, 1, 2, 1, 1, 2, 1, 2, 1]
Number of misclassified samples: 0
k-NN accuracy: 1.00
MLC accuracy: 0.75
Fold 10
Predicted labels: [2, 2, 1, 2, 2, 2, 1, 2, 1, 2, 1, 1, 2, 2, 2, 2, 1, 1, 1, 1]
Number of misclassified samples: 4
k-NN accuracy: 0.80
MLC accuracy: 0.60
k-NN average accuracy: 94.50 %
MLC average accuracy: 65.00 %
Performing 10-fold cross validation with k = 4
Fold 1
Predicted labels: [1, 2, 1, 1, 1, 1, 1, 2, 2, 2, 1, 1, 2, 2, 1, 1, 2, 1, 1, 2]
Number of misclassified samples: 1
k-NN accuracy: 0.95
MLC accuracy: 0.60
Fold 2
Predicted labels: [1, 1, 2, 1, 1, 1, 1, 2, 1, 1, 2, 1, 2, 1, 2, 1, 2, 1, 1, 1, 1]
Number of misclassified samples: 1
k-NN accuracy: 0.95
MLC accuracy: 0.55
Fold 3
Predicted labels: [2, 1, 2, 1, 1, 1, 1, 1, 1, 2, 2, 1, 1, 2, 1, 1, 2, 1]
Number of misclassified samples: 0
k-NN accuracy: 1.00
MLC accuracy: 0.60
```

Predicted labels: [2, 2, 1, 1, 2, 2, 2, 1, 1, 1, 1, 2, 1, 2, 2, 1, 2, 2, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 1.00

MLC accuracy: 0.80 Fold 5 Predicted labels: [1, 2, 2, 2, 2, 1, 1, 2, 2, 2, 2, 2, 1, 1, 1, 1, 1, 1, 2, 1] Number of misclassified samples: 0 k-NN accuracy: 1.00 MLC accuracy: 0.75 Fold 6 Predicted labels: [1, 2, 1, 2, 1, 2, 2, 2, 2, 2, 1, 1, 1, 1, 1, 1, 1, 1] Number of misclassified samples: 2 k-NN accuracy: 0.90 MLC accuracy: 0.70 Fold 7 Predicted labels: [1, 1, 2, 2, 2, 1, 1, 2, 2, 1, 1, 2, 1, 2, 1, 1, 2, 2, 2, 1] Number of misclassified samples: 0 k-NN accuracy: 1.00 MLC accuracy: 0.60 Fold 8 Predicted labels: [2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 2, 2, 2, 1, 1, 1, 1, 1, 1] Number of misclassified samples: 3 k-NN accuracy: 0.85 MLC accuracy: 0.65 Fold 9 Predicted labels: [1, 1, 1, 2, 1, 1, 2, 2, 1, 2, 1, 2, 2, 2, 2, 2, 1, 2, 1, 2] Number of misclassified samples: 2 k-NN accuracy: 0.90 MLC accuracy: 0.70 Fold 10 Predicted labels: [2, 2, 1, 2, 1, 2, 2, 1, 1, 2, 1, 1, 2, 2, 1, 1, 1, 1, 1, 2, 1] Number of misclassified samples: 0 k-NN accuracy: 1.00 MLC accuracy: 0.70 k-NN average accuracy: 95.50 % MLC average accuracy: 66.50 % Performing 10-fold cross validation with k = 5

Fold 1

Predicted labels: [1, 2, 2, 1, 1, 1, 1, 1, 1, 2, 2, 2, 1, 2, 2, 1, 1, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.95 MLC accuracy: 0.70

Predicted labels: [1, 1, 2, 2, 2, 2, 1, 2, 1, 1, 1, 2, 2, 2, 1, 2, 2, 2, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.80

Fold 3

Predicted labels: [2, 2, 2, 1, 2, 1, 2, 1, 1, 1, 2, 1, 1, 1, 2, 1, 2, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.95
MLC accuracy: 0.65

Fold 4

Predicted labels: [1, 2, 1, 1, 1, 1, 1, 1, 1, 2, 1, 1, 1, 2, 2, 2, 2, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.95 MLC accuracy: 0.75

Fold 5

Predicted labels: [2, 1, 1, 2, 1, 2, 2, 1, 2, 2, 1, 2, 1, 2, 1, 2, 2, 2, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.95 MLC accuracy: 0.70

Fold 6

Predicted labels: [1, 1, 2, 1, 2, 2, 1, 1, 1, 2, 1, 2, 2, 2, 2, 2, 1, 2, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.95 MLC accuracy: 0.75

Fold 7

Predicted labels: [1, 1, 2, 2, 2, 2, 1, 1, 1, 2, 1, 1, 2, 1, 1, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.95
