#### Technische Universität Darmstadt





# TK1: Distributed Systems Programming & Algorithms

Chapter 3: Distributed Algorithms

Section 4: Cooperation – Multicast & Consensus

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# **Multicast Communication**



### Meaning? (distinguish from unicast, broadcast)

- usually considered: same msg sent to "several" receivers
  - "all" receivers (?): broadcast ("whoever wants it can get it")
  - implies receiver group; membership considered transparent to sender
  - usually, all receivers in group intended to receive msg
- essential properties: "more than syntactic sugar' for N \* send()"
  - 1 multicast operation ≠ multiple sends
    - higher efficiency and/or
    - stronger delivery guarantees
- operations: g = group, m = message
  - X-multicast(g, m)
  - X-deliver(m)
    - ≠ receive(m) (e.g., delivery only after addt'l ctrl. msgs)
  - $X: \rightarrow$  additional property
    - Basic-, Reliable-, FIFO-,...



# Multicast (cont.)



#### Major issues (cf. properties):

- addressing, in particular: "optimal routing for minimal # of msgs"
- coordination
  - guarantees that msgs are received by a group of recipients
  - delivery ordering amongst group members
- advanced: grp overlaps, membership (grp change during op.?), admission, ...

#### Uses of multicast, e.g.,

- Computer Supported Cooperative Work (CSCW)
  - shared WhiteBoards & applications, video-conferencing, ...
- communication w/ replicated servers (to achieve fault-tolerance)
- boosting importance: event notification, publish/subscribe systems
- discovery services in spontaneous networking

#### Open vs. closed: multicast group is

- closed if multicast only within (+ grp overlap forbidden → becomes broadcast algo.)
- open, if proc's not member of the group may send (work-around: first unicast to grp-member, then closed-multicast)



#### Multicast in IP



- only implemented by some IP routers (though part of IPv4!): cf "mbone"
- available for UDP, uses IP auxiliary IGMP (Internet grp. mgmt.) protocol
- addressing: multicast address and port number
- IP multicast group (membership is dynamic):
  - class D IP address for which first 4 bits are 1110 in IPv4
  - IP node ∈ multicast grp if ≥ 1 proc's have sockets belonging to a multicast grp
- implementation of multicast IP routers
  - efficiency 1: on LAN, use broadcast capabilities (e.g., Ethernet)
    - use locally valid multicast address, set Time To Live (TTL) counter in IP header to 1 so that packet will never get routed outside LAN
  - efficiency 2: in Internet, router forwards msgs to all other routers that have members in multicast group (late packet replication)
    - end-2-end replication: more traffic, a packet delays following ones
    - note: session directory (sd) = public domain tool (w/ GUI) allowing users to advertise multicast sessions as
       well as their valid multicast addresses
  - no guarantees whatsoever (msg loss, reordering, duplication, etc.)



#### **Basic Multicast**



- B-multicast = multicast with "delivery guarantee if multicasting process does not crash"
- straightforward algorithm (requires reliable send)

```
To B-multicast(g, m):

∀p ∈ g: send(p, m)

On receive(m) at p: B-deliver(m)
```

- - all receipients acknowledge receipt at about same time
  - buffer overflow leads to dropping of ack messages
  - retransmits, even more ack messages
- ∃ practical algorithm using IP-multicast



### **Reliable Multicast**



#### **Desired Properties:**

- integrity: a correct proc p delivers a msg at most once, and the delivered msg is identical to the msg sent in the multicast send operation (safety)
- validity: if a correct proc multicasts msg m,
   then it will eventually deliver it (liveness)
- agreement: if a correct proc delivers a msg m sent to group g, then all other correct proc's in g will also deliver msg m
- (additionally) uniform agreement: as above,
   no matter whether initially delivering proc is correct or fails

#### Notes:

- validity expressed in terms of self-delivery, for simplicity reasons
  - validity and agreement amount to overall liveness requirement: if one proc (the sender)
    delivers a msg m, then m will eventually be delivered to all the group's correct members
  - assumes closed multicast (no strong restriction, see above)
- agreement is similar to "atomicity": all-or-nothing semantics
- reliable unicast supposed to have integrity & validity, too





