# Formal Specification and Verification of Object-Oriented Programs



The Java Modeling Language: Basic Language Features (Part I)





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Lecture URL: https://moodle.informatik.tu-darmstadt.de/course/view.php?id=440





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Course: Lectures & Exercises

Course Language English Lecture/Exercise Sessions

► Monday, 11:40 - 13:20 in C110 (S2|02)

► Thursday, 13:30 - 15:10 in C110 (S2|02)





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### Lecture: Prerequisites

- Experience with Java-like object-oriented programming language
  - Classes, interfaces, inheritance, dynamic dispatch, visibility etc.
- (Basic) knowledge about
  - First-order logic (FOL): Syntax & Semantics
  - ▶ Deduction for FOL: E.g., sequent/tableaux/natural deduction calculus
  - ► Hoare logic or wp-calculus (Dijkstra)





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#### **Exercises**

- Assignments are published one week before an exercise session
- Not corrected, but:
  - Discussed in exercise sessions
  - Live from active participation



An act of identifying something precisely or of stating a precise requirement.

(Oxford Dictionary)



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"I need a screw."



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## "I need a screw."



### Imprecise

- Length, diameter, thickness
- ► For which material? Wood, metal, concrete?



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- Length, diameter, thickness
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#### Possible implicit assumptions

- ... and bring it to me.
- ... the one I've given you a few moments ago.



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## "I need a screw."



#### Imprecise

- Length, diameter, thickness
- ► For which material? Wood, metal, concrete?

#### Possible implicit assumptions

- ... and bring it to me.
- ▶ ... the one I've given you a few moments ago.

#### I do not need (framing)

- a hammer
- ▶ a sandwich, a hat . . .

## **Specification Target**



Explicit set of requirements to be satisfied by a

material, product, system, or service.

(Form and Style for ASTM Standards, Blue Book of ASTM)

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System level specification
(requirements analysis, GUI, use cases)
important, but
not subject of this course

## **Specification Target**



### Explicit set of requirements to be satisfied by a

material, product, system, or service.

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#### We focus (mostly) on:

#### Unit specification—contracts between implementors on various levels:

- ► Application level ↔ application level
- ► Application level ↔ library level
- ▶ Library level ↔ library level

## **Unit (Module) Specifications**



Cf. unit testing

## In Object-Oriented Setting:

Units to be specified are interfaces, classes, and their methods

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#### First focus on methods

## Method specifications must comprise the following aspects:

- Result value
- Initial values of formal parameters
- Pre-state and post-state

## **Unit (Module) Specifications**



#### Cf. unit testing

## In Object-Oriented Setting:

Units to be specified are interfaces, classes, and their methods

#### First focus on methods

## Method specifications must comprise the following aspects:

- Result value
- Initial values of formal parameters
- Accessible part of pre-/post-state

## Meaning of Pre-/Post-Condition Pairs



#### Definition

A pre-/post-condition pair for a method m is satisfied by the implementation of m if:

When m is called in any state that satisfies the precondition then in any terminating state of m the postcondition is true.

## Meaning of Pre-/Post-Condition Pairs



#### Definition

A pre-/post-condition pair for a method m is satisfied by the implementation of m if:

When m is called in any state that satisfies the precondition then in any terminating state of m the postcondition is true.

#### Remarks

- 1. No guarantee when the precondition is not satisfied
- 2. Termination may or may not be guaranteed
- Terminating state may be reached by normal or by abrupt termination (e.g., exception)

## **Specifications as Contracts**



Useful analogy to stress the different roles/obligations/responsibilities in a specification:

Specification as a contract (between method implementor and user)

"Design by Contract" methodology (Meyer, 1992, EIFFEL)

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Contract between caller and callee (called method)

Callee guarantees certain outcome provided caller guarantees prerequisites

### Running Example: HealthTracker.java



```
public class HealthTracker {
//fields:
private String username;
private Category[] category;
private int nrCategories;
// methods:
public int getNumberCategories()
public String getUsername()
public Category findCategoryById(int)
public boolean addCategory(Category)
```

```
public class Category {
  private int id;
  public int getId();
  ...
}
```

## **Informal Specification**



Very informal specification of

boolean addCategory(Category p\_category)

"Add the given category p\_category to the list of categories and return success provided that no category with the same id exists and the maximal number of categories has not yet been reached.

