Capstone Final Results

Submitted By: Porur Kumanan

Student ID#: 500993016

Submission Date: April 6. 2020

```
-setwd("C:/Users/Arasan/Documents/Arasan/School/Ryerson/CKME 136- Capstone/Fi
nal Results and Code")
getwd()
## [1] "C:/Users/Arasan/Documents/Arasan/School/Ryerson/CKME 136- Capstone/Fi
nal Results and Code"
#file.path('C:\Users\Arasan\AppData\Local\Temp\RtmpkNTN45\downloaded packages
rm(list = ls())
library(factoextra)
## Warning: package 'factoextra' was built under R version 3.5.3
## Loading required package: ggplot2
## Warning: package 'ggplot2' was built under R version 3.5.3
## Welcome! Want to learn more? See two factoextra-related books at https://g
oo.gl/ve3WBa
GDPdata <- read.csv(file="GDP_Data_ProcessedNN.csv", header=TRUE, sep=",")</pre>
GDPdataCountry<-GDPdata
GDPdata <- na.omit(GDPdata)</pre>
#----
#is.na(GDPdata)
#check=sum(is.na(GDPdata))
#str(GDPdata)
#class(GDPdata x$GDPinUSDInMillions)
#----
#Data normalization
normalize <- function(x) {</pre>
  return ((x - min(x)) / (max(x) - min(x)))
GDPdata_norm <-normalize(GDPdata[,3:57])</pre>
GDPdata_lm <-GDPdata_norm# Data for regression analysis
GDPdata_x <-GDPdata_norm #Data for PCA analysis
```

```
if (FALSE){
GDPdata x <-GDPdata norm[,2:55]# Data for PCA analysis, removing the dependen
t variable GDPUSDInMillions
GDPdata_y <-GDPdata_norm[,1]</pre>
}
#GDPdata_x <-GDPdata[,3:57]# Data for PCA analysis
# Splitting the GDPdata dataset (GDPdata x) into training and test set.
train_index <- sample(1:nrow(GDPdata_x), 0.7 * nrow(GDPdata_x))</pre>
GDPdata.train.set <-GDPdata_x[train_index,-1]</pre>
GDPdata.test.set <- GDPdata_x[-train_index,-1]
GDPdata_y_train.set<-GDPdata_x[train_index,1]# removing the dependent variabl
e GDPUSDInMillions
GDPdata y test.set <- GDPdata x[-train index,1]# removing the dependent vari
able GDPUSDInMillions
GDPdataCountrytrainset=GDPdataCountry[train_index,]
#Apply normalization (scaling and centering) to the data.
#Calculate PCA with normalized data.
GDPdataTrainSet.pca.normdata <- prcomp(GDPdata.train.set, scale = TRUE, cente
r= TRUE)
GDPdataTrainSet.pca.normdata
## Standard deviations (1, ..., p=54):
## [1] 5.39103622 2.11885096 2.00233066 1.66606918 1.35194434 1.24835800
## [7] 1.07283015 1.02113059 0.93983212 0.87450993 0.82759021 0.75935873
## [13] 0.68428070 0.66621643 0.64472499 0.59363713 0.58473635 0.56078241
## [19] 0.52856213 0.51584534 0.48051591 0.44487235 0.42751129 0.41234470
## [25] 0.39599768 0.36777081 0.35826567 0.34108253 0.31369502 0.30361910
## [31] 0.29377105 0.27272400 0.26336194 0.25612041 0.24004477 0.23060747
## [37] 0.22146954 0.20875118 0.19809573 0.19150147 0.18487584 0.16700610
## [43] 0.15845476 0.14993811 0.14446424 0.13331155 0.11750949 0.11294562
## [49] 0.09905609 0.09356811 0.08600389 0.05447357 0.04899815 0.02283867
##
## Rotation (n x k) = (54 \times 54):
                                          PC2
##
                               PC1
                                                      PC3
                                                                  PC4
## MealInexpensive
                        ## MealFor2
                        ## McMealMcDonalds
                        ## DomesticBeer
                        0.15656357 -0.064088066 0.092619426 0.207671145
                        0.15095548 -0.147636257 0.087924868 0.181757182
## ImportedBeer
                        ## CokeOrPepsi
## Water1Litre
                        ## Milk1Litre
                        0.08962375 -0.113482240 0.248504107 -0.131161985
## LoafofBread
                        0.16734952 -0.028820403 -0.092048120 -0.007123153
## Eggs
                        0.15674918 0.101595579 0.048379691 0.060761199
## LocalCheese
                        0.13000863 -0.026126058 0.123870874 -0.231295369
## Water2Litre
                        0.14952559 -0.062136250 -0.152992668 0.008119030
## BottleofWine
                        0.09714495 -0.288992344 0.166927736 0.100190346
```

```
## Domestic1LitreBeer
                          0.09772663 -0.246829519
                                                   0.123087345
                                                                0.286824154
## Imported1LitreBeer
                          0.07157934 -0.274802478
                                                   0.142982357
                                                                0.283013582
## Cigarettes20Pack
                          0.13955641 -0.000192280 -0.104306346
                                                                0.095247248
## OnewayTicket
                          0.15823541 0.126555400 -0.090518849
                                                                0.094341355
## ChickenBreasts
                          0.16677886
                                      0.071000352 -0.059197002
                                                                0.034213561
## MonthlyPass
                          0.15424734
                                      0.016406173 -0.086827677
                                                                0.016252847
## Gasoline1Litre
                                      0.311166334
                                                   0.183160227 -0.117944994
                          0.04861856
## VWGolf
                          0.06454859 -0.035075907
                                                   0.322197940 -0.127322319
## Apartment1BD
                          0.16555516 -0.065946946 -0.037464754 -0.095363829
## Apartment1BD00C
                          0.16593329 -0.041431492 -0.065139351 -0.067910991
## Apartment3BDICC
                          0.16083960 -0.094831655
                                                   0.001924849 -0.148077694
## Apartment3BD00C
                          0.16555802 -0.063295666 -0.033643685 -0.092753376
                          0.09939399
## BasicUtilities
                                      0.215020688
                                                   0.006609223 -0.110940980
## PrepaidMobile1MIn
                          0.08450776
                                      0.045822763 -0.099931235
                                                                0.073187445
                          0.12833704 -0.142298877 -0.142346030
## Internet
                                                                0.174980749
## GymFees
                          0.11518932 -0.165771927
                                                   0.225812292 -0.014430538
## TennisCourtFeesPerHour
                          0.09608928
                                      0.077668261
                                                   0.107240490
                                                                0.230762288
## CinemaPerPerson
                                      0.044432434 -0.048303798
                          0.17376705
                                                                0.038148710
## PairofJeans
                          0.08353097
                                      0.308405043
                                                   0.240947505
                                                                0.062836881
## SummerDress
                          0.04965052 -0.098329723
                                                   0.201194756
                                                                0.250268529
                          0.08161500 0.121024732
                                                                0.123967412
## NikeRunningShoes
                                                   0.245550830
## LeatherShoes
                          0.13993672
                                      0.171150660
                                                   0.114379432 -0.032681723
## AptPricePerSquareM
                          0.12398159 -0.032683387
                                                   0.182961877 -0.299388219
## AptPricePerSqMOOC
                          0.13080389 -0.005364819
                                                   0.165011352 -0.264334577
## AvgMnthlyNetSalary
                          0.16532970 -0.077750523 -0.132897981 -0.006480517
## MortgageInterest
                          -0.09522553 -0.097373803
                                                   0.017318535
                                                                0.052175566
## TaxiStartingFare
                          0.14275140 0.181173611
                                                   0.053344740
                                                                0.088829482
## Taxi1KM
                          ## Taxi1HRWaiting
                          0.15681662
                                      0.155010241 -0.059193157
                                                                0.100759025
## Apples1KG
                          0.13330979 -0.206196094 -0.082076173 -0.144657802
## Oranges1KG
                          0.14508126 -0.130033829 -0.084859897 -0.172757225
## Potato1KG
                          0.15775094 -0.117332574 -0.085247461 -0.143578181
## Lettuce1Head
                          0.15282023 -0.018601443 -0.019945376
                                                                0.046998826
## CappucinoReg
                          0.15847468 -0.097471159
                                                   0.033108350
                                                                0.080624336
## WhiteRice
                          0.14534146 -0.095850558 -0.170191067 -0.065435258
                          0.16121374 -0.019165210 -0.112594208 -0.111445866
## Tomato1KG
## Banana1KG
                          0.11911303 0.023201220
                                                   0.152984365 -0.090936492
## Onion1KG
                          0.15185067 -0.116112767 -0.102868982 -0.171943500
                                     0.038216154 0.122929022 -0.083829354
## BeefRound1KG
                          0.14832905
## ToyotaCorolla
                          0.04522050 -0.027734791
                                                   0.330983512 -0.090837769
## PreschoolperMonth
                          0.14368983 -0.066729004 -0.138137998 -0.076296181
##
                                   PC5
                                                PC6
                                                            PC7
                                                                          PC
8
                                       0.0807728468
                                                     0.04366504 -0.054058359
## MealInexpensive
                          -0.050866908
9
## MealFor2
                          -0.001284243
                                       0.0894550666
                                                     0.01299348
                                                                 0.048678247
## McMealMcDonalds
                                       0.0282130045
                                                     0.07946622
                          0.006628627
                                                                 0.004586222
## DomesticBeer
                          -0.121140181 -0.0467425008 -0.01047789
                                                                 0.130525119
```

0 ## 9	ImportedBeer	-0.112504698	-0.0499001457	0.03991282	0.152792358
## 8	CokeOrPepsi	-0.018287169	-0.0370273263	0.11939970	0.059767022
	Water1Litre	-0.039105356	0.0114955248	0.13046602	0.047324697
	Milk1Litre	0.124779792	-0.2228449669	-0.18383050	0.017754428
	LoafofBread	0.083804450	0.0574637898	0.12840732	0.079586370
	Eggs	0.026557642	-0.1141785794	-0.07041589	0.010557232
## 8	LocalCheese	0.085888279	-0.0042464143	0.01657762	0.115314365
## 7	Water2Litre	0.062425050	0.0237745324	0.10249317	-0.071724714
	BottleofWine	-0.003739422	-0.0795800725	0.08705888	0.129795417
## 2	Domestic1LitreBeer	-0.137875743	-0.1682317325	-0.05017518	-0.019927385
## 8	Imported1LitreBeer	-0.101277895	-0.1976765866	-0.02639254	-0.004729357
## 5	Cigarettes20Pack	-0.240009880	-0.1300116054	-0.02624238	-0.232425755
## 5	OnewayTicket	-0.098607168	-0.0481170729	0.10688148	-0.041764975
	ChickenBreasts	0.042637128	0.0263991852	0.05180241	0.079075724
	MonthlyPass	-0.166278971	-0.0091329312	-0.03028172	-0.242845098
_	Gasoline1Litre	-0.161432040	-0.2363582258	-0.02047900	0.071853222
_	VWGolf	-0.093514860	0.0368180586	0.43985052	-0.233537428
	Apartment1BD	-0.188328121	0.1933800477	-0.07446875	0.017078772
	Apartment1BD00C	-0.187127708	0.1978806465	-0.06792769	0.017339534
	Apartment3BDICC	-0.170124057	0.1630899992	-0.11529893	0.037879573
	Apartment3BD00C	-0.174410251	0.1880585135	-0.10321317	0.049096940
	BasicUtilities	-0.023351115	-0.0411355034	-0.13584266	0.117777040
_	PrepaidMobile1MIn	0.003837996	-0.4039543807	-0.21239943	-0.497254890
	Internet	0.016005894	0.0042886665	-0.01543578	-0.029524431
	GymFees	0.013473644	-0.0020577346	-0.23751223	0.036357636

```
4
## TennisCourtFeesPerHour 0.246498291 0.0635222722 -0.07493970 0.166674466
## CinemaPerPerson -0.044181813 -0.0063236676 -0.05438254 0.014607210
6
## PairofJeans
                     5
                      ## SummerDress
## NikeRunningShoes 0.183862104 0.3071177519 -0.08940377 -0.266369131
3
                     ## LeatherShoes
3
## AptPricePerSquareM
                     -0.154281403 -0.0096749405 -0.16068829 0.014962603
                     -0.163069862 0.0041149394 -0.20746397 0.021292924
## AptPricePerSqMOOC
## AvgMnthlyNetSalary
                     -0.100098427 0.1338088393 0.04730733 0.051040466
## MortgageInterest
                     0.098820422  0.2512302195  0.00746212 -0.380137872
## TaxiStartingFare
                     0.017803285 -0.0749510625 0.07677888 0.042394533
2
## Taxi1KM
                      0.053493525 -0.0627519302 -0.02836553 -0.119799424
## Taxi1HRWaiting
                     -0.019771893 -0.0105582544 0.13891871 -0.035231478
                     0.200615887 -0.0476467654 0.14045827 0.009405806
## Apples1KG
1
                      0.223719656 -0.0367064999 0.05869990 -0.003295534
## Oranges1KG
2
## Potato1KG
                      0.155906354 -0.0623089280 0.03087516 -0.113950142
                     0.165991475 -0.1287779240 0.07481916 0.090556781
## Lettuce1Head
                      0.021309577 -0.0006878552 0.01330612 0.213479321
## CappucinoReg
## WhiteRice
                      0.164999787  0.0414504712  0.09624321  0.010116093
## Tomato1KG
                      ## Banana1KG
                      0.170280963 -0.1851219268 -0.05883164 -0.239044660
3
                      0.141676353 -0.0674724536 0.07054741 -0.065170290
## Onion1KG
1
## BeefRound1KG
               0.227202984 -0.1067664671 0.06947581 0.047697744
                     -0.181659289   0.0859420782   0.51563402   -0.159622421
## ToyotaCorolla
## PreschoolperMonth -0.195688191 0.1759223667 -0.16812881 -0.141611944
```

3					
## 12		PC9	PC10	PC11	PC
## 46	MealInexpensive	0.006949559	-0.0001871233	0.010421624	-0.02516381
	MealFor2	0.070842999	-0.0432963829	-0.078253506	0.04278753
	McMealMcDonalds	0.055695792	-0.0516856287	-0.068456220	-0.00688109
	DomesticBeer	0.015407198	0.0839698710	-0.053304798	-0.14124265
## 09	ImportedBeer	0.018856664	0.0812309667	-0.041512480	-0.10738861
## 93	CokeOrPepsi	-0.012461240	0.0426586949	0.064927131	-0.14943738
## 76	Water1Litre	0.039765894	0.0141193425	0.176710093	-0.09295454
	Milk1Litre	0.310801171	-0.2884826190	0.055995848	0.04116279
	LoafofBread	0.163461503	-0.0716033835	-0.041424171	-0.05282036
	Eggs	0.147241580	-0.1360798695	-0.082555051	-0.23880948
## 58	LocalCheese	0.094915351	-0.1332366045	0.007865879	0.03758349
## 56	Water2Litre	0.219014506	-0.1513757449	0.056367920	-0.05256037
## 63	BottleofWine	0.035638562	-0.1796620709	0.057105442	0.05385192
	Domestic1LitreBeer	-0.063806588	0.1376545480	0.092795149	-0.07867462
## 57	Imported1LitreBeer	-0.054764516	0.1419432538	0.060279167	0.04895519
	Cigarettes20Pack	0.121987645	0.0237418709	0.378823089	0.05986333
	OnewayTicket	0.060210980	0.0291535352	0.111607789	0.12783717
	ChickenBreasts	0.215622001	-0.0720517678	0.022940264	-0.03606281
	MonthlyPass	-0.033180652	0.0392490025	0.116478103	0.27974116
	Gasoline1Litre	0.044146484	0.0979160392	-0.183433931	0.01355991
	VWGolf	-0.190592779	-0.1824848820	-0.059583471	-0.06906458
	Apartment1BD	-0.024729505	-0.0146201837	-0.074181579	-0.00816440
	Apartment1BD00C	-0.005117369	-0.0259664618	-0.083242925	-0.03625566
	Apartment3BDICC	-0.019478234	-0.0028066759	-0.084786503	-0.00067769

	Apartment3BD00C	0.004260919	-0.0254518412	-0.107784612	-0.04293930
69 ## 58	BasicUtilities	-0.478248422	-0.0310000342	0.216206459	-0.33007796
## 44	PrepaidMobile1MIn	-0.099368596	-0.2242327089	-0.127173808	0.02305472
	Internet	-0.084385002	-0.2965414687	-0.257072201	-0.20500892
	GymFees	-0.215690858	-0.1079144806	-0.130480046	-0.05021911
## 62	TennisCourtFeesPerHour	-0.163643049	0.0691906988	-0.316785247	0.35700015
## 87	CinemaPerPerson	-0.060975367	0.0826649380	-0.063382021	0.08536108
## 22	PairofJeans	-0.072537974	-0.0324611978	0.049768127	-0.01250691
## 58	SummerDress	-0.048400820	0.1494891818	0.270620437	0.16949390
93	NikeRunningShoes	0.048916777	-0.2414835299	0.142095015	-0.01356682
## 65	LeatherShoes	-0.015854328	-0.1443914397	0.055372991	-0.03117101
93	AptPricePerSquareM	0.163242141	0.1810367905	0.005872004	0.11823936
65	AptPricePerSqMOOC	0.212890334		-0.004010940	0.06516592
15	AvgMnthlyNetSalary	-0.082217685	0.0555842556		-0.11267349
77	MortgageInterest	0.335877183		-0.284548453	
## 14	TaxiStartingFare	0.042713507		-0.123201128	0.04110808
84	Taxi1KM	-0.063723019		-0.376438141	0.31794224
99	Taxi1HRWaiting		0.1285183191		
34	Apples1KG	-0.087690840	0.1258395057		
20	Oranges1KG Potato1KG	-0.135047961			0.05827562
86	Lettuce1Head	0.175042916	-0.0243281276	0.185193389	
38	CappucinoReg	-0.002444364		-0.080159481	
41	WhiteRice	-0.117367786		-0.053251969	
47	Tomato1KG	-0.088028702		0.089799307	
11 11	. J.II.d COZING	3.000020702	3,113,70,702	3.005/5550/	3.03130431

57 ## 00	Banana1KG	-0.140960478	0.3814396932 -0.056317069 -0.27202587
	Onion1KG	-0.015922723	-0.0778654727 -0.029940357 -0.02646599
## 21	BeefRound1KG	0.064340450	0.2041669981 0.059054594 -0.01758975
## 62	ToyotaCorolla	-0.117183398	-0.0324423170 -0.055386258 0.11226596
	PreschoolperMonth	-0.137876713	-0.0100181605 0.048926212 0.05953687
## 6		PC13	PC14 PC15 PC1
_	MealInexpensive	0.063337798	-0.078790062 0.021005111 -0.127639484
	MealFor2	-0.021714138	-0.078339142 -0.030198078 0.049507888
	McMealMcDonalds	0.065303788	0.179456015 0.039231427 0.006176619
##	DomesticBeer	0.067368098	-0.086717378 -0.059928495 -0.066854500
## 5	ImportedBeer	0.064307249	-0.036826632 -0.055357672 -0.057586028
##	CokeOrPepsi	0.067653222	0.123141318 0.089895483 0.102514992
## 6	Water1Litre	-0.045107088	0.051495246 0.167743355 0.183963675
## 0	Milk1Litre	-0.125631623	-0.291932483 -0.003345691 -0.167708791
## 8	LoafofBread	0.013586084	0.012733875 0.058264509 -0.002401556
## 0	Eggs	0.015791767	0.192075035 0.166865616 -0.088553667
## 1	LocalCheese	0.475828538	0.225235045 0.018462332 -0.221531357
## 9	Water2Litre	-0.271464800	-0.062585190 0.309570059 0.142017746
## 6	BottleofWine	0.060564859	0.028941934 -0.044885644 -0.061070963
## 5	Domestic1LitreBeer	-0.009204659	0.087917881 0.027744252 0.028236790
## 2	Imported1LitreBeer	-0.063739674	0.187063259 0.126399562 0.006360581
## 1	Cigarettes20Pack	0.048437046	-0.012566700 0.024023355 0.164950480
## 7	OnewayTicket	0.065905804	-0.123590169 -0.091254738 -0.072808261
## 1	ChickenBreasts	0.016418423	0.185733566 0.094889568 -0.047977874
##	MonthlyPass	0.002308145	-0.144618953 0.096648347 -0.059274380

```
9
## Gasoline1Litre
                      -0.194233596  0.230339825  0.258003301  -0.022678519
## VWGolf
                     0.060125721 -0.174820637 0.016996922 -0.026072838
1
               0.049406933 -0.002438621 -0.060771979 0.079094228
## Apartment1BD
                     0.062866792 0.014286184 -0.018947984 0.073092139
## Apartment1BD00C
## Apartment3BDICC
                 0.021766902 0.027414766 -0.094770234 0.060749157
                      0.046416451 0.048083049 -0.043804328 0.044287694
## Apartment3BD00C
## BasicUtilities
                      -0.163311761 -0.161926207 0.248040325 -0.273372229
## PrepaidMobile1MIn
                     0.195477486 -0.022540237 0.016391864 -0.192454672
## Internet
                      -0.121008610 0.046403433 -0.142720411 0.099589942
## GymFees
                      -0.110659082 0.047410800 0.028809447 0.437899452
## TennisCourtFeesPerHour 0.338011090 -0.282616687 0.400009295 0.123903306
1
## CinemaPerPerson -0.052831442 -0.090621492 -0.045742281 -0.153762817
3
## PairofJeans
                     -0.057232072 -0.028614836 -0.058780597 0.154542410
3
                     -0.216222700 0.191879162 0.133532547 -0.237552728
## SummerDress
                      -0.017230905 0.123444347 -0.212454533 0.001063545
## NikeRunningShoes
## LeatherShoes
                      -0.022692975 -0.031096965 -0.110562584 0.058173549
## AptPricePerSquareM
                      -0.103840300 -0.059821778 0.005845261 -0.004547719
## AptPricePerSqMOOC
                      -0.082000758 -0.029506020 0.071214210 -0.031376120
## AvgMnthlyNetSalary 0.040962481 0.003392056 -0.083039063 -0.055036053
## MortgageInterest
                      0.033525206 -0.189915251 0.236537978 -0.081803050
## TaxiStartingFare
                      -0.118152475 -0.142777778 -0.367774183 -0.092544236
2
## Taxi1KM
                      2
## Taxi1HRWaiting
                      ## Apples1KG
                      -0.047850785 -0.127012279 -0.096912238 -0.010950039
## Oranges1KG
```

```
8
                                      0.112742940
## Potato1KG
                         -0.072379232
                                                  0.027892670
                                                               0.020243816
2
## Lettuce1Head
                         0.010781730 -0.310104749
                                                  0.018923607
                                                               0.306256834
2
                         -0.152489102 -0.235956593 -0.058012935 -0.328304863
## CappucinoReg
3
## WhiteRice
                         -0.096491333 0.060329466
                                                  0.052295972 -0.187372021
0
## Tomato1KG
                         0.022597958 -0.117776280
                                                  0.036090775 0.091823456
7
                         0.100839721 -0.001140093 -0.213754731
## Banana1KG
                                                               0.201170384
6
## Onion1KG
                         -0.004862221 0.041094026 0.085206853
                                                               0.114264602
5
## BeefRound1KG
                         ## ToyotaCorolla
                         -0.096585574 -0.010655904
                                                  0.117001922 -0.000701279
9
## PreschoolperMonth
                         0.244883370 -0.023337141
                                                  0.117770868 -0.045884081
6
##
                                PC17
                                             PC18
                                                         PC19
                                                                      PC20
                         0.035179223
                                      0.063901020 -0.171389409
## MealInexpensive
                                                               0.022206497
## MealFor2
                         -0.049844673
                                      0.033416475
                                                  0.038791697
                                                               0.106460094
## McMealMcDonalds
                         0.104208960
                                      0.176144674 -0.216460122 -0.014843481
## DomesticBeer
                         -0.057146004
                                      0.057685748 -0.055739101
                                                               0.156733633
## ImportedBeer
                         -0.069957965 -0.003462511 -0.151083820
                                                               0.068964991
## CokeOrPepsi
                         0.014823027
                                      0.068810066 -0.028751704 -0.199133405
## Water1Litre
                         0.026532305
                                      0.159112531
                                                 0.019257403 -0.221921718
## Milk1Litre
                         -0.042812417
                                      0.230524971 -0.080681556 0.041820513
## LoafofBread
                         -0.113456865 -0.121737449
                                                  0.063324090 -0.182945892
                         -0.175015307
                                      0.125435177
                                                  0.295971390 -0.041452683
## Eggs
## LocalCheese
                         0.352914042
                                      0.103326278 -0.138173078 -0.034632525
## Water2Litre
                         -0.123609434
                                      0.001372733 -0.031165641 -0.067730654
## BottleofWine
                         0.124072371 -0.197941849
                                                  0.475810065 -0.049827480
## Domestic1LitreBeer
                         0.077073607 -0.088573957
                                                  0.108934185
                                                               0.096545581
## Imported1LitreBeer
                         0.198178436 -0.101578216
                                                  0.050919558 -0.184296433
## Cigarettes20Pack
                         -0.059700047
                                      0.124442769 -0.013457176
                                                               0.012689040
## OnewayTicket
                         0.144490695 -0.040216074
                                                  0.076891304
                                                               0.090890810
## ChickenBreasts
                         0.001411996
                                      0.006064748 -0.068463885
                                                               0.265124517
## MonthlyPass
                         0.112734507
                                      0.138659773
                                                  0.232002840
                                                               0.172022511
## Gasoline1Litre
                         -0.085298957 -0.296645003
                                                  0.005641645
                                                               0.233728108
## VWGolf
                         -0.034388733
                                      0.102161606
                                                  0.029286959
                                                               0.072387544
## Apartment1BD
                         -0.033141492 -0.080400792 -0.005025633 -0.023484130
## Apartment1BD00C
                         -0.068677678 -0.079632866 -0.004042951
                                                               0.031138514
## Apartment3BDICC
                         -0.015557833 -0.140850809
                                                  0.013008082 -0.114669003
## Apartment3BD00C
                         -0.066006478 -0.102195683 -0.004928420 -0.046071284
## BasicUtilities
                         0.303024999
                                      ## PrepaidMobile1MIn
                         -0.134536395 -0.312774185 -0.240630088 -0.091329294
                         ## Internet
```

```
## GymFees
                      0.157730351 0.129955116 -0.139845959 0.237004128
## TennisCourtFeesPerHour -0.155165336  0.036218862  0.030926967 -0.113540588
## CinemaPerPerson
                     0.054591090 -0.184994752
## PairofJeans
                      0.120985851 -0.228094499
## SummerDress
                     -0.129593614 -0.019299968 -0.275859342 -0.036909342
## NikeRunningShoes
                     -0.029765162
                                 0.019174160
                                            0.166484488 -0.006684213
## LeatherShoes
                      0.011531855 -0.231814405
                                            0.128324680 0.133585842
## AptPricePerSquareM
                      ## AptPricePerSqMOOC
                     ## AvgMnthlyNetSalary
                     -0.093591601 -0.049678388 -0.064677583 0.050632168
## MortgageInterest
                      0.377678241 -0.074689626
                                            0.078722968 0.018092045
## TaxiStartingFare
                      0.188353268 -0.185968596 -0.207537921 -0.095502062
## Taxi1KM
                      0.223241265
                                 0.316090524 0.192633307 0.054164621
                      0.030290650 -0.021119694
## Taxi1HRWaiting
                                            0.143614756 -0.059988197
## Apples1KG
                      0.066226984 -0.021381840 -0.127153373 -0.176942478
## Oranges1KG
                      ## Potato1KG
                     -0.066012650 -0.069015923 -0.018861492 -0.124482988
                      0.149575448 -0.116103250 -0.181314881 0.196537874
## Lettuce1Head
## CappucinoReg
                     ## WhiteRice
                     -0.187709983 -0.121519093
                                            0.022125543 0.466609211
## Tomato1KG
                      0.024765053 -0.201213331
                                            0.111209367 0.078983517
## Banana1KG
                     -0.310282469
                                 0.260830086
                                            0.107511776 -0.072726146
## Onion1KG
                      0.083645926 -0.185691200
                                            0.050682014 -0.160904432
## BeefRound1KG
                      0.001164197
                                 0.108074135
                                            0.024425500
                                                       0.173488340
## ToyotaCorolla
                     -0.074492744 -0.053112878 -0.146294168 -0.013936426
## PreschoolperMonth
                     -0.013028309 0.108116515
                                            0.062123933 0.033826513
##
                            PC21
                                        PC22
                                                   PC23
24
## MealInexpensive
                     0.034634120 0.0939173254 -0.276981606 0.15070715
54
## MealFor2
                      0.032476526  0.0439322843  0.028621331  -0.15635823
99
## McMealMcDonalds
                      32
## DomesticBeer
                      0.058657253  0.0907248183  0.219835444  0.12618460
12
                   0.022113244 0.0637525089 0.081735494 0.12154316
## ImportedBeer
80
                     0.208955936 -0.0449912320 0.034406434 0.15666463
## CokeOrPepsi
86
## Water1Litre
                      0.201222912 -0.1238319714 0.078642637 0.11604706
40
                     0.076608821 -0.0187693447 -0.226447115 0.08731633
## Milk1Litre
94
## LoafofBread
                      0.022554103 -0.0017317246 -0.133192468 -0.12131853
39
## Eggs
                     92
## LocalCheese
                      0.092259446 -0.2060346471 0.214148789 -0.32972523
98
```