MLC accuracy: 0.60

Fold 8

Predicted labels: [1, 2, 1, 2, 2, 2, 1, 1, 1, 1, 2, 2, 2, 2, 2, 2, 2, 1, 1, 1]

Number of misclassified samples: 2

k-NN accuracy: 0.90 MLC accuracy: 0.60

Fold 9

Predicted labels: [2, 1, 2, 1, 2, 1, 2, 1, 1, 2, 1, 2, 1, 1, 1, 1, 2, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.60

Predicted labels: [1, 1, 2, 1, 2, 1, 1, 1, 1, 2, 2, 2, 2, 2, 1, 1, 1, 1, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.95 MLC accuracy: 0.60

k-NN average accuracy: 95.50 % MLC average accuracy: 67.50 %

Performing 10-fold cross validation with k = 6

Fold 1

Predicted labels: [1, 2, 2, 2, 1, 2, 1, 2, 2, 2, 2, 1, 2, 1, 2, 2, 1, 1, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.85

Fold 2

Predicted labels: [2, 2, 1, 1, 1, 1, 1, 2, 1, 1, 1, 2, 2, 1, 2, 2, 2, 1, 1, 2]

Number of misclassified samples: 3

k-NN accuracy: 0.85 MLC accuracy: 0.70

Fold 3

Predicted labels: [1, 1, 2, 2, 2, 2, 1, 2, 2, 2, 2, 2, 1, 1, 1, 1, 2, 1, 1, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.95 MLC accuracy: 0.80

Fold 4

Predicted labels: [1, 1, 1, 1, 2, 2, 2, 1, 1, 1, 1, 1, 2, 1, 1, 2, 1, 1, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.60

Fold 5

Predicted labels: [1, 1, 1, 2, 2, 1, 1, 2, 2, 2, 2, 1, 2, 1, 1, 2, 2, 2, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.95 MLC accuracy: 0.80

Fold 6

Predicted labels: [2, 1, 2, 1, 2, 1, 2, 1, 1, 1, 2, 2, 1, 1, 2, 2, 1, 1, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.95 MLC accuracy: 0.60

Fold 7

Predicted labels: [1, 1, 1, 2, 1, 2, 2, 1, 2, 1, 1, 2, 2, 1, 2, 2, 1, 2, 2, 1]

```
Number of misclassified samples: 1
k-NN accuracy: 0.95
MLC accuracy: 0.75
Fold 8
Predicted labels: [2, 2, 1, 1, 1, 2, 1, 1, 2, 1, 1, 1, 1, 1, 1, 2, 2, 1, 1, 1]
Number of misclassified samples: 1
k-NN accuracy: 0.95
MLC accuracy: 0.70
Fold 9
Predicted labels: [1, 2, 1, 2, 1, 1, 1, 2, 2, 1, 1, 1, 2, 2, 1, 1, 2, 2, 1, 1]
Number of misclassified samples: 2
k-NN accuracy: 0.90
MLC accuracy: 0.55
Fold 10
Predicted labels: [2, 2, 2, 1, 1, 1, 1, 2, 1, 1, 1, 2, 2, 1, 2, 1, 2, 1, 1, 1]
Number of misclassified samples: 0
k-NN accuracy: 1.00
MLC accuracy: 0.45
k-NN average accuracy: 95.00 %
MLC average accuracy: 68.00 %
Performing 10-fold cross validation with k = 7
Fold 1
Predicted labels: [1, 1, 1, 2, 1, 1, 2, 1, 1, 2, 1, 1, 2, 1, 1, 2, 1]
Number of misclassified samples: 2
k-NN accuracy: 0.90
MLC accuracy: 0.35
Fold 2
Predicted labels: [1, 1, 1, 2, 2, 1, 1, 1, 2, 1, 2, 1, 1, 2, 1, 2, 2, 2, 1, 1]
Number of misclassified samples: 2
k-NN accuracy: 0.90
MLC accuracy: 0.65
Fold 3
Predicted labels: [2, 1, 1, 1, 1, 2, 2, 1, 1, 2, 1, 2, 1, 2, 2, 2, 1, 2, 1, 2]
Number of misclassified samples: 1
k-NN accuracy: 0.95
MLC accuracy: 0.80
Fold 4
```

Number of misclassified samples: 0

k-NN accuracy: 1.00

Predicted labels: [2, 1, 2, 1, 1, 2, 1, 2, 1, 2, 2, 2, 2, 2, 2, 1, 2, 2, 1, 1]

