

# Features for Large-Scale Visual Recognition

Florent Perronnin

Xerox Research Centre Europe

CVPR tutorial: Large-Scale Visual Recognition (LSVR)

June 23, 2013

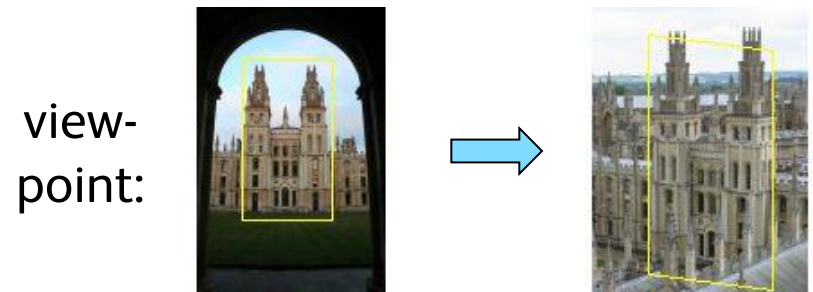
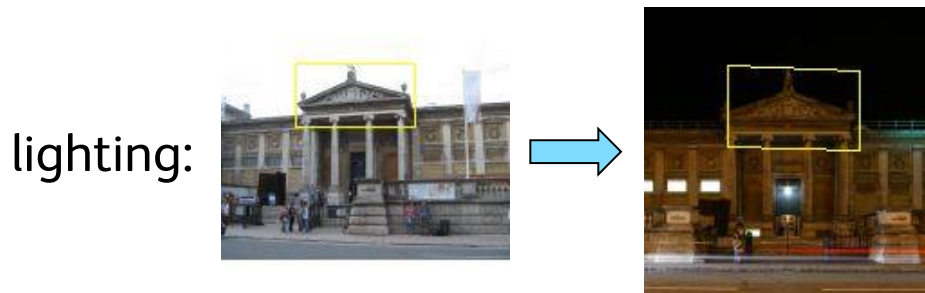
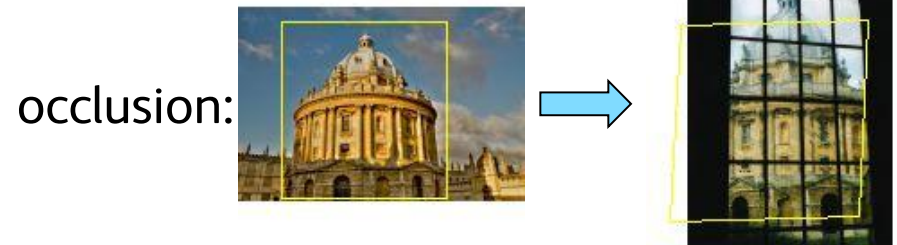
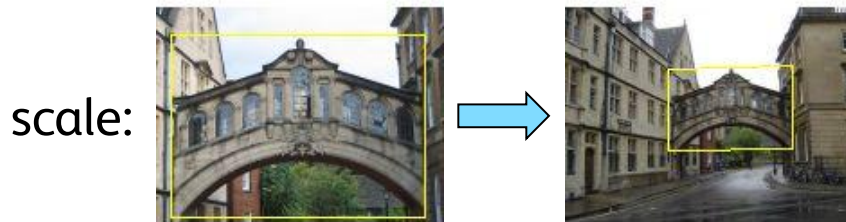
# Image description

Goal: convert an image into a mathematical representation such that

- “similar” images have similar representations
- “dissimilar” images have dissimilar representations

Difficulty: robustness to viewpoint, lighting, occlusion, intra-class variability, etc.

→ need **invariant representation**



## Image description

Goal: convert an image into a mathematical representation such that

- “similar” images have similar representations
- “dissimilar” images have dissimilar representations

But the representation should be **informative** enough:



# Image description

Goal: convert an image into a mathematical representation such that

- “similar” images have similar representations
- “dissimilar” images have dissimilar representations

And it should be **efficient**:

- to compute
- to store in RAM / on disk, to transfer, etc.
- to process: e.g. fast comparison between images or between image and class model

# Image description

Goal: convert an image into a mathematical representation such that

- “similar” images have similar representations
- “dissimilar” images have dissimilar representations

Trade-off between three conflicting requirements:

- robust to variations: scale, occlusion, lighting, etc.
- informative
- efficient: to compute, store, process

**→ trade-off is application-dependent**

# Image description

Caveat: **there is no clear cut between description and learning!**

Better description can lead to simpler learning:

→ see [A. Vedaldi's part on explicit feature maps](#)

Features and classifiers learned jointly

→ see [M'A Ranzato's part on large-scale deep learning](#)

In this part: focus on features which are obtained through the **aggregation/pooling** of local **codes/statistics**

# Outline

Global vs local descriptors

The bag-of-visual-words

Higher-order representations

Examples

Conclusion

# Outline

## **Global vs local descriptors**

The bag-of-visual-words

Higher-order representations

Examples

Conclusion



# Global descriptors (of pixel statistics)

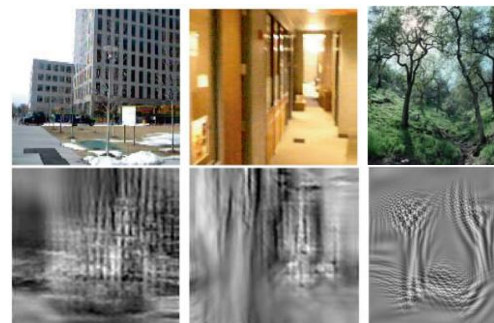
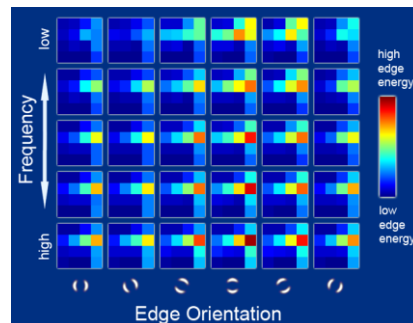
Color Histogram: high invariance but limited discriminative power

Swain, Ballard, “Color indexing”, IJCV’91.

## GIST of a scene:

Oliva, Torralba, “Modeling the shape of the scene: a holistic representation of the spatial envelope”, IJCV’01.

Douze, Jegou, Sandhawalia, Amsaleg, Schmid, “Evaluation of GIST descriptors for web-scale image search”, CIVR’09.



## CENTRIST: CENsus Transform hISTogram

Wu, Rehg, “CENTRIST: a visual descriptor for scene categorization”, TPAMI’11.

Highly efficient to compute and to match → **perfect for LSVR**

But **robustness vs informativeness tradeoff** is hard to set

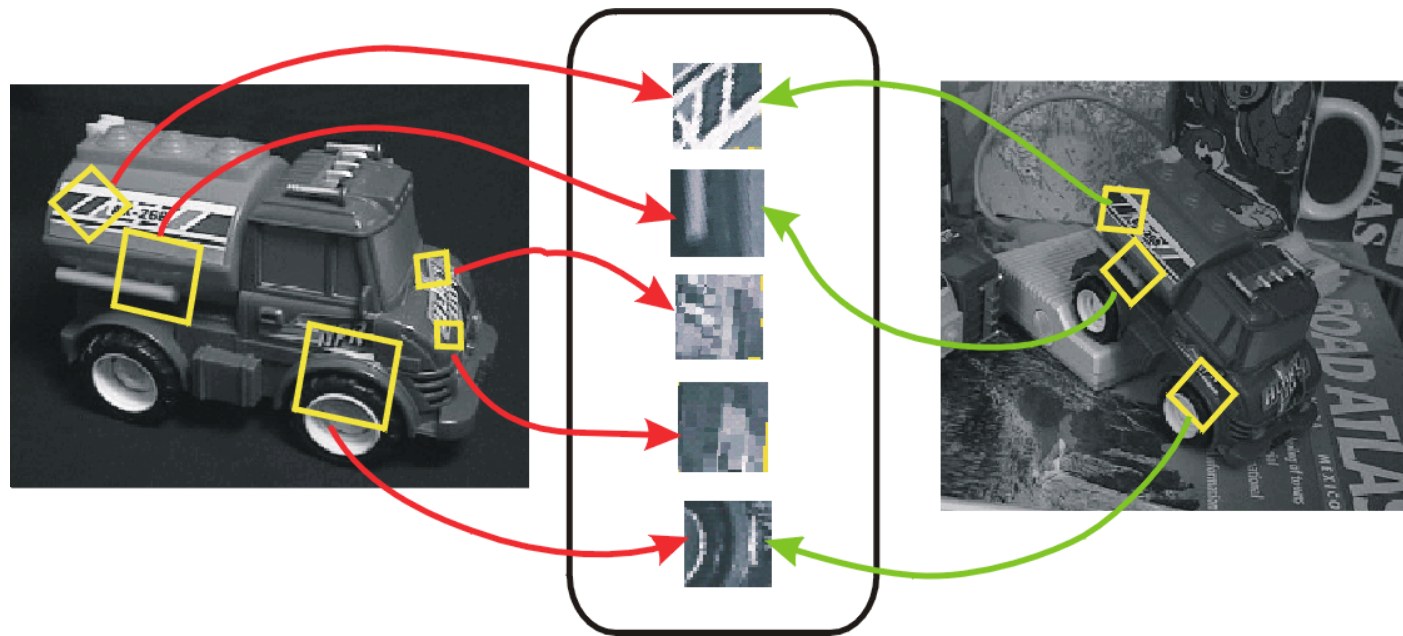
# Local representations

Image content is transformed into a set of invariant descriptors (to photometric/geometric transformations) extracted from small image patches

Very intuitive in retrieval / matching context:

Schmid, Mohr, “Local greyvalue invariants for image retrieval”, TPAMI’97.

