# Assignment #9: 图论: 遍历, 及 树算

Updated 1739 GMT+8 Apr 14, 2024

2024 spring, Complied by 王业成 生命科学学院

#### 说明:

- 1)请把每个题目解题思路(可选),源码Python,或者C++(已经在Codeforces/Openjudge上AC),截图(包含Accepted),填写到下面作业模版中(推荐使用 typora <a href="https://typoraio.cn">https://typoraio.cn</a>,或者用word)。AC或者没有AC,都请标上每个题目大致花费时间。
- 2) 提交时候先提交pdf文件,再把md或者doc文件上传到右侧"作业评论"。Canvas需要有同学清晰头像、提交文件有pdf、"作业评论"区有上传的md或者doc附件。
- 3) 如果不能在截止前提交作业,请写明原因。

#### 编程环境

== (请改为同学的操作系统、编程环境等) ==

操作系统: macOS Ventura 13.4.1 (c)

Python编程环境: Spyder IDE 5.2.2, PyCharm 2023.1.4 (Professional Edition)

C/C++编程环境: Mac terminal vi (version 9.0.1424), g++/gcc (Apple clang version 14.0.3, clang-

1403.0.22.14.1)

## 1. 题目

# 04081: 树的转换

http://cs101.openjudge.cn/dsapre/04081/

思路:自己的代码挑了半天一直不对,最后发现还是思路有问题,应该重点找在上一层而不是根据下一层判断是否-1

存一个左儿子, 存一个右兄弟, 找最大

```
# class TreeNode:
    def __init__(self):
        self.children = []
        self.first_child = None
        self.next_sib = None

def build(seq):
    root = TreeNode()
    stack = [root]
```

```
depth = 0
    for act in seq:
        cur\_node = stack[-1]
        if act == 'd':
            new_node = TreeNode()
            if not cur_node.children:
                cur_node.first_child = new_node
                cur_node.children[-1].next_sib = new_node
            cur_node.children.append(new_node)
            stack.append(new_node)
            depth = max(depth, len(stack) - 1)
        else:
            stack.pop()
    return root, depth
def cal_h_bin(node):
    if not node:
         return -1
    return max(cal_h_bin(node.first_child), cal_h_bin(node.next_sib)) + 1
seq = input()
root, h_orig = build(seq)
h_bin = cal_h_bin(root)
print(f'{h_orig} => {h_bin}')
```

#### 代码运行截图 == (至少包含有"Accepted") ==

#### 状态: Accepted

```
源代码
                                                                                    #: 44742668
                                                                                  题目: 04081
 class TreeNode:
                                                                                提交人: wangyecheng
     def __init__(self):
                                                                                  内存: 3676kB
         self.children = []
        self.first_child = None
                                                                                  时间: 29ms
        self.next_sib = None
                                                                                  语言: Python3
 def build(seq):
                                                                               提交时间: 2024-04-21 17:55:23
    root = TreeNode()
stack = [root]
     depth = 0
     for act in seq:
         cur_node = stack[-1]
if act == 'd':
             new_node = TreeNode()
             if not cur_node.children:
                 cur_node.first_child = new_node
                cur node.children[-1].next sib = new node
             cur_node.children.append(new_node)
             stack.append(new_node)
             depth = max(depth, len(stack) - 1)
         else:
            stack.pop()
     return root, depth
 def cal h bin(node):
    if not node:
     return max(cal_h_bin(node.first_child), cal_h_bin(node.next_sib)) +
 seq = input()
 root, h_orig = build(seq)
 h_bin = cal_h_bin(root)
 print(f' {h_orig} => {h_bin}')
```

## 08581: 扩展二叉树

http://cs101.openjudge.cn/dsapre/08581/

思路: 建树模拟, 感觉用"."填充之后好像跟容易建了

```
# class Treenode():
    def __init__(self,value):
        self.value=value
        self.left=None
        self.right=None
def buildtree(lst):
    if not 1st:
        return None
    value=1st.pop(0)
    if value==".":
        return None
    else:
        node=Treenode(value)
        node.left=buildtree(lst)
        node.right=buildtree(lst)
    return node
def inorder(root):
    if not root:
        return []
    else:
        left=inorder(root.left)
        right=inorder(root.right)
        return left+[root.value]+right
def postorder(root):
    if not root:
        return []
    else:
        left = postorder(root.left)
        right = postorder(root.right)
        return left+right+[root.value]
1st=list(input())
root=buildtree(lst)
a= inorder(root)
b= postorder(root)
print("".join(a))
print("".join(b))
```

```
#: 44/4/442
源代码
                                                                                题目: 08581
 class Treenode():
                                                                              提交人: wangyecheng
    def __init__(self, value):
                                                                                内存: 3664kB
         self.value=value
        self.left=None
                                                                                时间: 26ms
        self.right=None
                                                                                语言: Python3
 def buildtree(lst):
                                                                             提交时间: 2024-04-21 22:13:08
    if not lst:
        return None
     value=lst.pop(0)
     if value==".
        return None
     else:
        node=Treenode (value)
        node.left=buildtree(lst)
        node.right=buildtree(lst)
     return node
 def inorder(root):
     if not root:
        return []
        left=inorder(root.left)
        right=inorder(root.right)
         return left+[root.value]+right
 def postorder(root):
     if not root:
        left = postorder(root.left)
        right = postorder(root.right)
        return left+right+[root.value]
 lst=list(input())
 root=buildtree(lst)
 a= inorder(root)
 b= postorder (root)
```

