

I. Stokes' theorem example

```
1 #showybox(  
2   title: "Stokes' theorem",  
3   frame: (  
4     border-color: blue,  
5     title-color: blue.lighten(30%),  
6     body-color: blue.lighten(95%),  
7     footer-color: blue.lighten(80%)  
8   ),  
9   footer: "Information extracted from a well-known public encyclopedia"  
10 ) [  
11   Let  $\Sigma$  be a smooth oriented surface in  $\mathbb{R}^3$  with boundary  $\partial\Sigma \equiv \Gamma$ . If a vector field  $\mathbf{F}(x,y,z) = (F_x(x,y,z), F_y(x,y,z), F_z(x,y,z))$  is defined and has continuous first order partial derivatives in a region containing  $\Sigma$ , then  
12  
13    $\iint_{\Sigma} (\nabla \times \mathbf{F}) \cdot \mathbf{n} \, d\mathbf{r} = \oint_{\Gamma} \mathbf{F} \cdot d\mathbf{r}$   
14 ]
```

Stokes' theorem

Let Σ be a smooth oriented surface in \mathbb{R}^3 with boundary $\partial\Sigma \equiv \Gamma$. If a vector field $\mathbf{F}(x,y,z) = (F_x(x,y,z), F_y(x,y,z), F_z(x,y,z))$ is defined and has continuous first order partial derivatives in a region containing Σ , then

$$\iint_{\Sigma} (\nabla \times \mathbf{F}) \cdot \mathbf{n} \, d\mathbf{r} = \oint_{\Gamma} \mathbf{F} \cdot d\mathbf{r}$$

Information extracted from a well-known public encyclopedia

II. Gauss's Law example

```
1 #showybox(  
2   frame: (  
3     border-color: red.darken(30%),  
4     title-color: red.darken(30%),  
5     radius: 0pt,  
6     thickness: 2pt,  
7     body-inset: 2em,  
8     dash: "densely-dash-dotted"  
9   ),  
10  title: "Gauss's Law"  
11 ) [  
12  The net electric flux through any hypothetical closed surface is equal  
   to  $\frac{1}{\epsilon_0}$  times the net electric charge enclosed within that
```

closed surface. The closed surface is also referred to as Gaussian surface. In its integral form:

```

13
14 $ \Phi_E = \oint_S \mathbf{E} \cdot d\mathbf{A} = Q/\epsilon_0 $
15 ]

```

Gauss's Law

The net electric flux through any hypothetical closed surface is equal to $\frac{1}{\epsilon_0}$ times the net electric charge enclosed within that closed surface. The closed surface is also referred to as Gaussian surface. In its integral form:

$$\Phi_E = \oint_S \mathbf{E} \cdot d\mathbf{A} = \frac{Q}{\epsilon_0}$$

III. Carnot's cycle efficiency example

```

1 #showybox(
2   title-style: (
3     weight: 900,
4     color: red.darken(40%),
5     sep-thickness: 0pt,
6     align: center
7   ),
8   frame: (
9     title-color: red.lighten(80%),
10    border-color: red.darken(40%),
11    thickness: (left: 1pt),
12    radius: 0pt
13  ),
14  title: "Carnot cycle's efficiency"
15 ) [
16   Inside a Carnot cycle, the efficiency  $\eta$  is defined to be:
17
18   $ \eta = W/Q_H = \frac{Q_H + Q_C}{Q_H} = 1 - T_C/T_H $
19 ]

```

Carnot cycle's efficiency

Inside a Carnot cycle, the efficiency η is defined to be:

$$\eta = \frac{W}{Q_H} = \frac{Q_H + Q_C}{Q_H} = 1 - \frac{T_C}{T_H}$$

IV. Clairaut's theorem example

```
1 #showybox(  
2   title-style: (  
3     boxed-style: (  
4       anchor: (  
5         x: center,  
6         y: horizon  
7       ),  
8       radius: (top-left: 10pt, bottom-right: 10pt, rest: 0pt),  
9     )  
10  ),  
11  frame: (  
12    title-color: green.darken(40%),  
13    body-color: green.lighten(80%),  
14    footer-color: green.lighten(60%),  
15    border-color: green.darken(60%),  
16    radius: (top-left: 10pt, bottom-right: 10pt, rest: 0pt)  
17  ),  
18  title: "Clairaut's theorem",  
19  footer: text(size: 10pt, weight: 600, emph("This will be useful every  
20    time you want to interchange partial derivatives in the future.))  
21  ) [  
22    Let $f: A \to \mathbb{R}$ with $A \subset \mathbb{R}^n$ an open set such that its  
23    cross derivatives of any order exist and are continuous in $A$. Then for  
24    any point $(a_1, a_2, \dots, a_n) \in A$ it is true that  
  
25    $ \frac{\partial^n f}{\partial x_i \dots \partial x_j}(a_1, a_2, \dots, a_n) = $  
26    $ \frac{\partial^n f}{\partial x_j \dots \partial x_i}(a_1, a_2, \dots, a_n) $  
27  ]
```

Clairaut's theorem

Let $f: A \rightarrow \mathbb{R}$ with $A \subset \mathbb{R}^n$ an open set such that its cross derivatives of any order exist and are continuous in A . Then for any point $(a_1, a_2, \dots, a_n) \in A$ it is true that

$$\frac{\partial^n f}{\partial x_i \dots \partial x_j}(a_1, a_2, \dots, a_n) = \frac{\partial^n f}{\partial x_j \dots \partial x_i}(a_1, a_2, \dots, a_n)$$

This will be useful every time you want to interchange partial derivatives in the future.

