Formal Specification and Verification of Object-Oriented Programs



The Java Modeling Language: Basic Language Features (Part II)



Focus: Basic JML expressions and normal behavior specification of methods

```
/*@ < visibility modifier > normal_behavior
@ requires P;
@ ensures Q;
@ assignable < set of locations >;
@*/
T m(T1 p1, ..., Tn pn)
```

- ▶ JML method specification attached to methods as comments (must be placed directly before the method declaration)
- visibility of a specification case determines access: only accessible fields and methods can be used
 - spec_public can be used to lift visibility of fields for specifications (similar: spec_protected)
- normal_behavior opens a normal behavior specification case



Focus: Basic JML expressions and normal behavior specification of methods

```
/*@ < visibility modifier > normal_behavior @ requires P; @ ensures Q; @ assignable < set of locations >; @*/
T \ m(T1 \ p_1, \ \ldots, \ Tn \ p_n)
```

- keyword
 - requires means that boolean JML expression P denotes a precondition
 - ensures means that boolean JML expression Q denotes a postcondition of method m
- several requires clauses with preconditions P₁,..., P_n are equivalent to a single requires clause with precondition P₁ && ... && P_n (same for ensures)



Focus: Basic JML expressions and normal behavior specification of methods

```
/*@ < visibility modifier > normal_behavior
@ requires P;
@ ensures Q;
@ assignable < set of locations >;
@*/
T m(T1 p<sub>1</sub>, ..., Tn p<sub>p</sub>)
```

keyword assignable defines a list of heap locations (static/instance fields, array elements) the method is allowed to change (locations not listed must be unchanged after termination of m or must not have existed in the pre-state).

Special values:

- assignable \everything: method may cause arbitrary side effects
- assignable \nothing: method must not change any location existing in the pre-state (may create new objects)
- assignable \strictly_nothing: method must neither change any location nor create new objects



Focus: Basic JML expressions and normal behavior specification of methods

```
/*@ < visibility modifier > normal_behavior
@ requires P;
@ ensures Q;
@ assignable < set of locations >;
@*/
T m(T1 p<sub>1</sub>, ..., Tn p<sub>n</sub>)
```

- for a method to adhere to the above normal behavior specification, it must guarantee that if called in a state (the pre-state) which satisfies the precondition P that it will
 - terminate normally,
 - terminate in a state (the post-state) satisfying Q and
 - in the post-state only the locations allowed by the assignable clause might have a different value than in the pre-state

JML Expressions (so far)



Definition (JML Expressions)

- ► Each side-effect free JAVA expression is a JML expression
- ▶ If E is a side-effect free JAVA expression, then \old(E) is a JML expression
- If a and b are boolean JML expressions, x is a variable of type t:

```
▶ !a ("not a"), a && b ("a and b"), a || b ("a or b")
```

- ▶ a ==> b ("a implies b")
- a <==> b ("a is equivalent to b")
- ► (\forall t x; a) ("for all x of type t, a is true")
- ► (\exists t x; a) ("there exists x of type t such that a")
- ► (\forall t x; a; b) ("for all x of type t fulfilling a, b is true")
- (\exists t x; a; b) ("there exists an x of type t fulfilling a,

such that b is true")

are also boolean JML expressions.

Range Predicates



Definition (Range predicate)

```
In the JML expressions (forall\ t\ x;\ a;\ b) and (exists\ t\ x;\ a;\ b) the boolean a is called range predicate.
```

Range predicates are syntactic sugar for standard FOL quantifiers:

```
(\forall t x; a; b)
        equivalent to
(\forall t x; a ==> b)

(\exists t x; a; b)
        equivalent to
(\exists t x; a && b)
```

Pragmatics of Range Predicates



Range predicates used to restrict range of x further than to its type t

Example

"Array a is sorted between indices 0 and 9":

```
(\forall int i,j; 0<=i && i<j && j<10; a[i] <= a[j])
```

Using Quantified JML Expressions



► An array int a contains only non-negative elements

— JML —

(\forall int i; 0 <= i && i < a.length; a[i] >= 0)

——— JML —

▶ The variable m holds a maximal element of array a

— .IMI —

(\forall int i; 0 <= i && i < a.length; m >= a[i])

– JML ——

Is this sufficient? Need in addition:

— JML —

(\exists int i; 0 <= i && i < a.length; m == a[i])

· JML —

HealthTracker: StepCounter

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How to specify the behavior of methods in an interface? Use pure methods.