#### Possible implementation: Realize *R-multicast* as a layer on top of *B-multicast*

- R-multicast: just B-multicast to all procs in group g
- On B-deliver (@R-multicast-layer): perform a complete B-multicast again to g; then R-Deliver
- properties
  - validity: a correct proc will eventually B-deliver to itself
  - integrity: based on underlying communication medium
  - agreement: B-multicast to all other proc's after B-deliver
- inefficient, since each msg is sent |g| times to each proc

```
On initialization Received := \{\};

For process p to R-multicast message m to group g

B-multicast(g, m);   //p \in g is included as a destination

On B-deliver(m) at process q with g = group(m)

if (m \notin Received)

then

Received := Received \cup \{m\};

if (q \neq p) then B-multicast(g, m); end if R-deliver m;

end if
```





#### Reliable Multicast over IP Multicast (R-IP-Multicast):

- counters "ACK implosion" plus: may benefit from efficiency of IP-Multicast
- based on observation: multicast is successful in most cases
  - therefore: use negative acknowledgement NACK to indicate non-delivery
- Sketch of algorithm (note: assumes closed multicast groups)
  - data structures: at proc. p:
    - S<sub>g</sub><sup>p</sup>: msg sequence no. for group g (# of msg's sent to g)
    - $\{R_g^q\}$ : seq. no. of latest msg that p delivered from proc  $q \in g$  (that was sent to group g)
  - init:  $S_g^p := 0$ ;  $R_g^q_i := -1 \ \forall q_i \neq p$
  - piggybacking idea: when p R-IP-multicasts msg m to group g
    - it piggybacks onto m
      - S<sub>g</sub>p
      - $q_i$ ,  $R_g^q$  as acknowledgements for all  $q_i \neq p$
    - IP-Multicast msg and piggyback information as above
    - increment S<sub>g</sub><sup>p</sup> by one





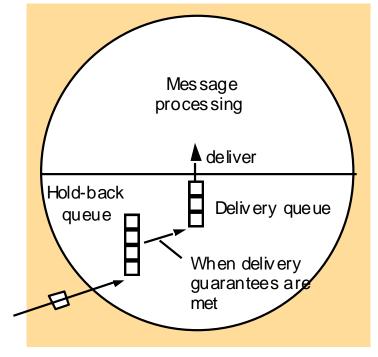
```
For process p to R-IP-multicast msg m to group g:
   S_{\rho}^{p} ++;
   IP-multicast (g, <m, S_g^p, <q<sub>1</sub>, R_g^{q1} >, ..., <q<sub>n</sub>, R_g^{qn} > >); (\forall q_i \neq p)
                                            /* below: S,q,R without index for simplicity */
On IP-deliver (<m, S, <.,.>, ..., <q, R>, ..., <.,.> ) at process r, from process p:
  if S = R_{\sigma}^{p} + 1
                                                                          /* 'expected' case */
      then R-IP-deliver (m);
              R_{\rho}^{p} ++;
                                                                          /* was msg a 'late' one? */
               « check hold-back-O »
      else if S > R_g^p + 1 then <store m in hold-back-Q>
                                                                         /* missing msg */
                                                                          /* received already */
                                        discard (m)
                                                         endif;
                               else
  endif;
  if S > R_g^p + 1 or \langle R \rangle R_q^q for any process q \in g »
                                                                          /* \ge 1 msg missing */
              « request missing msg's via nack's » endif;
```





### R-IP-Multicast (cont.):

- hold-back Q's are rather common in algo's w/ delivery guarantees
- note: piggybacked R<sub>g</sub><sup>q</sup><sub>i</sub> counters speed up detection of lost msg's
- note: nack may be send to neighbour close by, not necessarily to originator (neighbour retains copy? how long?)



