

For instructions on how to checkout the template code for the assignment and submit solutions using git, see <http://dna.engr.uconn.edu/moodle/mod/page/view.php?id=129>

### Exercise 1. Polynomial evaluation (70 points)

(a) Write a recursive function `double power( double x, int n )` based on the following identity:

$$x^n = \begin{cases} x^{\lfloor n/2 \rfloor} \times x^{\lfloor n/2 \rfloor} & \text{if } n \text{ is even} \\ x \times x^{\lfloor n/2 \rfloor} \times x^{\lfloor n/2 \rfloor} & \text{if } n \text{ is odd} \end{cases}$$

Make sure to use an appropriate base case to avoid infinite recursion!

(b) A univariate polynomial

$$a_0 + a_1x^1 + a_2x^2 \dots + a_{n-1}x^{n-1} + a_nx^n$$

is a mathematical expression involving the sum of powers of a variable  $x$  multiplied by constant coefficients. Each term in the above sum is called a monomial,  $a_i$ ,  $i = 0, \dots, n$  are called the coefficients of the polynomial, and  $n$ , the largest power  $n$  with non-zero coefficient, is called the degree.

A simple representation of a polynomial uses an array for storing the coefficients. Complete the provided code by implementing a function that returns the value of a given polynomial for a given value of  $x$ . Write two versions of the function. The first version should use the power function from part (a). The second version should implement **Horner's rule**, which reduces the number of necessary multiplications by factoring out powers of  $x$  as follows:

$$a_0 + x(a_1 + x(a_2 + x(\dots x(a_{n-1} + xa_n)\dots)))$$

The main function in the provided template reads from the standard input a double  $x$ , a non-negative degree  $n$ , and the  $n + 1$  integer coefficients of a polynomial, then prints the values computed by each of the two versions of your evaluation function.

### Exercise 2. Super-permutations (30 points)

A permutation of the integers from 1 to  $n$  is an ordering of these integers. A natural way to represent a permutation is to list the integers in the desired order. For example, for  $n = 5$ , a permutation might look like 2, 3, 4, 5, 1. However, there is alternative way of representing a permutation: you create a list of  $n$  numbers where the  $i$ -th number is the position of integer  $i$  in the permutation. For the above permutation this alternative representation is 5, 1, 2, 3, 4 since 1 appears on position 5, 2 appears on position 1, and so on (note that in math position numbering starts from 1). A super-permutation is a permutation for which the two representations are identical. For example, 1, 4, 3, 2 is a super-permutation. You have to write a program which detects if a given permutation is a super-permutation or not.

Input: The program should read from the standard input one or more test cases. The first line of each test case contains an integer  $n$  ( $1 \leq n \leq 100,000$ ). Then a permutation of the integers 1 to  $n$  follows on the next line. There is exactly one space character between consecutive integers. You may assume that every integer between 1 and  $n$  appears exactly once in the permutation. The last test case is followed by a zero.

Output: For each test case print to the standard output one line with the answer formatted as in the sample below.

Sample Input:

```
4
1 4 3 2
5
2 3 4 5 1
1
1
0
```

Sample Output:

```
super
not super
super
```