

## 编程语言的设计原理 Design Principles of Programming Languages

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# Chapter 14: Exceptions

Why exceptions

Raising exceptions (aborting whole program)

Handling exceptions

Exceptions carrying values



# Exceptions



Real world programming is full of situations where a function needs to signal to it caller that it is unable to perform its task for:

- Division by zero
- Arithmetic overflow
- Array index out of bound
- Lookup key missing
- File could not be opened
- **—** .....

Most programming languages *provide some mechanism* for interrupting the normal flow of control in a program to signal some exceptional condition ( & the transfer of control flow)



```
# type '\alpha list = None | Some of '\alpha

# let head I = match I with

[] -> None

| x::_ -> Some (x);;
```

Note that it is always possible to program without exceptions:

- instead of raising an exception, return None
- instead of returning result x normally, return Some(x)



```
# type \alpha list = None | Some of \alpha
# let head I = match I with
                     -> None
                 x::_ -> Some (x);;
What is the result of type inference?
val head: '\alpha list -> '\alpha Option = <fun>
While what we expect:
val head: '\alpha list -> '\alpha = <fun>
# let head I = match I with
                         -> raise Not_found
                   X∷_ -> X;;
```



If we want to wrap every function application in a case to find out whether it returned a result or an exception?

It is much more convenient to build this mechanism into the language, and *provide mechanism* for *interrupting the normal flow of control* in a program to *signal some exceptional condition* ( & the transfer of control flow).

#### Varieties of non-local control



There are many ways of adding "non-local control flow"

- exit(1)
- goto
- setjmp/ longjmp
- raise/ try (or catch/throw) in many variations
- callcc / continuations
- more esoteric variants (cf. many Scheme papers)

that allow programs to effect non-local "jumps" in the flow of control

Let's begin with the simplest of these.



# Raising exceptions

(aborting whole program)

## An "abort" primitive in $\lambda$



Raising exceptions (but not catching them), which cause the *abort of the whole program* 

#### Syntactic forms

#### **Evaluation rules**

## An "abort" primitive in $\lambda$



terms run-time error

- only the syntax of terms not in the syntax of values
  - e.g.,

- (x:Nat.0) error

– (fix (x:Nat.x)) error

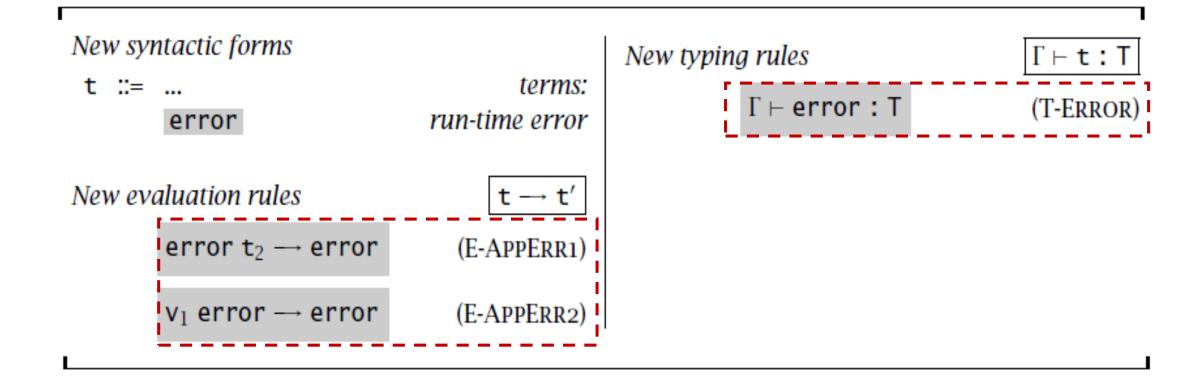
## An "abort" primitive in $\lambda_{\rightarrow}$



#### Typing rule

$$\Gamma \vdash error : T$$

(T-Error)



## Typing errors



Note that the typing rule for error allows us to give it any type T.

$$\Gamma \vdash \text{error} : T$$
 (T-Error)

What if we had booleans and numbers in the language?