In coming mes sages





#### R-IP-Multicast (cont.):

#### Properties:

- integrity
  - follows from detection of duplicates and properties of IP multicast (e.g., checksum to detect message corruption)
- validity
  - msg loss can only be detected when a successor msg is eventually transmitted
  - requires processes to multicast msgs indefinitely
- agreement
  - requires unbounded history for broadcast messages so that retransmit is always possible
- there exist practical variants that ensure validity and agreement



### **Ordered Multicast**



```
if a correct process P:
three "subclasses":
                                                      multicast(g, m);
                                                      multicast(g, m');
                                          then for all correct processes:
                                                      deliver(m') \Rightarrow
                                                           deliver(m) before deliver(m')
                                          if multicast(g, m) \rightarrow_g multicast(g, m')
                                          then for all correct processes:
                    Causal
                                                      deliver(m') \Rightarrow
                                                           deliver(m) before deliver(m')
                                          if \exists p: deliver(m) \rightarrow deliver(m')
                                          then for all correct processes:
                    Total
                                                      deliver(m') \Rightarrow
                                                           deliver(m) before deliver(m')
```



### **Ordered Multicast**



#### Notes:

- assume below: every process belongs to at most one group
- happen-before  $\rightarrow_g$  means "restricted to communication within g"
- causal ordering implies FIFO ordering
- FIFO ordering and causal ordering are partial orders
- total order allows arbitrary ordering of deliver events relative to multicast events, as long as order is identical in all correct proc's
- atomic multicast: reliable, totally ordered multicast

#### **Combinations:**

- FIFO-Total = FIFO + Total
- Causal-Total = Causal + Total
- Atomic = reliable + Total

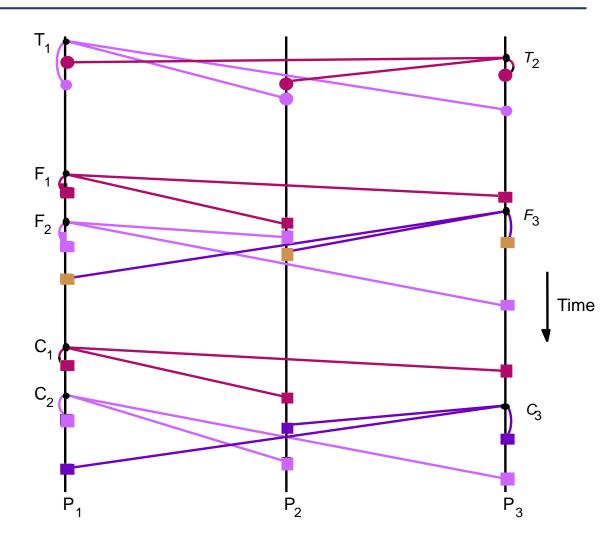


# **Ordered Multicast (cont.)**





- totally ordered msgs T<sub>1</sub> & T<sub>2</sub>
- FIFO-related msgs F<sub>1</sub> & F<sub>2</sub>
- causally related msgs  $C_1 \& C_3$
- and the otherwise arbitrary delivery ordering of msgs.





# **Ordered Multicast (cont.)**



- practical example: bulletin board:
  - FIFO makes "Hanlon's second posting" a consistent statement
  - causal assures "Re: Microkernels" appears after "Microkernels"
  - total makes "posting #24" a consistent statement
- note: Usenet ist neither causal nor total (reason: "cost")

Bulletin board: os.interesting			
Item	From	Subject	
23	A.Hanlon	Mach	
24	G.Joseph	Microkernels	
25	A.Hanlon	Re: Microkernels	
26	T.L'Heureux	RPC performance	
27	M.Walker	Re: Mach	
end	_		



# FIFO Multicast (cont.)



#### FO-multicast on top of any B-multicast:

#### Data structures at process p:

 $S_g^p$ : seq.no;  $R_g^q$ : seq.no. of latest msg it has delivered from q

#### On initialization:

$$S_g^p = 0$$

For process p to FO-multicast message m to group g

B-multicast (g, S\_g^p >)  
$$S_g^p ++$$

On B-deliver (<m, S >) at q from p

if 
$$S = R_g^p + 1$$
  
then FO-deliver (m)  
 $R_g^p ++$ 

check hold-back queue

else if  $S > R_g^p + 1$  then store m in hold-back queue endif endif

Note: IP-R-multicast is FIFO & reliable!



