Towards Formal Verification of Neuro-symbolic Multi-agent Systems

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Abstract

This paper outlines some of the key methods we developed towards the formal verification of multiagent systems, covering both symbolic and connectionist systems. It discusses logic-based methods for the verification of unbounded multi-agent systems (i.e., systems composed of an arbitrary number of homogeneous agents, e.g., robot swarms), optimisation approaches for establishing the robustness of neural network models, and methods for analysing properties of neuro-symbolic multiagent systems.

1 Introduction

Recent advances in Artificial Intelligence (AI) have enabled the automation of challenging tasks, such as computer vision, that have been traditionally difficult to tackle using classical approaches. This accelerated the trend of incorporating AI components in diverse applications with high societal impact, such as healthcare and transportation.

Still, even though there is an increasing consensus in AI being beneficial for society, its inherent fragility and opacity hinders its adoption in safety-critical applications. The associated risks are compounded in an increasingly interconnected, socio-techno-economic world, where systems of multiple interacting intelligent agents, or multi-agent systems (MAS), constitute a paradigm shift from object-oriented to interaction-oriented design standards.

In response to these concerns the area of formal verification of AI has grown rapidly over the past few years to provide methods to automatically verify that AI systems robustly behave as intended.

One of the key techniques that has emerged in the area is that of model checking [Clarke et al., 1999]. Model checking provides automated solutions to the problem of estabilishing whether a model M_S representing a system S satisfies a logical formula ϕ_P encoding a specification P. In the case of MAS, the formula φ does not simply express temporal properties of systems, as in reactive systems, but it may also be accounting for high-level attitudes of agency, such as knowledge and strategies, which can be described in temporal-epistemic logic [Fagin et al., 1995a] and alternating-time logic [Alur et al., 1998].

Whilst a number of methods, such as binary binary decision diagrams [Gammie and van der Meyden, 2004] and bounded model checking [Penczek and Lomuscio, 2003], enabled the model checking of complex systems of large state spaces, a main drawback of the approach remains the *state-space explosion problem*. Succinctly put, whereas model checking whether M_S satisfies ϕ can be solved in polynomial time [Clarke *et al.*, 1999], the size of the model M_S to analyse is exponential in the number of variables encoding the agents in the system S.

Notwithstanding that in practice this limits model checking to the verification of systems with only few constituents, the analysis of systems with arbitrarily many participants, such as robot swarms and applications in the Internet of Things, raises a principal barrier to the application of model checking. Indeed, verifying systems of this kind, henceforth *unbounded multi-agent systems* (UMAS), requires checking whether any system for any number of agents satisfies the specification in question. This renders model checking intractable when enumerating and analysing all individual systems.

Another key limitation of model checking is the requirement that the systems are given in traditional and agent-based programming languages, thereby not accounting for the recent shift to synthesise parts of the agents from data and implement via neural networks. Systems of this kind, henceforth *neuro-symbolic multi-agent systems* (NMAS), constitute important forthcoming applications, such as autonomous vehicles and personal negotiation assistants, where the neural components are employed to perform complex tasks, such as computer vision and natural language processing.

While the efficacy of neural networks with respect to these tasks has significantly improved over the past few years, their fragility to adversarial attacks [Szegedy et al., 2014] and lack of interpretability [Doshi-Velez and Kim, 2017] raise additional concerns regarding the overall system safety, thereby strengthening the need for their principled analysis before deployment.

This paper gives an overview of the methods that we developed within the Verification of Automous Systems research group ¹ towards the formal verification of UMAS and NMAS. Our pioneering work in the verification of UMAS, discussed in Section 2, overcomes the model checking barrier with the

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development of methods that enable the derivation of the number of agents that is sufficient to consider when evaluating a specification. Our studies in the analysis of NMAS, outlined in Section 3, include efficient methods for the verification of neural networks and mixed integer programming formulations for checking system-level specifications. The paper concludes in Section 4 with directions for future work.

2 Unbounded Multi-agent Systems

Interpreted systems are a standard semantics for describing multi-agent systems [Fagin *et al.*, 1995b]. They provide a natural setup to interpret specifications in a variety of languages including temporal-epistemic logic and alternating temporal logic [Fagin *et al.*, 1995a; Lomuscio and Raimondi, 2006]. Parameterised Interpreted Systems (PIS) is a parametric extension to interpreted systems that we put forward to reason about the temporal-epistemic properties of UMAS in both synchronous [Kouvaros and Lomuscio, 2015b] and asynchronous [Kouvaros and Lomuscio, 2016c] settings. The parameter in PIS denotes the number of agents in the system, each homogeneously constructed from an agent template.

The verification problem for PIS (generally known as the *parameterised verification problem* in the reactive systems' literature [Bloem *et al.*, 2015]) is to check whether any system for any value of the parameter satisfies a given specification. This is in general undecidable [Kouvaros and Lomuscio, 2016c]. Solutions to the problem can thus be given only in the form of incomplete techniques. Alternatively, decidable fragments can be curved by imposing restrictions on the systems and/or the specifications.