MLC accuracy: 0.70 Fold 5 Predicted labels: [1, 2, 2, 2, 2, 1, 1, 1, 1, 2, 2, 2, 1, 1, 2, 2, 2, 1, 2] Number of misclassified samples: 1 k-NN accuracy: 0.95 MLC accuracy: 0.65 Fold 6 Predicted labels: [2, 2, 2, 1, 1, 1, 2, 2, 1, 1, 2, 2, 2, 1, 1, 1, 1, 1, 1, 1] Number of misclassified samples: 2 k-NN accuracy: 0.90 MLC accuracy: 0.60 Fold 7 Predicted labels: [2, 1, 2, 1, 1, 2, 1, 1, 1, 1, 2, 1, 2, 1, 2, 1, 2, 2, 1] Number of misclassified samples: 0 k-NN accuracy: 1.00 MLC accuracy: 0.65 Fold 8 Predicted labels: [1, 2, 2, 1, 1, 1, 1, 1, 1, 2, 2, 1, 2, 1, 2, 1, 1, 2, 1, 1] Number of misclassified samples: 0 k-NN accuracy: 1.00 MLC accuracy: 0.65 Fold 9 Predicted labels: [2, 1, 1, 1, 1, 2, 2, 2, 1, 2, 2, 2, 2, 2, 2, 1, 1, 2, 1, 1] Number of misclassified samples: 0 k-NN accuracy: 1.00 MLC accuracy: 0.65 Fold 10 Predicted labels: [2, 2, 2, 1, 2, 2, 1, 1, 1, 2, 2, 1, 1, 1, 2, 2, 1, 2, 2, 1] Number of misclassified samples: 0 k-NN accuracy: 1.00 MLC accuracy: 0.85

k-NN average accuracy: 96.00 % MLC average accuracy: 65.50 %

Performing 10-fold cross validation with k = 8

Fold 1

Predicted labels: [1, 2, 2, 2, 1, 1, 2, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 1, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.95 MLC accuracy: 0.75

Predicted labels: [1, 1, 1, 2, 1, 2, 2, 1, 1, 2, 1, 1, 1, 1, 1, 1, 2, 2, 2, 2]

Number of misclassified samples: 2

k-NN accuracy: 0.90 MLC accuracy: 0.75

Fold 3

Predicted labels: [1, 2, 1, 1, 2, 2, 1, 1, 2, 1, 1, 1, 2, 2, 1, 1, 2, 1, 1, 2]

Number of misclassified samples: 2

k-NN accuracy: 0.90 MLC accuracy: 0.65

Fold 4

Predicted labels: [1, 1, 1, 2, 2, 1, 2, 1, 2, 1, 1, 2, 1, 1, 1, 2, 1, 1, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.70

Fold 5

Predicted labels: [1, 1, 1, 2, 2, 1, 1, 1, 2, 2, 1, 1, 1, 2, 2, 2, 1, 2, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.70

Fold 6

Predicted labels: [2, 1, 1, 1, 1, 1, 2, 2, 2, 1, 1, 1, 2, 2, 2, 1, 1, 2, 1, 2]

Number of misclassified samples: 2

k-NN accuracy: 0.90 MLC accuracy: 0.60

Fold 7

Predicted labels: [2, 1, 2, 1, 2, 1, 2, 1, 1, 2, 1, 1, 2, 1, 1, 2, 2, 1, 2, 2]

Number of misclassified samples: 4

k-NN accuracy: 0.80 MLC accuracy: 0.70

Fold 8

Predicted labels: [2, 2, 2, 2, 2, 1, 2, 2, 2, 2, 1, 1, 1, 1, 2, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.95 MLC accuracy: 0.65

Fold 9

Predicted labels: [1, 1, 1, 1, 2, 2, 1, 1, 1, 1, 1, 1, 2, 1, 1, 1, 1, 2, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.55

```
Fold 10
```

Predicted labels: [1, 2, 1, 1, 2, 2, 1, 2, 1, 1, 2, 2, 2, 1, 1, 2, 1, 1, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.60

k-NN average accuracy: 94.00 % MLC average accuracy: 66.50 %

Performing 10-fold cross validation with k = 9

Fold 1

Predicted labels: [2, 1, 2, 2, 1, 1, 1, 2, 2, 2, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.95 MLC accuracy: 0.65

Fold 2

Predicted labels: [1, 1, 2, 1, 2, 2, 1, 1, 2, 1, 1, 1, 1, 1, 1, 1, 2, 1, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.50

Fold 3

Predicted labels: [2, 2, 2, 2, 1, 2, 1, 1, 2, 1, 2, 2, 2, 1, 1, 1, 1, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.85

Fold 4

Predicted labels: [1, 2, 1, 1, 2, 2, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 1, 1, 1]

Number of misclassified samples: 2

k-NN accuracy: 0.90 MLC accuracy: 0.65

Fold 5

Predicted labels: [2, 1, 1, 1, 1, 1, 1, 1, 2, 1, 2, 2, 1, 1, 1, 2, 2, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.50