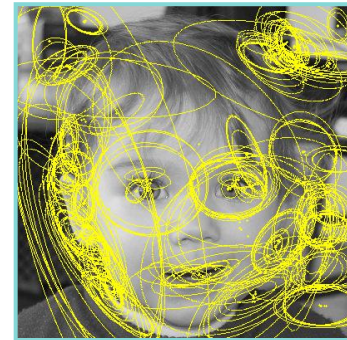
Lowe, “Distinctive image features from scale-invariant keypoints”, IJCV’04.



# Local representations: detectors

## Roles of the detector:

- provide invariance to transformations
- **reduce the number of descriptors**



## Popular detectors:

- **Maximally Stable Extremal Regions (MSER)**  
Matas, Chum, Urban, Pajdla, “Robust wide-baseline stereo from maximally stable extremal regions”, BMVC’02.
- **Difference of Gaussians (DoG)**  
Lowe, “Distinctive image features from scale-invariant keypoints”, IJCV’04.
- **Harris-Affine and Hessian-Affine**  
Mikolajczyk, Schmid, “Scale and affine invariant interest point detectors”, IJCV’04.  
→ See also Mikolajczyk et al., “A comparison of affine region detectors”, IJCV’05.

## Dense descriptors are also possible

- **Mainly for classification** → let the classifier decide  
Leung, Malik, “Representing and recognizing the visual appearance of materials using 3D textons”, IJCV’01.
- **But also for image/scene/object retrieval**  
Gordo, Rodriguez, Perronnin, Valveny, “Leveraging category-level labels for instance-level image retrieval”, CVPR’12.

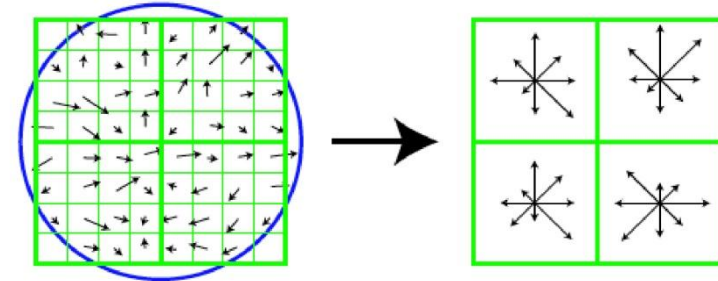
# Local representations: descriptors

Description of a patch after orientation/scale/photometric normalization

## Most widely-used patch descriptor: SIFT

Lowe, “Distinctive image features from scale-invariant keypoints”, IJCV’04.

- 8 orientations of the gradient → 128 dimensions
- 4x4 spatial grid



Many descriptors derive from SIFT:

- **More efficient: SURF**

Bay, Tuytelaars, Van Gool, “SURF: speeded up robust features”, ECCV’06.

- **More compact: CHOG, DAISY**

Chandrasekhar et al, “Compressed histograms of gradients: a low-bit rate descriptor”, IJCV’11.

Tola, Lepetit, Fua, “DAISY: an efficient dense descriptor applied to wide baseline stereo”, TPAMI’10.

- **With color: color SIFT**

Van de Weijer, Schmid, “Coloring local feature extraction”, ECCV’06.

Burghouts and Geseborek, “Performance evaluation of local colour invariants”, CVIU’09.

# Outline

Global vs local descriptors

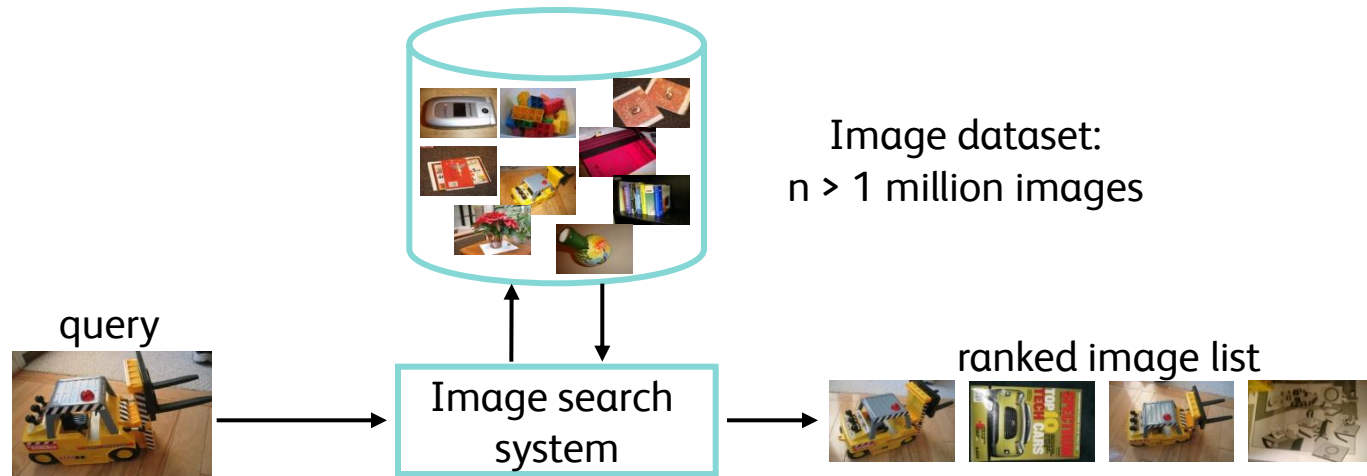
**The bag-of-visual-words**

Higher-order representations

Examples

Conclusion

# Direct matching: a retrieval example



Assume an image described by  $m=1000$  descriptors (dimension  $d=128$ )

- $n*m=1$  billion descriptors to index

Database representation in RAM: 128 GB with 1 byte per dimension

Search:  $m^2 \times n \times d$  elementary operations

- $10^{14} \rightarrow$  **computationally intractable**
- The quadratic term  $m^2$ : severely impacts the efficiency

# The bag-of-visual-words (BOV)

Concurrently introduced in image search and classification:

- in image search: “Video Google”

Sivic, Zisserman, “Video Google: A Text Retrieval Approach to Object Matching in Videos”, ICCV’03.

- in image classification:

Csurka, Dance, Fan, Willamowski, Bray, “Visual categorization with bag of keypoints”, ECCV SLCV’04.

See also: Zhang, Marszalek, Lazebnik, Schmid, “Local features and kernels for classification of textures and object categories: a comprehensive study”, IJCV’07.

Key idea: **aggregate**  $n$  local descriptors into 1 vector

- inherits invariance of the local descriptors
- (possibly) sparse vector → efficient comparison

# The bag-of-visual-words (BOV)

The goal: “put the images into words”, namely **visual words**

- input local descriptors are continuous
- need to define what a visual word is
- done by a **quantizer**:  $q: \mathbb{R}^d \rightarrow \omega$   
 $x \rightarrow c(x) \in \omega$
- $q$  is typically a k-means

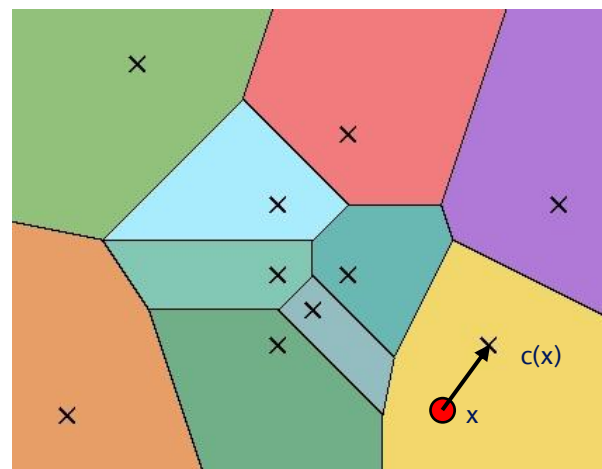
$\omega$  is called a **visual dictionary**