### **Total Multicast**



### TO-multicast: (note: still assuming non-overlapping groups)

- idea: assign totally ordered IDs to multicast msgs so that every proc makes same delivery decision based on these IDs
- delivery similar to FIFO delivery, only that group-specific seq.no's rather than procspecific seq.no's are used
- two main methods for assignment of IDs
  - sequencer
  - collective agreement on the assignment of msg IDs

#### A) Sequencer

- proc wishing to TO-broadcast attaches a unique ID i = id(m) to msg
- msg is sent to sequencer as well as all members of g
- sequencer maintains group-specific seq.no. s<sub>g</sub> which it uses to assign increasing and consecutive seq.no's to the messages it B-delivers
- announces the order in which members of g have to deliver these msgs using a B-multicasted order-msg

note: sequencer is bottleneck !!





1. Algorithm for group member *p* 

```
On initialization: r_g := 0;

To TO-multicast message m to group g
B-multicast(g \cup \{sequencer(g)\}, < m, i>);

On B-deliver(< m, i>) with g = group(m)
Place < m, i> in hold-back queue;

On B-deliver(<"order", i, S>) with g = group(m)
wait until < m, i> in hold-back queue and S = r_g + 1;
TO-deliver m; // (after deleting it from the hold-back queue) r_g = S;
```

2. Algorithm for sequencer of *g* 

```
On initialization: s_g := 0;

On B-deliver(<m, i>) with g = group(m)

B-multicast(g, <"order", i, s_g>);

s_g := s_g + 1;
```





#### B) collective agreement on the assignment of msg IDs

- background: implemented in the ISIS toolkit, groups may be open or closed
- idea: receiving proc's bounce proposed seq.no.'s to sender, sender returns agreed seq.no.'s
- data structures: each proc q in group g maintains
  - A<sub>g</sub>q: largest agreed seq.no. it has observed so far for group g
  - P<sub>g</sub><sup>q</sup>: own largest proposed seq.no.
- p B-multicasts <m, i> to g, where i is unique ID(m)
- each recipient q:
  - replies to g with **proposal for agreed** seq.no.  $P_g^q := max(A_g^q, P_g^q) + 1$
  - as above, might yield identical seq.no for multicasts of different proc's
     → possible solution: concatenate with unique proc-ID (see example two slides below)
  - provisionally assigns own proposed seq.no. to msg and queues msg in hold back queue, ordered according to proposed seq.no.
- p, having received all replies:
  - chooses largest proposed number as agreed seq.no. α
  - B-multicasts <*i*, *a*> to g





### B) collective agreement on the assignment of msg IDs (cont.)

- each proc q in g, having received  $\langle i, a \rangle$  from p, sets  $A_g^q := max(A_g^q, a)$ 
  - reorders received msg in hold-back Q if received seq.no. differs from proposed no.
  - only when msg at head of hold-back queue is assigned an agreed seq.no., it will be queued in delivery queue

#### re. correctness of B (obvious: correct proc's eventually agree on seq.no.)

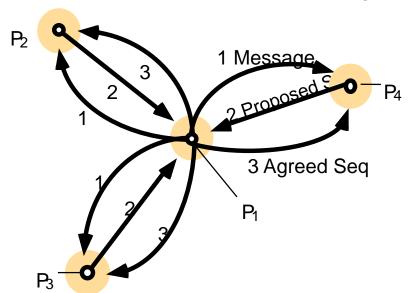
- to be shown, that
  - seq.no.s are monotonically increasing
  - no proc delivers msg before there is agreement
- assume m<sub>1</sub> i) to have "agreed seq.no."; ii) to be at head of hold-back Q
  - a msg received after this state should be 'to be delivered' after m<sub>1</sub>,
     i.e. it should be guaranteed to get a larger agreed seq.no. than m<sub>1</sub>
  - let m<sub>2</sub> msg, not yet w/ agreed seq.no., but in same Q as m<sub>1</sub>
  - agreedSeq $(m_2) \ge proposedSeq(m_2)$  (by construction of algorithm)
  - proposedSeq(m<sub>2</sub>) > agreedSeq(m<sub>1</sub>) (since m<sub>1</sub> at head of queue)
  - $\Rightarrow$  agreedSeq(m<sub>2</sub>) > agreedSeq(m<sub>1</sub>)

