

# Slides for Patryk's Notes

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# Outline

1. Why UEG MP2 poles are bad
2. Implementation of QP MP2
3. Comparison to evGW

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So MP2 self-energy is only reliable if the  $\chi_0(\omega)$  is small, and thus the MP2 pole at  $r_s = 4$  is bad. When we do this large scale study of molecular IP/EAs, we should find a way to quantify the  $\chi_0(\omega)$ , so we can see if this trend gets reproduced.

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# Algorithm for QP MP2

Likely, we want to do:

- ① Start with HF reference orbitals and energies.
- ② Solve QP equation for each orbital using MP2 self-energy of 2.
- ③ Update *some* orbital energies in 2, keeping the numerator fixed.
- ④ Repeat steps 2-3 until convergence in the orbital energies *of interest*.

$$\Sigma_{pp}^{(2)}(\omega) = \sum_{iab} \frac{(pa|ib)\left(2(qa|ib) - (qb|ia)\right)}{\omega - \epsilon_a - \epsilon_b + \epsilon_i + i\eta} + \sum_{ija} \frac{(pi|aj)\left(2(qi|aj) - (qj|ai)\right)}{\omega - \epsilon_i - \epsilon_j + \epsilon_a + i\eta} \quad (2)$$

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When solving the QP equation, we can linearize, so do

$$\epsilon_p^i = \epsilon_p^{i-1} + Z_p \Sigma_{pp}^c (\omega = \epsilon_p^{i-1}) \quad (3)$$

where  $\epsilon_p^i \equiv \epsilon_p^{HF}$  at  $i = 0$  and

$$Z_p = \left[ 1 - \frac{\partial \Sigma_{pp}^c(\omega)}{\partial \omega} \Bigg|_{\omega=\epsilon_p^{i-1}} \right]^{-1} \quad (4)$$

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- ② Orbital energy updates: Do we update all orbital energies in 2, just HOMO/LUMO, or all occupied plus some virtuals?
- ③ Is GW100 the right test set? They compare to some  $\Delta CCSD(T)$  results. Do we want to use that reference or do something else?

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Note that we can do  $evGW$  and/or  $evGW_0$ . To understand the difference, consider the GW self-energy

$$\Sigma_{pq}^c(\omega) = \sum_{im} \frac{M_{pi,m} M_{qi,m}}{\omega - \epsilon_i + \Omega_m - i\eta} + \sum_{am} \frac{M_{pa,m} M_{qa,m}}{\omega - \epsilon_a - \Omega_m + i\eta} \quad (5)$$

In  $evGW_0$ , we update only green, while in  $evGW$  we update both green and red.