Otherwise return false to indicate failure."



Contract states what is guaranteed under which conditions



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precondition

 $p\_{\rm category}$  , category are not null, nrCategories is non-negative, maximal number of categories reached



Contract states what is guaranteed under which conditions

precondition p\_category, category are not null, nrCategories is non-negative,

maximal number of categories reached

postcondition category is not added, false is returned



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-------------------------	------------------	--------------------------------------

precondition p\_category, category are not null, nrCategories is non-negative,

maximal number of categories reached

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precondition p\_category, category are not null, nrCategories is non-negative,

category with same id is present

maximal number of categories not reached

postcondition category is not added, false is returned



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precondition p\_category, category are not null, nrCategories is non-negative,

maximal number of categories reached

postcondition category is not added, false is returned

precondition p\_category, category are not null, nrCategories is non-negative,

category with same id is present

maximal number of categories not reached

postcondition category is not added, false is returned

precondition p\_category, category are not null, nrCategories is non-negative

maximal number of categories not reached,

category with same id is not present



Contract states	s what is guaranteed under which conditions
precondition	$p\_$ category, category are not null, $nrCategories$ is non-negative, maximal number of categories reached
postcondition	category is not added, false is returned
precondition	$p\_{\rm category}$ , category are not null, nrCategories is non-negative, category with same id is present
postcondition	maximal number of categories not reached category is not added, false is returned
precondition	$p\_$ category, category are not null, $nrCategories$ is non-negative maximal number of categories not reached, category with same id is not present
postcondition	category is added , nrCategories increased by 1 and true is returned

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## **Formal Specification**



Natural language specs are very important and widely used

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Natural language specs are very important and widely used, we focus on

## Formal Specification

Describe contracts of units with mathematical rigour

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## Formal Specification

Describe contracts of units with mathematical rigour

#### Motivation

- ► High degree of precision
  - formalization often exhibits omissions/inconsistencies
  - avoid ambiguities inherent to natural language
- ► Potential for automation of program analysis
  - run-time assertion checking
  - monitoring
    - test case generation
  - program verification



In contrast to testing:

Program verification proves absence of bugs



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We focus on deductive program verification

Specification of properties in a formal logic language



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- Specification of properties in a formal logic language
- ► Use of semi-automated theorem proving to verify with mathematical rigour that the implementation adheres to its specification



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the implementation adheres to its specification

- Input:
  - Specification & Implementation
- Output:

Machine-checkable mathematical proof of correctness



In contrast to testing:

Program verification proves absence of bugs (\*)

We focus on deductive program verification

- Specification of properties in a formal logic language
- ▶ Use of semi-automated theorem proving to verify with mathematical rigour that

the implementation adheres to its specification

Input:

Specification & Implementation

Output:

Machine-checkable mathematical proof of correctness

(\*) under the assumption that compiler, virtual machine, operating system, hardware are correct and no interference by cosmic rays



JML is a specification language tailored to JAVA

## General JML Philosophy

#### Integrate

- specification
- implementation

in one single language

⇒ JML is not external to JAVA, but an extension of JAVA



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JML

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Java + First-Order Logic



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**JML** 

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JAVA + First-Order Logic + pre-/post-conditions, invariants



JML is a specification language tailored to JAVA

## General JML Philosophy

## Integrate

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⇒ JML is not external to JAVA, but an extension of JAVA

JML

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JAVA + First-Order Logic + pre-/post-conditions, invariants + more . . .