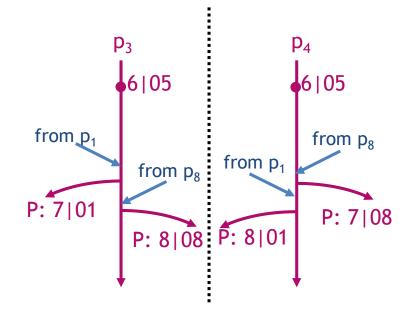




#### Example to the right:

- concatenate seq. no. (1,2,3...) with proc-ID of sender, e.g. 4|03 (<100 proc's)</li>
- last agreed seq.no was 6 | 05
- two proc's p<sub>3</sub>, p<sub>5</sub> receive multicasts in different order from p<sub>1</sub>, p<sub>8</sub>





Performance?

- 3 serial messages!





#### Data structures at process p:

 $A_g^p$ : largest agreed seq.no. seen,  $P_g^p$ : largest proposed seq.no. of process p

On initialization:  $P_g^p = 0$ 

For process p to **TO-multicast** message m to group g

**B-multicast** (g, <m, i >) /i = unique id for m, contains sender no.

On **B-deliver (<m, i> )** at q from p

$$P_g^q = max (A_g^q, P_g^q) + 1; send (p, < i, P_g^q >);$$

store <m, i,  $P_g^q$  > in hold-back Q: for order, use  $A_g^q$  if assigned,  $P_g^q$  otherwise

On receive (<i, P>) at p from q (wait for all replies; A is the largest reply)

B-multicast(g, < "order", i, A >)

On **B-deliver (<"order", i, A > )** at q from p

$$A_g^q = max (A_g^q, A)$$

attach A to message i in hold-back Q → re-order messages in hold-back Q, (increasing seq.no.'s, if identical seq.no.: use sender no. to order)

while msg m in front of hold-back Q has been assigned an agreed seq.no.

do remove m from hold-back Q; TO-deliver (m) od;



### **Consensus: Introduction**



### Some consensus proNotrused in 2015/16 Lecture

"all correct computers controlling a spaceship should decide to proceed with landing, or all of them should decide to abort (after each has proposed one action or the other)"

"in an electronic money transfer transaction, all involved processes must consistently agree on whether to perform the transaction (debit and credit), or not"

"in mutual exclusion, processes need to agree on which process enters critical section"

"in election, processes need to agree on elected process"

"in totally ordered multicast, processes need to agree on a consistent message delivery order"



# **Consensus: Introduction (cont.)**



### process failure mod Not used in 2015/16 Lecture

- crash failures: processes stop (fail), but remain silent
- byzantine failures: processes fail, but may still respond to environment with arbitrary, erratic behavior (e.g., send false acknowledgements, etc.)
- ... a more detailed definition (for your records):

Class of failure	Affects	Description
Fail-stop	Process	Process halts and remains halted. Other processes may detect this state.
Crash	Process	Process halts and remains halted. Other processes may not be able to detect this state.
Omission	Channel	A message inserted in an outgoing message buffer never arrives at the other end's incoming message buffer.
Send-omission	Process	A process completes a <i>send</i> , but the message is not put in its outgoing message buffer.
Receive- omission	Process	A message is put in a process's incoming message buffer, but that process does not receive it.
Arbitrary (Byzantine)	Process or channel	Process/channel exhibits arbitrary behaviour: it may send/transmit arbitrary messages at arbitrary times, commit omissions; a process may stop or take an
		meorreet step.



# **Consensus: Introduction (cont.)**



# Factors threatening Not used in 2015/16 Lecture

- failures
  - communication link or process failures
  - crash failures (fail-silent) or byzantine failures (arbitrary)
     (after Byzantine Empire 330-1453, in which unfaithfulness and untruthfulness have allegedly been very common)
- network characteristics
  - synchronous or asynchronous
- failure detectors
  - reliable or unreliable
- are msgs authenticated (digitally signed) or not
  - can a process lie about the content of message that it received from a correct process?
  - can adversary claim to send message under a false expedient's ID?