In either case, a key concept that enables the verification of UMAS is that of a *cutoff*. A cutoff is a natural number that expresses the number of agents that is sufficient to consider when evaluating a given specification. In other words, if a cutoff can be computed, then the verification problem can be solved by checking all systems whose number of agents is below the cutoff value.

Whilst we've shown that cutoffs do not always exist [Kouvaros and Lomuscio, 2013b], strong empirical evidence supports their existence for real-world systems [Emerson and Kahlon, 2000; Emerson and Namjoshi, 1995; Aminof *et al.*, 2014]. Moreover, for the cases where they do not exist, theoretical analyses that we conducted show that these often concern systems that can exhibit *impractical* cyclic behaviours whose number of repetitions depends on the exact number of agents in the system [Kouvaros and Lomuscio, 2013b].

Following these observations we have analysed various sufficient conditions for the identification of cutoffs. The conditions were drawn with respect to different synchronisation primitives endowing the agents. In the fully synchronous setting, we have shown that cutoffs can always be identified and gave a procedure for their computation [Kouvaros and Lomuscio, 2015b]. In the asynchronous case, where agents communicate via broadcast actions, we have similarly given a sound and complete technique for their derivation [Kouvaros and Lomuscio, 2013a]. When the agents can additionally participate in pairwise communication with their environment, we have shown that if

(i) the environment can never block pairwise synchronisations for the system of one agent only, and (ii) each synchronisation can happen in unique configurations for the environment,

then cutoffs can be computed in an efficient procedure that runs in linear time in the size of the agent template [Kouvaros and Lomuscio, 2013b]. The second restriction can be lifted in a cutoff procedure that runs in exponential time [Kouvaros and Lomuscio, 2015a].

While these results were drawn with respect to homogeneous UMAS, where every agent is instantiated from a unique agent template, we have also provided extensions that account for heterogeneous UMAS, where agents can assume different roles and responsibilities, e.g., heterogeneous robot swarms [Kouvaros and Lomuscio, 2016c]. The heterogeneous semantics that we introduced allow for broadcast actions that may either concern all agents of all agent templates or all agents following a certain template. They additionally enable pairwise interactions between agents of different roles, thereby surpassing the expressive power of the homogeneous model.

Further gains in the expressivity of the protocols that can be verified have been obtained from our studies on UMAS programmed using variables with infinite domains [Kouvaros and Lomuscio, 2017a]. The resulting verification method combines predicate abstraction [Lomuscio and Michaliszyn, 2015] with parameterised verification, the former addressing the unboundedness of the state-space of the agents and the latter tackling the unboundedness of their number.

We have released the open-source parameterised verification toolkit MCMAS-P implementing the cutoff procedures for UMAS. MCMAS-P enabled for the first time the verification of aggregation and foraging algorithms for robot swarms irrespective of the number of robots composing the swarm [Kouvaros and Lomuscio, 2015b; Kouvaros and Lomuscio, 2016c].

Further applications included the analysis of the security of an unbounded number of concurrent sessions of cryptographic protocols, for which we provided a mapping from a Dolev-Yao threat model to PIS [Boureanu *et al.*, 2016]. Others concerned the verification of UMAS comprising *dataaware agents*, i.e., agents that are endowed with possibly infinite domains and that interact with an environment composed of (semi)-structured data [Montali *et al.*, 2014]. Having used simulation-based abstractions to deal with the infinity of the agents, we have then presented a translation to PIS to solve their verification problem [Belardinelli *et al.*, 2017]. Analogous translations to PIS were given for *open MAS*, where countably many agents can join and leave the system at runtime [Kouvaros *et al.*, 2019].

Finally, adaptations of the verification methods for PIS enabled us to derive techniques for the verification of opinion formation protocols in swarms, which we used to give formal guarantees on the outcome of consensus protocols [Kouvaros and Lomuscio, 2016a]. Still others facilitated the verification of strategic properties of UMAS expressed in a parameterised variant of Alternating-time temporal logic that we introduced [Kouvaros and Lomuscio, 2016b].

I conclude this section by noting that complementary to protocol correctness, which the aforementioned methods can formally ascertain, the evaluation of protocols also requires analyses of the extent to which they are are resilient to adverse functioning behaviours for some of the agents in the system. For instance, when evaluating a robot swarm searchand-rescue scenario, it is not sufficient to establish that the swarm will collectively cover the search area, but it is also crucial to determine that local faults, e..g, hardware malfunctions, will be tolerated by the swarm, instead of being propagated through agent interactions thereby dis-coordinating the search. To address this concern we have put forward an automated procedure to establish the robustness of UMAS against a given ratio of faulty to non-faulty agents in the system [Kouvaros and Lomuscio, 2017b], which we followed by a symbolic method to automatically synthesise the maximum ratio of faulty to non-faulty agents a UMAS can tolerate [Kouvaros et al., 2018].