## 37	Water2Litre	-0.203608482	-0.2630742573	0.008598669	-0.19446637
	BottleofWine	-0.017949700	0.3113971723	-0.034669241	-0.12456813
	Domestic1LitreBeer	0.076329567	-0.1749403523	0.082447285	0.14517873
## 19	Imported1LitreBeer	0.087115229	-0.3414999853	-0.175282310	0.08862265
## 71	Cigarettes20Pack	-0.051754114	0.0889468063	-0.088401070	-0.10694575
## 62	OnewayTicket	-0.193896357	-0.0656697894	0.056242606	-0.13114823
## 25	ChickenBreasts	-0.088859628	0.0031791974	0.123554985	0.18591439
## 57	MonthlyPass	-0.312759995	0.0479728739	0.112412210	-0.05654973
## 34	Gasoline1Litre	-0.119408351	-0.0474382484	0.042864503	-0.14363240
## 10	VWGolf	0.065993035	-0.1588539429	0.079837745	-0.06384338
## 33	Apartment1BD	0.031423348	0.0443263887	-0.043191475	-0.00309660
## 28	Apartment1BD00C	-0.007262661	0.1117231497	0.005214384	-0.01035409
## 88	Apartment3BDICC	0.008499105	0.0509363504	-0.025238689	-0.00205489
## 81	Apartment3BD00C	-0.009795657	0.1066264090	0.018100065	-0.02539651
## 81	BasicUtilities	-0.071842759	0.1599239467	0.051017876	0.07318489
## 07	PrepaidMobile1MIn	0.165433432	0.0827100723	0.076249278	0.00369966
## 44	Internet	-0.381254687	-0.0088347236	0.338871727	0.01572174
## 80	GymFees	0.029410217	-0.0240019600	-0.229543787	-0.16337317
## 03	TennisCourtFeesPerHour	-0.121945535	-0.0334057589	0.040312564	0.15285913
## 16	CinemaPerPerson	0.052473978	-0.2530752618	0.051134278	-0.18908234
## 28	PairofJeans	-0.090753205	-0.0013096737	-0.049315116	-0.20966470
## 05	SummerDress	0.058259576	0.2530757180	0.169528614	-0.19900842
## 69	NikeRunningShoes	-0.119516543	-0.2326428702	0.058158359	0.33306793
## 41	LeatherShoes	0.252415750	-0.1240734756	-0.019710632	-0.00022928
	AptPricePerSquareM	-0.022521544	-0.0778492278	0.095410425	0.14677077

```
## AptPricePerSqMOOC -0.016224034 -0.0314370006 0.213097527 0.17106000
62
## AvgMnthlyNetSalary 0.144750801 -0.0220716744 -0.040645779 -0.02949975
## MortgageInterest 0.038468376 0.0423939421 -0.053063967 -0.04752666
37
## TaxiStartingFare -0.255049708 -0.0320620228 -0.317059855 0.09057251
## Taxi1KM
                   0.354482721 0.1406098455 0.049308527 0.06301244
84
## Taxi1HRWaiting 0.153993150 -0.0095250792 0.155828760 -0.05978448
75
                  ## Apples1KG
10
## Oranges1KG 0.005866207 -0.0065731468 -0.042776967 0.01391550
48
## Potato1KG
                   24
## Lettuce1Head 0.242123662 0.2196565092 0.146217455 -0.06422780
77
## CappucinoReg
                  0.031350011 -0.0878672746 -0.006589424 -0.13947748
55
## WhiteRice
                  0.051079605 -0.2658654072 -0.090498687 0.01824607
62
                   0.003260612 -0.0335273647 0.042125128 0.04097484
## Tomato1KG
77
                   ## Banana1KG
39
## Onion1KG
                   -0.063216729 0.0729085029 0.110302351 0.27921383
26
## BeefRound1KG
                   -0.237587146  0.1565400859  -0.131168398  0.17765971
81
## ToyotaCorolla 0.035160751 0.1977811624 -0.055631363 0.09153193
## PreschoolperMonth 0.030662706 -0.0868724534 -0.292473294 0.03857151
52
                          PC25
##
                                    PC26
                                              PC27
                                                        PC28
## MealInexpensive
                    0.166303094 -0.219564379 -0.160747112 -0.140141454
## MealFor2
                    0.026260603 -0.038975324 -0.129918826 0.006711220
## McMealMcDonalds
                   ## DomesticBeer
                    -0.032542008 -0.082028171 -0.088984383 0.074189289
                   ## ImportedBeer
                    ## CokeOrPepsi
                    0.199573954   0.180678781   0.061317687   -0.088617390
## Water1Litre
## Milk1Litre
                    0.257496051 0.041228254 0.202564243 -0.169050767
## LoafofBread
                   ## Eggs
                   -0.012848933 -0.134714835 0.199548800 0.335921972
                   -0.067634945 -0.152932943 -0.002975556 0.073908406
## LocalCheese
## Water2Litre
                   -0.215042112 -0.158501869 -0.132781916 0.027233946
## BottleofWine
```

```
## Domestic1LitreBeer
                            0.084511261 -0.125279184
                                                       0.148964433 -0.107040031
## Imported1LitreBeer
                           -0.043814213 -0.207128201
                                                       0.113858245 -0.035351935
## Cigarettes20Pack
                           -0.164758380
                                         0.051810636
                                                       0.001078488
                                                                    0.093479294
## OnewayTicket
                            0.171174606
                                         0.295566019
                                                       0.207278955 -0.021267468
## ChickenBreasts
                            0.183357657 -0.033393747 -0.057774315
                                                                    0.205575000
## MonthlyPass
                            0.162482293 -0.100081262
                                                       0.002770762
                                                                    0.060074702
## Gasoline1Litre
                            0.036442947 -0.072350006
                                                     -0.021859300 -0.318010658
## VWGolf
                           -0.037247485 -0.006178150
                                                       0.248624311 -0.069535433
## Apartment1BD
                           -0.033981402 -0.082179069
                                                       0.121556327 -0.060636284
## Apartment1BD00C
                           -0.042706824 -0.097099017
                                                       0.165900732 -0.089497521
## Apartment3BDICC
                            0.011005405 -0.001226869
                                                       0.071719151 -0.043417696
## Apartment3BD00C
                           -0.026719852 -0.061337141
                                                       0.149562605 -0.046876678
## BasicUtilities
                           -0.256823864
                                         0.087892931
                                                       0.030293105 -0.050603185
## PrepaidMobile1MIn
                           -0.057320271
                                         0.111580587 -0.070130467
                                                                    0.150085503
                            0.178633943
## Internet
                                        -0.048425069
                                                       0.005805862 -0.145206497
## GymFees
                            0.079915226
                                         0.332173628 -0.042628243
                                                                    0.301981876
  TennisCourtFeesPerHour -0.038099108
                                         0.060440998
                                                       0.058130395 -0.030817331
## CinemaPerPerson
                            0.006855607
                                         0.279095225
                                                       0.035523089 -0.108955897
## PairofJeans
                            0.163143367 -0.236248718 -0.023710855
                                                                    0.239066816
## SummerDress
                            0.129557443
                                         0.065720774
                                                       0.124377114 -0.082709638
                                         0.065543662 -0.062291060 -0.008185126
## NikeRunningShoes
                           -0.370695520
## LeatherShoes
                            0.203046478
                                        -0.124796505 -0.094691989
                                                                   -0.084714384
## AptPricePerSquareM
                           -0.065205645
                                         0.099989898 -0.168247698
                                                                    0.050188854
## AptPricePerSqMOOC
                                         0.108960522 -0.120410482
                                                                    0.037368448
                           -0.084081737
## AvgMnthlyNetSalary
                            0.046008286
                                         0.100185204
                                                      0.167700847
                                                                    0.012849956
## MortgageInterest
                            0.068941683
                                         0.093551965 -0.016822303
                                                                    0.044262728
## TaxiStartingFare
                           -0.102443239
                                         0.033119778
                                                       0.091617927
                                                                    0.063220907
## Taxi1KM
                           -0.178936729 -0.118386100
                                                       0.109365977
                                                                    0.012975830
## Taxi1HRWaiting
                            0.018320432
                                         0.073937342 -0.080007255
                                                                    0.088060616
## Apples1KG
                           -0.042528381
                                         0.052784406 -0.040916209
                                                                    0.179225295
## Oranges1KG
                            0.219301010 -0.243423530 -0.168035064
                                                                    0.034484717
## Potato1KG
                            0.088031682 -0.005509736
                                                       0.151760805 -0.180571884
## Lettuce1Head
                           -0.298807804 -0.144413233
                                                       0.057004566 -0.117117654
## CappucinoReg
                           -0.015331036 -0.124663204 -0.136218311
                                                                    0.153500301
## WhiteRice
                           -0.032538691
                                         0.160949430 -0.135242773
                                                                    0.077774575
## Tomato1KG
                           -0.070921124 -0.104040399
                                                       0.144973021
                                                                    0.114613193
## Banana1KG
                            0.006396967 -0.053691532 -0.114650930 -0.202258559
## Onion1KG
                            0.105590753
                                         0.054421187 -0.131308668 -0.090682820
## BeefRound1KG
                           -0.054678421
                                         0.025462918
                                                      0.187380848 -0.032823420
  ToyotaCorolla
##
                            0.048334643 -0.066778955 -0.115574381
                                                                    0.157933750
## PreschoolperMonth
                            0.025340848 -0.106198636 -0.195999446 -0.075057801
##
                                  PC29
                                               PC30
                                                             PC31
                                                                          PC32
## MealInexpensive
                            0.21283265
                                        0.141511951
                                                      0.123788697 -0.112635608
## MealFor2
                            0.10533475 -0.009152441
                                                      0.120378607 -0.185963301
## McMealMcDonalds
                            0.11034018
                                        0.022134054 -0.199016774 -0.193836597
## DomesticBeer
                           -0.06756192 -0.016334758 -0.068960052
                                                                   0.056297549
## ImportedBeer
                           -0.12510596
                                        0.136728136 -0.053053964
                                                                   0.168346568
## CokeOrPepsi
                           -0.01045915
                                        0.103279782
                                                      0.015293365
                                                                   0.198343395
## Water1Litre
                           -0.10501459
                                        0.002826941 -0.138333530
                                                                   0.090246308
## Milk1Litre
                           -0.02904283 -0.048252887 -0.002010343
                                                                   0.010186069
```

```
## LoafofBread
                           0.20491150 0.224614304 -0.130141666
                                                                  0.166515359
## Eggs
                           0.16255686 -0.112376738
                                                     0.056666672
                                                                  0.050888227
## LocalCheese
                          -0.12379095 -0.034761827
                                                     0.133414936 -0.018019599
                                        0.141574218 -0.051047905
## Water2Litre
                          -0.26036351
                                                                  0.029142376
## BottleofWine
                          -0.17178358
                                       0.044090636 -0.047679079
                                                                  0.025849200
## Domestic1LitreBeer
                          -0.05556083
                                        0.007741198
                                                     0.006802694 -0.058077422
## Imported1LitreBeer
                           0.17220975
                                       0.065298643
                                                     0.035359302 -0.066892349
## Cigarettes20Pack
                          -0.31592687 -0.222583935
                                                     0.259675908 -0.133440746
## OnewayTicket
                           0.09129070
                                       0.032260374
                                                     0.263871882 -0.041526356
## ChickenBreasts
                          -0.12609045 -0.204942614 -0.069071949
                                                                  0.003382719
## MonthlyPass
                           0.12833867
                                       0.314288353 -0.194348226
                                                                  0.179360356
## Gasoline1Litre
                           0.06984504 -0.195059711
                                                     0.192698001
                                                                  0.227032317
## VWGolf
                          -0.08300842 -0.037961056 -0.261462595 -0.060399966
## Apartment1BD
                           0.01754071 -0.058308600 -0.056399903
                                                                  0.063359082
## Apartment1BD00C
                          -0.03172772 -0.033648644 -0.058344203 -0.084098522
## Apartment3BDICC
                           0.04303481
                                       0.030566770
                                                     0.079553441
                                                                  0.157228380
## Apartment3BD00C
                          -0.06569374
                                       0.043259470
                                                     0.044606311 -0.012458394
## BasicUtilities
                          -0.03422107
                                        0.053109025
                                                     0.094738475 -0.065180667
## PrepaidMobile1MIn
                           0.03804020
                                       0.097301883 -0.072040492
                                                                  0.051376283
## Internet
                           0.07817496
                                       0.027567325
                                                     0.058946908 -0.006870934
                           0.09730094 -0.059679928
                                                     0.046039114 -0.033984223
## GymFees
## TennisCourtFeesPerHour -0.13200384
                                        0.003985777
                                                     0.176602538 -0.042650703
## CinemaPerPerson
                           0.15750489 -0.299514311 -0.120715535
                                                                  0.111572287
## PairofJeans
                           0.01193976
                                       0.087462349 -0.322312836 -0.201860121
## SummerDress
                          -0.06971133 -0.100712086 -0.134439849
                                                                  0.042169809
## NikeRunningShoes
                           0.19769063 -0.094866528
                                                     0.208645396
                                                                  0.152409525
## LeatherShoes
                          -0.27006105
                                        0.274911092
                                                     0.169500399
                                                                  0.097770690
## AptPricePerSquareM
                           0.13959917
                                        0.119379499 -0.037337085 -0.052869807
## AptPricePerSqMOOC
                          -0.02093875
                                        0.168946803 -0.031534321 -0.225389188
## AvgMnthlyNetSalary
                          -0.04010222
                                        0.118838102
                                                     0.140363679
                                                                  0.043746736
## MortgageInterest
                          -0.01799618 -0.042332187
                                                     0.078313922
                                                                  0.025288312
## TaxiStartingFare
                          -0.39119798 -0.098896799 -0.060193108
                                                                  0.128978833
## Taxi1KM
                          -0.19405374
                                       0.024163792 -0.030238564
                                                                  0.087980636
## Taxi1HRWaiting
                           0.17419415 -0.101883693
                                                     0.042593174 -0.301417303
## Apples1KG
                           0.05009582
                                       0.110318551
                                                     0.132704934
                                                                  0.184241925
## Oranges1KG
                           0.13276578 -0.120664004
                                                     0.134998593
                                                                  0.224756079
## Potato1KG
                          -0.07605235
                                        0.087831685
                                                     0.237500361 -0.413484109
## Lettuce1Head
                           0.24454830 -0.011765371 -0.019330990
                                                                  0.154443400
## CappucinoReg
                           0.06294036 -0.158915686
                                                     0.054945311 -0.045256096
                                       0.144454907 -0.099886878 -0.183557060
## WhiteRice
                          -0.02116965
## Tomato1KG
                           0.04887614 -0.224359412 -0.104934932 -0.195996817
## Banana1KG
                          -0.07721317
                                        0.038880431
                                                     0.038697511
                                                                  0.078484324
## Onion1KG
                          -0.01090999 -0.365903988 -0.216704836 -0.033558879
## BeefRound1KG
                                       0.113016788 -0.188465338 -0.031890949
                           0.03251801
## TovotaCorolla
                           0.06377494 -0.033402524
                                                     0.211208614
                                                                  0.002547043
## PreschoolperMonth
                          -0.04026918 -0.223969857 -0.141354533
                                                                  0.149632121
##
                                   PC33
                                                PC34
                                                              PC35
                                                                           PC3
6
                          -0.064962401 -0.008804325 -0.1031045252 -0.05230281
## MealInexpensive
```

## 0	MealFor2	0.065006246	-0.007520308	-0.3322349162	0.02804673
	McMealMcDonalds	-0.069699063	-0.283755824	0.0398559934	-0.00465500
	DomesticBeer	0.211580437	-0.030159226	-0.0359912047	-0.08311171
	ImportedBeer	0.327272753	-0.093213894	-0.1724415893	-0.22760911
	CokeOrPepsi	-0.055144946	0.036467204	0.0713269402	-0.10103821
	Water1Litre	0.012661085	-0.181085572	-0.0300275664	0.06420635
_	Milk1Litre	0.093752250	0.112015515	0.1065387745	-0.31225324
	LoafofBread	0.031567533	0.324661656	-0.1333684849	0.10810344
	Eggs	-0.052177871	0.033648523	-0.1824412839	0.10746719
-	LocalCheese	-0.062748713	0.034490631	-0.0786941555	-0.03000795
_	Water2Litre	-0.116230758	-0.018922784	-0.1282031389	-0.03200577
_	BottleofWine	-0.134045523	-0.002263568	0.0177348161	0.00391276
_	Domestic1LitreBeer	-0.089222397	-0.124854321	0.0619406327	0.23251631
## 0	Imported1LitreBeer	-0.106787051	0.194802726	-0.0669706184	-0.17959121
## 9	Cigarettes20Pack	0.290666713	0.045755872	-0.0525692930	-0.00716284
	OnewayTicket	-0.088399659	-0.089200486	-0.0156687216	0.06080712
	ChickenBreasts	-0.384432118	0.038615674	0.2477270880	-0.10604879
	MonthlyPass	-0.070239735	-0.116783046	0.0886235767	-0.09172906
	Gasoline1Litre	0.186736181	-0.034885590	0.0530572164	0.05159759
	VWGolf	0.097348352	-0.088883206	-0.0571153505	0.09608020
	Apartment1BD	-0.049454801	-0.083977581	-0.0465287759	-0.12806628
	Apartment1BD00C	-0.094444347	-0.069709300	0.0626731962	-0.17688535
	Apartment3BDICC	-0.001253546	-0.111232940	-0.0653177754	-0.18281352
_	Apartment3BD00C	-0.089201119	-0.058434225	0.0630003654	-0.17189304
	BasicUtilities	-0.048697309	0.134312636	-0.0236444010	-0.12955590

## 2	PrepaidMobile1MIn	-0.102805541	-0.106487259	-0.0232991883	0.05585434
	Internet	0.117501114	0.282040864	0.0224841645	0.17605506
	GymFees	-0.080583663	-0.068736026	-0.0267022999	0.08200983
	TennisCourtFeesPerHour	0.003612576	0.022571826	0.0138707559	-0.01235033
_	CinemaPerPerson	0.046412016	-0.072174644	-0.0392207260	-0.11597487
-	PairofJeans	0.254634907	-0.036565608	0.1836932005	-0.06762044
	SummerDress	-0.058352356	0.108424731	-0.1170003374	0.05674012
	NikeRunningShoes	0.023111923	-0.145273463	0.0952717815	-0.07046969
	LeatherShoes	0.102988846	0.100283231	-0.0184172716	0.14338725
## 6	AptPricePerSquareM	-0.006817559	0.045483804	-0.1697975416	0.24760087
	AptPricePerSqMOOC	-0.090281305	0.048436907	0.0311698197	0.14557613
	AvgMnthlyNetSalary	-0.001271912	-0.044011171	0.1321206478	0.23873145
## 7	MortgageInterest	0.112934813	-0.068845627	0.0415371232	-0.02613996
	TaxiStartingFare	-0.214734557	0.091007538	-0.0798837676	0.09906013
## 4	Taxi1KM	0.023870812	-0.024315277	-0.0004946969	0.04565117
## 0	Taxi1HRWaiting	0.109348301	0.334329016	0.0697678069	-0.16488426
## 1	Apples1KG	0.263760121	-0.087018624	0.3652264936	-0.14875139
	Oranges1KG	-0.004475613	-0.181144267	-0.3704191164	0.06175048
	Potato1KG	0.101487539	-0.167434786	0.1161395465	0.04853309
	Lettuce1Head	-0.070260227	0.073381991	0.2578143485	0.10931612
	CappucinoReg	-0.023925624	-0.245584812	0.3180246851	0.27243224
## 0	WhiteRice	0.058805039	0.111759460	0.0007774745	-0.14980650
## 5	Tomato1KG	-0.126448547	-0.046809543	-0.0757809775	-0.02807151
	Banana1KG	-0.256000375	0.150656170	0.0614070004	-0.17822378
	Onion1KG	0.122461085	0.022114949	-0.1325764459	-0.03886432

## 9	BeefRound1KG	0.184138396	-0.038233681	-0.0288132804	0.20391954
	ToyotaCorolla	-0.144509479	0.171287397	0.0397384327	-0.01324970
	PreschoolperMonth	0.145214653	0.375908833	0.2274329291	0.26818687
## 40		PC37	PC38	PC39	PC
	MealInexpensive	-0.0595440933	-0.098654997	0.308243690	0.19665674
	MealFor2	-0.0009676442	0.092594871	-0.089366510	0.08801706
	McMealMcDonalds	0.0117877150	-0.070611569	-0.301706320	-0.03752096
	DomesticBeer	-0.0645025647	-0.033461748	-0.141635285	0.21705814
	ImportedBeer	0.1049101696	0.011859871	-0.032853599	0.11762192
	CokeOrPepsi	0.0962953737	0.269626379	-0.023274139	-0.08336279
	Water1Litre	0.1050357338	0.152832519	0.198526789	-0.02609367
	Milk1Litre	0.1454606088	0.052635230	-0.087948896	0.05901742
	LoafofBread	0.0127883036	-0.121557645	-0.398557298	-0.09129276
## 46	Eggs	-0.1329894739	0.062680435	0.131536001	0.10761211
	LocalCheese	-0.0306690346	0.097471729	0.040277514	0.00628711
	Water2Litre	-0.0340124585	-0.006925366	0.096435207	0.24128424
	BottleofWine	0.1790430564	0.097743436	0.160981005	-0.00975997
	Domestic1LitreBeer	-0.0850370160	0.046417936	-0.231634702	0.16470930
	Imported1LitreBeer	0.0214343846	-0.115956805	0.138517415	-0.17616118
	Cigarettes20Pack	0.0087151353	-0.105019595	0.016882825	-0.34501973
	OnewayTicket	0.2111855997	-0.372115788	-0.047406870	0.20466726
	ChickenBreasts	-0.0430399466	-0.225875678	-0.233753718	-0.16251009
	MonthlyPass	-0.2704257115	0.220545720	-0.058152334	-0.09206372
	Gasoline1Litre	0.0921155225	0.148393616	-0.055773107	-0.01445031
	VWGolf	-0.0715390462	0.031586717	-0.051037548	-0.01910046

## 74	Apartment1BD	0.0150178423	-0.024442498	-0.064796329	-0.15025200
	Apartment1BD00C	0.1578510141	-0.012693128	0.110428556	0.03105673
	Apartment3BDICC	-0.1990978446	-0.010983921	-0.031355708	-0.19655258
	Apartment3BD00C	0.0267469714	0.060366629	0.093670579	-0.00816074
	BasicUtilities	-0.0645413630	-0.062064093	-0.105599175	-0.01447104
## 71	PrepaidMobile1MIn	0.0749119540	0.008361991	0.008867038	-0.02247896
	Internet	0.1803936250	0.068363455	0.131353925	-0.14920477
	GymFees	-0.1376385634	0.060508027	-0.008753786	0.06135770
## 43	TennisCourtFeesPerHour	0.0006416143	-0.016899181	-0.022754906	-0.13027764
## 68	CinemaPerPerson	-0.1957033938	-0.104866333	0.336457583	0.04622273
## 75	PairofJeans	0.2401470851	-0.176282281	-0.006809289	-0.09534365
## 12	SummerDress	-0.0099171874	0.065085006	0.014183381	0.00060015
## 14	NikeRunningShoes	0.0968365086	0.081850201	-0.010434412	0.02398793
## 44	LeatherShoes	-0.2736201907	-0.213121538	0.037196682	0.03863291
## 96	AptPricePerSquareM	0.0588311801	-0.041522872	-0.017650314	-0.06442662
## 01	AptPricePerSqMOOC	0.0561784101	-0.014488819	0.057337197	0.05802894
## 14	AvgMnthlyNetSalary	0.1263352850	-0.107747759	-0.007466480	0.07503196
## 34	MortgageInterest	0.0454033092	0.016055770	-0.011435336	-0.07625274
## 77	TaxiStartingFare	-0.1191111332	0.252453919	0.014826223	0.00965761
## 68	Taxi1KM	0.1688537780	-0.164459743	0.017245611	-0.01526788
## 51	Taxi1HRWaiting	-0.2043479117	0.234312626	-0.123841629	0.06242210
## 45	Apples1KG	-0.0283003268	-0.040900557	-0.036465220	0.28040783
## 23	Oranges1KG	0.2001519693	0.055125096	-0.209223756	-0.23153649
## 80	Potato1KG	-0.1894034939	0.275531448	-0.101181427	-0.01613758
## 89	Lettuce1Head	-0.0869096166	0.054118316	0.182221565	-0.10652085

```
## CappucinoReg
                        -0.0673223694 -0.044398497 0.036439048 -0.21582973
82
## WhiteRice
                         53
                         0.3589861020 0.193769170 -0.020923550 0.26726075
## Tomato1KG
65
## Banana1KG
                         0.0372600785 -0.142787902 -0.026067086
                                                              0.05662426
23
## Onion1KG
                        -0.2891247107 -0.316547223 -0.005468723
                                                              0.08379113
74
                        -0.0080048786 -0.076076184 0.272031973 -0.11079586
## BeefRound1KG
28
                         0.0718451382 -0.079073823 0.082841408
## ToyotaCorolla
                                                             0.00247770
06
## PreschoolperMonth
                         0.18570593
00
##
                                PC41
                                            PC42
                                                        PC43
                                                                    PC44
## MealInexpensive
                         0.191134005 -0.285743907 -0.362197870 -0.139009821
## MealFor2
                         0.077900305
                                     0.107839871
                                                 0.173184356
                                                             0.155323049
## McMealMcDonalds
                        -0.250672892
                                     0.147577399
                                                 0.084525128
                                                             0.030184893
## DomesticBeer
                        -0.046400879
                                                 0.091452693 -0.129881204
                                     0.036600465
## ImportedBeer
                         0.093186037
                                     0.169024352 -0.201644870
                                                             0.040940601
## CokeOrPepsi
                         0.079320539
                                     0.056752702 -0.123839519 -0.008058045
## Water1Litre
                         0.041337709
                                     0.002609029
                                                 0.149970974
                                                             0.083280851
## Milk1Litre
                        -0.012366245 -0.063636164
                                                 0.086767079
                                                             0.138334167
## LoafofBread
                         0.045539690 -0.063853342 -0.178924382
                                                             0.152448511
## Eggs
                        -0.237275486
                                     0.217406996
                                                 0.032148861 -0.149542110
## LocalCheese
                         0.123570438
                                     0.023535674 -0.078146175
                                                             0.175712526
## Water2Litre
                         0.091781761 -0.251707636
                                                 0.125683524 -0.049643292
## BottleofWine
                        -0.033061678 -0.113245718 -0.068717093 -0.123198553
## Domestic1LitreBeer
                        -0.120394556 -0.226399482 -0.031463709
                                                             0.254072568
## Imported1LitreBeer
                                     0.059450268
## Cigarettes20Pack
                        -0.080155114 -0.072372725 -0.145244157
                                                             0.052158668
## OnewayTicket
                         0.226221032
                                     ## ChickenBreasts
                        -0.105113001 -0.124749182 -0.133316351 -0.206828994
## MonthlyPass
                         0.037639776
                                     0.131814446 -0.036803713
                                                             0.217485351
                         0.154722125 -0.063343957 -0.019517314 -0.034239308
## Gasoline1Litre
## VWGolf
                         0.027301535 -0.038294115 -0.080522169 -0.425666785
## Apartment1BD
                         0.067123081 -0.177549921
                                                 0.017691299 0.070285857
## Apartment1BD00C
                        -0.011374513
                                     0.032176897
                                                 0.197852943
                                                             0.125341496
## Apartment3BDICC
                         0.063050567 -0.097506839 -0.076299145 -0.155484870
## Apartment3BD00C
                        -0.048858915
                                     0.059218859
                                                 0.144942336 -0.067338047
## BasicUtilities
                        -0.026183541 -0.104023747
                                                 0.074796736 0.026971564
## PrepaidMobile1MIn
                         0.022114777 -0.114000684
                                                 0.126117295 -0.003798013
## Internet
                        -0.152693559 -0.011187852 -0.066437459
                                                             0.020057883
## GymFees
                         0.196618317 -0.096540720
                                                 0.003377736
                                                             0.010193120
## TennisCourtFeesPerHour -0.062551162 -0.072735771
                                                 0.017662024 -0.057237760
                        -0.462192357 -0.033774799 -0.129929784
## CinemaPerPerson
                                                             0.089368114
## PairofJeans
                        -0.021562833 -0.014846054 -0.056095345 -0.001358553
                         ## SummerDress
```

```
## NikeRunningShoes
                         0.081700264 0.001592781 -0.004581583
                                                             0.033661531
## LeatherShoes
                        -0.230605553 0.097404288
                                                0.019336566 0.058049953
## AptPricePerSquareM
                        -0.127526462 -0.039879508 -0.301510664 -0.041706219
## AptPricePerSqMOOC
                                                0.231452761 -0.143295260
                        -0.055474540
                                    0.123283771
## AvgMnthlyNetSalary
                        -0.056652823 -0.150713577
                                                 0.141717919 0.048533150
## MortgageInterest
                        -0.035571941 -0.044104316
                                                 0.031788872 0.019152567
## TaxiStartingFare
                         0.009903370 0.127439421
                                                0.024625593 -0.008838686
## Taxi1KM
                         0.093115935 -0.003943657 -0.096408098 0.013814157
## Taxi1HRWaiting
                         0.053213523 -0.339150057
                                                 0.227901794 -0.108636050
## Apples1KG
                        -0.170599163 -0.054538880
                                                 0.046481420 -0.120302906
## Oranges1KG
                        -0.149471605 -0.079374392
                                                 0.262843680 -0.196176231
## Potato1KG
                        ## Lettuce1Head
                         ## CappucinoReg
                        ## WhiteRice
                        0.050177200 0.173592979
                                                0.033006683
                                                            0.025169452
## Tomato1KG
                        -0.114282558 -0.008908647 -0.300525036
                                                             0.137795751
## Banana1KG
                        0.073961185
                                    0.058088715 -0.074831327
                                                             0.042375898
## Onion1KG
                                                0.065494885
                        0.283237189
                                    0.163685823
                                                             0.185016962
## BeefRound1KG
                        0.079159584 -0.282208320
                                                 0.217001568
                                                             0.106081258
## ToyotaCorolla
                        -0.152816601 0.061045810
                                                 0.073381221
                                                            0.384446262
## PreschoolperMonth
                        0.063831478 0.152512305
                                                 0.058536912 -0.113615207
##
                                PC45
                                             PC46
                                                          PC47
C48
## MealInexpensive
                        -1.429668e-01 -1.146787e-01 0.0818318544 0.149703
## MealFor2
                        1.847032e-01 -5.331235e-01 -0.4357268485 -0.032694
881
## McMealMcDonalds
                        -7.253750e-02 2.864139e-01 -0.0444397416 -0.055310
870
## DomesticBeer
                        -1.381634e-01 -1.979791e-01 0.2498209356 -0.117969
608
## ImportedBeer
                        3.047286e-01 2.594953e-01 0.0823107985 0.077702
785
                        -6.544329e-03 6.926395e-02 -0.3694542704 -0.165866
## CokeOrPepsi
383
                        -8.967449e-02 -1.395050e-01 0.2908131703
## Water1Litre
                                                               0.011193
173
## Milk1Litre
                        -4.568276e-02 4.987569e-02 -0.0809318698
                                                               0.021036
748
## LoafofBread
                        1.268201e-02 -2.083317e-01 0.2607901474
                                                               0.021252
643
## Eggs
                        -2.043820e-01 1.753505e-01 -0.0532863661
                                                               0.127301
987
                        -9.248091e-02 -6.729444e-03 0.0792883177
## LocalCheese
                                                               0.111948
302
## Water2Litre
                        7.537334e-02 1.353482e-01 0.0230387965 -0.089419
625
## BottleofWine
                        2.380197e-02 -5.695463e-02 -0.0027919955
                                                               0.068469
140
## Domestic1LitreBeer -3.483248e-01 -7.961510e-02 -0.0441517384 0.008953
```

299 ## Imported1LitreBeer	2.409277e-01	1.026461e-03	-0.0664908560	-0.037192
393 ## Cigarettes20Pack 139	-8.753131e-02	-2.427664e-02	-0.0329938359	0.010539
## OnewayTicket 056	-1.135494e-01	1.317134e-01	0.0546624332	-0.204747
## ChickenBreasts 344	2.641471e-01	-1.785054e-01	0.0097622508	0.014012
## MonthlyPass 279	9.240178e-02	6.712351e-02	0.0158611726	0.130819
## Gasoline1Litre 365	5.208334e-02	3.374286e-02	0.0320638273	0.074659
## VWGolf 322	1.411303e-02	-3.716108e-02	-0.1821186240	0.004661
## Apartment1BD 566	-7.517083e-02	7.155024e-02	-0.1591958561	-0.051553
## Apartment1BD00C 616	4.597294e-02	-2.520605e-02	-0.0877831615	-0.055142
## Apartment3BDICC 930	-1.519706e-01	5.662121e-02	0.0317530573	-0.198847
## Apartment3BDOOC 983	-8.356771e-02	-7.475656e-02	0.0984445354	-0.072193
## BasicUtilities 314	5.205591e-02	-2.647275e-02	-0.0353199292	-0.037013
## PrepaidMobile1MIn 686	4.336874e-02	-4.402541e-02	0.0028696401	-0.092793
## Internet 303	-4.488988e-02	7.653944e-02	-0.0343506521	-0.058515
## GymFees 702	6.728238e-02	3.027905e-02	0.1476173960	-0.006728
<pre>## TennisCourtFeesPerHour 041</pre>	-7.738301e-02	5.841847e-02	-0.0171592197	0.097776
## CinemaPerPerson 095	1.879879e-01	-1.308768e-01	0.0971946062	0.020855
## PairofJeans 314	-5.751747e-02	-1.005706e-01	0.0773236199	0.187476
## SummerDress 100	-5.857864e-02	7.397800e-02	-0.0389359959	-0.014016
<pre>## NikeRunningShoes 431</pre>	-7.163429e-05	-5.986325e-02	0.0492356522	0.114890
## LeatherShoes 972	8.215639e-02	1.573585e-01	-0.0314252303	-0.238108
<pre>## AptPricePerSquareM 918</pre>	-7.433921e-02	8.030562e-02	-0.2314526159	-0.062206
<pre>## AptPricePerSqMOOC 465</pre>	-1.601228e-02	-7.344371e-02	0.1192236249	0.131001
<pre>## AvgMnthlyNetSalary 619</pre>	2.258327e-01	1.933657e-01	-0.1826131859	0.597879
## MortgageInterest	3.055757e-02	-4.316197e-03	0.0008473215	-0.016302

560 ## TaxiStartingFare	-8.970245e-02 -6.635214e-02 -0.0246259753 0.109152
623 ## Taxi1KM	-8.451783e-03 -3.626644e-02 0.0298265863 0.009792
380 ## Taxi1HRWaiting	1.640110e-02 3.000014e-01 0.0721381247 -0.003794
897 ## Apples1KG	-1.753952e-01 -1.969933e-01 -0.2359862691 -0.044300
698 ## Oranges1KG	2.154877e-02 9.489208e-03 0.1800137720 0.079658
965 ## Potato1KG	2.583715e-01 -1.062674e-01 0.2113284880 0.025178
914 ## Lettuce1Head	-5.637855e-02 -1.019112e-02 -0.0403438221 0.049275
304 ## CappucinoReg	4.590310e-02 5.433460e-02 -0.0039108570 -0.196229
749 ## WhiteRice	-3.795551e-01 -1.950438e-02 0.0124396300 0.086982
471 ## Tomato1KG	8.098213e-02 1.679991e-01 0.0014605959 -0.203462
151 ## Banana1KG	-1.184182e-02 -3.956731e-02 0.0022417074 0.073646
156 ## Onion1KG	-1.001809e-01 9.325795e-02 -0.1287731034 0.206885
<pre>019 ## BeefRound1KG</pre>	1.972654e-01 4.626566e-05 -0.0134731341 -0.280195
753 ## ToyotaCorolla	2.401470e-03 2.697386e-02 0.1714530900 -0.091844
## PreschoolperMonth	8.540241e-02 -4.628790e-02 0.0694682184 -0.114999
954 ##	PC49 PC50 PC51 PC
## MealInexpensive	0.0487376849 0.163110867 0.059338770 -0.07993896
## MealFor2	0.0257545018 -0.184216303 0.066689584 0.00798829
<pre>## McMealMcDonalds</pre>	0.1015572899 0.005235678 -0.031263539 0.00316691
<pre>35 ## DomesticBeer</pre>	0.2845146882 0.037320810 -0.487336696 0.04939088
10 ## ImportedBeer	-0.2058817273 -0.066458403 0.370486566 -0.02381642
92 ## CokeOrPepsi	-0.2527845579 0.239450437 -0.348731636 -0.12220063
06 ## Water1Litre	0.2909146213 -0.235650972 0.321093479 0.14321453
45 ## Milk1Litre	0.0203897997 -0.066469335 -0.046646558 0.03689426
38 ## LoafofBread	0.0352053633 0.199793941 0.025972640 -0.05030685

