



## TK1: Distributed Systems - Programming & Algorithms

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### Extra Theory Assignment Submission Date: -

By handing in a solution you confirm that you are the exclusive author(s) of all the materials. Additional information can be found here: <https://www.informatik.tu-darmstadt.de/de/sonstiges/plagiarismus/>

### Task 1: Applying SOS-rules (3P)

The semantics of CCS (Calculus of Communicating Systems) is defined on the basis of Structural Operational Semantics (SOS)-rules. By applying these rules on CCS expressions the corresponding Labelled Transition System (LTS) can be built, which shows the system as a directed graph.

Apply the SOS-rules on the CCS processes  $P_1$  to  $P_7$  and sketch the corresponding LTSs as shown in the following example (Figure 1). Please write the number of the SOS-rule that you used for solving next to the corresponding edge. You can find the number of the SOS-rule in the lecture slides.

*Example*  $\coloneqq (b)((a.'b.0|'a.b.0))$

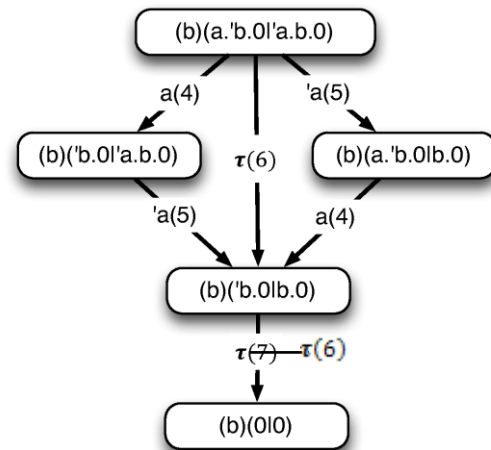


Figure 1: LTS of the process “Example”

Processes (for Task 1):

$$P_1 \coloneqq b.0 + c.0$$

$$P_2 \coloneqq a.(b.0 + c.0)$$

$$P_3 \coloneqq a.\tau.(\tau.b.0 + c.0)$$

$$P_4 \coloneqq (d,e)(a.d.(e.b.0 + c.0)|'d.'e.0)$$

$$P_5 \coloneqq ((a.'b.0 + c.'b.0)|'a.b.0)$$

$$P_6 \coloneqq (b)((a.'b.0 + c.'b.0)|('a.b.0 + 'c.b.0))$$

$$P_7 \coloneqq (a,d)(c.d.0[c/d][d/a]|'a.0|'b.0)$$

## Task 2: Weak Bisimulation (3P)

Four processes are given

$$P := a. (b.P + c.P)$$

$$R := \tau. a. (b.R + c.R)$$

$$Q := a. (\tau. b.Q + \tau. c.Q)$$

$$S := a. (\tau. b.S + c.S)$$

Sketch the LTS for each process. Then test each process to each other process on weak Bisimulation equivalence ( $P \approx Q$ ): Which processes are equivalent to each other? Provide the equivalence relation R for the equivalent processes.

## Task 3: Switch (4P)

The process in figure 2 models a switch. Model different behavior in CCS:

1. Initially, every incoming  $a$  is channeled through. After an  $s$  is received, the following  $a$ 's are discarded.
2. Initially, every incoming  $a$  is discarded. After an  $s$  has been received, incoming  $a$ 's are transformed into  $b$ 's. Another  $s$  changes the behavior back again, etc.
3. Initially, every incoming  $a$  is transformed into  $b$ . If an  $s$  is received, the next two  $a$ 's are channeled through. The following  $a$ 's are again transformed into  $b$ 's.

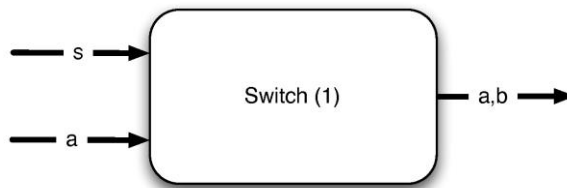


Figure 2: Depending on the internal behavior of the agent and depending on the reception of  $s$ , the message  $a$  is either channeled through, discarded or transformed into  $b$ .