- A local descriptor is assigned to its nearest neighbor

$$q(x) = \arg \min_{w \in \omega} \|x - w\|^2$$

$$w \in \omega$$

- Quantization is lossy: we cannot get back to the original descriptor
- But much more compact (few bytes per descriptor)





# BOV and retrieval

## Video Google system

### Extract local descriptors

- Detector
- Describe the patch

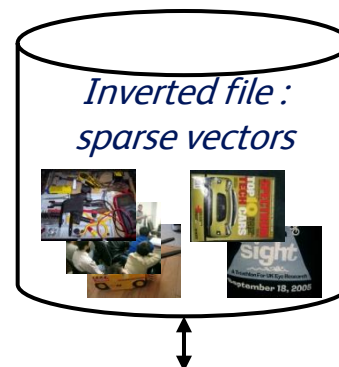
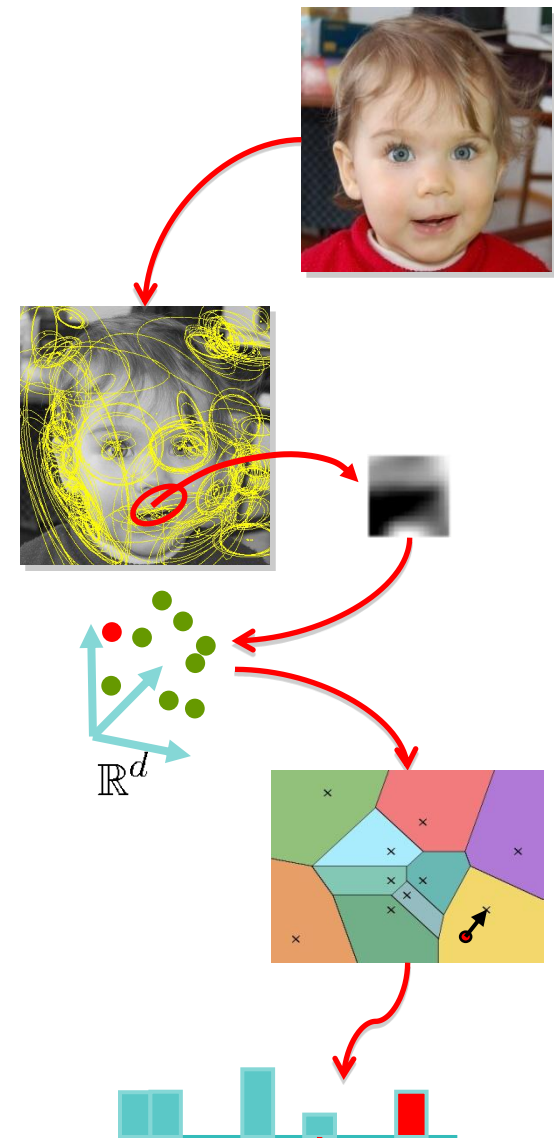
### Quantize all descriptors

- Subsequently compute the vector of frequencies
- Weight by IDF (rare is more important) → TF-IDF vectors

### Search similar vectors

### Optionally: re-ranking

→ see O. Chum's part on  
large-scale geometry



# BOV and retrieval

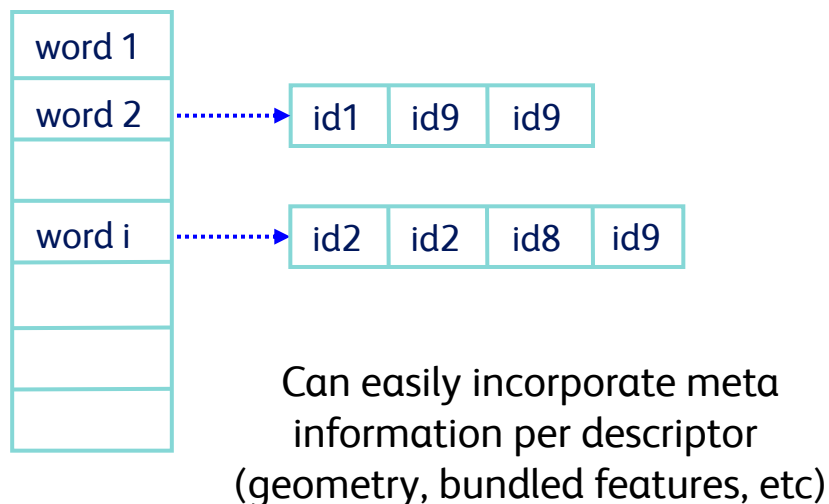
## Efficiency through inverted files

Set of lists that store the **sparse vector components**

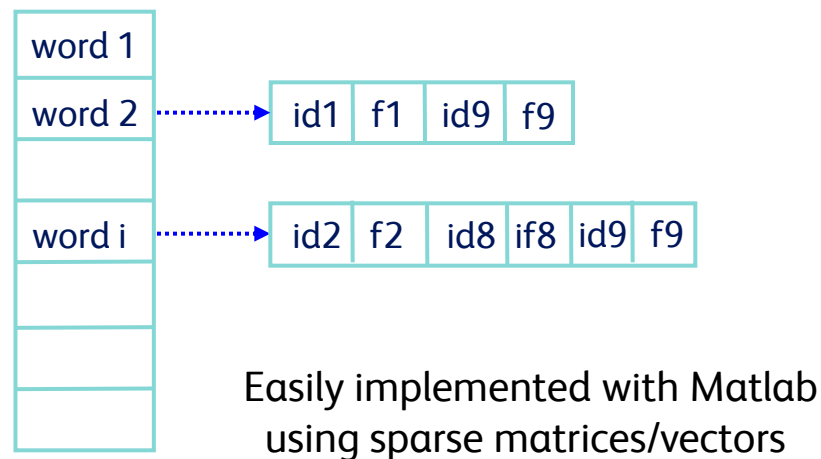
→ useful if  $\# \text{ descriptors} \ll \# \text{ visual words (retrieval)}$

Two implementations:

- store one image id per descriptor:



- store image id+nb of descriptors:



→ **histogram representation**

# BOV and classification

## Coding and pooling

### Coding: how to go beyond VQ + hard coding?

- **soft coding, e.g. using a mixture model or a “kernel” codebook**  
Winn, Criminisi, Minka, “Object categorization by learned universal visual dictionary”, ICCV’05.  
Perronnin, Dance, Csurka, Bressan, “Adapted vocabularies for generic visual categorization”, ECCV’06.  
van Gemert, Geusebroek, Veenman, Smeulders, “Kernel codebooks for scene categorization”, ECCV’08.
- **sparse coding**  
Yang, Yu, Gong, Huang, “Linear spatial pyramid matching using sparse coding for image classification”, CVPR’09.  
Wang, Yang, Yu, Lv, Huang, Gong, “Locality-constrained linear coding for image classification”, CVPR’10.  
Boureau, Bach, LeCun, Ponce, “Learning mid-level features for reognition”, CVPR’10.

### Pooling / aggregation:

- **average pooling**  
Csurka, Dance, Fan, Willamowski, Bray, “Visual categorization with bag of keypoints”, ECCV SLCV’04.
- **max pooling**  
Yang, Yu, Gong, Huang, “Linear spatial pyramid matching using sparse coding for image classification”, CVPR’09.  
Boureau, Ponce, LeCun, “A theoretical analysis of feature pooling in vision algorithms”, ICML’10.
- **Lp pooling**  
Boureau, Ponce, LeCun, “A theoretical analysis of feature pooling in vision algorithms”, ICML’10.