70					
78 ## 41	Eggs	-0.0180896449	-0.071189469	0.084200513	-0.02931334
## 40	LocalCheese	-0.0014945957	-0.012121654	-0.031337036	0.01924048
	Water2Litre	-0.1976893621	-0.089626060	-0.184232371	0.05246053
	BottleofWine	0.0215527146	-0.004048836	-0.018392183	-0.02231527
	Domestic1LitreBeer	-0.3285727499	-0.008120029	0.125138294	-0.02436391
## 86	Imported1LitreBeer	0.2118835687	0.014068218	-0.053046313	0.02903860
## 76	Cigarettes20Pack	0.1123058835	0.173095430	-0.021616629	-0.05432583
##	OnewayTicket	-0.1484687766	-0.082804559	-0.002501281	0.00727155
-	ChickenBreasts	0.0083349797	-0.078647020	0.146648242	0.04958553
	MonthlyPass	0.1456894191	0.076057148	-0.046778200	-0.00401108
	Gasoline1Litre	0.0977060648	0.088655537	0.014958356	-0.02647060
	VWGolf	0.0566261553	0.125021755	0.089577640	-0.03112994
	Apartment1BD	0.0241793934	-0.203182408	0.091764405	-0.38664726
## 45	Apartment1BD00C	-0.0892595148	0.379609771	0.195103515	0.06606307
## 61	Apartment3BDICC	0.0388557340	-0.458336524	-0.141805599	-0.07211867
## 35	Apartment3BD00C	-0.0635302840	0.272467011	-0.033450534	0.45605153
## 59	BasicUtilities	-0.0341967088	-0.052758684	0.063121081	0.04599154
## 32	PrepaidMobile1MIn	0.0466422089	-0.040310411	0.053169478	0.04665341
## 08	Internet	0.0829375344	-0.012440376	0.032730018	-0.05779989
## 87	GymFees	0.0434368258	0.133682434	0.005670819	-0.00440623
## 57	TennisCourtFeesPerHour	-0.0130261502	-0.011382301	0.015368268	0.02933389
## 29	CinemaPerPerson	-0.2278623147	0.023822869	-0.109803041	-0.07850849
## 04	PairofJeans	-0.1964906613	-0.118777260	-0.106033637	0.03614368
## 71	SummerDress	-0.0003586595	0.012152113	-0.011795326	0.00284755
##	NikeRunningShoes	-0.0199689181	0.011630644	-0.028623177	0.02318949

24					
31 ## 88	LeatherShoes	0.1619016522	0.134232798	0.122286930	-0.06574189
	AptPricePerSquareM	0.0255144271	-0.078524045	0.041452700	0.48613318
	AptPricePerSqMOOC	-0.0084253220	0.145183732	0.035062445	-0.52592005
## 43	AvgMnthlyNetSalary	0.1732525568	-0.126048243	-0.254641240	0.08431864
## 44	MortgageInterest	0.0162586009	0.005256925	0.012114110	0.00746531
## 45	TaxiStartingFare	0.0461595366	0.001006755	0.021418919	0.00036280
## 15	Taxi1KM	-0.0755842134	-0.011004018	-0.065997164	-0.00838010
## 52	Taxi1HRWaiting	-0.0155781601	0.005690173	0.143625578	0.08846479
## 85	Apples1KG	0.1613125337	0.031880113	0.206551323	-0.03604124
## 48	Oranges1KG	-0.1687607193	0.154369316		-0.00391742
11	Potato1KG	-0.1981097366			0.02743925
55	Lettuce1Head	-0.1275476197		0.021575342	0.01047739
## 03	CappucinoReg	0.0953315531	0.117769808		-0.00408427
94	WhiteRice	-0.0444400743		0.005003077	0.00280970
## 16	Tomato1KG	0.3412597018	0.016318424		
66	Banana1KG	0.0266651867		0.048791091	0.01715363
87	Onion1KG	0.0135499498		-0.064295848	0.05472575
36	BeefRound1KG	-0.0779074203			0.00015460
97	ToyotaCorolla	-0.0532103708			
72	PreschoolperMonth	-0.1474773713		0.028739823	0.02612435
##		PC53	PC54		
	MealInexpensive	-0.040926658 -			
	MealFor2	-0.149240105 -			
	McMealMcDonalds DomesticBeer	-0.081806224 - 0.279333705			
	ImportedBeer	-0.111878366 -			
	CokeOrPepsi	-0.016209489 -			
	Water1Litre	0.057056628			
	Milk1Litre	-0.040042368			

```
## LoafofBread
                           -0.020797659
                                         0.0252725453
## Eggs
                           0.054913401
                                         0.0134162581
## LocalCheese
                           0.042963351
                                         0.0277526774
## Water2Litre
                           0.053364291
                                         0.0081428538
## BottleofWine
                           0.051747043
                                         0.0001994061
## Domestic1LitreBeer
                           -0.122439373
                                         0.0215815288
## Imported1LitreBeer
                           0.042775598 -0.0152382316
## Cigarettes20Pack
                           -0.072972317
                                         0.0078518385
## OnewayTicket
                           0.073718276 -0.0378267292
## ChickenBreasts
                           -0.022629711
                                         0.0048752715
## MonthlyPass
                          -0.012669617 -0.0068084683
## Gasoline1Litre
                           -0.015636303 -0.0022688660
## VWGolf
                          -0.075626756
                                         0.0065703304
## Apartment1BD
                           0.491646180 -0.4825009654
## Apartment1BD00C
                           0.299796026
                                         0.5820337230
## Apartment3BDICC
                           -0.377648948
                                         0.3930530284
## Apartment3BD00C
                           -0.357980190 -0.5081737176
## BasicUtilities
                           0.003340740 -0.0042706840
## PrepaidMobile1MIn
                           0.018473048 -0.0016413591
## Internet
                           -0.038388968
                                         0.0023535455
                                         0.0032998560
## GymFees
                           0.026125079
## TennisCourtFeesPerHour
                           0.021314865
                                         0.0173861707
## CinemaPerPerson
                           0.016682347 -0.0262752857
## PairofJeans
                           0.009170703
                                         0.0110123701
## SummerDress
                           0.011318553
                                         0.0083825410
## NikeRunningShoes
                           0.023830675
                                         0.0045413523
## LeatherShoes
                           0.017910131 -0.0237164093
## AptPricePerSquareM
                           0.260267572
                                         0.0273604923
## AptPricePerSqMOOC
                           -0.217891827 -0.0202651116
## AvgMnthlyNetSalary
                           -0.060017710
                                         0.0404046876
## MortgageInterest
                           -0.003168412 -0.0031590041
## TaxiStartingFare
                           0.047251084
                                         0.0323642396
## Taxi1KM
                           -0.035688948
                                         0.0103333867
## Taxi1HRWaiting
                           0.018575339
                                         0.0082170383
## Apples1KG
                           0.027336814 -0.0064044135
## Oranges1KG
                           0.022652712
                                         0.0190805483
## Potato1KG
                           0.226280209 -0.0054119788
                           0.007574130 -0.0084231517
## Lettuce1Head
## CappucinoReg
                          -0.037291981 -0.0043590933
## WhiteRice
                           0.017867987
                                         0.0118756342
## Tomato1KG
                          -0.196107974 -0.0176161846
## Banana1KG
                           0.001177722 -0.0028967086
## Onion1KG
                          -0.056410869 -0.0248139173
## BeefRound1KG
                          -0.056128592 -0.0283601292
## TovotaCorolla
                          -0.007273613 -0.0108357173
## PreschoolperMonth
                          -0.014084245
                                         0.0026938504
```

#All the varaiables in PCA 1 are negative. hence all contribute to GDP #In PCA 2 DomesticBeer, ImportedBeer, Milk1Liter, LoafofBread, Water2Litre, B ottleofWine, Domestic1LitreBeer, Imported1LitreBeer, abd Cigarettes20Pack hav

```
e positve values
#Whereas MealInexpensive,
                           MealFor2,
                                       McMealMcDonalds, CokeOrPepsi,
                                                                       Water
1Litre, Eggs, LocalCheese, OnewayTicket, and ChickenBreasts have negative va
Lues
#Negative values are important than positive values
#That is GDF is significantly influenced by if only buy negative valued varia
bles
#In the case of 3rd PCA MealFor2,
                                   McMealMcDonalds,
                                                       DomesticBeer.
tedBeer, milk1Litre, Eggs, LocalCheese, BottleofWine, and Domestic1LitreBeer
have negative values
#whereas MealInexpensive, CokeOrPepsi, Water1Litre, Water2Litre, Cigarettes2
OPack OnewayTicket and ChickenBreasts have positive values
#MealInexpensive, CokeOrPepsi, Water1Litre, etc positively influence GDP
```

GDPdataTrainSet.pca.normdata\$rotation # eigen vector / rotation matrix / tranformation matrix

```
##
                             PC1
                                        PC2
                                                   PC3
                                                              PC4
## MealInexpensive
                       0.16129485 0.131439310 -0.097449538 0.098067275
## MealFor2
                       0.16974396  0.096653111  -0.008732676  0.140311935
## McMealMcDonalds
                       0.15692693 0.136291904 0.008695408 0.164603186
## DomesticBeer
                       0.15656357 -0.064088066 0.092619426 0.207671145
## ImportedBeer
                       0.15095548 -0.147636257
                                            0.087924868 0.181757182
## CokeOrPepsi
                       0.14697262 0.233630177 -0.045288505 0.048889105
## Water1Litre
                       ## Milk1Litre
                       0.08962375 -0.113482240 0.248504107 -0.131161985
## LoafofBread
                       0.16734952 -0.028820403 -0.092048120 -0.007123153
## Eggs
                       0.15674918 0.101595579 0.048379691 0.060761199
                       0.13000863 -0.026126058 0.123870874 -0.231295369
## LocalCheese
## Water2Litre
                       0.14952559 -0.062136250 -0.152992668 0.008119030
## BottleofWine
                       0.09714495 -0.288992344 0.166927736 0.100190346
## Domestic1LitreBeer
                       0.09772663 -0.246829519 0.123087345 0.286824154
## Imported1LitreBeer
                       0.07157934 -0.274802478 0.142982357 0.283013582
                       0.13955641 -0.000192280 -0.104306346  0.095247248
## Cigarettes20Pack
## OnewayTicket
                       0.15823541 0.126555400 -0.090518849 0.094341355
## ChickenBreasts
                       ## MonthlyPass
                       ## Gasoline1Litre
## VWGolf
                       0.06454859 -0.035075907
                                            0.322197940 -0.127322319
                       0.16555516 -0.065946946 -0.037464754 -0.095363829
## Apartment1BD
```

```
0.16593329 -0.041431492 -0.065139351 -0.067910991
## Apartment1BD00C
## Apartment3BDICC
                       0.16083960 -0.094831655
                                             0.001924849 -0.148077694
## Apartment3BD00C
                       0.16555802 -0.063295666 -0.033643685 -0.092753376
## BasicUtilities
                       0.09939399 0.215020688
                                             0.006609223 -0.110940980
## PrepaidMobile1MIn
                       ## Internet
                       0.12833704 -0.142298877 -0.142346030
                                                        0.174980749
## GymFees
                       0.11518932 -0.165771927
                                             0.225812292 -0.014430538
## TennisCourtFeesPerHour
                       0.09608928 0.077668261
                                             0.107240490
                                                        0.230762288
                       ## CinemaPerPerson
## PairofJeans
                       0.08353097 0.308405043
                                             0.240947505
                                                        0.062836881
## SummerDress
                       0.04965052 -0.098329723
                                             0.201194756 0.250268529
                       0.08161500 0.121024732 0.245550830
                                                        0.123967412
## NikeRunningShoes
## LeatherShoes
                       ## AptPricePerSquareM
                       0.12398159 -0.032683387
                                             0.182961877 -0.299388219
## AptPricePerSqMOOC
                       0.13080389 -0.005364819
                                             0.165011352 -0.264334577
## AvgMnthlyNetSalary
                       0.16532970 -0.077750523 -0.132897981 -0.006480517
## MortgageInterest
                      -0.09522553 -0.097373803
                                             0.017318535
                                                        0.052175566
## TaxiStartingFare
                       0.14275140 0.181173611
                                             0.053344740
                                                        0.088829482
## Taxi1KM
                       ## Taxi1HRWaiting
                       0.15681662 0.155010241 -0.059193157
                                                        0.100759025
                       0.13330979 -0.206196094 -0.082076173 -0.144657802
## Apples1KG
## Oranges1KG
                       0.14508126 -0.130033829 -0.084859897 -0.172757225
                       0.15775094 -0.117332574 -0.085247461 -0.143578181
## Potato1KG
## Lettuce1Head
                       0.15282023 -0.018601443 -0.019945376
                                                        0.046998826
## CappucinoReg
                       0.15847468 -0.097471159
                                             0.033108350
                                                        0.080624336
## WhiteRice
                       0.14534146 -0.095850558 -0.170191067 -0.065435258
## Tomato1KG
                       0.16121374 -0.019165210 -0.112594208 -0.111445866
## Banana1KG
                       0.15185067 -0.116112767 -0.102868982 -0.171943500
## Onion1KG
## BeefRound1KG
                       ## ToyotaCorolla
                       0.04522050 -0.027734791
                                             0.330983512 -0.090837769
## PreschoolperMonth
                       0.14368983 -0.066729004 -0.138137998 -0.076296181
##
                              PC5
                                          PC6
                                                     PC7
                                                                 PC
8
## MealInexpensive
                      -0.050866908 0.0807728468
                                               0.04366504 -0.054058359
9
                      ## MealFor2
0
## McMealMcDonalds
                       0.006628627 0.0282130045 0.07946622 0.004586222
0
## DomesticBeer
                      -0.121140181 -0.0467425008 -0.01047789
                                                         0.130525119
0
## ImportedBeer
                      -0.112504698 -0.0499001457
                                               0.03991282
                                                         0.152792358
9
## CokeOrPepsi
                      -0.018287169 -0.0370273263
                                               0.11939970
                                                         0.059767022
8
## Water1Litre
                      -0.039105356 0.0114955248
                                               0.13046602
                                                         0.047324697
5
## Milk1Litre
                       0.124779792 -0.2228449669 -0.18383050
                                                         0.017754428
```

## 8	LoafofBread	0.083804450	0.0574637898	0.12840732	0.079586370
	Eggs	0.026557642	-0.1141785794	-0.07041589	0.010557232
-	LocalCheese	0.085888279	-0.0042464143	0.01657762	0.115314365
	Water2Litre	0.062425050	0.0237745324	0.10249317	-0.071724714
	BottleofWine	-0.003739422	-0.0795800725	0.08705888	0.129795417
##	Domestic1LitreBeer	-0.137875743	-0.1682317325	-0.05017518	-0.019927385
## 8	Imported1LitreBeer	-0.101277895	-0.1976765866	-0.02639254	-0.004729357
	Cigarettes20Pack	-0.240009880	-0.1300116054	-0.02624238	-0.232425755
	OnewayTicket	-0.098607168	-0.0481170729	0.10688148	-0.041764975
	ChickenBreasts	0.042637128	0.0263991852	0.05180241	0.079075724
## 8	MonthlyPass	-0.166278971	-0.0091329312	-0.03028172	-0.242845098
## 1	Gasoline1Litre	-0.161432040	-0.2363582258	-0.02047900	0.071853222
## 0	VWGolf	-0.093514860	0.0368180586	0.43985052	-0.233537428
## 2	Apartment1BD	-0.188328121	0.1933800477	-0.07446875	0.017078772
## 4	Apartment1BD00C	-0.187127708	0.1978806465	-0.06792769	0.017339534
	Apartment3BDICC	-0.170124057	0.1630899992	-0.11529893	0.037879573
## 2	Apartment3BD00C	-0.174410251	0.1880585135	-0.10321317	0.049096940
	BasicUtilities	-0.023351115	-0.0411355034	-0.13584266	0.117777040
	PrepaidMobile1MIn	0.003837996	-0.4039543807	-0.21239943	-0.497254890
	Internet	0.016005894	0.0042886665	-0.01543578	-0.029524431
## 4	GymFees	0.013473644	-0.0020577346	-0.23751223	0.036357636
## 6	TennisCourtFeesPerHour	0.246498291	0.0635222722	-0.07493970	0.166674466
## 6	CinemaPerPerson	-0.044181813	-0.0063236676	-0.05438254	0.014607210
## 5	PairofJeans	0.032955926	0.0421087946	-0.12396572	-0.000854134
	SummerDress	0.215690306	0.3568411039	-0.16472303	-0.129458387

## 3	NikeRunningShoes	0.183862104	0.3071177519	-0.08940377	-0.266369131
	LeatherShoes	0.206030875	0.1576456223	-0.12158530	-0.022724919
	AptPricePerSquareM	-0.154281403	-0.0096749405	-0.16068829	0.014962603
	AptPricePerSqMOOC	-0.163069862	0.0041149394	-0.20746397	0.021292924
## 1	AvgMnthlyNetSalary	-0.100098427	0.1338088393	0.04730733	0.051040466
## 9	MortgageInterest	0.098820422	0.2512302195	0.00746212	-0.380137872
## 2	TaxiStartingFare	0.017803285	-0.0749510625	0.07677888	0.042394533
## 6	Taxi1KM	0.053493525	-0.0627519302	-0.02836553	-0.119799424
## 0	Taxi1HRWaiting	-0.019771893	-0.0105582544	0.13891871	-0.035231478
	Apples1KG	0.200615887	-0.0476467654	0.14045827	0.009405806
## 2	Oranges1KG	0.223719656	-0.0367064999	0.05869990	-0.003295534
## 3	Potato1KG	0.155906354	-0.0623089280	0.03087516	-0.113950142
## 6	Lettuce1Head	0.165991475	-0.1287779240	0.07481916	0.090556781
## 8	CappucinoReg	0.021309577	-0.0006878552	0.01330612	0.213479321
## 7	WhiteRice	0.164999787	0.0414504712	0.09624321	0.010116093
## 2	Tomato1KG	0.199325469	0.0078363478	-0.01763858	0.002251798
## 3	Banana1KG	0.170280963	-0.1851219268	-0.05883164	-0.239044660
## 1	Onion1KG	0.141676353	-0.0674724536	0.07054741	-0.065170290
## 0	BeefRound1KG	0.227202984	-0.1067664671	0.06947581	0.047697744
	ToyotaCorolla	-0.181659289	0.0859420782	0.51563402	-0.159622421
## 3	PreschoolperMonth	-0.195688191	0.1759223667	-0.16812881	-0.141611944
## 12		PC9	PC10	PC11	L PC
	MealInexpensive	0.006949559	-0.0001871233	0.010421624	-0.02516381
	MealFor2	0.070842999	-0.0432963829	-0.078253506	0.04278753
	McMealMcDonalds	0.055695792	-0.0516856287	-0.068456220	0 -0.00688109

## 04	DomesticBeer	0.015407198	0.0839698710	-0.053304798	-0.14124265
## 09	ImportedBeer	0.018856664	0.0812309667	-0.041512480	-0.10738861
	CokeOrPepsi	-0.012461240	0.0426586949	0.064927131	-0.14943738
	Water1Litre	0.039765894	0.0141193425	0.176710093	-0.09295454
## 01	Milk1Litre	0.310801171	-0.2884826190	0.055995848	0.04116279
## 81	LoafofBread	0.163461503	-0.0716033835	-0.041424171	-0.05282036
## 60	Eggs	0.147241580	-0.1360798695	-0.082555051	-0.23880948
## 58	LocalCheese	0.094915351	-0.1332366045	0.007865879	0.03758349
56	Water2Litre		-0.1513757449	0.056367920	-0.05256037
63	BottleofWine		-0.1796620709	0.057105442	0.05385192
05	Domestic1LitreBeer	-0.063806588	0.1376545480	0.092795149	
## 57	Imported1LitreBeer	-0.054764516	0.1419432538	0.060279167	0.04895519
## 91	Cigarettes20Pack	0.121987645	0.0237418709	0.378823089	0.05986333
## 25	OnewayTicket	0.060210980	0.0291535352	0.111607789	0.12783717
94	ChickenBreasts	0.215622001		0.022940264	
49	MonthlyPass	-0.033180652	0.0392490025	0.116478103	0.27974116
91	Gasoline1Litre	0.044146484	0.0979160392		0.01355991
21	VWGolf		-0.1824848820		
29	Apartment1BD		-0.0146201837 -0.0259664618		
20	Apartment1BD00C Apartment3BDICC		-0.0028066759		
35	Apartment3BD00C		-0.0254518412		
69	BasicUtilities		-0.0310000342		
58	PrepaidMobile1MIn		-0.2242327089		
44	Internet		-0.2965414687		
90	The contract	0.00-00002	0.2JUJT1400/	0.23/0/2201	0.20300032

## 22	GymFees	-0.215690858	-0.1079144806	-0.130480046	-0.05021911
	TennisCourtFeesPerHour	-0.163643049	0.0691906988	-0.316785247	0.35700015
## 87	CinemaPerPerson	-0.060975367	0.0826649380	-0.063382021	0.08536108
	PairofJeans	-0.072537974	-0.0324611978	0.049768127	-0.01250691
## 58	SummerDress	-0.048400820	0.1494891818	0.270620437	0.16949390
## 93	NikeRunningShoes	0.048916777	-0.2414835299	0.142095015	-0.01356682
## 65	LeatherShoes	-0.015854328	-0.1443914397	0.055372991	-0.03117101
## 93	AptPricePerSquareM	0.163242141	0.1810367905	0.005872004	0.11823936
## 65	AptPricePerSqMOOC	0.212890334	0.1407593546	-0.004010940	0.06516592
## 15	AvgMnthlyNetSalary	-0.082217685	0.0555842556	0.044381192	-0.11267349
## 77	MortgageInterest	0.335877183	0.3328180455	-0.284548453	-0.36658312
## 14	TaxiStartingFare	0.042713507	0.1573819991	-0.123201128	0.04110808
84	Taxi1KM	-0.063723019	0.0083238048		0.31794224
99	Taxi1HRWaiting	0.084254037	0.1285183191	-0.048288609	0.14079138
34	Apples1KG	-0.087690840	0.1258395057	0.037132827	0.15790382
## 20	Oranges1KG	-0.135047961	0.0927830033	0.149709389	0.05827562
## 86	Potato1KG	-0.034096415	-0.0243281276	-0.012889377	-0.04060075
38	Lettuce1Head	0.175042916	0.0056063175	0.185193389	-0.00883750
41	CappucinoReg		0.0071722606		
47	WhiteRice	-0.117367786		-0.053251969	
57	Tomato1KG	-0.088028702		0.089799307	
00	Banana1KG		0.3814396932		
11	Onion1KG		-0.0778654727		
21			0.2041669981		
## 62	ToyotaCorolla	-0.117183398	-0.0324423170	-0.055386258	0.11226596

## 37	PreschoolperMonth	-0.137876713	-0.0100181605	0.048926212	0.05953687
##		PC13	PC14	PC15	PC1
6 ## 9	MealInexpensive	0.063337798	-0.078790062	0.021005111	-0.127639484
	MealFor2	-0.021714138	-0.078339142	-0.030198078	0.049507888
	McMealMcDonalds	0.065303788	0.179456015	0.039231427	0.006176619
_	DomesticBeer	0.067368098	-0.086717378	-0.059928495	-0.066854500
## 5	ImportedBeer	0.064307249	-0.036826632	-0.055357672	-0.057586028
	CokeOrPepsi	0.067653222	0.123141318	0.089895483	0.102514992
	Water1Litre	-0.045107088	0.051495246	0.167743355	0.183963675
-	Milk1Litre	-0.125631623	-0.291932483	-0.003345691	-0.167708791
_	LoafofBread	0.013586084	0.012733875	0.058264509	-0.002401556
	Eggs	0.015791767	0.192075035	0.166865616	-0.088553667
_	LocalCheese	0.475828538	0.225235045	0.018462332	-0.221531357
_	Water2Litre	-0.271464800	-0.062585190	0.309570059	0.142017746
	BottleofWine	0.060564859	0.028941934	-0.044885644	-0.061070963
## 5	Domestic1LitreBeer	-0.009204659	0.087917881	0.027744252	0.028236790
## 2	Imported1LitreBeer	-0.063739674	0.187063259	0.126399562	0.006360581
	Cigarettes20Pack	0.048437046	-0.012566700	0.024023355	0.164950480
	OnewayTicket	0.065905804	-0.123590169	-0.091254738	-0.072808261
	ChickenBreasts	0.016418423	0.185733566	0.094889568	-0.047977874
	MonthlyPass	0.002308145	-0.144618953	0.096648347	-0.059274380
	Gasoline1Litre	-0.194233596	0.230339825	0.258003301	-0.022678519
	VWGolf	0.060125721	-0.174820637	0.016996922	-0.026072838
_	Apartment1BD	0.049406933	-0.002438621	-0.060771979	0.079094228
	Apartment1BD00C	0.062866792	0.014286184	-0.018947984	0.073092139

## 3	Apartment3BDICC	0.021766902	0.027414766	-0.094770234	0.060749157
	Apartment3BD00C	0.046416451	0.048083049	-0.043804328	0.044287694
- ## 4	BasicUtilities	-0.163311761	-0.161926207	0.248040325	-0.273372229
	PrepaidMobile1MIn	0.195477486	-0.022540237	0.016391864	-0.192454672
## 4	Internet	-0.121008610	0.046403433	-0.142720411	0.099589942
## 6	GymFees	-0.110659082	0.047410800	0.028809447	0.437899452
## 1	TennisCourtFeesPerHour	0.338011090	-0.282616687	0.400009295	0.123903306
## 3	CinemaPerPerson	-0.052831442	-0.090621492	-0.045742281	-0.153762817
## 3	PairofJeans	-0.057232072	-0.028614836	-0.058780597	0.154542410
## 4	SummerDress	-0.216222700	0.191879162	0.133532547	-0.237552728
## 9	NikeRunningShoes	-0.017230905	0.123444347	-0.212454533	0.001063545
## 2	LeatherShoes	-0.022692975	-0.031096965	-0.110562584	0.058173549
## 9	AptPricePerSquareM	-0.103840300	-0.059821778	0.005845261	-0.004547719
## 2	AptPricePerSqMOOC	-0.082000758	-0.029506020	0.071214210	-0.031376120
## 3	AvgMnthlyNetSalary	0.040962481	0.003392056	-0.083039063	-0.055036053
## 4	MortgageInterest	0.033525206	-0.189915251	0.236537978	-0.081803050
2	TaxiStartingFare	-0.118152475	-0.142777778	-0.367774183	-0.092544236
## 2	Taxi1KM	-0.342269896	0.160614031	-0.064593877	-0.039641000
## 7	Taxi1HRWaiting	-0.034995036	0.002995050	-0.246347256	-0.022085231
## 9	Apples1KG	-0.089890161	0.186306332	0.048554578	-0.017078997
## 8	Oranges1KG	-0.047850785	-0.127012279	-0.096912238	-0.010950039
## 2	Potato1KG	-0.072379232	0.112742940	0.027892670	0.020243816
## 2	Lettuce1Head	0.010781730	-0.310104749	0.018923607	0.306256834
3	CappucinoReg	-0.152489102	-0.235956593	-0.058012935	-0.328304863
## 0	WhiteRice	-0.096491333	0.060329466	0.052295972	-0.187372021

```
## Tomato1KG
                           0.022597958 -0.117776280
                                                     0.036090775 0.091823456
7
## Banana1KG
                           0.100839721 -0.001140093 -0.213754731
                                                                  0.201170384
6
## Onion1KG
                          -0.004862221 0.041094026
                                                     0.085206853
                                                                  0.114264602
5
## BeefRound1KG
                           0.232199975
                                        0.235599941 -0.079899376 -0.058869278
## ToyotaCorolla
                          -0.096585574 -0.010655904
                                                     0.117001922 -0.000701279
9
## PreschoolperMonth
                           0.244883370 -0.023337141
                                                     0.117770868 -0.045884081
6
##
                                  PC17
                                               PC18
                                                            PC19
                                                                         PC20
## MealInexpensive
                           0.035179223
                                        0.063901020 -0.171389409
                                                                  0.022206497
## MealFor2
                          -0.049844673
                                                     0.038791697
                                        0.033416475
                                                                  0.106460094
## McMealMcDonalds
                           0.104208960
                                        0.176144674 -0.216460122 -0.014843481
## DomesticBeer
                          -0.057146004
                                        0.057685748 -0.055739101
                                                                  0.156733633
## ImportedBeer
                          -0.069957965 -0.003462511 -0.151083820
                                                                  0.068964991
## CokeOrPepsi
                           0.014823027
                                        0.068810066 -0.028751704 -0.199133405
## Water1Litre
                           0.026532305
                                        0.159112531
                                                     0.019257403 -0.221921718
## Milk1Litre
                                        0.230524971 -0.080681556
                          -0.042812417
                                                                  0.041820513
## LoafofBread
                          -0.113456865 -0.121737449
                                                     0.063324090 -0.182945892
## Eggs
                          -0.175015307
                                        0.125435177
                                                     0.295971390 -0.041452683
## LocalCheese
                           0.352914042
                                        0.103326278 -0.138173078 -0.034632525
## Water2Litre
                          -0.123609434
                                        0.001372733 -0.031165641 -0.067730654
## BottleofWine
                           0.124072371
                                       -0.197941849
                                                     0.475810065 -0.049827480
## Domestic1LitreBeer
                           0.077073607 -0.088573957
                                                     0.108934185
                                                                  0.096545581
## Imported1LitreBeer
                           0.198178436 -0.101578216
                                                     0.050919558 -0.184296433
## Cigarettes20Pack
                          -0.059700047
                                        0.124442769 -0.013457176
                                                                  0.012689040
## OnewayTicket
                           0.144490695 -0.040216074
                                                     0.076891304
                                                                  0.090890810
## ChickenBreasts
                           0.001411996
                                        0.006064748 -0.068463885
                                                                  0.265124517
## MonthlyPass
                           0.112734507
                                        0.138659773
                                                     0.232002840
                                                                  0.172022511
## Gasoline1Litre
                          -0.085298957 -0.296645003
                                                     0.005641645
                                                                  0.233728108
## VWGolf
                          -0.034388733
                                        0.102161606
                                                     0.029286959
                                                                  0.072387544
## Apartment1BD
                          -0.033141492 -0.080400792 -0.005025633 -0.023484130
## Apartment1BD00C
                          -0.068677678 -0.079632866 -0.004042951
                                                                  0.031138514
## Apartment3BDICC
                          -0.015557833 -0.140850809
                                                     0.013008082 -0.114669003
## Apartment3BD00C
                          -0.066006478 -0.102195683 -0.004928420 -0.046071284
## BasicUtilities
                           0.303024999
                                        0.063278794
                                                     0.045300376 -0.020523580
## PrepaidMobile1MIn
                          -0.134536395 -0.312774185 -0.240630088 -0.091329294
## Internet
                                        0.130361165 -0.194158380 -0.063304139
                           0.143298264
## GymFees
                           0.157730351
                                        0.129955116 -0.139845959
                                                                  0.237004128
## TennisCourtFeesPerHour -0.155165336
                                        0.036218862
                                                     0.030926967 -0.113540588
## CinemaPerPerson
                          -0.021955448
                                        0.014652477 -0.013946392 -0.031106779
## PairofJeans
                           0.120985851 -0.228094499
                                                     0.054591090 -0.184994752
## SummerDress
                          -0.129593614 -0.019299968 -0.275859342 -0.036909342
## NikeRunningShoes
                          -0.029765162
                                        0.019174160
                                                     0.166484488 -0.006684213
## LeatherShoes
                           0.011531855 -0.231814405
                                                     0.128324680
                                                                 0.133585842
## AptPricePerSquareM
                           0.009914883
                                        0.021206118 -0.050224743 -0.064838730
## AptPricePerSqMOOC
```

```
## AvgMnthlyNetSalary
                       -0.093591601 -0.049678388 -0.064677583 0.050632168
## MortgageInterest
                        0.377678241 -0.074689626 0.078722968 0.018092045
## TaxiStartingFare
                        0.188353268 -0.185968596 -0.207537921 -0.095502062
## Taxi1KM
                        0.223241265
                                    0.316090524 0.192633307
                                                           0.054164621
## Taxi1HRWaiting
                        0.030290650 -0.021119694
                                                0.143614756 -0.059988197
## Apples1KG
                        0.066226984 -0.021381840 -0.127153373 -0.176942478
## Oranges1KG
                        0.067838266  0.035465694  -0.007511716  -0.026518263
## Potato1KG
                       -0.066012650 -0.069015923 -0.018861492 -0.124482988
## Lettuce1Head
                        0.149575448 -0.116103250 -0.181314881 0.196537874
                       ## CappucinoReg
## WhiteRice
                       -0.187709983 -0.121519093
                                                0.022125543 0.466609211
                        0.024765053 -0.201213331 0.111209367 0.078983517
## Tomato1KG
## Banana1KG
                       -0.310282469
                                    0.260830086
                                                0.107511776 -0.072726146
## Onion1KG
                        0.083645926 -0.185691200
                                                0.050682014 -0.160904432
## BeefRound1KG
                       0.001164197
                                    0.108074135
                                                0.024425500
                                                            0.173488340
## ToyotaCorolla
                       -0.074492744 -0.053112878 -0.146294168 -0.013936426
## PreschoolperMonth
                       -0.013028309 0.108116515 0.062123933 0.033826513
##
                                           PC22
                               PC21
                                                       PC23
                                                                    PC
24
## MealInexpensive
                        0.034634120 0.0939173254 -0.276981606 0.15070715
54
## MealFor2
                        0.032476526 0.0439322843 0.028621331 -0.15635823
99
## McMealMcDonalds
                        32
## DomesticBeer
                        0.058657253  0.0907248183  0.219835444  0.12618460
12
                      0.022113244 0.0637525089 0.081735494 0.12154316
## ImportedBeer
80
                       0.208955936 -0.0449912320 0.034406434 0.15666463
## CokeOrPepsi
86
## Water1Litre
                       0.201222912 -0.1238319714 0.078642637 0.11604706
40
## Milk1Litre
                        0.076608821 -0.0187693447 -0.226447115 0.08731633
94
                        0.022554103 -0.0017317246 -0.133192468 -0.12131853
## LoafofBread
39
## Eggs
                       92
## LocalCheese
                       0.092259446 -0.2060346471 0.214148789 -0.32972523
98
## Water2Litre
                       -0.203608482 -0.2630742573 0.008598669 -0.19446637
37
## BottleofWine
                       -0.017949700 0.3113971723 -0.034669241 -0.12456813
91
## Domestic1LitreBeer 0.076329567 -0.1749403523 0.082447285 0.14517873
91
## Imported1LitreBeer 0.087115229 -0.3414999853 -0.175282310 0.08862265
## Cigarettes20Pack -0.051754114 0.0889468063 -0.088401070 -0.10694575
```