Fold 6

Predicted labels: [1, 1, 2, 1, 1, 2, 2, 1, 2, 2, 1, 1, 1, 1, 1, 1, 2, 2, 2, 1, 2]

Number of misclassified samples: 2

k-NN accuracy: 0.90 MLC accuracy: 0.70

Fold 7

Predicted labels: [1, 2, 2, 2, 1, 1, 1, 1, 2, 1, 2, 2, 1, 1, 2, 1, 1, 1, 1, 2]

```
Number of misclassified samples: 4
k-NN accuracy: 0.80
MLC accuracy: 0.55
Fold 8
Predicted labels: [2, 2, 1, 1, 2, 1, 1, 1, 2, 2, 2, 2, 1, 2, 2, 1, 2, 2, 1, 2]
Number of misclassified samples: 1
k-NN accuracy: 0.95
MLC accuracy: 0.70
Fold 9
Predicted labels: [2, 1, 2, 1, 2, 1, 1, 1, 2, 1, 2, 2, 1, 1, 2, 2, 1, 2, 2, 1]
Number of misclassified samples: 2
k-NN accuracy: 0.90
MLC accuracy: 0.70
Fold 10
Predicted labels: [2, 2, 1, 1, 1, 2, 2, 1, 1, 1, 1, 2, 1, 2, 2, 1, 2, 1, 2, 2]
Number of misclassified samples: 1
k-NN accuracy: 0.95
MLC accuracy: 0.70
k-NN average accuracy: 93.50 %
MLC average accuracy: 65.00 %
Performing 10-fold cross validation with k = 10
Fold 1
Predicted labels: [2, 2, 1, 2, 1, 1, 1, 1, 1, 1, 1, 2, 1, 2, 1, 1, 1, 1, 2, 1]
Number of misclassified samples: 1
k-NN accuracy: 0.95
MLC accuracy: 0.65
Fold 2
Predicted labels: [2, 2, 1, 2, 2, 2, 1, 2, 1, 1, 2, 2, 1, 1, 1, 1, 1, 1, 2, 1, 2]
Number of misclassified samples: 0
k-NN accuracy: 1.00
MLC accuracy: 0.75
Fold 3
Predicted labels: [2, 1, 1, 1, 2, 1, 1, 1, 1, 1, 2, 2, 2, 1, 1, 2, 1, 2, 1, 1]
Number of misclassified samples: 1
k-NN accuracy: 0.95
MLC accuracy: 0.55
```

Predicted labels: [2, 1, 1, 2, 2, 1, 2, 1, 1, 1, 1, 1, 1, 1, 2, 1, 1, 1, 1]

Number of misclassified samples: 3

k-NN accuracy: 0.85

MLC accuracy: 0.60

Fold 5

Predicted labels: [2, 1, 1, 2, 1, 1, 2, 1, 2, 2, 1, 1, 2, 2, 2, 2, 1, 1, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.65

Fold 6

Predicted labels: [1, 2, 2, 2, 1, 2, 2, 1, 2, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 1]

Number of misclassified samples: 2

k-NN accuracy: 0.90 MLC accuracy: 0.85

Fold 7

Predicted labels: [1, 2, 2, 2, 2, 1, 1, 2, 1, 1, 2, 2, 1, 1, 2, 1, 1]

Number of misclassified samples: 2

k-NN accuracy: 0.90 MLC accuracy: 0.65

Fold 8

Predicted labels: [1, 2, 2, 2, 2, 2, 2, 2, 2, 1, 2, 1, 1, 2, 1, 2, 1, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.95
MLC accuracy: 0.65

Fold 9

Predicted labels: [1, 2, 2, 1, 1, 2, 2, 2, 1, 1, 1, 1, 2, 1, 1, 2, 2, 2, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.70

Fold 10

Predicted labels: [2, 2, 2, 1, 1, 2, 2, 2, 1, 1, 1, 1, 1, 1, 1, 2, 1, 2, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.95 MLC accuracy: 0.65

k-NN average accuracy: 94.50 % MLC average accuracy: 67.00 %

k: [2, 3, 4, 5, 6, 7, 8, 9, 10]

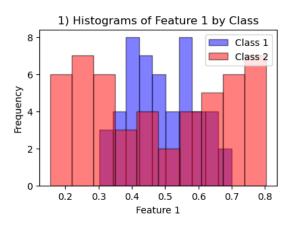
Average accuracy for k-NN classifier: [92.5 94.5 95.5 95.5 95. 96. 94. 93.5

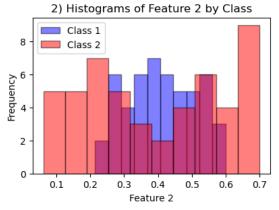
94.5] %

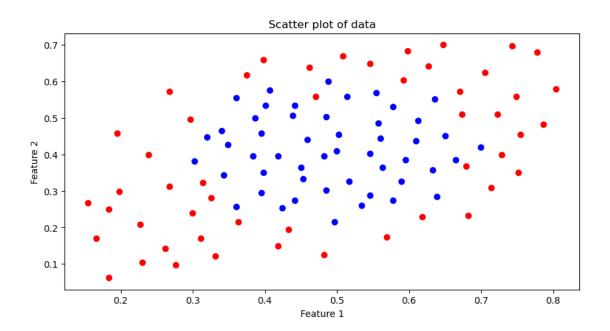
8 ELLIPSE dataset

```
[41]: file_path = "ellipse.pat"
      try:
          with open(file_path, "r") as file:
              content = file.read()
              data = content.split()
              # print(data)
      except FileNotFoundError:
          print("File not found!")