# BOV and classification

## Choice of classifier

BOV histograms are generally used together with **kernel classifiers**

### Linear kernel classifiers:

- fast to learn and evaluate  
→ [see Z. Harchaoui's part on large-scale learning](#)
- perform poorly on the BOV (at least with average pooling)

### Non-linear kernel classifiers:

- perform well on the BOV (chi2 or intersection kernel)
- direct approach leads to slow learning and evaluation  
→ [see A. Vedaldi's part on explicit feature maps](#)

# Visual vocabulary size

For LSVR, we need image signatures which contain **fine-grained information**:

- in retrieval: the larger the dataset size, the higher the probability to find another similar but irrelevant image to a given query
- in classification: the larger the number of other classes, the higher the probability to find a class which is similar to any given class

BOV answer to the problem: increase visual vocabulary size

- practical problem: assignment of descriptors to visual words becomes costly  
→ [see H. Jégou's part on efficient matching](#)

How to increase amount of information  
**without increasing the visual vocabulary size?**

→ higher-order representations

# Outline

Global vs local descriptors

The bag-of-visual-words

**Higher-order representations**

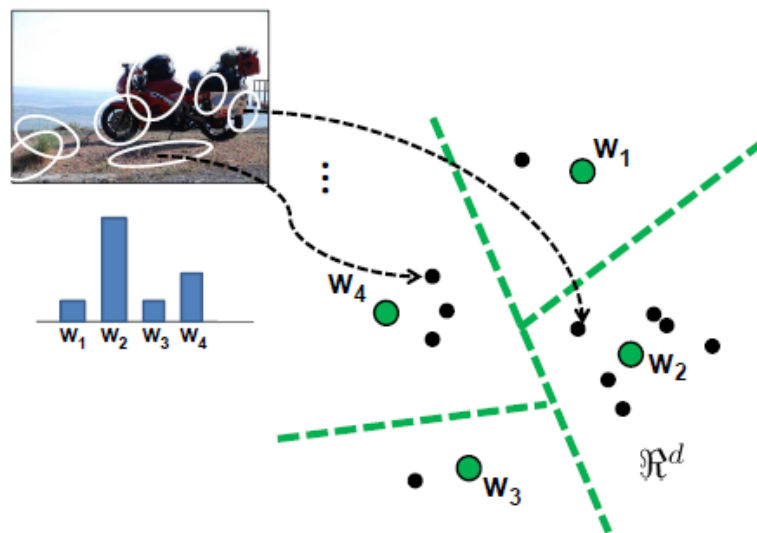
Examples

Conclusion

# Motivation

BOV is only about **counting** the number of local descriptors assigned to each Voronoi region

Why not including **other statistics**?



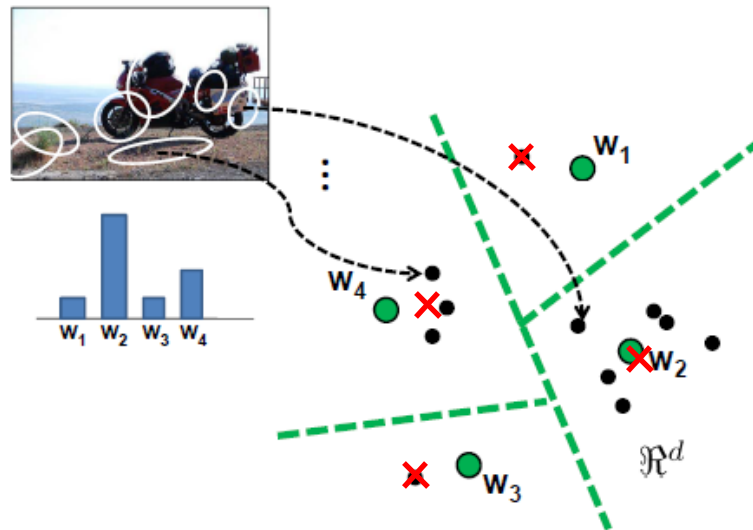
[http://www.cs.utexas.edu/~grauman/courses/fall2009/papers/bag\\_of\\_visual\\_words.pdf](http://www.cs.utexas.edu/~grauman/courses/fall2009/papers/bag_of_visual_words.pdf)

# Motivation

BOV is only about **counting** the number of local descriptors assigned to each Voronoi region

Why not including **other statistics**? For instance:

- mean of local descriptors ✗



[http://www.cs.utexas.edu/~grauman/courses/fall2009/papers/bag\\_of\\_visual\\_words.pdf](http://www.cs.utexas.edu/~grauman/courses/fall2009/papers/bag_of_visual_words.pdf)

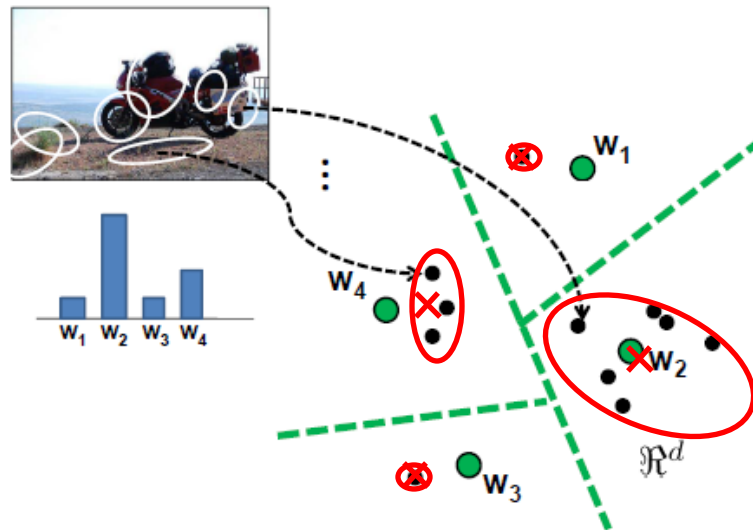


# Motivation

BOV is only about **counting** the number of local descriptors assigned to each Voronoi region

Why not including **other statistics**? For instance:

- mean of local descriptors ✗
- (co)variance of local descriptors ○



[http://www.cs.utexas.edu/~grauman/courses/fall2009/papers/bag\\_of\\_visual\\_words.pdf](http://www.cs.utexas.edu/~grauman/courses/fall2009/papers/bag_of_visual_words.pdf)

# Motivation

BOV is only about **counting** the number of local descriptors assigned to each Voronoi region

Why not including **other statistics**? For instance:

- mean of local descriptors
- (co)variance of local descriptors

Model the approximate distribution of samples in each cell

→ **aggregate higher order statistics**

# The Vector of Locally Aggregated Descriptors (VLAD)

Given a codebook  $\{\mu_i, i = 1 \dots N\}$ ,  
e.g. learned with K-means, and a set of  
local descriptors  $X = \{x_t, t = 1 \dots T\}$ :

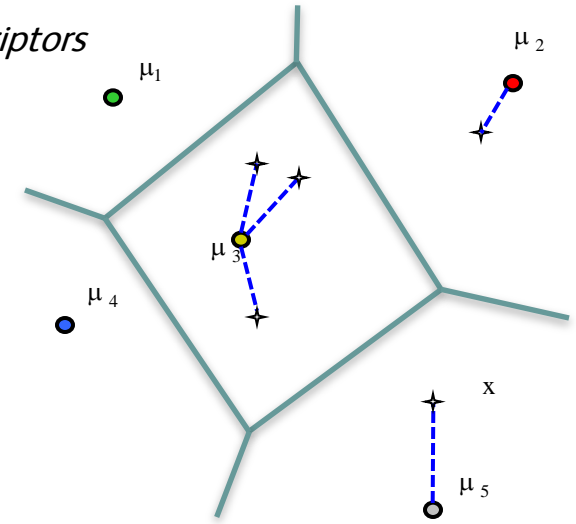
- ① assign:  $\text{NN}(x_t) = \arg \min_{\mu_i} \|x_t - \mu_i\|$

- ②③ compute:  $v_i = \sum_{x_t: \text{NN}(x_t) = \mu_i} x_t - \mu_i$

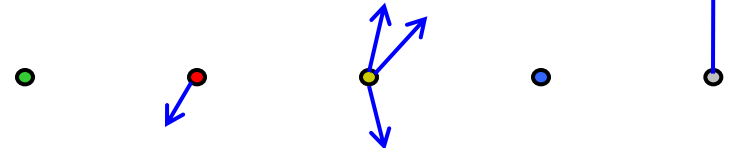
- concatenate  $v_i$ 's +  $\ell_2$  normalize

→ the VLAD is  $D \times N$  dimensional

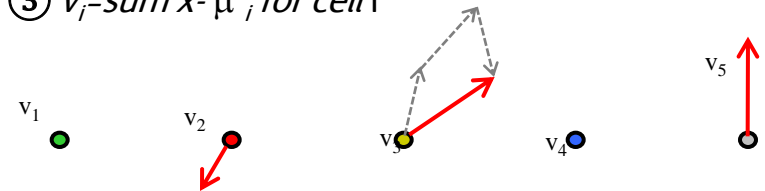
① assign descriptors



② compute  $x - \mu_i$



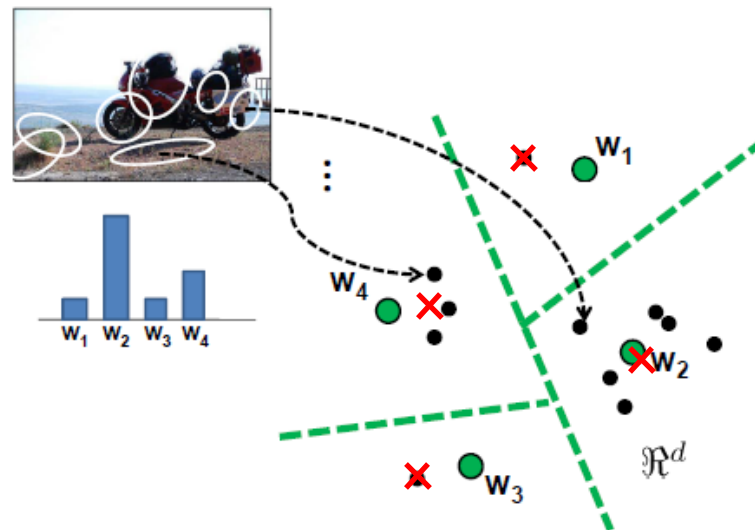
③  $v_i = \text{sum } x - \mu_i \text{ for cell } i$



Jégou, Douze, Schmid and Pérez, "Aggregating local descriptors into a compact image representation", CVPR'10.