71 ##	OnewayTicket	-0.193896357	-0.0656697894	0.056242606	-0.13114823
62 ## 25	ChickenBreasts	-0.088859628	0.0031791974	0.123554985	0.18591439
	MonthlyPass	-0.312759995	0.0479728739	0.112412210	-0.05654973
	Gasoline1Litre	-0.119408351	-0.0474382484	0.042864503	-0.14363240
	VWGolf	0.065993035	-0.1588539429	0.079837745	-0.06384338
## 33	Apartment1BD	0.031423348	0.0443263887	-0.043191475	-0.00309660
## 28	Apartment1BD00C	-0.007262661	0.1117231497	0.005214384	-0.01035409
## 88	Apartment3BDICC	0.008499105	0.0509363504	-0.025238689	-0.00205489
## 81	Apartment3BD00C	-0.009795657	0.1066264090	0.018100065	-0.02539651
## 81	BasicUtilities	-0.071842759	0.1599239467	0.051017876	0.07318489
## 07	PrepaidMobile1MIn	0.165433432	0.0827100723	0.076249278	0.00369966
## 44	Internet	-0.381254687	-0.0088347236	0.338871727	0.01572174
## 80	GymFees	0.029410217	-0.0240019600	-0.229543787	-0.16337317
## 03	TennisCourtFeesPerHour	-0.121945535	-0.0334057589	0.040312564	0.15285913
## 16	CinemaPerPerson	0.052473978	-0.2530752618	0.051134278	-0.18908234
## 28	PairofJeans	-0.090753205	-0.0013096737	-0.049315116	-0.20966470
## 05	SummerDress	0.058259576	0.2530757180	0.169528614	-0.19900842
## 69	NikeRunningShoes	-0.119516543	-0.2326428702	0.058158359	0.33306793
## 41	LeatherShoes	0.252415750	-0.1240734756	-0.019710632	-0.00022928
## 84	AptPricePerSquareM	-0.022521544	-0.0778492278	0.095410425	0.14677077
## 62	AptPricePerSqMOOC	-0.016224034	-0.0314370006	0.213097527	0.17106000
## 16	AvgMnthlyNetSalary	0.144750801	-0.0220716744	-0.040645779	-0.02949975
## 37	MortgageInterest	0.038468376	0.0423939421	-0.053063967	-0.04752666
## 64	TaxiStartingFare	-0.255049708	-0.0320620228	-0.317059855	0.09057251
##	Taxi1KM	0.354482721	0.1406098455	0.049308527	0.06301244

```
84
                         0.153993150 -0.0095250792 0.155828760 -0.05978448
## Taxi1HRWaiting
75
## Apples1KG
                        10
## Oranges1KG
                         0.005866207 -0.0065731468 -0.042776967 0.01391550
48
## Potato1KG
                        -0.001285302  0.1047659994  -0.045267448  0.08506714
24
## Lettuce1Head
                         0.242123662  0.2196565092  0.146217455  -0.06422780
77
                         0.031350011 -0.0878672746 -0.006589424 -0.13947748
## CappucinoReg
55
## WhiteRice
                         0.051079605 -0.2658654072 -0.090498687 0.01824607
62
## Tomato1KG
                         0.003260612 -0.0335273647 0.042125128 0.04097484
77
## Banana1KG
                        39
## Onion1KG
                        -0.063216729 0.0729085029 0.110302351 0.27921383
26
                        -0.237587146  0.1565400859  -0.131168398  0.17765971
## BeefRound1KG
81
## ToyotaCorolla
                         0.035160751 0.1977811624 -0.055631363 0.09153193
75
## PreschoolperMonth
                         0.030662706 -0.0868724534 -0.292473294 0.03857151
52
##
                                PC25
                                            PC26
                                                        PC27
                                                                     PC28
                         0.166303094 -0.219564379 -0.160747112 -0.140141454
## MealInexpensive
## MealFor2
                         0.026260603 -0.038975324 -0.129918826
                                                              0.006711220
## McMealMcDonalds
                        -0.176062179
                                     0.041321826 -0.277819790 -0.336926163
## DomesticBeer
                        -0.032542008 -0.082028171 -0.088984383
                                                              0.074189289
## ImportedBeer
                        0.145955883
## CokeOrPepsi
                         0.219180621 0.191844306 -0.075299946
                                                              0.119725774
## Water1Litre
                         0.199573954 0.180678781
                                                 0.061317687 -0.088617390
## Milk1Litre
                         0.257496051 0.041228254
                                                  0.202564243 -0.169050767
## LoafofBread
                        -0.167631317
                                     0.191652420
                                                  0.226019828 -0.036980580
                        -0.012848933 -0.134714835
                                                  0.199548800 0.335921972
## Eggs
## LocalCheese
                        -0.067634945 -0.152932943 -0.002975556 0.073908406
## Water2Litre
                        -0.215042112 -0.158501869 -0.132781916
                                                              0.027233946
## BottleofWine
                         0.013419595
                                     0.262942506 -0.343854905 -0.191717696
## Domestic1LitreBeer
                         0.084511261 -0.125279184
                                                  0.148964433 -0.107040031
## Imported1LitreBeer
                        -0.043814213 -0.207128201
                                                  0.113858245 -0.035351935
## Cigarettes20Pack
                        -0.164758380 0.051810636
                                                  0.001078488 0.093479294
## OnewayTicket
                                     0.295566019
                         0.171174606
                                                  0.207278955 -0.021267468
## ChickenBreasts
                         0.183357657 -0.033393747 -0.057774315
                                                              0.205575000
## MonthlyPass
                         0.162482293 -0.100081262
                                                  0.002770762 0.060074702
## Gasoline1Litre
                         0.036442947 -0.072350006 -0.021859300 -0.318010658
## VWGolf
                        -0.037247485 -0.006178150
                                                  0.248624311 -0.069535433
                        -0.033981402 -0.082179069
## Apartment1BD
                                                  0.121556327 -0.060636284
```

```
-0.042706824 -0.097099017
                                                       0.165900732 -0.089497521
## Apartment1BD00C
## Apartment3BDICC
                            0.011005405 -0.001226869
                                                       0.071719151 -0.043417696
## Apartment3BD00C
                           -0.026719852 -0.061337141
                                                       0.149562605 -0.046876678
                           -0.256823864
## BasicUtilities
                                         0.087892931
                                                       0.030293105 -0.050603185
## PrepaidMobile1MIn
                           -0.057320271
                                         0.111580587 -0.070130467
                                                                    0.150085503
## Internet
                            0.178633943 -0.048425069
                                                       0.005805862 -0.145206497
## GymFees
                                                     -0.042628243
                            0.079915226
                                         0.332173628
                                                                    0.301981876
  TennisCourtFeesPerHour -0.038099108
                                         0.060440998
                                                      0.058130395 -0.030817331
## CinemaPerPerson
                            0.006855607
                                         0.279095225
                                                      0.035523089 -0.108955897
## PairofJeans
                                        -0.236248718 -0.023710855
                            0.163143367
                                                                    0.239066816
## SummerDress
                            0.129557443
                                         0.065720774
                                                      0.124377114 -0.082709638
## NikeRunningShoes
                           -0.370695520
                                         0.065543662 -0.062291060 -0.008185126
## LeatherShoes
                            0.203046478 -0.124796505 -0.094691989 -0.084714384
## AptPricePerSquareM
                           -0.065205645
                                         0.099989898 -0.168247698
                                                                    0.050188854
## AptPricePerSqMOOC
                                         0.108960522 -0.120410482
                           -0.084081737
                                                                    0.037368448
## AvgMnthlyNetSalary
                            0.046008286
                                         0.100185204
                                                      0.167700847
                                                                    0.012849956
## MortgageInterest
                            0.068941683
                                         0.093551965 -0.016822303
                                                                    0.044262728
## TaxiStartingFare
                           -0.102443239
                                         0.033119778
                                                      0.091617927
                                                                    0.063220907
## Taxi1KM
                           -0.178936729 -0.118386100
                                                       0.109365977
                                                                    0.012975830
## Taxi1HRWaiting
                            0.018320432
                                         0.073937342 -0.080007255
                                                                    0.088060616
## Apples1KG
                           -0.042528381
                                         0.052784406 -0.040916209
                                                                    0.179225295
## Oranges1KG
                            0.219301010 -0.243423530 -0.168035064
                                                                    0.034484717
## Potato1KG
                            0.088031682 -0.005509736
                                                       0.151760805 -0.180571884
## Lettuce1Head
                           -0.298807804 -0.144413233
                                                      0.057004566 -0.117117654
## CappucinoReg
                           -0.015331036 -0.124663204 -0.136218311
                                                                    0.153500301
## WhiteRice
                           -0.032538691
                                         0.160949430 -0.135242773
                                                                    0.077774575
## Tomato1KG
                           -0.070921124 -0.104040399
                                                      0.144973021
                                                                    0.114613193
## Banana1KG
                            0.006396967 -0.053691532 -0.114650930 -0.202258559
## Onion1KG
                            0.105590753
                                         0.054421187 -0.131308668 -0.090682820
## BeefRound1KG
                           -0.054678421
                                         0.025462918
                                                      0.187380848 -0.032823420
  ToyotaCorolla
                            0.048334643 -0.066778955 -0.115574381
                                                                    0.157933750
## PreschoolperMonth
                            0.025340848 -0.106198636 -0.195999446 -0.075057801
##
                                  PC29
                                               PC30
                                                             PC31
                                                                          PC32
## MealInexpensive
                            0.21283265
                                        0.141511951
                                                     0.123788697 -0.112635608
## MealFor2
                            0.10533475
                                      -0.009152441
                                                     0.120378607 -0.185963301
## McMealMcDonalds
                            0.11034018
                                        0.022134054 -0.199016774 -0.193836597
## DomesticBeer
                           -0.06756192 -0.016334758 -0.068960052
                                                                   0.056297549
## ImportedBeer
                                        0.136728136 -0.053053964
                           -0.12510596
                                                                   0.168346568
## CokeOrPepsi
                           -0.01045915
                                        0.103279782
                                                     0.015293365
                                                                   0.198343395
## Water1Litre
                           -0.10501459
                                        0.002826941 -0.138333530
                                                                   0.090246308
## Milk1Litre
                           -0.02904283 -0.048252887 -0.002010343
                                                                   0.010186069
## LoafofBread
                            0.20491150
                                        0.224614304 -0.130141666
                                                                   0.166515359
## Eggs
                            0.16255686 -0.112376738
                                                     0.056666672
                                                                   0.050888227
## LocalCheese
                           -0.12379095 -0.034761827
                                                     0.133414936 -0.018019599
## Water2Litre
                           -0.26036351
                                        0.141574218 -0.051047905
                                                                   0.029142376
## BottleofWine
                           -0.17178358
                                        0.044090636 -0.047679079
                                                                   0.025849200
## Domestic1LitreBeer
                           -0.05556083
                                        0.007741198
                                                     0.006802694 -0.058077422
## Imported1LitreBeer
                            0.17220975
                                        0.065298643
                                                     0.035359302 -0.066892349
## Cigarettes20Pack
                           -0.31592687 -0.222583935
                                                     0.259675908 -0.133440746
## OnewayTicket
                            0.09129070 0.032260374
                                                     0.263871882 -0.041526356
```

```
## ChickenBreasts
                      -0.12609045 -0.204942614 -0.069071949
                                                       0.003382719
                       ## MonthlyPass
                                                       0.179360356
## Gasoline1Litre
                       0.06984504 -0.195059711
                                            0.192698001
                                                       0.227032317
                      -0.08300842 -0.037961056 -0.261462595 -0.060399966
## VWGolf
## Apartment1BD
                       0.01754071 -0.058308600 -0.056399903 0.063359082
## Apartment1BD00C
                      -0.03172772 -0.033648644 -0.058344203 -0.084098522
## Apartment3BDICC
                       0.04303481 0.030566770 0.079553441 0.157228380
                      ## Apartment3BD00C
## BasicUtilities
                      -0.03422107
                                 0.053109025
                                            0.094738475 -0.065180667
## PrepaidMobile1MIn
                       0.03804020 0.097301883 -0.072040492
                                                      0.051376283
## Internet
                       ## GymFees
                       0.09730094 -0.059679928
                                            0.046039114 -0.033984223
## TennisCourtFeesPerHour -0.13200384 0.003985777
                                            0.176602538 -0.042650703
## CinemaPerPerson
                       0.15750489 -0.299514311 -0.120715535 0.111572287
## PairofJeans
                       ## SummerDress
                      -0.06971133 -0.100712086 -0.134439849 0.042169809
## NikeRunningShoes
                       0.19769063 -0.094866528
                                            0.208645396 0.152409525
## LeatherShoes
                                            0.169500399
                      -0.27006105 0.274911092
                                                       0.097770690
## AptPricePerSquareM
                       0.13959917
                                 0.119379499 -0.037337085 -0.052869807
## AptPricePerSqMOOC
                      ## AvgMnthlyNetSalary
                                            0.140363679 0.043746736
                      -0.04010222 0.118838102
## MortgageInterest
                      -0.01799618 -0.042332187
                                            0.078313922 0.025288312
## TaxiStartingFare
                      -0.39119798 -0.098896799 -0.060193108 0.128978833
## Taxi1KM
                      0.087980636
## Taxi1HRWaiting
                       0.17419415 -0.101883693
                                            0.042593174 -0.301417303
## Apples1KG
                       0.05009582 0.110318551
                                            0.132704934
                                                       0.184241925
## Oranges1KG
                       0.13276578 -0.120664004
                                            0.134998593
                                                       0.224756079
## Potato1KG
                      ## Lettuce1Head
                       0.24454830 -0.011765371 -0.019330990
                                                       0.154443400
                       0.06294036 -0.158915686
                                            0.054945311 -0.045256096
## CappucinoReg
## WhiteRice
                      ## Tomato1KG
                       0.04887614 -0.224359412 -0.104934932 -0.195996817
## Banana1KG
                      -0.07721317
                                 0.038880431
                                            0.038697511
                                                       0.078484324
## Onion1KG
                      -0.01090999 -0.365903988 -0.216704836 -0.033558879
## BeefRound1KG
                       ## ToyotaCorolla
                       0.06377494 -0.033402524
                                            0.211208614
                                                       0.002547043
## PreschoolperMonth
                      -0.04026918 -0.223969857 -0.141354533 0.149632121
##
                             PC33
                                        PC34
                                                    PC35
                                                               PC3
6
                      -0.064962401 -0.008804325 -0.1031045252 -0.05230281
## MealInexpensive
8
## MealFor2
                       0.065006246 -0.007520308 -0.3322349162 0.02804673
0
## McMealMcDonalds
                      -0.069699063 -0.283755824 0.0398559934 -0.00465500
8
## DomesticBeer
                       0.211580437 -0.030159226 -0.0359912047 -0.08311171
                      0.327272753 -0.093213894 -0.1724415893 -0.22760911
## ImportedBeer
5
## CokeOrPepsi
                      -0.055144946   0.036467204   0.0713269402   -0.10103821
```

```
1
                     0.012661085 -0.181085572 -0.0300275664 0.06420635
## Water1Litre
## Milk1Litre
                      0.093752250 0.112015515 0.1065387745 -0.31225324
## LoafofBread
                     -0.052177871 0.033648523 -0.1824412839 0.10746719
## Eggs
                     ## LocalCheese
                    -0.116230758 -0.018922784 -0.1282031389 -0.03200577
## Water2Litre
## BottleofWine
                     -0.134045523 -0.002263568 0.0177348161 0.00391276
## Domestic1LitreBeer -0.089222397 -0.124854321 0.0619406327 0.23251631
## Imported1LitreBeer -0.106787051 0.194802726 -0.0669706184 -0.17959121
## Cigarettes20Pack 0.290666713 0.045755872 -0.0525692930 -0.00716284
                     -0.088399659 -0.089200486 -0.0156687216 0.06080712
## OnewayTicket
## ChickenBreasts
                     ## MonthlyPass
                    -0.070239735 -0.116783046 0.0886235767 -0.09172906
## Gasoline1Litre 0.186736181 -0.034885590 0.0530572164 0.05159759
## VWGolf
                     0.097348352 -0.088883206 -0.0571153505 0.09608020
## Apartment1BD
                     -0.049454801 -0.083977581 -0.0465287759 -0.12806628
## Apartment1BD00C
                     -0.094444347 -0.069709300 0.0626731962 -0.17688535
## Apartment3BDICC
                     -0.001253546 -0.111232940 -0.0653177754 -0.18281352
## Apartment3BD00C
                     -0.089201119 -0.058434225 0.0630003654 -0.17189304
## BasicUtilities
                     -0.048697309  0.134312636  -0.0236444010  -0.12955590
## PrepaidMobile1MIn -0.102805541 -0.106487259 -0.0232991883 0.05585434
                     0.117501114 0.282040864 0.0224841645 0.17605506
## Internet
2
## GymFees
                     -0.080583663 -0.068736026 -0.0267022999 0.08200983
## TennisCourtFeesPerHour 0.003612576 0.022571826 0.0138707559 -0.01235033
## CinemaPerPerson 0.046412016 -0.072174644 -0.0392207260 -0.11597487
```

4					
4 ## 8	PairofJeans	0.254634907	-0.036565608	0.1836932005	-0.06762044
## 1	SummerDress	-0.058352356	0.108424731	-0.1170003374	0.05674012
## 3	NikeRunningShoes	0.023111923	-0.145273463	0.0952717815	-0.07046969
## 7	LeatherShoes	0.102988846	0.100283231	-0.0184172716	0.14338725
## 6	AptPricePerSquareM	-0.006817559	0.045483804	-0.1697975416	0.24760087
##	AptPricePerSqM00C	-0.090281305	0.048436907	0.0311698197	0.14557613
	AvgMnthlyNetSalary	-0.001271912	-0.044011171	0.1321206478	0.23873145
0 ## 7	MortgageInterest	0.112934813	-0.068845627	0.0415371232	-0.02613996
	TaxiStartingFare	-0.214734557	0.091007538	-0.0798837676	0.09906013
##	Taxi1KM	0.023870812	-0.024315277	-0.0004946969	0.04565117
	Taxi1HRWaiting	0.109348301	0.334329016	0.0697678069	-0.16488426
0 ## 1	Apples1KG	0.263760121	-0.087018624	0.3652264936	-0.14875139
## 8	Oranges1KG	-0.004475613	-0.181144267	-0.3704191164	0.06175048
6 ##	Potato1KG	0.101487539	-0.167434786	0.1161395465	0.04853309
##	Lettuce1Head	-0.070260227	0.073381991	0.2578143485	0.10931612
##	CappucinoReg	-0.023925624	-0.245584812	0.3180246851	0.27243224
_	WhiteRice	0.058805039	0.111759460	0.0007774745	-0.14980650
_	Tomato1KG	-0.126448547	-0.046809543	-0.0757809775	-0.02807151
	Banana1KG	-0.256000375	0.150656170	0.0614070004	-0.17822378
	Onion1KG	0.122461085	0.022114949	-0.1325764459	-0.03886432
	BeefRound1KG	0.184138396	-0.038233681	-0.0288132804	0.20391954
## 9	ToyotaCorolla	-0.144509479	0.171287397	0.0397384327	-0.01324970
	PreschoolperMonth	0.145214653	0.375908833	0.2274329291	0.26818687
## 40		PC37	7 PC38	3 PC39	PC
	MealInexpensive	-0.0595440933	3 -0.098654997	7 0.308243690	0.19665674

	MealFor2	-0.0009676442	0.092594871	-0.089366510	0.08801706
95 ## 19	McMealMcDonalds	0.0117877150	-0.070611569	-0.301706320	-0.03752096
## 82	DomesticBeer	-0.0645025647	-0.033461748	-0.141635285	0.21705814
## 23	ImportedBeer	0.1049101696	0.011859871	-0.032853599	0.11762192
	CokeOrPepsi	0.0962953737	0.269626379	-0.023274139	-0.08336279
## 17	Water1Litre	0.1050357338	0.152832519	0.198526789	-0.02609367
## 91	Milk1Litre	0.1454606088	0.052635230	-0.087948896	0.05901742
## 33	LoafofBread	0.0127883036	-0.121557645	-0.398557298	-0.09129276
## 46	Eggs	-0.1329894739	0.062680435	0.131536001	0.10761211
## 56	LocalCheese	-0.0306690346	0.097471729	0.040277514	0.00628711
## 62	Water2Litre	-0.0340124585	-0.006925366	0.096435207	0.24128424
## 23	BottleofWine	0.1790430564	0.097743436	0.160981005	-0.00975997
## 41	Domestic1LitreBeer	-0.0850370160	0.046417936	-0.231634702	0.16470930
## 81	Imported1LitreBeer		-0.115956805		-0.17616118
## 41	Cigarettes20Pack		-0.105019595		-0.34501973
## 22	OnewayTicket		-0.372115788		0.20466726
33	ChickenBreasts	-0.0430399466			
06	MonthlyPass	-0.2704257115		-0.058152334	
08	Gasoline1Litre	0.0921155225		-0.055773107	
99	VWGolf	-0.0715390462		-0.051037548	
74	Apartment1BD		-0.024442498		
72	Apartment1BD00C		-0.012693128		
67	Apartment3BDICC	-0.1990978446			
21	Apartment3BD00C		0.060366629		
##	BasicUtilities	-0.0645413630	-0.062064093	-0.1055991/5	-0.0144/104

64 ##	PrepaidMobile1MIn	0.0749119540	0.008361991	0.008867038	-0.02247896
71 ## 26	Internet	0.1803936250	0.068363455	0.131353925	-0.14920477
## 40	GymFees	-0.1376385634	0.060508027	-0.008753786	0.06135770
## 43	TennisCourtFeesPerHour	0.0006416143	-0.016899181	-0.022754906	-0.13027764
	CinemaPerPerson	-0.1957033938	-0.104866333	0.336457583	0.04622273
	PairofJeans	0.2401470851	-0.176282281	-0.006809289	-0.09534365
	SummerDress	-0.0099171874	0.065085006	0.014183381	0.00060015
## 14	NikeRunningShoes	0.0968365086	0.081850201	-0.010434412	0.02398793
## 44	LeatherShoes	-0.2736201907	-0.213121538	0.037196682	0.03863291
## 96	AptPricePerSquareM	0.0588311801	-0.041522872	-0.017650314	-0.06442662
## 01	AptPricePerSqMOOC	0.0561784101	-0.014488819	0.057337197	0.05802894
## 14	AvgMnthlyNetSalary	0.1263352850	-0.107747759	-0.007466480	0.07503196
## 34	MortgageInterest	0.0454033092	0.016055770	-0.011435336	-0.07625274
## 77	TaxiStartingFare	-0.1191111332	0.252453919	0.014826223	0.00965761
## 68	Taxi1KM	0.1688537780		0.017245611	-0.01526788
51	Taxi1HRWaiting	-0.2043479117		-0.123841629	0.06242210
45	Apples1KG	-0.0283003268			0.28040783
23	Oranges1KG		0.055125096		
80	Potato1KG	-0.1894034939		-0.101181427	
89	Lettuce1Head	-0.0869096166			
82	CappucinoReg	-0.0673223694			
53	WhiteRice		0.075224597		
65	Tomato1KG		0.193769170		
23	Banana1KG		-0.142787902		
##	Onion1KG	-0.2891247107	-0.31034/223	-0.000408/23	0.08379113

```
74
## BeefRound1KG
                           -0.0080048786 -0.076076184
                                                       0.272031973 -0.11079586
28
## ToyotaCorolla
                            0.0718451382 -0.079073823
                                                       0.082841408
                                                                     0.00247770
06
                                          0.121206390 -0.067195006
## PreschoolperMonth
                            0.1003143416
                                                                     0.18570593
00
##
                                   PC41
                                                PC42
                                                              PC43
                                                                           PC44
                            0.191134005 -0.285743907 -0.362197870 -0.139009821
## MealInexpensive
## MealFor2
                            0.077900305
                                         0.107839871
                                                      0.173184356
                                                                    0.155323049
## McMealMcDonalds
                           -0.250672892
                                         0.147577399
                                                      0.084525128
                                                                    0.030184893
## DomesticBeer
                           -0.046400879
                                         0.036600465
                                                      0.091452693 -0.129881204
## ImportedBeer
                                         0.169024352 -0.201644870
                            0.093186037
                                                                    0.040940601
## CokeOrPepsi
                            0.079320539
                                         0.056752702 -0.123839519 -0.008058045
## Water1Litre
                            0.041337709
                                         0.002609029
                                                      0.149970974
                                                                    0.083280851
## Milk1Litre
                           -0.012366245 -0.063636164
                                                      0.086767079
                                                                    0.138334167
## LoafofBread
                            0.045539690 -0.063853342 -0.178924382
                                                                    0.152448511
## Eggs
                           -0.237275486
                                         0.217406996
                                                      0.032148861 -0.149542110
## LocalCheese
                            0.123570438
                                         0.023535674 -0.078146175
                                                                    0.175712526
## Water2Litre
                            0.091781761 -0.251707636
                                                      0.125683524 -0.049643292
## BottleofWine
                           -0.033061678 -0.113245718 -0.068717093 -0.123198553
## Domestic1LitreBeer
                           -0.120394556 -0.226399482 -0.031463709
                                                                    0.254072568
## Imported1LitreBeer
                            0.059450268
                                         0.182596257
                                                      0.115987294 -0.147275884
## Cigarettes20Pack
                           -0.080155114 -0.072372725 -0.145244157
                                                                    0.052158668
## OnewayTicket
                            0.226221032
                                         0.263626447
                                                      0.061044918 -0.167581957
## ChickenBreasts
                           -0.105113001 -0.124749182 -0.133316351 -0.206828994
                                         0.131814446 -0.036803713
## MonthlyPass
                            0.037639776
                                                                    0.217485351
## Gasoline1Litre
                            0.154722125 -0.063343957 -0.019517314 -0.034239308
## VWGolf
                            0.027301535 -0.038294115 -0.080522169 -0.425666785
## Apartment1BD
                            0.067123081 -0.177549921
                                                      0.017691299
                                                                    0.070285857
## Apartment1BD00C
                           -0.011374513
                                         0.032176897
                                                      0.197852943
                                                                    0.125341496
                            0.063050567 -0.097506839 -0.076299145 -0.155484870
## Apartment3BDICC
## Apartment3BD00C
                           -0.048858915
                                         0.059218859
                                                      0.144942336 -0.067338047
## BasicUtilities
                           -0.026183541 -0.104023747
                                                      0.074796736
                                                                    0.026971564
## PrepaidMobile1MIn
                            0.022114777 -0.114000684
                                                      0.126117295 -0.003798013
## Internet
                           -0.152693559 -0.011187852 -0.066437459
                                                                    0.020057883
## GymFees
                            0.196618317 -0.096540720
                                                      0.003377736
                                                                    0.010193120
## TennisCourtFeesPerHour -0.062551162 -0.072735771
                                                      0.017662024 -0.057237760
## CinemaPerPerson
                           -0.462192357 -0.033774799 -0.129929784
                                                                    0.089368114
## PairofJeans
                           -0.021562833 -0.014846054 -0.056095345 -0.001358553
## SummerDress
                            0.134527154
                                         0.038490209 -0.031009236 -0.074676703
## NikeRunningShoes
                            0.081700264
                                         0.001592781 -0.004581583
                                                                    0.033661531
## LeatherShoes
                           -0.230605553
                                         0.097404288
                                                      0.019336566
                                                                    0.058049953
## AptPricePerSquareM
                           -0.127526462 -0.039879508 -0.301510664 -0.041706219
## AptPricePerSqMOOC
                           -0.055474540
                                         0.123283771
                                                      0.231452761 -0.143295260
## AvgMnthlyNetSalary
                           -0.056652823 -0.150713577
                                                      0.141717919
                                                                    0.048533150
## MortgageInterest
                           -0.035571941 -0.044104316
                                                      0.031788872
                                                                    0.019152567
## TaxiStartingFare
                            0.009903370
                                         0.127439421
                                                      0.024625593 -0.008838686
## Taxi1KM
                            0.093115935 -0.003943657 -0.096408098
                                                                    0.013814157
## Taxi1HRWaiting
                            0.053213523 -0.339150057
                                                      0.227901794 -0.108636050
```

```
## Apples1KG
                      -0.170599163 -0.054538880 0.046481420 -0.120302906
## Oranges1KG
                      -0.149471605 -0.079374392 0.262843680 -0.196176231
## Potato1KG
                      ## Lettuce1Head
                      ## CappucinoReg
                      0.050177200 0.173592979 0.033006683 0.025169452
## WhiteRice
## Tomato1KG
                      -0.114282558 -0.008908647 -0.300525036 0.137795751
## Banana1KG
                      0.073961185  0.058088715  -0.074831327
                                                        0.042375898
## Onion1KG
                      0.283237189 0.163685823 0.065494885 0.185016962
## BeefRound1KG
                      0.079159584 -0.282208320 0.217001568 0.106081258
## ToyotaCorolla
                      -0.152816601 0.061045810 0.073381221 0.384446262
## PreschoolperMonth
                      ##
                             PC45
                                         PC46
                                                     PC47
C48
## MealInexpensive
                      -1.429668e-01 -1.146787e-01 0.0818318544 0.149703
967
                     1.847032e-01 -5.331235e-01 -0.4357268485 -0.032694
## MealFor2
881
## McMealMcDonalds -7.253750e-02 2.864139e-01 -0.0444397416 -0.055310
870
## DomesticBeer
                    -1.381634e-01 -1.979791e-01 0.2498209356 -0.117969
608
## ImportedBeer 3.047286e-01 2.594953e-01 0.0823107985 0.077702
785
## CokeOrPepsi
                     -6.544329e-03 6.926395e-02 -0.3694542704 -0.165866
383
## Water1Litre
                      -8.967449e-02 -1.395050e-01 0.2908131703 0.011193
173
## Milk1Litre
                     -4.568276e-02 4.987569e-02 -0.0809318698 0.021036
748
## LoafofBread
                      1.268201e-02 -2.083317e-01 0.2607901474 0.021252
643
## Eggs
                      -2.043820e-01 1.753505e-01 -0.0532863661 0.127301
987
## LocalCheese
                     -9.248091e-02 -6.729444e-03 0.0792883177 0.111948
302
## Water2Litre 7.537334e-02 1.353482e-01 0.0230387965 -0.089419
625
## BottleofWine
                     2.380197e-02 -5.695463e-02 -0.0027919955 0.068469
140
## Domestic1LitreBeer
                     -3.483248e-01 -7.961510e-02 -0.0441517384 0.008953
299
## Imported1LitreBeer 2.409277e-01 1.026461e-03 -0.0664908560 -0.037192
393
## Cigarettes20Pack
                     -8.753131e-02 -2.427664e-02 -0.0329938359 0.010539
139
## OnewayTicket -1.135494e-01 1.317134e-01 0.0546624332 -0.204747
056
## ChickenBreasts
                    2.641471e-01 -1.785054e-01 0.0097622508 0.014012
344
```

## MonthlyPass	9.240178e-02	6.712351e-02	0.0158611726	0.130819
279 ## Gasoline1Litre	5.208334e-02	3.374286e-02	0.0320638273	0.074659
365 ## VWGolf	1.411303e-02	-3.716108e-02	-0.1821186240	0.004661
322 ## Apartment1BD	-7.517083e-02	7.155024e-02	-0.1591958561	-0.051553
566 ## Apartment1BD00C	4.597294e-02	-2.520605e-02	-0.0877831615	-0.055142
<pre>616 ## Apartment3BDICC</pre>	-1.519706e-01	5.662121e-02	0.0317530573	-0.198847
930 ## Apartment3BD00C	-8.356771e-02	-7.475656e-02	0.0984445354	-0.072193
983 ' ## BasicUtilities		-2.647275e-02		
314 ## PrepaidMobile1MIn		-4.402541e-02		
686				
## Internet 303	-4.488988e-02		-0.0343506521	
## GymFees 702	6.728238e-02	3.027905e-02	0.1476173960	-0.006728
<pre>## TennisCourtFeesPerHour 041</pre>	-7.738301e-02	5.841847e-02	-0.0171592197	0.097776
## CinemaPerPerson 095	1.879879e-01	-1.308768e-01	0.0971946062	0.020855
## PairofJeans 314	-5.751747e-02	-1.005706e-01	0.0773236199	0.187476
## SummerDress	-5.857864e-02	7.397800e-02	-0.0389359959	-0.014016
## NikeRunningShoes	-7.163429e-05	-5.986325e-02	0.0492356522	0.114890
<pre>431 ## LeatherShoes</pre>	8.215639e-02	1.573585e-01	-0.0314252303	-0.238108
972 ## AptPricePerSquareM	-7.433921e-02	8.030562e-02	-0.2314526159	-0.062206
918 ## AptPricePerSqMOOC	-1.601228e-02	-7.344371e-02	0.1192236249	0.131001
465 ## AvgMnthlyNetSalary	2.258327e-01	1.933657e-01	-0.1826131859	0.597879
619 ## MortgageInterest	3.055757e-02	-4.316197e-03	0.0008473215	-0.016302
560 ## TaxiStartingFare		-6.635214e-02		
623				
## Taxi1KM 380		-3.626644e-02		
## Taxi1HRWaiting 897		3.000014e-01		
## Apples1KG 698	-1.753952e-01	-1.969933e-01	-0.2359862691	-0.044300