      data = np.array(data).reshape(-1, 5).T
      print(data.shape)
      f1 = data[1].astype(float)
      f2 = data[2].astype(float)
      class_labels = data[4].astype(int) + 1 # Convert class labels from O-indexed to_
       \hookrightarrow 1-indexed
      data_processed = np.array([f1, f2, class_labels]).T
     (5, 100)
[42]: # Separate data by class
      class1 data = [sample[:-1] for sample in data processed if sample[-1] == 1]
      class2_data = [sample[:-1] for sample in data_processed if sample[-1] == 2]
      # Features (replace these labels with your actual feature names)
      feature_labels = ['Feature 1', 'Feature 2']
      # Create a subplot of 2x2 graphs, each with a size of 10x10
      fig, axs = plt.subplots(1, 2, figsize=(10, 3))
      # Plot histograms for each feature
      for i in range(len(feature_labels)):
          ax = axs[i]
          ax.hist([x[i] for x in class1_data], bins=10, alpha=0.5, color='blue',
       ⇔label='Class 1', edgecolor='black')
          ax.hist([x[i] for x in class2 data], bins=10, alpha=0.5, color='red',
       →label='Class 2', edgecolor='black')
          ax.set_xlabel(feature_labels[i])
          ax.set ylabel('Frequency')
          ax.set_title(f'{i+1}) Histograms of {feature_labels[i]} by Class')
          ax.legend()
          # ax.grid(True)
      # plot scatter plot of data
      plt.figure(figsize=(10, 5))
      plt.title("Scatter plot of data")
```

```
plt.xlabel("Feature 1")
plt.ylabel("Feature 2")
plt.scatter(f1, f2, c=class_labels, cmap='bwr')
plt.show()
```







8.1 Results

 $[43]: \ \#\ cross_validation(np.array(data_processed),\ k=3,\ name='ELLIPSE',\ plot=True)$

[44]: # run cross validation from k = 2 to 10 # collect the average accuracy for each k k_list = [2, 3, 4, 5, 6, 7, 8, 9, 10]

```
avg_accuracy_knn_list = []
avg_accuracy_mlc_list = []
for k in k_list:
    avg_accuracy_knn, avg_accuracy_mlc = cross_validation(np.
  →array(data_processed), fold=10, k=k, name='ELLIPSE', plot=False)
    avg accuracy knn list.append(avg accuracy knn)
    avg_accuracy_mlc_list.append(avg_accuracy_mlc)
print(f'\nk: {k_list}')
print(f'Average accuracy for k-NN classifier: {100*np.
  →array(avg_accuracy_knn_list)} %')
print(f'Average accuracy for MLC classifier: {100*np.
  →mean(avg_accuracy_mlc_list)} %\n')
Performing 10-fold cross validation with k = 2
Fold 1
Predicted labels: [1, 1, 1, 2, 2, 2, 1, 1, 1, 2]
Number of misclassified samples: 1
k-NN accuracy: 0.90
MLC accuracy: 0.80
Fold 2
Predicted labels: [1, 2, 2, 2, 1, 1, 1, 1, 1, 1]
Number of misclassified samples: 3
k-NN accuracy: 0.70
MLC accuracy: 0.80
Fold 3
Predicted labels: [1, 1, 2, 2, 1, 1, 1, 1, 1, 2]
Number of misclassified samples: 2
k-NN accuracy: 0.80
MLC accuracy: 0.60
Fold 4
Predicted labels: [1, 2, 1, 1, 1, 2, 1, 1, 1]
Number of misclassified samples: 1
k-NN accuracy: 0.90
MLC accuracy: 0.90
Fold 5
Predicted labels: [1, 1, 1, 2, 1, 1, 2, 1, 1, 2]
Number of misclassified samples: 3
k-NN accuracy: 0.70
MLC accuracy: 0.90
Fold 6
```

Predicted labels: [1, 1, 2, 1, 1, 1, 1, 1, 1]

Number of misclassified samples: 5

k-NN accuracy: 0.50 MLC accuracy: 0.50

Fold 7

Predicted labels: [1, 1, 2, 1, 1, 1, 1, 2, 1, 2]

Number of misclassified samples: 4

k-NN accuracy: 0.60 MLC accuracy: 0.60

Fold 8

Predicted labels: [2, 2, 2, 1, 2, 2, 1, 1, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.90

Fold 9

Predicted labels: [1, 1, 1, 1, 2, 1, 2, 1, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.90

Fold 10

Predicted labels: [1, 2, 1, 2, 1, 2, 2, 1, 1, 1]

Number of misclassified samples: 2

k-NN accuracy: 0.80 MLC accuracy: 0.70