#### **JML Annotations**



#### JML extends JAVA by annotations

#### In this course ...

- Preconditions & postconditions
- Class invariants
- Additional modifiers
- Loop invariants
- Specification of interfaces, abstract classes & modular specification
  - "Specification-only" fields
  - "Specification-only" methods
  - Static & dynamic frames

## JML/JAVA integration



JML annotations are attached to JAVA programs by writing them directly into the JAVA source code files

Ensures compatibility with standard JAVA compiler:

JML annotations live in special JAVA comments, ignored by JAVA compiler, recognized by JML tools

#### JML embedded as JAVA Comments



 ${\tt Demo: HealthTracker\#addCategory}$ 

#### JML embedded as JAVA Comments



Demo: HealthTracker#addCategory

```
/*@ public normal_behavior
  @ requires p_category != null
  @ requires category != null
  @ requires nrCategories >= 0;
  @ requires nrCategories >= category.length - 1;;
  @ ensures \result == false;
  @*/
public boolean addCategory(Category p_category)
```

Everything between /\* and \*/ is invisible for JAVA compiler

#### JML embedded as JAVA Comments



#### JAVA comment lines starting with @ read and parsed by JML tools

```
/*@ public normal_behavior
  @ requires p_category != null; @ only to beautify
  @ requires category != null
  @ requires nrCategories >= 0;
  @ requires nrCategories >= category.length - 1;
  @*/
//@ ensures \result == false;
//_@ ensures \result == false; no JML: @ not first
public boolean addCategory(Category p_category)
```

## JML by Example: Public Modifier



```
/*@ public normal_behavior
  @ requires p_category != null;
  @ requires category != null
  @ requires nrCategories >= 0;
  @ requires nrCategories >= category.length - 1;
  @ ensures \result == false;
  @*/
public boolean addCategory(Category p_category)
```

#### This is a **public** specification case:

- 1. it is accessible from all classes and interfaces
- 2. it can only refer to public fields/methods of this class (can be problematic, come back to it later)

Visibility will become important later when discussing modular specification.

## JML by Example: Specification Cases



```
/*@ public normal behavior
  @ requires p_category != null;
  @ requires category != null
  @ requires nrCategories >= 0;
  @ requires nrCategories >= category.length - 1;
  @ ensures \result == false;
  @*/
public boolean addCategory(Category p_category)
```

Each keyword ending with **behavior** opens a specification case

## normal\_behavior Specification Case

The called method guarantees to terminate and to not throw an exception, if the caller guarantees all preconditions of this specification case

## JML by Example: Preconditions



```
/*@ public normal_behavior
  @ requires p_category != null;
  @ requires category != null
  @ requires nrCategories >= 0;
  @ requires nrCategories >= category.length - 1;
  @ ensures \result == false;
  @*/
public boolean addCategory(Category p_category)

Specification case has four preconditions (marked by requires)
```

## JML by Example: Preconditions



```
/*@ public normal_behavior
  @ requires p_category != null;
  @ requires category != null
  @ requires nrCategories >= 0;
  @ requires nrCategories >= category.length - 1;
  @ ensures \result == false;
  @*/
public boolean addCategory(Category p_category)
Specification case has four preconditions (marked by requires)
Here:
preconditions happen to be boolean JAVA expressions
In general:
preconditions are boolean JML expressions (including quantifiers)
```

#### JML by Example: Preconditions Cont'd

/\*@ public normal\_behavior

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@ requires p\_category != null;
@ requires category != null
@ requires nrCategories >= 0;



```
@ requires nrCategories >= category.length - 1;
@ ensures \result == false;
@*/

Both preconditions must be true in prestate

Equivalent to:
/*@ public normal_behavior
@ requires p_category != null && category != null &&
@ nrCategories >= 0 && nrCategories >= category.length - 1;
@ ensures \result == false;
@*/
```

## JML by Example: Postconditions



```
/*@ public normal_behavior
  @ requires p_category != null && ... && nrCategories >= 0;
  @ requires nrCategories >= category.length - 1;
  @ ensures \result == false;
  @*/
```

Specification case has one postcondition (marked by ensures)

- Postconditions speaks about the poststate
- Postconditions are boolean JML expressions
- If there is more than one ensures clause: postcondition is the conjunction of all clauses

## JML by Example: Accessing the Return Value



```
/*@ public normal_behavior
  @ requires p_category != null && ... && nrCategories >= 0;
  @ requires nrCategories >= category.length - 1;
  @ ensures \result == false;
  @*/
```

Special keyword \result to refer to the return value of a method. Only allowed in postconditions.