## Oranges1KG 965	2.154877e-02	9.489208e-03 0.1800137720 0.079658
## Potato1KG 914	2.583715e-01	-1.062674e-01 0.2113284880 0.025178
## Lettuce1Head 304	-5.637855e-02	-1.019112e-02 -0.0403438221 0.049275
## CappucinoReg 749	4.590310e-02	5.433460e-02 -0.0039108570 -0.196229
## WhiteRice 471	-3.795551e-01	-1.950438e-02 0.0124396300 0.086982
## Tomato1KG 151	8.098213e-02	1.679991e-01 0.0014605959 -0.203462
## Banana1KG 156	-1.184182e-02	-3.956731e-02 0.0022417074 0.073646
## Onion1KG 019	-1.001809e-01	9.325795e-02 -0.1287731034 0.206885
<pre>## BeefRound1KG 753</pre>	1.972654e-01	4.626566e-05 -0.0134731341 -0.280195
## ToyotaCorolla 461	2.401470e-03	2.697386e-02 0.1714530900 -0.091844
<pre>## PreschoolperMonth 954</pre>	8.540241e-02	-4.628790e-02 0.0694682184 -0.114999
## 52	PC49	PC50 PC51 PC
<pre>## MealInexpensive 42</pre>	0.0487376849	0.163110867 0.059338770 -0.07993896
## MealFor2 85	0.0257545018	-0.184216303 0.066689584 0.00798829
<pre>## McMealMcDonalds 35</pre>	0.1015572899	0.005235678 -0.031263539 0.00316691
## DomesticBeer 10	0.2845146882	0.037320810 -0.487336696 0.04939088
<pre>## ImportedBeer 92</pre>	-0.2058817273	-0.066458403
## CokeOrPepsi 06	-0.2527845579	0.239450437 -0.348731636 -0.12220063
## Water1Litre 45	0.2909146213	-0.235650972 0.321093479 0.14321453
## Milk1Litre 38	0.0203897997	-0.066469335 -0.046646558 0.03689426
## LoafofBread 78	0.0352053633	0.199793941 0.025972640 -0.05030685
## Eggs 41	-0.0180896449	-0.071189469 0.084200513 -0.02931334
## LocalCheese 40	-0.0014945957	-0.012121654 -0.031337036 0.01924048
## Water2Litre 72	-0.1976893621	-0.089626060 -0.184232371 0.05246053
## BottleofWine 68	0.0215527146	-0.004048836 -0.018392183 -0.02231527

## 03	Domestic1LitreBeer	-0.3285727499	-0.008120029	0.125138294	-0.02436391
## 86	Imported1LitreBeer	0.2118835687	0.014068218	-0.053046313	0.02903860
	Cigarettes20Pack	0.1123058835	0.173095430	-0.021616629	-0.05432583
	OnewayTicket	-0.1484687766	-0.082804559	-0.002501281	0.00727155
	ChickenBreasts	0.0083349797	-0.078647020	0.146648242	0.04958553
## 66	MonthlyPass	0.1456894191	0.076057148	-0.046778200	-0.00401108
## 02	Gasoline1Litre	0.0977060648	0.088655537	0.014958356	-0.02647060
## 04	VWGolf	0.0566261553	0.125021755	0.089577640	-0.03112994
## 16	Apartment1BD	0.0241793934	-0.203182408	0.091764405	-0.38664726
## 45	Apartment1BD00C	-0.0892595148	0.379609771	0.195103515	0.06606307
## 61	Apartment3BDICC	0.0388557340	-0.458336524	-0.141805599	-0.07211867
## 35	Apartment3BD00C	-0.0635302840	0.272467011	-0.033450534	0.45605153
## 59	BasicUtilities	-0.0341967088	-0.052758684	0.063121081	0.04599154
## 32	PrepaidMobile1MIn	0.0466422089	-0.040310411	0.053169478	0.04665341
## 08	Internet	0.0829375344	-0.012440376	0.032730018	-0.05779989
## 87	GymFees	0.0434368258	0.133682434	0.005670819	-0.00440623
## 57	TennisCourtFeesPerHour	-0.0130261502	-0.011382301	0.015368268	0.02933389
## 29	CinemaPerPerson	-0.2278623147	0.023822869	-0.109803041	-0.07850849
## 04	PairofJeans	-0.1964906613	-0.118777260	-0.106033637	0.03614368
## 71	SummerDress	-0.0003586595	0.012152113	-0.011795326	0.00284755
## 31	NikeRunningShoes	-0.0199689181	0.011630644	-0.028623177	0.02318949
## 88	LeatherShoes	0.1619016522	0.134232798	0.122286930	-0.06574189
## 73	AptPricePerSquareM	0.0255144271	-0.078524045	0.041452700	0.48613318
## 82	AptPricePerSqMOOC	-0.0084253220	0.145183732	0.035062445	-0.52592005
## 43	AvgMnthlyNetSalary	0.1732525568	-0.126048243	-0.254641240	0.08431864

```
## MortgageInterest
                        0.0162586009 0.005256925 0.012114110 0.00746531
44
## TaxiStartingFare
                        0.0461595366 0.001006755 0.021418919 0.00036280
45
## Taxi1KM
                       -0.0755842134 -0.011004018 -0.065997164 -0.00838010
15
## Taxi1HRWaiting
                       -0.0155781601 0.005690173 0.143625578 0.08846479
## Apples1KG
                        85
## Oranges1KG
                       -0.1687607193   0.154369316   0.008434803   -0.00391742
48
## Potato1KG
                       -0.1981097366 -0.124848445 -0.108460916 0.02743925
11
## Lettuce1Head
                       -0.1275476197 -0.083216523 0.021575342 0.01047739
55
## CappucinoReg
                       0.0953315531 0.117769808 0.051032396 -0.00408427
03
## WhiteRice
                       -0.0444400743 -0.068718993 0.005003077 0.00280970
94
## Tomato1KG
                       16
## Banana1KG
                       0.0266651867 -0.064334579 0.048791091 0.01715363
66
## Onion1KG
                        0.0135499498 0.091069584 -0.064295848 0.05472575
87
                       -0.0779074203 -0.037897099 -0.099324431 0.00015460
## BeefRound1KG
36
## ToyotaCorolla
                       -0.0532103708 -0.134164006 -0.085022511 -0.00676844
97
## PreschoolperMonth
                       -0.1474773713 -0.154834204 0.028739823 0.02612435
72
##
                               PC53
                                            PC54
## MealInexpensive
                       -0.040926658 -0.0021474407
## MealFor2
                       -0.149240105 -0.0206055389
## McMealMcDonalds
                       -0.081806224 -0.0037375392
## DomesticBeer
                        0.279333705 0.0366014921
## ImportedBeer
                       -0.111878366 -0.0389141748
## CokeOrPepsi
                       -0.016209489 -0.0012196268
## Water1Litre
                        0.057056628 0.0087740033
## Milk1Litre
                       -0.040042368 0.0012611924
                       -0.020797659 0.0252725453
## LoafofBread
                        0.054913401 0.0134162581
## Eggs
## LocalCheese
                        0.042963351 0.0277526774
## Water2Litre
                        0.053364291 0.0081428538
## BottleofWine
                        0.051747043 0.0001994061
## Domestic1LitreBeer
                       ## Imported1LitreBeer
                        0.042775598 -0.0152382316
## Cigarettes20Pack
                       -0.072972317
                                    0.0078518385
                       0.073718276 -0.0378267292
## OnewayTicket
```

```
## ChickenBreasts
                           -0.022629711
                                         0.0048752715
## MonthlyPass
                           -0.012669617 -0.0068084683
## Gasoline1Litre
                           -0.015636303 -0.0022688660
## VWGolf
                           -0.075626756
                                         0.0065703304
## Apartment1BD
                           0.491646180 -0.4825009654
## Apartment1BD00C
                           0.299796026
                                         0.5820337230
## Apartment3BDICC
                           -0.377648948
                                         0.3930530284
## Apartment3BD00C
                           -0.357980190 -0.5081737176
## BasicUtilities
                           0.003340740 -0.0042706840
## PrepaidMobile1MIn
                           0.018473048 -0.0016413591
## Internet
                           -0.038388968
                                         0.0023535455
## GymFees
                           0.026125079
                                         0.0032998560
## TennisCourtFeesPerHour
                           0.021314865
                                         0.0173861707
## CinemaPerPerson
                           0.016682347 -0.0262752857
## PairofJeans
                           0.009170703
                                         0.0110123701
## SummerDress
                           0.011318553
                                         0.0083825410
## NikeRunningShoes
                           0.023830675
                                         0.0045413523
## LeatherShoes
                           0.017910131 -0.0237164093
## AptPricePerSquareM
                           0.260267572
                                         0.0273604923
## AptPricePerSqMOOC
                           -0.217891827 -0.0202651116
## AvgMnthlyNetSalary
                           -0.060017710
                                         0.0404046876
## MortgageInterest
                           -0.003168412 -0.0031590041
## TaxiStartingFare
                           0.047251084
                                         0.0323642396
                           -0.035688948
## Taxi1KM
                                         0.0103333867
## Taxi1HRWaiting
                           0.018575339
                                         0.0082170383
## Apples1KG
                           0.027336814 -0.0064044135
## Oranges1KG
                           0.022652712
                                         0.0190805483
## Potato1KG
                           0.226280209 -0.0054119788
## Lettuce1Head
                           0.007574130 -0.0084231517
                           -0.037291981 -0.0043590933
## CappucinoReg
## WhiteRice
                           0.017867987
                                         0.0118756342
                           -0.196107974 -0.0176161846
## Tomato1KG
## Banana1KG
                           0.001177722 -0.0028967086
## Onion1KG
                          -0.056410869 -0.0248139173
## BeefRound1KG
                           -0.056128592 -0.0283601292
## ToyotaCorolla
                          -0.007273613 -0.0108357173
## PreschoolperMonth
                          -0.014084245
                                         0.0026938504
head(GDPdataTrainSet.pca.normdata$x)
                                            # Transformed data
##
             PC1
                        PC<sub>2</sub>
                                    PC3
                                                PC4
                                                             PC5
                                                                        PC<sub>6</sub>
## 61
       -3.039865 -2.0859707 -1.8315668 -0.06937856
                                                     0.06623432 -1.2784415
## 64
       0.59009946
                                                                  0.6051857
## 133 -5.298737 -0.3362346 -0.2490153
                                                     0.94280609
                                                                  2.1805977
                                         0.61966623
## 9
       -5.589605 -0.4956479
                             0.7318659
                                         0.94858751
                                                     1.19345039
                                                                  1.9612752
## 62
        3.403006 -3.8100249
                              2.4338965
                                         3.29248427
                                                     0.38989446
                                                                  0.4529685
## 97
       -2.325029
                  1.7114247
                              0.1024440
                                         0.46254778 -0.03674554
                                                                  0.4989894
##
              PC7
                         PC8
                                     PC9
                                                PC10
                                                            PC11
                                                                       PC12
## 61
        0.1866662
                   0.3956465
                              0.8519720 -0.04475955 -2.0977228 -0.1249151
```

0.5431546 -0.10181693 -0.1926114 -0.2683056

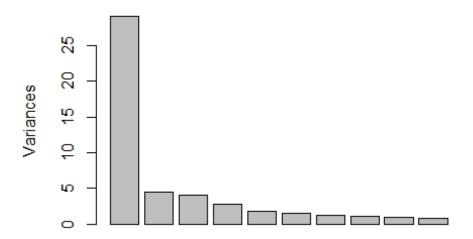
64

-1.5989538 -0.1983527

```
## 133 -0.5300393 -2.9062132 2.7430591 2.06421034 -1.5802090 -2.4944185
     -0.7881909 -0.4685455 -0.2190076 -0.05968880 0.3623404 0.7738729
     ## 62
## 97
     -0.4000785 0.9512749 -0.2972072 -0.24543437 0.6998274 0.5293423
##
          PC13
                  PC14
                           PC15
                                    PC16
                                            PC17
                                                     PC18
     -1.41022616   0.6037959   -0.1303786   0.39039608   1.6025362   1.21907599
## 61
     -0.03606751 -0.3561753 -1.0379504 0.34272840 -0.3003305 -0.16985189
## 133 -0.14005681 -1.0473703 1.9147476 -0.49530642 1.8985743 -0.40283070
## 9
     -0.04287590 -0.2202414 -0.7746910 0.06317333 -1.1130884 0.62299100
      0.51581961 -1.2902555 -1.2616186 0.17830163 -0.7233297 0.84834689
## 62
      0.15118660 -0.3622167 0.7446460 -0.02884784 -0.6636075 0.02904599
## 97
##
          PC19
                   PC20
                                             PC23
                            PC21
                                     PC22
                                                      PC24
## 61
      ## 64
      ## 133 -0.66218408 -0.58879763 0.60539715 0.1625065 0.2207253 -0.64253464
     -0.09916299 -0.22177450 -0.14991175 -0.4114198 -0.3224662 0.65366007
## 62
     -1.43192502 0.07672738 -0.71972522 1.2146985 1.1155333 -0.35012882
## 97
      0.03082389 0.29450918 0.84161592 -0.2964861 0.4086776 0.01642432
##
           PC25
                    PC26
                             PC27
                                       PC28
                                                PC29
C30
## 61
     -0.082001155 -0.06538442 -0.41311152 -0.337088395 -0.24364814 -0.55447
190
      ## 64
998
## 133 0.423544998 0.91648929 0.01684388 0.093856946 0.16524401 -0.03084
172
## 9
     -0.318622195 -0.13228087 -0.26674490 0.006067111 0.16431070 -0.09323
857
     ## 62
656
     -0.005161004 0.34149406 -0.10339531 -0.399620377 -0.15162225 0.21150
## 97
918
                                                         Ρ
##
           PC31
                    PC32
                             PC33
                                      PC34
                                                PC35
C36
## 61
      0.185693063 -0.01785285 -0.51830277 -0.69447816 -0.058988467 0.25255
701
     ## 64
813
423
## 9
      0.335649430 -0.28963499 -0.35471183 -0.12760030 -0.202838021 0.07260
857
## 62
     520
## 97
      0.101173263  0.42551178  0.05091355  -0.04566099  -0.222227134  0.22286
952
##
          PC37
                    PC38
                              PC39
                                        PC40
                                                 PC41
PC42
## 61
    -0.19161214 0.211619658 -0.2024545751 0.083444024 -0.24197975 0.285
1998
```

```
## 64 -0.14252696 -0.164827460 -0.0402622368 0.083279219 -0.25093744 -0.171
4923
## 133 0.09869151 0.007460935 -0.0003300664 -0.024808602 -0.24826440 -0.251
4427
## 9
      -0.03041904 -0.150249054 0.1564791402 -0.316593730 0.31590721 0.210
6341
## 62
       0.21229120 0.256529999 0.1145339032 -0.100028491 -0.25711252 0.104
9903
## 97 -0.04395584 0.169627467 0.1046777530 0.004875151 0.08408511 0.111
5071
            PC43
                       PC44
                                   PC45
                                               PC46
                                                           PC47
##
PC48
## 61 -0.36315818 -0.21378580 -0.13754042 -0.079842817 -0.059862301 -0.03677
8722
## 64
       6776
## 133 -0.03187235 0.15448581 -0.01152059 0.011909934 -0.009966696 -0.06013
9969
       0.06256042 0.00338789 0.04481897 0.206511025 -0.068380725 -0.02966
## 9
8158
## 62 -0.02736285 -0.07166560 -0.07280740 0.117699648 0.083833775 -0.04416
8461
## 97 -0.04754129 0.03336189 -0.18236025 -0.009878981 -0.031374356 -0.21727
2000
##
            PC49
                                                 PC52
                        PC50
                                    PC51
                                                           PC53
PC54
      -0.06832886 -0.120045948 0.006066169 0.010152616 0.06117844 0.0041
## 61
26251
## 64
       0.04454729 0.075955533 -0.053654638 -0.022885334 0.01890509 -0.0052
66749
## 133 0.01637246 0.084773078 -0.017561232 0.001170816 -0.04401355 0.0161
36920
## 9
       0.01191469 -0.007379773 0.017500785 0.031273143 -0.05680666 0.0140
84495
       0.01976251 -0.038873174 -0.074515994 0.026576185 -0.06409826 -0.0085
## 62
11902
## 97
       0.11371829 0.051823962 0.009862491 -0.050441851 0.07822175 0.0238
14635
plot(GDPdataTrainSet.pca.normdata)
```

GDPdataTrainSet.pca.normdata



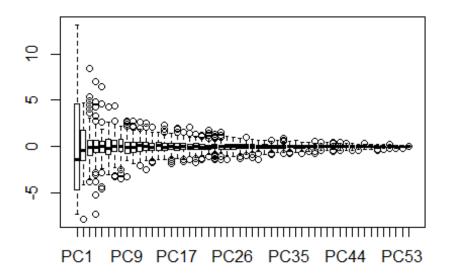
```
var <- get pca var(GDPdataTrainSet.pca.normdata)</pre>
head(var$contrib, 4)
##
                      Dim.1
                                Dim.2
                                             Dim.3
                                                      Dim.4
                                                                  Dim.5
                                                                             D
## MealInexpensive 2.601603 1.7276292 0.949641244 0.961719 0.258744233 0.6524
2528
## MealFor2
                   2.881301 0.9341824 0.007625963 1.968744 0.000164928 0.8002
2089
## McMealMcDonalds 2.462606 1.8575483 0.007561012 2.709421 0.004393870 0.0795
## DomesticBeer
                   2.451215 0.4107280 0.857835803 4.312730 1.467494336 0.2184
8614
##
                        Dim.7
                                    Dim.8
                                                 Dim.9
                                                             Dim.10
                                                                        Dim.11
## MealInexpensive 0.19066358 0.292230627 0.004829637 3.501514e-06 0.01086103
## MealFor2
                   0.01688304 0.236957173 0.501873045 1.874577e-01 0.61236112
## McMealMcDonalds 0.63148795 0.002103343 0.310202121 2.671404e-01 0.46862541
## DomesticBeer
                   0.01097863 1.703680670 0.023738174 7.050939e-01 0.28414015
##
                        Dim.12
                                   Dim.13
                                              Dim.14
                                                         Dim.15
## MealInexpensive 0.063321757 0.40116766 0.6207874 0.04412147 1.629183810
## MealFor2
                   0.183077325 0.04715038 0.6137021 0.09119239 0.245103101
## McMealMcDonalds 0.004734944 0.42645848 3.2204461 0.15391049 0.003815063
## DomesticBeer
                   1.994948629 0.45384607 0.7519904 0.35914245 0.446952422
##
                      Dim.17
                                Dim.18
                                           Dim.19
                                                      Dim.20
                                                                  Dim.21
                                                                            Di
m.22
## MealInexpensive 0.1237578 0.4083340 2.9374330 0.04931285 0.119952225 0.882
```

```
0464
                  0.2484491 0.1116661 0.1504796 1.13337517 0.105472472 0.193
## MealFor2
0046
## McMealMcDonalds 1.0859507 3.1026946 4.6854984 0.02203289 0.002332839 0.280
1623
                  0.3265666 0.3327646 0.3106847 2.45654316 0.344067336 0.823
## DomesticBeer
0993
                      Dim.23
                               Dim.24
                                          Dim.25
##
                                                    Dim.26
                                                             Dim.27
                                                                          Di
m.28
## MealInexpensive 7.67188102 2.271265 2.76567192 4.8208516 2.583963 1.96396
2723
## MealFor2
                  0.08191806 2.444790 0.06896193 0.1519076 1.687890 0.00450
4047
## McMealMcDonalds 6.84917982 1.278699 3.09978908 0.1707493 7.718384 11.35192
## DomesticBeer 4.83276223 1.592255 0.10589823 0.6728621 0.791822 0.55040
5058
##
                     Dim.29
                                 Dim.30
                                           Dim.31
                                                     Dim.32
                                                                           D
                                                               Dim.33
im.34
## MealInexpensive 4.5297739 2.002563231 1.5323642 1.2686780 0.4220114 0.0077
51615
## MealFor2
                  1.1095409 0.008376718 1.4491009 3.4582349 0.4225812 0.0056
55504
## McMealMcDonalds 1.2174954 0.048991633 3.9607676 3.7572626 0.4857959 8.0517
## DomesticBeer 0.4564613 0.026682430 0.4755489 0.3169414 4.4766282 0.0909
57888
                      Dim.35
                                 Dim.36
                                              Dim.37
                                                        Dim.38
##
                                                                  Dim.39
## MealInexpensive 1.0630543 0.27355848 3.545499e-01 0.9732808 9.5014173
                  11.0380040 0.07866191 9.363353e-05 0.8573810 0.7986373
## MealFor2
## McMealMcDonalds 0.1588500 0.00216691 1.389502e-02 0.4985994 9.1026704
## DomesticBeer
                   0.1295367 0.69075575 4.160581e-01 0.1119689 2.0060554
##
                     Dim.40
                               Dim.41
                                         Dim.42
                                                    Dim.43
                                                               Dim.44
                                                                         Dim
## MealInexpensive 3.8673874 3.6532208 8.1649580 13.1187297 1.93237303 2.0439
518
                  0.7747005 0.6068458 1.1629438 2.9992821 2.41252495 3.4115
## MealFor2
288
## McMealMcDonalds 0.1407823 6.2836899 2.1779089 0.7144497 0.09111278 0.5261
## DomesticBeer
                  4.7114240 0.2153042 0.1339594 0.8363595 1.68691272 1.9089
123
##
                     Dim.46
                                 Dim.47
                                          Dim.48
                                                     Dim.49
                                                                 Dim.50
## MealInexpensive 1.315122 0.6696452 2.2411008 0.23753619 2.660515503
## MealFor2
                  28.422061 18.9857886 0.1068955 0.06632944 3.393564633
## McMealMcDonalds 8.203293 0.1974891 0.3059292 1.03138831 0.002741232
## DomesticBeer
                   3.919573 6.2410500 1.3916828 8.09486078 0.139284286
##
                                   Dim.52
                                             Dim.53
                       Dim.51
                                                          Dim. 54
## MealInexpensive 0.35210897 0.639023800 0.1674991 0.0004611501
                   0.44475007 0.006381291 2.2272609 0.0424588233
## MealFor2
```

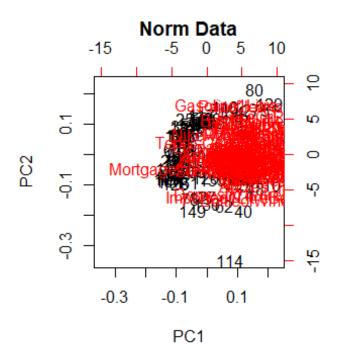
```
## McMealMcDonalds 0.09774089 0.001002934 0.6692258 0.0013969199
## DomesticBeer
                   23.74970555 0.243945912 7.8027319 0.1339669223
#-----
#pca 1 have the most variance
#To confirm it do summary (pca)
summary(GDPdataTrainSet.pca.normdata)
## Importance of components:
##
                             PC1
                                     PC2
                                             PC3
                                                    PC4
                                                            PC5
                                                                    PC6
                                                                            Ρ
C7
## Standard deviation
                          5.3910 2.11885 2.00233 1.6661 1.35194 1.24836 1.072
## Proportion of Variance 0.5382 0.08314 0.07425 0.0514 0.03385 0.02886 0.021
31
## Cumulative Proportion 0.5382 0.62135 0.69559 0.7470 0.78085 0.80970 0.831
02
##
                              PC8
                                      PC9
                                             PC10
                                                     PC11
                                                             PC12
                                                                     PC13
PC14
                          1.02113 0.93983 0.87451 0.82759 0.75936 0.68428 0.6
## Standard deviation
6622
## Proportion of Variance 0.01931 0.01636 0.01416 0.01268 0.01068 0.00867 0.0
## Cumulative Proportion 0.85033 0.86669 0.88085 0.89353 0.90421 0.91288 0.9
2110
##
                            PC15
                                    PC16
                                            PC17
                                                    PC18
                                                            PC19
                                                                    PC20
                                                                            Ρ
C21
## Standard deviation
                          0.6447 0.59364 0.58474 0.56078 0.52856 0.51585 0.48
052
## Proportion of Variance 0.0077 0.00653 0.00633 0.00582 0.00517 0.00493 0.00
428
## Cumulative Proportion 0.9288 0.93532 0.94166 0.94748 0.95265 0.95758 0.96
186
##
                             PC22
                                     PC23
                                             PC24
                                                    PC25
                                                           PC26
                                                                   PC27
                                                                           PC
28
## Standard deviation
                          0.44487 0.42751 0.41234 0.3960 0.3678 0.35827 0.341
80
## Proportion of Variance 0.00367 0.00338 0.00315 0.0029 0.0025 0.00238 0.002
15
## Cumulative Proportion 0.96552 0.96891 0.97205 0.9750 0.9775 0.97984 0.981
99
##
                             PC29
                                     PC30
                                            PC31
                                                    PC32
                                                            PC33
                                                                    PC34
                                                                            Ρ
C35
                          0.31370 0.30362 0.2938 0.27272 0.26336 0.25612 0.24
## Standard deviation
## Proportion of Variance 0.00182 0.00171 0.0016 0.00138 0.00128 0.00121 0.00
107
## Cumulative Proportion 0.98382 0.98552 0.9871 0.98850 0.98978 0.99100 0.99
207
```

```
##
                             PC36
                                    PC37
                                            PC38
                                                     PC39
                                                             PC40
                                                                     PC41
PC42
## Standard deviation
                          0.23061 0.22147 0.20875 0.19810 0.19150 0.18488 0.1
6701
## Proportion of Variance 0.00098 0.00091 0.00081 0.00073 0.00068 0.00063 0.0
## Cumulative Proportion 0.99305 0.99396 0.99477 0.99549 0.99617 0.99680 0.9
9732
                             PC43
                                     PC44
##
                                            PC45
                                                     PC46
                                                             PC47
                                                                     PC48
PC49
## Standard deviation
                          0.15845 0.14994 0.14446 0.13331 0.11751 0.11295 0.0
9906
## Proportion of Variance 0.00046 0.00042 0.00039 0.00033 0.00026 0.00024 0.0
0018
## Cumulative Proportion 0.99779 0.99820 0.99859 0.99892 0.99917 0.99941 0.9
9959
##
                             PC50
                                     PC51
                                             PC52
                                                     PC53
                                                             PC54
## Standard deviation
                          0.09357 0.08600 0.05447 0.04900 0.02284
## Proportion of Variance 0.00016 0.00014 0.00005 0.00004 0.00001
## Cumulative Proportion 0.99975 0.99989 0.99995 0.99999 1.00000
# We obtained 55 principle component
#The first 19 components account for >95% of total variance in the data
# Biplot the first two PCs.
#dim(GDPdataTrainSet.pca.normdata$x)
boxplot(GDPdataTrainSet.pca.normdata$x, main='Norm Data Transformation')
```

Norm Data Transformation



#Visualize first two components of your PCA. biplot(GDPdataTrainSet.pca.normdata, choices = 1:2, main='Norm Data')