3 Neuro-symbolic Multi-agent Systems

To reason about the properties of NMAS, we have introduced *neural interpreted systems* (NIS), a novel formalisation of MAS based on interpreted systems. In a nutshell, an agent in NIS comprises a perception mechanism implement via neural networks and coupled with a symbolic action mechanism.

The neural network components, which endow the agents with infinite domains, pose significant challenges to the verification problem. In particular, differently from traditional verification for symbolic systems, where atomic formulae are evaluated in constant time at symbolic states of the system, the evaluation of atomic formulae in NIS includes the computation of the output regions of the neural networks for a (potentially infinite) set of inputs, which is an NP-complete problem [Katz et al., 2017]. Increasingly sophisticated solutions to the problem have been put forward in the past few years offering a principled way of analysing the robustness of neural networks to adversarial attacks [Singh et al., 2019; Kouvaros and Lomuscio, 2021; Wang et al., 2021]

We first discuss our work on the verification of standalone neural networks which forms the backbone of our studies on the analysis of NMAS outlined later.

3.1 Neural network verification

The neural network verification problem is to determine whether the output of a neural network is as expected for a potentially infinite set of inputs. Perhaps the most common instantiation of the problem is the adversarial robustness check for computer vision models, whereby the set of inputs denotes imperceptible perturbations to a given image and the set of outputs encodes classification equivalence for all perturbations. While significant progress has been made in pushdown engines to solve the problem [Brix et al., 2023], scalability to industrial-size models found in complex tasks such as computer vision remains a key difficulty in the area.

Advances in the area are driven by *complete* and *incomplete* methods. Complete methods can in principle return a definite answer as to the whether the verification problem is satisfied, whereas incomplete methods may be unable to

decide one way or the other. Complete methods are based on exact MILP/SMT formulations SMT encodings or dedicated branch-and-bound procedures tackling the optimisation mappings of the problem. Incomplete methods typically rely on linear/semi-definite relaxations of of the problem, which improves their scalability over complete methods, but potentially hinders their efficacy to solve the problem because of the induced over-approximations.

Our efforts in the area included methods towards improving scalability in complete verification and techniques in the direction of strengthening precision in incomplete verification. In complete verification, we have introduced the novel concept of *ReLU dependency* whereby ReLU nodes are in a dependency relation if their operational states for a set of inputs is connected by logical implication. We have devised methods for the computation of the dependency relations, which we have translated into MILP cuts, thereby improving the efficacy of MILP formulations of the verification problem [Botoeva *et al.*, 2020]. Further improvements have been possible via the derivation of dependency-based branching heuristics in a branch-and-bound procedure [Kouvaros and Lomuscio, 2021].

In incomplete verification, we have devised an abstraction method that strengthens the linear relaxations of ReLU nodes by additionally accounting for intra-layer dependencies, instead of simply the local over-approximation areas, when choosing a relaxation [Hashemi *et al.*, 2021]. This enabled proofs of adversarial robustness to be given to computer vision models that could not be previously resolved. To a similar effect we have strengthen semidefinite approximations of the verification problem considering layer-wise relaxations and incorporating linear cuts into the semidefinite formulation.

We have released the open-source neural network verification toolkit VENUS implementing the aforementioned methods. In the span of four years, VENUS has progressed from analysing networks of few thousands of nodes to examining networks of millions of nodes. Among the latter are neural network-based systems in the aircraft domain developed by Boeing, including object detection and landing assistance systems [Kouvaros *et al.*, 2021], and semantic segmentation models for pose estimation [Kouvaros *et al.*, 2023].

3.2 NMAS verification

The scalability hurdle is even more prevalent in the formal analysis of closed-loop systems with neural components such as NMAS. In fact, we've shown their verification problem to be undecidable for plain reachability properties [Akintunde *et al.*, 2022]. In the light of this we've isolated bounded fragments of CTL and ATL, whereby formulae can be evaluated in a bounded number of execution steps, thus allowing for expressing properties concerning, for instance, whether the agents can bring about a state of affairs or reach a safe configuration within a bounded number of steps. We have shown that verification with respect to this fragment is in coNEXPTIME and solved the resulting verification problem via a mixed-integer linear programming (MILP) formulations. that encapsulate the neural network verification procedures described earlier for tight encodings of the net-

works [Akintunde et al., 2020a; Akintunde et al., 2020b]. To 313 further alleviate the difficulty of the verification problem, we 314 also introduce a novel algorithm that checks for the occur-315 rence of bugs in parallel over the execution paths. As we 316 show, in the case of bounded safety specifications, this enables us to return a bug to the user as soon as a violation is 318 identified on any of the branching paths that are explored in 319 parallel. 320

4 Conclusions and Future Work

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