#### JML by Example: Multiple Specification Cases



#### Multiple specification cases connected by also

```
/*@ public normal behavior
 @ requires p_category != null && ... && nrCategories >= 0;
 @ requires nrCategories >= category.length - 1;
 @ ensures \result == false:
 0
 @ also
 @ public normal_behavior
 @ requires p_category != null && ... && nrCategories >= 0;
 @ requires nrCategories < category.length - 1:
 @ requires (\forall int i; i>=0 && i<nrCategories;
                                  p_category.id != category[i].id);
 @ ensures category[nrCategories - 1] == p_category;
   ensures nrCategories == \old(nrCategories + 1);
 @ ensures \result == true: @*/
public boolean addCategory(Category p_category)
```

#### JML by Example: Quantified Expressions



## Quantified JML Expressions (usage & more, see later)

- ► (\forall t x; a; b): "for all x of type t fulfilling a, b is true"
- (\exists t x; a; b): "there exists an x of type t fulfilling a, such that b is true"

#### JML by Example: Access of Prestate



```
/*@ public normal_behavior
@ requires p_category != null && ... && nrCategories >= 0 &&
@ nrCategories < category.length - 1;
@ requires (\forall int i; i>=0 && i<nrCategories;
@ p_category.id != category[i].id);
@ ensures category[nrCategories - 1] == p_category;
@ ensures nrCategories == \old(nrCategories + 1);
@ ensures \result == true;
@*/</pre>
```

## Access to value of prestate in postcondition

**\old(E)** means: E evaluated in the prestate (of addCategory(Category))

- ▶ \old(E) is a JML expression that is not a JAVA expression
- ► E can be any (arbitrarily complex) JAVA/JML expression

# **Specification Cases Complete?**



```
@ requires p_category != null && ... && nrCategories >= 0 &&
@ nrCategories < category.length - 1;
@ requires (\forall int i; i>=0 && i<nrCategories;
@ p_category.id != category[i].id);
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@ ensures nrCategories == \old(nrCategories + 1);
@ ensures \result == true;</pre>
```

# **Specification Cases Complete?**



```
@ requires p_category != null && ... && nrCategories >= 0 &&
@ nrCategories < category.length - 1;
@ requires (\forall int i; i>=0 && i<nrCategories;
@ p_category.id != category[i].id);
@ ensures category[nrCategories - 1] == p_category;
@ ensures nrCategories == \old(nrCategories + 1);
@ ensures \result == true;</pre>
```

What does the specification case not tell about poststate?

# **Specification Cases Complete?**



```
@ requires p_category != null && ... && nrCategories >= 0 &&
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@ requires (\forall int i; i>=0 && i<nrCategories;
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@ ensures category[nrCategories - 1] == p_category;
@ ensures nrCategories == \old(nrCategories + 1);
@ ensures \result == true;</pre>
```

What does the specification case not tell about poststate?

Fields of class HealthTracker:

```
username, category, nrCategories
```

What happens with username, category and category[j] (j<nrCategories - 1)?

## **Completing Specification Cases**



```
@ requires ...
@ ensures category[nrCategories - 1] == p_category;
@ ensures nrCategories == \old(nrCategories + 1) && \result == true;
@ ensures username == \old(username);
@ ensures category == \old(category);
@ ensures (\forall int j; j>=0 && j<category.length && j != nrCategories-1;
@ category[j] == \old(category[j]))</pre>
```

- Similar postconditions added for the other specification cases
- Assumption that environment is unchanged unless explicitly stated: usually called frame condition

