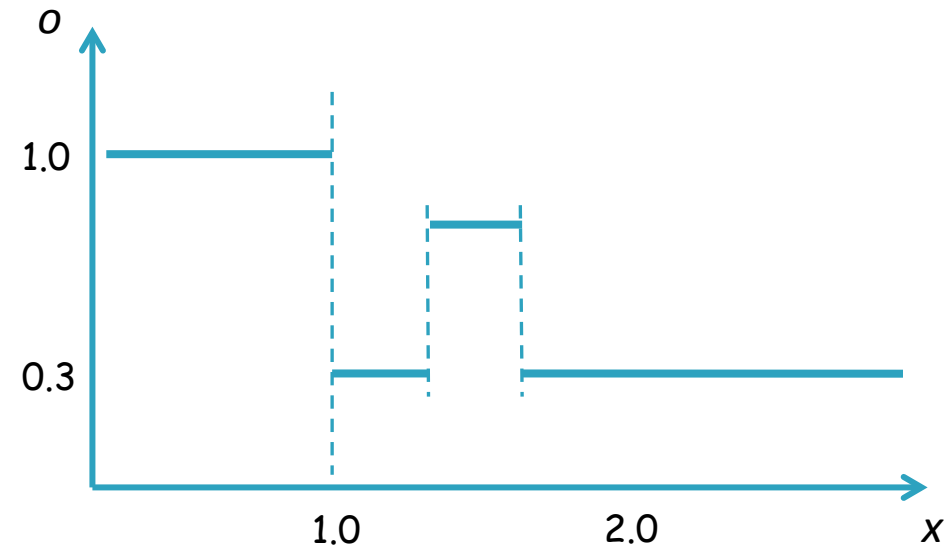


Discrete Factors



```
1  x = sample(1.5);
2  y = (int) x;
3  if (x < 1.0)
4      o = 1 + y;
5  else
6      if (t(x) > 0.3)
7          o = 0.3;
8      else
9          o = 0.75;
```

- ▶ Discrete factors:
 - real value -> discrete value
 - predicate
 - type cast
 - discrete mathematical library functions

Theorem 1: Given two sample executions, if all of their DFs produce the **same** discrete values, they must have the **same** mathematical output function.