k-NN average accuracy: 77.00 % MLC average accuracy: 76.00 %

Performing 10-fold cross validation with k = 3

Fold 1

Predicted labels: [1, 1, 1, 1, 2, 2, 1, 1, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.70

Fold 2

Predicted labels: [2, 1, 1, 1, 2, 1, 2, 2, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.90

Fold 3

Predicted labels: [1, 1, 1, 2, 1, 2, 2, 1, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.90

Fold 4

Predicted labels: [1, 1, 2, 2, 1, 1, 2, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.60

Fold 5

Predicted labels: [2, 1, 1, 2, 1, 2, 1, 2, 1]

Number of misclassified samples: 3

k-NN accuracy: 0.70 MLC accuracy: 0.60

Fold 6

Predicted labels: [1, 2, 1, 2, 2, 2, 2, 2, 1, 1]

Number of misclassified samples: 2

k-NN accuracy: 0.80 MLC accuracy: 0.70

Fold 7

Predicted labels: [2, 2, 1, 1, 1, 1, 1, 1, 1]

Number of misclassified samples: 4

k-NN accuracy: 0.60 MLC accuracy: 0.50

Fold 8

Predicted labels: [1, 2, 2, 1, 1, 1, 2, 1, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.70

Fold 9

Predicted labels: [1, 1, 1, 1, 1, 2, 2, 2, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.80

Fold 10

Predicted labels: [1, 1, 2, 2, 2, 1, 2, 1, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.80

k-NN average accuracy: 86.00 % MLC average accuracy: 72.00 %

Performing 10-fold cross validation with k = 4

Predicted labels: [2, 2, 2, 1, 1, 1, 1, 2, 1, 2]

Number of misclassified samples: 2

k-NN accuracy: 0.80 MLC accuracy: 0.70

Fold 2

Predicted labels: [1, 2, 1, 1, 2, 2, 1, 1, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.90

Fold 3

Predicted labels: [1, 1, 2, 1, 1, 2, 1, 2, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.90

Fold 4

Predicted labels: [1, 2, 2, 1, 1, 1, 1, 1, 1, 2]

Number of misclassified samples: 3

k-NN accuracy: 0.70 MLC accuracy: 0.70

Fold 5

Predicted labels: [1, 1, 1, 1, 1, 1, 1, 2, 2, 1]

Number of misclassified samples: 4

k-NN accuracy: 0.60 MLC accuracy: 0.60

Fold 6

Predicted labels: [1, 1, 2, 1, 2, 1, 1, 2, 2, 1]

Number of misclassified samples: 2

k-NN accuracy: 0.80 MLC accuracy: 0.80

Fold 7

Predicted labels: [1, 1, 1, 1, 2, 2, 2, 1, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.90

Fold 8

Predicted labels: [1, 1, 1, 1, 1, 1, 1, 1, 1]

Number of misclassified samples: 4

k-NN accuracy: 0.60 MLC accuracy: 0.60

Predicted labels: [1, 2, 2, 1, 1, 1, 2, 2, 2, 1]

Number of misclassified samples: 2

k-NN accuracy: 0.80 MLC accuracy: 0.60

Fold 10

Predicted labels: [1, 2, 1, 1, 1, 1, 2, 1, 1, 1]

Number of misclassified samples: 2

k-NN accuracy: 0.80 MLC accuracy: 0.80

k-NN average accuracy: 79.00 % MLC average accuracy: 75.00 %

Performing 10-fold cross validation with k = 5

Fold 1

Predicted labels: [2, 1, 2, 1, 1, 2, 2, 2, 2, 1]

Number of misclassified samples: 2

k-NN accuracy: 0.80 MLC accuracy: 0.60

Fold 2

Predicted labels: [2, 1, 2, 1, 2, 1, 2, 1, 2]

Number of misclassified samples: 3

k-NN accuracy: 0.70 MLC accuracy: 0.70

Fold 3

Predicted labels: [2, 2, 1, 1, 2, 2, 2, 1, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.70

Fold 4

Predicted labels: [1, 2, 1, 2, 2, 1, 2, 1, 2, 2]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.80

Fold 5

Predicted labels: [1, 1, 2, 1, 2, 2, 1, 1, 2, 2]

Number of misclassified samples: 2

k-NN accuracy: 0.80 MLC accuracy: 0.70

Fold 6

Number of misclassified samples: 0 k-NN accuracy: 1.00

Predicted labels: [1, 1, 2, 1, 1, 2, 1, 1, 1, 2]

MLC accuracy: 0.80

Fold 7

Predicted labels: [2, 1, 1, 2, 1, 1, 1, 2, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.90