# The Vector of Locally Aggregated Descriptors (VLAD)

The distribution of samples in each cell is encoded by its mean (minus the centroid mean)



[http://www.cs.utexas.edu/~grauman/courses/fall2009/papers/bag\\_of\\_visual\\_words.pdf](http://www.cs.utexas.edu/~grauman/courses/fall2009/papers/bag_of_visual_words.pdf)

→ The VLAD is a special case of a more general descriptor: the Fisher Vector

# The Fisher Vector (FV)

## Score function

Given a likelihood function  $u_\lambda$  with parameters  $\lambda$ , the **score function** of a given sample  $X$  is given by:

$$G_\lambda^X = \nabla_\lambda \log u_\lambda(X)$$

→ Fixed-length vector whose **dimensionality depends only on # parameters**.

Intuition: direction in which the parameters  $\lambda$  of the model should be modified to better fit the data.

# The Fisher Vector (FV)

## Fisher Kernel

**Fisher information matrix (FIM)** or negative Hessian:

$$F_{\lambda} = E_{x \sim u_{\lambda}} [\nabla_{\lambda} \log u_{\lambda}(x) \nabla_{\lambda} \log u_{\lambda}(x)']$$

Measure similarity between gradient vectors using the **Fisher Kernel (FK)**:

$$K(X, Y) = G_{\lambda}^{X'} F_{\lambda}^{-1} G_{\lambda}^Y$$

Jaakkola and Haussler, “Exploiting generative models in discriminative classifiers”, NIPS’98.

→ can be interpreted as a score whitening

As the FIM, is PSD, it can be decomposed as:  $F_{\lambda}^{-1} = L'_{\lambda} L_{\lambda}$

and the FK can be rewritten as a dot product between **Fisher Vectors (FV)**:

$$\mathcal{G}_{\lambda}^X = L_{\lambda} G_{\lambda}^X$$

# The Fisher Vector (FV)

## Application to images

$X = \{x_t, t = 1 \dots T\}$  is the set of  $T$  i.i.d.  $D$ -dim local descriptors (e.g. SIFT) extracted from an image:

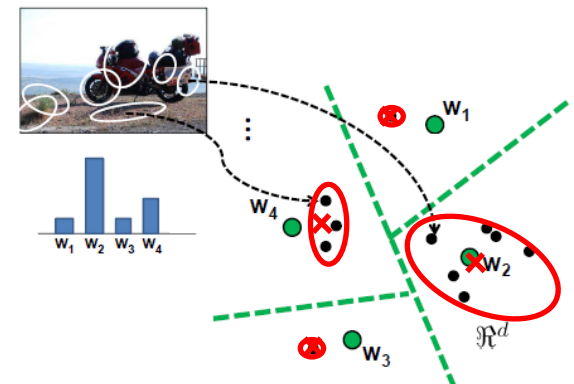
$$G_{\lambda}^X = \frac{1}{T} \sum_{t=1}^T \nabla_{\lambda} \log u_{\lambda}(x_t)$$

$u_{\lambda}(x) = \sum_{i=1}^K w_i u_i(x)$  is a Gaussian Mixture Model (GMM) with parameters  $\lambda = \{w_i, \mu_i, \Sigma_i, i = 1 \dots N\}$

The FV is typically  $2 \times D \times N$  dimensional

With respect to the VLAD:

- add 2nd order moments
- soft-assignment of local descriptors
- per-dimension whitening



Perronnin and Dance, “Fisher kernels on visual categories for image categorization”, CVPR’07.

# The Fisher Vector (FV)

## Practical considerations

PCA on the local descriptors is necessary:

- because of the GMM diagonal approximation

$\ell_2$  -normalization:

- to make the FV more compliant with the dot-product assumption

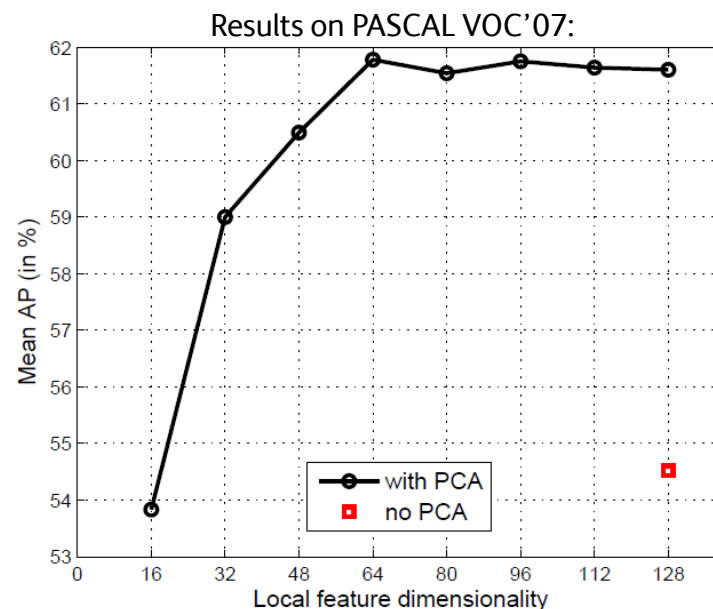
Power-normalization:

$$f(z) = \text{sign}(z)|z|^\alpha \text{ with } 0 \leq \alpha \leq 1$$

- to correct the patch independence assumption

Cinbis, Verbeek, Schmid, “Image categorization using Fisher kernels of non-iid image models”, CVPR’12.

→ For a detailed analysis see: Sánchez, Perronnin, Mensink, Verbeek, “Image Classification with the Fisher Vector: Theory and Practice”, IJCV’13.





# Embedding view of the BOV and FV

BOV:  $\varphi_{BOV}(x_t) = [0, \dots, 0, 1, 0, \dots, 0]$

$$\text{FV: } \varphi_{FV}(x_t) = \left[ 0, \dots, 0, \overbrace{\frac{1}{\sqrt{w_i}} \left( \frac{x_t - \mu_i}{\sigma_i} \right), \frac{1}{\sqrt{2w_i}} \left( \frac{(x_t - \mu_i)^2}{\sigma_i^2} - 1 \right)}^{2D \text{ non-zero dim}}, 0, \dots, 0 \right]$$

A linear classifier on these representations induces in the descriptor space:

Csurka and Perronnin, "An efficient approach to semantic segmentation", IJCV '10.

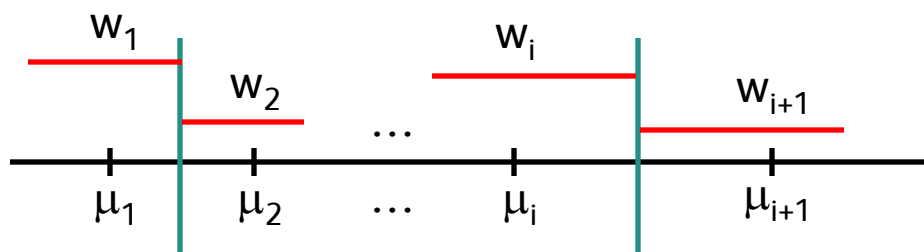
# Embedding view of the BOV and FV

BOV:  $\varphi_{BOV}(x_t) = [0, \dots, 0, 1, 0, \dots, 0]$

$$\text{FV: } \varphi_{FV}(x_t) = \left[ 0, \dots, 0, \overbrace{\frac{1}{\sqrt{w_i}} \left( \frac{x_t - \mu_i}{\sigma_i} \right), \frac{1}{\sqrt{2w_i}} \left( \frac{(x_t - \mu_i)^2}{\sigma_i^2} - 1 \right)}^{2D \text{ non-zero dim}}, 0, \dots, 0 \right]$$

A linear classifier on these representations induces in the descriptor space:

- in the BOV case: a piece-wise constant decision function



Csurka and Perronnin, "An efficient approach to semantic segmentation", IJCV '10.