V. Divergence theorem example

```
1 #showybox(  
2   footer-style: (  
3     sep-thickness: 0pt,
```

```

4      align: right,
5      color: black
6    ),
7    title: "Divergence theorem",
8    footer: [
9      In the case of  $n=3$ ,  $V$  represents a volume in three-dimensional
10     space, and  $\partial V = S$  its surface
11   ]
12   ) [
13     Suppose  $V$  is a subset of  $\mathbb{R}^n$  which is compact and has a piecewise
14     smooth boundary  $S$  (also indicated with  $\partial V = S$ ). If  $\mathbf{F}$  is a
15     continuously differentiable vector field defined on a neighborhood of
16      $V$ , then:
17
18     
$$\iiint_V (\nabla \cdot \mathbf{F}) dV = \iint_S (\mathbf{F} \cdot \hat{\mathbf{n}}) dS$$

19
20   ]

```

Divergence theorem

Suppose V is a subset of \mathbb{R}^n which is compact and has a piecewise smooth boundary S (also indicated with $\partial V = S$). If \mathbf{F} is a continuously differentiable vector field defined on a neighborhood of V , then:

$$\iiint_V (\nabla \cdot \mathbf{F}) dV = \iint_S (\mathbf{F} \cdot \hat{\mathbf{n}}) dS$$

In the case of $n = 3$, V represents a volume in three-dimensional space, and $\partial V = S$ its surface

VI. Coulomb's law example

```

1  #showybox(
2    shadow: (
3      color: yellow.lighten(55%),
4      offset: 3pt
5    ),
6    frame: (
7      title-color: red.darken(30%),
8      border-color: red.darken(30%),
9      body-color: red.lighten(80%)
10   ),
11   title: "Coulomb's law"
12 ) [
13   Coulomb's law in vector form states that the electrostatic force
14    $\mathbf{F}$  experienced by a charge  $q_1$  at position  $\mathbf{r}$  in the
15   vicinity of another charge  $q_2$  at position  $\mathbf{r}'$ , in a vacuum is
16   equal to

```

```

14
15   $ \boldsymbol{F} = \frac{q_1 q_2}{4 \pi \epsilon_0} \frac{\boldsymbol{r} - \boldsymbol{r}'}{|\boldsymbol{r} - \boldsymbol{r}'|^3} $
16 ]

```

Coulomb's law

Coulomb's law in vector form states that the electrostatic force \boldsymbol{F} experienced by a charge q_1 at position \boldsymbol{r} in the vicinity of another charge q_2 at position \boldsymbol{r}' , in a vacuum is equal to

$$\boldsymbol{F} = \frac{q_1 q_2}{4\pi\epsilon_0} \frac{\boldsymbol{r} - \boldsymbol{r}'}{|\boldsymbol{r} - \boldsymbol{r}'|^3}$$

VII. Newton's second law example

```

1  #block(
2    height: 4.5cm,
3    inset: 1em,
4    fill: luma(250),
5    stroke: luma(200),
6    breakable: false,
7    columns(2)[
8      #showybox(
9        title-style: (
10          boxed-style: (
11            anchor: (x: center, y: horizon)
12          )
13        ),
14        breakable: true,
15        width: 90%,
16        align: center,
17        title: "Newton's second law"
18      )
19      If a body of mass  $m$  experiments an acceleration  $\boldsymbol{a}$  due to
20      a net force  $\sum \boldsymbol{F}$ , this acceleration is related to the mass and
21      force by the following equation:
22
23      $ \boldsymbol{a} = \frac{\sum \boldsymbol{F}}{m} $
24    ]

```

Newton's second law

If a body of mass m experiments an acceleration a due to a net force $\sum F$, this acceleration is related to the

mass and force by the following equation:

$$a = \frac{\sum F}{m}$$

VIII. Encapsulation example

```
1 #showybox(  
2   title: "Parent container",  
3   lorem(10),  
4   columns(2)[  
5     #showybox(  
6       title-style: (boxed-style: (:)),  
7       title: "Child 1",  
8       lorem(10)  
9     )  
10    #colbreak()  
11    #showybox(  
12      title-style: (boxed-style: (:)),  
13      title: "Child 2",  
14      lorem(10)  
15    )  
16  ]  
17 )
```

Parent container

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do.

Child 1

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do.

Child 2

Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do.