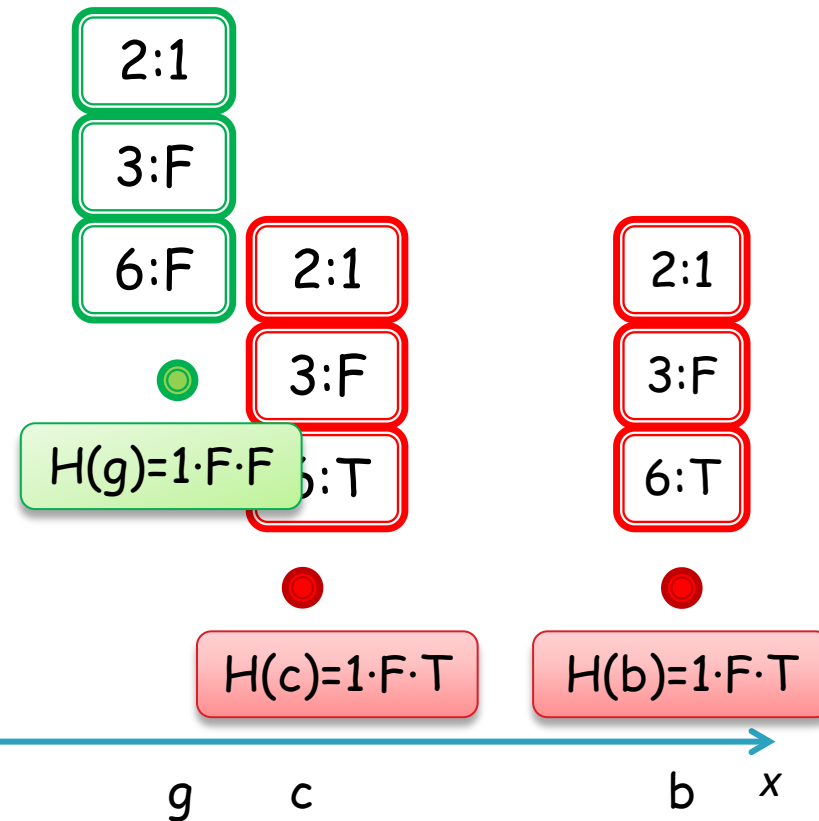
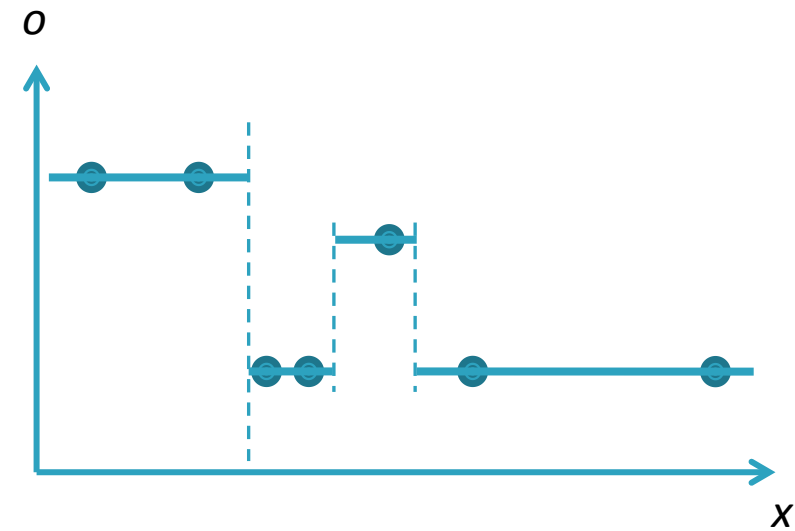
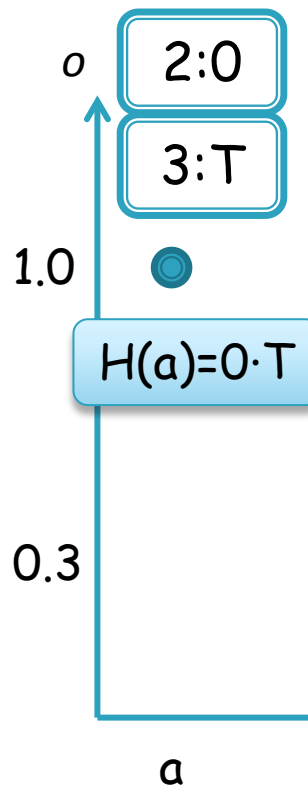
~~Tracing the DFs~~