This means that both

if x > 0 then 5 else error

and

if x > 0 then true else error

will typecheck

## Aside: Syntax-directedness



**Note:** this rule

```
\Gamma \vdash \text{error} : T (T-Error)
```

has a **problem** from the **point of view of implementation**: it is **not syntax directed** 

## Aside: Syntax-directed rules



When we say a set of rules is *syntax-directed* we mean *two things*:

- 1. There is exactly one rule in the set that applies to each syntactic form (in the sense that we can tell by the syntax of a term which rule to use)
  - e.g., to derive a type for  $t_1$   $t_2$ , we must use T-App
- 2. We don't have to "guess" an input (or output) for any rule
  - e.g., to derive a type for  $t_1$   $t_2$ , we need to derive a type for  $t_1$  and a type for  $t_2$

## Aside: Syntax-directedness



**Note:** this rule

$$\Gamma \vdash \text{error} : T$$
 (T-Error)

has a *problem* from the *point of view of implementation*: it is *not syntax* directed

This will cause the *Uniqueness of Types* theorem to fail

For purposes of *defining the language and proving its type safety*, this is not a problem — *Uniqueness of Types* is not critical

Let's think a little about how the rule might be fixed ...

## An alternative: Ascription



Can't we just *decorate the* error *keyword* with its *intended type*, as we have done to fix related problems with other constructs?

$$\Gamma \vdash (\text{error as } T) : T$$
 (T-Error)

## An alternative: Ascription



Can't we just *decorate the error keyword* with its intended type, as we have done to fix related problems with other constructs?

$$\Gamma \vdash (\text{error as } T) : T$$
 (T-Error)

Unfortunately, this doesn't work!

e.g. assuming our language also has *numbers* and *booleans*:

```
succ (if (error as Bool) then 3 else 8)

→ succ (error as Bool)
```

## Another alternative: Variable type



In a system with *universal polymorphism* (like OCaml), the variability of typing for error can be dealt with by *assigning it a variable type*?

 $\Gamma \vdash \text{error} : '\alpha$  (T-ERROR)

## Another alternative: Variable type



In a system with *universal polymorphism* (like OCaml), the variability of typing for error can be dealt with by assigning it a variable type!

 $\Gamma \vdash \text{error} : '\alpha$  (T-ERROR)

In effect, we are replacing the uniqueness of typing property by a weaker (but still very useful) property called most general typing

 i.e., although a term may have many types, we always have a compact way of representing the set of all of its possible types

## Yet another alternative: minimal type



Alternatively, in a system with subtyping (which will be discussed in chapter 15) and a minimal Bot type, we can give error a unique type:

## Yet another alternative: minimal type



Alternatively, in a system with subtyping (which will be discussed in chapter 15) and a minimal Bot type, we can give error a unique type:

 $\Gamma \vdash \text{error} : \text{Bot}$  (T-ERROR)

#### Note:

What we've really done is *just pushed the complexity* of the old error rule *onto the* Bot *type*!

#### For now...



Let's stick with the original rule

$$\Gamma \vdash \text{error} : T$$
 (T-Error)

and live with the resulting *non-determinism* of the typing relation

## Type safety



Property of preservation?

The preservation theorem requires *no changes* when we add error: if *a term* of type T reduces to *error*, that's fine, since *error* has every type T

## Type safety



Property of preservation?

The preservation theorem requires no changes when we add error: : if a term of type T reduces to error, that's fine, since error has every type T.

Whereas,

Progress requires a little more care

## **Progress**



First, *note that* we do *not* want to extend the set of *values* to include error, since this would make *our new rule* for *propagating errors* through applications

$$v_1 = error \longrightarrow error$$
 (E-APPERR2)

overlap with our existing computation rule for applications:

$$(\lambda x:T_{11}.t_{12})$$
  $v_2 \longrightarrow [x \mapsto v_2]t_{12}$  (E-APPABS)

e.g, the term

$$(\lambda x: Nat. 0)$$
 error

could evaluate to either 0 (which would be wrong) or error (which is what we intend).

## **Progress**



Instead, we **keep** *error* as a *non-value normal form*, and **refine the statement of progress** to explicitly mention the *possibility* that *terms may evaluate to error* instead of to a value

Theorem [Progress]:

Suppose t is a closed, well-typed normal form.

Then either t is a value or t = error.



# Handling exceptions

## Catching exceptions



#### syntax

**Fvaluation** 

t ::= ... terms try t with t trap errors 
$$try \ v_1 \ with \ t_2 \longrightarrow v_1 \qquad (E-TryV)$$
 try error with  $t_2 \longrightarrow t_2 \quad (E-TryError)$ 

$$\frac{\mathtt{t}_1 \longrightarrow \mathtt{t}_1'}{\mathtt{try} \ \mathtt{t}_1 \ \mathtt{with} \ \mathtt{t}_2 \longrightarrow \mathtt{try} \ \mathtt{t}_1' \ \mathtt{with} \ \mathtt{t}_2} \qquad \text{(E-Try)}$$

Typing

$$\frac{\Gamma \vdash t_1 : T \qquad \Gamma \vdash t_2 : T}{\Gamma \vdash try \ t_1 \ with \ t_2 : T}$$
 (T-TRY)



# Exceptions carrying values

## Exceptions carrying values



When something unusual happened, it's useful to send back some extra information about which unusual thing has happened so that the handler can take some actions depending on this information.

```
	t ::= ...
```

terms raise exception

## Exceptions carrying values



When something unusual happened, it's useful to send back some extra information about which unusual thing has happened so that the handler can take some actions depending on this information.