#### Model:

- processes communicating by msg passing
- desirable: reaching consensus even in the presence of faults
  - assumption: communication is reliable, but processes may fail

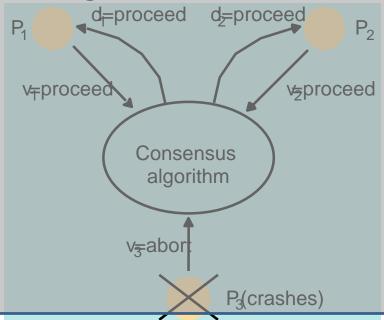


#### Consensus: C



### The Consensus ProbNot used in 2015/16 Lecture

- agreement wrt. value of a decision variable among all correct proc's
  - p<sub>i</sub> is in state undecided & proposes a single value v<sub>i</sub>
  - next, processes communicate with each other to exchange values
  - in doing so, p<sub>i</sub> sets decision variable d<sub>i</sub> and enters *decided* state after which the value of d<sub>i</sub> remains unchanged





#### **Consensus: BG**



### The Byzantine Gene Not Used m 2015/16 Lecture

- $\blacksquare$   $\ge$  3 generals to agree on attack or retreat; commander issues order, others (lieutenant to commander) must decide: attack or retreat
- one of the generals may be treacherous
  - if commander treacherous:proposes attacking to one general and retreating to the other
  - if lieutenants treacherous: tell some peers that commander ordered to attack, and others that commander ordered to retreat
- difference to consensus problem:one process supplies a value that others have to agree on
- properties
  - termination: eventually each correct process sets decision variable
  - agreement: the decision value of all correct processes is the same
  - integrity: if commander is correct, then all processes decide on the value that the commander proposes
    - note: implies agreement only if commander is correct, but: commander need not be correct (see above)



# Consensus: BG in Sync. Net



- allow arbitrary (byzantin Notilused in 2015/16 Lecture
- up to f faulty processes
- correct processes can detect absence of a msg through timeout, but: cannot conclude that sender crashed, since it may be silent for some time and then start sending messages again
- assume private communication channels
  - 4<sup>th</sup> proc cannot detect
    - if proc sends msg's w/ different content to 2 peers
  - no faulty proc can inject msgs into channels connecting correct proc's
- assume that msgs are not digitally signed (authenticated and verifiable)
- general result (Lamport, Shostak and Pease)
  - no solution if  $N \le 3f$
  - give an algorithm for N ≥ 3f+1







#### impossibility for N = 3 processes

- read "3:1:u" as "three says one says u"
- both scenarios show two rounds of messages
- left: all p<sub>2</sub> knows is that it has received two different values
- right: same situation, even though now commander is faulty
- assume a solution existed
  - p<sub>2</sub> would have to decide on value v, by integrity condition of BG
- assume no algorithm can decide locally for p<sub>2</sub> between the 2 scenarios
  - then p<sub>2</sub> would need to decide on w (sent by commander) in 2<sup>nd</sup> scenario
- same reasoning for p<sub>3</sub> w
  - will have to decide about commander's value, which is violation of agreement in right hand scenario, hence contradiction





### impossibility for N ≤Not(Pasedin \$2015/16 Lecturert; sketch)

- assume a solution existed for  $N \le 3f \rightarrow construct$  solution for (3, 1)
- let each of 3 proc's  $p_1$ ,  $p_2$  &  $p_3$  simulate  $n_1$ ,  $n_2$  &  $n_3$  generals, where  $n_1+n_2+n_3=N$  and  $n_1$ ,  $n_2$ ,  $n_3 \le f$
- assume that one of the processes is faulty
- correct processes simulate correct generals
  - internal interaction of "own" generals
  - send msgs from "own" generals to those simulated by other processes
- faulty general's f proc's are faulty and may emit spurious messages
- since  $n_1 + n_2 + n_3 = N$  and  $n_1$ ,  $n_2$ ,  $n_3 \le N/3$ ,  $\le f$  generals are faulty
- however, now there is a way for 2of3 proc's to reach consensus: each proc decides on value chosen by all generals it simulates
- contradicts impossibility for N = 3