#correlations of the PCs

cor(GDPdataTrainSet.pca.normdata\$x)

```
##
                  PC1
                                PC2
                                              PC3
                                                            PC4
                                                                          PC5
## PC1
         1.000000e+00 -7.948002e-15
                                    5.913282e-16
                                                  5.076718e-16 -7.564693e-16
## PC2
        -7.948002e-15
                      1.000000e+00 -9.553407e-16 -5.294540e-16
                                                                9.984320e-17
## PC3
         5.913282e-16 -9.553407e-16
                                    1.000000e+00
                                                  1.239250e-16 -2.082033e-16
## PC4
         5.076718e-16 -5.294540e-16
                                                 1.000000e+00
                                    1.239250e-16
                                                                1.208962e-16
## PC5
        -7.564693e-16 9.984320e-17 -2.082033e-16 1.208962e-16
                                                                 1.000000e+00
## PC6
         3.414830e-16
                      2.648861e-16 -4.616705e-16 -3.496233e-16 -2.058682e-16
## PC7
        -5.575013e-16 -1.543831e-16 -2.340112e-16 -1.361384e-17
                                                                 2.800049e-18
## PC8
         3.263520e-17 -3.533789e-16 -1.639907e-16
                                                  3.528985e-16 -2.465244e-16
## PC9
         1.439891e-16 2.236913e-16 5.502265e-16
                                                  3.173884e-18 -2.887374e-17
## PC10 -9.559588e-17 -3.941180e-17 -4.775818e-16 -3.850242e-16
                                                                1.269447e-16
## PC11 -6.927158e-16 -3.836315e-17 -1.060939e-17 -1.816881e-16
                                                                3.894019e-16
## PC12 -7.047251e-17
                      3.024758e-16 9.012465e-17 -6.673443e-16
                                                                3.009198e-16
                                                  3.709589e-16
## PC13 -2.259207e-16 -3.199110e-16 -1.022500e-15
                                                                1.776320e-16
## PC14 7.798662e-16 -7.901216e-16 2.230754e-16
                                                  1.971315e-16
                                                                 1.923559e-16
## PC15
        1.673981e-15
                      6.396877e-16
                                    2.371545e-16 8.157703e-17 -1.775563e-16
## PC16 3.033266e-17 -4.829173e-16
                                    1.305529e-16
                                                  1.144085e-16 -3.712162e-16
## PC17 -1.234843e-16 -3.755865e-16
                                    1.626027e-16 -4.162635e-16
                                                                 3.804050e-16
## PC18 -2.582267e-16 7.351428e-16 4.609631e-16 -3.816621e-17 5.259228e-16
```

```
3.743394e-16 -5.382046e-16 -2.248387e-16 2.995117e-16 -5.444638e-16
## PC19
## PC20
         2.056028e-16
                       4.741192e-16
                                    7.913332e-16 -1.250846e-16 8.194161e-17
## PC21
         1.283282e-15
                       3.281815e-16
                                    2.413560e-16
                                                  3.936299e-16 -7.179894e-16
## PC22 -5.616205e-16
                       8.081755e-17
                                    3.152204e-16 -8.394959e-16 2.006950e-16
## PC23
         1.226856e-15
                       8.729398e-16 -1.033733e-15
                                                  1.406302e-15 -9.860354e-16
## PC24 -7.957892e-16
                       5.737854e-16 -1.383258e-15
                                                   3.468024e-16 -1.200057e-15
                       1.550473e-15 -1.933245e-16
## PC25
         1.365530e-15
                                                   8.949048e-16 -3.184151e-16
## PC26 -5.921703e-16
                     -2.137280e-16 2.680470e-16
                                                   4.325525e-16 -1.102550e-15
## PC27 -2.211472e-15
                       4.672536e-16 -8.058100e-16
                                                   6.830964e-16 -2.635223e-16
## PC28 -2.523559e-15
                       4.346105e-16 -1.515687e-15 -2.273751e-16
                                                                3.355442e-16
## PC29
        4.536241e-15 -8.683120e-17 8.370679e-16 -7.036917e-16
                                                                 5.415253e-16
## PC30 -2.031036e-15
                       1.392623e-17 4.349247e-16
                                                   6.157842e-16
                                                                 3.208016e-16
                       8.927090e-16 -2.971606e-16 -5.112951e-16
## PC31 -2.155999e-15
                                                                 4.184851e-17
## PC32 -3.768546e-15
                      3.913387e-16 -2.533964e-16
                                                  8.563905e-17 -7.862438e-16
## PC33 -6.168452e-15 -1.067530e-15 -2.566158e-16 -8.773179e-16
                                                                 2.559996e-16
## PC34 -2.393364e-16
                      1.637275e-15 -9.551166e-16
                                                   5.122861e-16
                                                                 5.337431e-16
## PC35
         1.063132e-15 -1.766521e-15
                                    2.372577e-16 -1.485564e-15 -7.716034e-16
## PC36
         1.476919e-15 -5.246839e-16
                                    1.235353e-17 -4.005139e-16 1.289234e-15
## PC37 -8.809601e-16 -3.434880e-16
                                    9.998540e-16
                                                  9.656370e-16 -3.152642e-16
## PC38
         4.255249e-16
                      3.907053e-16
                                    8.309061e-16
                                                   1.458198e-15 -7.134943e-16
## PC39 -2.292278e-15 -2.096479e-15 -1.131211e-18
                                                   2.201110e-15 -1.829186e-15
## PC40
        7.677715e-15 -1.021114e-15 -1.063400e-15
                                                   4.268771e-16 -7.188552e-16
## PC41 -2.008741e-15
                      8.937684e-16 -1.096736e-15
                                                   1.777538e-16 -2.154393e-16
        4.589955e-15 -1.489897e-16 -2.469240e-16
## PC42
                                                   1.436391e-15 -1.990360e-16
## PC43
         1.032674e-14 -6.518663e-16 -4.665142e-16
                                                  4.698862e-19 3.694317e-16
## PC44
         1.741612e-16
                      2.119164e-15
                                    3.126149e-16 -1.634674e-15 1.217966e-15
## PC45 -3.196953e-15
                      1.469111e-15 -8.140933e-16 -4.514577e-16 -2.723826e-17
## PC46 -5.931774e-15 -3.618915e-15 -7.085198e-16 -1.992713e-15 -1.048438e-16
## PC47 -2.213842e-15
                      1.044760e-15
                                    5.076239e-15
                                                  1.588380e-15 -8.894109e-16
## PC48 -2.885707e-15 -1.108834e-15 -1.240739e-15 -2.296829e-17 -2.324959e-15
## PC49 -1.090175e-15 -3.734902e-16
                                    1.297233e-15
                                                   6.330508e-16 -3.646366e-15
## PC50 -1.085299e-14 -3.105598e-15 -2.793472e-15
                                                   1.427591e-15 -2.901522e-15
## PC51 -4.277645e-15
                      9.069281e-16 -6.792805e-16
                                                   3.666771e-16 -2.781161e-15
## PC52 -1.106550e-14
                      5.520437e-17
                                    6.858737e-16 -3.255756e-17 -2.937246e-15
## PC53
         1.182701e-14 -4.470542e-15
                                     2.766986e-15 -4.749521e-15
                                                                3.777338e-15
## PC54
         3.752027e-15
                       1.119677e-15 -1.081259e-16 -3.682398e-16
                                                                 3.611327e-15
##
                  PC<sub>6</sub>
                                PC7
                                              PC8
                                                            PC9
                                                                         PC10
## PC1
         3.414830e-16 -5.575013e-16
                                    3.263520e-17
                                                   1.439891e-16 -9.559588e-17
## PC2
         2.648861e-16 -1.543831e-16 -3.533789e-16
                                                  2.236913e-16 -3.941180e-17
## PC3
        -4.616705e-16 -2.340112e-16 -1.639907e-16
                                                   5.502265e-16 -4.775818e-16
                                                   3.173884e-18 -3.850242e-16
        -3.496233e-16 -1.361384e-17 3.528985e-16
## PC4
## PC5
        -2.058682e-16
                      2.800049e-18 -2.465244e-16 -2.887374e-17
                                                                 1.269447e-16
## PC6
         1.000000e+00 -4.014249e-16 8.634608e-16 -1.358350e-16 -1.419515e-16
## PC7
        -4.014249e-16
                      1.000000e+00 -1.361944e-16 -4.764861e-16
                                                                 2.804249e-16
## PC8
         8.634608e-16 -1.361944e-16
                                    1.000000e+00
                                                  1.362426e-16
                                                                 2.906796e-17
## PC9
        -1.358350e-16 -4.764861e-16
                                    1.362426e-16 1.000000e+00 -1.842655e-16
## PC10 -1.419515e-16
                      2.804249e-16
                                    2.906796e-17 -1.842655e-16
                                                                 1.000000e+00
                                                                 8.801365e-16
## PC11 -4.493073e-18 -1.079487e-16 -1.764076e-16 -5.100238e-16
## PC12
         2.733683e-16
                      1.570343e-16 -1.046860e-16 5.587428e-16
                                                                 4.386427e-16
## PC13 2.027779e-17 2.233654e-16 4.049102e-16 -6.247068e-16 1.382096e-16
```

```
2.574289e-16 -3.146632e-16 -1.335866e-16 -2.603191e-16
## PC14 -3.030562e-16
## PC15 -4.718471e-16
                       1.244291e-16
                                     2.517309e-16
                                                   1.029417e-17 -1.765237e-16
## PC16 -1.265993e-16
                       2.925690e-16
                                     1.459095e-16 -1.826173e-17 -9.923439e-18
## PC17 -6.465558e-17
                       7.122154e-17
                                     5.379533e-17
                                                   4.340017e-17 -3.377054e-16
## PC18 -6.562445e-17 -5.411412e-16 -2.401466e-16
                                                   1.712789e-16 3.013491e-16
## PC19 -7.069633e-16
                       1.991034e-16
                                     2.732003e-16 -3.358372e-16 -1.670304e-16
                                                   5.053958e-17 -6.147474e-16
## PC20
         3.134041e-16 -1.061703e-16
                                     5.737116e-16
## PC21 -8.267770e-16 -9.434006e-17
                                     1.590591e-17
                                                   4.642507e-17 -3.062753e-16
## PC22 -4.047782e-16
                       1.317516e-16
                                     4.005745e-16
                                                   6.891306e-17 -2.748791e-17
## PC23
         6.082520e-17
                       7.631276e-16
                                     1.782941e-17
                                                   1.193405e-15
                                                                 2.402679e-16
## PC24 -9.740826e-16 -1.542939e-17 -1.513397e-16
                                                   2.192129e-16
                                                                 4.892508e-16
## PC25 -7.905831e-16
                      3.244108e-16 6.991549e-16 -1.879264e-17
                                                                 1.569171e-16
## PC26 -4.079467e-17 -4.326666e-16 -1.086271e-16 -6.582951e-16 -6.361224e-16
## PC27 -8.096428e-16
                      3.093751e-16 -8.309554e-16 -7.225492e-16 -9.960662e-18
## PC28 -2.082327e-16 -1.858685e-16
                                    5.559183e-16
                                                   4.364620e-16 -3.148686e-16
## PC29 -5.466496e-16
                       7.802713e-16 -5.179820e-16
                                                   2.269082e-16 -2.669807e-16
## PC30 -1.134762e-17
                       1.436733e-16
                                     2.935981e-16
                                                   4.062375e-16
                                                                 3.872260e-16
## PC31 -3.833190e-17 -4.605445e-16
                                     4.249529e-16 -6.725630e-17
                                                                  1.591461e-16
## PC32 -1.840207e-15
                       2.779780e-16
                                    3.683630e-16
                                                   6.550889e-16
                                                                  2.130666e-16
## PC33 -2.968977e-16
                       9.378604e-16 -1.423947e-16
                                                   5.443978e-16 -3.795640e-16
                      4.830788e-16 -5.914536e-16
## PC34
        1.508202e-16
                                                   2.164918e-16
                                                                 5.946172e-17
## PC35 -1.066555e-15
                       4.716800e-16 -6.168508e-16 -5.067762e-18
                                                                 5.570065e-16
## PC36 -1.430756e-16
                       2.201266e-16
                                    2.095009e-16 -2.627233e-16 -6.600205e-17
                     -5.163609e-16
                                     6.178868e-16 -1.155442e-15
## PC37
         8.411065e-16
                                                                  5.624459e-16
## PC38 -8.991797e-16 -3.410506e-16
                                     1.632976e-16 -3.373767e-16
                                                                 8.166380e-16
## PC39 -9.552180e-16
                     -8.051125e-16
                                     2.307728e-16 -7.017284e-16 -8.282789e-17
## PC40
         1.310452e-15
                       1.102308e-16 -7.560182e-16 -7.515547e-16 -4.486314e-17
## PC41
        6.759947e-16
                       1.220395e-16
                                    1.072385e-15 -7.098112e-16 -6.570273e-16
## PC42
         1.282472e-15
                       1.449709e-15 -1.105054e-16 -1.959209e-15 -1.135296e-15
## PC43 -2.962904e-16 -1.929744e-16
                                     1.596568e-16
                                                   9.885919e-17 -2.187183e-16
## PC44 -2.137477e-16
                       2.552666e-16
                                    4.166522e-16 8.214928e-16 -2.130978e-16
                                    1.112178e-16 -7.384909e-16 -1.054244e-16
## PC45 -1.992477e-16
                       9.468981e-17
## PC46
         3.036041e-16
                       1.107838e-16 -7.500215e-16 -7.716128e-16 -1.267356e-16
## PC47 -9.267837e-16
                     -1.059120e-15 -5.713611e-16 -9.503313e-16 1.817920e-15
## PC48
         7.838965e-16
                       1.126691e-15 -1.215339e-15 -1.102115e-16 -3.603879e-16
## PC49
                       4.467436e-16 1.093566e-15 -1.468961e-15 -1.646864e-16
         1.594357e-15
## PC50 -3.083829e-15
                       3.657712e-16 -1.425415e-15 6.928758e-16
                                                                 1.842490e-15
## PC51
         2.025886e-15 -2.127660e-16 -3.421823e-15 -2.021353e-15 -1.835860e-16
## PC52
         1.897820e-15 -1.552744e-15
                                    1.460050e-15 -1.468410e-15
                                                                 3.281656e-15
## PC53
         7.076433e-16 -1.594417e-15
                                     5.579465e-15 -3.004247e-16
                                                                  2.567748e-15
## PC54 -3.436094e-15
                       4.974963e-16 -6.944760e-15
                                                   2.867047e-16
                                                                  5.320617e-15
##
                 PC11
                               PC12
                                             PC13
                                                            PC14
                                                                          PC15
## PC1
        -6.927158e-16 -7.047251e-17 -2.259207e-16
                                                   7.798662e-16
                                                                  1.673981e-15
## PC2
        -3.836315e-17
                       3.024758e-16 -3.199110e-16 -7.901216e-16
                                                                  6.396877e-16
## PC3
        -1.060939e-17
                      9.012465e-17 -1.022500e-15
                                                   2.230754e-16
                                                                  2.371545e-16
## PC4
        -1.816881e-16 -6.673443e-16
                                     3.709589e-16
                                                   1.971315e-16
                                                                  8.157703e-17
## PC5
         3.894019e-16
                       3.009198e-16
                                     1.776320e-16
                                                   1.923559e-16 -1.775563e-16
## PC6
        -4.493073e-18
                       2.733683e-16
                                     2.027779e-17 -3.030562e-16 -4.718471e-16
## PC7
        -1.079487e-16
                       1.570343e-16
                                     2.233654e-16 2.574289e-16
                                                                  1.244291e-16
## PC8
        -1.764076e-16 -1.046860e-16 4.049102e-16 -3.146632e-16 2.517309e-16
```

```
5.587428e-16 -6.247068e-16 -1.335866e-16
## PC9 -5.100238e-16
                                                                 1.029417e-17
## PC10
        8.801365e-16
                       4.386427e-16
                                    1.382096e-16 -2.603191e-16 -1.765237e-16
## PC11
         1.000000e+00 -6.362304e-17 -5.749425e-16 -5.231204e-17
                                                                 1.857895e-16
## PC12 -6.362304e-17
                       1.000000e+00
                                    2.585180e-16 -2.248990e-16
                                                                 5.160888e-16
## PC13 -5.749425e-16
                       2.585180e-16
                                     1.000000e+00 1.443996e-15
                                                                 3.165052e-16
## PC14 -5.231204e-17 -2.248990e-16
                                     1.443996e-15
                                                   1.000000e+00 -8.610867e-17
## PC15
         1.857895e-16
                       5.160888e-16
                                     3.165052e-16 -8.610867e-17
                                                                 1.000000e+00
## PC16 -5.794859e-17
                     -5.408934e-17 -1.440872e-15 -5.930428e-16
                                                                 6.493372e-16
## PC17
         4.860485e-18
                       1.004205e-15
                                     1.107497e-16 -1.596030e-16 -5.864633e-16
## PC18 -5.478085e-17
                                     1.234221e-16 -6.734329e-16 -9.240250e-16
                       4.142568e-16
## PC19 -1.805263e-16
                       2.363011e-16
                                     1.411593e-16 -4.820401e-16 -6.058638e-16
## PC20
         4.423225e-17
                       4.624105e-16
                                    1.372080e-16 -5.840336e-17 -3.242585e-16
                       7.897297e-17 -4.513741e-16 -1.691606e-16
## PC21
         2.020379e-16
                                                                 6.503725e-17
## PC22 -4.032636e-16
                       1.607042e-16 -1.288564e-16 -2.141705e-16
                                                                 2.027448e-16
## PC23
         4.433897e-16 -8.476026e-16
                                    4.878715e-16
                                                  3.754774e-16
                                                                 2.276740e-16
        1.118628e-16 -4.062789e-17 -1.897198e-16
                                                  4.679475e-16 -1.361754e-16
## PC25 -1.312711e-16
                      2.273441e-16 -1.608222e-16
                                                   3.665444e-16 -2.917067e-16
## PC26 -7.003257e-16
                      4.607068e-16 -1.109613e-15 -2.015698e-16
                                                                 1.822501e-16
## PC27 -3.374269e-16 -2.081138e-16
                                    2.653563e-16
                                                  4.581133e-16
                                                                 2.494247e-16
## PC28 -1.067309e-16 -4.258527e-16
                                    3.504692e-16
                                                  4.455973e-16
                                                                 2.371446e-16
                      2.495130e-16 -3.698455e-16 -2.294963e-16
## PC29 -2.416930e-16
                                                                 8.245281e-16
## PC30 -2.543881e-16 -8.129161e-16
                                    7.365181e-16 -1.959507e-16
                                                                 2.837868e-16
        1.057565e-15 -9.701685e-17
                                    1.291271e-16 -2.193495e-16
                                                                 2.043228e-16
## PC31
## PC32 -3.778523e-16 -2.262537e-16 -9.592282e-16
                                                   8.209465e-16 -7.553435e-17
## PC33 -5.316405e-18 -1.389578e-16
                                    5.727076e-16
                                                   1.039719e-15
                                                                 1.661001e-16
## PC34
         7.418326e-16 -8.920061e-16
                                    3.659120e-17 -3.945580e-16 -6.077413e-17
## PC35
         5.346556e-16 -4.705552e-17 -4.840942e-16
                                                  6.417451e-16
                                                                 1.275349e-15
## PC36 4.868095e-17 -6.248170e-17 -1.090400e-15 -3.502286e-17
                                                                 2.073138e-16
## PC37 -3.723511e-16 -1.763202e-16 -5.668982e-16 -3.338089e-16
                                                                 1.917475e-16
## PC38 -9.122181e-16 9.898756e-16 -2.789325e-16 -6.320873e-16 -2.556118e-17
## PC39 -8.236149e-16 -2.426580e-15
                                    4.425938e-16
                                                   9.425632e-16
                                                                 4.962271e-16
## PC40 -7.271162e-16 -5.986058e-16
                                    1.159689e-16
                                                   4.095940e-17
                                                                 1.733377e-16
## PC41
        7.653457e-16 -2.738959e-16
                                    8.067283e-16
                                                   7.691240e-17
                                                                 7.962203e-16
## PC42 -1.014142e-15 -1.355900e-15
                                    1.839691e-17
                                                   6.030467e-17
                                                                 1.785575e-16
## PC43 -4.471126e-16 -6.471907e-16 -3.820958e-16
                                                   1.001862e-15
                                                                 3.262412e-16
## PC44 -1.030759e-16
                      2.180975e-16 -3.521385e-16 -2.064989e-16 -5.191069e-16
## PC45 -1.106814e-15 -1.677471e-16 -5.942605e-16
                                                  9.604160e-16 -1.005448e-15
                      8.854368e-16
## PC46
       4.122429e-16
                                    3.874791e-16
                                                   5.956798e-17 -1.088020e-16
## PC47 -9.204675e-16 -6.739227e-16 4.670321e-16 -3.983414e-16 4.922746e-16
## PC48 -4.341432e-16 -6.848356e-16
                                    1.149226e-15 -6.463740e-16 -1.270110e-15
## PC49 -6.250681e-16 -1.467558e-15
                                    4.208661e-16 -9.257280e-17
                                                                 1.145147e-16
## PC50 1.768489e-15 -1.368166e-15 -4.429650e-16
                                                  6.932432e-16
                                                                 8.517087e-16
## PC51 -4.032251e-16
                      1.247552e-15 -1.647988e-16
                                                  1.165759e-15 -1.067912e-15
## PC52 -5.313427e-16 -3.017558e-15 -9.894621e-17 -2.443149e-15
                                                                 2.168672e-15
## PC53 -1.657473e-15
                      3.311296e-15 -8.531662e-16
                                                  1.144921e-15 -7.977412e-16
## PC54 -4.145559e-15 -5.822745e-15
                                     1.204401e-16
                                                   3.942666e-15 -6.294080e-15
##
                 PC16
                               PC17
                                             PC18
                                                           PC19
                                                                         PC20
## PC1
         3.033266e-17 -1.234843e-16 -2.582267e-16
                                                   3.743394e-16
                                                                 2.056028e-16
## PC2
        -4.829173e-16 -3.755865e-16
                                    7.351428e-16 -5.382046e-16
                                                                 4.741192e-16
## PC3
        1.305529e-16 1.626027e-16 4.609631e-16 -2.248387e-16 7.913332e-16
```

```
## PC4
         1.144085e-16 -4.162635e-16 -3.816621e-17 2.995117e-16 -1.250846e-16
## PC5
        -3.712162e-16
                       3.804050e-16 5.259228e-16 -5.444638e-16
                                                                 8.194161e-17
## PC6
        -1.265993e-16 -6.465558e-17 -6.562445e-17 -7.069633e-16
                                                                 3.134041e-16
                       7.122154e-17 -5.411412e-16
## PC7
         2.925690e-16
                                                   1.991034e-16 -1.061703e-16
         1.459095e-16
## PC8
                       5.379533e-17 -2.401466e-16
                                                   2.732003e-16
                                                                 5.737116e-16
## PC9
        -1.826173e-17
                       4.340017e-17
                                     1.712789e-16 -3.358372e-16
                                                                 5.053958e-17
## PC10 -9.923439e-18 -3.377054e-16
                                     3.013491e-16 -1.670304e-16 -6.147474e-16
## PC11 -5.794859e-17
                       4.860485e-18 -5.478085e-17 -1.805263e-16
                                                                 4.423225e-17
## PC12 -5.408934e-17
                       1.004205e-15
                                    4.142568e-16
                                                   2.363011e-16
                                                                 4.624105e-16
## PC13 -1.440872e-15
                                     1.234221e-16
                                                                 1.372080e-16
                       1.107497e-16
                                                   1.411593e-16
## PC14 -5.930428e-16 -1.596030e-16 -6.734329e-16 -4.820401e-16 -5.840336e-17
## PC15
         6.493372e-16 -5.864633e-16 -9.240250e-16 -6.058638e-16 -3.242585e-16
## PC16
                      2.584054e-16
         1.000000e+00
                                    1.705568e-15
                                                   3.121189e-16
                                                                 2.212962e-16
## PC17
         2.584054e-16
                      1.000000e+00 -4.339928e-16 -4.881352e-16
                                                                 1.441765e-16
## PC18
         1.705568e-15 -4.339928e-16
                                    1.000000e+00 -5.397083e-16
                                                                 3.644388e-16
## PC19
         3.121189e-16 -4.881352e-16 -5.397083e-16
                                                   1.000000e+00
                                                                 1.491278e-16
## PC20
         2.212962e-16
                      1.441765e-16
                                    3.644388e-16
                                                   1.491278e-16
                                                                 1.000000e+00
## PC21 -5.458251e-16 -4.575513e-16 -3.209766e-16
                                                   8.871609e-16 -1.567397e-16
## PC22
        8.568371e-17 -4.338806e-16 -2.346479e-16
                                                   1.065501e-16 -2.550405e-16
## PC23 -1.733882e-16
                      5.843531e-16
                                    5.701653e-16
                                                   6.959729e-16 -2.855981e-16
## PC24 -1.232275e-16 -4.801295e-16 -5.538206e-16
                                                   3.186580e-16 -8.611716e-17
## PC25
         4.487146e-16
                      2.378190e-16
                                    9.362966e-17 -3.625792e-16 -2.445928e-16
## PC26 -6.889961e-17 -3.173468e-16
                                     1.975048e-16
                                                   3.798933e-16 -2.026112e-16
## PC27 -1.724740e-16
                                                   2.029943e-16 1.810865e-16
                       1.167727e-16
                                     5.900153e-17
## PC28
         5.671087e-16
                      6.036476e-16 -5.718813e-16
                                                   1.418524e-16 -2.712589e-16
## PC29 -1.441955e-16 -6.062723e-16 -6.692100e-18
                                                   2.293551e-16 -4.133915e-16
## PC30
         1.566994e-16 -1.567311e-16
                                                   4.688787e-16 2.005391e-16
                                    7.400339e-16
## PC31 -6.449148e-16
                      6.402692e-16
                                    1.883117e-16
                                                   1.087290e-16 3.568049e-16
## PC32
         4.318954e-16 -5.351941e-16 -1.644074e-16
                                                   5.947182e-16 -3.057060e-16
                                                   4.420698e-16 -4.029685e-16
## PC33
                       1.594904e-16 -4.402171e-16
         2.027496e-16
## PC34 -4.954333e-16
                       6.849574e-16
                                    1.295974e-16
                                                   1.031238e-16 -4.298513e-16
## PC35
         7.474324e-16
                       3.325550e-16 -9.426969e-16
                                                   6.835815e-16 2.730781e-18
## PC36
         1.664614e-16
                       1.238976e-15
                                    2.715106e-16 -7.403869e-16
                                                                 8.646833e-16
## PC37
         6.716925e-16 -1.351509e-16 -1.295783e-16
                                                   3.199250e-16 -1.630519e-16
## PC38
         8.033814e-16 -3.637049e-16 -6.883829e-16
                                                   7.523124e-17 -3.045536e-16
## PC39 -3.628482e-16 -4.126695e-16 9.508136e-17 -6.180309e-16 -2.538614e-16
## PC40 -1.117760e-16
                      3.166447e-16 -1.187367e-15 -7.294901e-17
                                                                 2.561349e-17
                      2.923074e-16 -3.555179e-16
## PC41 -8.473388e-16
                                                   8.621749e-17 -1.143850e-16
        3.267219e-16 -4.567887e-16 2.274444e-16 -1.710286e-15
                                                                 1.817502e-16
## PC42
## PC43 -1.004384e-16 -4.454406e-16 -5.355739e-16 -1.072965e-16 -1.231776e-16
## PC44 -2.918449e-16
                      3.114973e-16 -1.237697e-15 -3.222329e-16
                                                                 2.127922e-16
## PC45
         2.064584e-16 -1.891637e-16
                                    1.305911e-16 -5.420260e-16
                                                                 8.084053e-16
## PC46
         4.594167e-16 -1.635312e-16 -9.970177e-16
                                                   3.591923e-16
                                                                -2.437023e-16
## PC47 -9.979405e-16
                      7.250476e-16 2.508653e-17
                                                   6.087997e-16
                                                                 1.969475e-16
## PC48 -1.311204e-15 -4.156936e-16 -1.020571e-15
                                                   2.640294e-16
                                                                 4.025027e-17
## PC49
        4.192908e-16 -5.429973e-16 -2.544524e-16 -2.690889e-16
                                                                 1.269315e-15
## PC50
        3.205167e-17 -5.180771e-17
                                    2.970991e-16
                                                   6.087083e-16
                                                                 3.609723e-18
## PC51 -1.199537e-15 -1.796229e-15 -6.908279e-16 -2.286192e-15
                                                                 1.680352e-15
## PC52 -2.959468e-16
                      3.393597e-17
                                    2.073048e-15 -1.348470e-15
                                                                 1.898225e-15
## PC53 1.516552e-15 2.178308e-15 -1.161311e-15 3.343703e-15
                                                                 1.092237e-15
```

```
## PC54
                      6.298601e-15
                                     9.671620e-16 -3.734364e-15
         4.302859e-15
                                                                  1.426010e-15
##
                 PC21
                               PC22
                                             PC23
                                                            PC24
                                                                          PC25
## PC1
         1.283282e-15
                      -5.616205e-16
                                     1.226856e-15 -7.957892e-16
                                                                  1.365530e-15
## PC2
         3.281815e-16
                       8.081755e-17
                                     8.729398e-16
                                                   5.737854e-16
                                                                  1.550473e-15
## PC3
         2.413560e-16
                       3.152204e-16 -1.033733e-15 -1.383258e-15 -1.933245e-16
## PC4
         3.936299e-16
                     -8.394959e-16
                                     1.406302e-15
                                                   3.468024e-16
                                                                  8.949048e-16
## PC5
                                    -9.860354e-16 -1.200057e-15 -3.184151e-16
        -7.179894e-16
                       2.006950e-16
## PC6
        -8.267770e-16 -4.047782e-16
                                     6.082520e-17 -9.740826e-16 -7.905831e-16
## PC7
        -9.434006e-17
                       1.317516e-16
                                     7.631276e-16 -1.542939e-17
                                                                 3.244108e-16
## PC8
                                     1.782941e-17 -1.513397e-16
         1.590591e-17
                       4.005745e-16
                                                                  6.991549e-16
## PC9
         4.642507e-17
                       6.891306e-17
                                     1.193405e-15
                                                   2.192129e-16 -1.879264e-17
## PC10 -3.062753e-16 -2.748791e-17
                                     2.402679e-16
                                                   4.892508e-16
                                                                 1.569171e-16
         2.020379e-16 -4.032636e-16
                                                   1.118628e-16 -1.312711e-16
## PC11
                                     4.433897e-16
## PC12
         7.897297e-17
                      1.607042e-16 -8.476026e-16 -4.062789e-17
                                                                 2.273441e-16
## PC13 -4.513741e-16 -1.288564e-16
                                     4.878715e-16 -1.897198e-16 -1.608222e-16
## PC14 -1.691606e-16 -2.141705e-16
                                     3.754774e-16 4.679475e-16
                                                                 3.665444e-16
## PC15
         6.503725e-17
                       2.027448e-16
                                     2.276740e-16 -1.361754e-16 -2.917067e-16
## PC16 -5.458251e-16
                      8.568371e-17 -1.733882e-16 -1.232275e-16
                                                                 4.487146e-16
## PC17 -4.575513e-16 -4.338806e-16
                                     5.843531e-16 -4.801295e-16
                                                                  2.378190e-16
## PC18 -3.209766e-16 -2.346479e-16
                                     5.701653e-16 -5.538206e-16
                                                                  9.362966e-17
## PC19
         8.871609e-16
                       1.065501e-16
                                     6.959729e-16
                                                   3.186580e-16 -3.625792e-16
## PC20 -1.567397e-16 -2.550405e-16 -2.855981e-16 -8.611716e-17 -2.445928e-16
## PC21
         1.000000e+00
                       3.498968e-17
                                    6.655008e-16 7.004277e-16
                                                                 4.320383e-16
## PC22
                       1.000000e+00 -3.743668e-16 -1.090458e-15
         3.498968e-17
                                                                  3.724290e-16
## PC23
         6.655008e-16 -3.743668e-16
                                    1.000000e+00 -9.779268e-16
                                                                  5.379558e-17
## PC24
         7.004277e-16 -1.090458e-15 -9.779268e-16
                                                   1.000000e+00
                                                                  1.076917e-16
## PC25
                      3.724290e-16
                                    5.379558e-17
         4.320383e-16
                                                   1.076917e-16
                                                                  1.000000e+00
## PC26
         1.975073e-16 -9.047705e-16 6.938211e-16 -2.746274e-16
                                                                  3.411375e-16
## PC27
         3.952673e-16 -6.765692e-16
                                    5.711712e-16 -2.171631e-16 -4.836220e-16
## PC28
         2.373684e-16 -1.067840e-17 -1.968228e-16
                                                   5.323179e-16
                                                                 7.079297e-17
## PC29
         3.220129e-16 -2.031372e-16 -9.081696e-16 -6.201059e-16 -2.991428e-16
## PC30 -1.768836e-16 -1.073249e-16 -3.758030e-16
                                                   1.058629e-16 -4.839418e-17
## PC31 -7.046020e-16
                       7.872936e-16 -2.851115e-16
                                                   6.262042e-16
                                                                  3.926918e-16
## PC32
         5.887120e-16 -2.408766e-18 1.487602e-17 -1.855054e-16 -8.062035e-17
## PC33
         4.412897e-18 -8.975258e-17 -4.427006e-16 -8.676965e-16
                                                                 9.501292e-17
## PC34
                      2.248980e-16 -1.654271e-16
         2.686926e-16
                                                   8.709009e-16
                                                                 1.421465e-15
## PC35 -7.407990e-16 -3.507744e-16
                                    1.165673e-16 4.998070e-16 -3.130122e-16
                       7.259129e-16 -6.088846e-17 -4.349920e-17 -1.168050e-16
## PC36 -4.573592e-16
## PC37 -2.340338e-16
                       5.880067e-16
                                    5.866880e-16 -4.452363e-16 -4.440995e-16
## PC38
         5.050587e-16
                       6.747881e-16
                                     6.462580e-16 -1.002660e-16 -1.650603e-17
## PC39
         2.425847e-16
                       9.039142e-16
                                     1.469814e-16
                                                   2.408670e-16
                                                                3.625894e-16
## PC40 -3.697230e-16 -1.760284e-16
                                     4.391360e-16
                                                   1.647694e-15 -6.168158e-16
## PC41 -6.493451e-17 -3.390257e-16 -1.058046e-15 -1.691452e-16 -8.520200e-17
## PC42
         3.708618e-16
                       1.021352e-16 -5.064490e-16 -4.040710e-16
                                                                5.543269e-16
## PC43 -1.172176e-16
                       5.823872e-16 -9.461822e-16 -2.773436e-16 -9.710104e-16
## PC44 -5.473717e-16
                       1.200936e-16 -1.352264e-16 4.420489e-16
                                                                 2.615476e-16
## PC45 -1.040598e-16
                       2.178554e-16 -4.522907e-16
                                                   6.057840e-16
                                                                  2.012775e-16
## PC46 -7.120226e-17 -8.766105e-16 8.241293e-16 -9.632417e-16
                                                                 5.897586e-16
## PC47 -1.682566e-15
                       5.601245e-16
                                     8.241872e-16 -1.859112e-16 -1.796516e-15
## PC48 -3.014174e-16 2.757408e-17 6.481592e-16 3.904550e-16 4.306521e-16
```

```
## PC49 -1.710611e-15 2.835024e-15 -3.520886e-17 1.250139e-15 -3.918283e-16
## PC50 4.999508e-16 -9.918918e-16 4.171823e-19 5.367373e-16 9.222670e-16
## PC51
        1.452539e-15
                      1.737924e-15 -2.147507e-15
                                                  5.729243e-16 5.145923e-17
## PC52 -2.600317e-16
                      2.319329e-15 4.576027e-16
                                                  3.058556e-16
                                                                4.067921e-15
## PC53 -2.271826e-15 -2.395680e-15 8.069232e-17 -1.829256e-15 -1.659596e-15
## PC54
        2.086086e-15 -2.186907e-15 -3.849053e-15 -1.021630e-15 -7.424496e-17
##
                 PC26
                               PC27
                                             PC28
                                                           PC29
                                                                         PC30
## PC1
        -5.921703e-16 -2.211472e-15 -2.523559e-15
                                                   4.536241e-15 -2.031036e-15
## PC2
        -2.137280e-16
                     4.672536e-16 4.346105e-16 -8.683120e-17
## PC3
         2.680470e-16 -8.058100e-16 -1.515687e-15
                                                                 4.349247e-16
                                                  8.370679e-16
## PC4
         4.325525e-16 6.830964e-16 -2.273751e-16 -7.036917e-16
                                                                 6.157842e-16
## PC5
        -1.102550e-15 -2.635223e-16 3.355442e-16
                                                  5.415253e-16
                                                                 3.208016e-16
       -4.079467e-17 -8.096428e-16 -2.082327e-16 -5.466496e-16 -1.134762e-17
## PC6
## PC7
        -4.326666e-16 3.093751e-16 -1.858685e-16 7.802713e-16
                                                                 1.436733e-16
        -1.086271e-16 -8.309554e-16 5.559183e-16 -5.179820e-16
## PC8
                                                                 2.935981e-16
## PC9
        -6.582951e-16 -7.225492e-16 4.364620e-16 2.269082e-16
                                                                 4.062375e-16
## PC10 -6.361224e-16 -9.960662e-18 -3.148686e-16 -2.669807e-16
                                                                 3.872260e-16
## PC11 -7.003257e-16 -3.374269e-16 -1.067309e-16 -2.416930e-16 -2.543881e-16
## PC12 4.607068e-16 -2.081138e-16 -4.258527e-16 2.495130e-16 -8.129161e-16
## PC13 -1.109613e-15
                       2.653563e-16
                                   3.504692e-16 -3.698455e-16
                                                                 7.365181e-16
                      4.581133e-16 4.455973e-16 -2.294963e-16 -1.959507e-16
## PC14 -2.015698e-16
## PC15
        1.822501e-16
                       2.494247e-16
                                    2.371446e-16 8.245281e-16
                                                                2.837868e-16
## PC16 -6.889961e-17 -1.724740e-16
                                    5.671087e-16 -1.441955e-16
                                                               1.566994e-16
                                    6.036476e-16 -6.062723e-16 -1.567311e-16
## PC17 -3.173468e-16
                       1.167727e-16
## PC18
        1.975048e-16
                       5.900153e-17 -5.718813e-16 -6.692100e-18
                                                                 7.400339e-16
## PC19
         3.798933e-16
                       2.029943e-16
                                    1.418524e-16 2.293551e-16
                                                                4.688787e-16
                       1.810865e-16 -2.712589e-16 -4.133915e-16
## PC20 -2.026112e-16
                                                                2.005391e-16
                      3.952673e-16 2.373684e-16 3.220129e-16 -1.768836e-16
## PC21 1.975073e-16
## PC22 -9.047705e-16 -6.765692e-16 -1.067840e-17 -2.031372e-16 -1.073249e-16
                      5.711712e-16 -1.968228e-16 -9.081696e-16 -3.758030e-16
## PC23
        6.938211e-16
## PC24 -2.746274e-16 -2.171631e-16 5.323179e-16 -6.201059e-16 1.058629e-16
        3.411375e-16 -4.836220e-16 7.079297e-17 -2.991428e-16 -4.839418e-17
## PC25
## PC26
         1.000000e+00 -2.541110e-16 -4.365409e-16 4.187686e-16 -6.653631e-17
## PC27 -2.541110e-16
                      1.000000e+00 -1.001886e-15 -4.830323e-16
                                                                 5.557819e-16
## PC28 -4.365409e-16 -1.001886e-15
                                    1.000000e+00 -8.661335e-17
                                                                 6.309230e-16
## PC29
        4.187686e-16 -4.830323e-16 -8.661335e-17
                                                  1.000000e+00 -1.770756e-16
                                                                 1.000000e+00
## PC30 -6.653631e-17
                      5.557819e-16 6.309230e-16 -1.770756e-16
## PC31 -2.629922e-16 -1.146680e-16 1.398148e-16
                                                                 8.443320e-17
                                                   2.053350e-16
## PC32 -2.827447e-17
                      3.542129e-16 -6.006236e-16
                                                   2.796691e-16
                                                                 9.892874e-17
## PC33
        4.610291e-16 -3.952813e-16 -1.726786e-16
                                                   5.193066e-16
                                                                 7.629203e-17
## PC34
         2.494442e-16 -2.731931e-16 -4.243344e-16 -6.170452e-17 -2.384289e-16
                      1.522993e-16 3.672013e-16
## PC35
         1.297751e-16
                                                   9.387496e-16
                                                                 6.719547e-16
## PC36 -2.980545e-16 -2.221175e-16 -9.869036e-17
                                                   2.198614e-16
                                                                 9.325376e-16
## PC37
         2.937669e-16 -7.293349e-16 -4.268335e-16
                                                   8.666109e-16
                                                                 1.432419e-16
## PC38
        1.274057e-16
                      9.964544e-16
                                    1.413923e-17
                                                   3.055279e-16
                                                                 7.986349e-16
## PC39
        6.488032e-17
                      6.082558e-17
                                    1.922361e-16 -2.618853e-16
                                                                 1.590692e-16
## PC40 -8.076244e-16
                      5.087621e-16
                                    2.595359e-16
                                                   8.096646e-16
                                                                 4.041056e-16
        2.334016e-16 -2.121327e-16 1.500402e-16
                                                  5.390151e-16
                                                                 7.663259e-16
## PC41
## PC42
        3.912716e-16 -3.598952e-16 -4.388648e-17 -8.211921e-16
                                                                 4.815785e-16
## PC43 -6.387898e-17 3.508160e-16 -3.893239e-16 1.457338e-15 3.642031e-16
```

```
## PC44 -6.451040e-16 4.665846e-16 -3.277021e-16 3.584606e-16 1.074275e-16
## PC45
         8.370583e-16 -5.305293e-16 -1.427875e-16 -9.067582e-16 -1.893156e-15
## PC46
         2.899280e-16
                      6.872461e-16 1.231838e-15
                                                   2.828862e-16 -2.558993e-17
## PC47
         1.438885e-16
                       3.498239e-16 -9.194330e-18 -6.607552e-17 -1.174270e-15
## PC48
         1.306591e-15
                       9.379877e-16 4.932172e-16
                                                   5.605006e-16 -5.827599e-16
## PC49
         2.180920e-16 -5.928267e-17 -1.138725e-16 -6.087424e-16 -8.615460e-17
## PC50
                                                   1.878429e-16 -9.620639e-16
         2.544707e-16
                       3.447442e-16 -7.618808e-16
## PC51 -1.551765e-15
                       2.473667e-16 -1.648349e-17 -4.702651e-16 -1.114008e-16
         6.962311e-16 -5.155597e-16
                                    1.020107e-15 -1.824643e-16 1.815349e-15
## PC53 -7.097315e-16 -1.061289e-16
                                    4.457204e-16 -7.152995e-16 -1.682030e-16
## PC54
         5.143136e-15
                       6.938201e-15 -5.974576e-15
                                                   2.494087e-17 -1.074394e-15
##
                 PC31
                               PC32
                                             PC33
                                                            PC34
                                                                          PC35
## PC1
        -2.155999e-15
                     -3.768546e-15 -6.168452e-15 -2.393364e-16
                                                                  1.063132e-15
## PC2
         8.927090e-16
                      3.913387e-16 -1.067530e-15
                                                   1.637275e-15 -1.766521e-15
        -2.971606e-16 -2.533964e-16 -2.566158e-16 -9.551166e-16
## PC3
                                                                 2.372577e-16
## PC4
        -5.112951e-16
                      8.563905e-17 -8.773179e-16
                                                    5.122861e-16 -1.485564e-15
## PC5
         4.184851e-17 -7.862438e-16
                                    2.559996e-16
                                                   5.337431e-16 -7.716034e-16
## PC6
        -3.833190e-17 -1.840207e-15 -2.968977e-16
                                                   1.508202e-16 -1.066555e-15
                       2.779780e-16 9.378604e-16
## PC7
        -4.605445e-16
                                                   4.830788e-16 4.716800e-16
## PC8
         4.249529e-16
                       3.683630e-16 -1.423947e-16 -5.914536e-16 -6.168508e-16
## PC9
        -6.725630e-17
                       6.550889e-16 5.443978e-16
                                                   2.164918e-16 -5.067762e-18
## PC10
         1.591461e-16
                       2.130666e-16 -3.795640e-16
                                                   5.946172e-17
                                                                 5.570065e-16
## PC11
         1.057565e-15 -3.778523e-16 -5.316405e-18
                                                   7.418326e-16
                                                                 5.346556e-16
## PC12 -9.701685e-17 -2.262537e-16 -1.389578e-16 -8.920061e-16 -4.705552e-17
## PC13
         1.291271e-16 -9.592282e-16
                                     5.727076e-16
                                                   3.659120e-17 -4.840942e-16
## PC14 -2.193495e-16
                      8.209465e-16
                                     1.039719e-15 -3.945580e-16
                                                                  6.417451e-16
## PC15
         2.043228e-16 -7.553435e-17
                                     1.661001e-16 -6.077413e-17
                                                                  1.275349e-15
## PC16 -6.449148e-16
                      4.318954e-16
                                     2.027496e-16 -4.954333e-16
                                                                  7.474324e-16
## PC17
         6.402692e-16 -5.351941e-16
                                     1.594904e-16
                                                   6.849574e-16
                                                                  3.325550e-16
## PC18
         1.883117e-16 -1.644074e-16 -4.402171e-16
                                                   1.295974e-16 -9.426969e-16
## PC19
         1.087290e-16
                      5.947182e-16
                                     4.420698e-16
                                                   1.031238e-16
                                                                  6.835815e-16
## PC20
         3.568049e-16 -3.057060e-16 -4.029685e-16 -4.298513e-16
                                                                  2.730781e-18
## PC21 -7.046020e-16
                       5.887120e-16
                                     4.412897e-18
                                                   2.686926e-16 -7.407990e-16
## PC22
         7.872936e-16 -2.408766e-18 -8.975258e-17
                                                    2.248980e-16 -3.507744e-16
## PC23
        -2.851115e-16
                      1.487602e-17 -4.427006e-16 -1.654271e-16
                                                                  1.165673e-16
## PC24
         6.262042e-16 -1.855054e-16 -8.676965e-16
                                                   8.709009e-16
                                                                  4.998070e-16
## PC25
         3.926918e-16 -8.062035e-17
                                     9.501292e-17
                                                   1.421465e-15 -3.130122e-16
## PC26 -2.629922e-16 -2.827447e-17
                                                   2.494442e-16
                                     4.610291e-16
                                                                  1.297751e-16
## PC27 -1.146680e-16
                       3.542129e-16 -3.952813e-16 -2.731931e-16
                                                                  1.522993e-16
## PC28
         1.398148e-16 -6.006236e-16 -1.726786e-16 -4.243344e-16
                                                                  3.672013e-16
                                     5.193066e-16 -6.170452e-17
## PC29
                       2.796691e-16
         2.053350e-16
                                                                  9.387496e-16
## PC30
         8.443320e-17
                       9.892874e-17
                                     7.629203e-17 -2.384289e-16
                                                                  6.719547e-16
## PC31
         1.000000e+00
                       4.529497e-16
                                     5.333112e-16 -6.169021e-17
                                                                  8.134070e-16
## PC32
         4.529497e-16
                       1.000000e+00 -1.312767e-17
                                                   4.288441e-16
                                                                  2.451507e-16
## PC33
         5.333112e-16
                      -1.312767e-17
                                     1.000000e+00 -1.845508e-16
                                                                -3.167785e-16
## PC34 -6.169021e-17
                       4.288441e-16 -1.845508e-16
                                                   1.000000e+00
                                                                  6.445534e-16
## PC35
         8.134070e-16
                       2.451507e-16 -3.167785e-16
                                                   6.445534e-16
                                                                  1.000000e+00
## PC36 -8.449072e-16
                       2.110732e-16
                                     3.719279e-17 -3.126879e-16
                                                                  5.814507e-16
## PC37
         8.880429e-17
                       2.552403e-16
                                     2.994994e-17 -6.432229e-16 -1.058066e-16
## PC38
        2.531049e-16
                      3.853288e-16 4.985313e-16 -1.599198e-16 -1.655383e-16
```

```
## PC39
         7.100230e-17 4.434314e-16 2.387130e-17 4.974699e-16 -4.397998e-16
## PC40
         2.888201e-16 -7.551425e-16 -5.391274e-16 -2.241385e-16 -5.449489e-16
## PC41
         1.533847e-16 -2.062719e-16 -4.923912e-17
                                                   2.654904e-16 4.456680e-16
## PC42
         3.446436e-16
                      1.112521e-16
                                    2.028288e-16 -5.898712e-16 -8.924899e-16
## PC43 -6.496418e-17 -7.155726e-16 8.264898e-16 7.521814e-16 -7.590868e-16
## PC44
         1.179889e-15 -1.016783e-15 -9.283544e-16 -5.059872e-16 -1.121396e-15
## PC45
                      2.734856e-17 -1.050942e-17 -1.304384e-15
         3.763869e-16
                                                                 1.132307e-15
## PC46 -1.263179e-15 -3.554421e-16
                                    2.659597e-16
                                                   3.657319e-16
                                                                 1.030907e-16
## PC47
         4.180779e-16 -6.816243e-16
                                     1.218886e-15
                                                   8.519426e-16
                                                                 1.412481e-15
## PC48
         1.118195e-15
                                                                 4.182023e-16
                      4.882756e-16 -6.849415e-16
                                                   1.368228e-15
## PC49 -4.469183e-16
                      4.993996e-16
                                    1.457884e-16 -1.468721e-15
                                                                 1.353830e-16
## PC50 -8.621746e-16
                       7.386231e-16
                                    3.925396e-16
                                                   1.251339e-15
                                                                 2.238343e-16
## PC51 -6.482901e-16 -1.443760e-15 -1.945586e-16
                                                   4.450717e-16
                                                                 1.263267e-15
## PC52 -9.616746e-17
                       2.567465e-15
                                    2.275808e-15
                                                   1.366859e-15
                                                                 1.634383e-15
                      9.569618e-16 -1.415512e-15 -1.765261e-15 -3.987856e-17
## PC53
         2.177625e-15
## PC54 -3.167474e-15 -2.196190e-15 -4.692200e-15 -6.219265e-15
                                                                 5.232600e-15
##
                 PC36
                               PC37
                                             PC38
                                                           PC39
                                                                          PC40
## PC1
                                     4.255249e-16 -2.292278e-15
         1.476919e-15 -8.809601e-16
                                                                 7.677715e-15
## PC2
        -5.246839e-16 -3.434880e-16
                                     3.907053e-16 -2.096479e-15 -1.021114e-15
## PC3
                      9.998540e-16
                                     8.309061e-16 -1.131211e-18 -1.063400e-15
         1.235353e-17
## PC4
        -4.005139e-16
                      9.656370e-16
                                     1.458198e-15 2.201110e-15
                                                                 4.268771e-16
## PC5
         1.289234e-15 -3.152642e-16 -7.134943e-16 -1.829186e-15 -7.188552e-16
## PC6
        -1.430756e-16 8.411065e-16 -8.991797e-16 -9.552180e-16
                                                                 1.310452e-15
## PC7
         2.201266e-16 -5.163609e-16 -3.410506e-16 -8.051125e-16
                                                                 1.102308e-16
## PC8
         2.095009e-16
                      6.178868e-16 1.632976e-16 2.307728e-16 -7.560182e-16
## PC9
        -2.627233e-16 -1.155442e-15 -3.373767e-16 -7.017284e-16 -7.515547e-16
## PC10 -6.600205e-17
                      5.624459e-16 8.166380e-16 -8.282789e-17 -4.486314e-17
## PC11
        4.868095e-17 -3.723511e-16 -9.122181e-16 -8.236149e-16 -7.271162e-16
## PC12 -6.248170e-17 -1.763202e-16 9.898756e-16 -2.426580e-15 -5.986058e-16
## PC13 -1.090400e-15 -5.668982e-16 -2.789325e-16 4.425938e-16
                                                                 1.159689e-16
## PC14 -3.502286e-17 -3.338089e-16 -6.320873e-16
                                                   9.425632e-16
                                                                 4.095940e-17
                      1.917475e-16 -2.556118e-17
## PC15
         2.073138e-16
                                                   4.962271e-16
                                                                 1.733377e-16
## PC16
         1.664614e-16
                      6.716925e-16 8.033814e-16 -3.628482e-16 -1.117760e-16
## PC17
         1.238976e-15 -1.351509e-16 -3.637049e-16 -4.126695e-16
                                                                 3.166447e-16
## PC18
         2.715106e-16 -1.295783e-16 -6.883829e-16
                                                   9.508136e-17 -1.187367e-15
## PC19 -7.403869e-16
                      3.199250e-16
                                    7.523124e-17 -6.180309e-16 -7.294901e-17
## PC20
       8.646833e-16 -1.630519e-16 -3.045536e-16 -2.538614e-16 2.561349e-17
## PC21 -4.573592e-16 -2.340338e-16
                                    5.050587e-16
                                                   2.425847e-16 -3.697230e-16
## PC22 7.259129e-16
                      5.880067e-16
                                    6.747881e-16
                                                   9.039142e-16 -1.760284e-16
## PC23 -6.088846e-17
                       5.866880e-16
                                     6.462580e-16
                                                   1.469814e-16 4.391360e-16
## PC24 -4.349920e-17 -4.452363e-16 -1.002660e-16
                                                   2.408670e-16
                                                                 1.647694e-15
## PC25 -1.168050e-16 -4.440995e-16 -1.650603e-17
                                                   3.625894e-16 -6.168158e-16
## PC26 -2.980545e-16
                      2.937669e-16
                                     1.274057e-16
                                                   6.488032e-17 -8.076244e-16
## PC27 -2.221175e-16 -7.293349e-16
                                     9.964544e-16
                                                   6.082558e-17
                                                                 5.087621e-16
## PC28 -9.869036e-17 -4.268335e-16
                                     1.413923e-17
                                                   1.922361e-16
                                                                 2.595359e-16
## PC29
         2.198614e-16
                       8.666109e-16
                                     3.055279e-16 -2.618853e-16
                                                                 8.096646e-16
## PC30
         9.325376e-16
                       1.432419e-16
                                     7.986349e-16
                                                   1.590692e-16
                                                                 4.041056e-16
## PC31 -8.449072e-16
                       8.880429e-17
                                     2.531049e-16
                                                   7.100230e-17
                                                                 2.888201e-16
## PC32
         2.110732e-16
                       2.552403e-16
                                     3.853288e-16
                                                   4.434314e-16 -7.551425e-16
        3.719279e-17 2.994994e-17 4.985313e-16 2.387130e-17 -5.391274e-16
```