Hashing

```

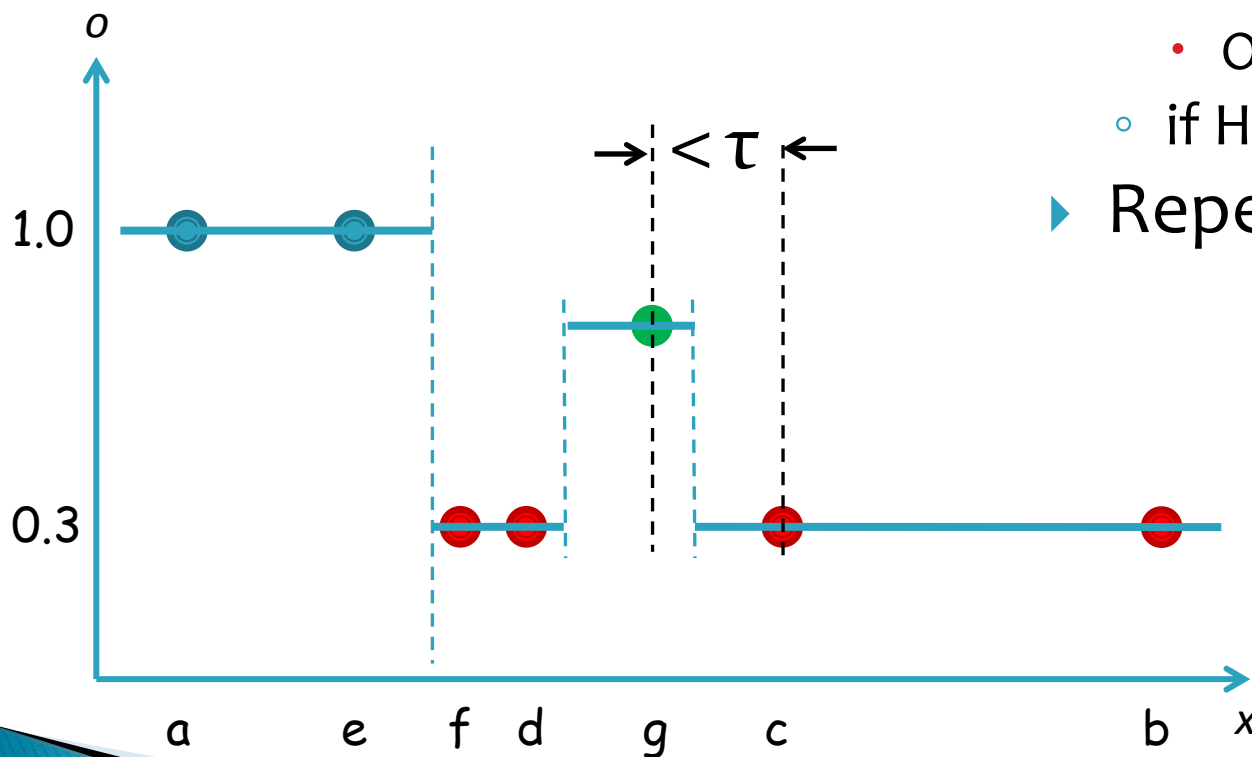
1  x = ...
2  y = (int) x;
3  if (x < 1.0)
4      o = 1 + y;
5  else
6      if (t(x) > 0.3)
7          o = 0.3;
8      else
9          o = 0.75;

```



White-box Sampling Algorithm

- ▶ To sample region $[a, b]$:
 - if $H(a) \neq H(b)$
 - if $|a-b| \geq \tau$, take another sample at $c = (a+b)/2$;
 - Otherwise, stop.
 - if $H(a) = H(b)$, then stop
- ▶ Repeat the process



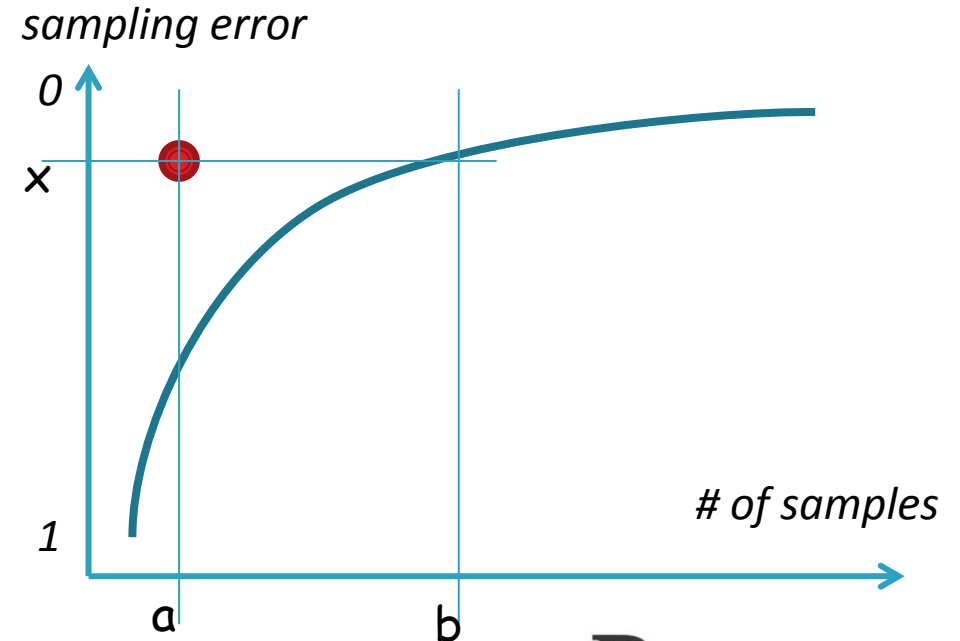
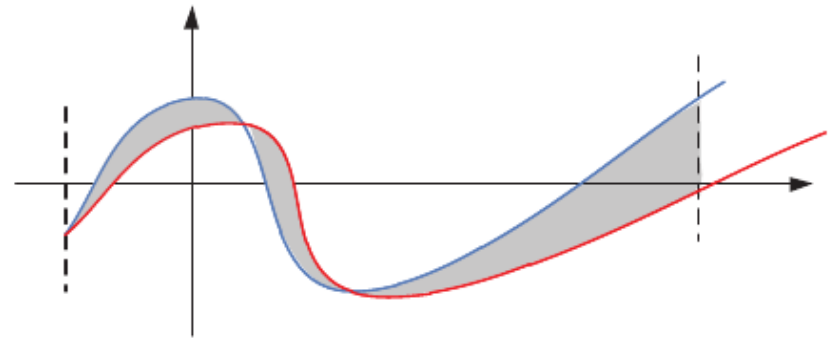
Experiments: Efficiency

