

$$\langle K|O_1|K \rangle = (\sum_{m=1}^{\frac{N}{2}=N_\alpha} [m|h|m] + \sum_{m=1}^{\frac{N}{2}=N_\beta} [m|h|m]) = \sum_{m=1}^N [m|h|m]$$