Fold 8

Predicted labels: [2, 2, 1, 2, 1, 2, 1, 2, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.80

Fold 9

Predicted labels: [2, 1, 1, 1, 2, 1, 1, 2, 1, 1]

Number of misclassified samples: 3

k-NN accuracy: 0.70 MLC accuracy: 0.60

Fold 10

Predicted labels: [2, 1, 2, 1, 1, 2, 1, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.80

k-NN average accuracy: 89.00 % MLC average accuracy: 74.00 %

Performing 10-fold cross validation with k = 6

Fold 1

Predicted labels: [1, 1, 2, 1, 1, 2, 2, 1, 1, 1]

Number of misclassified samples: 3

k-NN accuracy: 0.70 MLC accuracy: 0.50

Fold 2

Predicted labels: [2, 1, 1, 1, 1, 1, 1, 1, 1]

Number of misclassified samples: 3

k-NN accuracy: 0.70 MLC accuracy: 0.70

Fold 3

Predicted labels: [1, 1, 1, 2, 1, 2, 1, 2, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.70

Fold 4

Predicted labels: [2, 1, 2, 2, 2, 1, 1, 1, 1, 1]

Number of misclassified samples: 4

k-NN accuracy: 0.60 MLC accuracy: 0.60

Fold 5

Predicted labels: [2, 1, 1, 2, 1, 2, 1, 2, 1]

Number of misclassified samples: 2

k-NN accuracy: 0.80 MLC accuracy: 0.60

Fold 6

Predicted labels: [2, 1, 1, 1, 2, 1, 1, 2, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.90

Fold 7

Predicted labels: [2, 1, 1, 1, 1, 1, 2, 1, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 1.00

Fold 8

Predicted labels: [1, 2, 2, 2, 1, 1, 2, 1, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.90

Fold 9

Predicted labels: [1, 1, 2, 2, 1, 1, 1, 1, 2, 1]

Number of misclassified samples: 3

k-NN accuracy: 0.70 MLC accuracy: 0.70

Fold 10

Predicted labels: [2, 1, 1, 2, 1, 2, 1, 2, 1]

Number of misclassified samples: 2

k-NN accuracy: 0.80 MLC accuracy: 0.90

k-NN average accuracy: 80.00 % MLC average accuracy: 75.00 %

Performing 10-fold cross validation with k = 7

Predicted labels: [1, 1, 1, 1, 2, 2, 2, 2, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.60

Fold 2

Predicted labels: [2, 1, 1, 1, 1, 1, 2, 2, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.80

Fold 3

Predicted labels: [2, 2, 2, 1, 1, 1, 2, 2, 1, 2]

Number of misclassified samples: 2

k-NN accuracy: 0.80 MLC accuracy: 0.90

Fold 4

Predicted labels: [1, 2, 2, 1, 2, 2, 1, 1, 1, 1]

Number of misclassified samples: 5

k-NN accuracy: 0.50 MLC accuracy: 0.60

Fold 5

Predicted labels: [1, 1, 1, 2, 2, 2, 1, 1, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.90

Fold 6

Predicted labels: [1, 1, 2, 1, 1, 2, 2, 1, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.70

Fold 7

Predicted labels: [1, 1, 2, 2, 1, 2, 1, 1, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.80

Fold 8

Predicted labels: [2, 1, 1, 2, 2, 1, 1, 2, 1, 2]

Number of misclassified samples: 2

k-NN accuracy: 0.80 MLC accuracy: 0.70

Predicted labels: [2, 1, 1, 1, 1, 1, 1, 2, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.80

Fold 10

Predicted labels: [2, 2, 1, 1, 2, 1, 2, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.80

k-NN average accuracy: 85.00 % MLC average accuracy: 76.00 %

Performing 10-fold cross validation with k = 8

Fold 1

Predicted labels: [2, 2, 1, 1, 1, 1, 1, 1, 1]

Number of misclassified samples: 2

k-NN accuracy: 0.80 MLC accuracy: 0.70

Fold 2

Predicted labels: [1, 2, 1, 1, 2, 1, 1, 1, 1]

Number of misclassified samples: 3

k-NN accuracy: 0.70 MLC accuracy: 0.60

Fold 3

Predicted labels: [1, 1, 2, 1, 1, 2, 1, 1, 1]

Number of misclassified samples: 4

k-NN accuracy: 0.60 MLC accuracy: 0.60

Fold 4

Predicted labels: [1, 1, 1, 1, 2, 2, 1, 2, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.70

Fold 5

Predicted labels: [2, 1, 1, 1, 1, 1, 2, 1, 1]