## 22067: 快速堆猪

print("".join(a))
print("".join(b))

http://cs101.openjudge.cn/practice/22067/

思路:本来想用heap堆的懒删除做的,结果看到题解有一个绝妙的双栈做法,感觉有点类似于并查集的思路把,light栈一直添加最小元素,相当于把他做一个代表,学到了

```
# stack=[]
light=[]
while True:
    try:
        s=input().split()
        if s[0]=="pop":
            if stack:
                stack.pop()
                light.pop()
        elif s[0]=="min":
            if light:
                print(light[-1])
        else:
            value=int(s[1])
            stack.append(value)
            if light:
```

```
light.append(min(light[-1],value))
    else:
        light.append(value)
    except EOFError:
    break
```

```
源代码
 stack=[]
 light=[]
 while True:
     try:
         s=input().split()
         if s[0]=="pop":
             if stack:
                 stack.pop()
                 light.pop()
         elif s[0] == "min":
             if light:
                 print(light[-1])
             value=int(s[1])
             stack.append(value)
             if light:
                 light.append(min(light[-1], value))
                 light.append(value)
     except EOFError:
         break
```

#: 44747732 题目: 22067 提交人: wangyecheng 内存: 6672kB 时间: 313ms 语言: Python3 提交时间: 2024-04-21 22:38:

## 04123: 马走日

dfs, <a href="http://cs101.openjudge.cn/practice/04123">http://cs101.openjudge.cn/practice/04123</a>

思路: dfs回溯

```
# num=0
def dfs(chess,x,y,dirs,step):
    global num
    n=len(chess)
    m=len(chess[0])
    if step==n*m:
        num+=1
        return
    chess[x][y]=1
    for dx, dy in dirs:
        x1, y1=x+dx, y+dy
        if 0 \le x1 \le n and 0 \le y1 \le m and chess[x1][y1]==0:
             dfs(chess,x1,y1,dirs,step+1)
             chess[x1][y1]=0
s=int(input())
dirs=[(1,-2),(1,2),(-1,2),(-1,-2),(2,1),(2,-1),(-2,1),(-2,-1)]
```

```
for _ in range(s):
    num=0
    n,m,x,y=map(int,input().split())
    chess=[[0]*m for _ in range(n)]
    dfs(chess,x,y,dirs,1)
    print(num)
```

状态: Accepted

```
基本信息
源代码
                                                                                        #: 44747984
                                                                                       题目: 04123
num=0
                                                                                     提交人: wangyecheng
 def dfs(chess,x,y,dirs,step):
                                                                                      内存: 3680kB
    global num
                                                                                      时间: 2846ms
    n=len (chess)
     m=len(chess[0])
                                                                                      语言: Python3
    if step==n*m:
                                                                                   提交时间: 2024-04-21 23:11:02
        num+=1
         return
     chess[x][y]=1
     for dx, dy in dirs:
         x1, y1=x+dx, y+dy
         if 0 \le x1 \le n and 0 \le y1 \le m and chess[x1][y1] ==0:
             dfs(chess,x1,y1,dirs,step+1)
             chess[x1][y1]=0
 s=int(input())
\mathtt{dirs} = [\ (1,-2)\ ,\ (1,2)\ ,\ (-1,2)\ ,\ (-1,-2)\ ,\ (2,1)\ ,\ (2,-1)\ ,\ (-2,1)\ ,\ (-2,-1)\ ]
for _ in range(s):
     num=0
     n, m, x, y=map(int,input().split())
     chess=[[0]*m for _ in range(n)]
     dfs(chess,x,y,dirs,1)
     print(num)
```

