

You did this denervation previously, so I'm just doing it again to try things out.

$$\begin{aligned}
& \text{one e- int for no differences be twin determinants} \\
& \langle \Psi | H_0 | \Psi \rangle = h^{\alpha\beta} \langle vac | (\prod_{\kappa} a_{\kappa}) a_{\alpha}^{\dagger} a_{\beta} \prod_{\kappa'} a_{\kappa'}^{\dagger} | vac \rangle \\
& = h^{\alpha\beta} \langle vac | (\prod_{\kappa} a_{\kappa}) a_{\alpha}^{\dagger} \delta_{\beta\kappa_1} \prod_{\kappa'=\{\kappa_2 \dots \kappa_n\}} a_{\kappa'}^{\dagger} | vac \rangle \\
& - h^{\alpha\beta} \langle vac | \prod_{\kappa} a_{\kappa} a_{\alpha}^{\dagger} a_{\kappa_1}^{\dagger} a_{\beta} \prod_{\kappa'=\{\kappa_2 \dots \kappa_n\}} a_{\kappa'}^{\dagger} | vac \rangle \\
& = h^{\alpha\beta} \langle vac | (\prod_{\kappa} a_{\kappa}) a_{\alpha}^{\dagger} \delta_{\beta\kappa_1} \prod_{\kappa'=\{\kappa_2 \dots \kappa_n\}} a_{\kappa'}^{\dagger} | vac \rangle \\
& + h^{\alpha\beta} \langle vac | \prod_{\kappa=\{\kappa_n \dots \kappa_1\}} a_{\kappa} a_{\kappa_1}^{\dagger} a_{\alpha}^{\dagger} a_{\beta} \prod_{\kappa'=\{\kappa_2 \dots \kappa_n\}} a_{\kappa'}^{\dagger} | vac \rangle \\
& = h^{\alpha\beta} \langle vac | (\prod_{\kappa} a_{\kappa}) a_{\alpha}^{\dagger} \delta_{\beta\kappa_1} \prod_{\kappa'=\{\kappa_2 \dots \kappa_n\}} a_{\kappa'}^{\dagger} | vac \rangle \\
& + h^{\alpha\beta} \langle vac | \prod_{\kappa=\{\kappa_n \dots \kappa_2\}} a_{\kappa} a_{\alpha}^{\dagger} a_{\beta} \prod_{\kappa'=\{\kappa_2 \dots \kappa_n\}} a_{\kappa'}^{\dagger} | vac \rangle \\
& = h^{\alpha\beta} \delta_{\alpha\kappa_1} \delta_{\beta\kappa_1} + h^{\alpha\beta} \langle vac | (\prod_{\kappa=\{\kappa_n \dots \kappa_2\}} a_{\kappa}) a_{\alpha}^{\dagger} a_{\beta} \prod_{\kappa'=\{\kappa_2 \dots \kappa_n\}} a_{\kappa'}^{\dagger} | vac \rangle \\
& = \dots \\
& = \sum_{\kappa} h^{\alpha\beta} \delta_{\alpha\kappa} \delta_{\beta\kappa} \\
& = \sum_{\kappa} h^{\kappa\kappa} \\
& = \sum_{\kappa} h^{(\kappa)(\kappa)} \delta_{[\kappa],[\kappa]} \\
& = \sum_{\kappa} h^{(\kappa)(\kappa)}
\end{aligned}$$