Atomic term error is replaced by a term constructor raise t

where *t* is the *extra information* that we want to *pass to the exception* handler

#### **Evaluation**



```
(raise v_{11}) t_2 \longrightarrow raise v_{11} (E-APPRAISE1)
    v_1 (raise v_{21}) \longrightarrow raise v_{21} (E-APPRAISE2)
                    \mathsf{t}_1 \longrightarrow \mathsf{t}_1'
                                                                    (E-Raise)
         \mathtt{raise} \ \ \mathtt{t}_1 \longrightarrow \mathtt{raise} \ \ \mathtt{t}_1'
 raise (raise v_{11}) \longrightarrow raise v_{11} (E-RAISERAISE)
                                                                    (E-TRYV)
          try v_1 with t_2 \longrightarrow v_1
 try raise v_{11} with t_2 \longrightarrow t_2 v_{11} (E-TRYRAISE)
                     \mathsf{t}_1 \longrightarrow \mathsf{t}_1'
                                                                       (E-Try)
try t_1 with t_2 \longrightarrow try \ t'_1 with t_2
```

#### **Evaluation**



```
(raise v_{11}) t_2 \longrightarrow raise v_{11} (E-APPRAISE1)
    v_1 (raise v_{21}) \longrightarrow raise v_{21} (E-APPRAISE2)
                    \mathsf{t}_1 \longrightarrow \mathsf{t}_1'
                                                                   (E-Raise)
          \texttt{raise} \ \ \texttt{t}_1 \longrightarrow \texttt{raise} \ \ \texttt{t}_1'
raise (raise v_{11}) \longrightarrow raise v_{11} (E-RAISERAISE)
          try v_1 with t_2 \longrightarrow v_1
                                                                  (E-TRYV)
 try raise v_{11} with t_2 \longrightarrow t_2 v_{11} (E-TRYRAISE)
                    \mathsf{t}_1 \longrightarrow \mathsf{t}_1'
                                                                      (E-Try)
try t_1 with t_2 \longrightarrow try t'_1 with t_2
```

#### **Evaluation**



$$\begin{array}{c} (\text{raise } v_{11}) \ t_2 \longrightarrow \text{raise } v_{11} & (\text{E-AppRaise1}) \\ v_1 \ (\text{raise } v_{21}) \longrightarrow \text{raise } v_{21} & (\text{E-AppRaise2}) \\ \\ \frac{t_1 \longrightarrow t_1'}{\text{raise } t_1 \longrightarrow \text{raise } t_1'} & (\text{E-Raise}) \\ \\ \text{raise } (\text{raise } v_{11}) \longrightarrow \text{raise } v_{11} & (\text{E-RaiseRaise}) \\ \\ \text{try } v_1 \ \text{with } t_2 \longrightarrow v_1 & (\text{E-TryV}) \\ \\ \text{try raise } v_{11} \ \text{with } t_2 \longrightarrow t_2 \ v_{11} & (\text{E-TryRaise}) \\ \\ \frac{t_1 \longrightarrow t_1'}{\text{try } t_1 \ \text{with } t_2 \longrightarrow \text{try } t_1' \ \text{with } t_2} & (\text{E-Try}) \end{array}$$

## **Typing**



To typecheck raise expressions, we need to *choose a type* for *the* values that are  $carried\ along\ with\ exceptions$ , let's call it  $T_{exn}$ 

$$\Gamma \vdash t_1 : T_{exn}$$
 $\Gamma \vdash raise t_1 : T$ 

$$\frac{\Gamma \vdash t_1 : T \qquad \Gamma \vdash t_2 : T_{exn} \to T}{\Gamma \vdash try \ t_1 \ with \ t_2 : \ T}$$

## What is $T_{exn}$ ?



Further, we need to decide what type to use as  $T_{exn}$ . There are several possibilities.