## 28046: 词梯

bfs, http://cs101.openjudge.cn/practice/28046/

思路:本来想写一个不用图的代码的,但不是超内存就是超时,还是老老实实用题解中图的代码写吧

```
# import sys
from collections import deque
class Graph:
    def __init__(self):
        self.vertices = {}
        self.num_vertices = 0
    def add_vertex(self, key):
        self.num_vertices = self.num_vertices + 1
        new_vertex = Vertex(key)
        self.vertices[key] = new_vertex
        return new_vertex
    def get_vertex(self, n):
        if n in self.vertices:
```

```
return self.vertices[n]
        else:
            return None
    def __len__(self):
        return self.num_vertices
    def __contains__(self, n):
        return n in self.vertices
    def add_edge(self, f, t, cost=0):
        if f not in self.vertices:
            nv = self.add_vertex(f)
        if t not in self.vertices:
            nv = self.add_vertex(t)
        self.vertices[f].add_neighbor(self.vertices[t], cost)
    def get_vertices(self):
        return list(self.vertices.keys())
    def __iter__(self):
        return iter(self.vertices.values())
class Vertex:
    def __init__(self, num):
        self.key = num
        self.connectedTo = {}
        self.color = 'white'
        self.distance = sys.maxsize
        self.previous = None
        self.disc = 0
        self.fin = 0
    def add_neighbor(self, nbr, weight=0):
        self.connectedTo[nbr] = weight
    def get_neighbors(self):
        return self.connectedTo.keys()
def build_graph(all_words):
    buckets = {}
    the_graph = Graph()
    for line in all_words:
        word = line.strip()
        for i, _ in enumerate(word):
            bucket = f"{word[:i]}_{word[i + 1:]}"
            buckets.setdefault(bucket, set()).add(word)
    for similar_words in buckets.values():
        for word1 in similar_words:
            for word2 in similar_words - {word1}:
                the_graph.add_edge(word1, word2)
    return the_graph
def bfs(start, end):
    start.distnce = 0
    start.previous = None
    vert_queue = deque()
    vert_queue.append(start)
    while len(vert_queue) > 0:
        current = vert_queue.popleft()
        if current == end:
            return True
        for neighbor in current.get_neighbors():
            if neighbor.color == "white":
                neighbor.color = "gray"
                neighbor.distance = current.distance + 1
```

```
neighbor.previous = current
                vert_queue.append(neighbor)
        current.color = "black"
    return False
def traverse(starting_vertex):
    ans = []
    current = starting_vertex
    while (current.previous):
        ans.append(current.key)
        current = current.previous
    ans.append(current.key)
    return ans
n = int(input())
all_words = []
for _ in range(n):
    all_words.append(input().strip())
g = build_graph(all_words)
s, e = input().split()
start, end = g.get_vertex(s), g.get_vertex(e)
if start is None or end is None:
    print('NO')
    exit(0)
if bfs(start, end):
    ans = traverse(end)
    print(' '.join(ans[::-1]))
else:
    print('NO')
```

#### 状态: Accepted

```
源代码
 import sys
 from collections import deque
 class Graph:
     def __init__(self):
         self.num_vertices = 0
     def add_vertex(self, key):
        self.num_vertices = self.num_vertices + 1
         new_vertex = Vertex(key)
self.vertices[key] = new_vertex
         return new vertex
     def get_vertex(self, n):
         if n in self.vertices:
            return self.vertices[n]
             return None
           _len__(self):
         return self.num vertices
     def __contains__(self, n):
         return n in self.vertices
     def add_edge(self, f, t, cost=0):
         if f not in self.vertices:
            nv = self.add_vertex(f)
         if t not in self.vertices:
             nv = self.add_vertex(t)
         self.vertices[f].add_neighbor(self.vertices[t], cost)
     def get_vertices(self):
        return list(self.vertices.keys())
     def iter (self):
        return iter(self.vertices.values())
 class Vertex:
     def __init__(self, num):
         self.key = num
```

基本信息

#: 44750192 题目: 28046 提交人: wangyecheng 内存: 9508kB 时间: 82ms 语言: Python3 提交时间: 2024-04-22 11:43:06

### 28050: 骑士周游

dfs, <a href="http://cs101.openjudge.cn/practice/28050/">http://cs101.openjudge.cn/practice/28050/</a>