to e- int for no defences between two determinants

$$\begin{aligned}
& \langle \Psi | V | \Psi \rangle = v^{\alpha\beta\gamma\delta} \langle vac | (\prod_{\kappa} a_{\kappa}) a_{\alpha}^{\dagger} a_{\beta}^{\dagger} a_{\gamma} a_{\delta} \prod_{\kappa'} a_{\kappa'}^{\dagger} | vac \rangle \\
& = v^{\alpha\beta\gamma\delta} \langle vac | (\prod_{\kappa} a_{\kappa}) a_{\alpha}^{\dagger} a_{\beta}^{\dagger} a_{\gamma} \delta_{\delta\kappa_1} \prod_{\kappa'=\{\kappa_2 \dots \kappa_n\}} a_{\kappa'}^{\dagger} | vac \rangle \\
& - v^{\alpha\beta\gamma\delta} \langle vac | (\prod_{\kappa} a_{\kappa}) a_{\alpha}^{\dagger} a_{\beta}^{\dagger} a_{\gamma} a_{\kappa_1}^{\dagger} a_{\delta} \prod_{\kappa'=\{\kappa_2 \dots \kappa_n\}} a_{\kappa'}^{\dagger} | vac \rangle \\
& = v^{\alpha\beta\gamma\delta} \delta_{\delta\kappa_1} \langle vac | (\prod_{\kappa} a_{\kappa}) a_{\alpha}^{\dagger} a_{\beta}^{\dagger} a_{\gamma} \prod_{\kappa'=\{\kappa_2 \dots \kappa_n\}} a_{\kappa'}^{\dagger} | vac \rangle \\
& - (1) \\
& = v^{\alpha\beta\gamma\delta} \delta_{\delta\kappa_1} \delta_{\gamma\kappa_2} \langle vac | (\prod_{\kappa} a_{\kappa}) a_{\alpha}^{\dagger} a_{\beta}^{\dagger} \prod_{\kappa'=\{\kappa_3 \dots \kappa_n\}} a_{\kappa'}^{\dagger} | vac \rangle \\
& - v^{\alpha\beta\gamma\delta} \delta_{\delta\kappa_1} \langle vac | (\prod_{\kappa} a_{\kappa}) a_{\alpha}^{\dagger} a_{\beta}^{\dagger} a_{\kappa_2}^{\dagger} a_{\gamma} \prod_{\kappa'=\{\kappa_3 \dots \kappa_n\}} a_{\kappa'}^{\dagger} | vac \rangle - (1)
\end{aligned}$$

$$\begin{aligned}
& = \sum_{\kappa_1 \kappa_2} v^{\alpha\beta\gamma\delta} \delta_{\delta\kappa_1} \delta_{\gamma\kappa_2} \delta_{\beta\kappa_2} \delta_{\alpha\kappa_1} - v^{\alpha\beta\gamma\delta} \delta_{\delta\kappa_1} \langle vac | (\prod_{\kappa=\{\kappa_n \dots \kappa_2\}} a_{\kappa}) a_{\kappa_1}^{\dagger} a_{\kappa_2}^{\dagger} a_{\alpha}^{\dagger} a_{\beta}^{\dagger} a_{\gamma} \prod_{\kappa'=\{\kappa_3 \dots \kappa_n\}} a_{\kappa'}^{\dagger} | vac \rangle \\
& = \sum_{\kappa_1 \kappa_2} v^{\kappa_1 \kappa_2 \kappa_2 \kappa_1} - v^{\alpha\beta\gamma\delta} \delta_{\delta\kappa_1} \delta_{\kappa_1 \kappa_2} \langle vac | (\prod_{\kappa=\{\kappa_n \dots \kappa_2\}} a_{\kappa}) a_{\alpha}^{\dagger} a_{\beta}^{\dagger} a_{\gamma} \prod_{\kappa'=\{\kappa_3 \dots \kappa_n\}} a_{\kappa'}^{\dagger} | vac \rangle \\
& + v^{\alpha\beta\gamma\delta} \delta_{\delta\kappa_1} \langle vac | (\prod_{\kappa=\{\kappa_n \dots \kappa_3\}} a_{\kappa}) a_{\alpha}^{\dagger} a_{\beta}^{\dagger} a_{\gamma} \prod_{\kappa'=\{\kappa_3 \dots \kappa_n\}} a_{\kappa'}^{\dagger} | vac \rangle \\
& = \sum_{\kappa_1 \kappa_2} v^{(\kappa_1)(\kappa_2)(\kappa_2)(\kappa_1)} \delta_{[\kappa_1],[\kappa_2]} + \dots
\end{aligned}$$

Mainly I'm worried that I'm getting so many terms in my derivation, but maybe this aspect is normal?

In general I want to know if I'm making things too hard for myself or if I'm full doing the right process that could you comment on this?

I'm having trouble getting the 2 e- int to a form that I can access. Am I doing this correctly on the right here?