- 1. Numeric error codes:  $T_{exn} = Nat$  (as in Unix)
- 2. Error messages:  $T_{exn} = String$
- 3. A *predefined* variant type:

- 4. An extensible variant type (as in Ocaml)
- 5. A class of "throwable objects" (as in Java)

## Recapitulation: Error handling



→ error try

Extends  $\lambda_{\rightarrow}$  with errors (14-1)

New syntactic forms

New evaluation rules

terms: trap errors

$$t \rightarrow t'$$

(E-TRYV)

 $\begin{array}{c} \textbf{t}_1 \longrightarrow \textbf{t}_1' \\ \hline \textbf{try } \textbf{t}_1 \textbf{ with } \textbf{t}_2 \\ \longrightarrow \textbf{try } \textbf{t}_1' \textbf{ with } \textbf{t}_2 \end{array}$ 

New typing rules

$$\frac{\Gamma \vdash \mathsf{t}_1 : \mathsf{T} \qquad \Gamma \vdash \mathsf{t}_2 : \mathsf{T}}{\Gamma \vdash \mathsf{try}\; \mathsf{t}_1 \; \mathsf{with}\; \mathsf{t}_2 : \mathsf{T}}$$

(E-TRY)

 $\Gamma \vdash \textbf{t} : \textbf{T}$ 

(T-TRY)

try error with t<sub>2</sub>

try  $v_1$  with  $t_2 \rightarrow v_1$ 

 $\rightarrow$  t<sub>2</sub>

## Recapitulation: Exceptions carrying values



 $\rightarrow$  exceptions Extends  $\lambda_{\rightarrow}$  (9-1)

New syntactic forms

terms: raise exception handle exceptions

New evaluation rules

$$\textbf{t} \longrightarrow \textbf{t}'$$

(raise  $v_{11}$ )  $t_2 \rightarrow raise v_{11}$  (E-APPRAISE1)

 $v_1$  (raise  $v_{21}$ )  $\rightarrow$  raise  $v_{21}$  (E-APPRAISE2)

$$\frac{\mathtt{t}_1 \to \mathtt{t}_1'}{\mathtt{raise}\ \mathtt{t}_1 \to \mathtt{raise}\ \mathtt{t}_1'} \tag{E-RAISE}$$

$$\begin{array}{c} \text{raise (raise } v_{11}) \\ \longrightarrow \text{raise } v_{11} \end{array}$$

(E-RAISERAISE)

$$\texttt{try} \; \textbf{v}_1 \; \texttt{with} \; \textbf{t}_2 \longrightarrow \textbf{v}_1$$

(E-TRYV)

try raise 
$$v_{11}$$
 with  $t_2$   $\rightarrow$   $t_2$   $v_{11}$ 

(E-TRYRAISE)

$$\frac{\mathtt{t}_1 \to \mathtt{t}_1'}{\mathtt{try} \ \mathtt{t}_1 \ \mathsf{with} \ \mathtt{t}_2 \to \mathtt{try} \ \mathtt{t}_1' \ \mathsf{with} \ \mathtt{t}_2}$$

New typing rules

$$\Gamma \vdash \mathsf{t} : \mathsf{T}$$

$$\frac{\Gamma \vdash \mathsf{t}_1 : \mathsf{T}_{exn}}{\Gamma \vdash \mathsf{raise}\; \mathsf{t}_1 : \mathsf{T}}$$

(T-EXN)

(E-TRY)

$$\frac{\Gamma \vdash \mathsf{t}_1 : \mathsf{T} \qquad \Gamma \vdash \mathsf{t}_2 : \mathsf{T}_{exn} \rightarrow \mathsf{T}}{\Gamma \vdash \mathsf{try} \; \mathsf{t}_1 \; \mathsf{with} \; \mathsf{t}_2 : \mathsf{T}}$$

(T-TRY)

## Recapitulation



Raising exception is more than an error mechanism: it's a programmable control structure

- Sometimes a way to quickly escape from the computation.
- And allow programs to effect non-local "jumps" in the flow of control by setting a handler during evaluation of an expression that may be invoked by raising an exception.
- Exceptions are value-carrying in the sense that one may pass a value to the exception handler when the exception is raised.
- Exception values have a single type,  $T_{exn}$ , which is *shared by all exception handler*.

## Recapitulation



As an example, exceptions are used in OCaml as a control mechanism, either to signal errors, or to control the flow of execution.

- When an exception is raised, the current execution is aborted, and control is thrown to the most recently entered active exception handler, which may choose to handle the exception, or pass it through to the next exception handler.
- T<sub>exn</sub> is defined to be an extensible data type, in the sense that new constructors may be introduced using exception declaration, with no restriction on the types of value that may be associated with the constructor

## HW for chap14



- Read through chap 14
- Do exercise 14.3.2