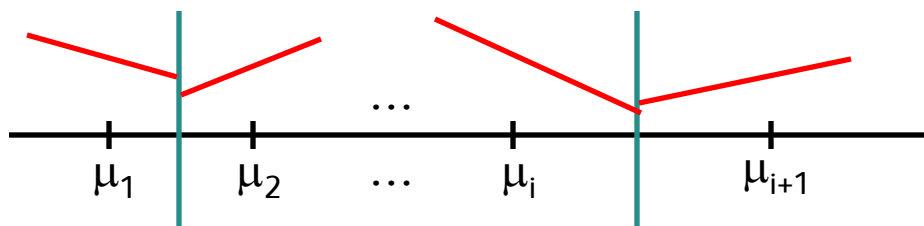
# Embedding view of the BOV and FV

BOV:  $\varphi_{BOV}(x_t) = [0, \dots, 0, 1, 0, \dots, 0]$

$$\text{FV: } \varphi_{FV}(x_t) = \left[ 0, \dots, 0, \overbrace{\frac{1}{\sqrt{w_i}} \left( \frac{x_t - \mu_i}{\sigma_i} \right), \frac{1}{\sqrt{2w_i}} \left( \frac{(x_t - \mu_i)^2}{\sigma_i^2} - 1 \right)}^{2D \text{ non-zero dim}}, 0, \dots, 0 \right]$$

A linear classifier on these representations induces in the descriptor space:

- in the BOV case: a piece-wise constant decision function
- in the FV case: a piecewise linear / quadratic decision function



Csurka and Perronnin, "An efficient approach to semantic segmentation", IJCV '10.

# Embedding view of the BOV and FV

BOV:  $\varphi_{BOV}(x_t) = [0, \dots, 0, 1, 0, \dots, 0]$

$$\text{FV: } \varphi_{FV}(x_t) = \left[ 0, \dots, 0, \overbrace{\frac{1}{\sqrt{w_i}} \left( \frac{x_t - \mu_i}{\sigma_i} \right), \frac{1}{\sqrt{2w_i}} \left( \frac{(x_t - \mu_i)^2}{\sigma_i^2} - 1 \right)}^{2D \text{ non-zero dim}}, 0, \dots, 0 \right]$$

A linear classifier on these representations induces in the descriptor space:

- in the BOV case: a piece-wise constant decision function
- in the FV case: a piecewise linear / quadratic decision function

→ **FV leads to more complex decision functions for same vocabulary size**

Csurka and Perronnin, "An efficient approach to semantic segmentation", IJCV '10.

# Super-Vector (SV) coding

Given a codebook  $\{\mu_i, i = 1 \dots N\}$  and a patch  $x_t$  we have:

$$f(x_t) \approx f(\mu_i) + \nabla f(\mu_i)'(x_t - \mu_i) = w' \varphi_{SV}(x_t)$$

with  $\varphi_{SV}(x_t) = \begin{bmatrix} \text{\scriptsize $(D+1)$ non-zero dim} \\ 0, \dots, 0, \overbrace{s, (x_t - \mu_i)}^{\text{\scriptsize $(D+1)$ non-zero dim}}, 0, \dots, 0 \end{bmatrix}$

and  $w = \begin{bmatrix} 0, \dots, 0, \frac{f(\mu_i)}{s}, \nabla f(\mu_i), 0, \dots, 0 \end{bmatrix}$  (to be learned)

Zhou, Yu, Zhang and Huang, "Image classification using super-vector coding of local image descriptors", ECCV'10.

# Super-Vector (SV) coding

Given a codebook  $\{\mu_i, i = 1 \dots N\}$  and a patch  $x_t$  we have:

$$f(x_t) \approx f(\mu_i) + \nabla f(\mu_i)'(x_t - \mu_i) = w' \varphi_{SV}(x_t)$$

with 
$$\varphi_{SV}(x_t) = \begin{bmatrix} \text{\scriptsize $(D+1)$ non-zero dim} \\ 0, \dots, 0, \quad \overbrace{s, (x_t - \mu_i)}^{\text{\scriptsize $(D+1)$ non-zero dim}}, 0, \dots, 0 \end{bmatrix}$$

average pooling  $\rightarrow$  **SV  $\approx$  BOV + VLAD**

Zhou, Yu, Zhang and Huang, "Image classification using super-vector coding of local image descriptors", ECCV'10.

# Super-Vector (SV) coding

Given a codebook  $\{\mu_i, i = 1 \dots N\}$  and a patch  $x_t$  we have:

$$f(x_t) \approx f(\mu_i) + \nabla f(\mu_i)'(x_t - \mu_i) = w' \varphi_{SV}(x_t)$$

with  $\varphi_{SV}(x_t) = \begin{bmatrix} \text{\scriptsize $(D+1)$ non-zero dim} \\ 0, \dots, 0, \overbrace{s, (x_t - \mu_i)}^{\text{\scriptsize $(D+1)$ non-zero dim}}, 0, \dots, 0 \end{bmatrix}$

average pooling  $\rightarrow$  **SV  $\approx$  BOV + VLAD**

$f : \mathbb{R}^D \rightarrow \mathbb{R}$  is Lipschitz smooth if  $\forall (x, y) \in \mathbb{R}^D \times \mathbb{R}^D :$

$$|f(x) - f(y) - \nabla f(y)'(x - y)| \leq \frac{\beta}{2} \|x - y\|^2$$

$\rightarrow$  bound in Lipschitz smooth inequality provides argument for k-means.

Zhou, Yu, Zhang and Huang, "Image classification using super-vector coding of local image descriptors", ECCV'10.

# Memory issue

Higher-order representations are typically:

- high-dimensional → few 100Ks of dims
- dense → on the order of 50 % sparsity for the FV

→ storing a dataset such as ImageNet can take tens of TBs

**Solution: compression**, e.g. with Product Quantization (PQ)

Jégou, Perronnin, Douze, Sánchez, Pérez and Schmid, “Aggregating local descriptors into compact codes”, TPAMI’11.

Sánchez and Perronnin, “High-dimensional signature compression for large-scale image classification”, CVPR’11.

→ see H. Jégou’s part on efficient matching

→ see also A. Vedaldi’s part on how to combine compression and learning



# Outline

Global vs local descriptors

The bag-of-visual-words

Higher-order representations

**Examples**

Conclusion

# Examples

## Retrieval

### Example on Holidays:

From: Jégou, Perronnin, Douze, Sánchez, Pérez and Schmid, “Aggregating local descriptors into compact codes”, TPAMI’11.

| Descriptor       | $K$    | $D$    | Holidays (mAP) |                       |                      |                      |                     |                     |
|------------------|--------|--------|----------------|-----------------------|----------------------|----------------------|---------------------|---------------------|
|                  |        |        | $D' = D$       | $\rightarrow D'=2048$ | $\rightarrow D'=512$ | $\rightarrow D'=128$ | $\rightarrow D'=64$ | $\rightarrow D'=32$ |
| BOW              | 1 000  | 1 000  | 40.1           |                       | 43.5                 | 44.4                 | 43.4                | 40.8                |
|                  | 20 000 | 20 000 | 43.7           | 41.8                  | 44.9                 | 45.2                 | 44.4                | 41.8                |
| Fisher ( $\mu$ ) | 16     | 1 024  | 54.0           |                       | 54.6                 | 52.3                 | 49.9                | 46.6                |
|                  | 64     | 4 096  | 59.5           | 60.7                  | 61.0                 | 56.5                 | 52.0                | 48.0                |
|                  | 256    | 16 384 | 62.5           | 62.6                  | 57.0                 | 53.8                 | 50.6                | 48.6                |
| VLAD             | 16     | 1 024  | 52.0           |                       | 52.7                 | 52.6                 | 50.5                | 47.7                |
|                  | 64     | 4 096  | 55.6           | 57.6                  | 59.8                 | 55.7                 | 52.3                | 48.4                |
|                  | 256    | 16 384 | 58.7           | 62.1                  | 56.7                 | 54.2                 | 51.3                | 48.1                |

# Examples

## Retrieval

### Example on Holidays:

From: Jégou, Perronnin, Douze, Sánchez, Pérez and Schmid, “Aggregating local descriptors into compact codes”, TPAMI’11.

| Descriptor       | $K$    | $D$    | Holidays (mAP) |                       |                      |                      |                     |                     |
|------------------|--------|--------|----------------|-----------------------|----------------------|----------------------|---------------------|---------------------|
|                  |        |        | $D' = D$       | $\rightarrow D'=2048$ | $\rightarrow D'=512$ | $\rightarrow D'=128$ | $\rightarrow D'=64$ | $\rightarrow D'=32$ |
| BOW              | 1 000  | 1 000  | 40.1           |                       | 43.5                 | 44.4                 | 43.4                | 40.8                |
|                  | 20 000 | 20 000 | 43.7           | 41.8                  | 44.9                 | 45.2                 | 44.4                | 41.8                |
| Fisher ( $\mu$ ) | 16     | 1 024  | 54.0           |                       | 54.6                 | 52.3                 | 49.9                | 46.6                |
|                  | 64     | 4 096  | 59.5           | 60.7                  | 61.0                 | 56.5                 | 52.0                | 48.0                |
|                  | 256    | 16 384 | 62.5           | 62.6                  | 57.0                 | 53.8                 | 50.6                | 48.6                |
| VLAD             | 16     | 1 024  | 52.0           |                       | 52.7                 | 52.6                 | 50.5                | 47.7                |
|                  | 64     | 4 096  | 55.6           | 57.6                  | 59.8                 | 55.7                 | 52.3                | 48.4                |
|                  | 256    | 16 384 | 58.7           | 62.1                  | 56.7                 | 54.2                 | 51.3                | 48.1                |