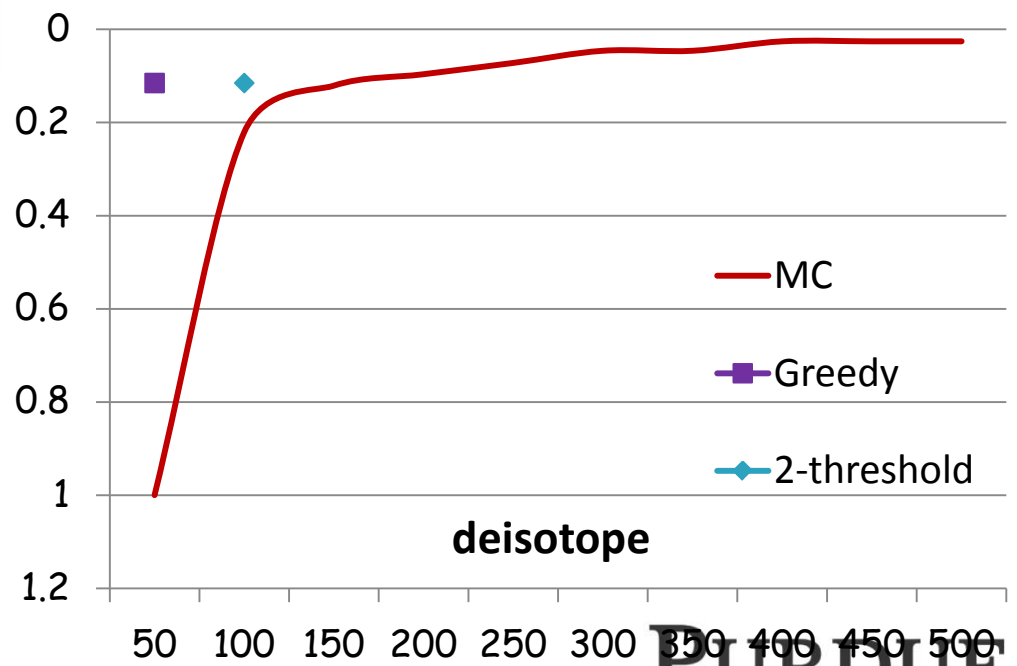
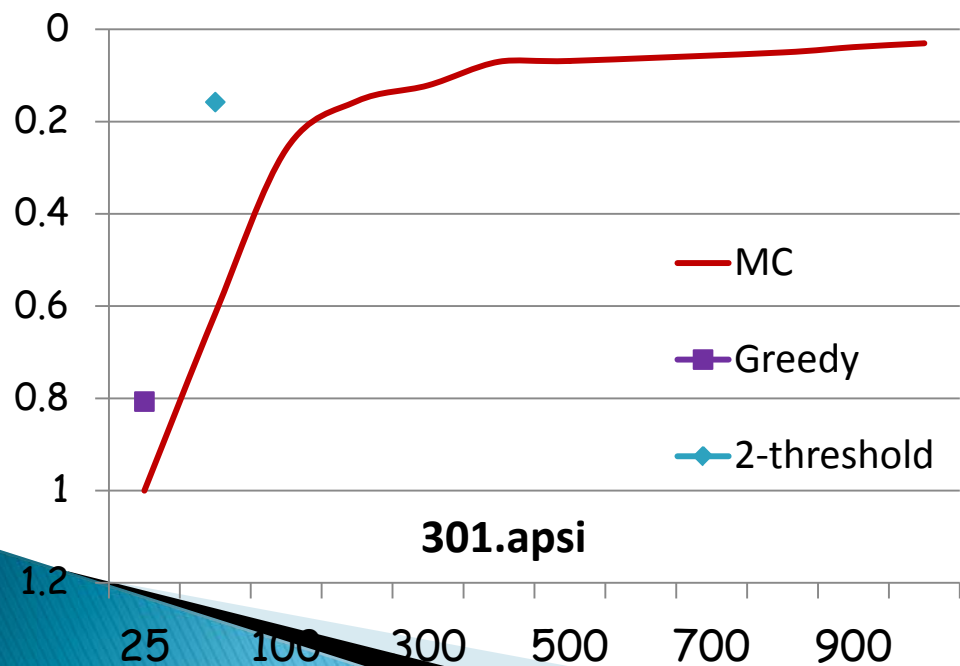
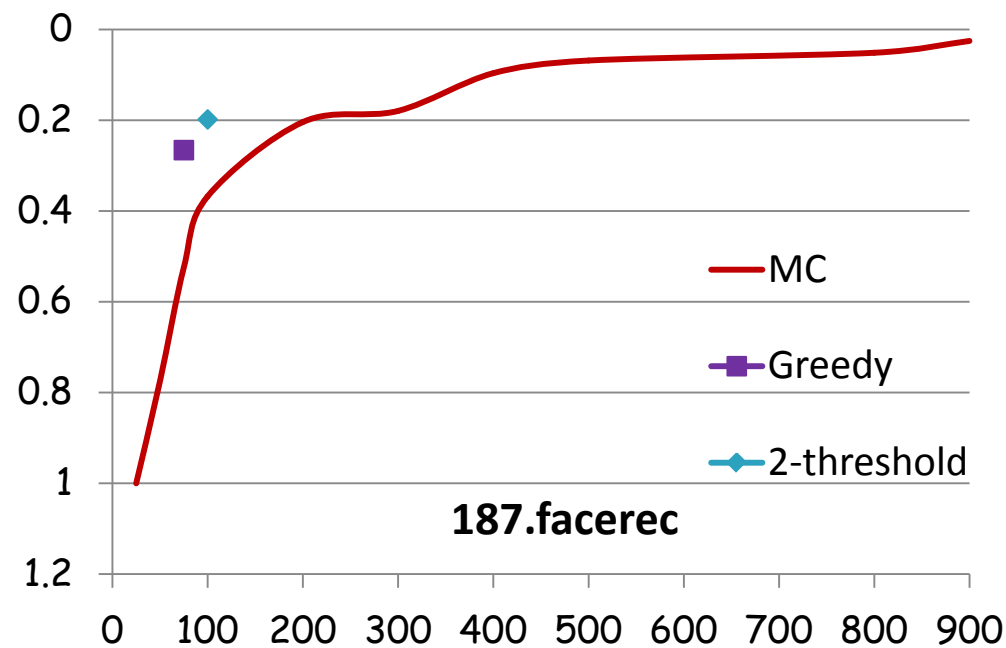
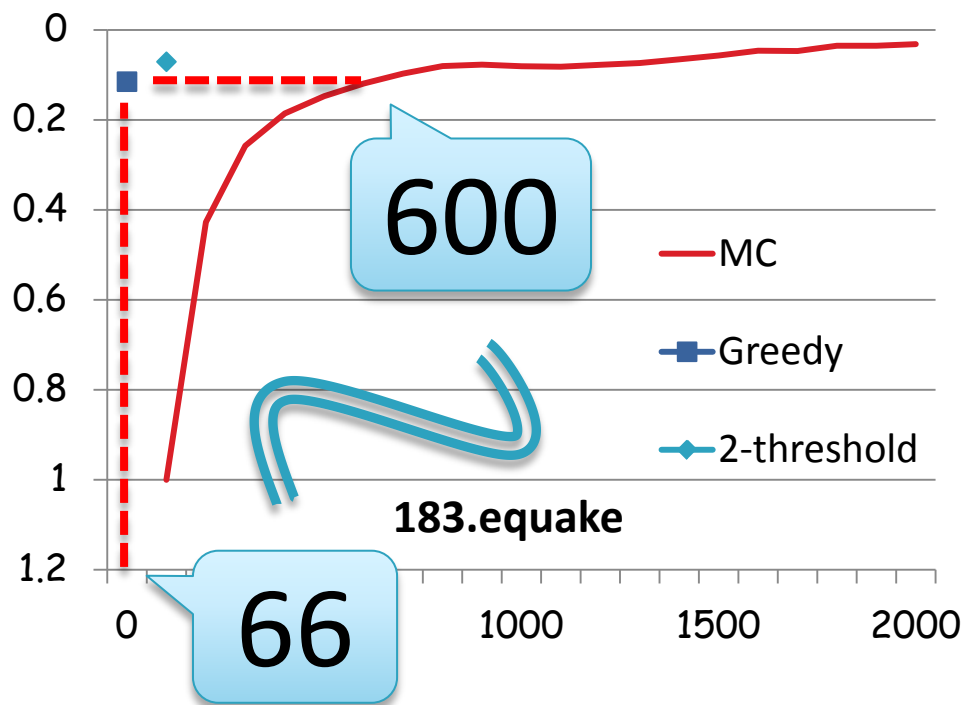
program	native	white-box	overhead	# of samples †
168.wupwise	2.05	2.14	4%	2
171.swim	0.15	0.15	1%	2
172.mgrid	3.31	3.32	0%	2
173.applu	0.06	0.07	6%	2
178.galgel	0.69	0.70	10%	416
183.quake	0.20	0.21	6%	66
187.facerec	1.23	1.25	2%	117
188.amp	2.72	2.73	0%	2
191.fma3d	0.02	0.02	0%	2
200.sixtrack	2.22	2.27	2%	2
301.apsi	1.75	1.77	1%	167
deisotope	0.02	0.02	0%	55
AVERAGE			2.67%	