思路:

```
# import sys
class Graph:
    def __init__(self):
        self.vertices = {}
        self.num_vertices = 0
    def add_vertex(self, key):
        self.num_vertices = self.num_vertices + 1
        new_vertex = Vertex(key)
        self.vertices[key] = new_vertex
        return new_vertex
    def get_vertex(self, n):
        if n in self.vertices:
            return self.vertices[n]
        else:
            return None
    def __len__(self):
        return self.num_vertices
    def __contains__(self, n):
        return n in self.vertices
    def add_edge(self, f, t, cost=0):
        if f not in self.vertices:
            nv = self.add_vertex(f)
        if t not in self.vertices:
            nv = self.add_vertex(t)
        self.vertices[f].add_neighbor(self.vertices[t], cost)
    def getVertices(self):
        return list(self.vertices.keys())
    def __iter__(self):
        return iter(self.vertices.values())
class Vertex:
    def __init__(self, num):
        self.key = num
        self.connectedTo = {}
        self.color = 'white'
        self.distance = sys.maxsize
        self.previous = None
        self.disc = 0
        self.fin = 0
    def __lt__(self,o):
        return self.key < o.key</pre>
    def add_neighbor(self, nbr, weight=0):
        self.connectedTo[nbr] = weight
    def get_neighbors(self):
```

```
return self.connectedTo.keys()
    def __str__(self):
        return str(self.key) + ":color " + self.color + ":disc " + str(self.disc)
+ ":fin " + str(
            self.fin) + ":dist " + str(self.distance) + ":pred \n\t[" +
str(self.previous) + "]\n"
def knight_graph(board_size):
    kt_graph = Graph()
    for row in range(board_size):
        for col in range(board_size):
            node_id = pos_to_node_id(row, col, board_size)
            new_positions = gen_legal_moves(row, col, board_size)
            for row2, col2 in new_positions:
                other_node_id = pos_to_node_id(row2, col2, board_size)
                kt_graph.add_edge(node_id, other_node_id)
    return kt_graph
def pos_to_node_id(x, y, bdSize):
    return x * bdSize + y
def gen_legal_moves(row, col, board_size):
    new_moves = []
    move_offsets = [
        (-1, -2),
        (-1, 2),
        (-2, -1),
        (-2, 1),
        (1, -2),
        (1, 2),
        (2, -1),
        (2, 1),
    for r_off, c_off in move_offsets:
                                             # #检查,不能走出棋盘
            0 <= row + r_off < board_size</pre>
            and 0 <= col + c_off < board_size
        ):
            new_moves.append((row + r_off, col + c_off))
    return new_moves
def knight_tour(n, path, u, limit):
    u.color = "gray"
    path.append(u)
    if n < limit:</pre>
        neighbors = ordered_by_avail(u)
        i = 0
        for nbr in neighbors:
            if nbr.color == "white" and \
                knight_tour(n + 1, path, nbr, limit):
                return True
        else:
            path.pop()
            u.color = "white"
            return False
    else:
        return True
def ordered_by_avail(n):
    res_list = []
    for v in n.get_neighbors():
```

```
if v.color == "white":
           c = 0
            for w in v.get_neighbors():
               if w.color == "white":
                    c += 1
            res_list.append((c,v))
    res_list.sort(key = lambda x: x[0])
    return [y[1] for y in res_list]
def NodeToPos(id):
    return ((id//8, id%8))
bdSize = int(input()) # 棋盘大小
*start_pos, = map(int, input().split()) # 起始位置
g = knight_graph(bdSize)
start_vertex = g.get_vertex(pos_to_node_id(start_pos[0], start_pos[1], bdSize))
if start_vertex is None:
   print("fail")
   exit(0)
tour_path = []
done = knight_tour(0, tour_path, start_vertex, bdSize * bdSize-1)
   print("success")
else:
   print("fail")
exit(0)
cnt = 0
for vertex in tour_path:
   cnt += 1
   if cnt % bdSize == 0:
       print()
   else:
       print(vertex.key, end=" ")
```

状态: Accepted

```
源代码
 class Graph:
     def __init__(self):
         self.vertices = {}
         self.num vertices = 0
     def add_vertex(self, key):
         self.num_vertices = self.num_vertices + 1
         new vertex = Vertex(key)
         self.vertices[key] = new_vertex
         return new vertex
     def get_vertex(self, n):
         if n in self.vertices:
             return self.vertices[n]
             return None
     def __len__(self):
         return self.num vertices
          contains (self, n):
         return n in self.vertices
     def add edge(self, f, t, cost=0):
         if f not in self.vertices:
            nv = self.add vertex(f)
         if t not in self.vertices:
             nv = self.add_vertex(t)
         self.vertices[f].add_neighbor(self.vertices[t], cost)
     def getVertices(self):
         return list(self.vertices.keys())
     def __iter__(self):
         return iter(self.vertices.values())
 class Vertex:
     def __init__(self, num):
         \overline{\text{self.key}} = \text{num}
```

基本信息

#: 44750285 题目: 28050 提交人: wangyecheng 内存: 4060kB 时间: 31ms 语言: Python3

提交时间: 2024-04-22 11:57:24

# 2. 学习总结和收获

==如果作业题目简单,有否额外练习题目,比如: OJ"2024spring每日选做"、CF、LeetCode、洛谷等网站题目。==

本周作业好难啊,由于之前的dfs和bfs基础比较薄弱,还专门花了一天时间来学习二者,结果发现题目还是不怎么会,好多题目基本都是看着题解一步一步理解,再一步一步写的,最后一题骑士周游还是直接粘了题解的代码慢慢理解的,感觉图的内容还是不够熟练,建图老是少写函数,实在不行机考的时候再cheeting-sheet上抄一份完整地图代码把,sigh!