* A step counter tracks the number of steps until a

```
* {@link reset()} occurs. After resetting, counting restarts
 * with 0 steps. Call {@link incSteps(int)} to update counter.
 * Walked distance is computed using the total number of steps
 * and the step size. */
public interface StepCounter {
  public int getStepsTotal();
 public void reset();
 public void incSteps(int p_inc);
 public int getStepSize();
 public int getDistance();
 public void setStepSize(int size);
```

Pure Methods: Using Queries in Specifications



```
Method get<XXX>() pure methods in interface (others have side-effects), e.g.,
              public /*@ pure @*/ int getStepsTotal();
Can be used to express the behavior of other methods, e.g.,
 /*@ public normal_behavior
   @ requires true; // <- can be ommitted
   @ ensures getStepsTotal() == 0; @*/
public void reset();
 /*@ public normal_behavior
   @ requires p_inc >= 0;
   @ ensures getStepsTotal()==\old(getStepsTotal()) + p_inc; @*/
public void incSteps(int p_inc);
```

All methods can be completely specified using getStepsTotal(). getStepSize()

Pure Methods: Using Queries in Specifications



Usage of pure methods enables us to

- specify the behavior of methods declared in interfaces
- reduce the need for spec_public fields in specifications (spec_public violates hiding in specifications)
- provide variability/flexibility for the actual implementation

What about assignable?

missing assignable clause means assignable \everything; (method may have arbitrary side-effects)

Limit of this approach. For a solution, see a later lecture.

(Exercise: Use queries to simplify the specification of classes HealthTracker and Category of previous lecture. Reduce/Eliminate usage of spec_public and usage of fields in method specifications.)

Capturing Object Inherent Design Properties



```
public interface StepCounter {
   public /*0 pure @*/ int getStepsTotal();
   public void reset();
   public void incSteps(int p_inc);

   public /*0 pure @*/ int getStepSize();
   public /*0 pure @*/ int getDistance();
   public void setStepSize(int size);
}
```

Which other properties would we expect?

For instance,

- step count non-negative
- step size positive (strictly greater than zero)

Capturing Object Inherent Design Properties



```
public interface StepCounter {
   public /*@ pure @*/ int getStepsTotal();
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   public /*@ pure @*/ int getDistance();
   public void setStepSize(int size);
}
```

Which other properties would we expect?

For instance,

- ▶ step count non-negative
- step size positive (strictly greater than zero)

These properties should hold at any time. Clients should be able to rely on them.

Capturing Object Inherent Design Properties



```
public interface StepCounter {
   public /*@ pure @*/ int getStepsTotal();
   public void reset();
   public void incSteps(int p_inc);

   public /*@ pure @*/ int getStepSize();
   public /*@ pure @*/ int getDistance();
   public void setStepSize(int size);
}
```

Which other properties would we expect?

For instance,

- ▶ step count non-negative
- step size positive (strictly greater than zero)

One possibility: Add them as pre- and postcondition to each method.

Object State Properties as Pre-/Post Pairs



Adding object properties as pre-/post pairs:

```
/*@ public normal_behavior
  @ requires getStepsTotal() >= 0 && getStepSize() >= 0;
  @ ensures getStepsTotal() == 0 &&
     getStepsTotal() >= 0 && getStepSize() >= 0;
  @*/
public void reset();
/*@ public normal behavior
  @ requires p_inc >= 0 &&
   getStepsTotal() >= 0 && getStepSize() >= 0;
  @ ensures getStepsTotal() == \old(getStepsTotal()) + p_inc &&
     getStepsTotal() >= 0 && getStepSize() >= 0
  0*/
public void incSteps(int p_inc);
```

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Object State Properties as Pre-/Post Pairs



Adding object properties as pre-/post pairs:

```
/*@ public normal_behavior
  @ requires getStepsTotal() >= 0 && getStepSize() >= 0;
    ensures getStepsTotal() == 0 &&
  0
  @*/
          Problems:
public
            clutters specification
/*@ pu
            must be added to all additional methods.
  @ r€
              of implementing classes
  0
          Better solution: Class Level Specifications
                                                       ()) + p_inc &&
    er
  0
  @*/
public void incSteps(int p_inc);
```

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Class Level Specifications



How to specify constraints on state of a class?

Class level specifications place restrictions on the object state

Kinds of Class Level Specifications in JML

- class invariants (or synonym: object invariants)
- (initially clauses)
- (history constraints)

We focus on class invariants.

From where do class invariants come?