## **Completing Specification Cases**



```
@ requires ...
@ ensures category[nrCategories - 1] == p_category;
@ ensures nrCategories == \old(nrCategories + 1) && \result == true;
@ ensures username == \old(username);
@ ensures category == \old(category);
@ ensures (\forall int j; j>=0 && j<category.length && j != nrCategories-1;
@ category[j] == \old(category[j]))</pre>
```

- ▶ Similar postconditions added for the other specification cases
- Assumption that environment is unchanged unless explicitly stated: usually called frame condition

Clearly unsatisfactory to add

```
@ ensures loc == \old(loc);
```

for all locations loc which do not change

#### **Assignable Locations**



More efficient to explicitly list all locations that may change:

```
@ assignable loc_1, \ldots, loc_n;
```

Assignable clause: value of no location besides  $loc_1, ..., loc_n$  can change (but could change temporarily during execution of method)

## **Assignable Locations**



More efficient to explicitly list all locations that may change:

```
@ assignable loc_1, \ldots, loc_n;
```

Assignable clause: value of no location besides  $loc_1, ..., loc_n$  can change (but could change temporarily during execution of method)

## Special cases of assignable clause

No location may be changed:

```
@ assignable \nothing;
```

Unrestricted, method allowed to change anything:

@ assignable \everything;

This is the default if no assignable clause is given



```
@ requires ...
@ ensures category[nrCategories - 1] == p_category;
@ ensures nrCategories == \old(nrCategories + 1);
@ ensures \result == true;
@ assignable nrCategories, category[nrCategories];
Expressions in assignable clause evaluated in pre-state.
```



ensures category[nrCategories - 1] == p\_category;

requires ...



```
requires ...
  ensures category[nrCategories - 1] == p_category;
 ensures nrCategories == \old(nrCategories + 1);
 ensures \result == true;
 assignable nrCategories, category[nrCategories];
Expressions in assignable clause evaluated in pre-state.
If a field of a different (i.e., not this) objectis changed (e.g., id of p_category)
                 @ assignable p_category.id;
Does
  @ assignable p_category;
make sense?
```

No! Parameters in Java are passed copy-by-value.



```
requires ...
 ensures category[nrCategories - 1] == p_category;
  ensures nrCategories == \old(nrCategories + 1);
 ensures \result == true;
 assignable nrCategories, category[nrCategories];
Expressions in assignable clause evaluated in pre-state.
If a field of a different (i.e., not this) objectis changed (e.g., id of p_category)
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#### **JML Modifiers**



#### JML extends the JAVA modifiers by additional modifiers

#### The most important ones are:

- ▶ spec\_public
- ▶ pure
- ► nullable (next lecture)
- non\_null (next lecture)
- ► helper (next lecture)

## JML Modifiers: spec\_public



In "addCategory" the specifications used class fields

But: public specifications can access only public fields

Not desired: make all fields mentioned in specification public

#### JML Modifiers: spec\_public



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# Control visibility with spec\_public

- Keep visibility of JAVA fields private/protected
- ▶ If necessary make them visible in specification only by spec\_public

#### JML Modifiers: spec\_public



In "addCategory" the specifications used class fields

But: public specifications can access only public fields

Not desired: make all fields mentioned in specification public

## Control visibility with spec\_public

- Keep visibility of JAVA fields private/protected
- ▶ If necessary make them visible in specification only by spec\_public

```
private /*@ spec_public @*/ Category[] category;
private /*@ spec_public @*/ int nrCategories;
```

(different solution(see lecture in 4-5 weeks): use specification-only fields )

## JML Modifiers: Notions of Purity — pure



Specifications more concise with method calls inside JML annotations:

Examples: o1.equals(o2) li.contains(elem) li1.max() < li2.min()</pre>

Specifications may not themselves change the state!

#### Definition (Pure method)

A JAVA method is called pure iff it has no visible side effects and it always terminates.

A method is strictly pure if it must not create new objects, otherwise weakly pure.

#### JML Modifiers: Notions of Purity — pure



Specifications more concise with method calls inside JML annotations:

```
Examples: o1.equals(o2) li.contains(elem) li1.max() < li2.min()</pre>
```

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#### Definition (Pure method)

A JAVA method is called pure iff it has no visible side effects and it always terminates.

A method is strictly pure if it must not create new objects, otherwise weakly pure.

JML expressions may call pure methods. These are annotated by **pure** (weakly pure) or **strictly\_pure** resp.

