

Microteaching: Understanding Quantum Absorption

Energy Levels in Hydrogen Atoms

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Check: Does everyone get the same result?

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Question: Why must the final value n_f be rounded to an integer?

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