- ► Modeled reality (e.g., there is no such thing as negative steps)
- Consistency of redundant data representations (e.g., caching)
- Restrictions for efficiency (e.g., maintaining sortedness)

Class Invariants: Step Counter Cnt'd



```
public interface StepCounter {
  //@ public instance invariant getStepsTotal() >= 0;
  //@ public instance invariant getStepSize() >= 0;
  //@ public instance invariant
  //@
           getStepSize() * getStepsTotal() == getDistance();
  public /*@ pure @*/ int getStepsTotal();
  public /*@ pure @*/ int getStepSize();
  public /*@ pure @*/ int getDistance();
  public void setStepSize(int size);
```

Specifying State Constraints



So far: JML used to specify (local) method behavior

How to specify constraints on state of a class?

- Consistency of redundant data representations (e.g., caching)
- Restrictions for efficiency (e.g., maintaining sortedness)

Constraints on state are global: all methods must preserve them

Static vs. instance invariants



Instance invariants, on the other hand, can access the ${f this}$ -reference. For instance.

```
public class SimpleStepCounter implements StepCounter{
  private int stepSize;
  //@ private instance invariant this.stepSize >=0;
  ...
}
```

Static invariants do not have access to the this-reference.

```
public class SimpleStepCounter implements StepCounter{
  private static int MAX_STEP_SIZE;
  //@ private static invariant MAX_STEP_SIZE >=0;
  ...
}
```

Static vs. instance invariants: Defaults



If no modifier instance or static is given, invariants

- ▶ in classes are by default instance invariants
- in interfaces are by default static invariants

System Correctness



When do we call a software system correct?

In other words, when does

- an implementation adhere to a specification, e.g., where and when does it need to
 - establish,
 - preserve and
 - assume invariants (and which of them)
- what are the global guarantees of a correct implementation, e.g.,
 - does it impose a closed-world or open-world assumption (modularity)

Non-trivial research question.

Class Invariants: Intuition, Notions & Scope



Basic Intention/Intuition: Class invariants must be

- established by
 - the constructor (instance invariants) and
 - static initialisation (static invariants)
- preserved by all non-helper methods
 - assumed in prestate (i.e., invariants are implicit preconditions)
 - ensured in poststate (i.e., invariants are implicit postconditions)
 - they can be violated during method execution

When must an implementation ensure that an invariant holds?

- Method invocation
- Method termination (normal or abrupt termination)

Scope of invariants

Invariants are written local, but are actually system wide properties.

Consequently: Invariants must not be violated by any object of any class.

The JML modifier: helper



JML helper methods

T /*@ helper @*/ m(T p1, ..., T pn) neither assume nor ensure any invariant.

Pragmatics & Usage examples of helper methods

Helper methods are almost always private.

Usage examples comprise:

- ▶ inside constructors, where invariants have not yet been established
- structural changes of a linked data structure might intermediately violate invariants (e.g., rotation methods in Red-Black trees)

Visible State Semantics for Class Invariants



Visible State Semantics (JML standard semantics)

- ▶ Instance invariants for an object o must be satisfied in all states visible for o
- Static invariants for a type T must be satisfied in all states visible for T

Definition (Visible State for an Object o (JML Ref. Manual, Sec. 8.2))

A visible state for an object o is a state that occurs at one of these moments:

- ▶ at the end of a non-helper constructor invocation (invoc.) that is initializing o,
- at the beginning or end of a non-helper
 - instance method invoc. with o as the receiver,
 - ▶ static method invoc. for a method in o's class or some of its superclasses, or
- when no constructor/instance method invoc. with o as receiver, or static method invoc. for a method in o's or some of its superclass is in progress.

Visible State Semantics for Class Invariants



Definition (Visible State for a Type *T* (JML Ref. Manual, Sec. 8.2))

A visible state for a type T is a state that

- occurs after static initialization for T is complete and
- ▶ it is a visible state for some object that has type *T*.

Note: Objects of subtypes of type T also have type T.

Visible State Semantics for Class Invariants: Example



Assume two different objects o, u of class SimpleStepCounter

```
m() { // neither a method of o or u
 O.mergeCounters(u);
                                                    Visible state for object o, u?
                                                           o,u
void mergeCounters(StepCounter p_other) {
                                                            u
 int otherSteps = p_other.getStepsTotal();
 int ownSteps = this.getStepsTotal();
                                                           o,u
  . . . ;
                         0
                                                           o.u
```