```
public /*@ pure @*/ int max() { ... }
```

## JML Modifiers: pure Cont'd



#### How do we know that a pure method is really pure?

- pure puts obligation on implementor not to cause side effects
- It is possible to formally verify that a method is pure
  - Write a contract that expresses purity and verify it
- pure implies assignable \nothing; (may create new objects)
- assignable \strictly\_nothing; expresses that no new objects are created
- Assignable clauses can be local to a specification case while pure fixes behavior of a method

#### **JML Expressions**



#### Definition (JML Expressions)

- ► Each side-effect free JAVA expression is a JML expression
- ▶ If E is a side-effect free JAVA expression, then \old(E) is a JML expression
- If a and b are boolean JML expressions, x is a variable of type t:

```
▶ !a ("not a"), a && b ("a and b"), a || b ("a or b")
```

- ▶ a ==> b ("a implies b")
- a <==> b ("a is equivalent to b")
- ► (\forall t x; a) ("for all x of type t, a is true")
- ► (\exists t x; a) ("there exists x of type t such that a")
- ► (\forall t x; a; b) ("for all x of type t fulfilling a, b is true")
- ► (\exists t x; a; b) ("there exists an x of type t fulfilling a,

such that b is true")

are also boolean JML expressions.

## **Range Predicates**



## Definition (Range predicate)

```
In the JML expressions (forall\ t\ x;\ a;\ b) and (exists\ t\ x;\ a;\ b) the boolean a is called range predicate.
```

Range predicates are syntactic sugar for standard FOL quantifiers:

```
(\forall t x; a; b)
    equivalent to
(\forall t x; a ==> b)

(\exists t x; a; b)
    equivalent to
(\exists t x; a && b)
```

# **Pragmatics of Range Predicates**



Range predicates used to restrict range of x further than to its type t

## Example

"Array a is sorted between indices 0 and 9":

```
(\forall int i,j; 0<=i && i<j && j<10; a[i] <= a[j])
```

## **Using Quantified JML Expressions**



► An array int a contains only non-negative elements

JML -

# **Using Quantified JML Expressions**



► An array int a contains only non-negative elements

\_\_\_\_\_JML\_\_\_\_\_\_\_(\forall int i; 0 <= i && i < a.length; a[i] >= 0)

—— JML —

► The variable m holds a maximal element of array a

— JML —

(\forall int i;  $0 \le i \&\& i \le a.length; m >= a[i]$ )

JML —

# **Using Quantified JML Expressions**



► An array int a contains only non-negative elements

— .IMI

(\forall int i; 0 <= i && i < a.length; a[i] >= 0)

——— JML —

▶ The variable m holds a maximal element of array a

— JMI —

(\forall int i; 0 <= i && i < a.length; m >= a[i])

– JML ——

Is this sufficient? Need in addition:

\_\_\_.IMI \_\_\_\_

(\exists int i; 0 <= i && i < a.length; m == a[i])

· JML —

#### Literature for this Lecture



## Reading

KeY Book Andreas Roth & Peter H. Schmitt: Formal Specification.
Chapter 5, Sections 5.1, 5.3, In: B. Beckert, R. Hähnle, and P. Schmitt, eds. Verification of Object-Oriented Software: The KeY Approach, vol 4334 of LNCS. Springer, 2006.

At http://link.springer.com/book/10.1007/978-3-540-69061-0

JML Reference Manual G. T. Leavens et. al, JML Reference Manual

JML Tutorial G. T. Leavens, Y. Cheon. Design by Contract with JML

JML Overview G. T. Leavens, A. L. Baker, and C. Ruby. JML: A Notation for Detailed Design

At www.jmplspecs.org