Number of misclassified samples: 3

k-NN accuracy: 0.70 MLC accuracy: 0.70

Fold 6

Predicted labels: [1, 1, 2, 1, 2, 1, 1, 2, 1, 1]
Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.90

Fold 7

Predicted labels: [1, 2, 2, 1, 1, 2, 2, 2, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.90

Fold 8

Predicted labels: [1, 1, 1, 1, 1, 2, 2, 2, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.90

Fold 9

Predicted labels: [1, 2, 1, 1, 1, 1, 1, 2, 1, 2]

Number of misclassified samples: 3

k-NN accuracy: 0.70 MLC accuracy: 0.60

Fold 10

Predicted labels: [1, 2, 1, 2, 2, 2, 1, 1, 1, 1]

Number of misclassified samples: 2

k-NN accuracy: 0.80 MLC accuracy: 0.90

k-NN average accuracy: 80.00 % MLC average accuracy: 75.00 %

Performing 10-fold cross validation with k = 9

Fold 1

Predicted labels: [2, 1, 1, 2, 1, 2, 1, 1, 1, 2]

Number of misclassified samples: 3

k-NN accuracy: 0.70 MLC accuracy: 0.80

Fold 2

Predicted labels: [2, 1, 1, 2, 1, 1, 1, 1, 1]

Number of misclassified samples: 2

k-NN accuracy: 0.80 MLC accuracy: 0.80

Fold 3

Predicted labels: [1, 1, 1, 1, 1, 2, 1, 2, 1, 1]

Number of misclassified samples: 3

k-NN accuracy: 0.70 MLC accuracy: 0.60

Fold 4

Predicted labels: [2, 2, 2, 2, 1, 1, 2, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.60

Fold 5

Predicted labels: [1, 1, 1, 1, 1, 2, 1, 1, 2, 2]

Number of misclassified samples: 3

k-NN accuracy: 0.70 MLC accuracy: 0.60

Fold 6

Predicted labels: [1, 1, 2, 1, 2, 2, 1, 2, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.90

Fold 7

Predicted labels: [2, 2, 2, 1, 1, 2, 1, 1, 2, 1]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 0.90

Fold 8

Predicted labels: [1, 2, 2, 2, 2, 1, 1, 1, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.80

Fold 9

Predicted labels: [2, 2, 1, 1, 1, 1, 2, 1, 1, 1]

Number of misclassified samples: 3

k-NN accuracy: 0.70 MLC accuracy: 0.70

Fold 10

Predicted labels: [1, 1, 2, 2, 1, 1, 2, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.70

k-NN average accuracy: 83.00 % MLC average accuracy: 74.00 %

Performing 10-fold cross validation with k = 10

Predicted labels: [2, 1, 1, 2, 1, 1, 2, 2, 1, 1]

Number of misclassified samples: 3

k-NN accuracy: 0.70 MLC accuracy: 0.70

Fold 2

Predicted labels: [1, 2, 1, 1, 1, 2, 1, 1, 1]

Number of misclassified samples: 5

k-NN accuracy: 0.50 MLC accuracy: 0.60

Fold 3

Predicted labels: [2, 1, 1, 2, 1, 1, 2, 1, 1]

Number of misclassified samples: 2

k-NN accuracy: 0.80 MLC accuracy: 0.70

Fold 4

Predicted labels: [2, 1, 1, 1, 1, 2, 2, 1, 1, 2]

Number of misclassified samples: 0

k-NN accuracy: 1.00
MLC accuracy: 1.00

Fold 5

Predicted labels: [2, 2, 1, 1, 1, 1, 2, 1, 1, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.60

Fold 6

Predicted labels: [1, 1, 2, 1, 1, 2, 1, 2, 1, 1]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.80

Fold 7

Predicted labels: [2, 1, 1, 2, 1, 1, 1, 1, 1]

Number of misclassified samples: 4

k-NN accuracy: 0.60 MLC accuracy: 0.60

Fold 8

Predicted labels: [1, 1, 1, 1, 1, 1, 2, 2, 2, 1]

Number of misclassified samples: 4

k-NN accuracy: 0.60 MLC accuracy: 0.60

Predicted labels: [1, 1, 2, 2, 1, 2, 1, 2, 1, 1]

Number of misclassified samples: 0

k-NN accuracy: 1.00 MLC accuracy: 1.00

Fold 10

Predicted labels: [1, 1, 1, 1, 1, 2, 2, 1, 2, 2]

Number of misclassified samples: 1

k-NN accuracy: 0.90 MLC accuracy: 0.90

k-NN average accuracy: 79.00 % MLC average accuracy: 75.00 %

k: [2, 3, 4, 5, 6, 7, 8, 9, 10]

Average accuracy for k-NN classifier: [77. 86. 79. 89. 80. 85. 80. 83. 79.] %

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