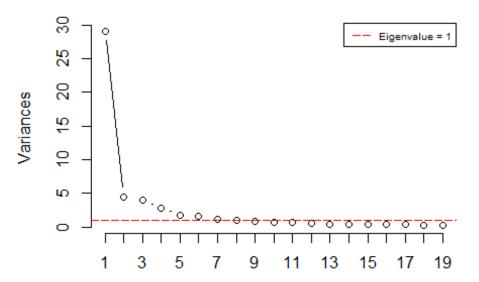
```
## PC34 -3.126879e-16 -6.432229e-16 -1.599198e-16 4.974699e-16 -2.241385e-16
## PC35
         5.814507e-16 -1.058066e-16 -1.655383e-16 -4.397998e-16 -5.449489e-16
## PC36
         1.000000e+00
                      8.808063e-16 6.407866e-16 -5.822037e-16 4.705975e-17
## PC37
        8.808063e-16
                       1.000000e+00
                                    6.177383e-16
                                                  3.152092e-16 -3.718119e-16
## PC38
        6.407866e-16
                      6.177383e-16
                                    1.000000e+00 -2.844881e-16 -1.242974e-15
## PC39 -5.822037e-16
                       3.152092e-16 -2.844881e-16
                                                  1.000000e+00
                                                                 3.360751e-16
## PC40
        4.705975e-17 -3.718119e-16 -1.242974e-15
                                                   3.360751e-16
                                                                 1.000000e+00
## PC41 -2.129735e-16 -1.376795e-15
                                    4.046030e-17
                                                   1.373358e-16
                                                                 7.256926e-17
        7.451724e-16
                      1.331255e-15 -3.169386e-16
                                                   1.548160e-16 -8.175973e-16
## PC43
         2.021785e-16 -1.664270e-17
                                    2.569307e-16
                                                   8.546017e-16 7.130285e-16
## PC44
        1.268730e-17 -6.470323e-16 -2.996047e-16
                                                   6.021840e-16 -7.262089e-16
## PC45 -7.358896e-16 2.752621e-17 -5.403918e-16 -1.621670e-16 -2.697848e-16
        7.234163e-16 -1.194701e-15 2.705668e-17
                                                   2.647576e-17 -1.816649e-16
## PC46
## PC47 -4.207460e-16
                      3.945803e-16 -3.052814e-16
                                                   1.103421e-15 -6.062723e-16
## PC48 -4.454592e-16 -9.196411e-16 -3.112450e-16
                                                   2.180149e-16 4.468174e-16
## PC49 -1.354915e-16 9.315573e-16 -4.165871e-16 -2.785893e-16 -3.601979e-16
## PC50 -4.722534e-16 -2.493228e-16 -5.266429e-16 -1.487038e-17 -4.620097e-16
## PC51 -2.123678e-15 -1.305588e-15
                                    1.130606e-15
                                                  7.476097e-17 -3.156203e-17
## PC52 -2.783227e-16 6.425458e-16
                                    1.857934e-15
                                                  1.564424e-15
                                                                1.751897e-15
## PC53 -1.714716e-16 -4.804819e-16 -1.665464e-15 -1.564432e-15
                                                                 1.188270e-16
## PC54 -3.451661e-15 -1.388356e-15 -3.160089e-15 -3.205366e-15
                                                                 2.467197e-15
##
                 PC41
                               PC42
                                             PC43
                                                           PC44
                                                                         PC45
## PC1
        -2.008741e-15
                      4.589955e-15
                                    1.032674e-14
                                                   1.741612e-16 -3.196953e-15
## PC2
         8.937684e-16 -1.489897e-16 -6.518663e-16
                                                   2.119164e-15
                                                                 1.469111e-15
## PC3
        -1.096736e-15 -2.469240e-16 -4.665142e-16
                                                   3.126149e-16 -8.140933e-16
## PC4
         1.777538e-16
                      1.436391e-15
                                    4.698862e-19 -1.634674e-15 -4.514577e-16
## PC5
                                    3.694317e-16
                                                  1.217966e-15 -2.723826e-17
        -2.154393e-16 -1.990360e-16
## PC6
         6.759947e-16
                      1.282472e-15 -2.962904e-16 -2.137477e-16 -1.992477e-16
## PC7
         1.220395e-16
                      1.449709e-15 -1.929744e-16
                                                  2.552666e-16
                                                                 9.468981e-17
## PC8
         1.072385e-15 -1.105054e-16
                                    1.596568e-16
                                                  4.166522e-16
                                                                 1.112178e-16
## PC9
        -7.098112e-16 -1.959209e-15 9.885919e-17
                                                  8.214928e-16 -7.384909e-16
## PC10 -6.570273e-16 -1.135296e-15 -2.187183e-16 -2.130978e-16 -1.054244e-16
## PC11
        7.653457e-16 -1.014142e-15 -4.471126e-16 -1.030759e-16 -1.106814e-15
## PC12 -2.738959e-16 -1.355900e-15 -6.471907e-16 2.180975e-16 -1.677471e-16
                       1.839691e-17 -3.820958e-16 -3.521385e-16 -5.942605e-16
## PC13
         8.067283e-16
## PC14
                       6.030467e-17 1.001862e-15 -2.064989e-16 9.604160e-16
        7.691240e-17
## PC15
         7.962203e-16
                       1.785575e-16 3.262412e-16 -5.191069e-16 -1.005448e-15
                       3.267219e-16 -1.004384e-16 -2.918449e-16
## PC16 -8.473388e-16
                                                                2.064584e-16
## PC17
        2.923074e-16 -4.567887e-16 -4.454406e-16 3.114973e-16 -1.891637e-16
## PC18 -3.555179e-16
                      2.274444e-16 -5.355739e-16 -1.237697e-15
                                                                 1.305911e-16
       8.621749e-17 -1.710286e-15 -1.072965e-16 -3.222329e-16 -5.420260e-16
## PC20 -1.143850e-16
                       1.817502e-16 -1.231776e-16
                                                  2.127922e-16
                                                                 8.084053e-16
## PC21 -6.493451e-17
                       3.708618e-16 -1.172176e-16 -5.473717e-16 -1.040598e-16
                      1.021352e-16 5.823872e-16 1.200936e-16
## PC22 -3.390257e-16
                                                                 2.178554e-16
## PC23 -1.058046e-15 -5.064490e-16 -9.461822e-16 -1.352264e-16 -4.522907e-16
## PC24 -1.691452e-16 -4.040710e-16 -2.773436e-16 4.420489e-16
                                                                6.057840e-16
## PC25 -8.520200e-17
                       5.543269e-16 -9.710104e-16 2.615476e-16
                                                                 2.012775e-16
## PC26 2.334016e-16
                      3.912716e-16 -6.387898e-17 -6.451040e-16 8.370583e-16
## PC27 -2.121327e-16 -3.598952e-16 3.508160e-16 4.665846e-16 -5.305293e-16
## PC28 1.500402e-16 -4.388648e-17 -3.893239e-16 -3.277021e-16 -1.427875e-16
```

```
## PC29
         5.390151e-16 -8.211921e-16 1.457338e-15 3.584606e-16 -9.067582e-16
## PC30
         7.663259e-16
                       4.815785e-16
                                    3.642031e-16
                                                   1.074275e-16 -1.893156e-15
## PC31
         1.533847e-16
                       3.446436e-16 -6.496418e-17
                                                   1.179889e-15
                                                                 3.763869e-16
## PC32 -2.062719e-16
                       1.112521e-16 -7.155726e-16 -1.016783e-15
                                                                 2.734856e-17
## PC33 -4.923912e-17
                       2.028288e-16 8.264898e-16 -9.283544e-16 -1.050942e-17
## PC34
         2.654904e-16 -5.898712e-16
                                     7.521814e-16 -5.059872e-16 -1.304384e-15
## PC35
         4.456680e-16 -8.924899e-16 -7.590868e-16 -1.121396e-15 1.132307e-15
## PC36 -2.129735e-16
                      7.451724e-16
                                     2.021785e-16
                                                   1.268730e-17 -7.358896e-16
## PC37 -1.376795e-15
                      1.331255e-15 -1.664270e-17 -6.470323e-16 2.752621e-17
## PC38
        4.046030e-17 -3.169386e-16
                                     2.569307e-16 -2.996047e-16 -5.403918e-16
## PC39
         1.373358e-16
                       1.548160e-16
                                     8.546017e-16
                                                  6.021840e-16 -1.621670e-16
## PC40
         7.256926e-17 -8.175973e-16
                                     7.130285e-16 -7.262089e-16 -2.697848e-16
## PC41
         1.000000e+00 -3.696939e-16 -9.133005e-17
                                                  4.378071e-16 -2.033743e-15
## PC42 -3.696939e-16
                       1.000000e+00
                                     6.452050e-16
                                                   2.959994e-16 4.407183e-16
## PC43 -9.133005e-17
                       6.452050e-16
                                     1.000000e+00
                                                   1.468217e-16
                                                                 1.483123e-15
                                     1.468217e-16
## PC44 4.378071e-16
                       2.959994e-16
                                                   1.000000e+00
                                                                 1.437040e-15
## PC45 -2.033743e-15
                       4.407183e-16
                                     1.483123e-15
                                                   1.437040e-15
                                                                 1.000000e+00
## PC46 -5.452410e-16 -3.097983e-16
                                     9.735665e-16 -5.944879e-16
                                                                 3.089046e-16
## PC47 -4.840475e-16 -1.262069e-15
                                    7.199259e-16 -2.069320e-16 -5.784528e-16
## PC48
                      4.648220e-16 -9.588765e-16 -6.190860e-16 -9.256331e-16
         8.172805e-16
         5.844783e-16 -6.242168e-16 -6.188944e-16 -1.010880e-15 -7.010568e-16
## PC49
## PC50 -5.056692e-16
                      3.269396e-16 -9.274414e-16 -6.937782e-16 -1.057224e-15
## PC51
        6.203761e-16
                      1.821181e-16 9.957144e-16 1.012977e-15 1.347340e-15
## PC52 -5.703370e-16 -1.775994e-15 -1.265209e-15
                                                   1.695290e-15 -5.560413e-16
         9.149870e-16 -3.749989e-16 -8.784876e-16 -1.540838e-15 -7.927421e-16
## PC54 -1.482356e-15
                       5.468640e-16
                                     2.942949e-15 -1.910253e-15 -2.307560e-15
##
                 PC46
                               PC47
                                             PC48
                                                           PC49
## PC1
        -5.931774e-15 -2.213842e-15 -2.885707e-15 -1.090175e-15 -1.085299e-14
## PC2
        -3.618915e-15
                       1.044760e-15 -1.108834e-15 -3.734902e-16 -3.105598e-15
## PC3
                       5.076239e-15 -1.240739e-15
                                                   1.297233e-15 -2.793472e-15
        -7.085198e-16
## PC4
        -1.992713e-15
                       1.588380e-15 -2.296829e-17
                                                   6.330508e-16 1.427591e-15
## PC5
        -1.048438e-16 -8.894109e-16 -2.324959e-15 -3.646366e-15 -2.901522e-15
## PC6
         3.036041e-16 -9.267837e-16
                                    7.838965e-16
                                                   1.594357e-15 -3.083829e-15
## PC7
         1.107838e-16 -1.059120e-15
                                    1.126691e-15
                                                   4.467436e-16
                                                                 3.657712e-16
## PC8
        -7.500215e-16 -5.713611e-16 -1.215339e-15
                                                   1.093566e-15 -1.425415e-15
        -7.716128e-16 -9.503313e-16 -1.102115e-16 -1.468961e-15
## PC9
                                                                 6.928758e-16
## PC10 -1.267356e-16
                      1.817920e-15 -3.603879e-16 -1.646864e-16
                                                                 1.842490e-15
         4.122429e-16 -9.204675e-16 -4.341432e-16 -6.250681e-16
## PC11
                                                                 1.768489e-15
## PC12
        8.854368e-16 -6.739227e-16 -6.848356e-16 -1.467558e-15 -1.368166e-15
## PC13
         3.874791e-16
                      4.670321e-16 1.149226e-15
                                                  4.208661e-16 -4.429650e-16
## PC14
         5.956798e-17 -3.983414e-16 -6.463740e-16 -9.257280e-17
                                                                 6.932432e-16
## PC15 -1.088020e-16
                      4.922746e-16 -1.270110e-15
                                                   1.145147e-16
                                                                 8.517087e-16
## PC16
         4.594167e-16 -9.979405e-16 -1.311204e-15
                                                  4.192908e-16
                                                                 3.205167e-17
## PC17 -1.635312e-16
                      7.250476e-16 -4.156936e-16 -5.429973e-16 -5.180771e-17
## PC18 -9.970177e-16
                       2.508653e-17 -1.020571e-15 -2.544524e-16
                                                                 2.970991e-16
## PC19
        3.591923e-16
                       6.087997e-16 2.640294e-16 -2.690889e-16
                                                                 6.087083e-16
## PC20 -2.437023e-16
                       1.969475e-16 4.025027e-17
                                                  1.269315e-15
                                                                 3.609723e-18
                                                                 4.999508e-16
## PC21 -7.120226e-17 -1.682566e-15 -3.014174e-16 -1.710611e-15
## PC22 -8.766105e-16
                       5.601245e-16
                                    2.757408e-17
                                                  2.835024e-15 -9.918918e-16
## PC23 8.241293e-16 8.241872e-16 6.481592e-16 -3.520886e-17 4.171823e-19
```

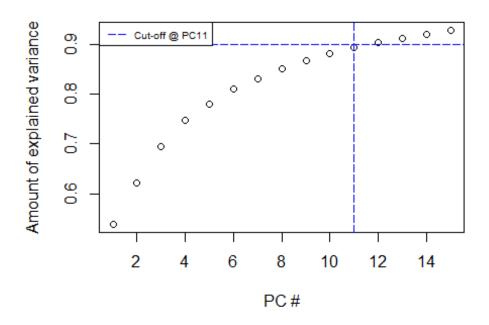
```
## PC24 -9.632417e-16 -1.859112e-16 3.904550e-16 1.250139e-15 5.367373e-16
## PC25
         5.897586e-16 -1.796516e-15
                                    4.306521e-16 -3.918283e-16
                                                                 9.222670e-16
## PC26
         2.899280e-16
                      1.438885e-16
                                    1.306591e-15
                                                  2.180920e-16
                                                                 2.544707e-16
## PC27
         6.872461e-16
                      3.498239e-16
                                    9.379877e-16 -5.928267e-17
                                                                 3.447442e-16
## PC28
         1.231838e-15 -9.194330e-18
                                    4.932172e-16 -1.138725e-16 -7.618808e-16
## PC29
         2.828862e-16 -6.607552e-17
                                     5.605006e-16 -6.087424e-16
                                                                 1.878429e-16
## PC30 -2.558993e-17 -1.174270e-15 -5.827599e-16 -8.615460e-17 -9.620639e-16
## PC31 -1.263179e-15
                      4.180779e-16
                                     1.118195e-15 -4.469183e-16 -8.621746e-16
## PC32 -3.554421e-16 -6.816243e-16
                                    4.882756e-16 4.993996e-16
                                                                 7.386231e-16
## PC33
         2.659597e-16
                       1.218886e-15 -6.849415e-16 1.457884e-16
                                                                 3.925396e-16
## PC34
         3.657319e-16
                      8.519426e-16
                                    1.368228e-15 -1.468721e-15
                                                                 1.251339e-15
## PC35
         1.030907e-16
                      1.412481e-15 4.182023e-16 1.353830e-16
                                                                 2.238343e-16
## PC36
         7.234163e-16 -4.207460e-16 -4.454592e-16 -1.354915e-16 -4.722534e-16
## PC37 -1.194701e-15
                      3.945803e-16 -9.196411e-16 9.315573e-16 -2.493228e-16
         2.705668e-17 -3.052814e-16 -3.112450e-16 -4.165871e-16 -5.266429e-16
## PC38
## PC39 2.647576e-17
                      1.103421e-15 2.180149e-16 -2.785893e-16 -1.487038e-17
## PC40 -1.816649e-16 -6.062723e-16 4.468174e-16 -3.601979e-16 -4.620097e-16
## PC41 -5.452410e-16 -4.840475e-16 8.172805e-16 5.844783e-16 -5.056692e-16
## PC42 -3.097983e-16 -1.262069e-15 4.648220e-16 -6.242168e-16 3.269396e-16
## PC43
         9.735665e-16
                      7.199259e-16 -9.588765e-16 -6.188944e-16 -9.274414e-16
## PC44 -5.944879e-16 -2.069320e-16 -6.190860e-16 -1.010880e-15 -6.937782e-16
## PC45
        3.089046e-16 -5.784528e-16 -9.256331e-16 -7.010568e-16 -1.057224e-15
## PC46
         1.000000e+00
                      4.442256e-16 -4.139869e-16 2.357053e-16 -2.578542e-17
## PC47
                       1.000000e+00 -3.976032e-16 -1.126204e-15
                                                                3.112592e-15
         4.442256e-16
## PC48 -4.139869e-16 -3.976032e-16
                                    1.000000e+00 5.583789e-16 -9.331399e-16
## PC49
         2.357053e-16 -1.126204e-15
                                    5.583789e-16
                                                  1.000000e+00 -3.140436e-16
## PC50 -2.578542e-17
                      3.112592e-15 -9.331399e-16 -3.140436e-16 1.000000e+00
## PC51 -4.675703e-16 -3.451715e-15
                                    4.381116e-16 -6.434410e-16 -3.935128e-16
## PC52
         2.577348e-15
                       1.253819e-15
                                    1.657396e-15 -1.998347e-15 2.456176e-15
## PC53
         1.850213e-16
                      4.767442e-16 -1.187114e-16
                                                  2.615703e-15 -1.248074e-15
## PC54
        4.762425e-15
                       4.104918e-15 -5.212001e-15
                                                   3.672734e-16 -1.246608e-15
                               PC52
##
                 PC51
                                             PC53
                                                           PC54
## PC1
        -4.277645e-15 -1.106550e-14
                                    1.182701e-14
                                                   3.752027e-15
## PC2
         9.069281e-16
                      5.520437e-17 -4.470542e-15
                                                   1.119677e-15
## PC3
        -6.792805e-16
                      6.858737e-16
                                    2.766986e-15 -1.081259e-16
## PC4
         3.666771e-16 -3.255756e-17 -4.749521e-15 -3.682398e-16
## PC5
        -2.781161e-15 -2.937246e-15
                                    3.777338e-15
                                                   3.611327e-15
                      1.897820e-15
                                     7.076433e-16 -3.436094e-15
## PC6
         2.025886e-15
## PC7
        -2.127660e-16 -1.552744e-15 -1.594417e-15
                                                   4.974963e-16
## PC8
        -3.421823e-15
                      1.460050e-15
                                    5.579465e-15 -6.944760e-15
## PC9
        -2.021353e-15 -1.468410e-15 -3.004247e-16
                                                   2.867047e-16
## PC10 -1.835860e-16
                      3.281656e-15
                                    2.567748e-15
                                                   5.320617e-15
## PC11 -4.032251e-16 -5.313427e-16 -1.657473e-15 -4.145559e-15
## PC12 1.247552e-15 -3.017558e-15
                                    3.311296e-15 -5.822745e-15
## PC13 -1.647988e-16 -9.894621e-17 -8.531662e-16
                                                  1.204401e-16
## PC14 1.165759e-15 -2.443149e-15
                                    1.144921e-15
                                                   3.942666e-15
## PC15 -1.067912e-15
                      2.168672e-15 -7.977412e-16 -6.294080e-15
## PC16 -1.199537e-15 -2.959468e-16
                                    1.516552e-15
                                                   4.302859e-15
## PC17 -1.796229e-15
                      3.393597e-17
                                     2.178308e-15
                                                   6.298601e-15
## PC18 -6.908279e-16 2.073048e-15 -1.161311e-15 9.671620e-16
```

```
## PC19 -2.286192e-15 -1.348470e-15 3.343703e-15 -3.734364e-15
## PC20 1.680352e-15
                     1.898225e-15 1.092237e-15 1.426010e-15
## PC21 1.452539e-15 -2.600317e-16 -2.271826e-15
                                                  2.086086e-15
## PC22
        1.737924e-15
                      2.319329e-15 -2.395680e-15 -2.186907e-15
## PC23 -2.147507e-15 4.576027e-16 8.069232e-17 -3.849053e-15
## PC24
        5.729243e-16
                     3.058556e-16 -1.829256e-15 -1.021630e-15
## PC25
        5.145923e-17 4.067921e-15 -1.659596e-15 -7.424496e-17
## PC26 -1.551765e-15
                      6.962311e-16 -7.097315e-16
                                                 5.143136e-15
## PC27 2.473667e-16 -5.155597e-16 -1.061289e-16
                                                 6.938201e-15
                     1.020107e-15 4.457204e-16 -5.974576e-15
## PC28 -1.648349e-17
## PC29 -4.702651e-16 -1.824643e-16 -7.152995e-16 2.494087e-17
                     1.815349e-15 -1.682030e-16 -1.074394e-15
## PC30 -1.114008e-16
## PC31 -6.482901e-16 -9.616746e-17 2.177625e-15 -3.167474e-15
## PC32 -1.443760e-15
                     2.567465e-15 9.569618e-16 -2.196190e-15
## PC33 -1.945586e-16
                     2.275808e-15 -1.415512e-15 -4.692200e-15
## PC34 4.450717e-16
                     1.366859e-15 -1.765261e-15 -6.219265e-15
## PC35
        1.263267e-15
                      1.634383e-15 -3.987856e-17 5.232600e-15
## PC36 -2.123678e-15 -2.783227e-16 -1.714716e-16 -3.451661e-15
## PC37 -1.305588e-15
                     6.425458e-16 -4.804819e-16 -1.388356e-15
## PC38 1.130606e-15
                      1.857934e-15 -1.665464e-15 -3.160089e-15
## PC39 7.476097e-17
                      1.564424e-15 -1.564432e-15 -3.205366e-15
## PC40 -3.156203e-17
                      1.751897e-15
                                   1.188270e-16
                                                 2.467197e-15
## PC41 6.203761e-16 -5.703370e-16 9.149870e-16 -1.482356e-15
## PC42 1.821181e-16 -1.775994e-15 -3.749989e-16
                                                  5.468640e-16
## PC43 9.957144e-16 -1.265209e-15 -8.784876e-16
                                                 2.942949e-15
## PC44 1.012977e-15
                      1.695290e-15 -1.540838e-15 -1.910253e-15
## PC45 1.347340e-15 -5.560413e-16 -7.927421e-16 -2.307560e-15
## PC46 -4.675703e-16
                     2.577348e-15
                                   1.850213e-16 4.762425e-15
## PC47 -3.451715e-15
                      1.253819e-15
                                    4.767442e-16 4.104918e-15
## PC48 4.381116e-16
                      1.657396e-15 -1.187114e-16 -5.212001e-15
## PC49 -6.434410e-16 -1.998347e-15
                                    2.615703e-15
                                                 3.672734e-16
## PC50 -3.935128e-16
                      2.456176e-15 -1.248074e-15 -1.246608e-15
## PC51 1.000000e+00 -9.516795e-17
                                   1.127204e-15 -3.562616e-16
## PC52 -9.516795e-17
                      1.000000e+00
                                   1.691972e-16 -3.864593e-15
                      1.691972e-16 1.000000e+00 1.753105e-15
## PC53 1.127204e-15
## PC54 -3.562616e-16 -3.864593e-15
                                   1.753105e-15 1.000000e+00
screeplot(GDPdataTrainSet.pca.normdata, type = "1", npcs = 19, main = "Screep
lot of the first 19 PCs")
abline(h = 1, col="red", lty=5)
legend("topright", legend=c("Eigenvalue = 1"),
       col=c("red"), lty=5, cex=0.6)
```