† Regular MC: 1000 samples

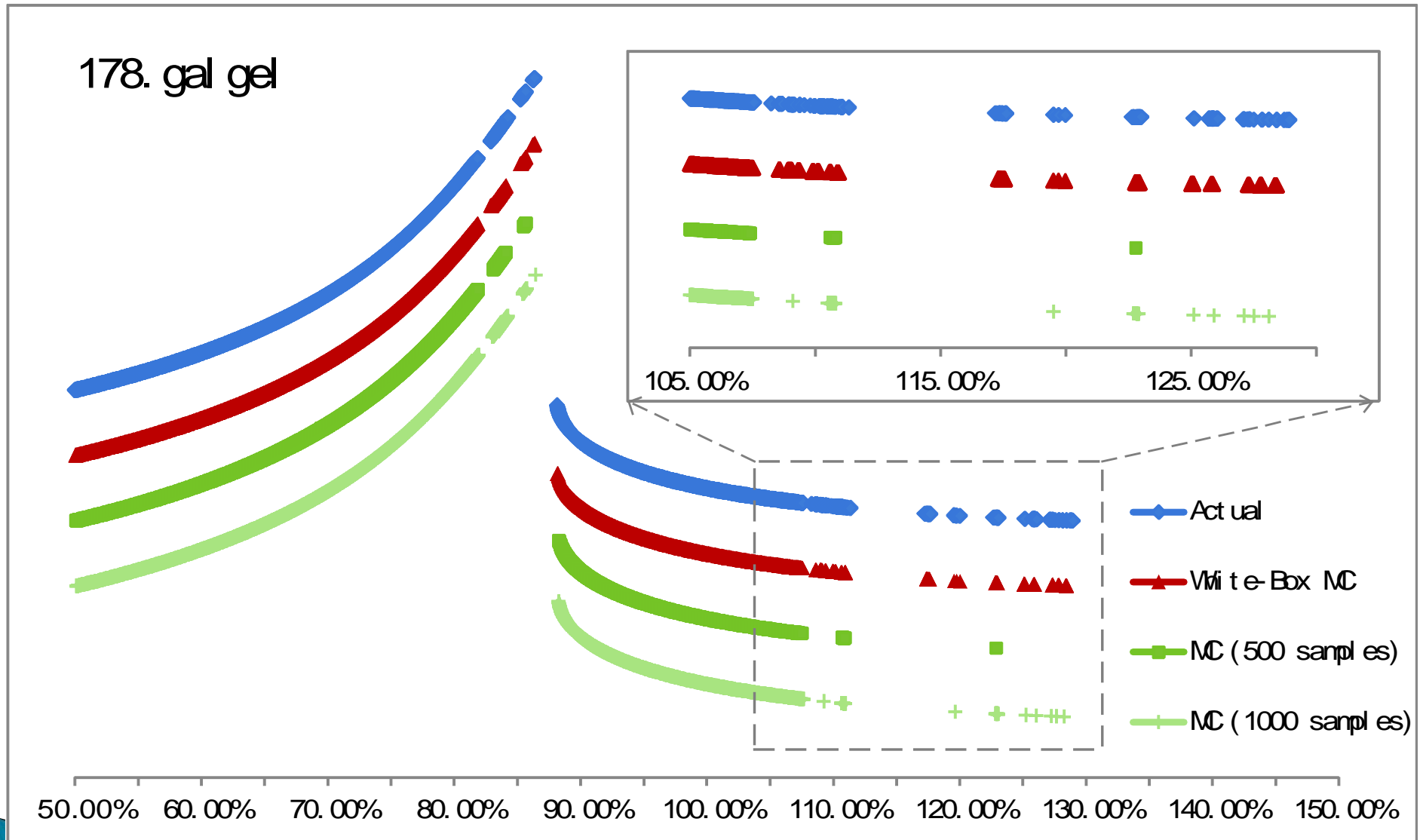
Experiments: Effectiveness

- ▶ Measuring the sampling quality
 - Comparing against the *ideal* curve.
- ▶ Goal
 - To achieve the precision of a high sampling rate with the cost of a low sampling rate.





Case study: 178.gal gel



Outline

- ▶ Overview
- ▶ External Errors
 - White-box Sampling (OOPSLA 2012)
- ▶ Internal Errors
 - On-the-fly detection of instability problems (OOPSLA 2013)

Internal Errors

```
1 float x, z;  
2 x = input();  
3 z = f(x);  
  
4 if (z > 0.5)  
5     printf ("hit");  
6 else  
7     printf ("miss");
```



$X = 100.0;$

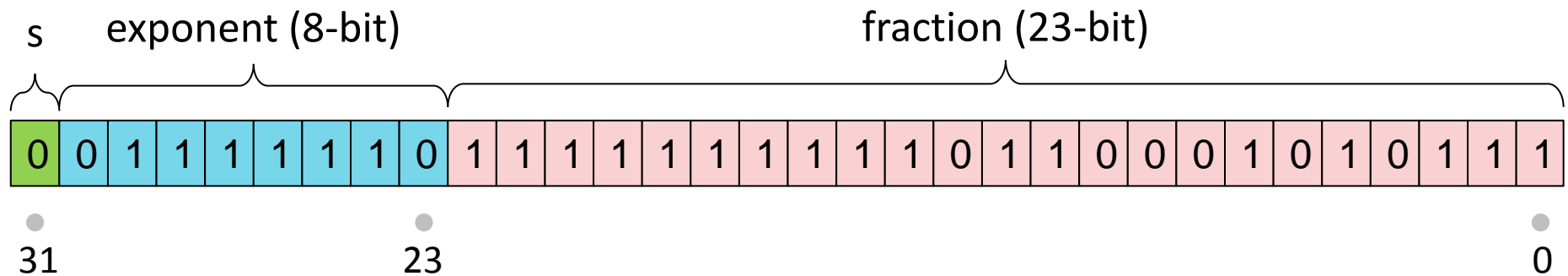
2. Are the computed results reliable?

miss



Floating-Point Representation

▶ IEEE 754-1985



▶ $0.9997_{10} \Rightarrow 0x3F7FEC57$

◦ $0.9997_{10} \approx 1.11111111110110001010111_2 * 2^{-1}$

◦ $0.9997 = 0.999700009822 + (-0.0000000009822)$

ideal

represented