→ second order statistics are not essential for retrieval

# Examples

## Retrieval

### Example on Holidays:

From: Jégou, Perronnin, Douze, Sánchez, Pérez and Schmid, “Aggregating local descriptors into compact codes”, TPAMI’11.

| Descriptor       | $K$    | $D$    | Holidays (mAP) |                       |                      |                      |                     |                     |
|------------------|--------|--------|----------------|-----------------------|----------------------|----------------------|---------------------|---------------------|
|                  |        |        | $D' = D$       | $\rightarrow D'=2048$ | $\rightarrow D'=512$ | $\rightarrow D'=128$ | $\rightarrow D'=64$ | $\rightarrow D'=32$ |
| BOW              | 1 000  | 1 000  | 40.1           |                       | 43.5                 | 44.4                 | 43.4                | 40.8                |
|                  | 20 000 | 20 000 | 43.7           | 41.8                  | 44.9                 | 45.2                 | 44.4                | 41.8                |
| Fisher ( $\mu$ ) | 16     | 1 024  | 54.0           |                       | 54.6                 | 52.3                 | 49.9                | 46.6                |
|                  | 64     | 4 096  | 59.5           | 60.7                  | 61.0                 | 56.5                 | 52.0                | 48.0                |
|                  | 256    | 16 384 | 62.5           | 62.6                  | 57.0                 | 53.8                 | 50.6                | 48.6                |
| VLAD             | 16     | 1 024  | 52.0           |                       | 52.7                 | 52.6                 | 50.5                | 47.7                |
|                  | 64     | 4 096  | 55.6           | 57.6                  | 59.8                 | 55.7                 | 52.3                | 48.4                |
|                  | 256    | 16 384 | 58.7           | 62.1                  | 56.7                 | 54.2                 | 51.3                | 48.1                |

→ second order statistics are not essential for retrieval

→ even for the same feature dim, the FV/VLAD can beat the BOV

# Examples

## Retrieval

### Example on Holidays:

From: Jégou, Perronnin, Douze, Sánchez, Pérez and Schmid, “Aggregating local descriptors into compact codes”, TPAMI’11.

| Descriptor       | $K$    | $D$    | Holidays (mAP) |                       |                      |                      |                     |                     |
|------------------|--------|--------|----------------|-----------------------|----------------------|----------------------|---------------------|---------------------|
|                  |        |        | $D' = D$       | $\rightarrow D'=2048$ | $\rightarrow D'=512$ | $\rightarrow D'=128$ | $\rightarrow D'=64$ | $\rightarrow D'=32$ |
| BOW              | 1 000  | 1 000  | 40.1           |                       | 43.5                 | 44.4                 | 43.4                | 40.8                |
|                  | 20 000 | 20 000 | 43.7           | 41.8                  | 44.9                 | 45.2                 | 44.4                | 41.8                |
| Fisher ( $\mu$ ) | 16     | 1 024  | 54.0           |                       | 54.6                 | 52.3                 | 49.9                | 46.6                |
|                  | 64     | 4 096  | 59.5           | 60.7                  | 61.0                 | 56.5                 | 52.0                | 48.0                |
|                  | 256    | 16 384 | 62.5           | 62.6                  | 57.0                 | 53.8                 | 50.6                | 48.6                |
| VLAD             | 16     | 1 024  | 52.0           |                       | 52.7                 | 52.6                 | 50.5                | 47.7                |
|                  | 64     | 4 096  | 55.6           | 57.6                  | 59.8                 | 55.7                 | 52.3                | 48.4                |
|                  | 256    | 16 384 | 58.7           | 62.1                  | 56.7                 | 54.2                 | 51.3                | 48.1                |

→ second order statistics are not essential for retrieval

→ even for the same feature dim, the FV/VLAD can beat the BOV

→ soft assignment + whitening of FV helps when number of Gaussians ↑

# Examples

## Retrieval

### Example on Holidays:

From: Jégou, Perronnin, Douze, Sánchez, Pérez and Schmid, “Aggregating local descriptors into compact codes”, TPAMI’11.

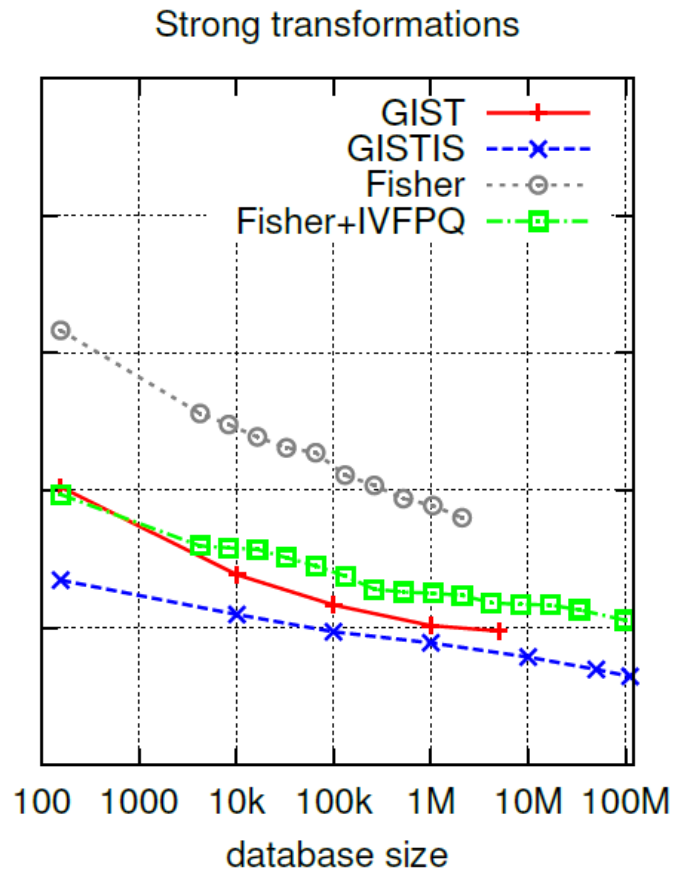
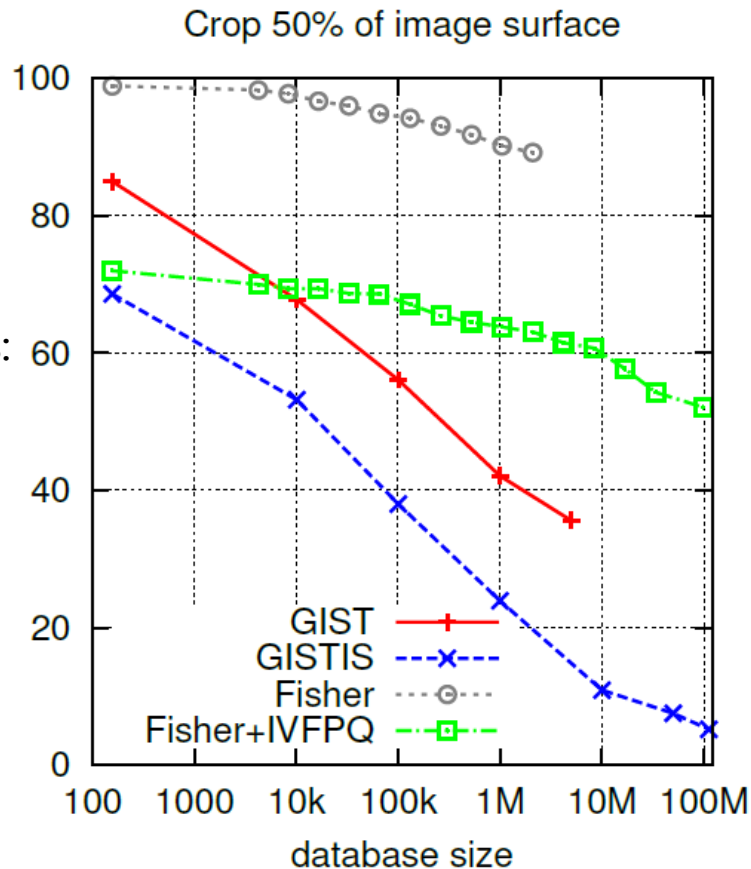
| Descriptor       | $K$    | $D$    | Holidays (mAP) |                       |                      |                      |                     |                     |
|------------------|--------|--------|----------------|-----------------------|----------------------|----------------------|---------------------|---------------------|
|                  |        |        | $D' = D$       | $\rightarrow D'=2048$ | $\rightarrow D'=512$ | $\rightarrow D'=128$ | $\rightarrow D'=64$ | $\rightarrow D'=32$ |
| BOW              | 1 000  | 1 000  | 40.1           |                       | 43.5                 | 44.4                 | 43.4                | 40.8                |
|                  | 20 000 | 20 000 | 43.7           | 41.8                  | 44.9                 | 45.2                 | 44.4                | 41.8                |
| Fisher ( $\mu$ ) | 16     | 1 024  | 54.0           |                       | 54.6                 | 52.3                 | 49.9                | 46.6                |
|                  | 64     | 4 096  | 59.5           | 60.7                  | 61.0                 | 56.5                 | 52.0                | 48.0                |
|                  | 256    | 16 384 | 62.5           | 62.6                  | 57.0                 | 53.8                 | 50.6                | 48.6                |
| VLAD             | 16     | 1 024  | 52.0           |                       | 52.7                 | 52.6                 | 50.5                | 47.7                |
|                  | 64     | 4 096  | 55.6           | 57.6                  | 59.8                 | 55.7                 | 52.3                | 48.4                |
|                  | 256    | 16 384 | 58.7           | 62.1                  | 56.7                 | 54.2                 | 51.3                | 48.1                |