Screeplot of the first 19 PCs



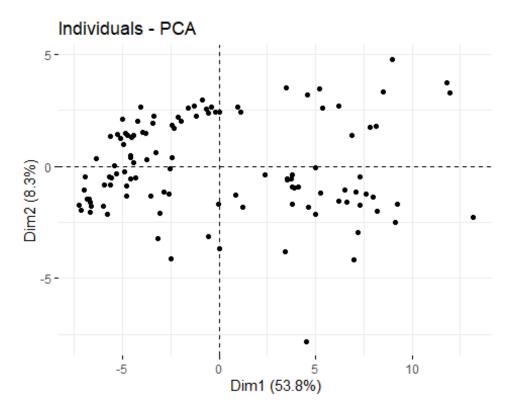
Cumulative variance plot



```
#Note: The first 11 components has an Eigenvalue >1 and explains almost 90% o
f variance
#We can effectively reduce dimensionality from 160 to 11 if we consider 90 %
variance
#----
#-----
#Predict using PCA
PredictingData<- predict(GDPdataTrainSet.pca.normdata, newdata = GDPdata.test</pre>
.set )
#select the first 19 pca components i.e., 95 % variance
# we tend to look at the first few principal components in order to find inte
resting patterns in the data.
#PredictingData<-PredictingData[,1:19]</pre>
#-----
fviz pca ind(GDPdataTrainSet.pca.normdata,
             col.ind = "cos2", # Color by the quality of representation
             gradient.cols = c("#00AFBB", "#E7B800", "#FC4E07"),
             repel = TRUE
                             # Avoid text overlapping
```

Individuals - PCA 5 - 125 35 112 93 55 117 30 118 80 129 146 122 25 67 53 86 109 6 27 51 9 34 137 57 18 99 154 140 4 121 64 9 100 94 90 81 23 144 71 22 13 17 105 97 85 58 31 157 158 cos2 80 -106 0 6 36 50 108 47 144 21 41 71 22 160 73 138 144 1 21 41 72 119 16 147 127 63 89 74 49 48 101 -5 0 5 10 0.25 Dim1 (53.8%)

Color individuals by groups
#Plots: quality and countries
fviz_pca_ind(GDPdataTrainSet.pca.normdata, label="none")



```
fviz pca ind(GDPdataTrainSet.pca.normdata, label="none", habillage=GDPdataCou
ntrytrainset$Country)
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '28'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '27'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
## pch value '26'
## Warning in grid.Call.graphics(C points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '28'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '28'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '28'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '30'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '28'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '28'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '28'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '28'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '31'
```

```
## Warning in grid.Call.graphics(C points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '29'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
## pch value '26'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '27'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '28'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '29'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '30'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '31'
## Warning in grid.Call.graphics(C points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '26'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '26'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '27'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '27'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '28'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '28'
```

```
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '29'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '29'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '30'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
## pch value '30'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '31'
## Warning in grid.Call.graphics(C_points, x$x, x$y, x$pch, x$size): unimplem
ented
## pch value '31'
ľ
```

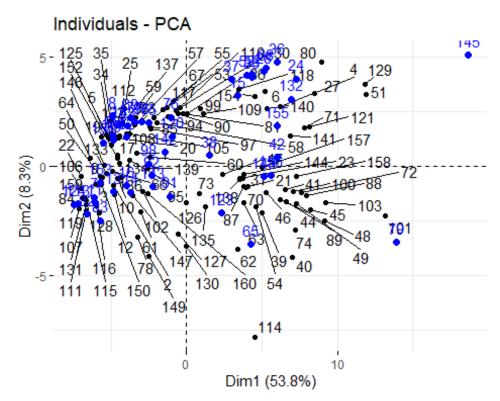
▼ Callaua	•	IIIuviiesia	•	ı illilibbili <u>c</u> ə	•	Officer Vian Pilliages
lividuals - PCA		Ireland	•	Poland	•	United Kingdom
China	•	Israel	•	Portugal	•	United States
 Colombia 	•	Italy	٠	Qatar	•	Uzbekistan
 Costa Rica 	٠	Japan	٠	Romania	•	Vietnam
Croatia	•	Jordan	٠	Russia		
 Czech Republic 	٠	Kazakhstan	•	Serbia		
 Denmark 	•	Kenya	•	Singapore		

Groups

٥	Albania	٠	Denmark	%	Japan	7	Per
Δ	Argentina	٠	Dominican Republic	&	Jordan	8	Phi
+	Armenia	0	Ecuador		Kazakhstan	9	Pol
X	Australia		Egypt	(Kenya	:	Por
♦	Austria	\Diamond	Estonia)	Latvia	į	Qat
∇	Azerbaijan	Δ	Finland	*	Lebanon	<	Roi
8∰)	Belarus	∇	France	+	Lithuania	=	Ru

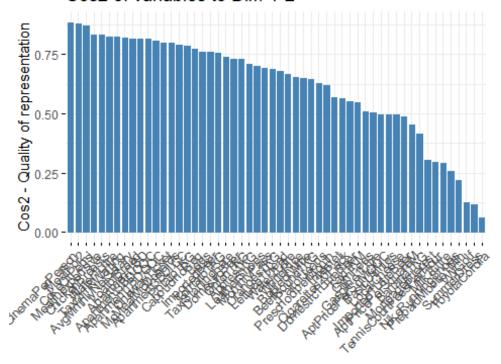
#-----

```
#-----
#Variable correlation plots
# Plot of train data
p <- fviz_pca_ind(GDPdataTrainSet.pca.normdata, repel = TRUE)
# Add predicted data
fviz_add(p, PredictingData, color = "blue")</pre>
```



#Posively and negatively (opposite to positive) correlated variables are grou
ped together
#The distance between variables and the origin measures the quality of the va
riables on the factor map
#Quality of representation
#The quality of representation of the variables on factor map is called cos2
(square cosine, squared coordinates)
Total cos2 of variables on Dim.1 and Dim.2
fviz_cos2(GDPdataTrainSet.pca.normdata, choice = "var", axes = 1:2)

Cos2 of variables to Dim-1-2



#A high cos2 shows a good representation of the variable on the principal com ponent.

#The closer a variable is to the circle of correlations, the better its repre sentation on the factor map

#more important to interpret these components

#A low cos2 indicates that the variable is not perfectly represented by the P Cs.

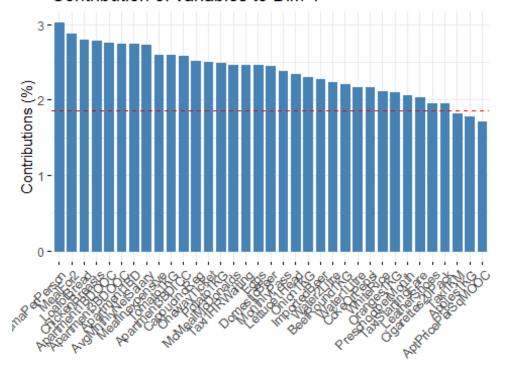
#In this case the variable is close to the center of the circle which are less important for the first components

#------
#The top variables contributing to the principal components:

Contributions of variables to PC1

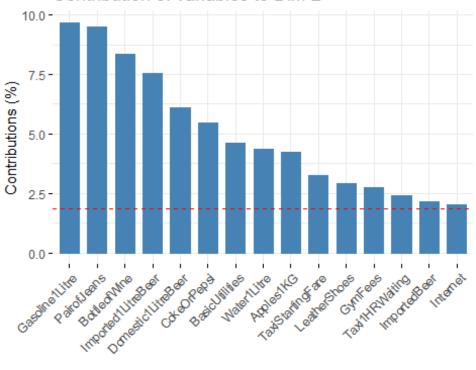
fviz_contrib(GDPdataTrainSet.pca.normdata, choice = "var", axes = 1, top = 35

Contribution of variables to Dim-1



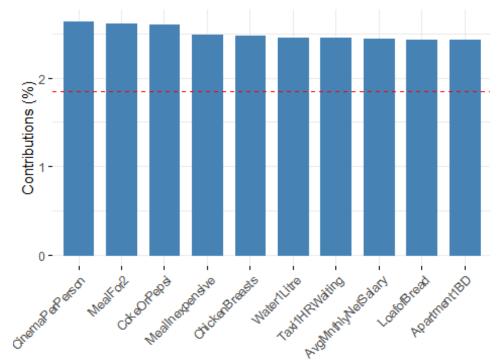
```
#Note:The red dashed line on the graph indicates the expected average contrib
ution.
#For a given component, the variables whose values greater than threshold (re
d line) are important contributers
# Contributions of variables to PC2
fviz_contrib(GDPdataTrainSet.pca.normdata, choice = "var", axes = 2, top = 15
```

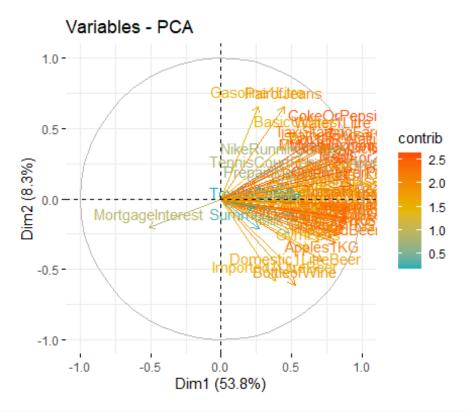
Contribution of variables to Dim-2



```
#By comparing PC1 and PC2
#We can say that CokeorPepsi, ImportedBeer, Water1Litre, LeatherShoes, TaxiSt
artingFare, Taxi1HRWaiting, Oranges1KG and Apple1KG, contribute the most to t
he dimensions 1 and 2.
#The total contribution to PC1 and PC2
fviz_contrib(GDPdataTrainSet.pca.normdata, choice = "var", axes = 1:2, top =
10)
```







```
#Investigated how the variables are related to one another
#plot('GDPdata(,1:5)')
#-----
#Regression analysis
#Regression helps show the relationship between a response variable with res
pect to predictor varaiables
#Building a model for estimating GDP of a country based on the monetary value
s of all the goods available in that country
GDPresults = 1m (GDPUSDInMillions ~ . , data = GDPdata_lm )
summary(GDPresults)
##
## Call:
## lm(formula = GDPUSDInMillions ~ ., data = GDPdata_lm)
##
## Residuals:
                         Median
         Min
                    10
                                       3Q
                                                Max
## -0.212080 -0.045360 -0.006231 0.039523 0.279102
##
## Coefficients:
                            Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                           5.193e-03 9.419e-02
                                                 0.055 0.956136
## MealInexpensive
                           1.479e+05 1.360e+05
                                                 1.087 0.279534
```

```
## MealFor2
                                        4.728e+04
                           -3.416e+04
                                                    -0.723 0.471556
                                                    0.777 0.438763
## McMealMcDonalds
                            2.148e+05
                                        2.764e+05
## DomesticBeer
                           -9.095e+05
                                        4.874e+05
                                                    -1.866 0.064817
## ImportedBeer
                            5.393e+05
                                        4.541e+05
                                                    1.188 0.237673
## CokeOrPepsi
                            1.915e+06
                                        1.275e+06
                                                    1.502 0.136005
## Water1Litre
                           -2.859e+06
                                        1.551e+06
                                                    -1.843 0.068165
                           -2.871e+06
                                        9.902e+05
                                                    -2.900 0.004550 **
## Milk1Litre
## LoafofBread
                            1.064e+06
                                        8.085e+05
                                                    1.316 0.191018
## Eggs
                            4.504e+05
                                        7.320e+05
                                                    0.615 0.539665
## LocalCheese
                            5.062e+05
                                                    4.392 2.69e-05 ***
                                        1.153e+05
## Water2Litre
                            4.541e+05
                                        1.130e+06
                                                    0.402 0.688612
## BottleofWine
                            1.848e+05
                                        8.799e+04
                                                    2.100 0.038117 *
## Domestic1LitreBeer
                           -3.431e+06
                                        8.790e+05
                                                    -3.904 0.000168 ***
## Imported1LitreBeer
                            2.216e+06
                                        5.965e+05
                                                    3.716 0.000327
## Cigarettes20Pack
                            1.245e+05
                                        1.298e+05
                                                    0.960 0.339401
## OnewayTicket
                           -2.434e+06
                                        5.674e+05
                                                    -4.290 3.99e-05
                                                    -5.199 9.96e-07 ***
## ChickenBreasts
                           -1.060e+06
                                        2.039e+05
                                                    4.285 4.06e-05 ***
## MonthlyPass
                            6.696e+04
                                        1.563e+04
## Gasoline1Litre
                            1.293e+06
                                        1.140e+06
                                                    1.134 0.259474
## VWGolf
                           -2.694e+01
                                        6.651e+01
                                                    -0.405 0.686279
                                                    0.929 0.354773
## Apartment1BD
                            5.210e+03
                                        5.606e+03
## Apartment1BD00C
                           -6.396e+03
                                        7.081e+03
                                                    -0.903 0.368468
## Apartment3BDICC
                            3.060e+02
                                        2.413e+03
                                                    0.127 0.899330
## Apartment3BD00C
                           -4.179e+02
                                        3.828e+03
                                                    -0.109 0.913277
## BasicUtilities
                           -3.292e+03
                                        6.945e+03
                                                    -0.474 0.636454
## PrepaidMobile1MIn
                           -1.103e+07
                                        3.246e+06
                                                    -3.398 0.000961
## Internet
                            1.663e+04
                                        2.362e+04
                                                    0.704 0.482807
## GymFees
                           -4.293e+04
                                        2.592e+04
                                                    -1.656 0.100726
## TennisCourtFeesPerHour -4.326e+04
                                        4.841e+04
                                                    -0.894 0.373611
## CinemaPerPerson
                            3.979e+05
                                        1.960e+05
                                                    2.031 0.044824 *
## PairofJeans
                           -4.577e+04
                                        2.945e+04
                                                    -1.554 0.123163
## SummerDress
                           -1.387e+04
                                        4.543e+04
                                                    -0.305 0.760806
## NikeRunningShoes
                            3.965e+03
                                        2.567e+04
                                                    0.154 0.877536
## LeatherShoes
                            3.510e+04
                                        2.435e+04
                                                    1.441 0.152483
## AptPricePerSquareM
                           -2.775e+01
                                        3.068e+02
                                                    -0.090 0.928112
## AptPricePerSqMOOC
                           -5.372e+02
                                        5.184e+02
                                                    -1.036 0.302442
## AvgMnthlyNetSalary
                            4.608e+03
                                        7.571e+02
                                                    6.086 1.91e-08 ***
## MortgageInterest
                            3.174e+04
                                        3.854e+04
                                                     0.824 0.412089
## TaxiStartingFare
                           -4.908e+04
                                        2.570e+05
                                                    -0.191 0.848944
## Taxi1KM
                           -1.135e+06
                                        5.356e+05
                                                    -2.118 0.036505 *
                                        4.793e+04
## Taxi1HRWaiting
                                                    0.576 0.565511
                            2.763e+04
## Apples1KG
                           -7.687e+05
                                        5.613e+05
                                                    -1.370 0.173755
## Oranges1KG
                           -5.166e+05
                                        6.219e+05
                                                    -0.831 0.408034
## Potato1KG
                           -1.988e+06
                                        1.098e+06
                                                    -1.810 0.073229
## Lettuce1Head
                           -3.946e+06
                                        8.893e+05
                                                    -4.437 2.25e-05
                                                    2.479 0.014784 *
## CappucinoReg
                            1.159e+06
                                        4.677e+05
## WhiteRice
                            2.236e+06
                                        5.188e+05
                                                    4.310 3.69e-05 ***
## Tomato1KG
                           -1.526e+05
                                        7.492e+05
                                                    -0.204 0.839013
## Banana1KG
                           -1.326e+06
                                        7.726e+05
                                                    -1.716 0.089093
## Onion1KG
                            2.906e+06
                                        9.945e+05
                                                    2.922 0.004262 **
```

```
## BeefRound1KG
                           1.903e+05 1.224e+05
                                                  1.555 0.122931
## ToyotaCorolla
                          -9.944e+01 6.813e+01
                                                -1.460 0.147408
## PreschoolperMonth
                          -2.350e+03 1.103e+03 -2.132 0.035373 *
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 0.08724 on 105 degrees of freedom
## Multiple R-squared: 0.9342, Adjusted R-squared: 0.9004
## F-statistic: 27.61 on 54 and 105 DF, p-value: < 2.2e-16
#Analysis of F-statistics(p-value: < 2.2e-16) shows that atleast one of the p
redictor variables is significantly related to the outcome variable
#Analysis the coefficients to find the predictor variables is significantly r
elated to the outcome variable.
summary(GDPresults)$coefficient
##
                               Estimate
                                          Std. Error
                                                         t value
                                                                     Pr(>|t|)
## (Intercept)
                           5.192999e-03 9.418798e-02
                                                      0.05513441 9.561362e-01
## MealInexpensive
                           1.478694e+05 1.360368e+05
                                                      1.08698086 2.795342e-01
## MealFor2
                          -3.416086e+04 4.727753e+04 -0.72256016 4.715565e-01
## McMealMcDonalds
                           2.147911e+05 2.763501e+05
                                                      0.77724273 4.387632e-01
## DomesticBeer
                          -9.095062e+05 4.873817e+05 -1.86610673 6.481724e-02
## ImportedBeer
                           5.392532e+05 4.540716e+05
                                                      1.18759504 2.376726e-01
                           1.915237e+06 1.274816e+06
## CokeOrPepsi
                                                      1.50236277 1.360050e-01
## Water1Litre
                          -2.858615e+06 1.551153e+06 -1.84289683 6.816509e-02
## Milk1Litre
                          -2.871150e+06 9.901803e+05 -2.89962353 4.550438e-03
## LoafofBread
                           1.064054e+06 8.085119e+05
                                                      1.31606433 1.910184e-01
                           4.504398e+05 7.320247e+05 0.61533419 5.396654e-01
## Eggs
## LocalCheese
                           5.061852e+05 1.152614e+05 4.39162657 2.693083e-05
## Water2Litre
                           4.540588e+05 1.129925e+06 0.40184871 6.886122e-01
## BottleofWine
                           1.847941e+05 8.799370e+04
                                                      2.10008370 3.811711e-02
## Domestic1LitreBeer
                          -3.431489e+06 8.790063e+05 -3.90382686 1.675786e-04
                                                      3.71553630 3.269821e-04
                           2.216299e+06 5.964950e+05
## Imported1LitreBeer
## Cigarettes20Pack
                           1.245246e+05 1.297509e+05 0.95972038 3.394007e-01
## OnewayTicket
                          -2.434010e+06 5.674122e+05 -4.28966818 3.990221e-05
## ChickenBreasts
                          -1.060027e+06 2.039079e+05 -5.19855582 9.958265e-07
## MonthlyPass
                           6.696182e+04 1.562712e+04 4.28497516 4.062534e-05
## Gasoline1Litre
                           1.293007e+06 1.140452e+06
                                                     1.13376710 2.594742e-01
## VWGolf
                          -2.693984e+01 6.651301e+01 -0.40503116 6.862786e-01
## Apartment1BD
                           5.210325e+03 5.605641e+03
                                                      0.92947876 3.547730e-01
## Apartment1BD00C
                          -6.396071e+03 7.081276e+03 -0.90323712 3.684676e-01
                           3.059728e+02 2.412776e+03 0.12681358 8.993305e-01
## Apartment3BDICC
## Apartment3BD00C
                          -4.179464e+02 3.828429e+03 -0.10916916 9.132767e-01
                          -3.292143e+03 6.944827e+03 -0.47404249 6.364539e-01
## BasicUtilities
## PrepaidMobile1MIn
                          -1.102839e+07 3.245850e+06 -3.39769011 9.610784e-04
                           1.663381e+04 2.361759e+04 0.70429723 4.828068e-01
## Internet
                          -4.292714e+04 2.592364e+04 -1.65590703 1.007264e-01
## GymFees
## TennisCourtFeesPerHour -4.325765e+04 4.841145e+04 -0.89354178 3.736106e-01
## CinemaPerPerson
                           3.978978e+05 1.959521e+05 2.03058680 4.482447e-02
## PairofJeans
                          -4.576977e+04 2.945045e+04 -1.55412809 1.231629e-01
```

```
## SummerDress
                          -1.386621e+04 4.543092e+04 -0.30521527 7.608064e-01
## NikeRunningShoes
                           3.964938e+03 2.566798e+04 0.15447020 8.775355e-01
## LeatherShoes
                           3.510103e+04 2.435419e+04 1.44127292 1.524833e-01
## AptPricePerSquareM
                          -2.774991e+01 3.068394e+02 -0.09043788 9.281116e-01
## AptPricePerSqMOOC
                          -5.371880e+02 5.183705e+02 -1.03630120 3.024424e-01
## AvgMnthlyNetSalary
                           4.608062e+03 7.571336e+02 6.08619420 1.913946e-08
## MortgageInterest
                           3.173890e+04 3.854138e+04 0.82350180 4.120892e-01
## TaxiStartingFare
                          -4.907808e+04 2.570381e+05 -0.19093695 8.489437e-01
## Taxi1KM
                          -1.134646e+06 5.356281e+05 -2.11834730 3.650511e-02
## Taxi1HRWaiting
                           2.763393e+04 4.793397e+04 0.57649993 5.655111e-01
## Apples1KG
                          -7.687057e+05 5.612909e+05 -1.36953156 1.737551e-01
## Oranges1KG
                          -5.165693e+05 6.218556e+05 -0.83069011 4.080336e-01
## Potato1KG
                          -1.987602e+06 1.098405e+06 -1.80953496 7.322888e-02
## Lettuce1Head
                          -3.946206e+06 8.893453e+05 -4.43720366 2.254945e-05
                          1.159173e+06 4.676810e+05 2.47855511 1.478412e-02
## CappucinoReg
## WhiteRice
                          2.235853e+06 5.187776e+05 4.30984817 3.693151e-05
## Tomato1KG
                          -1.525749e+05 7.491625e+05 -0.20366062 8.390129e-01
                          -1.325928e+06 7.726406e+05 -1.71609931 8.909290e-02
## Banana1KG
                          2.905669e+06 9.944923e+05 2.92176105 4.262036e-03
## Onion1KG
## BeefRound1KG
                          1.903040e+05 1.223740e+05 1.55510252 1.229307e-01
## ToyotaCorolla
                          -9.944125e+01 6.813297e+01 -1.45951728 1.474081e-01
## PreschoolperMonth
                          -2.350296e+03 1.102602e+03 -2.13159093 3.537336e-02
#Analysis of t-values show that local cheese, domestic1litrebeer imported1lit
erbeer, onewayticket, chickenbreasts, monthlypass, prepaidmobilephone,
#avgmonthlynetsalary, lettuce1head, and whiterice are significantly associate
d to changes in GDP
#-----
#Regression analysis using PCA
#PCA is due to various explanatory variables
#Standard linear models potentially more powerful when using PCA
#combining both the explanatory variables - PCs, and explained variable - y
pcs <- as.data.frame(GDPdataTrainSet.pca.normdata$x)</pre>
pcs.data <- cbind(GDPdata_y_train.set, pcs)</pre>
pcsmodel <- lm(GDPdata_y_train.set ~ ., data = pcs.data)</pre>
summary(pcsmodel)
##
## Call:
## lm(formula = GDPdata y train.set ~ ., data = pcs.data)
##
## Residuals:
                          Median
##
         Min
                    10
                                        3Q
                                                 Max
## -0.155582 -0.039609 -0.000687 0.037971 0.232669
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
```

```
## (Intercept)
                                        19.409
                                                 < 2e-16 ***
                 0.1550573
                            0.0079888
                                                 < 2e-16 ***
## PC1
                 0.0251157
                            0.0014885
                                        16.873
                                                 < 2e-16 ***
## PC2
                -0.0487008
                            0.0037873 -12.859
                                                 < 2e-16 ***
## PC3
                -0.0706349
                            0.0040077 -17.625
## PC4
                -0.0283475
                            0.0048166
                                        -5.885 2.21e-07 ***
## PC5
                -0.0090974
                            0.0059357
                                        -1.533 0.130890
## PC6
                 0.0834193
                            0.0064282
                                        12.977
                                                < 2e-16 ***
                                         5.933 1.85e-07 ***
## PC7
                 0.0443762
                            0.0074799
                                         5.742 3.79e-07 ***
## PC8
                 0.0451266
                            0.0078587
## PC9
                -0.0613281
                            0.0085385
                                        -7.183 1.58e-09 ***
## PC10
                 0.0063901
                            0.0091762
                                         0.696 0.489024
## PC11
                -0.0198361
                            0.0096965
                                        -2.046 0.045410 *
## PC12
                -0.0354073
                            0.0105677
                                        -3.351 0.001436 **
                                         4.037 0.000163 ***
## PC13
                 0.0473455
                            0.0117272
## PC14
                 0.0535734
                            0.0120452
                                         4.448 4.07e-05 ***
## PC15
                -0.0235756
                            0.0124467
                                        -1.894 0.063287 .
## PC16
                -0.1133667
                            0.0135179
                                        -8.386 1.57e-11 ***
## PC17
                                        -0.934 0.354015
                -0.0128240
                            0.0137236
## PC18
                -0.0418079
                            0.0143099
                                        -2.922 0.004983 **
                                         3.270 0.001825 **
## PC19
                 0.0496518
                            0.0151822
## PC20
                -0.0438881
                                        -2.821 0.006573 **
                            0.0155564
## PC21
                -0.0040672
                            0.0167002
                                        -0.244 0.808460
## PC22
                -0.0834910
                            0.0180382
                                        -4.629 2.17e-05 ***
## PC23
                -0.0849488
                            0.0187708
                                        -4.526 3.11e-05 ***
                                        -3.545 0.000792 ***
## PC24
                -0.0689898
                            0.0194612
## PC25
                -0.0502899
                            0.0202645
                                        -2.482 0.016049 *
## PC26
                 0.0383144
                            0.0218199
                                         1.756 0.084470 .
## PC27
                -0.0311136
                            0.0223988
                                        -1.389 0.170213
                                        -0.039 0.968867
## PC28
                -0.0009223
                            0.0235272
## PC29
                 0.0264901
                            0.0255813
                                         1.036 0.304795
## PC30
                 0.0614879
                            0.0264302
                                         2.326 0.023574 *
## PC31
                -0.0175088
                            0.0273162
                                        -0.641 0.524114
## PC32
                 0.0810688
                            0.0294243
                                         2.755 0.007862 **
## PC33
                 0.1025331
                            0.0304703
                                         3.365 0.001375 **
## PC34
                 0.0260269
                            0.0313318
                                         0.831 0.409616
## PC35
                                        -2.711 0.008856 **
                -0.0906184
                            0.0334301
## PC36
                -0.0145228
                            0.0347981
                                        -0.417 0.677994
## PC37
                -0.0880671
                            0.0362339
                                        -2.431 0.018248 *
## PC38
                 0.0119437
                            0.0384415
                                         0.311 0.757164
## PC39
                 0.1344123
                            0.0405093
                                         3.318 0.001583 **
## PC40
                -0.1368580
                            0.0419042
                                        -3.266 0.001849 **
## PC41
                 0.0879171
                            0.0434060
                                         2.025 0.047511 *
## PC42
                -0.0653448
                            0.0480504
                                        -1.360 0.179210
## PC43
                -0.0498128
                            0.0506436
                                        -0.984 0.329471
## PC44
                 0.0580525
                            0.0535202
                                         1.085 0.282628
## PC45
                 0.1399917
                            0.0555481
                                         2.520 0.014554 *
## PC46
                 0.2074172
                            0.0601952
                                         3.446 0.001076 **
## PC47
                -0.2299176
                            0.0682899
                                        -3.367 0.001367 **
## PC48
                 0.1958510
                            0.0710493
                                         2.757 0.007832 **
## PC49
                 0.1628580 0.0810118
                                         2.010 0.049140 *
```

```
## PC50
              ## PC51
              -0.1847696 0.0933064 -1.980 0.052510 .
              -0.1542097 0.1473139 -1.047 0.299606
## PC52
## PC53
              0.0328753 0.1637758 0.201 0.841622
              ## PC54
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.08455 on 57 degrees of freedom
## Multiple R-squared: 0.9615, Adjusted R-squared: 0.9249
## F-statistic: 26.33 on 54 and 57 DF, p-value: < 2.2e-16
#only the first principal components turned out to be significant
#Next analysis using only first principle component
#Pca 1 is used as it has the most variance
#Obtained pca 1 for your analyses with the following
#Built into a linear regression model using pca1
#pca1=GDPdataTrainSet.pca.normdata$x[,1]
pca1=as.data.frame(GDPdataTrainSet.pca.normdata$x[,1])
pca1.data <- cbind(GDPdata_y_train.set, pca1)</pre>
pca1model <- lm(GDPdata_y_train.set ~ ., data = pca1.data)</pre>
summary(pca1model)
##
## Call:
## lm(formula = GDPdata y train.set ~ ., data = pca1.data)
##
## Residuals:
##
                1Q Median
                                 3Q
       Min
                                         Max
## -0.45033 -0.15992 -0.04544 0.02160 0.75001
##
## Coefficients:
##
                                      Estimate Std. Error t value Pr(>|t|)
                                                0.026323
                                                         5.891 4.26e-08
## (Intercept)
                                      0.155057
                                                0.004905 5.121 1.31e-06
## `GDPdataTrainSet.pca.normdata$x[, 1]` 0.025116
***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.2786 on 110 degrees of freedom
## Multiple R-squared: 0.1925, Adjusted R-squared: 0.1852
## F-statistic: 26.22 on 1 and 110 DF, p-value: 1.306e-06
#-----
```

#Model accuracy assessment

#In multiple linear regression

#The R2 represents the correlation coefficient between the observed values #of the outcome variable (y) and the fitted (i.e., predicted) values of y. #An R2 value close to 1 indicates that the model explains a large portion of the variance in the outcome variable.

#But R2 will always increase when more variables are added to the model #A solution is to adjust the R2 by taking into account the number of predictor variables.

#By comparing multiple regression analysis using actual GDP data, all the principle components and first priciple component

it shows that analysis using all the PCAs shows maximum R2 value (0.9241) than using only first PCA (0.265) and predictor variables (GDP data) (0.9004) #The study shows the first 9 PCAs are enough for the analysis

#Regression analysis using PCA will give a better result

#However PCR is not a feature selection method because each of the calculated principal components

#is a linear combination of the original variables.