# solution for $N \ge 3f + 1$ Not used in 2015/16 Lecture

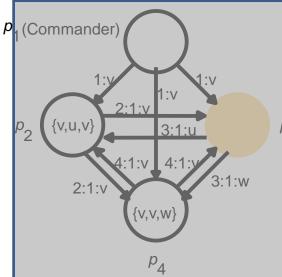
solution by Pease, Shostak & Lamport too complex to present (cf. http://www.cs.wisc.edu/~bart/739/papers/byzantine.pdf), therefore:

#### presentation of solution for N = 4, f = 1

- correct generals reach agreement in two rounds:
  - first, commander sends value to each lieutenant
  - second, each lieutenant sends value it received to all peers
- lieutenant receives:
  - 1 value from commander, N-2 values from peers
- if commander faulty, then all lieutenants correct, each will have gathered exactly the set of values that the commander sent out
- if one lieutenant faulty, each of its peers receives N-2 copies of the value the commander sent out, plus the faulty lieutenant value
- to reach agreement, simple majority function suffices
  - since  $N \ge 4$ ,  $N-2 \ge 2$ , majority function will ignore value of faulty lieutenant, and produce value of commander if commander is correct (may produce  $\bot$  if commander incorrect)
- note: BG requires integrity only if commander correct



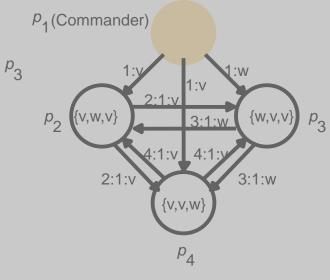




 $p_2$ : majority({v,u,v}) = v

 $p_3$ : majority( $\{v,v,w\}$ ) = v

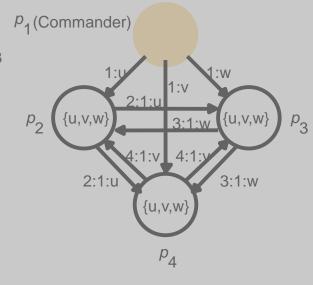
# Not used in 2015/16 Lecture



 $p_2$ : majority( $\{v, w, v\}$ ) = v

 $p_3$ : majority( $\{v,v,w\}$ ) = v

 $p_4$ : majority({w,v,v}) = v



 $p_2$ ,  $p_3$ ,  $p_4$ : majority( $\{v,u,w\}$ ) =  $\bot$ 



# **Consensus: Asynchronous Systems**



### Impossibility of agreNoteused in 2015/16clecture ms

- previous algo.s: synchrony assumed (msg exchange in rounds, timeouts)
- in asy. systems, no algo. can guarantee reaching consensus, even with just one process crash failure (Fischer, Lynch and Paterson, 1985)
  - proof idea: show that there is always some continuation of the proc's execution that avoids consensus being reached
- consequences: in async. systems, no solution to BG, IC, TOR-multicast
- of course, in practice consensus can often be reached, but a residual probability that consensus cannot be reached remains
- possible approaches to reaching consensus by weakening assumptions:
  - partial synchrony
  - masking faults
  - modified failure detectors
  - randomized algorithms





- G. Coulouris, J. Dollimore, T. Kindberg, Verteilte Systeme -Konzepte und Design 3. Aufl (2002) Pearson Studium
  - original: english; both available & good
  - closest to chapter 2, some slides included
- A. Tanenbaum, M.v.Steen, Verteilte Systeme: Grundlagen und Paradigmen, Pearson Studium 2003
  - original: english; both available & good
  - yet, MM: "does not compare to Tanenbaum's ,networks' or to ,Coulouris'"
- G. Tel, Introduction to Distributed Algorithms 2nd Ed (2001);
   Cambridge University Press, ISBN: 05217948
  - english, available
  - for those who want to go deep!