Visible State Semantics for Class Invariants: Example



Assume two different objects o, u of class SimpleStepCounter

```
m() { // neither a method of o or u
 O.mergeCounters(u);
                                                     Visible state for object o, u?
                                                            o,u
void mergeCounters(StepCounter p_other) {
 int otherSteps = p other.getStepsTotal():
                For all other objects (except the one executing m)
                all states of the considered states are visible states
 int ownSte
                          0
                                                            o.u
```

Visible State Semantics for Class Invariants



JML ensures invariants by implicitly requiring from each non-helper method (or constructor) *m*

- 1. to assume the
 - ▶ instance invariants of all objects o, for which m's pre-state is a visible state for o
 - ▶ static invariants of all types *T*, for which *m*'s pre-state is a visible state for *T*
- 2. to establish the
 - instance invariants of all objects o, for which m's post-state is a visible state for o
 - ▶ static invariants of all types T, for which m's post-state is a visible state for T

Visible State Semantics: Problems



The visible state semantics has some severe short-comings:

- non-modular: changing any invariant requires to reverify (almost) all methods
- too strong restrictions on methods/types and their clients

```
public class Pair {
   private Object first;
   private Object second;

public Pair(Object p_first, Object p_second) { ... }
   public /*@ pure @*/ Object getFirst() { return first; }
   public /*@ pure @*/ Object getSecond() { return second; }
}
```

Using visible state semantics, getFirst, getSecond— assume and ensure (among others) invariants of contained elements. Which is unnecessary as behavior of Pair does not rely on any properties of the contained objects.

Semantics of Class Invariants: JML*



We use JML*: A JML variant with (among others) a different invariants semantics (The basic idea is taken from Spec# and called the Boogie-Methodology; the realisation differs) Idea: Give responsibility where invariants are assume or ensured back to specifier

```
JML* Keyword: \invariant_for(o)
```

\invariant_for(o) is a Boolean JML expression which evaluates to true iff. all accessible instance invariants of *o* are satisfied.

Example

```
/*@ public normal_behavior
  @ requires \invariant_for(this) && \invariant_for(key);
  @ ensures \invariant_for(this) && \invariant_for(key); @*/
public void put(Object key, Object value) { ... }
specifies that put assumes and ensures the invariants of this and key
```

Semantics of Class Invariants: JML*



We use JML*: A JML variant with (among others) a different invariants semantics (The basic idea is taken from Spec# and called the Boogie-Methodology; the realisation differs) Idea: Give responsibility where invariants are assume or ensured back to specifier

JM For non-helper methods \invariant_for(this) \in implicitly added to pre- and postconditions! acc

es to true iff. all

For static invariants: \static_invariant_for(TypeRef)

- @ requires \invariant_for(this) && \invariant_for(key);
- @ ensures \invariant_for(this) && \invariant_for(key); @*/ public void put(Object key, Object value) { ... }

specifies that put assumes and ensures the invariants of this and key

Ex

Further Modifiers: non_null and nullable



JML extends the JAVA modifiers by further modifiers:

► Class fields, method parameters, method return types

can be declared as

- nullable: may or may not be null
- non_null: must not be null (this is the default)

non_null: Examples



```
private /*@ spec_public non_null @*/ String username;
Implicit invariant public invariant username != null; added to class for
fields of reference type
public void addCategory(/*@ non_null @*/ Category p_category)
Implicit precondition requires p_category != null;
added to each specification case of addCategory
public /*@ non_null @*/ Category findCategoryById(int)()
Implicit postcondition ensures \result != null;
added to each specification case of findCategoryById()
```

non_null is default in JML:
all of the above non_null's are redundant

nullable: Examples



Prevent non_null pre/post-conditions, invariants: nullable

private /*@ spec_public nullable @*/ String username;
No implicit invariant added, username might have value null

► Some of our earlier examples need nullable to work properly, e.g.:

private /*@ nullable @*/ Category findCategoryById(int p_id);

LinkedList: non_null or nullable?



```
public class LinkedList {
    private Object elem;
    private LinkedList next;
}
```

Consequence of default non_null in JML

- All elements in the list are non_null
- ► The list is either cyclic or infinite!

Repair so that the list can be finite:

```
public class LinkedList {
    private Object elem;
    private /*@ nullable @*/ LinkedList next;
}
```

Final Remarks on non_null and nullable



non_null as default in JML only since a few years

Older JML tutorials/articles might use nullable-by-default semantics

Pitfall!

```
/*@ non_null @*/ Category[] category;
is not the same as:
//@ invariant category != null;
/*@ nullable @*/ Category[] category;
The first adds implicitly:
(\forall int i; i>=0 && i<category.length; category[i] != null)
I.e., requires non_null of all array elements!</pre>
```