- second order statistics are not essential for retrieval
- even for the same feature dim, the FV/VLAD can beat the BOV
- soft assignment + whitening of FV helps when number of Gaussians ↑
- after dim-reduction however, the FV and VLAD perform similarly

# Examples

## Very large-scale retrieval

Results on  
INRIA copydays:



Jégou, Perronnin, Douze, Sánchez, Pérez and Schmid, "Aggregating local descriptors into compact codes", TPAMI'12.

# Examples

## Classification

### Example on PASCAL VOC 2007:

From: Chatfield, Lempitsky, Vedaldi and Zisserman,  
“The devil is in the details: an evaluation of recent  
feature encoding methods”, BMVC’11.

|     | Feature dim | mAP   |
|-----|-------------|-------|
| VQ  | 25K         | 55.30 |
| KCB | 25K         | 56.26 |
| LLC | 25K         | 57.27 |
| SV  | 41K         | 58.16 |
| FV  | 132K        | 61.69 |



# Examples

## Classification

### Example on PASCAL VOC 2007:

From: Chatfield, Lempitsky, Vedaldi and Zisserman, "The devil is in the details: an evaluation of recent feature encoding methods", BMVC'11.

|     | Feature dim | mAP   |
|-----|-------------|-------|
| VQ  | 25K         | 55.30 |
| KCB | 25K         | 56.26 |
| LLC | 25K         | 57.27 |
| SV  | 41K         | 58.16 |
| FV  | 132K        | 61.69 |

→ FV outperforms BOV-based techniques including:

- VQ: plain vanilla BOV
- KCB: BOV with soft assignment
- LLC: BOV with sparse coding

# Examples

## Classification

### Example on PASCAL VOC 2007:

From: Chatfield, Lempitsky, Vedaldi and Zisserman, "The devil is in the details: an evaluation of recent feature encoding methods", BMVC'11.

|     | Feature dim | mAP   |
|-----|-------------|-------|
| VQ  | 25K         | 55.30 |
| KCB | 25K         | 56.26 |
| LLC | 25K         | 57.27 |
| SV  | 41K         | 58.16 |
| FV  | 132K        | 61.69 |

→ FV outperforms BOV-based techniques including:

- VQ: plain vanilla BOV
- KCB: BOV with soft assignment
- LLC: BOV with sparse coding

→ including 2nd order information is important for classification

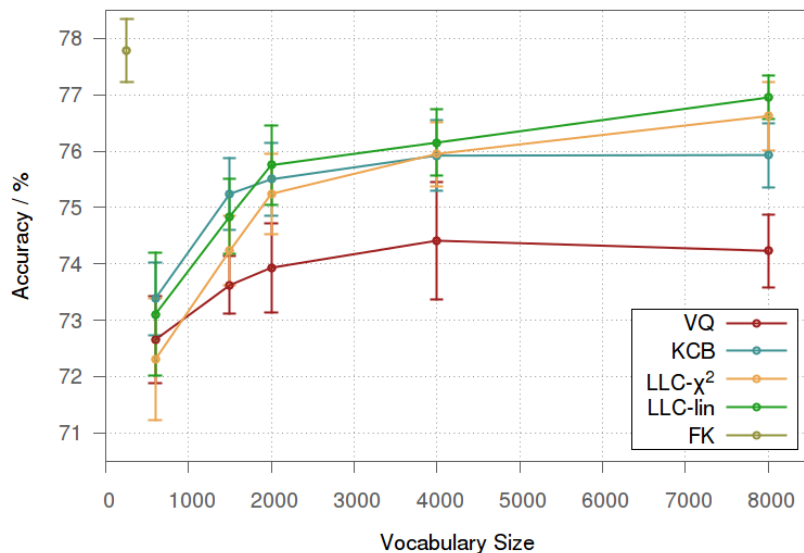
# Examples

## Classification

### Example on CalTech 101:

From: Chatfield, Lempitsky, Vedaldi and Zisserman, "The devil is in the details: an evaluation of recent feature encoding methods", BMVC'11.

Vocabulary Size vs. Accuracy over Caltech 101



→ FV outperforms BOV-based techniques including:

- VQ: plain vanilla BOV
- KCB: BOV with soft assignment
- LLC: BOV with sparse coding

→ including 2nd order information is important for classification

→ with higher-order information, one can get excellent results with tiny vocabularies

# Examples

## Very large-scale classification

Results on ImageNet10K:

- 10,184 classes (leaves and internal nodes)
- $\approx 9\text{M}$  images:  $\frac{1}{2}$  training /  $\frac{1}{2}$  test
- accuracy measured as % top-1 correct

# Examples

## Very large-scale classification

Results on ImageNet10K:

- 10,184 classes (leaves and internal nodes)
- $\approx 9\text{M}$  images:  $\frac{1}{2}$  training /  $\frac{1}{2}$  test
- accuracy measured as % top-1 correct

SIFT + BOV (21K-dim) + explicit embedding + linear SVM (SGD)

→ accuracy = 6.4 %

→ training time  $\approx 6$  CPU years

Deng, Berg, Li and Fei-Fei, “What does classifying more than 10,000 image categories tell us?”, ECCV’10.

# Examples

## Very large-scale classification

Results on ImageNet10K:

- 10,184 classes (leaves and internal nodes)
- $\approx 9\text{M}$  images:  $\frac{1}{2}$  training /  $\frac{1}{2}$  test
- accuracy measured as % top-1 correct

SIFT + BOV (21K-dim) + explicit embedding + linear SVM (SGD)

→ accuracy = 6.4 %

→ training time  $\approx 6$  CPU years

Deng, Berg, Li and Fei-Fei, “What does classifying more than 10,000 image categories tell us?”, ECCV’10.

SIFT + FV (130K-dim) + PQ compression + linear SVM (SGD)

→ accuracy = **19.1%**

→ training time  $\approx 1$  CPU year (**trick: do not sample all negatives**)

Perronnin, Akata, Harchaoui, Schmid, “Towards good practice in large-scale learning for image classification”, CVPR’12.

# Outline

Global vs local descriptors

The bag-of-visual-words

Higher-order representations

Examples

**Conclusion**

# Conclusion

Global descriptors should not be automatically discarded

→ still useful for such things as near duplicate detection or pre-filtering



# Conclusion

Global descriptors should not be automatically discarded

→ still useful for such things as near duplicate detection or pre-filtering

Among patch-based aggregation techniques, higher-order techniques seem to have an edge.

# Conclusion

Global descriptors should not be automatically discarded

→ still useful for such things as near duplicate detection or pre-filtering

Among patch-based aggregation techniques, higher-order techniques seem to have an edge.

The standard SIFT + BOV pipeline can be viewed as a first step toward a deep architecture as it combines multiple layers made of:

- coding
- pooling
- non-linearity

→ see [M'A Ranzato's part on large-scale deep learning](#)

# Packages

The INRIA package:

[http://lear.inrialpes.fr/src/inria\\_fisher/](http://lear.inrialpes.fr/src/inria_fisher/)

The Oxford package:

[http://www.robots.ox.ac.uk/~vgg/software/enceval\\_toolkit/](http://www.robots.ox.ac.uk/~vgg/software/enceval_toolkit/)

# Questions?